# Testing pleiotropy vs. separate QTL in multiparental populations

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## $\sim$ Chapter 1

## Introduction

Genetics studies in model organisms like mice can identify genomic regions that affect complex traits, such as systolic blood pressure and body weight (Sax, 1923; Lander and Botstein, 1989; K. W. Broman and Sen, 198 2009; Jansen, 2007). These genomic regions are called "quantitative trait loci" or "QTL". A genome-wide QTL "scan" reveals associations between genotypes and phenotypes by considering each position, one at 200 a time, as a candidate QTL for the trait of interest. A region with strong evidence of association with a 201 complex trait, then, defines a QTL (for that trait). Because nearby markers have correlated genotypes, a 202 QTL in a two-parent cross often spans multiple megabases in length and may contain more than a hundred 203 genes. Identification of the causal gene (for a given complex trait) from among those genes near the QTL 204 is challenging and may require costly and time-consuming experiments. The growing need for greater QTL 205 mapping resolution fueled development over the last two decades of model organism multiparental popula-206 tions for high-resolution QTL mapping (Koning and McIntyre, 2017; Churchill, Airey, et al., 2004; Svenson 207 et al., 2012; B. E. Huang et al., 2012; Shivakumar et al., 2018; X. Huang et al., 2011; Kover et al., 2009; Tisne et al., 2017; Stanley et al., 2017). With experimentalists now measuring tens of thousands of biomolec-209 ular traits in multiparental populations, the systems genetics community needs multivariate statistical tools 210 to fully examine the large volumes of data (Keller et al., 2018; Chick et al., 2016). Identifying loci that 211 affect multiple traits can aid in identifying biomolecular interactions and in clarifying complex trait genetic 212 architecture. A QTL that affects more than one trait is called a "pleiotropic" QTL. A test of pleiotropy 213 vs. separate QTL is one multivariate statistical tool that will inform complex trait genetics by enabling 214 researchers to identify the number of unique QTL in a genomic region of interest. In this thesis, I develop a test of pleiotropy vs. separate QTL in multiparental populations. I study its statistical properties and

demonstrate its utility by analyzing experimental data. 217

In the first chapter, I introduce statistical methods in QTL mapping studies and argue for the need 218 to develop a pleiotropy test in multiparental populations. Existing pleiotropy tests for two-parent crosses 219 don't directly apply to multiparental populations because of the multi-allelic genotype data and complex relatedness patterns. A pleiotropy test for multiparental populations with high-dimensional traits would 221 enable dissection of QTL hotspots (i.e., small genomic regions that affect many traits) and would complement 222 newly developed methods in causal inference for systems genetics. 223

I begin Chapter 1 by motivating the study of pleiotropy with a case study of the pleiotropic Agouti gene. 224 I then consider two-parent crosses, with emphases on experimental design, QTL mapping methods, and 225 pleiotropy testing. I then turn to multiparental populations, where I describe experimental design and QTL mapping methods. I conclude Chapter 1 by reiterating the need to develop a test of pleiotropy vs. separate QTL in multiparental populations. 228

#### Agouti biology & pleiotropy 1.1

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Pleiotropy is the biological phenomenon in which a gene affects multiple traits. Identifying a gene that affects 230 multiple traits may inform scientific understanding of interactions between biomolecules and ultimately contribute insights that aid development of new therapeutics. For example, mouse studies identified multiple 232 biological roles for the protein product of the Agouti gene. Mutations in the Agouti gene may lead to both 233 yellow hair (in mice that are typically black) and obesity (Attie, Churchill, and Nadeau, 2017). Subsequent 234 investigations uncovered two related biological roles for the Agouti protein. It antagonizes the action of 235  $\alpha$ -melanocyte-stimulating hormone both to prevent melanocyte-based melanin production and to disrupt melanocortin-4 receptor signaling in the brain (D. Lu et al., 1994; Klebig et al., 1995; Huszar et al., 1997). 237 The former leads to yellow hair, while the latter causes weight gain. Later research identified altered signaling by the melanocortin-4 receptor in the brain as a leading cause of inherited obesity in humans (Faroogi et 239 al., 2003; Vaisse et al., 2000). Therapeutics to mitigate the effects of disruptions in melanocortin receptor signaling are currently being developed (MacNeil et al., 2002; Fani et al., 2014). The case of pleiotropic 241 Agouti variants illustrates the potential value of examining pleiotropy in QTL studies. We next consider 242 designs and QTL mapping in two-parent crosses (Sections 1.2 and 1.3). 243



Figure 1.1: Agouti viable-yellow mutant mouse has yellow hair and is obese in comparison to a wild-type mouse. (https://upload.wikimedia.org/wikipedia/commons/4/4d/Agouti\_Mice.jpg)

### 1.2 Designs for two-parent crosses

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Two widely used two-parent crosses are the "backcross" and the "intercross". We first discuss the backcross design (Figure 1.2). A backcross starts with mating between members of two inbred lines. The offspring of this mating event, termed the "F<sub>1</sub>", or "first filial", generation then mate with members of one of the two parent lines. The experiment designers decide which line (A or B) mates with F<sub>1</sub> subjects with. The F<sub>1</sub> subjects mate with the specified founder line (A in Figure 1.2) to create generation "BC" subjects. Generation BC subjects are then genotyped and phenotyped for QTL mapping.

As Figure 1.2 illustrates, all backcross animals (generation BC) have, for any locus, only two possible genotypes: heterozygote (AB) and homozygote (AA). The  $F_1$  generation is heterozygous at all loci (Figure 1.2) because they inherited one chromosome (of each pair) from each parent. The meiotic crossovers that occur as the  $F_1$  animals produce gametes result in "BC" generation animals that have individual chromosomes that contain DNA from both founder lines.

I now consider the intercross design (Figure 1.3). An intercross differs from a backcross design by mating  $F_1$  subjects with each other, rather than with a parent line (as in a backcross). Because  $F_1$  subjects produce gametes with detectable crossovers, the  $F_2$  generation animals have, for every marker, three genotype classes:

AA, AB, and BB. Compare this with the backcross, where BC subjects have only two genotype classes (AA)



Figure 1.2: Breeding scheme for a backcross. Each pair of autosomes represents a single subject. (From K. W. Broman and Sen (2009))

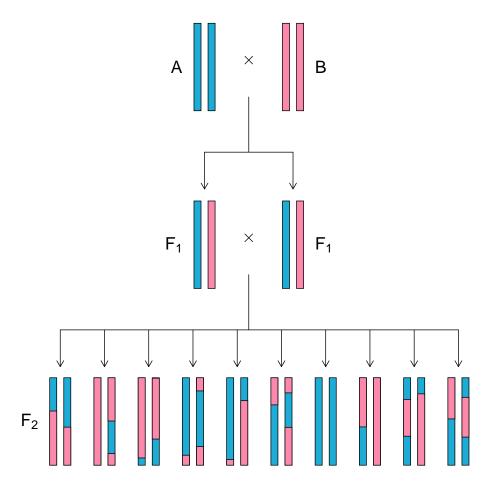


Figure 1.3: Breeding scheme for an intercross. Each pair of autosomes represents a single subject. (From K. W. Broman and Sen (2009))

260 and AB in Figure 1.2).

In an intercross, phenotyping and genotyping are typically done in only the F<sub>2</sub> subjects. As with a
backcross, intercross planning may involve genotyping and phenotyping of subjects from two (or more)
inbred lines. The designers then have the option of choosing as founders two inbred lines that demonstrate
a big difference in mean phenotype values (for traits of interest). Now that I've considered two widely used
two-parent designs, I discuss QTL mapping methods for two-parent designs.

## $_{ iny 66}$ 1.3 ${ m QTL}$ mapping in two-parent crosses

#### $_{57}$ 1.3.1 Overview

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QTL mapping is a systematic, statistical approach for identifying genetic loci where genetic variation affects
variation in a measured trait. A variety of statistical methods for QTL mapping exist. I discuss below three
QTL mapping methods: marker regression (Section 1.3.2), interval mapping (Section 1.3.3), and Haley-Knott
regression (Section 1.3.4). I consider the three methods in analysis of a backcross design. Before getting to
the details of our three QTL mapping methods, I discuss data inputs that are required for QTL mapping,
assuming at most one QTL somewhere in the genome.

Three standard inputs for QTL mapping are:

- 1. genome-wide marker genotypes for a collection of study subjects
- 2. a set of trait measurements on the same subjects
- 3. a genetic map that contains genomic positions for all molecular markers (Figure 1.4) (Sturtevant, 1913)

A physical map, with marker positions in units of megabases, may also be used. Additional inputs include genotype data (for the same set of markers) from founder lines, *i.e.*, the inbred lines that initiate the mating design. For example, in Figures 1.2 and 1.3 there are two founder lines at the top of the mating design, those with genotypes AA and those with genotypes BB.

Figure 1.4 depicts the positions of markers (horizontal hash marks) on each chromosome (vertical lines). 282 In practice, for QTL mapping, a genetic map object may be stored as a collection of two-column data frames, 283 where each row is a unique marker and the two columns contain marker identities and marker positions. 284 In this structure, each chromosome has its own map object. Marker distribution is not uniform across the 285 genome (Figure 1.4). Some chromosome regions in Figure 1.4, including parts of Chromosome 4, have dense marker coverage, while others, including Chromosome 2, have relatively sparse marker coverage. Dense 287 marker coverage is preferred in QTL mapping applications because it provides more genetic information and enables more accurate genotype inference between markers. Before the recent development of high-density single nucleotide polymorphism marker arrays, many studies relied on sparse microsatellite and restriction fragment length polymorphism markers. 291

A univariate QTL scan is a procedure to interrogate the entire genome for genetic variants that affect a single trait of interest. One assesses genotype-phenotype associations by considering each location, one at a time. Those loci for which the evidence for a QTL is sufficiently strong are declared QTL.



Figure 1.4: Genetic map for markers from Sugiyama et al. (2001). Figure from K. W. Broman and Sen (2009).

In QTL mapping, two major statistical challenges are what K. W. Broman and Sen (2009) call the "missing data" problem and the "model selection" problem. The "missing data" problem arises in QTL studies because genotypes are obtained at only select markers. In this sense, genotypes at positions between markers are "missing" because they aren't explicitly measured (Figure 1.5). Figure 1.5 presents, for one subject, a chromosome with genotyped markers at the tick marks. The triangle represents a position at which we wish to know the allele's identity. In Section 1.3.3, we discuss methods for genotype inference at positions between markers.

The three statistical methods for QTL mapping, marker regression, interval mapping, and Haley-Knott

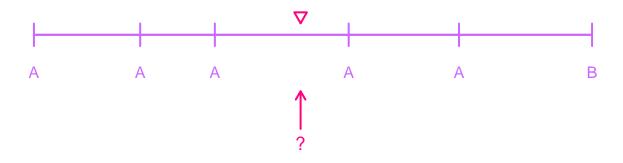


Figure 1.5: Inferring genotypes at an intermarker position (from K. W. Broman and Sen (2009))

regression, differ in strategies for addressing the "missing data" problem. I first discuss marker regression,
because it is the simplest approach and because the other methods share some aspects of it.

### 1.3.2 Marker regression

Marker regression inputs are genome-wide marker genotypes and measured values of a complex trait of interest (from the same subjects). At each marker, one fits a linear model by regressing trait values on marker genotypes (Equation 1.1), sequentially, at each marker. In a backcross, the "B allele count" variable, also denotes  $x_i$ , where i indexes the subjects, takes values of 0 or 1. In an intercross, the "B allele count" may be 0, 1, or 2. Both backcross and intercross designs permit solution of the regression by a statistical technique called "maximum likelihood estimation". I assume that the random errors for all subjects have a normal distribution with mean zero and variance  $\sigma^2$  and are statistically independent. Statistical independence means that knowing the value of one subject's random error provides no information about the distribution of another subject's random error.

rait = (mean for AA genotype) + (B allele count)(B allele effect) + (random error)
$$y_i = \mu_{AA} + x_i \beta + \epsilon_i \tag{1.1}$$

$$\epsilon_i \sim N(0, \sigma^2), \qquad \epsilon_i \text{ independent}$$
 (1.2)

Equation 1.2 specifies the random error distribution. Equation 1.2 also introduces notation that requires 315 explanation. The "~" symbol designates a probability distribution. The left-hand side "is distributed as" the 316 right-hand side. In this case, I describe the distribution of the random errors. Capital "N", in a distribution, 317 abbreviates "Normal". The first number after the "N" is the distribution mean, while the second is the 318 variance. These two numbers, mean and variance, completely specify a normal distribution. Equation 1.9 319 gives a mathematical definition of the normal probability density. The linear regression equation (Equation 1.1) has three statistical parameters, "mean for AA genotype" 321  $(\mu_{AA})$ , "B allele effect" ( $\beta$ ), and the variance ( $\sigma^2$ ) of the random errors. In this statistical framework, I treat parameters as fixed, but unknown, numbers. I then seek the parameter values that are most compatible 323 with the data. To do this, I use the approach called "maximum likelihood estimation".

The maximum likelihood estimates for two parameters, "B allele effect" and the random error variance, are given in Equations 1.3 and 1.4. Note that I've replaced "B allele effect" with the Greek letter  $\beta$ , while  $\sigma^2$ denotes the random error variance. The "hat" above  $\beta$  indicates that  $\hat{\beta}$  is a maximum likelihood estimate of the parameter  $\beta$  (*i.e.*, the unknown "B allele effect").

$$\hat{\beta} = \frac{\sum_{i=1}^{n} (x_i - \bar{x}) y_i}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$
(1.3)

$$\hat{\sigma}^2 = \frac{RSS_1}{n} \tag{1.4}$$

The residual sum of squares "RSS<sub>1</sub>", which is central to the calculation of the pooled variance estimate  $\hat{\sigma}^2$  in Equation 1.4, is an expression that tells us how far the observed trait measurements are from the predicted values, for a set of specified parameter values. Equation 1.6 defines residual sum of squares for a univariate QTL analysis. I make an additional substitution in Equation 1.6 by replacing "B allele count" with  $x_i$ , where "i" indexes subjects. In Equation 1.6, I introduce  $\hat{\mu}_{g_i}$  as an estimate of the parameter  $\mu_{g_i}$ .  $\mu_{g_i}$  is the mean trait value of the genotype class to which subject i belongs. If subject i has genotype AA, then  $\mu_{g_i} = \mu_{AA}$ . I estimate  $\mu_{g_i}$  with Equation 1.5

$$\hat{\mu}_g = \frac{\sum_{i=1}^n y_i \mathbb{1} g_i = g}{n_g} \tag{1.5}$$

In Equation 1.5, g is any of AA, AB, or BB.  $\mathbb{1}g_i = g$  takes values 0 and 1; if  $g_i = g$ , then  $\mathbb{1}g_i = g = 1$ ; otherwise, it's zero.  $n_g$  is the number of subjects with  $g_i = g$ .

$$RSS_1 = \sum_{i=1}^{n} (y_i - \hat{\mu}_{g_i})^2 \tag{1.6}$$

We ultimately want to calculate a likelihood ratio test statistic for the competing statistical hypotheses of Equation 1.7.

 $H_1$ : A QTL is present at a specified marker

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$$H_0$$
: No QTL is present in the genome (1.7)

I wish to calculate the likelihood for both the alternative hypothesis and the null hypothesis. I write the

likelihood as a product of per-subject likelihoods in Equation 1.8.

$$L_1(\mu_{AA}, \beta, \sigma^2) = P(\text{data}|\text{QTL at marker}, \mu_{AA}, \beta, \sigma^2) = \prod_{i=1}^n \phi(y_i; \mu_{g_i}, \sigma^2)$$
(1.8)

I introduce new notation in Equation 1.8.  $L_1$  denotes the likelihood under hypothesis  $H_1$ , where a QTL is present. The likelihood of the model parameters is equal, by definition, to the joint probability of the data conditional on presence of a QTL and the parameter values. This, by the assumption of statistical independence of subjects, is equal to the product of the n per-subject likelihoods, where  $\phi(y; \mu, \sigma^2)$  denotes the density at y for a normal distribution with mean  $\mu$  and variance  $\sigma^2$  (Equation 1.9).

$$\phi(y; \mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(y-\mu)^2}{2\sigma^2}\right)$$
 (1.9)

I also need to calculate the maximum likelihood under the null model constraints, *i.e.*, under the assumption that there is no QTL in the genome, in which case the genotype classes have the same mean trait value.

$$L_0(\mu_0, \sigma_0^2) = P(\text{data}|\mu_0, \sigma_0^2) = \prod_{i=1}^n \phi_i(y_i; \mu_0, \sigma_0^2)$$
(1.10)

After calculating the likelihood ratio test statistic at every marker, one needs to obtain p-values for every 350 test. Because a researcher performs many tests (i.e., one per marker) in a genome-wide QTL scan, one needs 351 to account for multiple testing. One way to do this is to perform a permutation test to determine adjusted 352 p-values. In this permutation test, one shuffles or randomizes subjects' trait values to get a "permuted 353 phenotype". One does this many times to obtain, say, 1000 permuted phenotypes. Each permuted phenotype is then analyzed with a univariate QTL scan. The statistician records, for each permuted phenotype, the 355 maximum observed LOD score from the genome-wide scan to obtain an empirical distribution of "max LOD 356 score" statistics. One then determines the  $95^{th}$  percentile of this empirical distribution and uses it as a 357 critical value when assessing statistical significance of observed peaks. 358

### 359 1.3.3 Interval mapping

I highlight elements from the exposition of interval mapping in K. W. Broman and Sen (2009). More details are available in its Chapter 4. Lander and Botstein (1989) describe interval mapping for QTL studies. While marker regression considers only marker positions as candidate QTL, in interval mapping one probabilistically

Table 1.1: Probabilities for genotypes at intermediate putative QTL in a backcross, conditional on flanking marker genotypes.

Marker 1 genotype	Marker 2 genotype	P(AA)	P(AB)
AA	AA	$\frac{(1-r_{1Q})(1-r_{Q2})}{1-r_{12}}$	$\frac{r_{1Q}r_{Q2}}{(1-r_{12})}$
AA	AB	$\frac{(1-r_{1Q})r_{Q2}}{r_{12}}$	$\frac{r_{1Q}(1-r_{Q2})}{r_{12}}$
AB	AA	$\frac{r_{1Q}(1-r_{Q2})}{r_{12}}$	$\frac{(1-r_{1Q})r_{Q2}}{r_{12}}$
AB	AB	$\frac{r_{1Q}r_{Q2}}{(1-r_{12})}$	$\frac{(1-r_{1Q})(1-r_{Q2})}{(1-r_{12})}$

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infers genotypes for all positions on a grid along each chromosome. One leverages the entire collection of 363 marker genotypes on each chromosome and their correlations to do this.

To illustrate this approach, consider a backcross sample with two adjacent markers. I suppose that the backcross follows the design in Figure 1.2, with generation BC subjects having either AA or AB genotypes. I wish to know the genotype probabilities at an intermediate point, i.e., the putative QTL, between the two markers. Calling the markers "marker 1" and "marker 2", suppose that the recombination fraction between marker 1 and marker 2 is  $r_{12}$ . Assume that all subjects are genotyped at markers 1 and 2. With two additional assumptions, that of no crossover interference (i.e., recombinations are assumed independent) and that of no genotyping errors, I can write expressions for genotype probabilities at the putative QTL, conditional on the genotypes at markers 1 and 2 (Table 1.1).

In Table 1.1, I present genotype probabilities for a putative QTL, denoted "Q", between marker 1 and marker 2, in a backcross (Figure 1.2).  $r_{12}$  is the recombination probability between marker 1 and marker 2, 374  $r_{1Q}$  is the recombination probability between marker 1 and putative QTL Q, and  $r_{Q2}$  is the recombination probability between putative QTL Q and marker 2. Each row in the table represents an ordered pair of 376 genotypes for markers 1 and 2. Since I'm considering a backcross, each marker has one of two possible 377 genotypes, so only four rows are needed. The first two columns list the genotypes at the two genotyped 378 markers. The third and fourth columns contain the putative QTL's genotype probabilities. Note that these 379 are conditional probabilities, where the conditioning is done on the marker genotypes. To calculate these values, recall the relationship between joint and conditional probabilities (Equation 1.11). Application of 381 this relationship yields the probabilities in Table 1.1. A more general solution for these calculations can be 382 implemented with algorithms for hidden Markov models (K. W. Broman and Sen, 2009; K. W. Broman, 383 2006).

$$\frac{P(g_1 = AA, g_2 = AA, g_Q = AA)}{P(g_1 = AA, g_2 = AA)} = P(g_Q = AA|g_1 = AA, g_2 = AA)$$
(1.11)

In interval mapping, trait values are modeled statistically as having a distribution that is a mixture of normal distributions, where each component in the mixture corresponds to a genotype class. I assume a single variance common to all components (at a single putative QTL). In a backcross, there are thus two normal distribution components for each grid point, *i.e.*, each putative QTL. Fitting such a model by maximum likelihood requires an iterative procedure like the expectation-maximization algorithm (Dempster, Laird, and Rubin, 1977). Performing the iterative procedure is required at every putative QTL position. Thus, it is more computationally intensive than other approaches, such as Haley-Knott regression, to which I now turn attention.

### $_{_{393}}$ 1.3.4 Haley-Knott regression

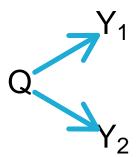
A computationally simpler approach that yields results similar to those of interval mapping is "Haley-Knott" regression (Haley and Sarah A Knott, 1992; Martinez and Curnow, 1992). In Haley-Knott regression, one first infers genotype probabilities along a grid of putative QTL positions. As mentioned above, algorithms for hidden Markov models provide a flexible framework for this task (K. W. Broman, 2006; K. W. Broman and Sen, 2009). At each grid point, then, one regresses the trait values on the genotype probabilities, much like the marker regression method (Section 1.3.2). In contrast to interval mapping, Haley-Knott regression doesn't require an iterative method. Haley-Knott regression treats the distribution of trait values, conditional on genome-wide marker data, as arising from a single normal distribution (Equation 1.12).

$$y_i|M_i \sim N(\sum_j p_{ij}\mu_j, \sigma^2) \tag{1.12}$$

In Equation 1.12, "j" indexes the genotype classes, while "i" indexes the subjects.  $p_{ij}$  is the probability that subject "i" belongs to genotype class "j", while  $\mu_j$  is the mean trait value for genotype class "j". While Haley-Knott regression may be insufficient when marker data is sparse, it performs well (compared to interval mapping) with dense marker data when all subjects are successfully genotyped. Having completed the discussion of Haley-Knott regression, I now consider pleiotropy testing in two-parent crosses.

### 1.4 Testing pleiotropy in two-parent crosses

In anticipation that multivariate mapping of correlated traits would enhance statistical power to detect QTL and would improve precision of QTL position estimates, both Jiang and Zeng (1995) and Korol, Ronin,



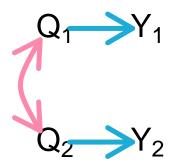


Figure 1.6: One pleiotropic QTL affecting two traits (left) and two distinct, but correlated, QTL each affecting one trait (right). Figure after code from https://github.com/kbroman/QTLFigs repository.

and Kirzhner (1995) developed multivariate interval mapping procedures for two-parent crosses. Among the novel methods from Jiang and Zeng (1995) is a test of pleiotropy vs. separate QTL. Such a test is useful when two traits map to a single genomic region. The question then arises "do the two traits associate with the same locus, or do they associate with separate loci"?

If both traits associate with the same locus, then that locus is called "pleiotropic". Figure 1.6 provides schematics for the two possibilities. On the left side of Figure 1.6, a single QTL (denoted by Q) affects both traits. On the right side of Figure 1.6 two distinct QTL ( $Q_1$  and  $Q_2$ ) affect one trait each. The pink arrows indicate that  $Q_1$  and  $Q_2$  are on the same chromosome and are correlated by linkage disequilibrium.

Figure 1.7 illustrates a small two-dimensional, two-QTL scan. Each point in the grid corresponds to an ordered pair of markers. Along the horizontal axis are the markers for the first component of the ordered pair; the second component of the ordered pair is indicated by the vertical axis. The red points correspond to those that are considered under the pleiotropy hypothesis. Under the alternative hypothesis, all grid points are considered.

Jiang and Zeng (1995) then calculate the likelihoods of the models corresponding to all grid points. The likelihood ratio test statistic (for the pleiotropy test) is the ratio of the maximum of the likelihoods under pleiotropy to the maximum of the likelihoods under the separate QTL hypothesis. Jiang and Zeng (1995) determined p-values for their test statistics by comparing them, after logarithm transformation and



Figure 1.7: Two-dimensional grid of ordered pairs of markers.

multiplication by two, to a chi-squared distribution with 1 degree of freedom. I continue this discussion in
Section 2.2.

### 1.5 Designs for Collaborative Cross and Diversity Outbred mice

Recognizing limitations of two-parent designs, geneticists sought populations with greater QTL mapping precision. And, rather than designing a high-resolution mapping resource for only one or few traits or 431 diseases, they aimed to develop a mapping population for study of a diverse collection of complex traits. 432 Since this required a collaborative, research community-supported investment, mammalian geneticists formed the Complex Trait Consortium to create a high-resolution mouse mapping population, the Collaborative 434 Cross (Koning and McIntyre, 2014; Threadgill, Hunter, and Williams, 2002; Churchill, Airey, et al., 2004; Threadgill and Churchill, 2012). 436 The Collaborative Cross is a collection of eight-way recombinant inbred lines for systems genetics studies (Figure 1.8). A "n-way recombinant inbred" line is an inbred line that arises from a mating design with n438 genetically distinct founder lines (Bailey, 1971; Crow, 2007). The Collaborative Cross incorporates DNA from eight inbred founder lines: A/J, C57BL/6J, 129S1/SvImJ, NOD/ShiLtJ, NZO/HILtJ, CAST/EiJ, 440 PWK/PhJ, WSB/EiJ. The designers of the Collaborative Cross used a "multi-funnel" mating scheme to generate mice with DNA from all eight founder lines over the course of 3 generations (Churchill, Airey, 442 et al., 2004). The term "funnel" refers to the design for the first three mating generations in which the DNA from eight founder lines "funnels" into animals that have DNA from all eight founders. For example, in one 444 funnel, mating pairs are: A x B, C x D, E x F, and G x H in the first generation (Figure 1.8) (where "x" 445 denotes mating). AB offspring then mate with CD offspring, and EF offspring mate with GH mice. Finally, the ABCD mice mate with the EFGH mice to create a generation of mice that contain genetic material from 447 all eight inbred founder lines. Subsequent generations of inbreeding resulted in multiple inbred lines for the Collaborative Cross. 449 The designers of the Diversity Outbred population started with 167 breeding pairs from Collaborative Cross generations  $F_4$  to  $F_{12}$  (Svenson et al., 2012). They since have maintained the Diversity Outbred 451 mouse population with about 175 mating pairs. They produce three or four generations per year. Offspring 452 from each mating are either used to create the next generation or shared with researchers around the world (Svenson et al., 2012; Chesler et al., 2016). 454

Due to the breeding scheme, each Diversity Outbred mouse is a highly heterozygous and essentially

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Figure 1.8: Schematic for a single funnel in the Collaborative Cross breeding design. Figure is created with R code from https://github.com/kbroman/QTLFigs repository.

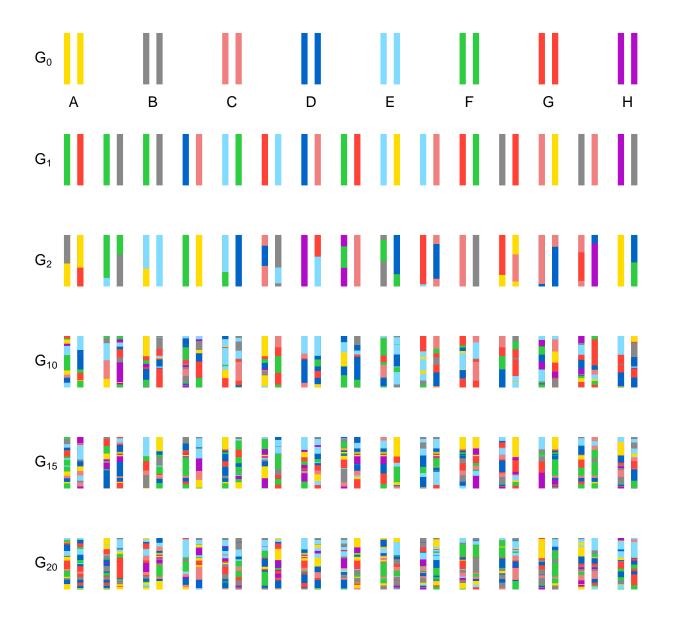


Figure 1.9: Diversity outbred mouse genomes are a highly heterozygous mixture of eight founder genomes. (R code to create figure from https://github.com/kbroman/QTLFigs repository.)

unique mosaic of founders' DNA. Figure 1.9 presents color-coded chromosomes for a collection of subjects from a multiparental population like the Diversity Outbred mice. DNA from each founder line is color-coded. Each pair of vertical bars corresponds to one subject. Each row corresponds to a single generation, with generation labels on the left. Generation number increases from top to bottom. With each new generation, the Diversity Outbred mouse genomes are shuffled in smaller and smaller chunks. The smaller DNA chunk sizes in later generations correspond to greater QTL mapping resolution.

### 1.6 QTL mapping in Diversity Outbred mice

QTL mapping in Diversity Outbred mice, like that in mice from two-parent crosses, is a multi-step procedure:

1. data acquisition, 2. inference of missing genotypes, and 3. modeling phenotypes as a function of genotypes.

Data acquisition involves measurement of phenotypes and, at specified genetic markers, termed "single nucleotide polymorphism" or SNP markers, measurement of two-allele genotypes. Often, the SNP marker genotypes are obtained by use of a microarray, such as the GigaMUGA SNP microarray (Morgan et al., 2015).

The next step, missing genotypes inference, is needed because of the "missing data problem" (K. W. Broman and Sen, 2009). It takes as input the two-allele genotypes at the measured SNP markers. An expectation-maximization algorithm (Dempster, Laird, and Rubin, 1977) for a hidden Markov model, de-

expectation-maximization algorithm (Dempster, Laird, and Rubin, 1977) for a hidden Markov model, developed by K. W. Broman (2012b) and K. W. Broman (2012a) and implemented in the qt12 R package (K. W. Broman, D. M. Gatti, et al., 2019), outputs 36-state genotype probabilities for all nuclear autosomal markers and pseudomarkers. The outputted genotypes have 36 states because each position has eight homozygote states (one for each founder line) and (<sup>8</sup>/<sub>2</sub>) heterozygote states. Pseudomarkers are arbitrary positions at which the researcher wants 36-state genotype probabilities. Finally, we collapse the 36-state genotype probabilities to eight founder allele dosages at each marker. This last step is optional, but often helpful, because the simplified models require specification of fewer parameters. We then treat the founder allele dosages as known quantities in subsequent steps.

After inferring founder allele dosages, we address the second major statistical challenge of QTL mapping:
the "model selection" problem (K. W. Broman and Sen, 2009). A genetically "additive" linear model, in
which we assume a linear relationship between a trait's values and each founder allele's dosage, is a popular
default model. (Daniel M Gatti et al., 2014; K. W. Broman, D. M. Gatti, et al., 2019).

Due to the complexity of the breeding design, Diversity Outbred mice have complicated pairwise relation-

ships. A given study cohort may include pairs of first cousins, parent-offspring pairs, grandparent-grandchild pairs, second cousin pairs, and others. Because relatedness can confound genotype-phenotype associations (J. Yang et al., 2014), researchers have developed methods to account for relatedness in their statistical models. One popular approach involves use of a polygenic random effect in the statistical model (Kang, Zaitlen, et al., 2008). The inclusion of a random effect to a model with fixed (*i.e.*, nonrandom) effects results in what statisticians call a "linear mixed effects model".

# 1.7 Potential benefits of a pleiotropy test in multiparental populations

The complex traits genetics community needs a pleiotropy test for multiparental populations. Having such a test, when experimentalists are measuring tens of thousands of traits on subjects from multiparental populations, would enable our community to address new and interesting biological questions. For example, we can dissect an expression trait QTL hotspot by asking how many separate QTL are present within the hotspot. Additionally, we can inform experimental validation studies by addressing whether a pair of putatively related traits share a pleiotropic QTL.

I present in Chapter 2 a pleiotropy test for multiparental populations. I discuss in detail our statistical methods before studying the test's statistical properties, including type I error rate and power. I then apply 500 the test to data from Diversity Outbred mice. In Chapter 3, I study the test through three vignettes. I first examine its contributions relative to mediation analysis in the dissection of expression QTL hotspots. I 502 then examine statistical power to distinguish local expression trait QTLs. I conclude Chapter 3 by applying 503 the pleiotropy test to two microbiome-related traits, where we obtain a result consistent with a pleiotropic 504 QTL that affects both traits. Chapter 4 presents the R software package qtl2pleio, which is available on 505 Github (https://github.com/fboehm/qtl2pleio, https://fboehm.us/static/software/qtl2pleio/). The Github repository also features integration with the Binder software project. With this, a user may explore the code 507 in an online, interactive R session.

## • Chapter 2

# Testing pleiotropy vs. separate QTL

# in multiparental populations

### 512 2.1 Introduction

<sup>1</sup>Complex trait studies in multiparental populations present new challenges in statistical methods and data analysis. Among these is the development of strategies for multivariate trait analysis. The joint analysis of two or more traits allows one to address additional questions, such as whether two traits share a single pleiotropic locus.

Previous research addressed the question of pleiotropy vs. separate QTL in two-parent crosses. Jiang and Zeng (1995) developed a likelihood ratio test for pleiotropy vs. separate QTL for a pair of traits. Their approach assumed that each trait was affected by a single QTL. Under the null hypothesis, the two traits were affected by a common QTL, and under the alternative hypothesis the two traits were affected by distinct QTL. Sara A Knott and Haley (2000) used linear regression to develop a fast approximation to the test of Jiang and Zeng (1995), while Tian et al. (2016) used the methods from Sara A Knott and Haley (2000) to dissect QTL hotspots in a F<sub>2</sub> population.

Multiparental populations, such as the Diversity Outbred (DO) mouse population (Churchill, Daniel M Gatti, et al., 2012), enable high-precision mapping of complex traits (Koning and McIntyre, 2014). The DO mouse population began with progenitors of the Collaborative Cross (CC) mice (Churchill, Airey, et al.,

<sup>&</sup>lt;sup>1</sup>Published at https://www.biorxiv.org/content/10.1101/550939v1.

2004) Each DO mouse is a highly heterozygous genetic mosaic of alleles from the eight CC founder lines. 527 Random matings among non-siblings have maintained the DO population for more than 23 generations 528 (Chesler et al., 2016). 529

Several limitations of previous pleiotropy vs. separate QTL tests prevent their direct application in multiparental populations. First, multiparental populations can have complex patterns of relatedness among 531 subjects, and failure to account for these patterns of relatedness may lead to spurious results (J. Yang et al., 2014). Second, previous tests allowed for only two founder lines (Jiang and Zeng, 1995). Finally, Jiang and 533 Zeng (1995) assumed that the null distribution of the test statistic follows a chi-square distribution.

We developed a pleiotropy vs. separate QTL test for two traits in multiparental populations. Our test 535 builds on research that Jiang and Zeng (1995), Sara A Knott and Haley (2000), Tian et al. (2016), and Zhou and Stephens (2014) initiated. Our innovations include the accommodation of k founder alleles per locus 537 (compared to the traditional two founder alleles per locus) and the incorporation of multivariate polygenic 538 random effects to account for relatedness. Furthermore, we implemented a parametric bootstrap to calibrate test statistic values (Efron, 1979; Tian et al., 2016). 540

Below, we describe our likelihood ratio test for pleiotropy vs. separate QTL. In simulation studies, we find that it is slightly conservative, and that it has power to detect two separate loci when the univariate 542 LOD peaks are strong. We further illustrate our approach with an application to data on a pair of behavior traits in a population of 261 DO mice (Logan et al., 2013; Recla et al., 2014). We find modest evidence for distinct QTL in a 2.5-cM region on mouse Chromosome 8.

#### 2.2Methods

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Our strategy involves first identifying two traits that map to a common genomic region. We then perform 547 a two-dimensional, two-QTL scan over the genomic region, with each trait affected by one QTL of varying position. We identify the QTL position that maximizes the likelihood under pleiotropy (that is, along the 549 diagonal where the two QTL are at a common location), and the ordered pair of positions that maximizes the likelihood under the model where the two QTL are allowed to be distinct. The logarithm of the ratio of 551 the two likelihoods is our test statistic. We calibrate this test statistic with a parametric bootstrap.

#### 553 2.2.1 Data structures

The data consist of three objects. The first is an n by k by m array of allele probabilities for n subjects with k alleles and m marker positions on a single chromosome [derived from the observed SNP genotype data by a hidden Markov model; see K. W. Broman, D. M. Gatti, et al. (2019)]. The second object is an n by n matrix of phenotype values. Each column is a phenotype and each row is a subject. The third object is an n by n by n0 matrix of covariates, where each row is a subject and each column is a covariate.

One additional object is the genotype-derived kinship matrix, which is used in the linear mixed model to account for population structure. We are focusing on a defined genomic interval, and we prefer to use a kinship matrix derived by the "leave one chromosome out" (LOCO) method (J. Yang et al., 2014), in which the kinship matrix is derived from the genotypes for all chromosomes except the chromosome under test.

#### 563 2.2.2 Statistical Models

Focusing on a pair of traits and a particular genomic region of interest, the next step is a two-dimensional, two-QTL scan (Jiang and Zeng, 1995). We consider two QTL with each affecting a different trait, and consider all possible pairs of locations for the two QTL. For each pair of positions, we fit the multivariate linear mixed effects model defined in Equation 2.1. Note that we have assumed an additive genetic model throughout our analyses, but extensions to design matrices that include dominance are straightforward.

$$vec(Y) = Xvec(B) + vec(G) + vec(E)$$
(2.1)

where Y is the n by 2 matrix of phenotypes values; X is a 2n by 2(k+c) matrix that contains the k allele probabilities for the two QTL positions and the c covariates in diagonal blocks; B is a (k+c) by 2 matrix of allele effects and covariate effects; G is a n by 2 matrix of random effects; and E is a n by 2 matrix of random errors. n is the number of mice. The 'vec' operator stacks columns from a matrix into a single vector. For example, a 2 by 2 matrix inputted to 'vec' results in a vector with length 4. Its first two entries are the matrix's first column, while the third and fourth entries are the matrix's second column.

We also impose distributional assumptions on G and E:

$$G \sim MN_{nx2}(0, K, V_g) \tag{2.2}$$

and

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$$E \sim MN_{nx2}(0, I, V_e) \tag{2.3}$$

where  $MN_{nx2}(0, V_r, V_c)$  denotes the matrix-variate (n by 2) normal distribution with mean being the n by2 matrix with all zero entries and row covariance  $V_r$  and column covariance  $V_c$ . We assume that G and Eare independent.

### <sup>580</sup> 2.2.3 Parameter inference and log likelihood calculation

Inference for parameters in multivariate linear mixed effects models is notoriously difficult and can be computationally intense (K. Meyer, 1989; K. Meyer, 1991). Thus, we estimate  $V_g$  and  $V_e$  under the null hypothesis of no QTL, and then take them as fixed and known in our two-dimensional, two-QTL genome scan. We use restricted maximum likelihood methods to fit the model:

$$vec(Y) = X_0 vec(B) + vec(G) + vec(E)$$
(2.4)

where  $X_0$  is a 2n by 2(c+1) matrix whose first column of each diagonal block in  $X_0$  has all entries equal to one (for an intercept); the remaining columns are the covariates.

We draw on our R implementation (Boehm, 2018a) of the GEMMA algorithm for fitting a multivariate linear mixed effects model with expectation-maximization (Zhou and Stephens, 2014). We use restricted maximum likelihood fits for the variance components  $V_g$  and  $V_e$  in subsequent calculations of the generalized least squares solution  $\hat{B}$ .

$$\hat{B} = (X^T \hat{\Sigma}^{-1} X)^{-1} X^T \hat{\Sigma}^{-1} vec(Y)$$
(2.5)

591 where

$$\hat{\Sigma} = \hat{V}_g \otimes K + \hat{V}_e \otimes I_n \tag{2.6}$$

where  $\otimes$  denotes the Kronecker product, K is the kinship matrix, and  $I_n$  is a n by n identity matrix. We then calculate the log likelihood for a normal distribution with mean  $Xvec(\hat{B})$  and covariance  $\hat{\Sigma}$  that depends on our estimates of  $V_g$  and  $V_e$  (Equation 2.6).

### <sup>595</sup> 2.2.4 Pleiotropy vs. separate QTL hypothesis testing framework

Our test applies to two traits considered simultaneously. Below,  $\lambda_1$  and  $\lambda_2$  denote putative locus positions for traits one and two. We quantitatively state the competing hypotheses for our test as:

$$H_0: \lambda_1 = \lambda_2$$

$$H_A: \lambda_1 \neq \lambda_2 \tag{2.7}$$

Our likelihood ratio test statistic is:

$$LOD = \log_{10} \left[ \frac{\max_{\lambda_1, \lambda_2} L(B, \Sigma, \lambda_1, \lambda_2)}{\max_{\lambda} L(B, \Sigma, \lambda, \lambda)} \right]$$
(2.8)

where L is the likelihood for fixed QTL positions, maximized over all other parameters.

### <sub>600</sub> 2.2.5 Visualizing profile LOD traces

The output of the above analysis is a two-dimensional log<sub>10</sub> likelihood surface. To visualize these results, we followed an innovation of Zeng et al. (2000) and Tian et al. (2016), and plot three traces: the results along the diagonal (corresponding to the null hypothesis of pleiotropy), and then the profiles derived by fixing one QTL's position and maximizing over the other QTL's position.

We define the LOD score for our test:

$$LOD(\lambda_1, \lambda_2) = ll_{10}(\lambda_1, \lambda_2) - \max ll_{10}(\lambda, \lambda)$$
(2.9)

where  $ll_{10}$  denotes  $log_{10}$  likelihood.

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We follow Zeng et al. (2000) and Tian et al. (2016) in defining profile LOD by the equation

profile 
$$LOD_1(\lambda_1) = \max_{\lambda_2} LOD(\lambda_1, \lambda_2)$$
 (2.10)

We define profile  $LOD_2(\lambda_2)$  analogously. The maximum value for the profile  $LOD_1$  profile  $LOD_2$  traces are
the same and are non-negative, and give the overall LOD test statistic.

We construct the pleiotropy trace by calculating the log-likelihoods for the pleiotropic models at every position.

$$LOD_{p}(\lambda) = ll_{10}(\lambda, \lambda) - \max ll_{10}(\lambda, \lambda)$$
(2.11)

By definition, the maximum value for this pleiotropy trace is zero.

### 613 2.2.6 Bootstrap for test statistic calibration

We use a parametric bootstrap to calibrate our test statistic (Efron, 1979). While Jiang and Zeng (1995) used 614 quantiles of a chi-squared distribution to determine p-values, this does not account for the two-dimensional search over QTL positions. We follow the approach of Tian et al. (2016), and identify the maximum likelihood 616 estimate of the QTL position under the null hypothesis of pleiotropy. We then use the inferred model parameters under that model and with the QTL at that position to simulate bootstrap data sets according 618 to the model in equations 2.1-2.3. For each of b bootstrap data sets, we perform a two-dimensional QTL scan (over the genomic region of interest) and derive the test statistic value. We treat these b test statistics 620 as the empirical null distribution, and calculate a p-value as the proportion of the b bootstrap test statistics that equal or exceed the observed one, with the original data,  $p = \#\{i : LOD_i^* \geq LOD\}/b$  where  $LOD_i^*$ 622 denotes the LOD score for the ith bootstrap replicate and LOD is the observed test statistic. 623

### <sup>624</sup> 2.2.7 Data & Software Availability

- Our methods have been implemented in an R package, qtl2pleio, available at GitHub:
- https://github.com/fboehm/qtl2pleio
- 627 Custom R code for our analyses and simulations are at GitHub:
- https://github.com/fboehm/qt2pleio-manuscript-clean
- The data from Recla et al. (2014) and Logan et al. (2013) are available at the Mouse Phenome Database:
- https://phenome.jax.org/projects/Chesler4 and https://phenome.jax.org/projects/Recla1.
- They are also available in R/qtl2 format at https://github.com/rqtl/qtl2data.

### $_{\scriptscriptstyle 2}$ 2.3 Simulation studies

We performed two types of simulation studies, one for type I error rate assessment and one to characterize the power to detect separate QTL. To simulate traits, we specified X, B,  $V_g$ , K, and  $V_e$  matrices (Equations

Table 2.1: Type I error rates for all runs in our  $2^3$  experimental design. We set (marginal) genetic variances (i.e., diagonal elements of  $V_g$ ) to 1 in all runs.  $V_e$  was set to the 2 by 2 identity matrix in all runs. We used allele probabilities at a single genetic marker to simulate traits for all eight sets of parameter inputs. In the column "Allele effects partitioning", "ABCD:EFGH" means that lines A-D carry one QTL allele while lines E-H carry the other allele. "F:ABCDEGH" means the QTL has a private allele in strain F.

Run	$\Delta$ (Allele effects)	Allele effects partitioning	Genetic correlation	Type I error rate
1	6	ABCD:EFGH	0	0.032
$^2$	6	ABCD:EFGH	0.6	0.035
3	6	F:ABCDEGH	0	0.040
4	6	F:ABCDEGH	0.6	0.045
5	12	ABCD:EFGH	0	0.038
6	12	ABCD:EFGH	0.6	0.042
7	12	F:ABCDEGH	0	0.025
8	12	F:ABCDEGH	0.6	0.025

2.1–2.3). For both we used the allele probabilities from a single genomic region derived empirically from data for a set of 479 Diversity Outbred mice from Keller et al. (2018).

## 7 2.3.1 Type I error rate analysis

To quantify type I error rate (i.e., false positive rate), we simulated 400 pairs of traits for each of eight sets
of parameter inputs (Table 2.1). We used a  $2^3$  factorial experimental design with three factors: allele effects
difference, allele effects partitioning, and genetic correlation, i.e., the off-diagonal entry in the 2 by 2 matrix  $V_g$ .

We chose two strong allele effects difference values, 6 and 12. These ensured that the univariate phenotypes mapped with high LOD scores to the region of interest. For the allele partitioning factor, we used either equally frequent QTL alleles, or a private allele in the CAST strain (F). For the residual genetic correlation (the off-diagonal entry in  $V_g$ ), we considered the values 0 and 0.6. The marginal genetic variances (i.e., the diagonal entries in  $V_g$ ) for each trait were always set to one.

We performed 400 simulation replicates per set of parameter inputs, and each used b = 400 bootstrap samples. For each bootstrap sample, we calculated the test statistic (Equation 2.8). We then compared the test statistic from the simulated trait against the empirical distribution of its 400 bootstrap test statistics. When the simulated trait's test statistic exceeded the 0.95 quantile of the empirical distribution of bootstrap test statistics, we rejected the null hypothesis. We observed that the test is slightly conservative over our range of parameter selections (Table 2.1), with estimated type I error rates < 0.05.

## $_{53}$ 2.3.2 Power analysis

We also investigated the power to detect the presence of two distinct QTL. We used a  $2 \times 2 \times 5$  experimental design, where our three factors were allele effects difference, allele effects partitioning, and inter-locus distance. The two levels of allele effects difference were 1 and 2. The two levels of allele effects partitioning were as in the type I error rate studies, ABCD:EFGH and F:ABCDEGH (Table C.1). The five levels of interlocus distance were 0, 0.5, 1, 2, and 3 cM.  $V_g$  and  $V_e$  were both set to the 2 by 2 identity matrix in all power study simulations.

We simulated 400 pairs of traits per set of parameter inputs. For each simulation replicate, we calculated the likelihood ratio test statistic. We then applied our parametric bootstrap to calibrate the test statistics. For each simulation replicate, we used b = 400 bootstrap samples. Because the bootstrap test statistics within a single set of parameter inputs followed approximately the same distribution, we pooled the 400 \* 400 = 160,000 bootstrap samples per set of parameter inputs and compared each test statistic to the empirical distribution derived from the 160,000 bootstrap samples. However, for parameter inputs with interlocus distance equal to zero, we didn't pool the 160,000 bootstrap samples; instead, we proceeded by calculating power (i.e., type I error rate, in this case), as we did in the type I error rate study above.

We present our power study results in Figure 2.1. Power increases as interlocus distance increases. The top two curves correspond to the case where the QTL effects are largest. For each value for the QTL effect, power is greater when the QTL alleles are equally frequent, and smaller when a QTL allele is private to one strain. One can have high power to detect that the two traits have distinct QTL when they are separated by > 1 cM and when the QTL have large effect.

# <sup>673</sup> **2.4** Application

To illustrate our methods, we applied our test to data from Logan et al. (2013) and Recla et al. (2014), on 261 DO mice measured for a set of behavioral phenotypes. Recla et al. (2014) identified *Hydin* as the gene that underlies a QTL on Chromosome 8 at 57 cM for the "hot plate latency" phenotype (a measure of pain tolerance). The phenotype "percent time in light" in a light-dark box (a measure of anxiety) was measured on the same set of mice (Logan et al., 2013) and also shows a QTL near this location, which led us to ask whether the same locus affects both traits. The two traits show a correlation of -0.15 (Figure C.1).

QTL analysis with the LOCO method, and using sex as an additive covariate, showed multiple suggestive QTL for each phenotype (Figure C.2; Table C.2). For our investigation of pleiotropy, we focused on the

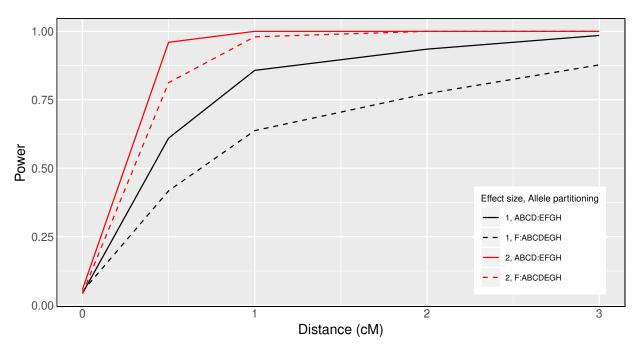


Figure 2.1: Pleiotropy vs. separate QTL power curves for each of four sets of parameter settings. Factors that differ among the four curves are allele effects difference and allele partitioning. Red denotes high allele effects difference, while black is the low allele effects difference. Solid line denotes the even allele partitioning (ABCD:EFGH), while dashed line denotes the uneven allele partitioning (F:ABCDEGH).

interval 53-64 cM on Chromosome 8. The univariate QTL results for this region are shown in Figure 2.2.

The estimated QTL allele effects for the two traits are quite different (Figure 2.3). With the QTL placed at 55 cM, for "percent time in light", the WSB and PWK alleles are associated with large phenotypes and NOD with low phenotypes. For "hot plate latency", on the other hand, CAST and NZO show low phenotypes and NOD and PWK are near the center.

In applying our test for pleiotropy, we performed a two-dimensional, two-QTL scan for the pair of phenotypes. With these results, we created a profile LOD plot (Figure 2.4). The profile LOD for "percent time in light" (in brown) peaks near 55 cM, as was seen in the univariate analysis. The profile LOD for "hot plate latency" (in blue) peaks near 57 cM, also similar to the univariate analysis. The pleiotropy trace (in gray) peaks near 55 cM.

The likelihood ratio test statistic for the test of pleiotropy was 1.2. Based on a parametric bootstrap with 1,000 bootstrap replicates, the estimated p-value was 0.11, indicating weak evidence for distinct QTL for the two traits.

## $_{\scriptscriptstyle 695}$ 2.5 Discussion

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We developed a test of pleiotropy vs. separate QTL for multiparental populations, extending the work of
Jiang and Zeng (1995) for multiple alleles and with a linear mixed model to account for population structure
(Kang, Sul, et al., 2010; J. Yang et al., 2014). Our simulation studies indicate that the test has power to
detect presence of separate loci, especially when univariate trait associations are strong (Figure 2.1). Type
I error rates indicate that our test is slightly conservative (Table 2.1).

In the application of our method to two behavioral phenotypes in a study of 261 Diversity Outbred mice (Recla et al., 2014; Logan et al., 2013), we obtained weak evidence (p=0.11) for the presence of two distinct QTL, with one QTL (which contained the *Hydin* gene) affecting only "hot plate latency" and a second QTL affecting "percent time in light" (Figure 2.4).

Founder allele effects plots provide further evidence for the presence of two distinct loci. As Macdonald and Long (2007) and King et al. (2012) have demonstrated in their analyses of multiparental *Drosophila* populations, a biallelic pleiotropic QTL would result in allele effects plots that have similar patterns. While we don't know that "percent time in light" and "hot plate latency" arise from biallelic QTL, the dramatic differences that we observe in allele effects patterns further support the argument for two distinct loci.

We have implemented our methods in an R package qtl2pleio, but analyses can be computationally

# percent time in light



# hot plate latency



Figure 2.2: Chromosome 8 univariate LOD scores for percent time in light and hot plate latency reveal broad, overlapping peaks between 53 cM and 64 cM. The peak for percent time in light spans the region from approximately 53 cM to 60 cM, with a maximum near 55 cM. The peak for hot plate latency begins near 56 cM and ends about 64 cM.

# percent time in light



# hot plate latency



Figure 2.3: Chromosome 8 univariate LOD scores for percent time in light and hot plate latency reveal broad, overlapping peaks between 53 cM and 64 cM. The peak for percent time in light spans the region from approximately 53 cM to 60 cM, with a maximum near 55 cM. The peak for hot plate latency begins near 56 cM and ends about 64 cM.

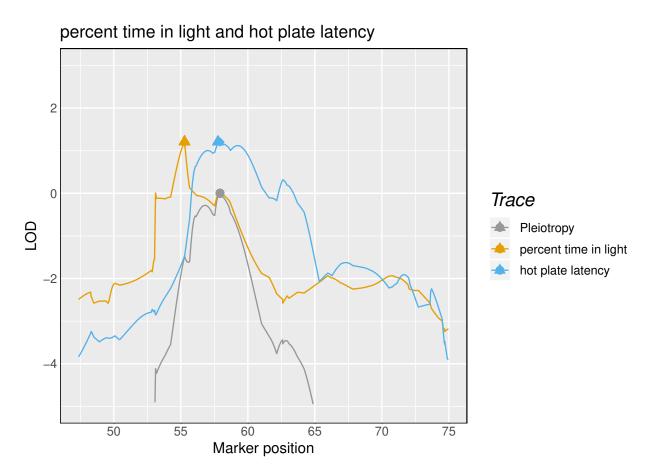


Figure 2.4: Profile LOD curves for the pleiotropy vs. separate QTL hypothesis test for "percent time in light" and "hot plate latency". Gray trace denotes pleiotropy LOD values. Triangles denote the univariate LOD maxima, while diamonds denote the profile LOD maxima. For "percent time in light", the brown triangle obscures the smaller brown diamond. Likelihood ratio test statistic value corresponds to the height of the blue and brown traces at their maxima.

intensive and time consuming. qtl2pleio is written mostly in R, and so we could likely obtain improved computational speed by porting parts of the calculations to a compiled language such as C or C++. To accelerate our multi-dimensional QTL scans, we have integrated C++ code into qtl2pleio, using the Rcpp package (Eddelbuettel et al., 2011).

Another computational bottleneck is the estimation of the variance components  $V_g$  and  $V_e$ . To accelerate this procedure, especially for the joint analysis of more than two traits, we will consider other strategies for variance component estimation, including that described by H. V. Meyer et al. (2018). H. V. Meyer et al. (2018), in joint analysis of dozens of traits, implement a bootstrap strategy to estimate variance components for lower-dimensional phenotypes before combining bootstrap estimates into valid covariance matrices for the full multivariate phenotype. Such an approach may ease some of the computational burdens that we encountered.

We view tests of pleiotropy as complementary to mediation tests and related methods that have become popular for inferring biomolecular causal relationships (Chick et al., 2016; Schadt et al., 2005; Baron and Kenny, 1986). A mediation test proceeds by including a putative mediator as a covariate in the regression analysis of phenotype and QTL genotype; a substantial reduction in the association between genotype and phenotype corresponds to evidence of mediation.

Mediation analyses and our pleiotropy test ask distinct, but related, questions. Mediation analysis seeks to establish causal relationships among traits, including molecular traits, or dependent biological and behavioral processes. Pleiotropy tests examine whether two traits share a single source of genetic variation, which may act in parallel or in a causal network. Pleiotropy is required for causal relations among traits. In many cases, the pleiotropy hypothesis is the only reasonable one.

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Schadt et al. (2005) argued that both pleiotropy tests and causal inference methods may contribute to
gene network reconstruction. They developed a model selection strategy, based on the Akaike Information
Criterion (Akaike, 1974), to determine which causal model is most compatible with the observed data.
Schadt et al. (2005) extended the methods of Jiang and Zeng (1995) to consider more complicated alternative
hypotheses, such as the possibility of two QTL, one of which associates with both traits, and one of which
associates with only one trait. As envisioned by Schadt et al. (2005), we foresee complementary roles emerging
for our pleiotropy test and mediation tests in the dissection of complex trait genetic architecture.

CAPE (Combinatorial Analysis of Pleiotropy and Epistasis) is a strategy for identifying higher-order relationships among traits and marker genotypes (Tyler, W. Lu, et al., 2013). Tyler, Ji, et al. (2017) used CAPE to identify epistatic gene networks in Diversity Outbred mice. Tyler, Donahue, et al. (2016) found

evidence for weak epistasis in a large intercross population.

CAPE uses linear models that are distinct from those in our pleiotropy test. A CAPE starts with founder allele dosages at all markers and a collection of two or more traits (Tyler, Ji, et al., 2017). After eigendecomposition to get two or more eigentraits, univariate QTL scans are performed and founder allele effects are estimated at all markers (or a subset of all markers). Next, one identifies markers with sufficiently strong effects of at least one founder allele. Resulting (eigentrait, marker, founder allele) triples are then subjected to a second model fitting. This second round of modeling involves two (eigentrait, marker, founder allele) triples that share an eigentrait. The shared (univariate) eigentrait is modeled as a linear function of the two founder allele dosages and their interaction.

In comparing CAPE and our pleiotropy test, it's important to recognize that the two methods ask 751 different questions. CAPE enables assessment of interactions among specific founder allele dosages at two (possibly identical) markers while examining one eigentrait at a time. Our pleiotropy test, on the other hand, 753 jointly models two phenotypes and quantifies the evidence against the pleiotropy hypothesis by performing a two-dimensional QTL scan over a genomic region. One limitation of CAPE is its inability to account for 755 population structure. Incorporation of a polygenic random effect into CAPE's linear models may improve its performance in multiparental populations. CAPE's methods also highlight a current limitation of our 757 pleiotropy test. While our multivariate linear models accommodate interactions between founder allele dosages at two markers, we haven't yet incorporated this functionality into our software. It is one direction 759 for future research. 760

Technological advances in mass spectrometry and RNA sequencing have enabled the acquisition of highdimensional biomolecular phenotypes (Ozsolak and Milos, 2011; X. Han, K. Yang, and Gross, 2012). Multiparental populations in *Arabidopsis*, maize, wheat, oil palm, rice, *Drosophila*, yeast, and other organisms
enable high-precision QTL mapping (Yu et al., 2008; Tisne et al., 2017; Stanley et al., 2017; Raghavan
et al., 2017; Mackay et al., 2012; Kover et al., 2009; Cubillos et al., 2013). The need to analyze highdimensional phenotypes in multiparental populations compels the scientific community to develop tools to
study genotype-phenotype relationships and complex trait architecture. Our test, and its future extensions,
will contribute to these ongoing efforts.

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# Chapter 3

# Applications

#### 3.1Expression trait hotspot dissection

#### 3.1.1 Introduction

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A central goal of systems genetics studies is to identify causal relationships between biomolecules. Recent 782 work by Chick et al. (2016), which builds on research from Baron and Kenny (1986), has popularized linear 783 regression-based methods, such as mediation analysis, for causal inference in genetics. Because of the great 784 successes of mediation analysis in systems genetics (Chick et al., 2016; Keller et al., 2018), we need to clarify a role for our pleiotropy test. We argue below that our pleiotropy test complements mediation analysis in 786 two ways. First, our test limits the set of candidate mediators by ruling out traits that don't share a single pleiotropic QTL. This is reasonable because it's unlikely that one trait mediates a relationship between a 788 genetic variant and a second trait unless the two traits share a pleiotropic QTL. Second, when regressionbased mediation analysis fails to identify a mediator, our pleiotropy test still provides information on the number of QTL, which may aid biological understanding and inform subsequent studies. Below, we first 791 review the prerequisite molecular biology, including the "central dogma", before discussing in some detail regression-based mediation analysis in the systems genetics context. 793 F. H. Crick (1958) articulated a pathway for transmission of biological information that is now known as the central dogma of molecular biology (Figure 3.1) (F. Crick, 1970). In it, he argued that information 795 encoded in DNA sequence is transmitted via transcription to RNA molecules, which, in turn, transfer the information to proteins via translation. The process of transcription uses DNA as a template for creating a



Figure 3.1: Biological information is encoded in DNA. This information is passed, via transcription, to sequence-specific RNA molecules. The process of translation transmits the information to sequence-specific proteins.

RNA molecule that conveys the information encoded in DNA. In this sense, every gene leads to a unique RNA molecule. Translation is the molecular biology process by which a RNA molecule's information is transferred to a protein. As in transcription, the nucleic acid (DNA in transcription and RNA in translation) serves as a template for synthesis of the product (RNA in transcription and protein in translation). Thus, RNA molecules from distinct genes lead to different proteins.

This sequence of information transfer, from DNA to RNA to protein, provides a natural setting by which
to examine mediation analysis. If a DNA variant affects protein concentrations only through its gene's RNA
transcripts, then conditioning on RNA transcript levels would greatly reduce the strength of association
between DNA variant and protein concentration. Before we continue our discussion, we define key terms
and discuss an example below.

We continue by stating what it means for one trait to mediate a relationship between a DNA variant 808 and another trait. To clarify our discussion, we refer to an example from Chick et al. (2016) (Figure 3.2). 809 Chick et al. (2016), in studying livers of 192 Diversity Outbred mice, found evidence that Dhtkd1 transcript 810 levels associated with a Chromosome 2 marker near the *Dhtkd1* gene. They also found that the same marker 811 affected DHTKD1 protein concentrations. (Note that DHTKD1 protein is the product of translation of 812 Dhtkd1 transcripts.) As anticipated, mediation analysis, in which the DHTKD1 protein concentrations are 813 regressed on founder allele dosages (at the Chromosome 2 marker) demonstrated that Dhtkd1 transcript 814 levels act as a mediator between DHTKD1 protein concentrations and founder allele dosages. In fact, the extent of the reduction in association strength indicates that the primary pathway by which the genetic 816 marker affects DHTKD1 protein concentrations is through *Dhtkd1* transcript levels.

In our studies below, we follow Keller et al. (2018) by generalizing this setting to the case where a DNA variant affects a local transcript level, which then affects a nonlocal transcript level. We term a transcript "local" to a marker when its gene is near that marker. We use a threshold of no more than 2 Mb to restrict

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Figure 3.2: A DNA variant in the *Dhtkd1* gene affects *Dhtkd1* transcript abundances which, in turn, affect DHTKD1 protein concentrations.

the number of local transcripts for a given marker. A nonlocal transcript, then, is either one that arises from a gene on another chromosome or from a distant gene on the same chromosome as the marker.

It is highly plausible that concentration variations in one transcript may affect abundances of a second transcript. For example, the first transcript may encode a transcription factor protein. In this case, the transcription factor protein may influence expression patterns of the second transcript (and perhaps other transcripts, too).

To determine whether a local transcript level mediates the relationship between a nonlocal transcript level and a DNA variant, we perform a series of regression analyses, which we detail below (Frame 3.1).

In brief, we regress the nonlocal transcript levels on founder allele dosages at the DNA variant, with and without conditioning on the candidate mediator (the local transcript levels). If the LOD score diminishes sufficiently upon conditioning on a candidate, then we declare the candidate a mediator.

The rationale behind this strategy follows. If the DNA variant affects the nonlocal transcript levels solely by way of local transcript levels, then conditioning on the local transcript levels would nullify the relationship between DNA variant and the nonlocal transcript levels. At the other extreme, if the DNA variant affects nonlocal transcript levels solely through mechanisms that don't involve the local transcript levels, then conditioning on local transcript levels would not affect the association between the DNA variant and nonlocal transcript levels.

We now consider the procedures needed for a mediation analysis in systems genetics. In the four linear regression models (Frame 3.1), X is a n by 8 matrix of founder allele dosages at a single marker, B is a 8 by 1 matrix of founder allele effects, E is a n by 1 matrix of random errors, b is an number, 1 is a n by 1 matrix with all entries set to 1, Y is a n by 1 matrix of phenotype values (for a single trait), and M is a n by 1 matrix of values for a putative mediator. C is a matrix of covariate effects, and W is a matrix of covariates.

We denote the coefficient of the mediator by  $\beta$ .

Frame 3.1: Four regressions for a single mediation analysis

$$Y = b1 + WC + E \tag{3.1}$$

$$Y = XB + WC + E \tag{3.2}$$

$$Y = b1 + WC + M\beta + E \tag{3.3}$$

$$Y = XB + WC + M\beta + E \tag{3.4}$$

We assume that the vector E is (multivariate) normally distributed with zero vector as mean and covariance matrix  $\Sigma = \sigma^2 I_n$ , where  $I_n$  is the n by n identity matrix.

In the above models with normally distributed random errors, the log-likelihoods are easily calculated.

For example, in Equation 3.1, the vector Y follows a multivariate normal distribution with mean (b1+WC)

and covariance  $\Sigma = \sigma^2 I$ . Thus, we can write the likelihood for Model 3.1 as:

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$$L(b, C, \sigma^{2}|Y, W) = (2\pi)^{-\frac{n}{2}} \exp\left(-\frac{1}{2}(Y - b1 - WC)^{T} \Sigma^{-1}(Y - b1 - WC)\right)$$
(3.5)

We thus have the following equation (3.6 for the log-likelihood for Model 3.1:

$$\log L(b, C, \sigma^2 | Y, W) = -\frac{n}{2} \log(2\pi) - \frac{1}{2} (Y - b1 - WC)^T \Sigma^{-1} (Y - b1 - WC)$$
(3.6)

Chick et al. (2016) calculated the log<sub>10</sub> likelihoods for all four models before determining two LOD scores
(Equations 3.7 and 3.8).

$$LOD_1 = log_{10}(\text{Model } 3.2 \text{ likelihood}) - log_{10}(\text{Model } 3.1 \text{ likelihood})$$
(3.7)

$$LOD_2 = log_{10}(\text{Model } 3.4 \text{ likelihood}) - log_{10}(\text{Model } 3.3 \text{ likelihood})$$
(3.8)

And, finally, Chick et al. (2016) calculated the LOD difference statistic (Equation 3.9).

$$LOD difference = LOD_1 - LOD_2$$
 (3.9)

LOD difference values need not be positive. For example, in the setting where the putative mediator is

#### **Frame 3.2:** Four assumptions for causal inference

- 1. No unmeasured confounding of the DNA variant-nonlocal transcript levels relationship
- 2. No unmeasured confounding of the local transcript levels-nonlocal transcript levels relationship
- 3. No unmeasured confounding of the DNA variant-local transcript levels relationship
- 4. No local transcript levels-nonlocal transcript levels confounder that is affected by the DNA variant

not a true mediator,  $LOD_1$  and  $LOD_2$  values may lead to a negative LOD difference statistic.

In our analyses below, we consider the LOD difference proportion (Equation 3.10).

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$$LOD difference proportion = \frac{(LOD_1 - LOD_2)}{LOD_1}$$
(3.10)

In other words, we consider what proportion of the association strength, on the LOD scale, is diminished by conditioning on a putative mediator. This statistic differs from the LOD difference statistic in that it scales the LOD difference by LOD<sub>1</sub> value. We do this in efforts to accommodate the diversity of LODs in our data. For example, a LOD difference statistic of 5 may be relevant when a trait has a LOD<sub>1</sub> of 10, but unimportant if the trait's LOD<sub>1</sub> is 100. Now that we've named our summary statistics for a mediation analysis in systems genetics, we turn attention to two statistical challenges in this area of research, 1.

Our first statistical challenge is due to confounding. To claim that the LOD difference statistic reflects a causal relationship, four assumptions about confounding are needed (Frame 3.2) (VanderWeele, 2015), yet it is often difficult or impossible to recognize unmeasured confounders. In studies of Diversity Outbred mice, relatedness is a possible confounder, yet the linear models (Equations 3.1, 3.2, 3.3, 3.4 in Frame 3.1) fail to account for the complex relatedness patterns among Diversity Outbred mice. In fact, the only covariates in our models are for wave membership and sex. Other sources of confounding, such as batch effects in the phenotyping, may be unmeasured.

In efforts to quantify the potential impact of unmeasured confounding, scientists have developed a suite of sensitivity analysis tools for use in regression-based mediation analysis. While a discussion of sensitivity analysis is beyond the scope of this thesis, it may be useful in future systems genetics studies to assess robustness of mediation analysis results in the presence of unmeasured confounders. VanderWeele (2015) discusses sensitivity analysis in the context of epidemiological studies.

Besides accounting for confounding, a second statistical challenge in mediation analysis is assessing signif-

icance of the LOD difference statistic. Chick et al. (2016) used individual transcript levels as sham mediators and tabulated their LOD difference statistics. They then compared the observed LOD difference statistics for putative mediators to the empirical distribution of LOD difference statistics obtained from the collection of sham mediators. Keller et al. (2018), on the other hand, in their study of pancreatic islet cell biology, declared mediators those local transcripts that diminished the LOD score of nonlocal transcripts by at least 1.5. While significance threshold determination remains an active area of research, we proceed below by examining all 147 nonlocal transcript levels that Keller et al. (2018) identified as mapping to the Chromosome 2 hotspot.

#### $_{884}$ 3.1.2 Methods

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We examined the potential that the two methods, 1. pleiotropy vs. separate QTL testing and 2. mediation
analysis, play complementary roles in efforts to dissect gene expression trait hotspots. We use the term
"hotspot" to refer to a contiguous genomic region, typically no more than 5 Mb in length, that affects many
expression traits. After describing our data below, we detail our statistical analyses involving 13 local gene
expression traits and 147 nonlocal gene expression traits, all of which map to a 4-Mb hotspot on Chromosome
2.

We analyzed data from 378 Diversity Outbred mice (Keller et al., 2018). Keller et al. (2018) genotyped tail biopsies with the GigaMUGA microarray (Morgan et al., 2015). They also used RNA sequencing to measure genome-wide pancreatic islet cell gene expression for each mouse at the time of sacrifice (Keller et al., 2018).

We examined the Chromosome 2 pancreatic islet cell expression trait hotspot that Keller et al. (2018) identified. Keller et al. (2018) found that 147 nonlocal traits map to the 4-Mb region centered at 165.5 Mb on Chromosome 2. The 147 nonlocal traits all exceeded the genome-wide LOD significance threshold, 7.18 (Keller et al., 2018). With regression-based mediation analyses, they identified transcript levels of local gene *Hnf4a* as a mediator of 88 of these 147 nonlocal traits.

We designed a study to examine the possible roles for mediation analysis and pleiotropy testing. Because Keller et al. (2018) reported that some nonlocal traits that map to the Chromosome 2 hotspot did not demonstrate evidence of mediation by Hnf4a expression levels, we elected to study a collection of local gene expression traits, rather than Hnf4a alone. This strategy enabled us to ask whether one of twelve other local traits mediates those nonlocal hotspot traits that are not mediated by Hnf4a. Our set of local gene expression traits includes Hnf4a and 12 other local genes (Table 3.1). Our 13 local genes are the only genes

#### Frame 3.3: Local gene inclusion criteria

1. QTL peak with LOD > 40

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- 2. QTL peak position within 2 Mb of hotspot center (165.5 Mb)
- 3. Gene midpoint within 2 Mb of hotspot center (165.5 Mb)

that met three criteria (Frame 3.3). The 147 nonlocal traits that we studied all had LOD peak heights above
7.18 and QTL positions within 2 Mb of the center of the hotspot (at 165.5 Mb).

We now describe our statistical analyses. After univariate QTL mapping to identify expression traits
that map to the Chromosome 2 hotspot, we performed both bivariate QTL scans and mediation analyses of
all 13 \* 147 = 1911 pairs involving one local expression trait and one nonlocal expression trait.

Our bivariate QTL analyses involved the same 13 local expression traits and 147 nonlocal expression traits. We described above (Frame 3.3) the criteria for choosing these expression traits.

We performed a series of two-dimensional QTL scans in which we paired each local gene's transcript levels with each nonlocal gene's transcript levels, for a total of  $13 \times 147 = 1,911$  two-dimensional scans. Each scan examined the same set of 180 markers, which spanned the interval from 163.1 Mb to 167.8 Mb and included univariate peaks for all 13 + 147 = 160 expression traits. We performed these analyses with the R package qt12pleio (Boehm, 2018b).

For each bivariate QTL scan, we fitted a collection of bivariate models for all 180 \* 180 = 32,400 ordered pairs of markers. For each ordered pair of markers, we fitted a bivariate linear mixed effects model using the methods of Chapter 2.

We performed mediation analyses for all 1,911 local-nonlocal trait pairs in which we probed the extent to which each nonlocal trait's association strength diminished upon conditioning on transcript levels of a putative mediator.

Each of the 13 local expression traits, considered one at a time, served as putative mediators. We thus
fitted the four linear regression models that we describe above (Equations 3.1, 3.2, 3.3, 3.4).

One question that needs clarification is the choice of genetic marker for each mediation analysis. We elected to use the founder allele dosages at the marker that demonstrated the univariate LOD peak for the putative mediator. Alternative analyses, in which one uses the founder allele dosages at which the nonlocal trait has its univariate peak, are also possible.

To visualize the summary statistics for our two methods, we plotted, for each local gene, a scatterplot of

931	LOD	difference	proportion	values	against	pleiotropy	test	statistics.
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Gene	Start	End	QTL peak position	LOD
Pkig	163.66	163.73	163.52	51.68
Serinc3	163.62	163.65	163.58	126.93
Hnf4a	163.51	163.57	164.02	48.98
Stk4	164.07	164.16	164.03	60.39
Pabpc1l	164.03	164.05	164.03	52.50
Slpi	164.35	164.39	164.61	40.50
Neurl2	164.83	164.83	164.64	64.58
Cdh22	165.11	165.23	165.05	53.84
$2810408\mathrm{M}09\mathrm{Rik}$	165.49	165.49	165.57	67.34
Eya2	165.60	165.77	165.72	98.89
Prex1	166.57	166.71	166.75	46.91
Ptgis	167.19	167.24	167.27	56.25
Gm14291	167.20	167.20	167.27	73.72

Table 3.1: Local gene annotations for analysis of Chromosome 2 expression trait hotspot. All positions are in units of Mb on Chromosome 2. LOD peak position and LOD peak height refer to those obtained from univariate analyses. "Start" and "end" refer to the local gene's DNA start and end positions, as annotated by Ensembl version 75.

We also examined the 1,911 pairs from the per-nonlocal gene perspective. For each of the 147 nonlocal genes, we plotted LOD difference proportion against pleiotropy test statistic values. We present below (Figure 3.6) examples that illustrate some of the observed patterns between pleiotropy test statistics and LOD difference proportion values.

## 936 3.1.3 Results

Below, we visualize results of our pleiotropy tests and mediation analyses. After examining a plot involving
all tested pairs, we take two distinct perspectives. In these, we visualize results from the perspective of
every local gene expression trait before taking the complementary perspective with visualizations from the
perspective of every nonlocal gene expression trait. We present below our scatter plot for all 147 x 13 =
1,911 pairs of traits (Figure 3.3). Each pair contains one local expression trait and one nonlocal expression
trait. Each point in the figure represents a single pair. We see that points with high values of LOD difference
proportion tend to have small values of pleiotropy test statistic, and those points with high values of the
pleiotropy test statistic tend to have small values of LOD difference proportion.

Some points demonstrate large values of pleiotropy test statistic (eg., > 10), yet still have sizeable LOD difference proportion statistics (Figure 3.3. One possible explanation for such points is that the univariate LOD (LOD<sub>1</sub>) value is small, so that even a modest LOD difference gives rise to a sizeable LOD difference

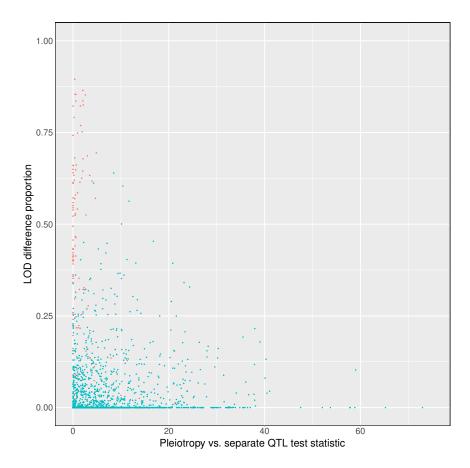


Figure 3.3: LOD difference proportion against pleiotropy vs. separate QTL test statistics for 1911 pairs of traits. Each point represents a single pair. Pairs that involve local expression trait Hnf4a are colored blue, while all others are colored red. Note the high prevalence of blue points in the upper left quadrant of the figure. These points, with low values of the pleiotropy vs. separate QTL test statistic and high values of LOD difference proportion, are consistent with Hnf4a transcript levels mediating the effect of Hnf4a genetic variants affecting nonlocal transcript abundances.

proportion value. A second possible explanation is that the phenotype variances for both phenotypes in the pair are large enough to skew the null distribution of the test statistic towards larger values. To distinguish 949 between these two, we would examine the LOD difference statistics and obtain bootstrap p-values.

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In Figure 3.3, we colored blue the points that involve Hnf4a; points with other local genes are red. The most striking feature of the coloring is that many blue points have small values of the pleiotropy test statistics and very high values of LOD difference proportion.

To more thoroughly examine the pleiotropy test and mediation analysis relationships across the 13 local genes, we created 13 plots of LOD difference proportion against pleiotropy test statistic (Figures 3.4 and 3.5). 955 They reveal common patterns. First, we see no points in the upper right quadrant of each plot (Figure 3.5).

This tells us that those nonlocal genes with high values of pleiotropy test statistic (when paired with the specified local gene) have low values of LOD difference proportion. Similarly, those nonlocal genes with high values of LOD difference proportion tend to have small values of the pleiotropy test statistic. Finally, some 959 trait pairs demonstrate low values of both the LOD difference proportion and pleiotropy test statistic. This observation suggests that, for a given local expression trait, the nonlocal trait is not mediated by the local 961 expression trait yet it shares a pleiotropic locus. Low power to resolve multiple nearby QTL may give rise to such findings. 963

In comparing the Hnf4a plot (Figure 3.4) with the other 12 plots (Figure 3.5), we see that none of the 12 plots in Figure 3.5 closely resembles Figure 3.4. Serinc3, Stk4, Neurl2, and Cdh22 are closest in appearance 965 to the plot of Hnf4a. However, each of Serinc3, Stk4, Neurl2, and Cdh22 has very few points with LOD difference proportion above 0.5, while Hnf4a has many points with LOD difference proportion above 0.5.

Now that we've examined our results from the perspective of every local gene expression trait, we turn 968 attention to the nonlocal gene expression trait perspective. Scatter plots of LOD difference proportion values against pleiotropy vs. separate QTL test statistics for each of the 147 nonlocal expression traits demonstrated 970 multiple patterns. Eighty-nine nonlocal genes' plots showed Hnf4a to have the greatest value, among the 13 putative mediators, of the LOD difference proportion statistic. In many cases, Hnf4a's LOD difference 972 proportion statistic was at least twice that of any of the other 12 local gene expression levels.

#### 3.1.4 Discussion 974

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Our pairwise analyses with both mediation analyses and pleiotropy tests provide additional evidence for the importance of Hnf4a in the biology of the Chromosome 2 hotspot in pancreatic islet cells. Our analyses, and, 976 specifically, the test of pleiotropy vs. separate QTL, may be more useful when studying nonlocal traits that 977 map to a hotspot yet don't show strong evidence of mediation by local expression traits. In such a setting, 978 the pleiotropy test can, at least, provide some information about the genetic architecture at the hotspot. 979 Specifically, our pleiotropy test may inform inferences about the number of underlying QTL in a given expression trait hotspot. Additionally, our test may limit the number of expression traits that are potential 981 intermediates between a QTL and a specified nonlocal expression trait. This relies on the assumption that a causally intermediate (local) expression trait and a target (nonlocal) expression trait presumably share a 983 QTL. On the other hand, mediation analyses, when they provide evidence for mediation of a nonlocal trait by a local expression trait, are possibly more valuable than the test of pleiotropy vs. separate QTL, since the mediation analyses identify precisely the intermediate expression trait.

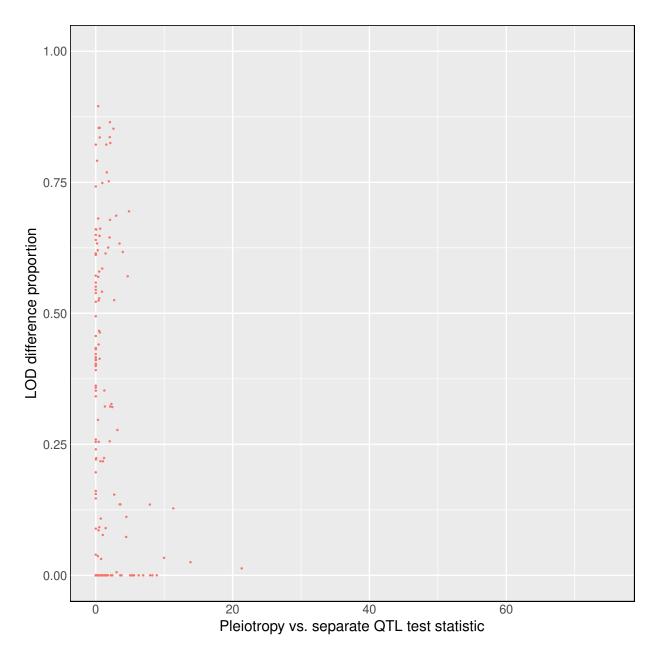


Figure 3.4: Scatter plot of LOD difference proportion against pleiotropy vs. separate QTL test statistic for 147 pairs of traits. Each pair includes Hnf4a and one of the nonlocal gene expression traits that map to the Chromosome 2 hotspot.

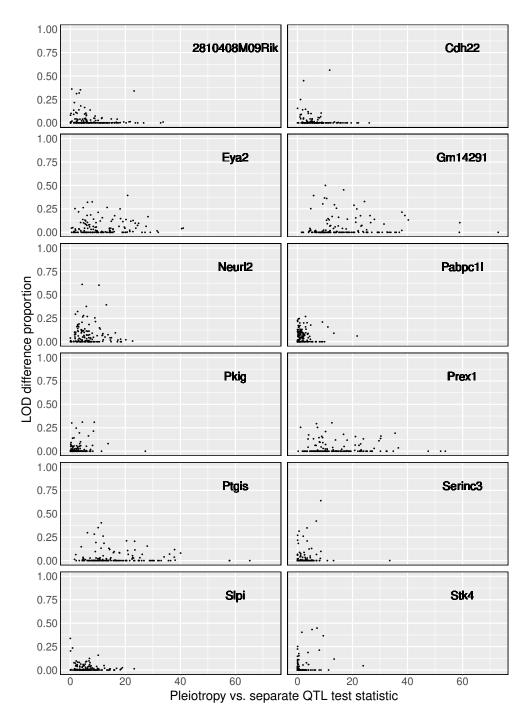
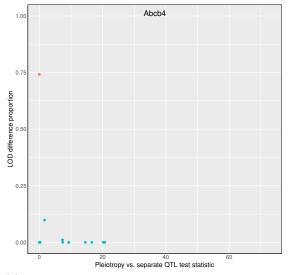
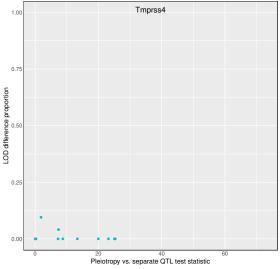


Figure 3.5: Scatter plots of LOD difference proportion against pleiotropy vs. separate QTL test statistic with 147 pairs of traits per panel. Each panel includes a local gene expression trait (per the label in the upper right quadrant) and one of the 147 nonlocal gene expression traits that map to the Chromosome 2 hotspot.

Figure 3.6: Scatter plots for four nonlocal expression traits. Each plot features 13 points, one for each local gene expression trait. The vertical axis denotes LOD difference proportion values, while the horizontal axis corresponds to pleiotropy test statistics. Blue points represent the pairing with local gene expression trait Hnf4a. Red points represent the other 12 local gene expression traits.



(a) Hnf4a transcript levels mediate Abcb4 transcript levels. The high LOD difference proportion and the very small pleiotropy test statistic together provide evidence that Hnf4a mediates Abcb4 transcript levels.



(c) Tmprss4 transcript levels are not mediated by any of the 13 local gene expression traits. However, several local gene expression traits arise from separate QTL, as evidenced by their large (greater than 5) values of the pleiotropy test statistic.



(b) Hnf4a transcript levels mediate Smim5 transcript levels. The high LOD difference proportion and the very small pleiotropy test statistic together provide evidence that Hnf4a mediates Smim5 transcript levels.



(d) Gm3095 transcript levels are not mediated by any of the 13 local genes. The tests of pleiotropy demonstrate evidence of separate QTL for some local expression traits when paired with Gm3095.

We recommend using both tests of pleiotropy vs separate QTL and mediation analyses when dissecting 987 an expression trait QTL hotspot. In practice, mediation analyses, which involve a collection of univariate 988 regressions at a small set of pre-specified markers, are less computationally intense than tests of pleiotropy 989 vs. separate QTL, since the latter requires a two-dimensional QTL scan over the region of interest. This two-dimensional QTL scan often involves fitting more than ten thousand bivariate regression models. In 991 light of the computational cost of testing pleiotropy vs separate QTL, future researchers may wish to use it as a follow-up to mediation analyses when examining expression trait hotspots. 993

Future research may investigate the use of polygenic random effects in the statistical models for media-994 tion analysis. Additional methodological questions include approaches for declaring significant a mediation 995 LOD difference proportion and consideration of other possible measures and scales of extent of mediation. Additionally, future researchers may wish to consider biological models that contain two mediators.

The social and health sciences have witnessed much methods research in mediation analysis. The field 998 of statistical genetics has not fully adopted these strategies yet, but, given the nature of current and future data, many opportunities exist for translation of approaches from causal inference in epidemiology to systems 1000 genetics. For example, VanderWeele (2015) contains detailed discussions of many methods issues that arose in mediation analyses in epidemiology studies. 1002

#### 3.2Power analyses

#### 3.2.1 Introduction 1004

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The goal of this section is to characterize the statistical power of our pleiotropy test under a variety of 1005 conditions by studying a real data set. We examine pancreatic islet expression traits from the Keller et al. 1006 (2018) data. As in chapters 2 and 3A, we test only two traits at a time. Because we've chosen local expression 1007 traits in our analysis, we both know where each trait's true QTL location (approximately), and we anticipate 1008 that each trait has a unique QTL that is distinct from QTL for other local expression traits. This design thus provides opportunities to study statistical power for our test. 1010

We anticipate that inter-locus distance, univariate QTL strength, and correlation of founder allele effects 1011 patterns are three factors that contribute to power for our test. Specifically, we expect that greater inter-1012 locus distance, greater univariate LOD scores, and less similar founder allele effects patterns correspond to 1013 greater statistical power to detect two separate QTL. 1014

We use pancreatic islet gene expression traits from a publicly available data set, which Keller et al.

(2018) first collected, analyzed, and shared. We examine a collection of 80 local traits on Chromosome 19 and perform our test for pleiotropy on pairs of traits. We also examine pairwise relationships among gene expression traits to characterize the impacts of univariate LOD score, inter-locus distance, and similarity of founder allele effects patterns on pleiotropy test statistics.

## 3.2.2 Methods

We analyzed data from 378 Diversity Outbred mice (Keller et al., 2018). Keller et al. (2018) genotyped tail
biopsies with the GigaMUGA microarray (Morgan et al., 2016). They used RNA sequencing to measure
genome-wide pancreatic islet cell gene expression for each mouse at the time of sacrifice (Keller et al.,
2018). They shared these data, together with inferred founder allele probabilities, on the Data Dryad site
(https://datadryad.org/resource/doi:10.5061/dryad.pj105). We performed analyses with the R statistical
computing environment (R Core Team, 2018) and the packages qt12 (K. W. Broman, D. M. Gatti, et al.,
2019) and qt12pleio (Boehm, 2018b).

We study below 80 Chromosome 19 local expression QTL and their corresponding transcript levels. We define a local expression QTL to be an expression QTL that is on the same chromosome as the gene itself. For example, the Asah2 gene is located on Chromosome 19 and its transcript levels have an expression QTL on Chromosome 19 (Table 3.2). Thus, we term the Chromosome 19 Asah2 expression QTL a local expression QTL.

We choose to focus on local expression QTL, while ignoring nonlocal expression QTL, because we know, approximately, the true locations for local expression QTL. That is, a local expression QTL is near the corresponding gene position. Additionally, we expect that a given local expression QTL affects only one local expression trait. In our example above, we expect that the *Asah2* expression QTL is near the *Asah2* gene position and that no other local expression traits map to it.

Our design involves selection of a set of "anchor" expression traits. Gene *Asah2* is located near the center of Chromosome 19 and has a very strong local expression QTL (Table 3.2). We chose it as our first "anchor" gene expression trait. To diversify our collection of anchor genes, we chose three additional expression traits with local expression QTL. These three are *Lipo1*, *Lipo2*, and *4933413C19Rik* (Table 3.2). Together, the four anchor genes represent a variety of strong local expression trait LOD scores (from 60 to 1043 101) and demonstrate modest variability in their founder allele effects (Table 3.3). All four anchor genes are located near the middle of Chromosome 19 (Table 3.2).

We identified a set of 76 non-anchor local expression traits that map to the 20-Mb region centered on

the peak for Asah2, at 32.1 Mb. Each trait among the 76 maps to Chromosome 19 with a univariate LOD score of at least 10 (Table D.2).

Table 3.2: Annotations for four anchor genes.

Gene	Start	End	QTL peak position	LOD
Asah2	31.98	32.06	32.14	101.20
Lipo 1	33.52	33.76	33.67	85.46
Lipo2	33.72	33.76	33.02	77.21
4933413C19Rik	28.58	28.58	28.78	60.41

We estimated founder allele and covariate effects for every trait on Chromosome 19. For each of the 80 expression traits, we calculated fitted values for each subject with these estimated founder allele and covariate effects. We then calculated correlations between fitted values for pairs of traits. Our motivation for working with the fitted values vectors (instead of the estimated founder allele effects vectors) is that the fitted values approximately weight the allele effects by allele frequency. We anticipated that more similar two traits' founder allele effects would correspond, on average, to smaller pleiotropy test statistics. We base this expectation on findings from Macdonald and Long (2007) and King et al. (2012), who found that two traits that associate with a single pleiotropic QTL tended to have similar founder allele effects patterns for biallelic markers.

We performed two-dimensional QTL scans for  $4*76+\binom{4}{2}=310$  pairs. Each pair included one of the four anchor gene expression traits and either one of 76 non-anchor gene expression traits or one of the remaining three anchor gene expression traits. Our two-dimensional QTL scan encompassed a 1000 by 1000 marker grid from 18.1 Mb to 42.5 Mb on Chromosome 19. Each scan involved fitting  $1000 \times 1000 = 1,000,000$  models via generalized least squares. For a given ordered pair of markers, we used the bivariate linear mixed effects model and methods of Chapter 2. These methods are implemented in the R package qtl2pleio (Boehm, 2018b).

#### 3.2.3 Results

All four anchor traits demonstrate strong PWK ("G") allele effects. *Lipo2* and *Asah2* have similar patterns among allele effects (at their respective QTL peaks) (Table 3.3).

Each anchor gene has its own panel in Figure 3.7. Along the horizontal axis is Chromosome 19 position. The vertical axis is for pleiotropy test statistics. Each point corresponds to a local gene expression trait (paired with the appropriate anchor gene expression trait). Point color corresponds to the local gene's



Figure 3.7: Each anchor gene has its own panel. Along the horizontal axis is Chromosome 19 position. The vertical axis is for pleiotropy test statistic value. Each point corresponds to a local gene expression trait (paired with the anchor gene). Point color corresponds to the local gene's univariate LOD score, with lighter shades of blue denoting greater values of univariate LOD score. Vertical black bar denotes the anchor gene's position on Chromosome 19. All four panels reveal that points further from the anchor gene tend to show greater test statistic values. Additionally, the Lipo1 and Lipo2 panels offer an opportunity to compare the impact of anchor gene univariate LOD score on pleiotropy test statistic values.

Table 3.3: Founder allele effect estimates at Chromosome 19 QTL peak position.

Gene	Founder allele	Effect	Standard error
	A	-0.96	0.17
	В	1.01	0.19
	$\mathbf{C}$	0.14	0.17
Asah2	D	-1.16	0.17
Asanz	${f E}$	1.05	0.16
	$\mathbf{F}$	-0.61	0.20
	G	1.81	0.16
	H	-0.18	0.18
	A	0.29	0.18
	В	0.13	0.21
	$^{\mathrm{C}}$	0.28	0.20
Lipo1	D	0.23	0.19
Lipo1	${ m E}$	-0.17	0.18
	$\mathbf{F}$	-0.28	0.21
	G	2.55	0.19
	H	-0.72	0.19
	A	-0.10	0.18
	В	-0.28	0.23
	$^{\mathrm{C}}$	0.00	0.20
Lipo2	D	0.01	0.18
Lipoz	${ m E}$	-0.77	0.17
	F	-0.89	0.22
	G	2.65	0.18
	H	-0.70	0.20
	A	0.29	0.23
	В	0.76	0.24
	$\mathbf{C}$	0.81	0.21
4933413C19Rik	D	0.49	0.24
4500410013111h	${ m E}$	0.67	0.20
	$\mathbf{F}$	-0.53	0.22
	G	-1.65	0.18
	H	0.67	0.21

univariate LOD score, with lighter shades of blue denoting greater values of univariate LOD score. Vertical 1070 black bar denotes the anchor gene's position on Chromosome 19. All four panels reveal that points further 1071 from the anchor gene tend to show greater test statistic values. Additionally, because of their nearly identical 1072 positions, the Lipo1 and Lipo2 panels offer an opportunity to compare the impact of anchor gene univariate 1073 LOD score on pleiotropy test statistics. The difference in univariate LOD scores is modest, 85.5 for Lipo1 1074 vs. 77.2 for Lipo2. The effect of univariate LOD scores is most apparent when examining local expression 1075 traits that have strong univariate LOD scores. For example, near 32 Mb is a point with light blue color. 1076 The light blue indicates that it has a high univariate LOD score. Lipo2, which has the lower univariate 1077 LOD score, shows a pleiotropy test statistic just over 30 when paired with this local expression trait. Lipo 1 demonstrates a greater test statistic value, about 40, when paired with the same local expression trait.

Similarly, a local expression trait near 29 Mb has a strong univariate LOD score (near 100). We see that its pleiotropy test statistic values in the Lipo1 and Lipo2 panels reflect the difference in univariate LOD for the two anchor gene expression traits. The pleiotropy test statistic value is greater when paired with Lipo1, the anchor gene expression trait with greater univariate LOD (compared to Lipo2).

In comparing the plot for Asah2 with those of Lipo1, Lipo2, and 4933413C19Rik, we also see that Asah2, with the largest (101.2) of the four univariate LOD scores, demonstrates the steepest ascent of points as interlocus distance increases.

Analyses for all four anchor gene expression traits demonstrate that greater univariate LOD scores tend to correspond to greater values of the pleiotropy test statistic (Figure 3.8). The coloring of points reflects interlocus distance from the anchor gene. All four panels reveal a common pattern in the coloring of points. For a given univariate LOD value, those genes with greater interlocus distance tend to have greater values of the pleiotropy test statistic. Anchor gene 4933413C19Rik, due to its position on Chromosome 19, has multiple light blue points. Nearly all of these light blue points have large pleiotropy test statistics relative to their univariate LOD scores.

Figure 3.9 features four panels, one for each anchor gene. Each point corresponds to a pairing between the specified anchor and one of the 79 other gene expression traits. None of the four panels reveals a strong relationship between fitted values correlation and pleiotropy test statistics. There may be weak evidence for a downward trend in pleiotropy test statistics at larger values of fitted values correlation, as demonstrated by *Asah2*, *Lipo1*, and *Lipo2*.

## 3.2.4 Discussion

Our goal for this study was to characterize the impacts of univariate LOD score, inter-locus distance, and founder allele effects pattern similarities on pleiotropy test statistic values. Our study design, in which we examined 310 pairs of local gene expression traits on Chromosome 19, allowed us to interrogate both the effects of univariate association strength and the effects of inter-locus distance. We found that stronger univariate associations and greater inter-locus distances correspond to greater pleiotropy test statistic values (Figures 3.7 and 3.8). We expected these trends based on our simulation studies in Chapter 2.

Figure 3.9 revealed no strong relationship between fitted values correlations and pleiotropy test statistics. However, close examination of Figure 3.9 reveals the possibility that there is an interaction between 1) fitted values correlations and 2) univariate LOD scores. In every panel, those expression traits with stronger



Figure 3.8: Vertical axis denotes pleiotropy test statistic value, while horizontal axis denotes univariate LOD score. Each point corresponds to a single gene expression trait. Panels correspond to the anchor gene expression trait. The pleiotropy test statistics correspond to analyses involving a single gene expression trait and the specified anchor gene expression trait.



Figure 3.9: Vertical axis denotes the pleiotropy test statistic value, and horizontal axis indicates absolute value of the correlation between vectors of fitted values. Each point corresponds to a pairing between the specified anchor expression trait and one of the 79 other expression traits.

univariate associations tend to have steeper slopes between the conditional mean pleiotropy test statistic 1109 values and fitted values correlations. The plots weakly suggest that, at greater univariate LOD values, there 1110 is a greater (negative) relationship between fitted values correlation and pleiotropy test statistic value. 1111

We anticipated that more similar founder allele effects patterns would correspond to smaller values for the pleiotropy test statistic, when holding other factors constant. As we stated above, Macdonald and Long (2007) and King et al. (2012) argued that, for biallelic markers, two pleiotropic traits should have similar founder allele effects patterns. In our setting, it's unclear whether the markers are biallelic in the collection of eight founder lines.

We've demonstrated strong evidence in support of the roles of 1) univariate QTL LOD scores and 2) 1117 interlocus distances impacting pleiotropy test statistic values. Greater univariate QTL scores and greater 1118 interlocus distance lead to greater pleiotropy test statistics. Future research may clarify the impoact of 1119 founder allele effects patterns on pleiotropy test statistics. The fact that all four anchor traits had strong 1120 PWK effects (Table 3.3) limited our ability to fully define the impact of allele effects patterns on our test statistics. 1122

Throughout this study, we elected to use test statistic values rather than p-values as our measure of evidence supporting the separate QTL hypothesis. The primary reason for doing this is to avoid the compu-1124 tationally costly bootstrap sampling and two-dimensional QTL scans that we would need to get bootstrap p-values. 1126

We share our analysis R code (R Core Team, 2018) as a git repository at this URL: https://github.com/ 1127 fboehm/keller-2018-chr19-power. 1128

#### 3.3 Microbiome case study

#### 3.3.1 Introduction

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Recent technological innovations have fueled exploration of ecological relationships between gut microbiota and their hosts. Advances in mass spectrometry experimental methods have enabled high-throughput quan-1132 tification of lipid levels and protein concentrations. These developments, when coupled with experiments to quantify gut microbiota, have the potential to uncover new microbiome-host interactions. Such discov-1134 eries would lead to a more nuanced understanding of organismal biology and health implications of the gut 1135 microbiome. 1136

Previous research demonstrated that hosts and gut microbiota communicate with each other via small

Figure 3.10: Cholic acid chemical structure. From Wikipedia, https://upload.wikimedia.org/wikipedia/commons/2/21/Chols%C3%A4ure.svg.

molecule metabolites, including bile acids. The liver uses cholesterol to synthesize an array of bile acids.

These bile acids are secreted into the gut, where bacteria chemically transform some bile acids. One function of bile acids is to aid digestion by emulsification of dietary fats. While a portion of bile acids are lost in the feces, much of the secreted bile acids is reabsorbed in the distal gut. Finally, reabsorbed bile acids are transported via the circulatory system back to the liver.

Below, we use our pleiotropy test to identify a pleiotropic QTL that affects both the abundance level of a group of bacteria in the distal gut and plasma cholic acid levels in the host. While many questions remain

after our investigation, our identification of a single pleiotropic locus that affects these two phenotypes is an

## 3.3.2 Methods

important preliminary step for further investigations.

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As we describe in Kemis et al. (submitted), we analyzed data from 384 Diversity Outbred mice. Keller et al. (2018) analyzed data from many of these same mice. Specifically, we examined two microbiomerelated phenotypes, 1. plasma cholic acid and 2. *Turicibacter* abundance in the distal gut. Both traits map to Chromosome 8 (4.3 Mb and 5.7 Mb, respectively) in univariate QTL scans (Table 3.4). Our methods proceed in three ordered steps. First, we collect the biological samples. Then, we prepare and process the data. Finally, we perform our pleiotropy test.

Our sample collection involves three steps, all of which are done at the time of sacrifice (at age 22 weeks).

We obtained fecal samples from all mice immediately after a four-hour fast. We also obtained blood plasma

from every mouse at the time of sacrifice. Tail clippings provided DNA for host genotyping. 1156

by summing the appropriate genotype probabilities.

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we obtain genotype probabilities for all markers for all mice. In the other set of procedures, we obtain phenotypes. Obtaining phenotypes in this study involves processing both fecal samples and blood samples. As the first ordered step in inferring genotype probabilities, we extracted DNA from tail clippings and 1160 subjected it to SNP genotyping with the GigaMUGA microarray (Morgan et al., 2015). We inferred 36-state genotype probabilities from SNP genotype calls for every (autosomal) marker and every mouse. We used a hidden Markov model strategy developed by K. W. Broman (2012a) and K. W. Broman (2012b) and implemented in the R package qt12 (K. W. Broman, D. M. Gatti, et al., 2019). We treated these inferred genotype probabilities as known quantities in the analyses below. Lastly, we calculated founder allele dosages

Data preparation and processing involves two parallel sets of procedures. In one set of procedures,

Phenotype processing proceeds in parallel by separately processing fecal samples and blood samples. Processing of fecal samples to obtain microbial taxa counts involves multiple experimental and computational steps. We extracted microbiome DNA from fecal samples and subjected it to 16S ribosomal RNA gene sequencing to infer abundances of microbial taxa. Demultiplexed, paired-end FASTQ files resulted from the sequencing. We used the QIIME2 (version 2018.4) software package (Bolyen et al., 2018) for quality control and processing of sequence data. We applied the DADA2 software package (Callahan et al., 2016) to denoise sequencing reads and to identify de novo sub-operational taxonomic units. We aligned sequence variants with the software package mafft (Katoh and Standley, 2013). After FastTree-based phylogeny reconstruction (Price, Dehal, and Arkin, 2010), we assigned taxonomic classifications with classify-sklearn against the Greengenes OTUs reference sequences (DeSantis et al., 2006). We normalized sequencing data with cumulative sum scaling with MetagenomeSeq (Paulson, Pop, and Bravo, 2013). We limited study of microbiota-derived traits to those that we detected in at least 20% of subjects. The Turicibacter abundance trait is one element of the resulting core measurable microbiota.

Contemporaneously with the fecal sample processing, we subjected plasma samples to multiple experimental and computational steps to obtain traits for QTL mapping. After removing soluble proteins from each plasma sample, we analyzed each sample by mass spectrometry to measure abundances of pre-specified bile acids. Finally, we processed and normalized plasma bile acid measurements to obtain QTL analysis traits.

We then had the needed inputs for QTL mapping. We performed univariate QTL analyses for our microbiome-related traits. For each marker and each univariate phenotype we fitted a linear mixed effects

model (with a polygenic random effect), as implemented in the R package qt12 (K. W. Broman, D. M. 1187 Gatti, et al., 2019). We treated founder allele effects as additive and neglected possible interactions. We 1188 incorporated four covariates into the model: sex and three binary indicators for wave number. 1189

We then calculated LOD values comparing the univariate models' log-likelihoods at each marker to the log-likelihood of the model without founder allele dosages. In summarizing LOD peak results, we identified a small region on Chromosome 8 that contains LOD peaks for both Turicibacter abundance and plasma cholic acid levels.

We use the R package qt12 to estimate founder allele effects at Chromosome 8 markers with the univariate linear mixed effects model. 1195

We then had the inputs needed for our pleiotropy test: founder allele probabilities for each mouse at every marker and two traits that map to a single genomic region. We performed a test of pleiotropy vs. separate QTL for our two traits, Turicibacter abundance and plasma cholic acid levels, using the methods of Chapter 2. To determine statistical significance, we performed a parametric bootstrap analysis to acquire 1000 bootstrap samples. With the collection of 1000 bootstrap test statistic values, we calculated a bootstrap p-value as the proportion of the 1000 test statistics that were at least as large as the true test statistic. Calculation of a bootstrap p-value is the last step in our hypothesis test for pleiotropy vs. separate QTL.

#### 3.3.3 Results

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phenotype	chromosome	position	LOD
	1	91.61	5.37
	3	40.53	5.80
plasma cholic acid	7	122.19	6.83
	8	4.32	6.52
	12	16.60	5.24
	2	17.20	5.40
Turicibacter abundance	8	5.68	7.22
	12	76.34	5.17

Table 3.4: Genome-wide LOD peaks greater than 5 for plasma cholic acid levels and *Turicibacter* abundance. Both traits map to approximately the same region on Chromosome 8. Chromosome positions are in Mb units.

Both plasma cholic acid and Turicibacter abundance demonstrate multiple univariate QTL across the genome. Each trait also maps to a 1.4-Mb region on Chromosome 8. Because these two traits map to a single genomic region, we elected to study them further.

Univariate LOD plots for the two traits reveal broad LOD peaks on Chromosome 8 (Figure 3.11). Plasma

#### Plasma cholic acid founder allele effects



(a) Plasma cholic acid founder allele effects over the scan interval.

#### Turicibacter abundance founder allele effects



(b) Turicibacter abundance founder allele effects over the scan interval.

Figure 3.11: Founder allele effects and LOD plots for our two traits over the Chromosome 8 region. Both traits demonstrate QTL peaks between 4 and 8 Mb and similar patterns of founder allele effects.

cholic acid's peak starts about 4 Mb and extends to approximately 6.5 Mb. *Turicibacter* abundance has an even broader peak, starting about 4 Mb and extending to 7.5 Mb. Although the two traits' peak position point estimates differ by 1.4 Mb, the univariate LOD plots demonstrate highly similar patterns for the two traits.

It is unclear from the univariate LOD plots whether there are two nearby QTLs that both affect *Turicibacter* abundance (Figure 3.11). Consistent with the possibility of two peaks is the observation that the *Turicibacter* peak extends further to the right than does the plasma cholic acid peak.

Founder allele effects plots for the two traits demonstrate similarities in the relative magnitudes of the eight effects. Specifically, the plasma cholic acid founder allele effects, at 5Mb, has AJ, NZO, CAST, and 129 above average, while WSB is well below average. Similarly, *Turicibacter* abundance has founder allele effects at 5Mb with AJ and 129 above average and WSB below average.

To explore relationships between the two traits, we created a scatter plot. The scatter plot of plasma cholic acid levels and *Turicibacter* abundance levels demonstrates modest correlation (Pearson correlation coefficient = 0.5) (Figure 3.12). *Turicibacter* was unobserved in fecal samples from 192 of 384 mice. After our data processing steps (described above), these 192 mice all have the smallest possible value of the *Turicibacter* abundance trait. Because these 192 mice possess a range of plasma cholic acid values, they appear as a vertical "line" on the left-hand side of the scatter plot.

Once we examined the univariate QTL scan results, we had the needed inputs for a bivariate scan; namely, two traits that map to a single genomic region and genotype probabilities for all mice and all markers. We performed a bivariate QTL scan over a 180-marker region on Chromosome 8. The profile LOD plot over our two-dimensional scan region reveals broad peaks for both traits' profile LODs (Figure 3.13). Plasma cholic acid has a peak that begins about 4 Mb and extends to approximately 6.5 Mb. *Turicibacter* abundance has a broader peak, with endpoints near 4 Mb and 7.5 Mb. Here, but not in the univariate LOD plots, one sees what appears to be a second peak in the *Turicibacter* abundance phenotype that begins near 7.5 Mb and ends near 8.7 Mb.

We used the R package qtl2pleio (Boehm, 2018b) to calculate the likelihood ratio test statistic,  $\Lambda = 0.45$ .

We determined the bootstrap p-value to be 0.531 with 1000 bootstrap samples. Thus, we failed to reject the null hypothesis of pleiotropy.

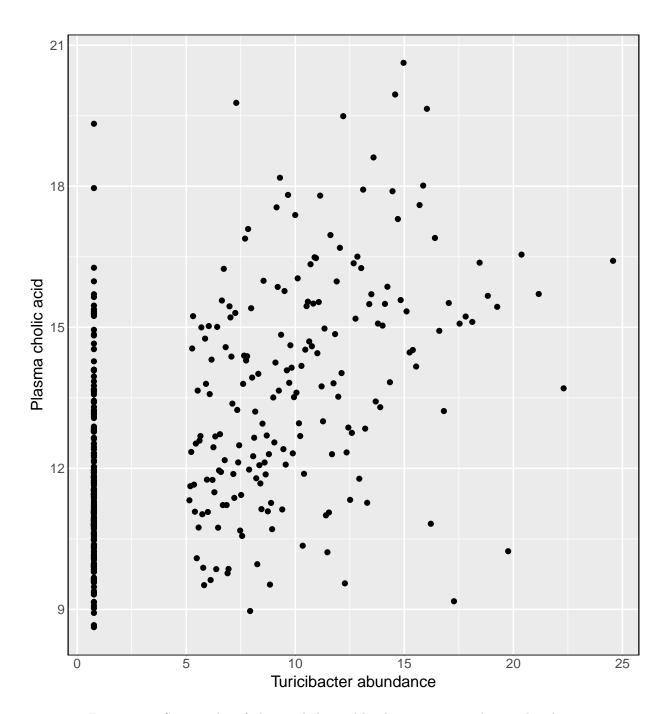


Figure 3.12: Scatter plot of plasma cholic acid levels against Turicibacter abundance

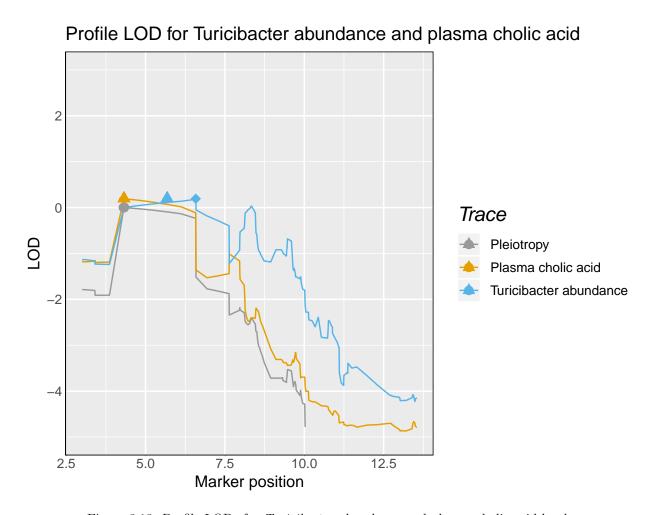


Figure 3.13: Profile LODs for Turicibacter abundance and plasma cholic acid levels.

#### 3.3.4 Discussion

Results from our analyses above, including the pleiotropy test, are consistent with a single pleiotropic QTL affecting both *Turicibacter* abundance and plasma cholic acid levels. The similarity of founder allele effects patterns (Figure 3.11) is also consistent with a single pleiotropic QTL (King et al., 2012; Macdonald and Long, 2007).

While our results indicate presence of a single pleiotropic QTL, they leave many questions unanswered.

For example, it would be interesting to know if one trait mediates the effects of the QTL on the other trait.

Statistical mediation analyses (Chick et al., 2016), like those discussed earlier in Chapter 3, may clarify
this issue. Both possibilities are biologically plausible: 1. that plasma cholic acid levels affect *Turicibacter*abundance and 2. that *Turicibacter* abundance affects plasma cholic acid levels.

A consideration of cholic acid biology illuminates this biological plausibility. Plasma cholic acid levels, which are related to absorption rates of cholic acid from the distal gut, may be influenced by cholic acid production rates in the liver. This, in turn, might affect gut colonization by *Turicibacter*. Alternatively, the second possibility above is also biologically plausible, because, for example, *Turicibacter* may affect plasma cholic acid levels by chemically transforming cholic acid while it's in the gut. Mediation analyses and causal model selection tests (Neto et al., 2013) may clarify the biological interactions that affect plasma cholic acid levels and *Turicibacter* abundance in the distal gut.

A second issue that arose in our analysis is the possibility of two nearby peaks for the *Turicibacter* abundance trait. While the univariate LOD plot doesn't indicate two *Turicibacter* peaks (Figure 3.11), the profile LOD plot suggests that there is a second *Turicibacter* abundance peak from approximately 8 to 8.7 Mb. We might clarify this possibility by examining statistical models that explicitly incorporate two QTL for *Turicibacter* while constraining plasma cholic acid levels to a single QTL (Schadt et al., 2005). Distinguishing whether there are two QTL that affect *Turicibacter* abundance offers insights into the trait's genetic architecture and, by suggesting candidate causal genes, may inform subsequent experiments.

In this microbiome study, we've illustrated another scientific application of our pleiotropy test. We plan to perform additional analyses, including mediation studies and causal model selection tests, with these data. Our pleiotropy test tells us that the data are consistent with presence of a single QTL affecting both *Turicibacter* abundance and plasma cholic acid levels. This insight serves as a starting point for follow-up studies into the directions of intertwined causal relationships between plasma cholic acid and *Turicibacter* abundance.

### Chapter 4

# Computing vignettes

### 1268 4.1 Pleiotropy testing

Our setting involves a pair of traits,  $Y_1$  and  $Y_2$ , each of which individually (univariately) maps to a single genomic region.  $Y_1$  and  $Y_2$  are both measured on the same subjects. The exact definition of a genomic region is imprecise; in practice, it may be as large as 4 or 5 Mb. We seek to distinguish whether  $Y_1$  and  $Y_2$  associations (in the genomic region of interest) arise due to a single QTL or whether there are two two distinct loci, each of which associates with exactly one of the two traits. We recognize that more complicated association patterns are possible, but we neglect them in this test.

### 1275 4.1.1 Installing qtl2pleio

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1276 We install qtl2pleio from github via the devtools R package, which is available from CRAN.

To install qtl2pleio, use install\_github() from the devtools package.

```
install.packages("devtools")
devtools::install_github("fboehm/qtl2pleio")
```

You may also wish to install R/qtl2 and the qt12convert package. We will use both below.

```
install.packages(c("qt12"), repos = "http://rqtl.org/qt12")
```

The above line only needs to be run once on a given computer (unless you wish to install a newer version of the package).

We then load the library into our R session with the library command:

```
library(qtl2pleio)
```

We also load the qtl2 package with the library command.

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```
library(qtl2)
```

### $_{\scriptscriptstyle{283}}$ 4.1.2 Reading data from qtl2data repository on github

We'll consider the DOex data in the qtl2data repository. We'll download the DOex.zip file before calculating founder allele dosages.

```
file <- paste0("https://raw.githubusercontent.com/rqtl/", "qtl2data/master/D0ex/D0ex.zip")
D0ex <- read_cross2(file)</pre>
```

Let's calculate the founder allele dosages from the 36-state genotype probabilities.

```
probs <- calc_genoprob(D0ex)
pr <- genoprob_to_alleleprob(probs)</pre>
```

We now have an allele probabilities object stored in pr.

```
names(pr)

#> [1] "2" "3" "X"

dim(pr$^3^)

#> [1] 261 8 102
```

- We see that **pr** is a list of 3 three-dimensional arrays one array for each of 3 chromosomes.
- We now have an allele probabilities object stored in pr.

```
names(pr)

#> [1] "2" "3" "X"

dim(pr$^3^)

#> [1] 261 8 102
```

We see that pr is a list of 3 three-dimensional arrays - one array for each of 3 chromosomes.

#### 4.1.3 Kinship calculations

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For our statistical model, we need a kinship matrix. Although we don't have genome-wide data - since
we have allele probabilities for only 3 chromosomes - let's calculate a kinship matrix using "leave-onechromosome-out". In practice, one would want to use allele probabilities from a full genome-wide set of
markers.

```
kinship <- calc_kinship(probs = pr, type = "loco")</pre>
```

```
str(kinship)
#> List of 3
   £ 2: num [1:261, 1:261] 0.6934 0.0705 0.2356 0.0558 0.0513 ...
     ..- attr(*, "n_pos") = int 195
     ..- attr(*, "dimnames")=List of 2
#>
     ....£ : chr [1:261] "1" "4" "5" "6" ...
#>
     .. ..£ : chr [1:261] "1" "4" "5" "6" ...
   £ 3: num [1:261, 1:261] 0.6662 0.0647 0.2024 0.1129 0.0772 ...
     ..- attr(*, "n_pos")= int 220
     ..- attr(*, "dimnames")=List of 2
     .. ..£ : chr [1:261] "1" "4" "5" "6" ...
     .. ..£ : chr [1:261] "1" "4" "5" "6" ...
   £ X: num [1:261, 1:261] 0.4871 0.0831 0.1953 0.1043 0.1125 ...
     ..- attr(*, "n_pos")= int 229
#>
#>
     ..- attr(*, "dimnames")=List of 2
     ....£ : chr [1:261] "1" "4" "5" "6" ...
   ....£ : chr [1:261] "1" "4" "5" "6" ...
```

We see that kinship is a list containing 3 matrices. Each matrix is 261 by 261 - where the number of subjects is 261 - and symmetric.

#### 4.1.4 Statistical model

- Before we simulate phenotype data, we first specify our statistical model.
- We use the model:

$$vec(Y) = Xvec(B) + vec(G) + vec(E)$$

where Y is a n by 2 matrix, where each row is one subject and each column is one quantitative trait. X is a 2n by 2f design matrix containing n by f allele probabilities matrices for each of two (possibly identical) markers. Thus, X is a block-diagonal matrix, with exactly two n by f blocks on the diagonal. B is a f by 2 matrix. "vec" refers to the vectorization operator. "vec(B)", where B is a f by 2 matrix, is, thus, a (column) vector of length 2f that is formed by stacking the second column of B beneath the first column of B.

G is a matrix of random effects. We specify its distribution as matrix-variate normal with mean being a n by 2 matrix of zeros, covariance among row vectors a n by n kinship matrix, K, and covariance among column vectors a 2 by 2 genetic covariance matrix,  $V_q$ .

In mathematical notation, we write:

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$$G \sim MN_{\text{n by 2}}(0, K, V_q)$$

We also need to specify the distribution of the E matrix, which contains the random errors. E is a random n by 2 matrix that is distributed as a matrix-variate normal distribution with mean being the n by 2 zero matrix, covariance among row vectors  $I_n$ , the n by n identity matrix, and covariance among columns the 2 by 2 matrix  $V_e$ .

$$E \sim MN_{\text{n by 2}}(0, I_n, V_e)$$

In practice, we typically measure the phenotype matrix Y. We also treat as known the design matrix X and the kinship matrix K. We then infer the values of B,  $V_g$ , and  $V_e$ .

#### 4.1.5 Simulating phenotypes with qtl2pleio::sim1

The function to simulate phenotypes in qtl2pleio is sim1. By examining its help page, we see that it takes
five arguments. The help page also gives the dimensions of the inputs.

```
# set up the design matrix, X

pp <- pr[[2]] #we'll work with Chr 3's genotype data</pre>
```

```
dim(pp)
#> [1] 261 8 102
```

We prepare a block-diagonal design matrix X that contains two nonzero blocks on the diagonal, one for each trait. We use here a function from the gemma2 R package to set up the needed matrix.

```
# Next, we prepare a design matrix X

X <- gemma2::stagger_mats(pp[, , 50], pp[, , 50])

dim(X)

#> [1] 522 16
```

```
# assemble B matrix of allele effects
-1, 1, 1, 1), nrow = 8, ncol = 2, byrow = FALSE)
# verify that B is what we want:
В
#>
       [,1] [,2]
#> [1,] -1 -1
#> [2,] -1
             -1
#> [3,] -1
            -1
#> [4,] -1
            -1
            1
#> [5,] 1
#> [6,]
       1 1
#> [7,]
       1 1
#> [8,] 1 1
# set.seed to ensure reproducibility
set.seed(2018 - 1 - 30)
# call to sim1
Ypre \leftarrow sim1(X = X, B = B, Vg = diag(2), Ve = diag(2), kinship = kinship[[2]])
Y <- matrix(Ypre, nrow = 261, ncol = 2, byrow = FALSE)
rownames(Y) <- rownames(pp)</pre>
colnames(Y) <- c("tr1", "tr2")</pre>
```

Let's perform univariate QTL mapping for each of the two traits in the Y matrix.

```
s1 <- scan1(genoprobs = pr, pheno = Y, kinship = kinship)
```

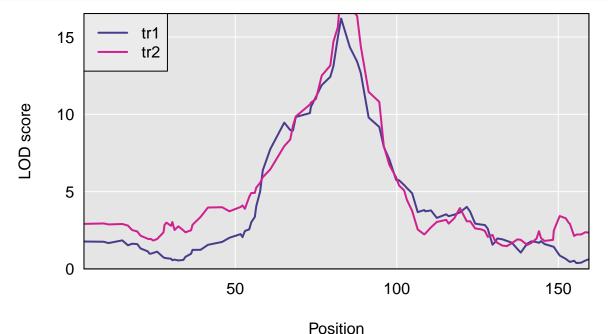
Here is a plot of the results.

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We see that the two traits share a peak on Chr 3.

And here are the observed QTL peaks with LOD > 8. In practice, we could do a permutation test to determine a threshold for family-wise error rate control.

# Perform two-dimensional scan as first step in pleiotropy vs. separate QTL hypothesis test

We now have the inputs that we need to do a pleiotropy vs. separate QTL test. We have the founder allele dosages for one chromosome, *i.e.*, Chr 3, in the R object pp, the matrix of two trait measurements in Y, and a LOCO-derived kinship matrix. We also specify, via the start\_snp argument, the starting point for the two-dimensional scan within the array of founder allele dosages. Here, we choose the 38th marker in the array as the starting point. Via the n\_snp argument, we specify the number of markers to include in the two-dimensional scan. Here, we input 25, so that we fit the bivariate linear mixed effects model at 25\*25 = 625 ordered pairs of markers. In practice, we usually use between 100 and 300 markers for most two-dimensional scans.

Lastly, we specify the number of cores to use, with the n\_cores argument. We set it to 1 here, to ensure
that the vignette can be run by CRAN. However, in practice, you may wish to increase the number of cores
to accelerate computing.

```
out <- scan_pvl(probs = pp, pheno = Y, kinship = kinship$`3`,
    start_snp = 38, n_snp = 25, n_cores = 1)
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
```

The number of cores available will vary by computer. For example, on my Macbook pro computer, with 16GB RAM, I have access to 8 cores. If I use all 8, I can't do other computing tasks, so I often set n\_cores to 7.

To check how many cores are available on your computer, run this code.

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```
parallel::detectCores()
```

Create a profile LOD plot to visualize results of two-dimensional scan To visualize results from our two-dimensional scan, we calculate profile LOD for each trait. The code below makes use of the R package ggplot2 to plot profile LODs over the scan region.

```
out
#> # A tibble: 625 x 3
#>
      Var1
                         Var2
                                      loglik
#>
      <chr>
                         <chr>
                                       <db1>
   1 JAX00108034
                         JAX00108034
                                       -866.
   2 backupUNC031096286 JAX00108034
                                      -863.
   3 JAX00525579
                         JAX00108034
                                      -865.
   4 JAX00525718
                         JAX00108034
                                      -865.
   5 UNC030088171
                         JAX00108034
                                      -864.
   6 backupUNC030474070 JAX00108034
                                      -864.
   7 backupUNC030474244 JAX00108034
                                      -863.
   8 UNC030103315
                         JAX00108034
                                      -862.
   9 UNC030107226
                         JAX00108034
                                      -861.
#> 10 JAX00527615
                         JAX00108034
                                      -861.
#> # ... with 615 more rows
```

We see that out is a 625 by 3 tibble, as expected. The first two columns contain the marker ids for each ordered pair of markers. The third column contains the log-likelihood values.

```
library(dplyr)

#>

#> Attaching package: 'dplyr'

#> The following objects are masked from 'package:stats':

#>

#> filter, lag

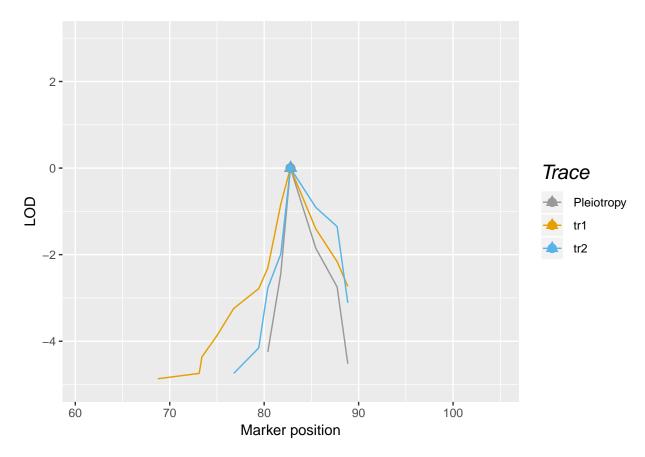
#> The following objects are masked from 'package:base':

#>

#> intersect, setdiff, setequal, union

out %>% tidy_scan_pvl(DOex$pmap$`3`) %>% add_intercepts(intercepts_univariate = c(82.8, 82.8)) %>% plot_pvl(phenames = c("tr1", "tr2"))

#> Warning: Removed 49 rows containing missing values (geom_path).
```



We first pass the scan\_pvl output, i.e., out, to the function tidy\_scan\_pvl to add the physical map coordinates to the out tibble. We pipe that output to the add\_intercepts function. This function adds columns for the univariate peak positions. Note that we need to specify the univariate peak positions by hand. In the current case, the two traits have identical peak positions.

Finally, the output of add\_intercepts is piped to plot\_pvl. This function uses ggplot2 functions to create a profile LOD plot with three "traces": one for each trait and a third for all ordered pairs under the pleiotropy hypothesis.

Calculate the likelihood ratio test statistic for pleiotropy v separate QTL We use the function calculate the likelihood ratio test statistic value for the specified traits and specified genomic region.

```
(lrt <- calc_lrt_tib(out))
#> [1] 0
```

#### Bootstrap analysis to get p-values

The calibration of test statistic values to get p-values uses bootstrap methods because we don't know the theoretical distribution of the test statistic under the null hypothesis. Thus, we use a bootstrap approach to obtain an empirical distribution of test statistic values under the null hypothesis of the presence of one pleiotropic locus.

We will use the function boot\_pvl from our package qtl2pleio.

We use a parametric bootstrap strategy in which we first use the studied phenotypes to infer the values of model parameters. Once we have the inferred values of the model parameters, we simulate phenotypes from the pleiotropy model (with the inferred parameter values).

A natural question that arises is "which marker's allele probabilities do we use when simulating phenotypes?" We use the marker that, under the null hypothesis, *i.e.*, under the pleiotropy constraint, yields the greatest value of the log-likelihood.

Before we call boot\_pvl, we need to identify the index (on the chromosome under study) of the marker
that maximizes the likelihood under the pleiotropy constraint. To do this, we use the qtl2pleio function
find\_pleio\_peak\_tib.

```
(pleio_index <- find_pleio_peak_tib(out, start_snp = 38))
#> loglik13
#> 50
```

```
set.seed(2018 - 11 - 25)
system.time(b_out <- boot_pvl(probs = pp, pheno = Y, pleio_peak_index = pleio_index,
    kinship = kinship$`3`, nboot_per_job = 10, start_snp = 38,
    n_snp = 25))
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> starting covariance matrices estimation with data from 261 subjects.
```

```
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
#> starting covariance matrices estimation with data from 261 subjects.
#> covariance matrices estimation completed.
      user system elapsed
   80.916
           4.184 85.332
```

lyzed. Here, we set nboot\_per\_job = 10, so we expect to see returned a numeric vector of length 10, where
each entry is a LRT statistic value from a distinct bootstrap sample.

Finally, we determine a bootstrap p-value in the usual method. We treat the bootstrap samples' test
statistics as an empirical distribution of the test statistic under the null hypothesis of pleiotropy. Thus, to
get a p-value, we want to ask "What is the probability, under the null hypothesis, of observing a test statistic
value that is at least as extreme as that which we observed?"

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The argument nboot\_per\_job indicates the number of bootstrap samples that will be created and ana-

```
b_out
#> [1] 2.8881948 0.0000000 0.9943472 0.0000000 1.1553322 0.6764714 0.0000000
#> [8] 1.1446433 0.0000000 1.0460109
(pvalue <- mean(b_out >= lrt))
#> [1] 1
```

In practice, one would want to use many more bootstrap samples to achieve an empirical distribution that is closer to the theoretical distribution of the test statistic under the null hypothesis.

However, if one wants to perform analyses with a reasonable number - say 400 - bootstrap samples, this will take a very long time - many days - on a single laptop computer. We have used a series of computer clusters that are coordinated by the University of Wisconsin-Madison's Center for High-throughput Computing (http://chtc.cs.wisc.edu). We typically are able to analyze 1000 bootstrap samples in less than 24 hours with this service.

#### $_{\circ}$ 4.1.7 Session info

```
devtools::session_info()
#> - Session info ----
    setting value
    version R version 3.5.3 (2019-03-11)
             macOS Mojave 10.14.3
             x86_64, darwin15.6.0
#>
    system
    ui
             RStudio
    language (EN)
#>
    collate en_US.UTF-8
             en_US.UTF-8
#>
    ctype
             America/Chicago
             2019-03-17
    date
#>
   - Packages ----
#>
    ! package
                      * version
                                   date
                                               lib
                                   2017-04-11 [1]
      assert that
                        0.2.0
#>
                        1.1.3
#>
      backports
                                   2018-12-14 [1]
                                   2018-05-29 [1]
#>
      bit
                        1.1-14
#>
                        0.9 - 7
                                   2017-05-08 [1]
      bit64
      blob
                        1.1.1
                                   2018-03-25 [1]
                                   2018-07-25 [1]
                        0.68-2
#>
      broman
                        3.2.0
                                   2019-03-15 [1]
#>
      callr
                                   2018-09-25 [1]
#>
      cli
                        1.0.1
```

#>	colorspace	1.4-0	2019-01-13	[1]
#>	commonmark	1.7	2018-12-01	[1]
#>	crayon	1.3.4	2017-09-16	[1]
#>	curl	3.3	2019-01-10	[1]
#>	data.table	1.12.0	2019-01-13	[1]
#>	DBI	1.0.0	2018-05-02	[1]
#>	desc	1.2.0	2018-05-01	[1]
#>	devtools	* 2.0.1	2018-10-26	[1]
#>	digest	0.6.18	2018-10-10	[1]
#>	dplyr	* 0.8.0.1	2019-02-15	[1]
#>	evaluate	0.13	2019-02-12	[1]
#>	fansi	0.4.0	2018-10-05	[1]
#>	formatR	1.6	2019-03-05	[1]
#>	fs	1.2.6	2018-08-23	[1]
#>	gemma2	0.0.1.1	2019-03-13	[1]
#>	ggplot2	3.1.0	2018-10-25	[1]
#>	glue	1.3.1	2019-03-12	[1]
#>	gtable	0.2.0	2016-02-26	[1]
#>	hms	0.4.2	2018-03-10	[1]
#>	htmltools	0.3.6	2017-04-28	[1]
#>	jsonlite	1.6	2018-12-07	[1]
#>	knitr	1.22	2019-03-08	[1]
#>	labeling	0.3	2014-08-23	[1]
#>	lattice	0.20-38	2018-11-04	[1]
#>	lazyeval	0.2.2	2019-03-15	[1]
#>	${\it magrittr}$	1.5	2014-11-22	[1]
#>	MASS	7.3-51.1	2018-11-01	[1]
#>	${\it Matrix}$	1.2-15	2018-11-01	[1]
#>	memoise	1.1.0	2017-04-21	[1]
#>	microbenchmark	1.4-6	2018-10-18	[1]

#>	$\mathit{munsell}$	0.5.0	2018-06-12
#>	mutnorm	1.0-10	2019-03-05
#>	packrat	0.5.0	2018-11-14
#>	pillar	1.3.1	2018-12-15
#>	pkgbuild	1.0.2	2018-10-16
#>	pkgconfig	2.0.2	2018-08-16
#>	pkgload	1.0.2	2018-10-29
#>	plyr	1.8.4	2016-06-08
#>	prettyunits	1.0.2	2015-07-13
#>	process x	3.3.0	2019-03-10
#>	progress	1.2.0	2018-06-14
#>	ps	1.3.0	2018-12-21
#>	purrr	0.3.2	2019-03-15
#>	qtl2	* 0.19-7	2019-03-17
#>	P qtl2pleio	* 0.1.2.900	1 2019-03-17
#>	<i>R6</i>	2.4.0	2019-02-14
#>	rc $m$ d $c$ h $e$ c $k$	1.3.2	2018-11-10
#>	V Rcpp	1.0.0.3	2019-03-17
#>	RcppEigen	0.3.3.5.0	2019-03-08
#>	readr	1.3.1	2018-12-21
#>	remotes	2.0.2	2018-10-30
#>	rlang	0.3.1	2019-01-08
#>	rmarkdown	* 1.11	2018-12-08
#>	roxygen2	6.1.1	2018-11-07
#>	rprojroot	1.3-2	2018-01-03
#>	$\mathit{RSQLite}$	2.1.1	2018-05-06
#>	rstudioapi	0.9.0	2019-01-09
#>	scales	1.0.0	2018-08-09
#>	session info	1.1.1	2018-11-05
#>	stringi	1.4.3	2019-03-12

#>	stringr	1.4.0	2019-02-10 [1]	
#>	testthat	2.0.1	2018-10-13 [1]	
#>	tibble	2.1.1	2019-03-16 [1]	
#>	tidyselect	0.2.5	2018-10-11 [1]	
#>	usethis	* 1.4.0	2018-08-14 [1]	
#>	utf8	1.1.4	2018-05-24 [1]	
#>	withr	2.1.2	2018-03-15 [1]	
#>	xfun	0.5	2019-02-20 [1]	
#>	xml2	1.2.0	2018-01-24 [1]	
#>	xopen	1.0.0	2018-09-17 [1]	
#>	yaml	2.2.0	2018-07-25 [1]	
#>	source			
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#> [1] /Library/Frameworks/R.framework/Versions/3.5/Resources/library

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#> V -- Loaded and on-disk version mismatch.

#> P -- Loaded and on-disk path mismatch.
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### 1391 4.2 Recla analysis

### 4.3 Cluster computing for bootstrap test

### • Chapter 5

## Conclusions

I've successfully developed a pleiotropy test for multiparental populations. I discussed our new methods 1395 in Chapter 2. In Chapter 3, we illustrated the test's use in three vignettes. The first vignette compared 1396 pleiotropy testing with mediation analysis in the dissection of expression trait QTL hotspots. I learned that the pleiotropy test provides information about the number of underlying QTL even when mediation analyses 1398 don't identify intermediates. The second vignette examined my test's power to detect separate QTL in pairs 1399 of local expression traits. I learned that both interlocus distance and univariate LOD scores impact test 1400 statistic values. In the last vignette, I applied my test to two gut microbiome-related traits. From this 1401 analysis, I learned that the two traits share a pleiotropic QTL and, thus, it is reasonable to conduct further 1402 causal modeling studies for these two traits. Chapter 4 demonstrates features of the 'qtl2pleio' R package. 1403 This package implements my pleiotropy test and uses the data structures in the R package 'qtl2' (K. W. 1404 Broman, D. M. Gatti, et al., 2019). 1405

### 5.1 A multivariate pleiotropy test

Pleiotropy tests for two traits at a time have a valuable role in complex trait genetics. However, to fully use the tens of thousands of experimentally measured traits, we need to consider testing more than two traits at a time. Suppose that five traits map to a single region spanned by 100 markers. One might perform a series of  $\binom{5}{2} = 10$  bivariate QTL scans and 10 pairwise tests for pleiotropy. Each bivariate scan would require  $100^2 = 10,000$  model fits by generalized least squares. Alternatively, one could perform a d-variate QTL scan, with d = 5 in this case. With the results of the d-variate scan, a variety of statistical

hypotheses could be tested. For example, one could formulate a test for the null hypothesis that all five traits share a pleiotropic QTL against the alternative that the first two traits share a single QTL and the last three traits share a distinct, pleiotropic QTL. The d-variate scan over the 100-marker region, would require  $100^d = 100^5 = 10$  billion model fits via generalized least squares. With distributed computing resources, including the resources at the University of Wisconsin's Center for High-throughput Computing, this is not an unreasonable volume of computing. The use of C++ for generalized least squares calculations decreases the computing time for each model fit.

### 5.2 X chromosome

5.3 Sensitivity analysis for unmeasured confounding in mediation
analysis

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Appendices

1658

# $_{\tiny 1659} \ \textbf{Appendix} \ \textbf{A}$

# Molecular biology primer

### A.1 Cell division

Our goals in this section are to explain meiosis and to understand why recombinations "accumulate" over multiple generations in subjects like Diversity Outbred mice.

### 1664 A.2 Central dogma of molecular biology

Appendix B

 $_{\tiny{1666}}$  Statistical inference primer

#### B.1 Overview of statistics

One characterization of statistics is that it is the science of learning about natural phenomena. The process 1668 of learning about natural phenomena proceeds in a cyclical fashion. One first posits a "model" for a natural 1669 phenomenon. She designs an experiment to measure a quantity related to the phenomenon of interest. 1670 She then collects data, summarizes it as a statistic, and performs a test of competing hypotheses before 1671 updating her hypothesis about the natural phenomenon. The newly updated hypothesis replaces the original 1672 hypothesis in the second iteration of the cycle. 1673 For example, we might wish to study the genetics of body weight in mice. We first posit the existence 1674 of body weight quantitative trait loci (QTL), which are regions of the genome that affect mouse body 1675 weight. We quantitatively state the competing possibilities as the null hypothesis that there is no QTL against the alternative hypothesis of presence of a QTL. We then design an experiment, perhaps using 1677 genetically diverse mice, like those from the Diversity Outbred mouse population. We measure body weight in, say, 100 Diversity Outbred mice and obtain genome-wide genetic data from each. We then summarize 1679 our observations by performing multiple instances of a statistical technique called "linear regression". We 1680

#### B.2 Maximum likelihood methods

1681

#### B.3 Restricted maximum likelihood methods

perform statistical hypothesis tests to quantify the evidence against the null hypothesis.

- B.4 Genotype inference with expectation-maximization
- B.5 Genotype inference with hidden Markov models

# $^{_{1696}}\ \mathbf{Appendix}\ \mathbf{C}$

# Supplementary materials for Chapter

688 2

Table C.1: Eight founder lines and their one-letter abbreviations.

Founder allele	One-letter abbreviation
A/J	A
C57BL/6J	В
129S1/SvImJ	С
NOD/ShiLtJ	D
NZO/H1LTJ	E
Cast/EiJ	F
PWK/PhJ	G
WSB/EiJ	Н

Table C.2: Both "hot plate latency" and "percent time in light" demonstrate multiple QTL peaks with LOD scores above 5.

phenotype	chr	pos	LOD score
percent time in light	8	55.28	5.27
hot plate latency	8	57.77	6.22
percent time in light	9	36.70	5.42
hot plate latency	9	46.85	5.22
percent time in light	11	63.39	6.46
hot plate latency	12	43.52	5.13
percent time in light	15	15.24	5.67
hot plate latency	19	47.80	5.48

## hot plate latency vs. percent time in light

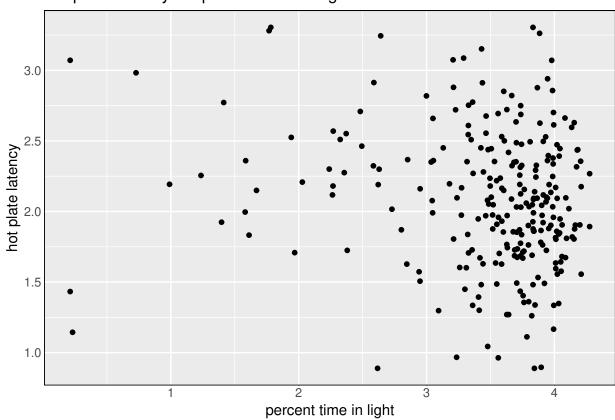
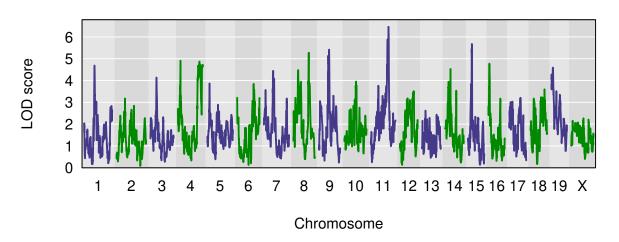


Figure C.1: Scatter plot of "hot plate latency" against "percent time in light", after applying logarithm transformations and winsorizing both traits.

## percent time in light



### hot plate latency



Figure C.2: Genome-wide QTL scan for percent time in light reveals multiple QTL, including one on Chromosome 8.

## ${}_{{}^{1689}}\ \mathbf{Appendix}\ \mathbf{D}$

# Supplementary materials for Chapter

**3** 

Table D.1: LOD peak positions and peak heights for 147 expression traits that map to the Chromosome 2 expression trait hotspot. We see that some transcript levels have LOD scores, per our calculations, below the 7.18 genome-wide threshold. We believe that this is due to differences in statistical modeling between our analyses and those of Keller et al. (2018).

Gene	Peak position	LOD
Mtfp1	163.52	17.79
Slc12a7	163.58	8.30
Gpa33	163.58	26.38
Tmem25	163.58	11.26
Klhl29	163.58	11.03
Slc9a3r1	163.58	8.40
Kif1c	163.58	11.12
Gata4	163.58	8.72
Ppp2r5b	163.58	7.80
Vil1	163.58	26.48
Aldh4a1	163.58	9.38
Cotl1	163.58	16.25
Tmprss4	163.58	18.30

Zfp750       163.58       7.83         Svop       163.58       10.12         Abcb4       163.58       16.59         Ccnjl       163.58       6.70         Sephs2       163.58       27.21         Pcdh1       163.58       12.48         Fat1       163.58       7.49         Sox4       163.58       14.71         Gm8206       163.58       10.47         Clcn5       164.02       10.49         Slc6a8       164.02       8.35         Bcm01       164.02       47.06         Sec14l2       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       13.70         Cpd       164.02       15.20         Muc13       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg312       164.02       13.70         Agap2       164.02       33.99         Plxna2       <	Fhod3	163.58	17.62
Abcb4       163.58       16.59         Ccnjl       163.58       6.70         Sephs2       163.58       27.21         Pcdh1       163.58       12.48         Fat1       163.58       7.49         Sox4       163.58       14.71         Gm8206       163.58       11.33         Gm8492       163.58       10.47         Clcn5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       13.70         Cpd       164.02       33.97         Cpd       164.02       15.20         Muc13       164.02       15.20         Muc13       164.02       10.39         Tff3       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       13.70         Afg3l2       164.02       33.99         Plxna2       164.02       33.99         Plxna2	Zfp750	163.58	7.83
Ccnjl       163.58       6.70         Sephs2       163.58       27.21         Pcdh1       163.58       12.48         Fat1       163.58       7.49         Sox4       163.58       14.71         Gm8206       163.58       10.47         Clcn5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       15.20         Muc13       164.02       10.39         Tff3       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       13.70         Afg3l2       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       33.99         Plxna2	Svop	163.58	10.12
Sephs2       163.58       27.21         Pcdh1       163.58       12.48         Fat1       163.58       7.49         Sox4       163.58       14.71         Gm8206       163.58       10.47         Clen5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       15.20         Muc13       164.02       15.20         Muc13       164.02       10.39         Tff3       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       33.99         Plxna2       164.02       33.99         Plxna2       164.02       20.99         Epb4.114b       164.02       9.21	Abcb4	163.58	16.59
Pcdh1       163.58       12.48         Fat1       163.58       7.49         Sox4       163.58       14.71         Gm8206       163.58       11.33         Gm8492       163.58       10.47         Clen5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       15.88         Baiap2l2       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       15.20         Muc13       164.02       10.39         Tff3       164.02       10.39         Tff3       164.02       19.12         Sema4g       164.02       13.70         Agap2       164.02       33.99         Plxna2       164.02       33.99         Plxna2       164.02       20.99         Epb4.114b       164.02       9.21	Ccnjl	163.58	6.70
Fat1       163.58       7.49         Sox4       163.58       14.71         Gm8206       163.58       11.33         Gm8492       163.58       10.47         Clcn5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg312       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       20.99         Epb4.114b       164.02       9.21	Sephs2	163.58	27.21
Sox4       163.58       14.71         Gm8206       163.58       11.33         Gm8492       163.58       10.47         Clcn5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       20.99         Epb4.1l4b       164.02       9.21	Pcdh1	163.58	12.48
Gm8206       163.58       11.33         Gm8492       163.58       10.47         Clcn5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       20.99         Epb4.114b       164.02       9.21	Fat1	163.58	7.49
Gm8492       163.58       10.47         Clcn5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       9.21	Sox4	163.58	14.71
Clcn5       164.02       10.49         Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       9.21	Gm8206	163.58	11.33
Slc6a8       164.02       8.35         Bcmo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.114b       164.02       9.21	Gm8492	163.58	10.47
Bemo1       164.02       47.31         Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.114b       164.02       9.21	Clcn5	164.02	10.49
Arrdc4       164.02       8.75         Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       9.21	Slc6a8	164.02	8.35
Cacnb3       164.02       47.06         Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       9.21	Bcmo1	164.02	47.31
Sec14l2       164.02       12.00         Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       9.21	Arrdc4	164.02	8.75
Pgrmc1       164.02       15.88         Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       9.21	Cacnb3	164.02	47.06
Baiap2l2       164.02       20.33         Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.114b       164.02       9.21	Sec14l2	164.02	12.00
Recql5       164.02       33.97         Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       23.39         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.114b       164.02       9.21	Pgrmc1	164.02	15.88
Cpd       164.02       13.70         Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       23.39         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.1l4b       164.02       9.21	Baiap2l2	164.02	20.33
Degs2       164.02       15.20         Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.114b       164.02       9.21	Recql5	164.02	33.97
Muc13       164.02       18.91         Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.114b       164.02       9.21	Cpd	164.02	13.70
Clic5       164.02       10.39         Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.1l4b       164.02       9.21	Degs2	164.02	15.20
Tff3       164.02       16.38         Myo7b       164.02       13.70         Afg3l2       164.02       19.12         Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.1l4b       164.02       9.21	Muc13	164.02	18.91
Myo7b164.0213.70Afg3l2164.0219.12Sema4g164.0223.39Agap2164.0233.99Plxna2164.028.61Aldob164.0220.99Epb4.1l4b164.029.21	Clic5	164.02	10.39
Afg3l2164.0219.12Sema4g164.0223.39Agap2164.0233.99Plxna2164.028.61Aldob164.0220.99Epb4.1l4b164.029.21	Tff3	164.02	16.38
Sema4g       164.02       23.39         Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.1l4b       164.02       9.21	Myo7b	164.02	13.70
Agap2       164.02       33.99         Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.1l4b       164.02       9.21	Afg3l2	164.02	19.12
Plxna2       164.02       8.61         Aldob       164.02       20.99         Epb4.1l4b       164.02       9.21	Sema4g	164.02	23.39
Aldob 164.02 20.99 Epb4.1l4b 164.02 9.21	Agap2	164.02	33.99
Epb4.1l4b 164.02 9.21	Plxna2	164.02	8.61
	Aldob	164.02	20.99
Sel1l3 164.02 17.92	Epb4.1l4b	164.02	9.21
	Sel1l3	164.02	17.92

Hpgds       164.02       31.14         Ush1c       164.02       21.90         Calml4       164.02       12.62         Fam83b       164.02       71.57         Myo15b       164.02       71.57         Inpp5j       164.02       15.20         Cdhr2       164.02       30.00         Myrf       164.02       37.55         Sh3bp4       164.02       9.04         Vgf       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23 <th>Sult1b1</th> <th>164.02</th> <th>17.63</th>	Sult1b1	164.02	17.63
Calml4       164.02       12.62         Fam83b       164.02       16.12         Myo15b       164.02       71.57         Inpp5j       164.02       15.20         Cdhr2       164.02       30.00         Myrf       164.02       37.55         Sh3bp4       164.02       9.04         Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       18.50         Zbtb16       164.02       13.51         Zfp541       164.02       13.51         Zfp541       164.02       9.13         Agxt2       164.02       9.13         Agxt2       164.02       14.54         Gm9429       164.02       14.54         Gm8281       164.02       8.40         Ddx23       164.03       9.29         Map2k6	Hpgds	164.02	31.14
Fam83b       164.02       16.12         Myo15b       164.02       71.57         Inpp5j       164.02       15.20         Ttyh2       164.02       30.00         Myrf       164.02       37.55         Sh3bp4       164.02       9.04         Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       18.50         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       8.40         Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       18.54         Npr1	Ush1c	164.02	21.90
Myo15b       164.02       71.57         Inpp5j       164.02       11.57         Ttyh2       164.02       15.20         Cdhr2       164.02       30.00         Myrf       164.02       37.55         Sh3bp4       164.02       9.04         Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       18.50         Zbtb16       164.02       13.51         Zfp541       164.02       13.51         Zfp541       164.02       9.13         Agxt2       164.02       9.13         Agxt2       164.02       14.54         Gm9429       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       18.54         Npr1	Calml4	164.02	12.62
Inpp5j       164.02       11.57         Ttyh2       164.02       15.20         Cdhr2       164.02       30.00         Myrf       164.02       37.55         Sh3bp4       164.02       9.04         Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       18.50         Osgin1       164.02       13.51         Zfp541       164.02       13.51         Zfp541       164.02       9.13         Agxt2       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       18.54         Npr1       164.03       18.54         Npr1	Fam83b	164.02	16.12
Ttyh2       164.02       15.20         Cdhr2       164.02       30.00         Myrf       164.02       37.55         Sh3bp4       164.02       9.04         Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       13.51         Zfp541       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       19.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Myo15b	164.02	71.57
Cdhr2       164.02       30.00         Myrf       164.02       37.55         Sh3bp4       164.02       9.04         Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Inpp5j	164.02	11.57
Myrf       164.02       37.55         Sh3bp4       164.02       9.04         Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       13.51         Zfp541       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       9.13         Agxt2       164.02       14.54         Gm9429       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       18.54         Npr1       164.03       18.54         Npr1       164.03       11.28	Ttyh2	164.02	15.20
Sh3bp4       164.02       9.04         Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       9.13         Agxt2       164.02       14.54         Gm9429       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       10.28         Hdac6       164.03       11.28	Cdhr2	164.02	30.00
Vgf       164.02       15.05         Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       9.13         Agxt2       164.02       14.54         Gm9429       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Myrf	164.02	37.55
Grtp1       164.02       23.88         B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Sh3bp4	164.02	9.04
B4galnt3       164.02       20.43         Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Vgf	164.02	15.05
Gucy2c       164.02       12.02         Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Grtp1	164.02	23.88
Smim5       164.02       18.20         Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	B4galnt3	164.02	20.43
Nrip1       164.02       9.50         Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Gucy2c	164.02	12.02
Clrn3       164.02       20.13         Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Smim5	164.02	18.20
Acot4       164.02       12.17         Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Nrip1	164.02	9.50
Hunk       164.02       18.50         Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Clrn3	164.02	20.13
Zbtb16       164.02       6.69         Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Acot4	164.02	12.17
Osgin1       164.02       13.51         Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Hunk	164.02	18.50
Zfp541       164.02       25.28         2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Zbtb16	164.02	6.69
2610042L04Rik       164.02       8.14         Gm9429       164.02       9.13         Agxt2       164.02       14.54         Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Osgin1	164.02	13.51
Gm9429164.029.13Agxt2164.0214.54Gm17147164.0226.94Gm8281164.028.40Ddx23164.039.29Map2k6164.0318.54Npr1164.039.68Hdac6164.0311.28	Zfp541	164.02	25.28
Agxt2164.0214.54Gm17147164.0226.94Gm8281164.028.40Ddx23164.039.29Map2k6164.0318.54Npr1164.039.68Hdac6164.0311.28	2610042 L04 Rik	164.02	8.14
Gm17147       164.02       26.94         Gm8281       164.02       8.40         Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Gm9429	164.02	9.13
Gm8281       164.02       8.40         Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Agxt2	164.02	14.54
Ddx23       164.03       9.29         Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Gm17147	164.02	26.94
Map2k6       164.03       18.54         Npr1       164.03       9.68         Hdac6       164.03       11.28	Gm8281	164.02	8.40
Npr1 164.03 9.68 Hdac6 164.03 11.28	Ddx23	164.03	9.29
Hdac6 164.03 11.28	Map2k6	164.03	18.54
	Npr1	164.03	9.68
Vav3 164.03 13.51	Hdac6	164.03	11.28
	Vav3	164.03	13.51

Atp11b	164.03	11.77
Aadat	164.03	8.08
Tmem19	164.03	20.60
Gbp4	164.03	7.14
Papola	164.03	12.14
Als2	164.03	18.35
Sult1d1	164.03	11.23
Myo6	164.03	10.27
Dnajc22	164.03	13.72
Unc5d	164.03	6.96
Gm3095	164.03	10.90
Gm26886	164.03	8.76
Eps8	164.06	12.49
Ddc	164.06	13.61
Fras1	164.06	10.06
Card11	164.06	7.20
Glyat	164.06	10.79
Pipox	164.08	15.90
Iyd	164.08	23.23
Man1a	164.26	8.77
Cdc42ep4	164.26	8.11
Ppara	164.26	8.84
Galr1	164.26	10.10
Ctdsp1	164.26	7.13
Eif2ak3	164.26	8.93
Misp	164.26	9.24
Sun1	164.26	7.35
Kctd8	164.26	9.76
Dcaf12l1	164.26	8.95
4930539 E08 Rik	164.26	8.25
Slc29a4	164.26	7.94
Gm3239	164.26	9.21
Gm3629	164.26	9.77

Gm3252	164.26	9.87
Gm3002	164.26	7.62
Ctsh	164.29	9.76
Dao	164.29	7.06
Ak7	164.31	10.07
Pcp4l1	164.35	9.11
Gm12929	164.62	37.80
Mgat1	164.63	10.10
Atg7	164.76	7.82
Gm11549	165.05	10.23
Ccdc111	165.12	7.77
Fam20a	165.15	7.59
Oscp1	165.16	7.99
Dsc2	165.28	8.06
Adam10	165.28	9.73
Plb1	165.28	8.85
Ccdc89	165.28	7.84
9930013L23Rik	165.28	7.93
Gm13648	165.28	7.08
Igfbp4	165.45	8.68
Ldlrap1	165.45	7.18
Cdh18	165.45	7.96
Arhgef10l	165.46	7.57
Cib3	165.48	8.70
Macf1	165.57	9.10
Fam63b	165.58	8.33
$1190002\mathrm{N}15\mathrm{Rik}$	165.63	9.02
Bcl2l14	165.71	7.54
Hist2h2be	165.88	8.96
Gm6428	165.89	7.32
Dennd5b	166.18	9.42
Gm12168	166.18	7.77
Gm12230	166.42	7.46

Acat3	166.61	7.17
Gpr20	166.84	8.41

Table D.2: Annotations for 76 non-anchor genes on Chromosome 19.

Gene	Start	End	Peak position	LOD
C030046E11Rik	29.52	29.61	29.55	95.58
Tctn3	40.60	40.61	40.59	90.00
Gm7237	33.41	33.42	33.67	74.61
Lipo4	33.50	33.52	34.00	68.23
Dock8	25.00	25.20	25.07	63.17
Sorbs1	40.30	40.40	40.48	61.89
Lipm	34.10	34.12	34.06	58.43
Blnk	40.93	40.99	40.76	57.16
A830019P07Rik	35.84	35.92	35.60	55.54
Uhrf2	30.03	30.09	29.96	54.40
Mbl2	30.23	30.24	30.18	52.81
Myof	37.90	38.04	38.05	48.46
Gm27042	40.59	40.59	40.61	44.27
Btaf1	36.93	37.01	36.90	41.25
Hoga1	42.05	42.07	42.09	41.23
Ppp1r3c	36.73	36.74	36.53	40.69
Pcgf5	36.38	36.46	36.24	40.06
Slc35g1	38.40	38.41	38.35	38.11
Pten	32.76	32.83	32.77	37.95
$\operatorname{Gldc}$	30.10	30.18	30.17	36.26
Lgi1	38.26	38.31	38.17	34.91
C330002G04Rik	23.04	23.08	23.34	34.84
Ppapdc2	28.96	28.97	29.09	34.71
Gm8978	33.61	33.63	33.03	34.59
Mms19	41.94	41.98	41.98	32.03
Ankrd22	34.12	34.17	34.04	31.83

Cdc37l1	28.99	29.02	29.03	31.14
Sgms1	32.12	32.39	32.11	30.10
Entpd1	40.61	40.74	40.50	29.73
Cbwd1	24.92	24.96	24.73	29.65
Gm14446	34.59	34.60	34.28	27.65
Ermp1	29.61	29.65	29.70	26.57
Gm9938	23.72	23.73	23.87	26.46
Insl6	29.32	29.33	29.37	26.23
Slc16a12	34.67	34.75	34.71	25.54
Pgm5	24.68	24.86	25.00	24.30
Morn4	42.07	42.09	41.79	23.86
Exosc1	41.92	41.93	42.10	23.28
Smarca2	26.61	26.78	26.59	23.25
$4930418\mathrm{C}01\mathrm{Rik}$	24.42	24.43	23.92	23.10
2700046 G09 Rik	32.39	32.39	32.25	23.02
Kcnv2	27.32	27.34	27.14	22.88
$1500017\mathrm{E}21\mathrm{Rik}$	36.61	36.71	37.07	22.78
Fra10ac1	38.19	38.22	38.35	22.48
Rnls	33.14	33.39	34.17	21.94
Noc3l	38.79	38.82	40.20	21.67
Pip5k1b	24.29	24.56	24.15	21.62
Plgrkt	29.35	29.37	29.37	20.65
Ifit3	34.58	34.59	34.28	20.45
Fas	34.29	34.33	34.20	19.65
Slit1	41.60	41.74	41.70	18.95
Rrp12	41.86	41.90	41.71	18.09
Ak3	29.02	29.05	29.55	16.90
A1cf	31.87	31.95	32.11	15.56
4430402 I18 Rik	28.90	28.97	29.37	15.43
Pdlim1	40.22	40.27	40.25	15.25
Gm26902	34.47	34.48	36.15	14.26
Plce1	38.48	38.79	38.42	14.26
Slc1a1	28.84	28.91	28.97	14.18

Fam122a	24.48	24.48	24.08	14.07
Lipa	34.49	34.53	34.29	14.06
Mamdc2	23.30	23.45	23.35	13.12
Kif11	37.38	37.42	37.33	12.93
$4933411\mathrm{K}16\mathrm{Rik}$	42.05	42.05	42.08	12.92
Ccnj	40.83	40.85	40.59	12.19
Gm340	41.58	41.59	41.30	12.17
Fxn	24.26	24.28	24.31	12.07
Stambpl1	34.19	34.24	34.28	11.62
Pde6c	38.13	38.18	38.07	11.54
Cyp26a1	37.70	37.70	37.48	11.35
Ch25h	34.47	34.48	32.50	10.74
Pank1	34.81	34.88	35.55	10.61
9930021 J03 Rik	29.71	29.81	28.71	10.32
Klf9	23.14	23.17	23.34	10.26
Ubtd1	41.98	42.03	41.71	10.25
Lipk	34.01	34.05	34.29	10.23