

$$\mu_X(n) = E[X(n)] = E[2Z(n) - 1] = 2 \underbrace{E[Z(n)]}_{=0.7} - 1 = 0.4$$

$$\sigma_X^2(n) = \text{Var}(2Z(n) - 1) = 4 \text{Var}(Z(n)) = 4 \times 0.7 \times 0.3 = 0.84$$

$$\mu_X(t) = E[At + B] = t E[A] + E[B] = \frac{1}{2}t + \frac{1}{2}$$

$$\sigma_X^2(t) = \text{Var}(At + B) = t^2 \text{Var}(A) + \text{Var}(B) = t^2 \frac{(2-0)^2}{12} + \frac{(2-0)^2}{12} = \frac{1}{3}t^2 + \frac{1}{3}$$

$$Y(n) = Y(n-1) + X(n), \quad X(n) \text{ random step de parámetro } p.$$

$$\mu_Y(n) = E[Y(n)] = E\left[\sum_{j=1}^n X(j)\right] = \sum_{j=1}^n E[X(j)] = n \mu_X(j) = n(2p-1)$$

$$\sigma_Y^2(n) = \text{Var}\left(\sum_{j=1}^n X(j)\right) \underset{iid}{=} \sum_{j=1}^n \text{Var}(X(j)) = n(4p(1-p))$$

No es ESA pues $\mu_Y(n)$ y $\sigma_Y^2(n)$ varían con n .

$$A = \mathcal{N}(1; 0.16) \quad \omega_0 = 0.015\pi$$

$$X(n) = A \cos(\omega_0 n)$$

$$\mu_X^{(n)} = E[X(n)] = E[A \cos(\omega_0 n)] = \overbrace{E[A]}^1 \cos(\omega_0 n) = \cos(0.015\pi n)$$

No es ESA pues $E[X(n)]$ depende de n .

$$\sigma_X^2(n) = \text{Var}(X(n)) = \text{Var}(A \cos(\omega_0 n)) = \cos^2(\omega_0 n) \text{Var}(A) = 0.16 \cos^2(\omega_0 n)$$

$$A=1, \quad \Theta \sim \mathcal{U}(0, 2\pi) \quad \omega_0 = 0.015\pi$$

$$X(n) = A \cos(\omega_0 n + \Theta)$$

$$\mu_X(n) = E[X(n)] = E[A \cos(\omega_0 n + \Theta)] = A E[\cos(\omega_0 n + \Theta)]$$

$$= A \int_0^{2\pi} \cos(\omega_0 n + t) \frac{1}{2\pi} dt = \frac{A}{2\pi} \sin(\omega_0 n + t) \Big|_0^{2\pi} = 0$$

$$\boxed{\mu_X(n) = 0}$$

$$\sigma_X^2(n) = \text{Var}(X(n)) = \text{Var}(A \cos(\omega_0 n + \Theta)) = A^2 \text{Var}(\cos(\omega_0 n + \Theta))$$

$$= A^2 E[\cos^2(\omega_0 n + \Theta)] = A^2 \int_0^{2\pi} \cos^2(\omega_0 n + t) \frac{1}{2\pi} dt = \frac{A^2}{2\pi} \left(\frac{2\omega_0 n + t}{2} + \frac{\sin(2\omega_0 n + t)}{4} \right) \Big|_0^{2\pi}$$

$$\boxed{\sigma_X^2(n) = \frac{A^2}{2}}$$

Es ESA.