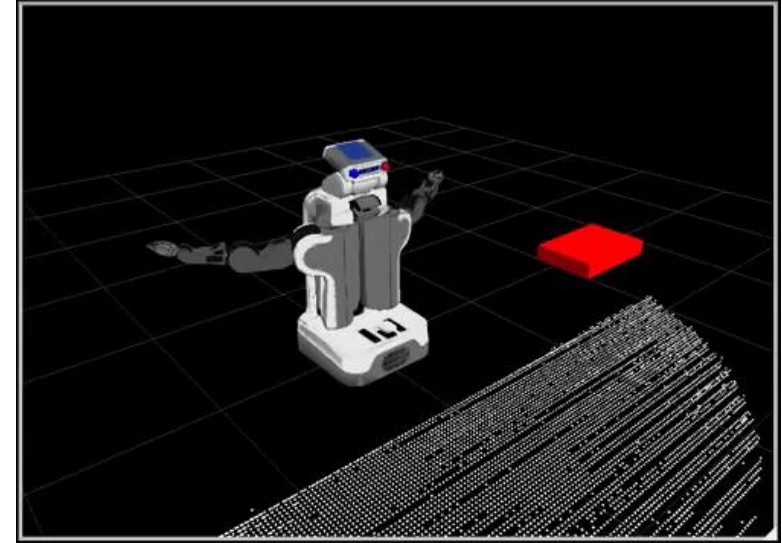


Robot Planning

Ok now we're more realistic...

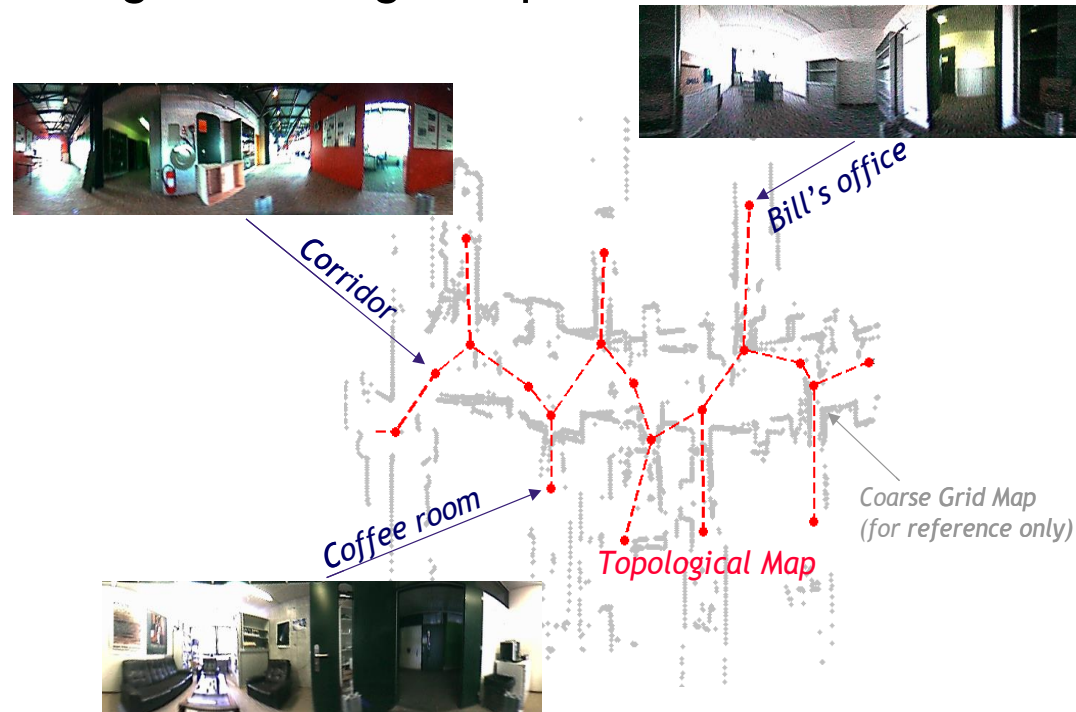
... however, still autonomous robots are more complex than this

- The robots have to autonomously find their way through..
 - Robotic Manipulators need:
 - To solve the inverse kinematics and dynamics problems
 - Find the correct trajectories to avoid obstacles
 - ...
 - Mobile Robots need to use path planning to navigate the environment



The Planning Problem (case of Mobile Robots 1/2)

- The problem: **find a path in the work space** (physical space) from the initial position to the goal position avoiding all collisions with the obstacles
- Assumption: there exists a good enough map of the environment for navigation.
 - Topological
 - Metric
 - Hybrid methods



The Planning Problem (case of Mobile Robots 2/2)

- We can generally distinguish between
 - (global) path planning and
 - (local) obstacle avoidance.
- First step:
 - Transformation of the map into a representation useful for planning
 - This step is planner-dependent
- Second step:
 - Plan a path on the transformed map
- Third step:
 - Send motion commands to controller
 - This step is planner-dependent (e.g. Model based feed forward, path following)

Planning Algorithms: Potential Fields

Goal: Attractive Force

Large Distance --> Large Force

Model as Spring

Hooke's Law

$$F = -k X$$



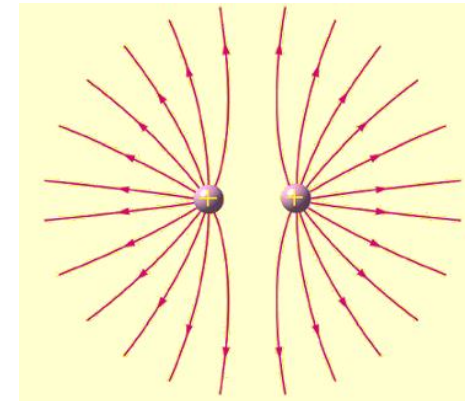
Obstacles: Repulsive Force

Small Distance --> Large Force

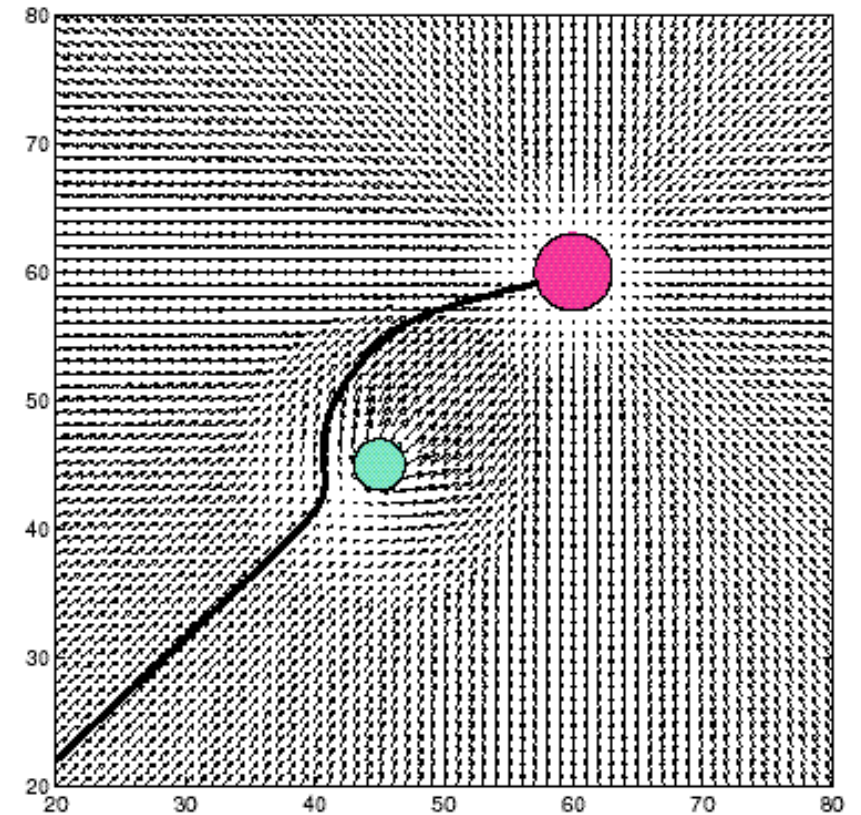
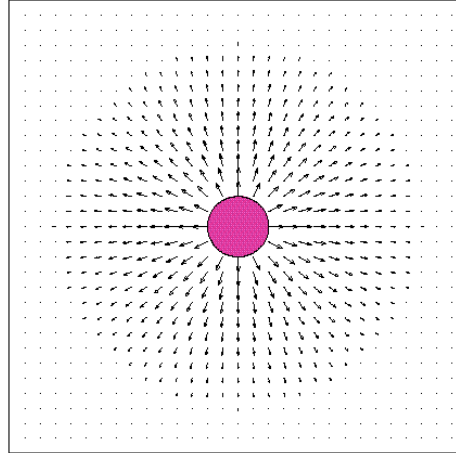
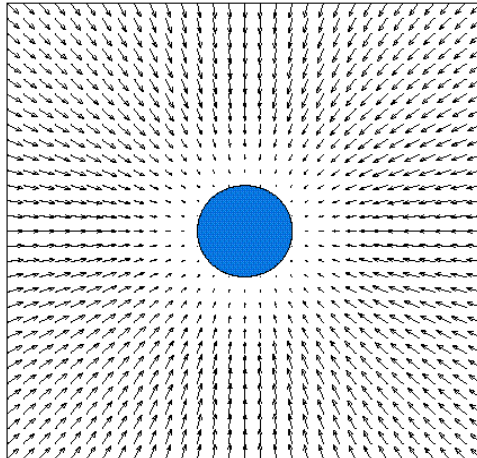
Model as Electrically Charged Particles

Coulomb's law

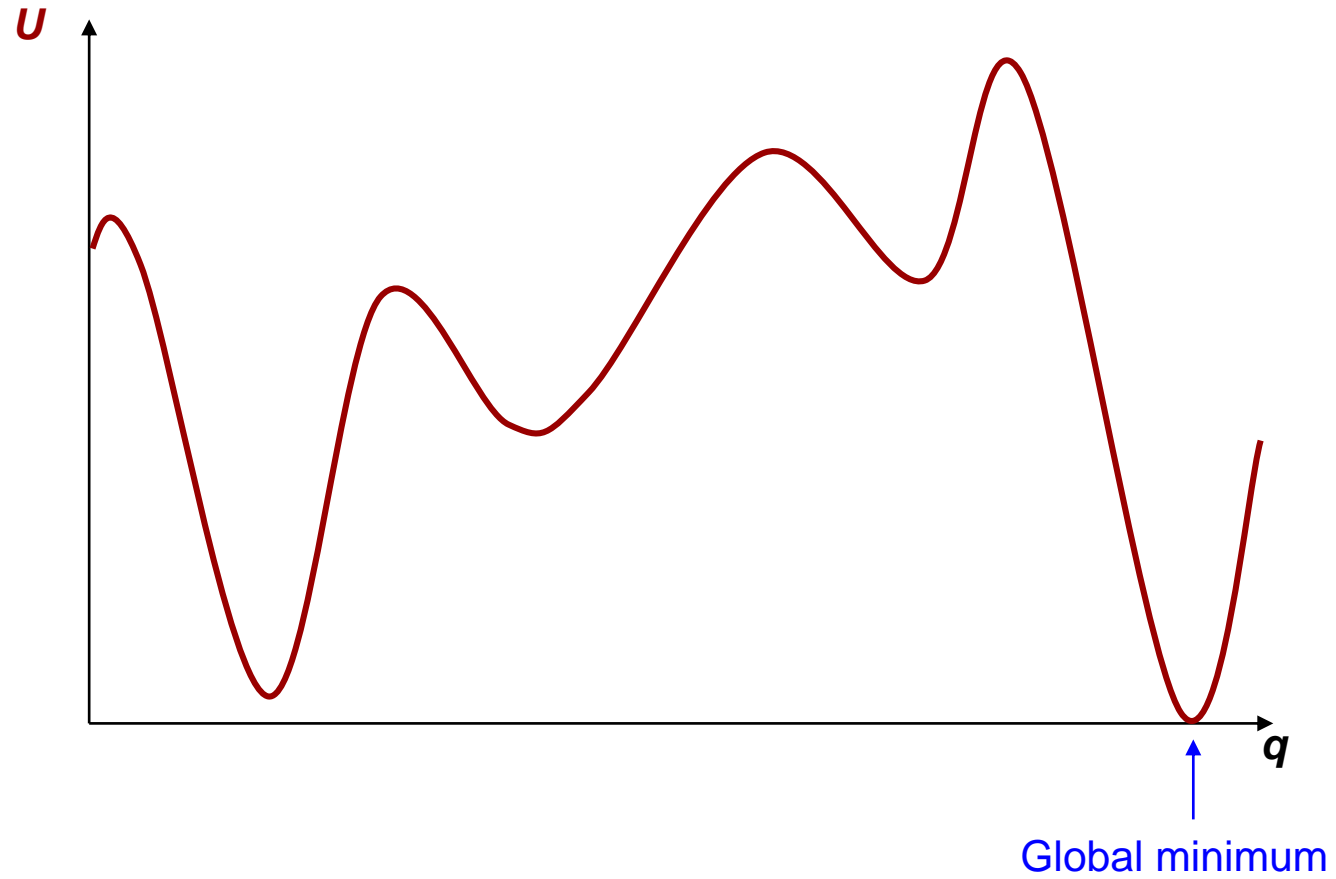
$$F = k q_1 q_2 / r^2$$



Planning Algorithms: Potential Fields



Bad Potential Field



Sampling-based Path Planning (or Randomized graph search)

- When the state space is large complete solutions are often infeasible.
- In practice, most algorithms are only resolution complete, i.e., only complete if the resolution is fine-grained enough
- Sampling-based planners create possible paths by randomly adding points to a tree until some solution is found

RRT

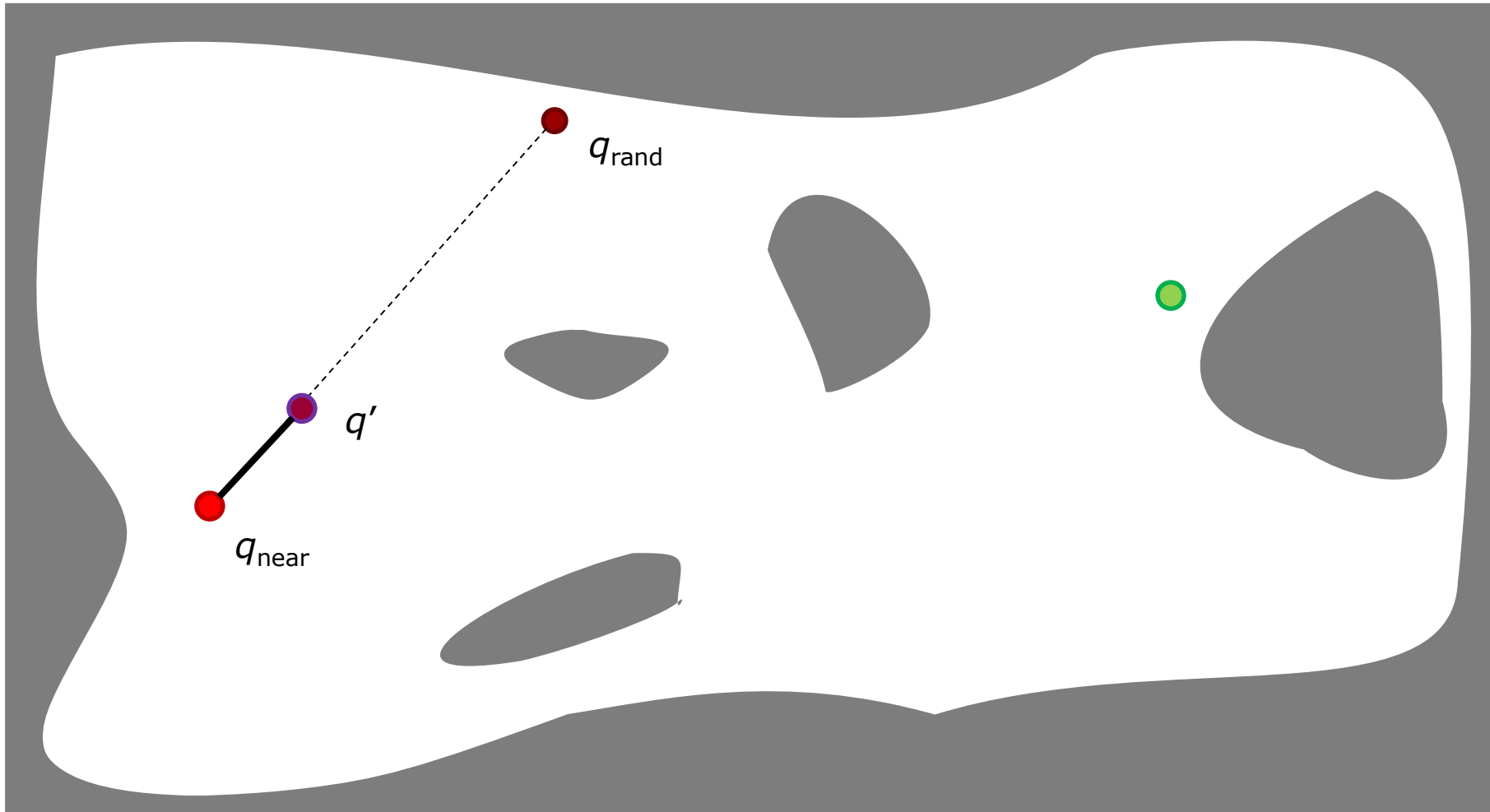
- RRT is a good example of a Sampling-based algorithm:

```
RRT( $q_0$ )
1   $\mathcal{G}.\text{init}(q_0)$ ;
2  for  $i = 1$  to  $k$  do
3       $q_n \leftarrow \text{NEAREST}(S, \alpha(i))$ ;
4       $q_s \leftarrow \text{STOPPING-CONFIGURATION}(q_n, \alpha(i))$ ;
5      if  $q_s \neq q_n$  then
6           $\mathcal{G}.\text{add\_vertex}(q_s)$ ;
7           $\mathcal{G}.\text{add\_edge}(q_n, q_s)$ 
```

- Several additional algorithms are worth exploring
 - RRT*
 - Informed RRT
 - ...

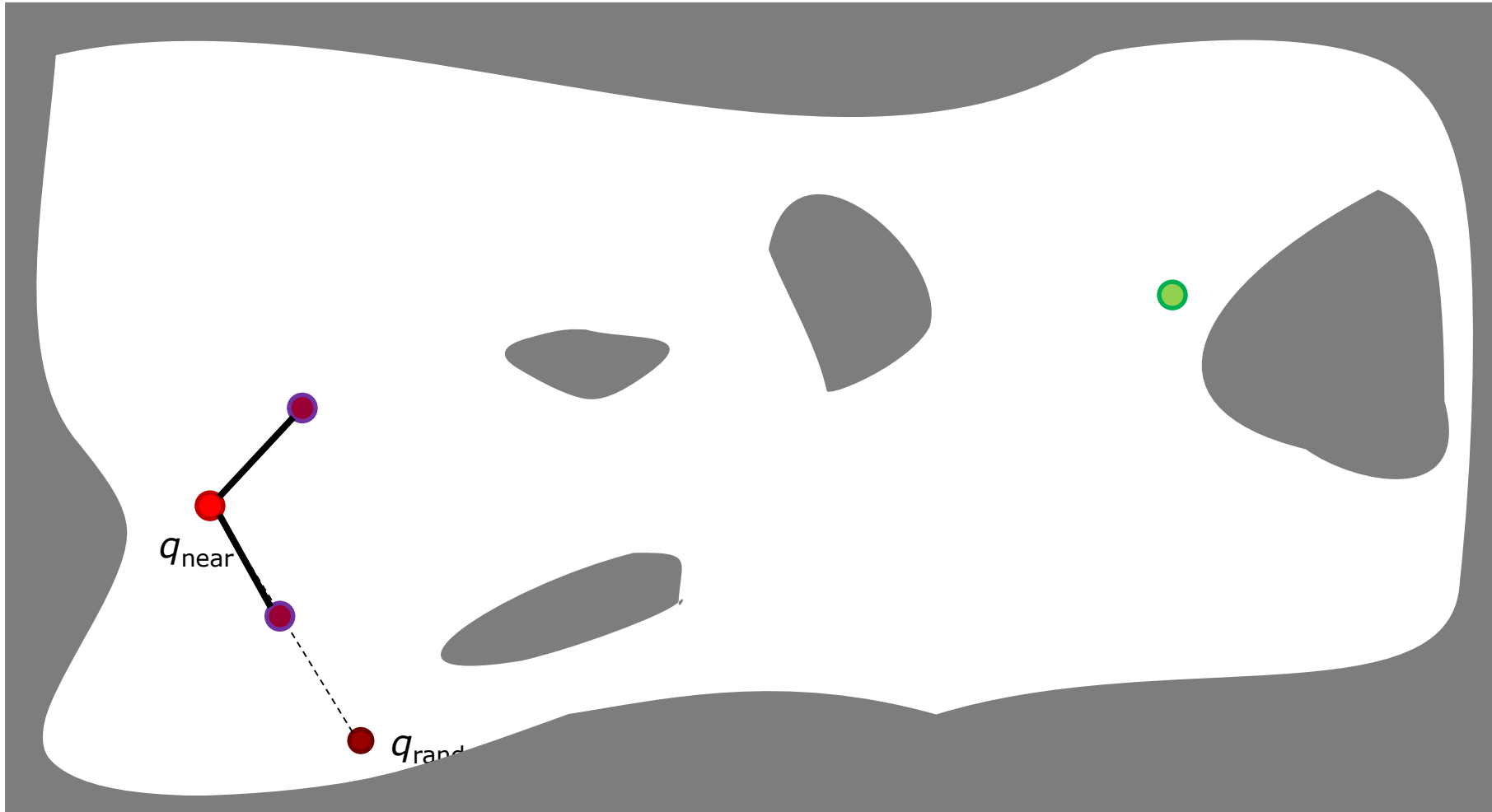
RRT

- Rapidly-exploring random trees



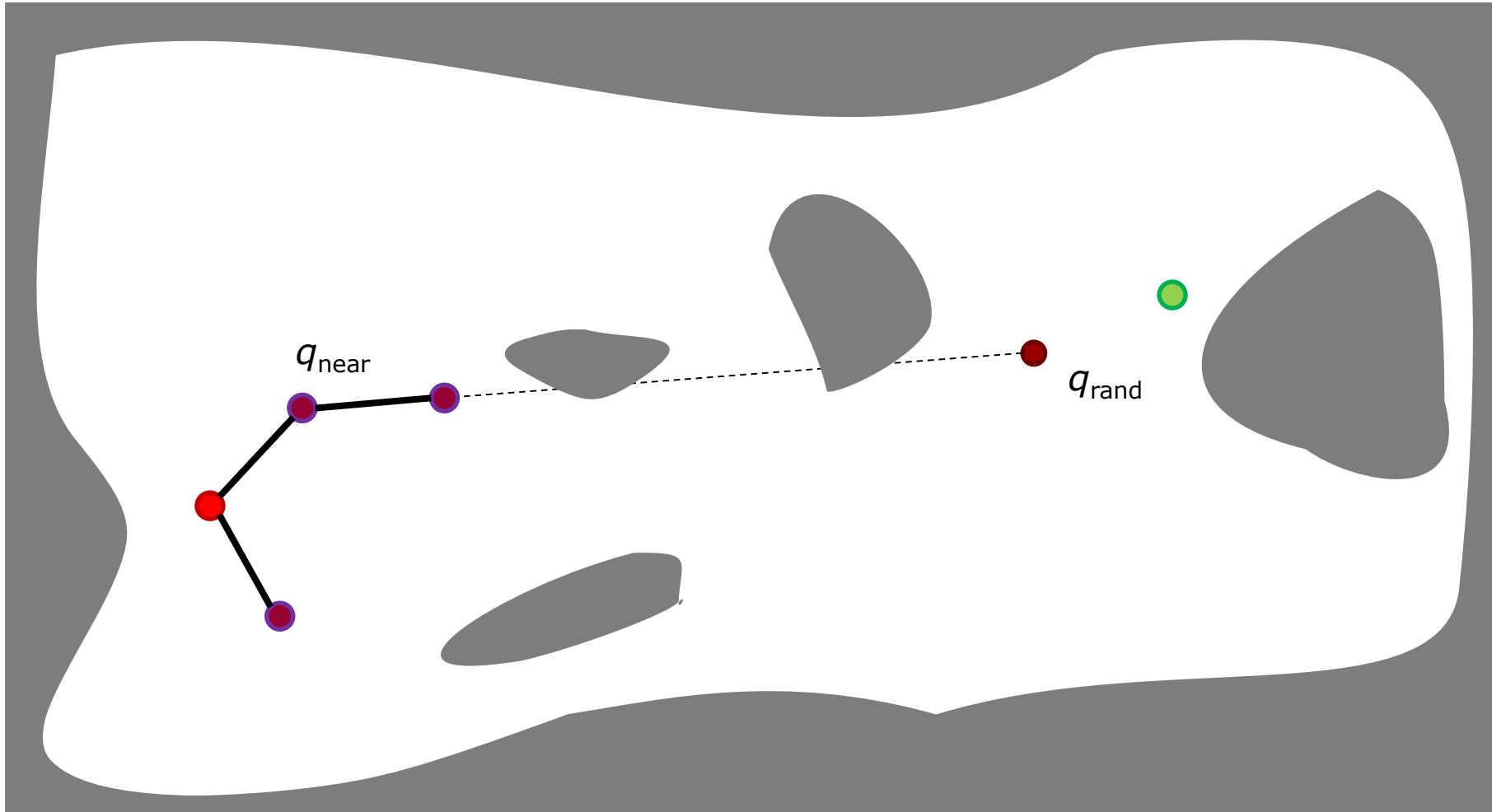
RRT

- Rapidly-exploring random trees



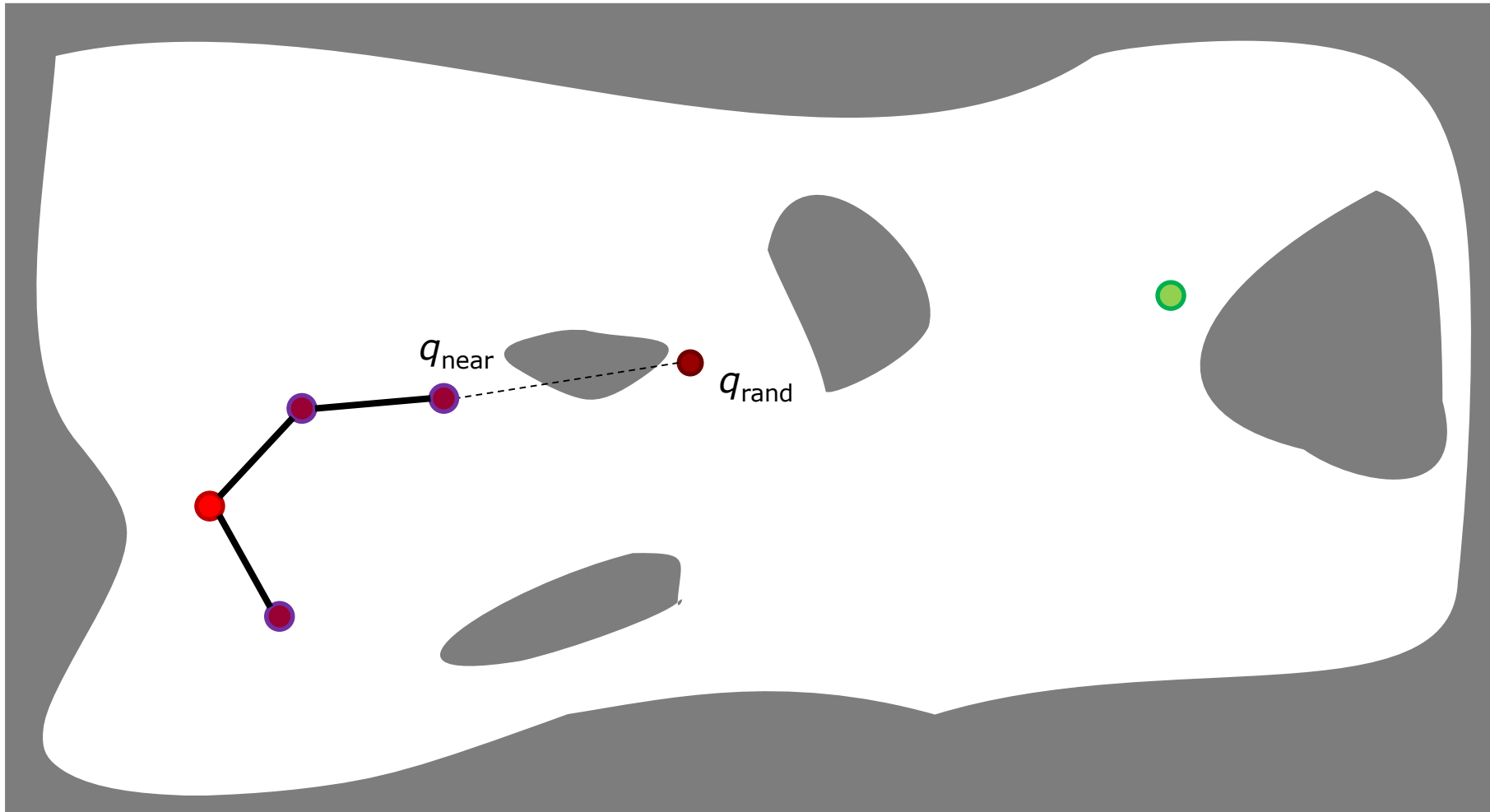
RRT

- Rapidly-exploring random trees



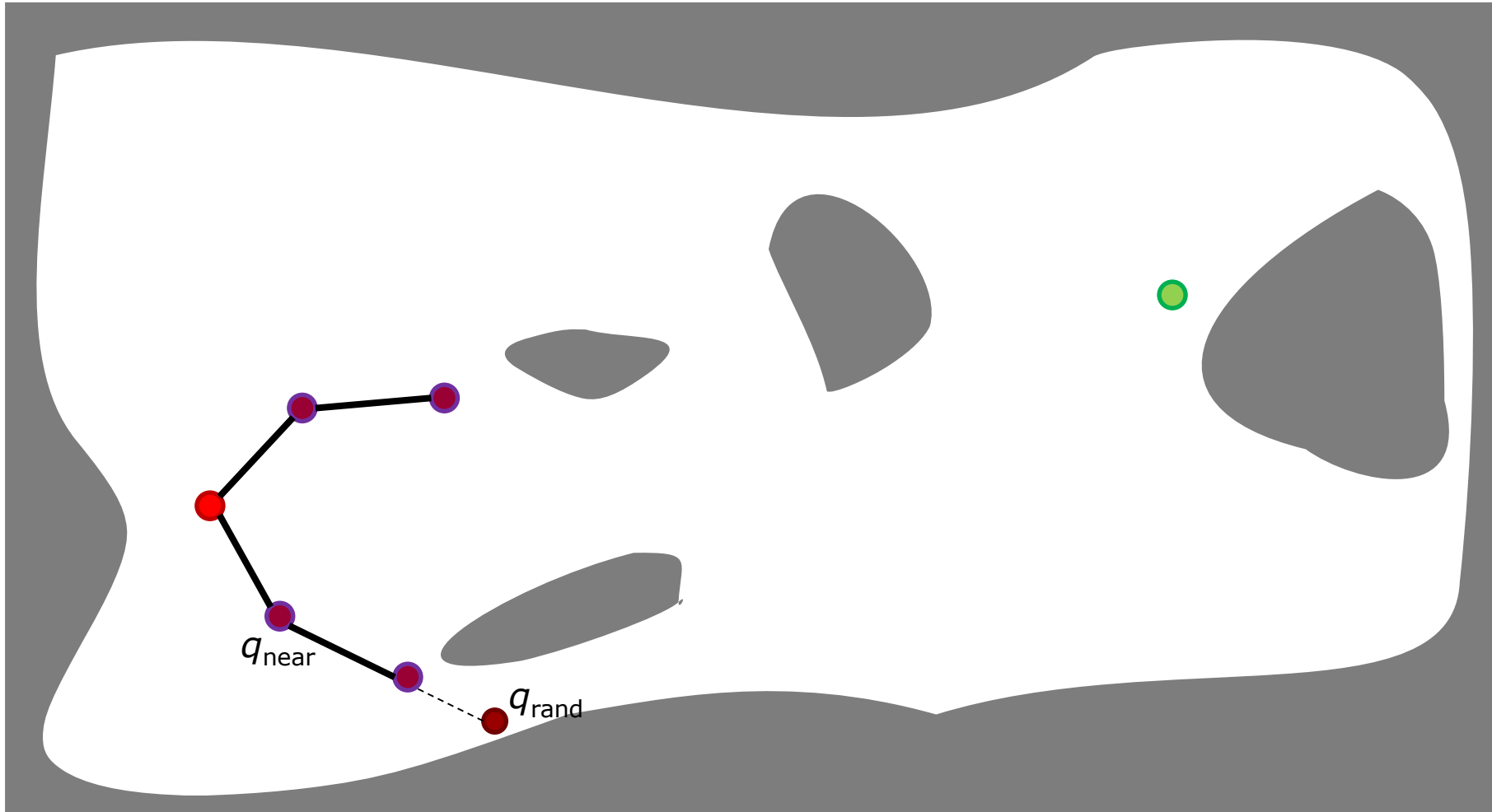
RRT

- Rapidly-exploring random trees



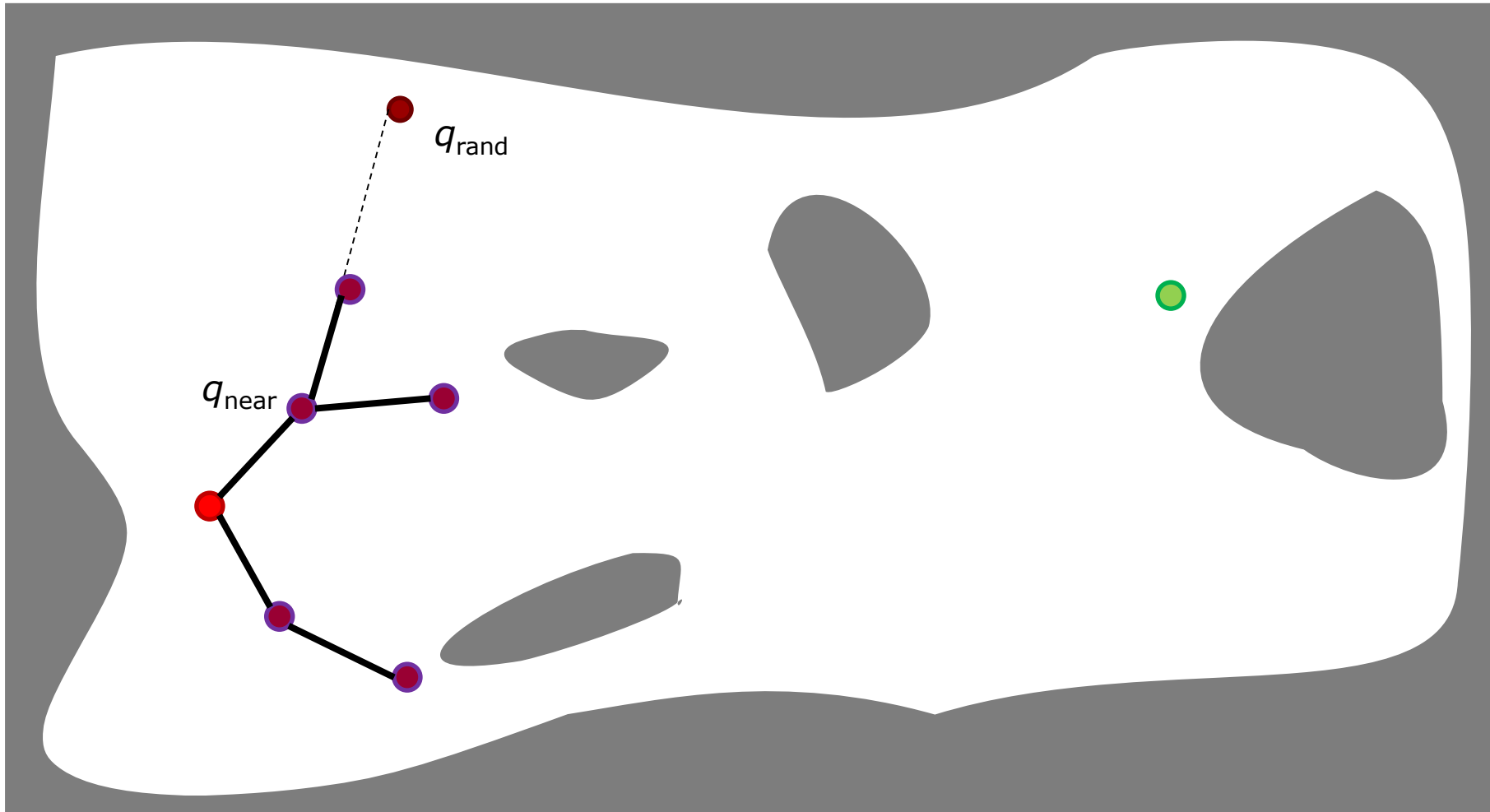
RRT:

- Rapidly-exploring random trees



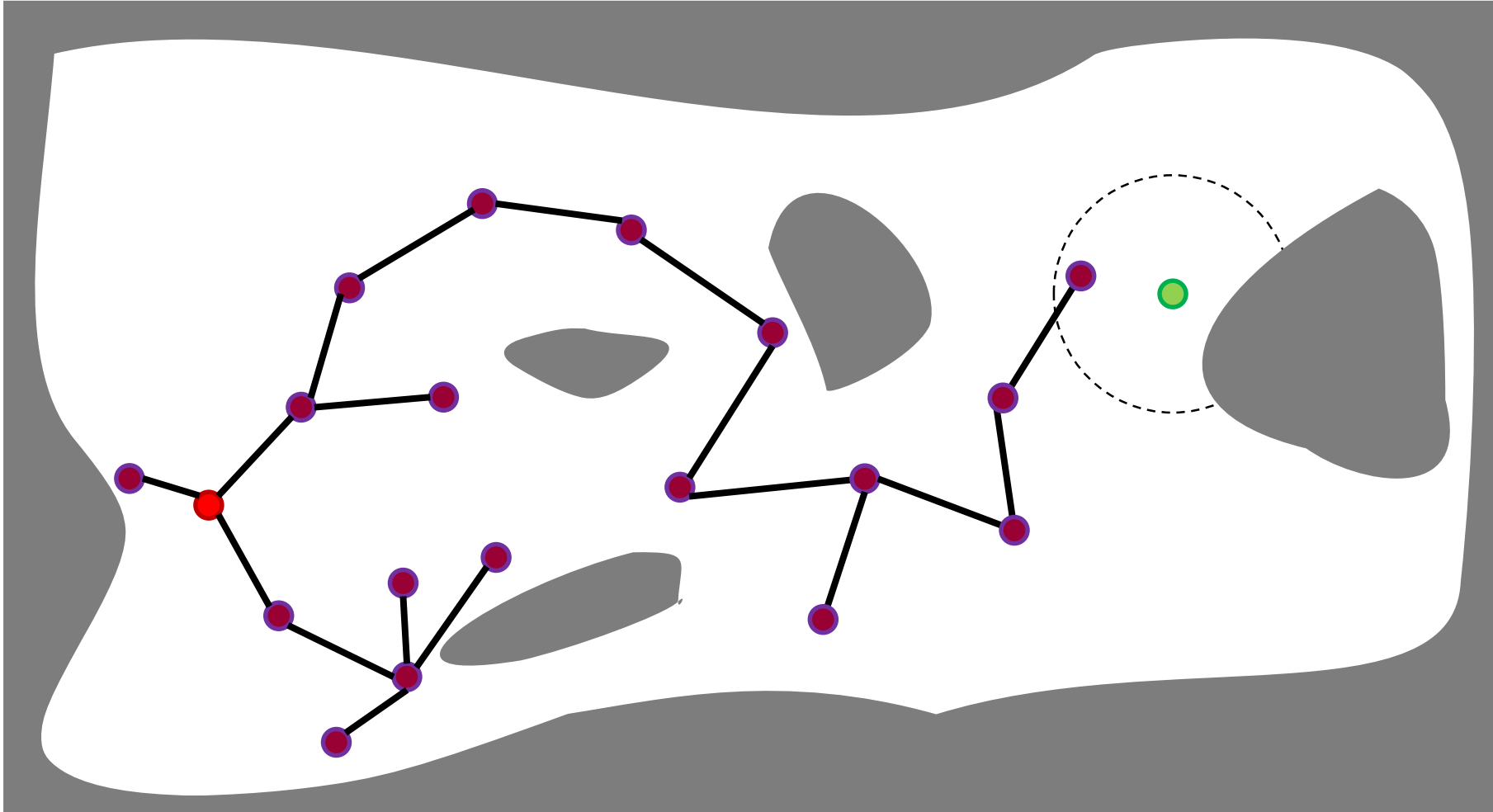
RRT

- Rapidly-exploring random trees



RRT

- Rapidly-exploring random trees



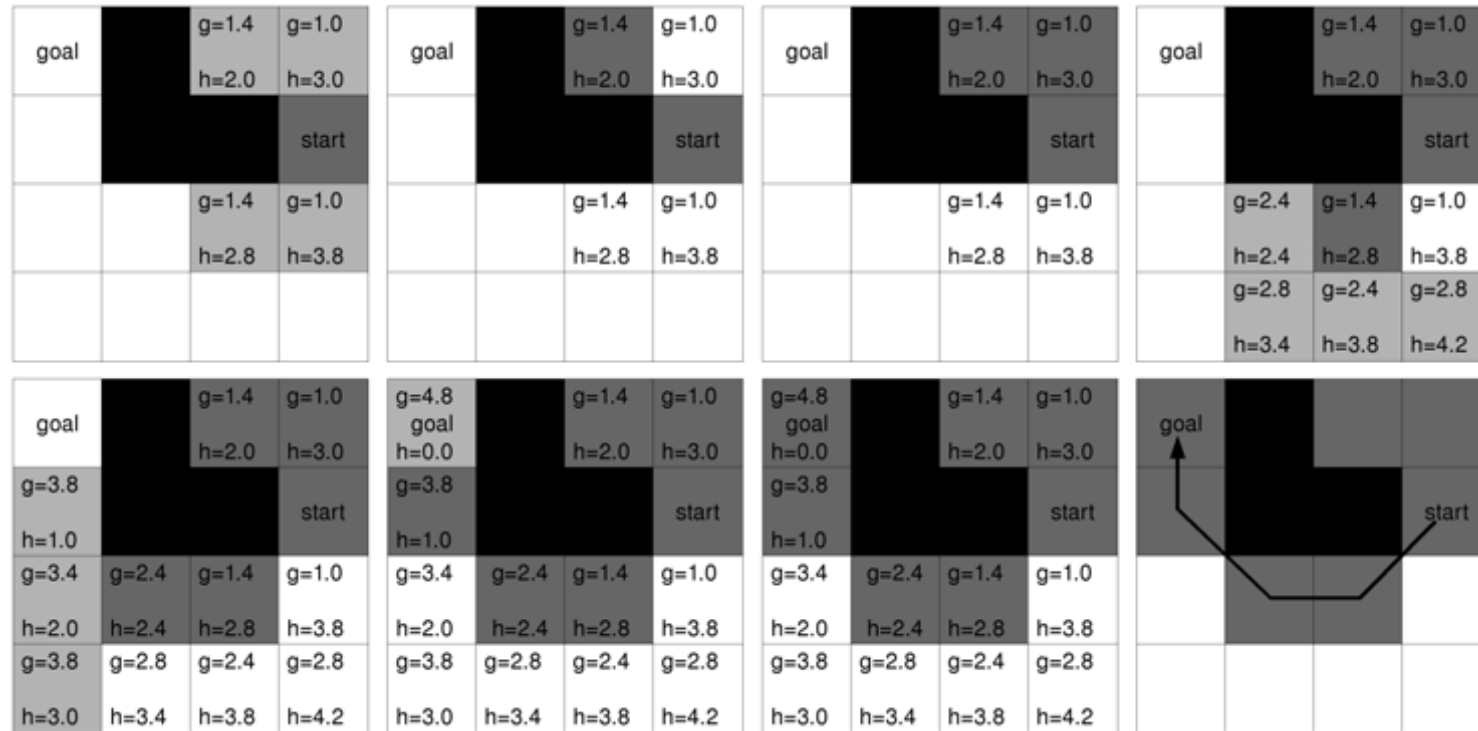
Forward Search Algorithms

- Forward Search Methods:
 - Breadth first
 - Dijkstra's algorithm
 - A*

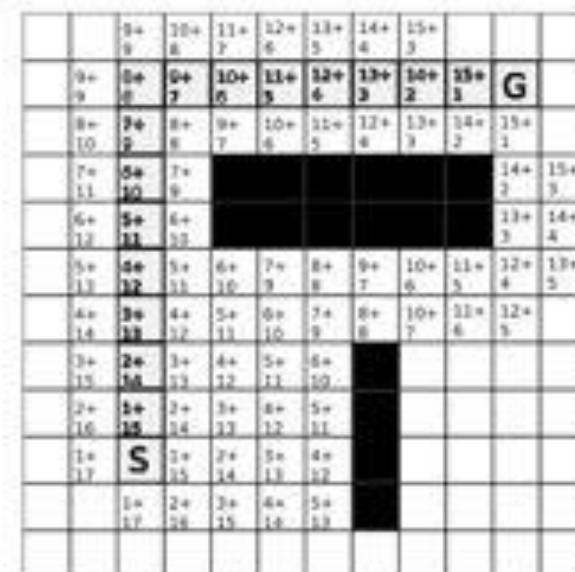
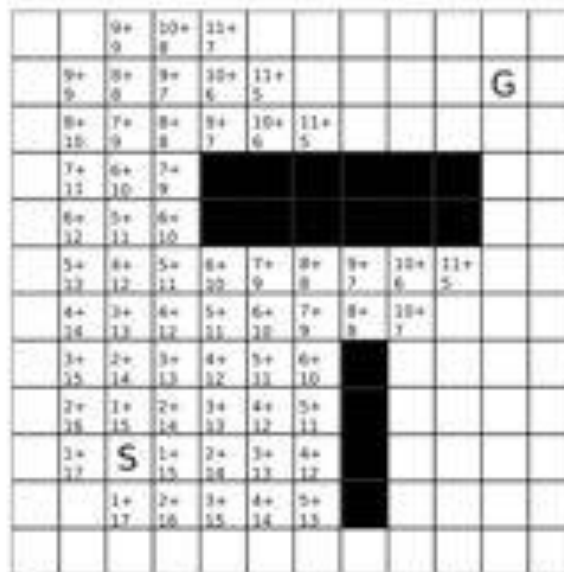
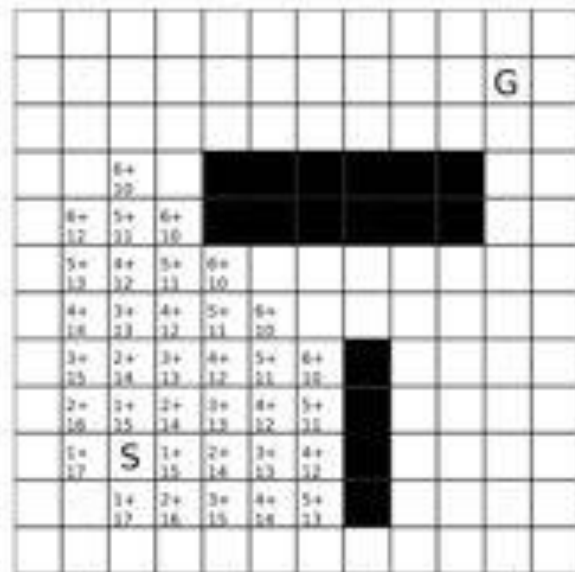
```
FORWARD_SEARCH
1   $Q.Insert(x_I)$  and mark  $x_I$  as visited
2  while  $Q$  not empty do
3       $x \leftarrow Q.GetFirst()$ 
4      if  $x \in X_G$ 
5          return SUCCESS
6      forall  $u \in U(x)$ 
7           $x' \leftarrow f(x, u)$ 
8          if  $x'$  not visited
9              Mark  $x'$  as visited
10              $Q.Insert(x')$ 
11          else
12              Resolve duplicate  $x'$ 
13  return FAILURE
```

Planning Algorithms: A* Search

- Similar to Dijkstra's algorithm, except that it uses a heuristic function $h(n)$
- $f(n) = g(n) + \epsilon h(n)$



Planning Algorithms: A*



Software for Autonomous Systems

SFfAS-31391:

Learning ROS Transforms (TF), Robot Visualization (RVIZ) and Simulation (Gazebo)

Lecturer, Course Coordinator: Evangelos Boukas—PhD