INTRODUCTION TO ARTIFICIAL INTELLIGENCE LECTURE 2: UNINFORMED SEARCH

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PROBLEM SOLVING

Problem solving is an essential part of intelligence.

Wolf, goat and cabbage problem

Once upon a time a farmer went to a market and purchased a wolf, a goat, and a cabbage. On his way home, the farmer came to the bank of a river and rented a boat. But crossing the river by boat, the farmer could carry only himself and a single one of his purchases: the wolf, the goat, or the cabbage. If left unattended together, the wolf would eat the goat, or the goat would eat the cabbage.

The farmer's challenge was to carry himself and his purchases to the far bank of the river, leaving each purchase intact. How did he do it?



SEARCH PROBLEMS FORMALLY

Formally, a **search problem** has 5 components:

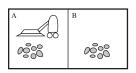
- ► s₀: Initial state
- ► ACTIONS(s): Returns the set of actions **applicable** in state s. (E.g. the action of opening a door might only be applicable if the door is unlocked.)
- ▶ RESULTS(s, a): Returns the state s' reached from s by executing action a.
- ▶ GOAL-TEST(s): Returns true if s is goal state, otherwise false.
- ▶ STEP-Cost(s, a): The cost of executing action a in s. Most often we will assume STEP-Cost(s, a) = 1 for all s and a.

A state g is called a **goal state** if GOAL-TEST(g) = true.

A **solution** to a search problem is a **sequence of actions** (a **path**) from s_0 to a goal state. It is **optimal** if it has minimum sum of step costs.

A TOY PROBLEM: VACUUM WORLD

Vacuum World consists of two locations, each of which may or may not contain dirt and the vacuum is in one of the locations.



A TOY PROBLEM: VACUUM WORLD

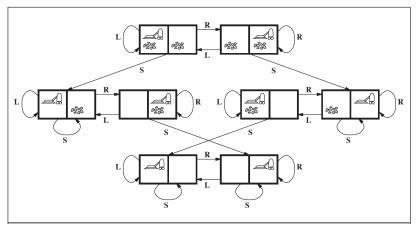
States space consists of each possible configuration (2 \times 2² possible states).

- ► s₀: Initial state
- ► ACTIONS(s): for each state three possible actions: L, R, S.
- ightharpoonup RESULTS(s, a): actions have their expected results.
- ► GOAL-TEST(s): are all squares clean?
- ▶ STEP-Cost(s, a): each step costs 1.

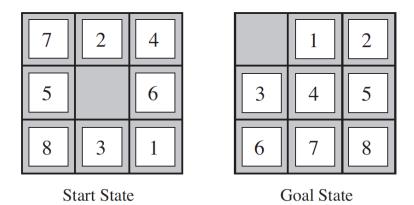
A TOY PROBLEM: VACUUM WORLD

Transition Model

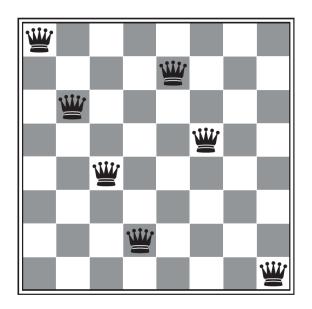
The transitions in the Vacuum World can be represented as a graph.



ANOTHER TOY PROBLEM: 8-PUZZLE



YET ANOTHER TOY PROBLEM: 8-QUEENS



LEVELS OF ABSTRACTION

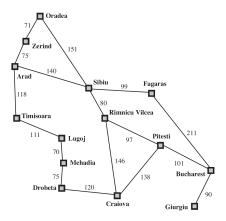


LEVELS OF ABSTRACTION



A REAL WORLD PROBLEM

ROUTE-FINDING



A REAL WORLD PROBLEM

States include a location and the current time, etc.

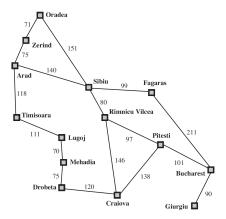
- $ightharpoonup s_0$: specified by the user's query.
- ightharpoonup ACTIONS(s): take any flight from the current location, in any class, etc.
- ► RESULTS(s, a): the state resulting from taking a flight.

 flight destination as current location and flight arrival time as current time.
- ► GOAL-TEST(s): Are we at the final destination specified by the user?
- ► STEP-Cost(s, a): monetary cost, waiting time, flight time, customs and immigration procedures, seat quality, time of day, type of airplane, frequent-flyer mileage awards, etc.

Another Real World Problem

Touring Problem

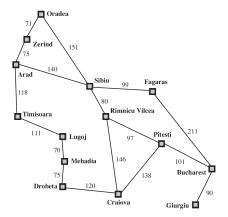
Visit every city in the figure at least once, starting and ending in Bucharest.

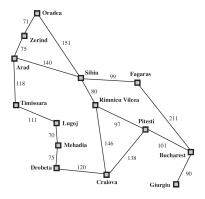


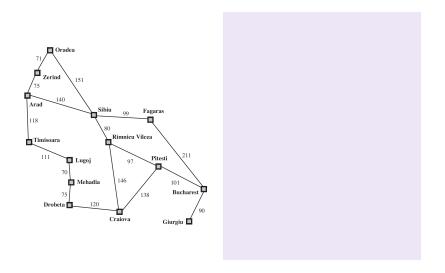
YET ANOTHER REAL WORLD PROBLEM

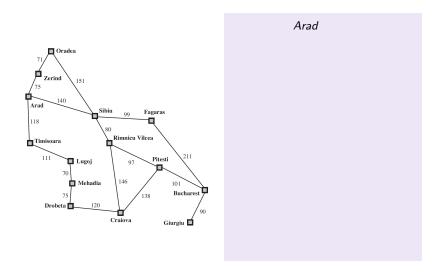
TRAVELLING SALESPERSON PROBLEM

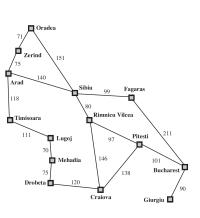
Find a travel plan that allows visiting every city **exactly once**.

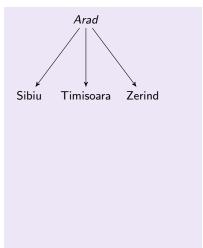


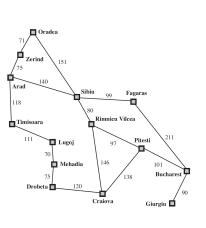


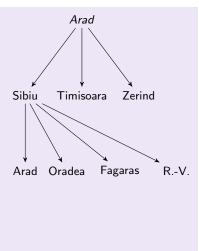


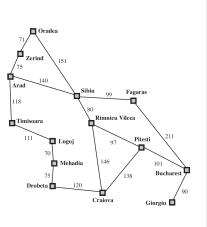


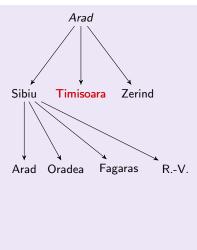


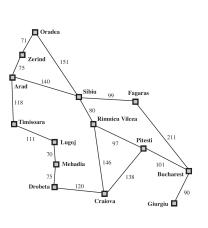


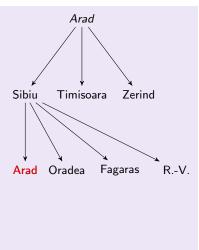


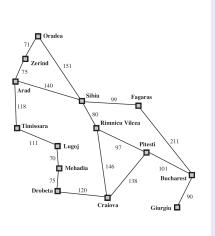


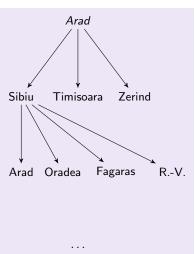












EXPANDED NODES & FRONTIER

In tree and graph search, we always generate **all** children of a chosen state s: We compute Result(s, a) for **all** applicable actions a. We call this process **expanding** s.

In tree search states are called **nodes**: In tree search we don't keep track of repeated states, and hence distinct tree nodes might represent the same state.

The search has two types of nodes:

- **Expanded nodes**: Nodes for which all children have been generated.
- ► Frontier: Nodes that we generated, but not expanded.

THE TREE-SEARCH ALGORITHM

```
function Tree-Search (problem) returns a solution, or failure frontier := \{s_0\} (initial state) // we initialise the frontier loop do

if frontier = \emptyset then return failure

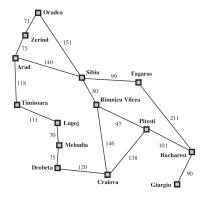
choose a node n from frontier

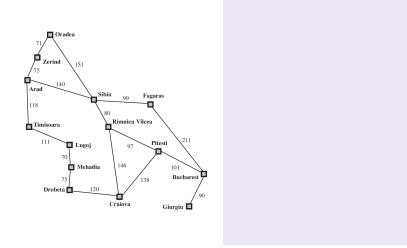
remove n from frontier

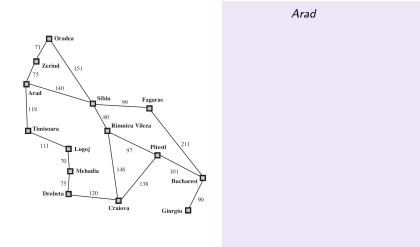
if n is a goal state then return solution

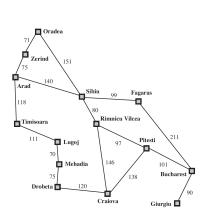
for each child m of n // we expand n

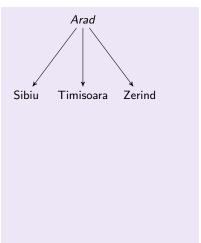
add child m to frontier
```

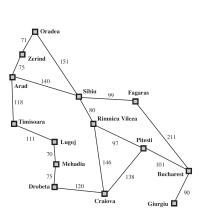


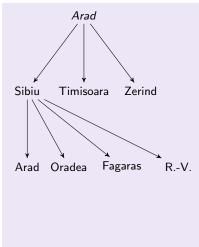


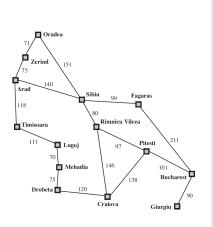


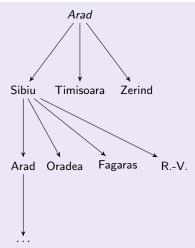


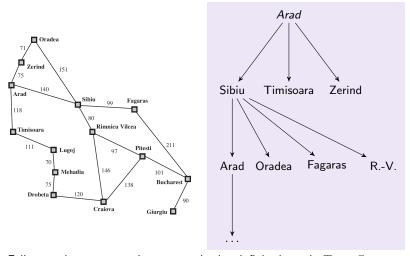












Failure to detect repeated states can lead to infinite loops in TREE-SEARCH.

Solution: Keep track of already generated states.

Adding this check to TREE-SEARCH gives us GRAPH-SEARCH.

THE GRAPH-SEARCH ALGORITHM

The red lines are those added to the ${\it Tree-Search}$ algorithm.

Solving search problems

Solutions to search problems split into:

- ► Tree search
- ► Graph search

The only difference is: graph search keeps track of repeated states.

Along a different dimension they split into:

- ▶ Uninformed search: No sense of closeness to the goal.
- ▶ Informed search: Heuristics used to give a sense of closeness to the goal (e.g. straight-line distance to goal in case of route finding on a map).

For now, we only consider uninformed search.

Along yet another dimension:

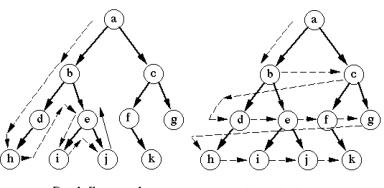
- **Breadth-based search**: Exploring shallow nodes first (close to s_0).
- ▶ **Depth-based search**: Exploring as deeply as possible, sacrificing breadth (might miss the goal).

Tree search: DFS vs BFS

DFS: Depth-first search.

BFS: Breadth-first search.

Order of node expansion:



Depth-first search

Breadth-first search

SEARCH STRATEGIES OF TREE-SEARCH AND GRAPH-SEARCH

Different search strategies can be achieved by simply changing how choose node from frontier and add child to frontier work.

Breadth-first search (BFS):

- ► Frontier is queue (FIFO).
- choose node from frontier: dequeue node from frontier.
- ▶ add child to frontier: enqueue node to frontier.

Depth-first search (DFS):

- ► Frontier is stack (LIFO).
- choose node from frontier: pop node from frontier.
- ▶ add child to frontier: push node to frontier.

Which search algorithm would you rather choose: BFS or DFS?

Go to www.menti.com and use the code 72 26 24

We can measure problem-solving performance by:

► Completeness Is the algorithm guaranteed to find a solution if one exists?

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 Optimal solution has the lowest path cost among solutions.
- ► Time complexity How long does it take to find a solution?
- ▶ Space complexity How much memory is needed to perform the search?

FOR TREE-SEARCH

Criterion	Breadth- First	Uniform- Cost	Depth- First	Depth- Limited	Iterative Deepening	Bidirectional
Complete?	Yesa	$Yes^{a,b}$	No	No	Yesa	$\mathrm{Yes}^{a,d}$
Time	$O(b^d)$	$O(b^{1+\lfloor C^*/\epsilon \rfloor})$	$O(b^m)$	$O(b^\ell)$	$O(b^d)$	$O(b^{d/2})$
Space	$O(b^d)$	$O(b^{1+\lfloor C^*/\epsilon\rfloor})$	O(bm)	$O(b\ell)$	O(bd)	$O(b^{d/2})$
Optimal?	Yes^c	Yes	No	No	Yes^c	$\mathrm{Yes}^{c,d}$

Figure 3.21 Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; l is the depth limit. Superscript caveats are as follows: a complete if b is finite; b complete if step costs b for positive b optimal if step costs are all identical; b if both directions use breadth-first search.

THE END OF LECTURE 2