Ecuaciones diferenciales homogeneas, exactas, factores integrantes

$$1. \qquad \frac{dy}{dx} = \frac{y-3}{x+y+1}$$

R:
$$\frac{x+4}{y-3} = \ln(y-3) + c$$

$$2. \qquad \frac{dy}{dx} = \frac{x - 3y - 7}{x - 4}$$

R:
$$(x-4)^4 - 4(x-4)^3(y+1) = c$$

3.
$$\frac{dy}{dx} = \frac{x+2y+7}{-2x+y-9}$$

R:
$$y^2 - 18y - 4xy - 14x - x^2 = c$$

$$4. \qquad \frac{dy}{dx} = \left(\frac{x+y+1}{x+1}\right)^2$$

R:
$$\frac{2}{\sqrt{3}} \operatorname{arctg}\left(\frac{x+2y+1}{\sqrt{3}(x+1)}\right) = \ln(x+1) + c$$

$$5. \qquad \frac{dy}{dx} = \frac{x - y + 2}{x - y + 3}$$

R:
$$x = \frac{(x-y+3)^2}{2} + c$$

6.
$$\frac{dy}{dx} = \frac{2x^3 + 6xy^2 - 2y^3 + 4x + 3y}{6xy^2 - 6x^2y + 4y^3 - 3x + 2y}$$

R:
$$\frac{x^4}{2} + 3x^2y^2 - 2xy^3 - y^4 + 2x^2 + 3xy - y^2 = c$$

7.
$$\frac{dy}{dx} = -\frac{2x^3y^2 + 4x^2y + 2xy^2 + xy^4 + 2y}{2(y^3 + x^2y + x)}$$

R:
$$ce^{-x^2} = 2x^2y^2 + 4xy + y^4$$

8.
$$\left(\frac{x^2-y^2}{x^2y}-\frac{y}{x^2+y^2}\right)dx+\left(\frac{x}{x^2+y^2}+\frac{y^2-x^2-x}{xy^2}\right)dy=0$$

R:
$$\operatorname{arctg}\left(\frac{y}{x}\right) + \frac{x^2 + x + y^2}{xy} = c$$

9.
$$\left(\frac{2x}{\sqrt{x^2+y^2}}-y^2\right)dx+\left(\frac{2y}{\sqrt{x^2+y^2}}-2xy\right)dy=0$$

R:
$$arctg(\frac{y}{x}) + \frac{x^2 + x + y^2}{xy} = c$$

10.
$$\left(\frac{1}{x-y} + \frac{x}{x^2+y^2}\right) dx + \left(\frac{1}{y-x} + \frac{y}{x^2+y^2}\right) dy = 0$$

R:
$$(x - y)^2(x^2 + y^2) = c$$

11.
$$(3x^2 + 2xy)dx + (2x^3 + x^2 + 2x^2y)dy = 0$$

$$R: x^2 e^{2y}(x+y) = c$$

12.
$$\arcsin(y)dx + \frac{x+2\sqrt{1-y^2}\cos(y)}{\sqrt{1-y^2}}dy = 0$$

$$R: x \operatorname{arcsen}(y) + 2 \operatorname{sen}(y) = c$$

13.
$$(x\ln(y) + y\ln(x) + y)dx + \left(\frac{x^2}{2y} + x\ln(x)\right)dy = 0$$

$$R: \frac{1}{2}x^2 \ln|y| + xy \ln|x| = c$$

14.
$$(10x^4y^2 + 4x^3y)dx - (2x^5y + 2x^4)dy = 0$$

R:
$$2x^5y + x^4 = cy^2$$

15.
$$xdx + (x^2 + y^2 + y)dy = 0$$

R:
$$(x^2 + y^2)e^{y^2} = c$$

16.
$$ydx - (x^2 + y^2 + x)dy = 0$$

$$R: x = y \tan(c + y)$$