



scratch ex.v

```
Inductive tm : Type :=
| tm_const : nat -> tm
| tm_plus : tm -> tm -> tm.
```

```
Inductive val : Type :=
| nval : nat -> val
| bval : bool -> val.
```

```
Inductive eval : tm -> val -> Prop :=
| E_Const : forall n,
  eval (tm_const n) (nval n)
| E_Plus : forall t1 t2 n1 n2,
  eval t1 (nval n1) ->
  eval t2 (nval n2) ->
  eval (tm_plus t1 t2) (nval (plus n1 n2)).
```

```
Lemma eval_plus:
forall n, eval (tm_plus (tm_const 1) (tm_const 2)) (nval n) -> n = 3.
```

Proof.

```
intros n e.
```

```
inversion e; subst; clear e.
```

```
inversion H2; subst; clear H2.
```

```
inversion H3; subst; clear H3.
```

```
reflexivity.
```

Qed.

1 subgoals

n1 : nat

n2 : nat

H2 : eval (tm_const 1) (nval n1)

H3 : eval (tm_const 2) (nval n2)

(1/1)

n1 + n2 = 3