Chapter 3B

Frederick Boehm

February 3, 2019

Todo list

Contents

List of Figures

List of Tables

1   Introduction

The goal of this section is to characterize the statistical power of our pleiotropy test under a variety of conditions by studying a real data set. We examine pancreatic islet expression traits from the Keller et al. (2018) data. As in chapters 2 and 3A, we test only two traits at a time. Because we've chosen local expression traits in our analysis, we both know where each trait's true QTL location (approximately), and we anticipate that each trait has a unique QTL that is distinct from QTL for other local expression traits. This design thus provides opportunities to study statistical power for our test.

We anticipate that inter-locus distance, univariate QTL strength, and correlation of founder allele effects patterns are three factors that contribute to power for our test. Specifically, we expect that greater inter-locus distance, greater univariate LOD scores, and less similar founder allele effects patterns correspond to greater statistical power to detect two separate QTL.

We use pancreatic islet gene expression traits from a publicly available data set, which Keller et al. (2018) first collected, analyzed, and shared. We examine a collection of 80 local traits on Chromosome 19 and perform our test for pleiotropy on pairs of traits. We also examine pairwise relationships among gene expression traits to characterize the impacts of univariate LOD score, inter-locus distance, and similarity of founder allele effects patterns on pleiotropy test statistics.

2   Methods

We analyzed data from 378 Diversity Outbred mice (Keller et al., 2018). Keller et al. (2018) genotyped tail biopsies with the GigaMUGA microarray (Morgan et al., 2016). They used RNA sequencing to measure genome-wide pancreatic islet cell gene expression for each mouse at the time of sacrifice (Keller et al., 2018). They shared these data, together with inferred founder allele probabilities, on the Data Dryad site (https://datadryad.org/resource/doi:10.5061/dryad.pj105). We performed analyses with the R statistical computing environment (R Core Team, 2018) and the packages qtl2 (K. W. Broman, 2018) and qtl2pleio (Boehm, 2018).

We study below 80 Chromosome 19 local expression QTL and their corresponding transcript levels. We define a local expression QTL to be an expression QTL that is on the same chromosome as the gene itself. For example, the *Asah2* gene is located on Chromosome 19 and its transcript levels have an expression QTL on Chromosome 19 (Table 1). Thus, we term the Chromosome 19 *Asah2* expression QTL a local expression QTL.

We choose to focus on local expression QTL, while ignoring nonlocal expression QTL, because we know,

approximately, the true locations for local expression QTL. That is, a local expression QTL is near the corresponding gene position. Additionally, we expect that a given local expression QTL affects only one local expression trait. In our example above, we expect that the *Asah2* expression QTL is near the *Asah2* gene position and that no other local expression traits map to it.

Our design involves selection of a set of "anchor" expression traits. Gene *Asah2* is located near the center of Chromosome 19 and has a very strong local expression QTL (Table 1). We chose it as our first "anchor" gene expression trait. To diversify our collection of anchor genes, we chose three additional expression traits with local expression QTL. These three are *Lipo1*, *Lipo2*, and *4933413C19Rik* (Table 1). Together, the four anchor genes represent a variety of strong local expression trait LOD scores (from 60 to 101) and demonstrate modest variability in their founder allele effects (Table 2). All four anchor genes are located near the middle of Chromosome 19 (Table 1).

We identified a set of 76 non-anchor local expression traits that map to the 20-Mb region centered on the peak for *Asah2*, at 32.1 Mb. Each trait among the 76 maps to Chromosome 19 with a univariate LOD score of at least 10 (Table 3).

Table 1: Annotations for four anchor genes.

symbol	start	end	peak_position	lod
Asah2	31.98	32.06	32.14	101.20
Lipo1	33.52	33.76	33.67	85.46
Lipo2	33.72	33.76	33.02	77.21
4933413C19Rik	28.58	28.58	28.78	60.41

For each Chromosome 19 marker, we estimated founder allele and covariate effects. We calculated:

$$(\widehat{B:C}) = \left((X:W)^T \hat{\Gamma}^{-1} (X:W)\right)^{-1} (X:W)^T \hat{\Gamma}^{-1} Y \tag{1}$$

where $B:C$ denotes the concatenation of B and C, and $X:W$ refers to the n by 12 matrix resulting from appending the columns of W to the X matrix. $\hat{\Gamma}$ is the covariance matrix defined by Equation 2.

$$\hat{\Gamma} = \hat{\sigma}_g^2 K + \hat{\sigma}_e^2 I_n \tag{2}$$

We denote the restricted maximum likelihood estimates of the variance components by $\hat{\sigma}_g^2$ and $\hat{\sigma}_e^2$.

For each of the 80 expression traits, we calculated fitted values for each subject with the estimated founder allele and covariate effects (Equation 1). We then calculated correlations between fitted values for pairs of traits. Each pairing involved one anchor gene expression trait and one other gene expression trait.

We anticipated that more similar two traits' founder allele effects would correspond, on average, to smaller

pleiotropy test statistics. We base this expectation on findings from Macdonald and Long (2007) and King et al. (2012). Macdonald and Long (2007) and King et al. (2012) found that two traits that associate with a single pleiotropic QTL tended to have similar founder allele effects patterns for biallelic markers.

We performed two-dimensional QTL scans for $4 * 76 + \binom{4}{2} = 310$ pairs. Each pair included one of the four anchor gene expression traits and either one of 76 non-anchor gene expression traits or one of the remaining three anchor gene expression traits.

Our two-dimensional QTL scan encompassed a 1000 by 1000 marker grid from 18.1 Mb to 42.5 Mb on Chromosome 19. Each scan involved fitting 1000 x 1000 = 1,000,000 models via generalized least squares. For a given ordered pair of markers, we used the bivariate linear mixed effects model and methods defined in Chapter 2. These methods are implemented in the R package `qtl2pleio` (Boehm, 2018).

For each of the 80 expression traits, we used the fitted founder allele and covariate effects ($\widehat{B:C}$ in Equation 1) to obtain fitted values vectors for every subject and all 80 traits (Equation 3). For each of the 310 pairings of traits, we calculated correlations among the fitted values vectors. Our motivation for working with the fitted values vectors (instead of the $\hat{B}$ estimated founder allele effects vectors) is that the fitted values approximately weight the allele effects by allele frequency. An alternative analysis might neglect the covariates when calculating fitted values.

$$\hat{Y} = X\hat{B} + W\hat{C} \tag{3}$$

3 Results

All four anchor traits demonstrate strong PWK ("G") allele effects. *Lipo2* and *Asah2* have similar patterns among allele effects (at their respective QTL peaks) (Table 2).

Each anchor gene has its own panel in Figure 1. Along the horizontal axis is Chromosome 19 position. The vertical axis is for pleiotropy test statistics. Each point corresponds to a local gene expression trait. Point color corresponds to the nonlocal gene's univariate LOD score, with lighter shades of blue denoting greater values of univariate LOD score. Vertical black bar denotes the anchor gene's position on Chromosome 19. All four panels reveal that points further from the anchor gene tend to show greater test statistic values. Additionally, because of their nearly identical positions, the *Lipo1* and *Lipo2* panels offer an opportunity to compare the impact of anchor gene univariate LOD score on pleiotropy test statistics.

Analyses for all four anchor gene expression traits demonstrate that greater univariate LOD scores tend to correspond to greater values of the pleiotropy test statistic (Figure 2).

Figure 3 features four panels, one for each anchor gene. Each point corresponds to a pairing between the
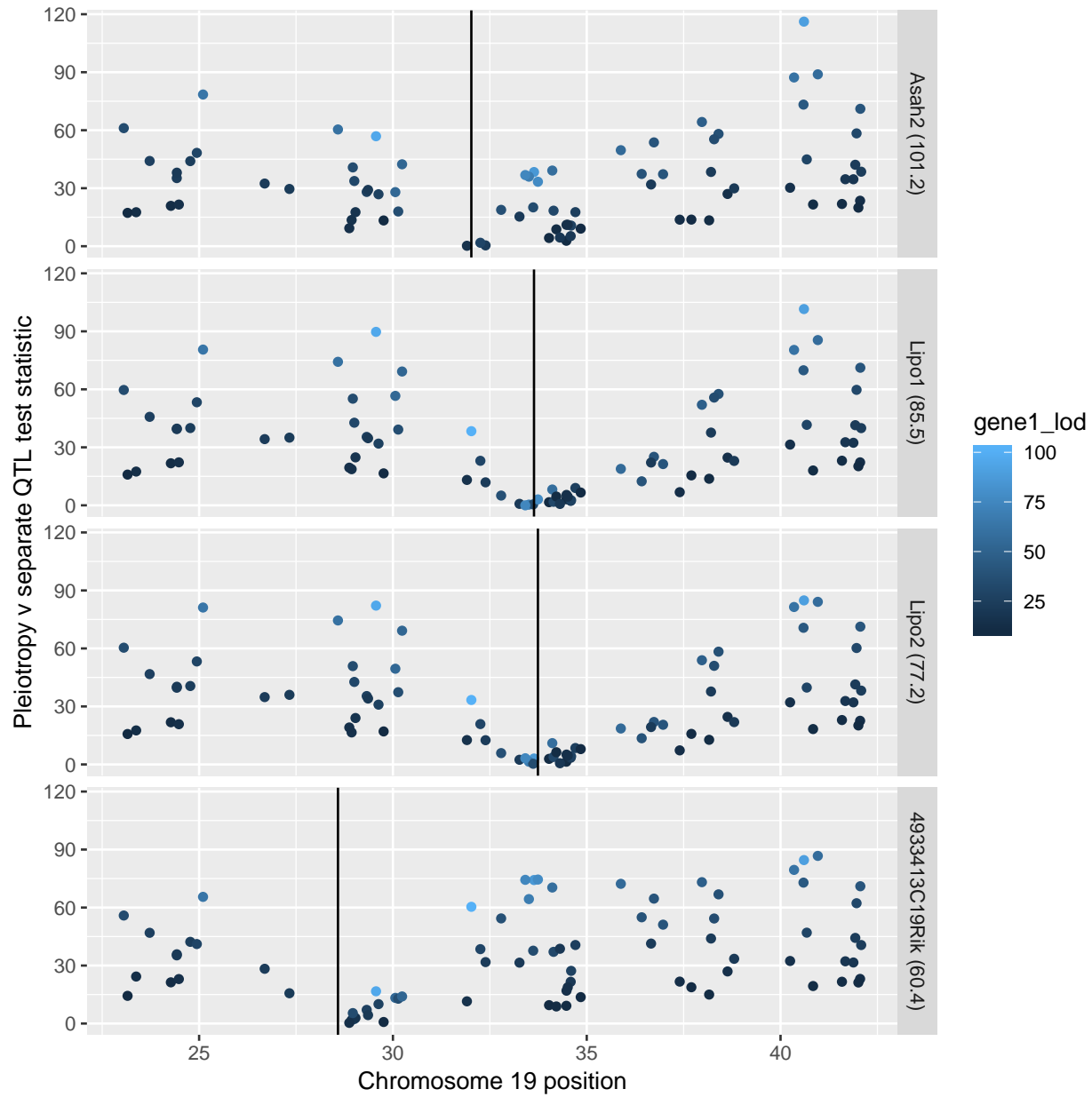
Figure 1: Each anchor gene has its own panel. Along the horizontal axis is Chromosome 19 position. The vertical axis is for pleiotropy test statistic value. Each point corresponds to a local gene expression trait. Point color corresponds to the nonlocal gene's univariate LOD score, with lighter shades of blue denoting greater values of univariate LOD score. Vertical black bar denotes the anchor gene's position on Chromosome 19. All four panels reveal that points further from the anchor gene tend to show greater test statistic values. Additionally, the Lipo1 and Lipo2 panels offer an opportunity to compare the impact of anchor gene univariate LOD score on pleiotropy test statistic values.
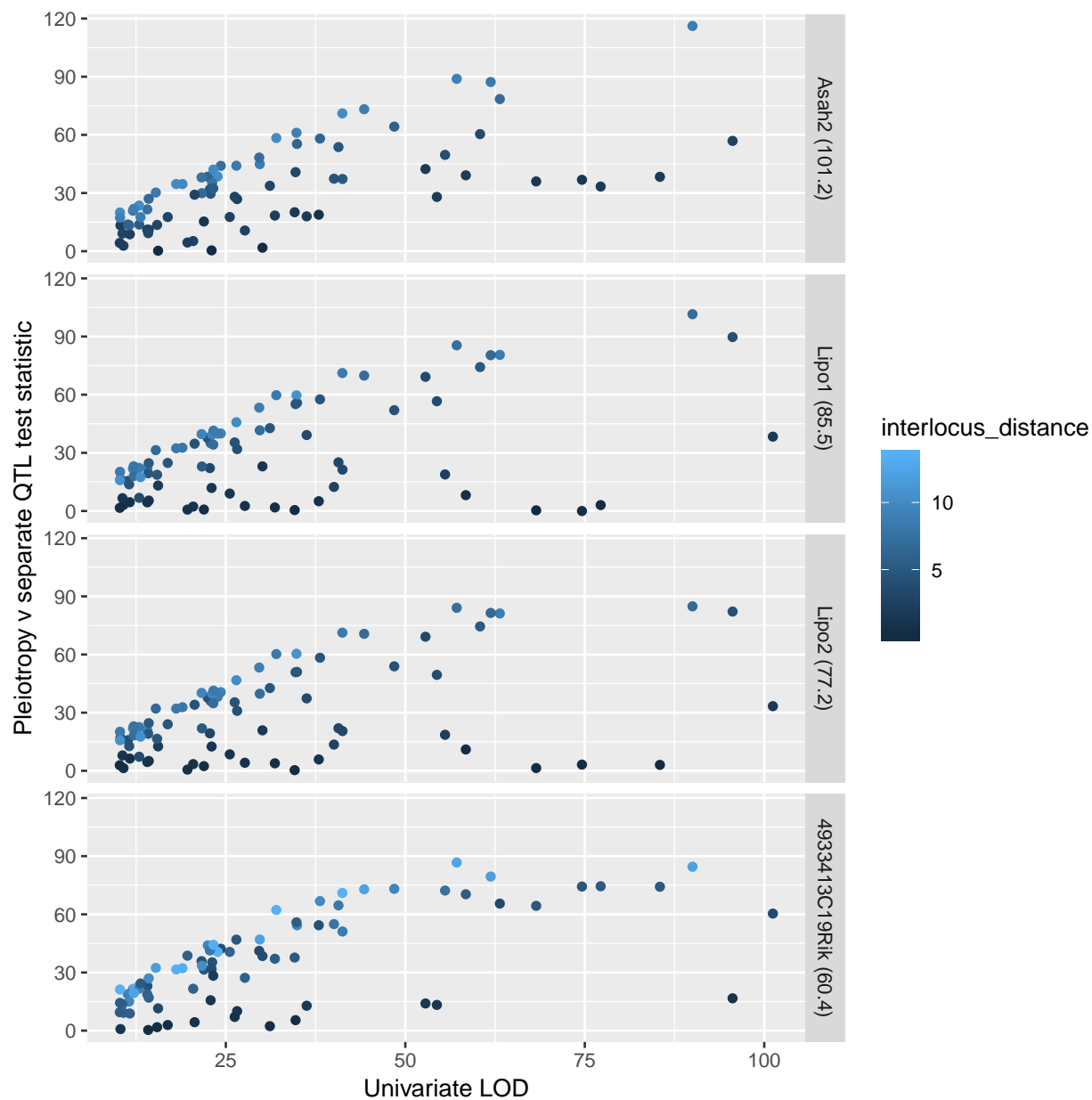
Figure 2: Vertical axis denotes pleiotropy test statistic value, while horizontal axis denotes univariate LOD score. Each point corresponds to a single gene expression trait. Panels correspond to the anchor gene expression trait. The pleiotropy test statistics correspond to analyses involving a single gene expression trait and the specified anchor gene expression trait.
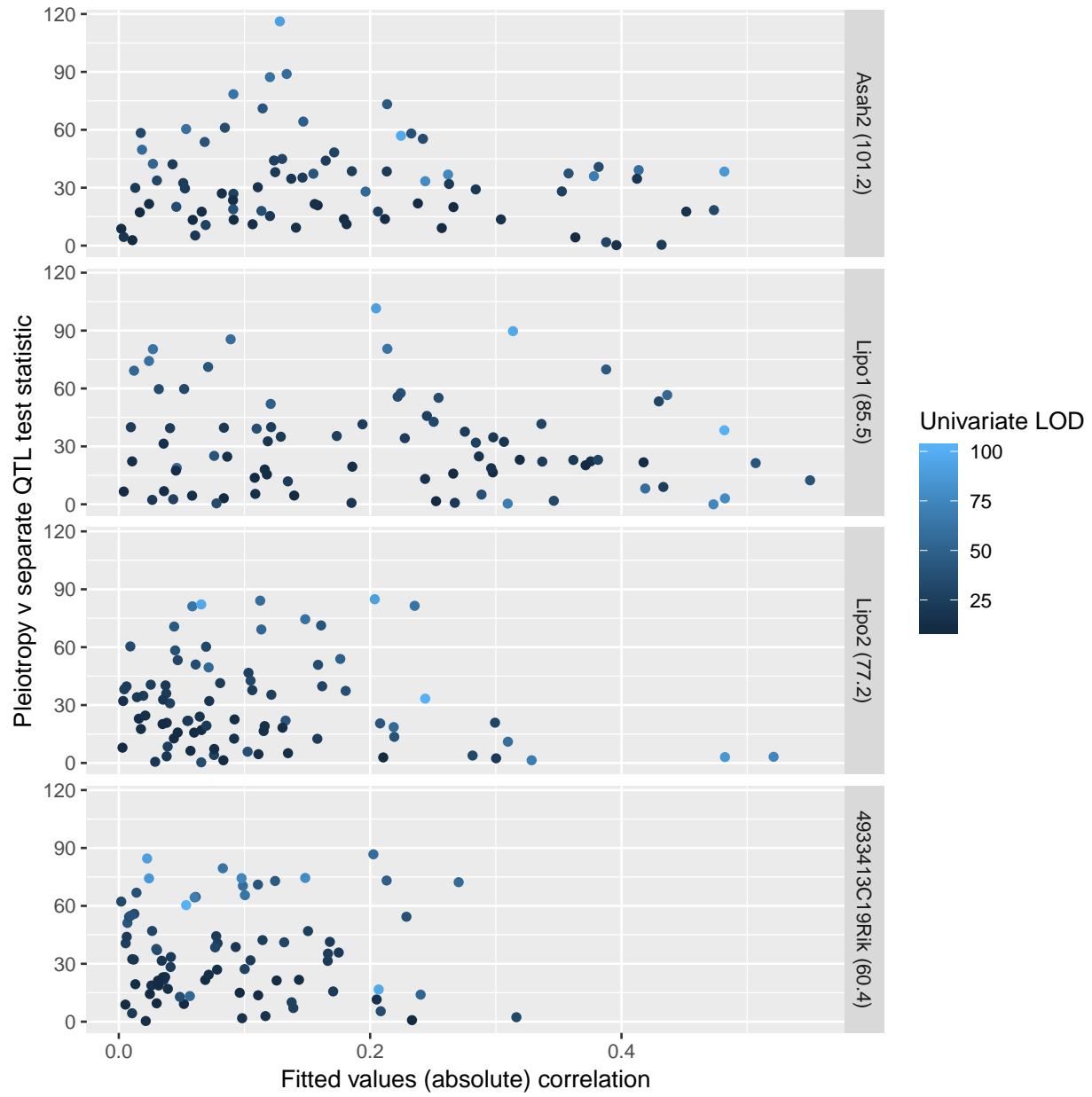
Figure 3: Vertical axis denotes the pleiotropy test statistic value, and horizontal axis indicates absolute value of the correlation between vectors of fitted values. Each point corresponds to a pairing between the specified anchor expression trait and one of the 79 other expression traits.

Table 2: Founder allele effect estimates at Chromosome 19 QTL peak position.

Gene Symbol	Founder allele	Effect	Standard error
	A	-0.96	0.17
	B	1.01	0.19
	C	0.14	0.17
	D	-1.16	0.17
Asah2	E	1.05	0.16
	F	-0.61	0.20
	G	1.81	0.16
	H	-0.18	0.18
	A	0.29	0.18
	B	0.13	0.21
	C	0.28	0.20
	D	0.23	0.19
Lipo1	E	-0.17	0.18
	F	-0.28	0.21
	G	2.55	0.19
	H	-0.72	0.19
	A	-0.10	0.18
	B	-0.28	0.23
	C	0.00	0.20
	D	0.01	0.18
Lipo2	E	-0.77	0.17
	F	-0.89	0.22
	G	2.65	0.18
	H	-0.70	0.20
	A	0.29	0.23
	B	0.76	0.24
	C	0.81	0.21
	D	0.49	0.24
4933413C19Rik	E	0.67	0.20
	F	-0.53	0.22
	G	-1.65	0.18
	H	0.67	0.21

specified anchor and one of the 79 other gene expression traits.

4   Discussion

Our goal for this study was to characterize the impacts of univariate LOD score, inter-locus distance, and founder allele effects pattern similarities on pleiotropy test statistic values. Our study design, in which we examined 310 pairs of local gene expression traits on Chromosome 19, allowed us to interrogate both the effects of univariate association strength and the effects of inter-locus distance. We found that stronger univariate associations and greater inter-locus distances correspond to greater pleiotropy test statistic values (Figures 1 and 2). We expected these trends based on our simulation studies in Chapter 2.

Figure 3 revealed no marginal relationship between fitted values correlations and pleiotropy test statistics.

However, close examination of Figure 3 reveals the possibility that there is an interaction between 1) fitted values correlations and 2) univariate association strength. In every panel, those expression traits with stronger univariate associations tend to have steeper slopes between the conditional mean pleiotropy test statistic values and fitted values correlations. The plots suggest that, at greater univariate LOD values, there is a greater (negative) relationship between fitted values correlation and pleiotropy test statistic value.

We anticipated that more similar founder allele effects patterns would correspond to smaller values for the pleiotropy test statistic, when holding other factors constant. As we stated above, Macdonald and Long (2007) and King et al. (2012) argued that, for biallelic markers, two pleiotropic traits should have similar founder allele effects patterns. In our setting, it's unclear whether the markers are biallelic in the collection of eight founder lines.

We've demonstrated strong evidence in support of the roles of 1) univariate QTL LOD scores and 2) interlocus distances impacting pleiotropy test statistic values. Greater univariate QTL scores and greater interlocus distance lead to greater pleiotropy test statistics. Future research may clarify the impoact of founder allele effects patterns on pleiotropy test statistics. The fact that all four anchor traits had strong PWK effects limited our ability to fully define the impact of allele effects patterns on our test statistics.

Throughout this study, we elected to use test statistic values rather than p-values, as our measure of evidence supporting the separate QTL hypothesis. The primary reason for doing this is to avoid the computationally costly bootstrap sampling and two-dimensional QTL scans that we would need to get bootstrap p-values.

We share our analysis `R` code (R Core Team, 2018) as a `git` repository at this URL: https://github.com/fboehm/keller-2018-chr19-power.

References

Boehm, Frederick (2018). *qtl2pleio: Hypothesis test of close linkage vs pleiotropy in multiparental populations.* R package version 0.1.0.

Broman, Karl W (2018). *qtl2: Quantitative Trait Locus Mapping in Experimental Crosses.* http://kbroman.org/qtl2, https://github.com/rqtl/qtl2.

Keller, Mark P et al. (2018). "Genetic Drivers of Pancreatic Islet Function". In: *Genetics*, genetics–300864.

King, Elizabeth G et al. (2012). "Genetic dissection of a model complex trait using the Drosophila Synthetic Population Resource". In: *Genome research*, gr–134031.

Macdonald, Stuart J and Anthony D Long (2007). "Joint Estimates of QTL Effect and Frequency Using Synthetic Recombinant Populations of Drosophila melanogaster". In: *Genetics* 176.2, pp. 1261–1281. URL: http://www.genetics.org/content/176/2/1261.

Morgan, Andrew P et al. (2016). "The mouse universal genotyping array: from substrains to subspecies". In: *G3: Genes, Genomes, Genetics* 6.2, pp. 263–279.

R Core Team (2018). *R: A Language and Environment for Statistical Computing.* R Foundation for Statistical Computing. Vienna, Austria. URL: https://www.R-project.org/.

Table 3: Annotations for 76 non-anchor genes on Chromosome 19.

Gene	Start	End	Peak position	LOD
C030046E11Rik	29.52	29.61	29.55	95.58
Tctn3	40.60	40.61	40.59	90.00
Gm7237	33.41	33.42	33.67	74.61
Lipo4	33.50	33.52	34.00	68.23
Dock8	25.00	25.20	25.07	63.17
Sorbs1	40.30	40.40	40.48	61.89
Lipm	34.10	34.12	34.06	58.43
Blnk	40.93	40.99	40.76	57.16
A830019P07Rik	35.84	35.92	35.60	55.54
Uhrf2	30.03	30.09	29.96	54.40
Mbl2	30.23	30.24	30.18	52.81
Myof	37.90	38.04	38.05	48.46
Gm27042	40.59	40.59	40.61	44.27
Btaf1	36.93	37.01	36.90	41.25
Hoga1	42.05	42.07	42.09	41.23
Ppp1r3c	36.73	36.74	36.53	40.69
Pcgf5	36.38	36.46	36.24	40.06
Slc35g1	38.40	38.41	38.35	38.11
Pten	32.76	32.83	32.77	37.95
Gldc	30.10	30.18	30.17	36.26
Lgi1	38.26	38.31	38.17	34.91
C330002G04Rik	23.04	23.08	23.34	34.84
Ppapdc2	28.96	28.97	29.09	34.71
Gm8978	33.61	33.63	33.03	34.59
Mms19	41.94	41.98	41.98	32.03
Ankrd22	34.12	34.17	34.04	31.83
Cdc37l1	28.99	29.02	29.03	31.14
Sgms1	32.12	32.39	32.11	30.10
Entpd1	40.61	40.74	40.50	29.73
Cbwd1	24.92	24.96	24.73	29.65
Gm14446	34.59	34.60	34.28	27.65
Ermp1	29.61	29.65	29.70	26.57
Gm9938	23.72	23.73	23.87	26.46
Insl6	29.32	29.33	29.37	26.23
Slc16a12	34.67	34.75	34.71	25.54
Pgm5	24.68	24.86	25.00	24.30
Morn4	42.07	42.09	41.79	23.86
Exosc1	41.92	41.93	42.10	23.28
Smarca2	26.61	26.78	26.59	23.25
4930418C01Rik	24.42	24.43	23.92	23.10
2700046G09Rik	32.39	32.39	32.25	23.02
Kcnv2	27.32	27.34	27.14	22.88
1500017E21Rik	36.61	36.71	37.07	22.78
Fra10ac1	38.19	38.22	38.35	22.48
Rnls	33.14	33.39	34.17	21.94
Noc3l	38.79	38.82	40.20	21.67
Pip5k1b	24.29	24.56	24.15	21.62
Plgrkt	29.35	29.37	29.37	20.65
Ifit3	34.58	34.59	34.28	20.45
Fas	34.29	34.33	34.20	19.65
Slit1	41.60	41.74	41.70	18.95
Rrp12	41.86	41.90	41.71	18.09
Ak3	29.02	29.05	29.55	16.90
A1cf	31.87	31.95	32.11	15.56
4430402I18Rik	28.90	28.97	29.37	15.43
Pdlim1	40.22	40.27	40.25	15.25
Gm26902	34.47	34.48	36.15	14.26
Plce1	38.48	38.79	38.42	14.26
Slc1a1	28.84	28.91	28.97	14.18
Fam122a	24.48	24.48	24.08	14.07
Lipa	34.49	34.53	34.29	14.06
Mamdc2	23.30	23.45	23.35	13.12
Kif11	37.38	37.42	37.33	12.93
4933411K16Rik	42.05	42.05	42.08	12.92
Ccnj	40.83	40.85	40.59	12.19
Gm340	41.58	41.59	41.30	12.17
Fxn	24.26	24.28	24.31	12.07
Stambpl1	34.19	34.24	34.28	11.62
Pde6c	38.13	38.18	38.07	11.54
Cyp26a1	37.70	37.70	37.48	11.35
Ch25h	34.47	34.48	32.50	10.74
Pank1	34.81	34.88	35.55	10.61
9930021J03Rik	29.71	29.81	28.71	10.32
Klf9	23.14	23.17	23.34	10.26
Ubtd1	41.98	42.03	41.71	10.25
Lipk	34.01	34.05	34.29	10.23