

$$I) \int_0^{\infty} x^{\alpha-1} \exp\left(-\alpha x - \frac{1}{x}\right) dx = I_a \quad (1)$$

$$\Delta \exp\left(\frac{1}{x}\right) = \sum_{n \geq 0} \frac{1^n}{n!} \quad \left\{ \exp\left(-\alpha x - \frac{1}{x}\right) = \sum_{n \geq 0} \phi\left(\alpha x + \frac{1}{x}\right)^n \right.$$

$$\Delta \left(\alpha x + \frac{1}{x}\right)^n = \left(\frac{1}{x}\right)^n (\alpha x^2 + 1)^n$$

poly-binario 4

$$\text{poly-bis 1) } (\alpha x^2 + 1)^n = \sum_{i \geq 0} \sum_{j \geq 0} \phi_i \phi_j \alpha^i x^{2i} \frac{\langle -n+i+j \rangle}{\Gamma(-n)}$$

en la integral:

$$I_a = \int_0^{\infty} x^{\alpha-1} x^{-n} \sum_{n \geq 0} \phi_n \sum_{i,j \geq 0} \phi_i \phi_j \alpha^i x^{2i} \frac{\langle -n+i+j \rangle}{\Gamma(-n)}$$

$$= \sum_{i,j,n \geq 0} \phi_i \langle \alpha - n + 2i \rangle \alpha^i \langle i+j-n \rangle \frac{1}{\Gamma(-n)}$$

solución: con i libre

$$I_{\alpha i} = \sum_i \phi_i \frac{\Gamma(-n) \Gamma(-j) \alpha^i}{\Gamma(-n)} \quad \left\{ \begin{array}{l} n = \alpha - 2i \\ j = n - i = -\alpha - 3i \end{array} \right.$$

$$I_{\alpha i} = \sum_i \phi_i \frac{\Gamma(\alpha + 2i) \Gamma(-\alpha - 3i) \alpha^i}{\Gamma(\alpha + 2i)}$$

solución: j libre

$$I_{\alpha j} = \sum_{j \geq 0} \phi_j \frac{\Gamma(-n) \Gamma(-i) \alpha^i}{\Gamma(-n)}$$

$$\det \begin{pmatrix} -2 & -1 \\ -1 & -1 \end{pmatrix} = 1 \quad \left\{ \det(h) = 1 \right.$$

$$I_{\alpha j} = \sum_{j \geq 0} \phi_j \Gamma(\alpha - j) \alpha^{(j-\alpha)}$$

$$\begin{pmatrix} 2 & -1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} i \\ n \end{pmatrix} = \begin{pmatrix} -\alpha \\ -j \end{pmatrix}$$

↙

$$\begin{array}{l} i = j - \alpha \\ n = 2j - \alpha \end{array}$$

$$I_{\alpha n} = \frac{1 \dots}{\Gamma(-n)} = 0 \quad \text{nula.}$$

$$I) \int_0^{\infty} x^{\alpha-1} \exp\left(-\alpha x - \frac{1}{x}\right) dx = I_a$$

①

$$\Delta \exp(z) = \sum_{n \geq 0} \frac{z^n}{n!} \quad \hookrightarrow \exp\left(-\alpha x - \frac{1}{x}\right) = \sum_{n \geq 0} \phi\left(\alpha x + \frac{1}{x}\right)^n$$

$$\Delta \left(\alpha x + \frac{1}{x}\right)^n = \left(\frac{1}{x}\right)^n \underbrace{(\alpha x^2 + 1)^n}_{\text{polynomial 1}}$$

$$\text{poly-bin 1)} (\alpha x^2 + 1)^n = \sum_{i \geq 0} \sum_{j \geq 0} \phi_i \phi_j \alpha^i x^{2i} \frac{\langle -n+i+j \rangle}{\Gamma(-n)}$$

en la integral:

$$I_a = \int_0^{\infty} x^{\alpha-1} x^{-n} \sum_{n \geq 0} \phi_n \sum_{i,j \geq 0} \phi_i \phi_j \alpha^i x^{2i} \frac{\langle -n+i+j \rangle}{\Gamma(-n)}$$

$$= \sum_{i,j,n \geq 0} \phi \langle \alpha - n + 2i \rangle \alpha^i \langle i+j-n \rangle \frac{1}{\Gamma(-n)}$$

solución con ϵ libre

solución con i libre

$$I_{\alpha i} = \sum_i \phi \frac{\Gamma(-n) \Gamma(-j)}{\Gamma(-n)} \alpha^i \quad \left| \begin{array}{l} n = -\alpha - 2i \\ j = n - i = -\alpha - 3i \end{array} \right.$$

$$I_{\alpha i} = \sum_i \phi \frac{\Gamma(\alpha + 2i) \Gamma(-\alpha - 3i)}{\Gamma(\alpha + 2i)} \alpha^i$$

solución j libre

$$I_{\alpha j} = \sum_{j \neq 0} \phi \frac{\Gamma(-n) \Gamma(-i)}{\Gamma(-n)} \alpha^i$$

$$I_{\alpha j} = \sum_{j \neq 0} \phi \Gamma(\alpha - j) \alpha^{j-\alpha}$$

$$I_{\alpha n} = \frac{1_{\alpha n}}{p(-n)} = 0 \quad \text{nula.}$$

$$\det \begin{pmatrix} -2 & -1 \\ 1 & -1 \end{pmatrix} = \det(h) = 1$$

$$h = \begin{pmatrix} -2 & -1 \\ 1 & -1 \end{pmatrix} \quad \alpha = \begin{pmatrix} i \\ n \end{pmatrix}$$

$$\begin{pmatrix} 2 & -1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} i \\ n \end{pmatrix} = \begin{pmatrix} -\alpha \\ -j \end{pmatrix}$$

\downarrow

$$\begin{array}{l} i = j - \alpha \\ n = 2j - \alpha \end{array}$$

$$I_2) \int_0^{\infty} x^{\alpha-1} \exp\left(-\alpha x^2 - \frac{1}{x^2}\right) dx = I_p$$

(2)

$$\exp\left(-\alpha x^2 - \frac{1}{x^2}\right) = \sum_{n=0}^{\infty} \phi_n \left(\alpha x^2 + \frac{1}{x^2}\right)^n$$

$$\left(\alpha x^2 + \frac{1}{x^2}\right)^n = \left(\left(\frac{1}{x^2}\right)(\alpha x^4 + 1)\right)^n = x^{-2n} (\alpha x^4 + 1)^n$$

$$= x^{-2n} \sum_{i=0}^n (\alpha x^4)^i (-n)_i \phi_i$$

$$\alpha x^i \exp(\dots) = \sum_{i,n} \phi_n \phi_i x^{-2n}$$

$$\dots \alpha^i x^{4i} (-n)_i$$

$$I_p = \sum_{i,n} \phi_n \langle -2n + 4i + \alpha \rangle \alpha^i (-n)_i$$

$$\frac{1}{2} \langle -n + 2i + \frac{\alpha}{2} \rangle$$

$$i \text{ libre: } I_{pi} = \sum_i \phi_i \frac{\Gamma(-n)}{2} \alpha^i (-n)_i \Big|_{n=2i+\frac{\alpha}{2}}$$

$$I_{pi} = \sum_i \phi_i \frac{\Gamma(2i+\frac{\alpha}{2})}{2} \alpha^i \left(2i+\frac{\alpha}{2}\right)_i$$

$$I_{pi} = \sum_i \phi_i \frac{\alpha^i \Gamma(3i+\frac{\alpha}{2})}{2}$$

$$\frac{\Gamma(3i+\frac{\alpha}{2})}{\Gamma(2i+\frac{\alpha}{2})}$$

$$n \text{ l.h.o: } I_{pn} = \sum_{n \geq 0} \phi_n \frac{\Gamma(-i)}{4} \alpha^i (-n)_i \Big|_{i=\frac{n-\alpha}{2}}$$

$$I_{pn} = \sum_{n \geq 0} \phi_n \frac{\Gamma(\frac{n-\alpha}{2})}{4} \frac{\alpha^{\frac{n-\alpha}{2}}}{\alpha^{\frac{\alpha}{4}}}$$

$$\frac{\Gamma(-\frac{n-\alpha}{2})}{\Gamma(-n)}$$

provoque solution nulle

$$I = I_{pi} = \sum_i \phi_i \frac{\alpha^i \Gamma(3i+\frac{\alpha}{2})}{2}$$

$$I_2) \int_0^{\infty} x^{\alpha-1} \exp\left(-\alpha x^2 - \frac{1}{x^2}\right) dx = I_p$$

(2)

$$\exp\left(-\alpha x^2 - \frac{1}{x^2}\right) = \sum_{n \geq 0} \phi_n \left(\alpha x^2 + \frac{1}{x^2}\right)^n$$

$$\left(\alpha x^2 + \frac{1}{x^2}\right)^n = \left(\left(\frac{1}{x^2}\right)(\alpha x^4 + 1)\right)^n = x^{-2n} (\alpha x^4 + 1)^n$$

$$= x^{-2n} \sum_{i \geq 0} \binom{n}{i} (\alpha x^4)^i (-n)_i \phi_i$$

$$\text{and } \exp(\cdot) = \sum_{i,n} \phi_n \phi_i x^{-2n}$$

$$\dots \alpha^i x^{4i} (-n)_i$$

$$I_p = \sum_{i,n} \phi_i \langle -2n + 4i + \alpha \rangle \alpha^i (-n)_i \leftarrow$$

$$\frac{1}{2} \langle -n + 2i + \frac{\alpha}{2} \rangle$$

$$i \text{ libre: } I_{pi} = \sum_i \phi_i \frac{\Gamma(-n)}{2} \alpha^i (-n)_i \Big|_{n=2i+\frac{\alpha}{2}}$$

$$I_{pi} = \sum_i \phi_i \frac{\Gamma(2i+\frac{\alpha}{2})}{2} \alpha^i \left(2i+\frac{\alpha}{2}\right)_i$$

$$I_{pi} = \sum_i \phi_i \frac{\alpha^i \Gamma(3i+\frac{\alpha}{2})}{2}$$

$$\frac{\Gamma(3i+\frac{\alpha}{2})}{\Gamma(2i+\frac{\alpha}{2})}$$

$$n \text{ libre: } I_{pn} = \sum \phi \Gamma(-i) \alpha^i (-n)_i$$

$$\text{and } \exp(\dots) = \sum_{i,n} \phi_i \phi_n \bar{\chi}^n$$

$$\dots \alpha^i \chi^{4i} (-n)_i$$

$$\hookrightarrow \mathcal{I}_p = \sum_{i,n} \phi_i \langle -2n + 4i + \alpha \rangle \alpha^i (-n)_i \quad \leftarrow$$

$$\frac{1}{2} \langle -n + 2i + \frac{\alpha}{2} \rangle$$

$$i \text{ libre: } \mathcal{I}_{pi} = \sum_i \phi_i \frac{\Gamma(-n)}{2} \alpha^i (-n)_i \Big|_{n=2i+\frac{\alpha}{2}}$$

$$\mathcal{I}_{pi} = \sum_i \phi_i \frac{\Gamma(2i+\frac{\alpha}{2})}{2} \alpha^i \underbrace{(2i+\frac{\alpha}{2})}_i$$

$$\mathcal{I}_{pi} = \sum_i \phi_i \frac{\alpha^i \Gamma(3i+\frac{\alpha}{2})}{2} \quad \frac{\Gamma(3i+\frac{\alpha}{2})}{\Gamma(2i+\frac{\alpha}{2})}$$

$$n \text{ libre: } \mathcal{I}_{pn} = \sum_{n \geq 0} \phi \frac{\Gamma(-i)}{4} \alpha^i (-n)_i \Big|_{i=\frac{n-\frac{\alpha}{2}}{4}}$$

$$\mathcal{I}_{pn} = \sum_{n \geq 0} \phi \frac{\Gamma(\frac{n}{2}-\frac{\alpha}{4})}{4} \frac{\alpha^{\frac{n}{2}}}{\alpha^{\frac{\alpha}{4}}} \frac{\Gamma(-\frac{n}{2}-\frac{\alpha}{4})}{\Gamma(-n)} \quad \leftarrow \text{provoca singularidade}$$

$$\boxed{\mathcal{I} = \mathcal{I}_{pi} = \sum_i \phi_i \frac{\alpha^i}{2} \Gamma(3i+\frac{\alpha}{2})}$$

(3)

$$II = \int_0^{\infty} J_{\nu}\left(\frac{\alpha}{x}\right) J_{\nu}(bx) dx$$

$$J_{\nu}\left(\frac{\alpha}{x}\right) = \left(\frac{\alpha}{2x}\right)^{\nu} \frac{1}{\Gamma(1+\nu)} {}_0F_1\left(-\right) - \frac{\alpha^2}{4x^2}$$

$$J_{\nu}(bx) = \left(\frac{bx}{2}\right)^{\nu} \frac{1}{\Gamma(1+\nu)} {}_0F_1\left(-\right) - \frac{bx^2}{4}$$

$$II = \int_0^{\infty} \frac{\alpha^{\nu} b^{\nu}}{4^{\nu}} \frac{1}{(\Gamma(1+\nu))^2} \sum_{i \geq 0} \frac{1}{(1+\nu)_i} \phi_i \frac{\alpha^{2i}}{4^i x^{2i}} \sum_{j \geq 0} \frac{1}{(1+\nu)_j} \phi_j \frac{b^{2j} x^{2j}}{4^j} dx$$

$$II = \sum_{i,j \geq 0} \frac{\alpha^{v+2i} b^{v+2j}}{4^{v+i+j}} \frac{1}{(\Gamma(1+\nu))^2} \frac{\Gamma(1+\nu)}{\Gamma(1+\nu+i)} \frac{\Gamma(1+\nu)}{\Gamma(1+\nu+j)} \int_0^{\infty} x^{2j-2i-1} dx$$

$$\frac{1}{2} \langle 2j - 2i - 1 \rangle$$

reolviendo i de j lib

$$II_j = \sum_{i \geq 0} \phi \frac{\alpha^{v+2j+1}}{2} \frac{b^{v+2j}}{4^{v+2j+\frac{1}{2}}} \frac{\Gamma(-j-\frac{1}{2})}{\Gamma(1+\nu+j+\frac{1}{2}) \Gamma(1+\nu+j)}$$

$$i = j + \frac{1}{2} \\ \downarrow \\ j = i - \frac{1}{2}$$

reolv j de i lib

$$II_i = \sum_{j \geq 0} \phi \frac{\alpha^{v+2i}}{2} \frac{b^{v+2i-2}}{4^{v+2i-\frac{1}{2}}} \frac{\Gamma(\frac{1}{2}+i)}{\Gamma(1+\nu+i) \Gamma(1+\nu+i-\frac{1}{2})}$$

solucion



III

4

$$\exp(xM^2) = \sum_{i \geq 0} \frac{x^i M^{2i}}{i!}; \quad \exp(yM^2) = \sum_{j \geq 0} \frac{y^j M^{2j}}{j!}$$

$$\exp\left(-\frac{xy}{x+y} p^2\right) = \sum_{k \geq 0} \phi_k (xy)^k p^{2k} (x+y)^{-k}$$

2 brackets y 3 sumatorias, veamos por jeta polinomio

$$(x+y)^k (x+y)^{-\frac{p}{2}} = \sum_{\delta \geq 0} \phi_{\delta} \sum_{\zeta \geq 0} \phi_{\zeta} x^{\delta} y^{\zeta} \frac{\langle \frac{p}{2} + k + \delta + \zeta \rangle}{\Gamma(\frac{p}{2} + k)} \quad \begin{matrix} + 2 \text{ en} \\ + 1 \text{ en } \end{matrix}$$

entonces III = $\int_0^{\infty} \sum_{i,j,k,\delta,\zeta} \phi$ 5 sum. $\therefore \binom{5}{2}$ forma una 2 brackets

idea $\xrightarrow{\quad}$ Juntar las exponenciales primero $\exp(xM^2) \exp(yM^2) \exp\left(-\frac{xy}{x+y} p^2\right)$

$$\exp(M^2(x+y)) = \sum_{i \geq 0} M^{2i} (x+y)^i; \quad \exp\left(-\frac{xy}{x+y} p^2\right) = \sum_{k \geq 0} \phi \frac{x^k y^k p^{2k}}{(x+y)^k}$$

multinomio que ya requerimos expandir

ahora jeta $(x+y)^i \rightarrow (x+y)^{-i+k+\frac{p}{2}} = \sum_{\delta, \zeta \geq 0} \phi \phi x^{\delta} y^{\zeta} \frac{\langle -i+k+\frac{p}{2} + \delta + \zeta \rangle}{\Gamma(-i+k+\frac{p}{2})}$

entonces

$$\text{III} = \sum_{i,j,k,\delta,\zeta} M^{2i} p^{2k} \frac{\langle k-i+\frac{p}{2} + \delta + \zeta \rangle}{\Gamma(k-i+\frac{p}{2})} \langle \alpha + k + \delta \rangle \langle \beta + k + \zeta \rangle$$

bucket de x bucket de y

1) Serie de brackets equivalente

ver $\textcircled{3}$ para matrices utiles

III
2)

Matrices Para distintos casos

$$A \begin{pmatrix} v_i \\ v_k \\ v_\gamma \end{pmatrix} = \begin{pmatrix} c_i \\ c_k \\ c_\gamma \end{pmatrix}$$

i libre $m_i \cdot v_i = c_i$

$$\begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix} \begin{pmatrix} k \\ \gamma \\ \zeta \end{pmatrix} = \begin{pmatrix} i - \frac{p}{2} \\ -\alpha \\ -\beta \end{pmatrix} \quad |\det(A)| = 1$$

k libre $m_k \cdot v_k = c_k$

$$\begin{pmatrix} -1 & 1 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} i \\ \gamma \\ \zeta \end{pmatrix} = \begin{pmatrix} -\frac{p}{2} - k \\ -\alpha - k \\ -\beta - k \end{pmatrix} \quad |\det(A)| = 0$$

γ libre $m_\gamma \cdot v_\gamma = c_\gamma$

$$\begin{pmatrix} -1 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 1 \end{pmatrix} \begin{pmatrix} i \\ k \\ \zeta \end{pmatrix} = \begin{pmatrix} -\frac{p}{2} - \gamma \\ -\alpha - \gamma \\ -\beta \end{pmatrix} \quad |\det(A)| = 1$$

ζ libre $m_\zeta \cdot v_\zeta = c_\zeta$

$$\begin{pmatrix} -1 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} i \\ k \\ \gamma \end{pmatrix} = \begin{pmatrix} -\frac{p}{2} - \zeta \\ -\alpha \\ -\beta - \zeta \end{pmatrix} \quad |\det(A)| = 1$$

Soluciones

i libre $k = \frac{p}{2} - i - \alpha - \beta$ γ libre $i = \frac{p}{2} - \beta + \gamma$

$\gamma = \frac{1}{2}(\gamma_i - p + 2\beta)$

$k = -\alpha - \gamma$

$\zeta = \frac{1}{2}(\zeta_i - p + 2\alpha)$

$\zeta = \alpha - \beta + \gamma$

γ libre

no solution
 $\det(m) = 0$

ζ libre $i = \frac{p}{2} - \alpha + \zeta$

$k = -\beta - \zeta$

$\gamma = -\alpha + \beta + \zeta$

solución i lib

$$\mathbb{II}_i = \sum_{i \geq 0} \phi_i \frac{\Gamma(-i-\alpha+\frac{P}{2}) \Gamma(-i-\beta+\frac{P}{2}) \Gamma(i+\alpha+\beta-\frac{P}{2})}{\Gamma(-2i+P-\alpha-\beta)} \frac{M^{2i}}{P^{2i}}$$

$\frac{P^P}{P^\alpha P^\beta}$ es constante definida por cond. de borde

$$\Gamma(-i-\alpha+\frac{P}{2}) = \frac{\Gamma(\frac{P}{2}-\alpha) (\frac{P}{2}-\alpha)_i}{(1+\alpha-\frac{P}{2})_i}$$

$$\Rightarrow = \Gamma(\frac{P}{2}-\alpha) \frac{(-1)^i}{(1+\alpha-\frac{P}{2})_i}$$

$$\Gamma(i+\alpha+\beta-\frac{P}{2}) = (\alpha+\beta-\frac{P}{2})_i \Gamma(\alpha+\beta-\frac{P}{2})$$

$$\Gamma(-i-\beta+\frac{P}{2}) = \frac{\Gamma(\frac{P}{2}-\beta) (-1)^i}{(1+\beta-\frac{P}{2})_i}$$

$$\Gamma(-2i+P-\alpha-\beta) = \frac{\Gamma(P-\alpha-\beta) (P-\alpha-\beta)_{-2i}}{(1-P+\alpha+\beta)_{2i}}$$

$$\frac{(1-P+\alpha+\beta)_{2i}}{2^{2i}} = \left(4^i \left(\frac{z}{2}\right)_i \left(\frac{z}{2} + \frac{1}{2}\right)_i\right)^{-1}$$

pero note algo

$$\frac{\Gamma(-i-\alpha+\frac{P}{2}) \Gamma(-i-\beta+\frac{P}{2})}{\Gamma(-2i+P-\alpha-\beta)} = B\left(-i-\alpha+\frac{P}{2}, -i-\beta+\frac{P}{2}\right)$$

sin embargo solo hay una representación hipergeométrica para la beta incompleta

$$\mathbb{II}_i = \sum_{i \geq 0} \phi_i P^{P-\alpha-\beta} \frac{\Gamma(\frac{P}{2}-\alpha) \Gamma(\frac{P}{2}-\beta) \Gamma(\alpha+\beta-\frac{P}{2})}{\Gamma(P-\alpha-\beta)} \frac{(\alpha+\beta-\frac{P}{2})_i}{(1+\alpha-\frac{P}{2})_i (1+\beta-\frac{P}{2})_i} \left(-4 \frac{M^2}{P^2}\right)^i$$

$$\mathbb{II} = P^{P-\alpha-\beta} \frac{\Gamma(\frac{P}{2}-\alpha) \Gamma(\frac{P}{2}-\beta) \Gamma(\alpha+\beta-\frac{P}{2})}{\Gamma(P-\alpha-\beta)}$$

$${}_3F_2 \left(\begin{matrix} \alpha+\beta-\frac{P}{2}, z, y \\ 1+\alpha-\frac{P}{2}, 1+\beta-\frac{P}{2} \end{matrix} \middle| -\frac{4M^2}{P^2} \right)$$

$$(z, y) = \left(\frac{1-P+\alpha+\beta}{2}, 1+\frac{\alpha+\beta-P}{2} \right)$$

24) F_2 converge por $\frac{4M^2}{P^2} < 1$

$$\hookrightarrow 1 < \frac{P^2}{4M^2}$$

solución γ libre

$$\text{III}_\gamma = \frac{M^{p-2\beta}}{p^{2\alpha}} \left(\frac{M^{2\delta}}{p^{2\delta}} \right) \frac{\Gamma\left(-\frac{p}{2} + \beta - \delta\right) \Gamma(-\alpha + \beta - \delta) \Gamma(\alpha + \delta)}{\Gamma(-\alpha + \beta - 2\delta)} \Bigg|_{\delta=0}$$

$$\left(\frac{\Gamma(-\alpha + \beta - 2\delta)}{\Gamma(-\alpha + \beta - \delta)} \right)^{-1} = \left(\frac{\Gamma(\beta - \alpha) (\beta - \alpha)_{2\delta}}{\Gamma(\beta - \alpha) (\beta - \alpha)_\delta} \right)^{-1} = \left(\frac{\Gamma(\beta - \alpha)}{(1 - \beta + \alpha)_\delta} \right)^{-1} = \left(\frac{\Gamma(\beta - \alpha)}{4^\delta \left(\frac{1 - \beta + \alpha}{2}\right)_\delta \left(\frac{\alpha - \beta}{2}\right)_\delta} \right)^{-1}$$

$$\Gamma\left(-\frac{p}{2} + \beta - \delta\right) = \Gamma\left(-\frac{p}{2} + \beta\right) (\beta - \frac{p}{2})_{-\delta} = \Gamma\left(-\frac{p}{2} + \beta\right) \frac{(-1)^\delta}{(1 - \beta + \frac{p}{2})_\delta}$$

$$\Gamma(-\alpha + \beta - \delta) = \Gamma(\beta - \alpha) \frac{(-1)^\delta}{(1 + \alpha - \beta)_\delta}$$

$$\Gamma(\alpha + \delta) = (\alpha)_\delta \Gamma(\alpha)$$

$$\text{III}_\gamma = \frac{M^{p-2\beta}}{p^{2\alpha}} \frac{\Gamma(\beta - \frac{p}{2}) \Gamma(\beta - \alpha) \Gamma(\alpha)}{\Gamma(\beta - \alpha)} \frac{(\alpha)_\delta \left(\frac{1 - \beta + \alpha}{2}\right)_\delta \left(\frac{\alpha - \beta}{2}\right)_\delta}{(1 - \beta + \frac{p}{2})_\delta (1 + \alpha - \beta)_\delta} \Bigg|_{\delta=0} = \frac{4 M^2}{p^2}$$

converge en $\left| \frac{4 M^2}{p^2} \right| < 1$

esta es posible para $M = 0$

$\text{III}_\gamma = 0$ pero $\frac{p-2\beta}{2} > 0$
condición

solu. ζ libre

(1st)

$$\text{III}_{\zeta} = \sum_{\zeta=0}^{\infty} \frac{M^p}{M^{\alpha} p^{2p}} \left(\frac{M^2}{p^2} \right)^{\zeta} \frac{\Gamma(-\frac{p}{2} + \alpha) \left(\alpha - \frac{p}{2} \right)_{\zeta} \Gamma(\alpha - p) (\alpha - p)_{\zeta} \Gamma(\beta) (\beta)_{\zeta}}{\Gamma(\alpha - \beta) (\alpha - \beta)_{-2\zeta}}$$

$$\left((\alpha - p)_{-2\zeta} \right)^{-1} = 4^{\zeta} \left(\frac{1 - \alpha + \beta}{2} \right)_{\zeta} \left(\frac{\beta - \alpha}{2} \right)_{\zeta} \quad \left| \quad \left(\alpha - \frac{p}{2} \right)_{\zeta} = \frac{(-1)^{\zeta}}{(1 - \alpha + \frac{p}{2})_{\zeta}} \right.$$

$$\left. \quad \quad \quad \left(\alpha - \beta \right)_{-\zeta} = \frac{(-1)^{\zeta}}{(1 - \alpha + \beta)_{\zeta}} \right.$$

$$\text{III}_{\zeta} = \frac{M^{p-\alpha}}{p^{2p}} \Gamma(\alpha - \frac{p}{2}) \Gamma(\beta) F \left(\begin{matrix} . \\ . \end{matrix} \right.$$

$$\left. \begin{matrix} \beta, \left(\frac{1 - \alpha + \beta}{2} \right), \left(\frac{\beta - \alpha}{2} \right) \\ \left(1 - \alpha + \frac{p}{2} \right), (1 - \alpha + \beta) \end{matrix} \right| - \frac{4M^2}{p^2}$$

converge in $\left| \frac{4M^2}{p^2} \right| < 1$

$$1 < \left| \frac{p^2}{4M^2} \right|$$