

PROBLEMA GUÍA I #10

La componente i -ésima de la operación $\nabla \psi(r)$, donde $r = |\vec{r}|$, está dada por:

$$(\nabla \psi)_i = \partial_i \psi(r) = \frac{\partial}{\partial x_i} \psi(r) = \underbrace{\frac{\partial r}{\partial x_i} \frac{d\psi(r)}{dr}}_{\text{Regla de la cadena}}$$

$$(\nabla \psi(r))_i = \partial_i r \frac{d\psi(r)}{dr}$$

$$(\nabla \psi(r))_i = \frac{x_i}{r} \frac{d\psi(r)}{dr}$$

\Downarrow

Vectorialmente tenemos que:

$$\nabla \psi(r) = \frac{\vec{r}}{r} \frac{d\psi(r)}{dr}$$

∴ $\nabla \psi(r)$ es paralelo a \vec{r} .