

Función Hamiltoniana

Hamiltoniano

E1

Obs. $X_i \equiv X_i(\{q\}, t)$

$$\Downarrow$$
$$\dot{X}_i \equiv \dot{X}_i(\{q\}, \{\dot{q}\}, t)$$

$$\Downarrow$$
$$L \equiv L(\{\dot{X}\}, \{X\}, t) \Rightarrow L \equiv L(\{\dot{q}\}, \{q\}, t)$$

DEF

$$H = \sum_{j=1}^s \pi_{q_j} \dot{q}_j - L \quad (\text{Hamiltoniano})$$

Obs.

$$\frac{dH}{dt} = \dot{H} = \sum_{j=1}^s \dot{\pi}_{q_j} \dot{q}_j + \sum_{j=1}^s \pi_{q_j} \ddot{q}_j - \frac{dL}{dt}$$

$$\text{con } \frac{dL}{dt} = \sum_{j=1}^s \frac{\partial L}{\partial q_j} \dot{q}_j + \sum_{j=1}^s \frac{\partial L}{\partial \dot{q}_j} \ddot{q}_j + \frac{\partial L}{\partial t}$$

$\pi_{q_j} \dot{q}_j \leftarrow$ de la ec. de movimiento
 $\pi_{q_j} \leftarrow$ por def.

∴

$$\frac{dH}{dt} = -\frac{\partial L}{\partial t}$$

E₂

si L no depende explícitamente de t



$H = \text{cte. de movimiento.}$

Obs. ligaduras esclerónomas.



↑ independientes de t

$$f(\{x\}) = 0$$

si ligaduras son esclerónomas



$$H = E = T + V$$