

Testing pleiotropy vs. separate QTL in multiparental populations

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ABSTRACT

The high mapping resolution of multiparental populations, combined with technology to measure tens of thousands of phenotypes, presents an opportunity for quantitative methods to enhance understanding of the genetic architecture of complex traits. When multiple traits map to a common genomic region, knowledge of the number of distinct loci provides important insight into the underlying mechanism and can assist planning for subsequent experiments. We extend the work of [Jiang and Zeng \(1995\)](#) to develop a likelihood ratio test for the case of more than two alleles, for a pair of traits, to test the null hypothesis of pleiotropy against the alternative hypothesis of separate QTL.

We also incorporate polygenic random effects to account for variation in relatedness among subjects. We use a parametric bootstrap to determine statistical significance. We apply our methods to a behavioral genetics data set from Diversity Outbred mice, where we find evidence for presence of two distinct loci in a 2.5 cM region. Our methods have been incorporated into the R package `qt12pleio`.

KEYWORDS Quantitative trait locus; pleiotropy; multivariate analysis; linear mixed effects models; systems genetics; ...

Complex trait studies in multiparental populations present new challenges in statistical methods and data analysis. Among these is the development of strategies for multivariate trait analysis. The joint analysis of two or more traits allows one to address additional questions, such as whether two traits share a single pleiotropic locus.

Previous research addressed the question of pleiotropy vs. separate QTL in two-parent crosses. [Jiang and Zeng \(1995\)](#) developed a likelihood ratio test for pleiotropy vs. separate QTL for a pair of traits. Their approach assumed that each trait was affected by a single QTL. Under the null hypothesis, the two traits were affected by a common QTL, and under the alternative hypothesis the two traits were affected by distinct QTL. [Knott and Haley \(2000\)](#) used linear regression to develop a fast approximation to the test of [Jiang and Zeng \(1995\)](#), while [Tian et al. \(2016\)](#) used the methods from [Knott and Haley \(2000\)](#) to dissect QTL hotspots in a F₂ population.

Multiparental populations, such as the Diversity Outbred (DO) mouse population ([Churchill et al. 2012](#)), enable high-precision mapping of complex traits ([de Koning and McIntyre 2014](#)). The DO mouse population began with progenitors of the Collaborative Cross (CC) mice ([Churchill et al. 2004](#)). Each DO mouse is a highly heterozygous genetic mosaic of alleles from the eight CC founder lines. Random matings among non-siblings have maintained the DO population for more than 23 generations ([Chesler et al. 2016](#)).

Several limitations of previous pleiotropy vs. separate QTL tests prevent their direct application in multiparental populations. First, multiparental populations can have complex patterns of relat-

edness among subjects, and failure to account for these patterns of relatedness may lead to spurious results (Yang *et al.* 2014). Second, previous tests allowed for only two founder lines (Jiang and Zeng 1995). Finally, Jiang and Zeng (1995) assumed that the null distribution of the test statistic follows a chi-square distribution.

We developed a pleiotropy vs. separate QTL test for two traits in multiparental populations. Our test builds on research that Jiang and Zeng (1995), Knott and Haley (2000), Tian *et al.* (2016), and Zhou and Stephens (2014) initiated. Our innovations include the accommodation of k founder alleles per locus (compared to the traditional two founder alleles per locus) and the incorporation of multivariate polygenic random effects to account for relatedness. Furthermore, we implemented a parametric bootstrap to calibrate test statistic values (Efron 1979; Tian *et al.* 2016).

Below, we describe our likelihood ratio test for pleiotropy vs. separate QTL. In simulation studies, we find that it is slightly conservative, and that it has power to detect two separate loci when the univariate LOD peaks are strong. We further illustrate our approach with an application to data on a pair of behavior traits in a population of 261 DO mice (Logan *et al.* 2013; Recla *et al.* 2014). We find modest evidence for distinct QTL in a 2.5-cM region on mouse Chromosome 8.

Methods

Our strategy involves first identifying two traits that map to a common genomic region. We then perform a two-dimensional, two-QTL scan over the genomic region, with each trait affected by one QTL of varying position. We identify the QTL position that maximizes the likelihood under pleiotropy (that is, along the diagonal where the two QTL are at a common location), and the ordered pair of positions that maximizes the likelihood under the model where the two QTL are allowed to be distinct. The logarithm of the ratio of the two likelihoods is our test statistic. We calibrate this test statistic with a parametric bootstrap.

Data structures

The data consist of three objects. The first is an n by k by m array of allele probabilities for n subjects with k alleles and m marker positions on a single chromosome [derived from the observed SNP genotype data by a hidden Markov model; see Broman *et al.* (2019)]. The second object is an n by 2 matrix of phenotype values. Each column is a phenotype and each row is a subject. The third object is an n by c matrix of covariates, where each row is a subject and each column is a covariate.

One additional object is the genotype-derived kinship matrix, which is used in the linear mixed model to account for population structure. We are focusing on a defined genomic interval, and we prefer to use a kinship matrix derived by the “leave one chromosome out” (LOCO) method (Yang *et al.* 2014), in which the kinship matrix is derived from the genotypes for all chromosomes except the chromosome under test.

Statistical Models

Focusing on a pair of traits and a particular genomic region of interest, the next step is a two-dimensional, two-QTL scan (Jiang and Zeng 1995). We consider two QTL with each affecting a different trait, and consider all possible pairs of locations for the two QTL. For each pair of positions, we fit the multivariate linear mixed effects model defined in Equation 1. Note that we have assumed an additive genetic model throughout our analyses, but extensions to design matrices that include dominance are straightforward.

$$\text{vec}(Y) = X\text{vec}(B) + \text{vec}(G) + \text{vec}(E) \quad (1)$$

where Y is the n by 2 matrix of phenotypes values; X is a $2n$ by $2(k + c)$ matrix that contains the k allele probabilities for the two QTL positions and the c covariates in diagonal blocks; B is a $(k + c)$ by 2 matrix of allele effects and covariate effects; G is a n by 2 matrix of random effects; and E is a n by 2 matrix of random errors. n is the number of mice. The ‘vec’ operator stacks columns from a matrix into a single vector. For example, a 2 by 2 matrix inputted to ‘vec’ results in a vector with length 4. Its first two entries are the matrix’s first column, while the third and fourth entries are the matrix’s second column.

We also impose distributional assumptions on G and E :

$$G \sim MN_{nx2}(0, K, V_g) \quad (2)$$

and

$$E \sim MN_{nx2}(0, I, V_e) \quad (3)$$

where $MN_{nx2}(0, V_r, V_c)$ denotes the matrix-variate (n by 2) normal distribution with mean being the n by 2 matrix with all zero entries and row covariance V_r and column covariance V_c . We assume that G and E are independent.

Parameter inference and log likelihood calculation

Inference for parameters in multivariate linear mixed effects models is notoriously difficult and can be computationally intense (Meyer 1989, 1991). Thus, we estimate V_g and V_e under the null hypothesis of no QTL, and then take them as fixed and known in our two-dimensional, two-QTL genome scan. We use restricted maximum likelihood methods to fit the model:

$$vec(Y) = X_0 vec(B) + vec(G) + vec(E) \quad (4)$$

where X_0 is a $2n$ by $2(c + 1)$ matrix whose first column of each diagonal block in X_0 has all entries equal to one (for an intercept); the remaining columns are the covariates.

We draw on our R implementation (Boehm 2018) of the GEMMA algorithm for fitting a multivariate linear mixed effects model with expectation-maximization (Zhou and Stephens 2014). We use restricted maximum likelihood fits for the variance components V_g and V_e in subsequent calculations of the generalized least squares solution \hat{B} .

$$\hat{B} = (X^T \hat{\Sigma}^{-1} X)^{-1} X^T \hat{\Sigma}^{-1} vec(Y) \quad (5)$$

where

$$\hat{\Sigma} = \hat{V}_g \otimes K + \hat{V}_e \otimes I_n \quad (6)$$

where \otimes denotes the Kronecker product, K is the kinship matrix, and I_n is a n by n identity matrix. We then calculate the log likelihood for a normal distribution with mean $X vec(\hat{B})$ and covariance $\hat{\Sigma}$ that depends on our estimates of V_g and V_e (Equation 6).

Pleiotropy vs. separate QTL hypothesis testing framework

Our test applies to two traits considered simultaneously. Below, λ_1 and λ_2 denote putative locus positions for traits one and two. We quantitatively state the competing hypotheses for our test as:

$$\begin{aligned} H_0 : \lambda_1 &= \lambda_2 \\ H_A : \lambda_1 &\neq \lambda_2 \end{aligned} \quad (7)$$

113 Our likelihood ratio test statistic is:

$$\text{LOD} = \log_{10} \left[\frac{\max_{\lambda_1, \lambda_2} L(B, \Sigma, \lambda_1, \lambda_2)}{\max_{\lambda} L(B, \Sigma, \lambda, \lambda)} \right] \quad (8)$$

114 where L is the likelihood for fixed QTL positions, maximized over all other parameters.

115 **Visualizing profile LOD traces**

116 The output of the above analysis is a two-dimensional \log_{10} likelihood surface. To visualize these
117 results, we followed an innovation of Zeng *et al.* (2000) and Tian *et al.* (2016), and plot three traces:
118 the results along the diagonal (corresponding to the null hypothesis of pleiotropy), and then the
119 profiles derived by fixing one QTL's position and maximizing over the other QTL's position.

120 We define the LOD score for our test:

$$\text{LOD}(\lambda_1, \lambda_2) = l_{10}(\lambda_1, \lambda_2) - \max l_{10}(\lambda, \lambda) \quad (9)$$

121 where l_{10} denotes \log_{10} likelihood.

122 We follow Zeng *et al.* (2000) and Tian *et al.* (2016) in defining profile LOD by the equation

$$\text{profile LOD}_1(\lambda_1) = \max_{\lambda_2} \text{LOD}(\lambda_1, \lambda_2) \quad (10)$$

123 We define profile $\text{LOD}_2(\lambda_2)$ analogously. The maximum value for the profile LOD_1 profile LOD_2
124 traces are the same and are non-negative, and give the overall LOD test statistic.

125 We construct the pleiotropy trace by calculating the log-likelihoods for the pleiotropic models at
126 every position.

$$\text{LOD}_p(\lambda) = l_{10}(\lambda, \lambda) - \max l_{10}(\lambda, \lambda) \quad (11)$$

127 By definition, the maximum value for this pleiotropy trace is zero.

128 **Bootstrap for test statistic calibration**

129 We use a parametric bootstrap to calibrate our test statistic (Efron 1979). While Jiang and Zeng (1995)
130 used quantiles of a chi-squared distribution to determine p-values, this does not account for the two-
131 dimensional search over QTL positions. We follow the approach of Tian *et al.* (2016), and identify
132 the maximum likelihood estimate of the QTL position under the null hypothesis of pleiotropy. We
133 then use the inferred model parameters under that model and with the QTL at that position to
134 simulate bootstrap data sets according to the model in equations 1–3. For each of b bootstrap data
135 sets, we perform a two-dimensional QTL scan (over the genomic region of interest) and derive the
136 test statistic value. We treat these b test statistics as the empirical null distribution, and calculate
137 a p-value as the proportion of the b bootstrap test statistics that equal or exceed the observed one,
138 with the original data, $p = \#\{i : \text{LOD}_i^* \geq \text{LOD}\} / b$ where LOD_i^* denotes the LOD score for the i th
139 bootstrap replicate and LOD is the observed test statistic.

140 **Data & Software Availability**

141 Our methods have been implemented in an R package, qt12pleio, available at GitHub:

142 <https://github.com/fboehm/qt12pleio>

143 Custom R code for our analyses and simulations are at GitHub:

144 <https://github.com/fboehm/qt2pleio-manuscript>

145 The data from Recla *et al.* (2014) and Logan *et al.* (2013) are available at the Mouse Phenome Database:

Table 1 Type I error rates for all runs in our 2^3 experimental design. We set (marginal) genetic variances (*i.e.*, diagonal elements of V_g) to 1 in all runs. V_e was set to the 2 by 2 identity matrix in all runs. We used allele probabilities at a single genetic marker to simulate traits for all eight sets of parameter inputs. In the column “Allele effects partitioning”, “ABCD:EFGH” means that lines A–D carry one QTL allele while lines E–H carry the other allele. “F:ABCDEGH” means the QTL has a private allele in strain F.

| Run | $\Delta(\text{Allele effects})$ | Allele effects partitioning | Genetic correlation | Type I error rate |
|-----|---------------------------------|-----------------------------|---------------------|-------------------|
| 1 | 6 | ABCD:EFGH | 0 | 0.032 |
| 2 | 6 | ABCD:EFGH | 0.6 | 0.035 |
| 3 | 6 | F:ABCDEGH | 0 | 0.040 |
| 4 | 6 | F:ABCDEGH | 0.6 | 0.045 |
| 5 | 12 | ABCD:EFGH | 0 | 0.038 |
| 6 | 12 | ABCD:EFGH | 0.6 | 0.042 |
| 7 | 12 | F:ABCDEGH | 0 | 0.025 |
| 8 | 12 | F:ABCDEGH | 0.6 | 0.025 |

146 <https://phenome.jax.org/projects/Chesler4> and <https://phenome.jax.org/projects/Recla1>.
 147 They are also available in R/qtl2 format at <https://github.com/rqtl/qtl2data>.

148 Simulation studies

149 We performed two types of simulation studies, one for type I error rate assessment and one to
 150 characterize the power to detect separate QTL. To simulate traits, we specified X , B , V_g , K , and V_e
 151 matrices (Equations 1–3). For both we used the allele probabilities from a single genomic region
 152 derived empirically from data for a set of 479 Diversity Outbred mice from Keller *et al.* (2018).

153 Type I error rate analysis

154 To quantify type I error rate (*i.e.*, false positive rate), we simulated 400 pairs of traits for each of eight
 155 sets of parameter inputs (Table 1). We used a 2^3 factorial experimental design with three factors:
 156 allele effects difference, allele effects partitioning, and genetic correlation, *i.e.*, the off-diagonal entry
 157 in the 2 by 2 matrix V_g .

158 We chose two strong allele effects difference values, 6 and 12. These ensured that the univariate
 159 phenotypes mapped with high LOD scores to the region of interest. For the allele partitioning factor,
 160 we used either equally frequent QTL alleles, or a private allele in the CAST strain (F). For the residual
 161 genetic correlation (the off-diagonal entry in V_g), we considered the values 0 and 0.6. The marginal
 162 genetic variances (*i.e.*, the diagonal entries in V_g) for each trait were always set to one.

163 We performed 400 simulation replicates per set of parameter inputs, and each used $b = 400$
 164 bootstrap samples. For each bootstrap sample, we calculated the test statistic (Equation 8). We
 165 then compared the test statistic from the simulated trait against the empirical distribution of its 400
 166 bootstrap test statistics. When the simulated trait’s test statistic exceeded the 0.95 quantile of the
 167 empirical distribution of bootstrap test statistics, we rejected the null hypothesis. We observed that

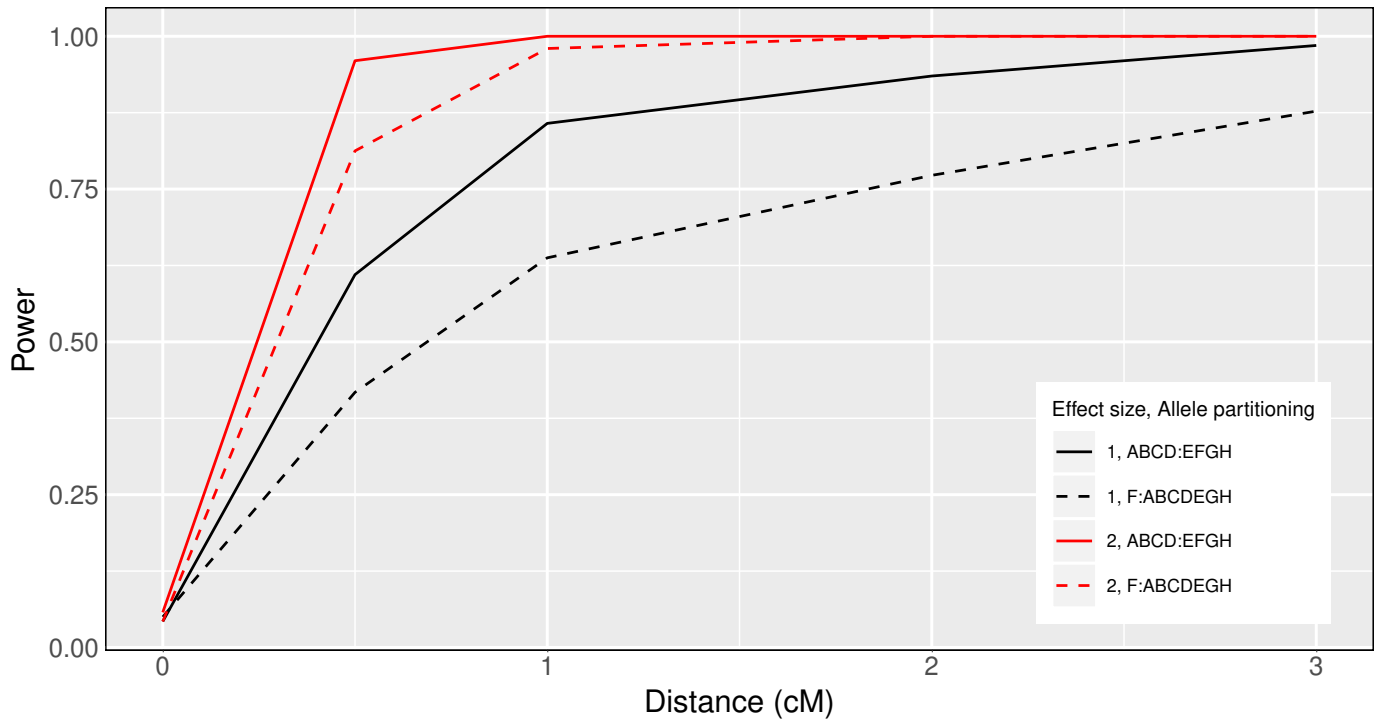


Figure 1 Pleiotropy vs. separate QTL power curves for each of four sets of parameter settings. Factors that differ among the four curves are allele effects difference and allele partitioning. Red denotes high allele effects difference, while black is the low allele effects difference. Solid line denotes the even allele partitioning (ABCD:EFGH), while dashed line denotes the uneven allele partitioning (F:ABCDEGH).

the test is slightly conservative over our range of parameter selections (Table 1), with estimated type I error rates < 0.05 .

Power analysis

We also investigated the power to detect the presence of two distinct QTL. We used a $2 \times 2 \times 5$ experimental design, where our three factors were allele effects difference, allele effects partitioning, and inter-locus distance. The two levels of allele effects difference were 1 and 2. The two levels of allele effects partitioning were as in the type I error rate studies, ABCD:EFGH and F:ABCDEGH (Table S1). The five levels of interlocus distance were 0, 0.5, 1, 2, and 3 cM. V_g and V_e were both set to the 2 by 2 identity matrix in all power study simulations.

We simulated 400 pairs of traits per set of parameter inputs. For each simulation replicate, we calculated the likelihood ratio test statistic. We then applied our parametric bootstrap to calibrate the test statistics. For each simulation replicate, we used $b = 400$ bootstrap samples. Because the bootstrap test statistics within a single set of parameter inputs followed approximately the same distribution, we pooled the $400 \times 400 = 160,000$ bootstrap samples per set of parameter inputs and compared each test statistic to the empirical distribution derived from the 160,000 bootstrap samples. However, for parameter inputs with interlocus distance equal to zero, we didn't pool the 160,000 bootstrap samples; instead, we proceeded by calculating power (*i.e.*, type I error rate, in this case), as we did in the type I error rate study above.

We present our power study results in Figure 1. Power increases as interlocus distance increases. The top two curves correspond to the case where the QTL effects are largest. For each value for the

QTL effect, power is greater when the QTL alleles are equally frequent, and smaller when a QTL allele is private to one strain. One can have high power to detect that the two traits have distinct QTL when they are separated by > 1 cM and when the QTL have large effect.

Application

To illustrate our methods, we applied our test to data from [Logan et al. \(2013\)](#) and [Recla et al. \(2014\)](#), on 261 DO mice measured for a set of behavioral phenotypes. [Recla et al. \(2014\)](#) identified *Hydin* as the gene that underlies a QTL on Chromosome 8 at 57 cM for the “hot plate latency” phenotype (a measure of pain tolerance). The phenotype “percent time in light” in a light-dark box (a measure of anxiety) was measured on the same set of mice ([Logan et al. 2013](#)) and also shows a QTL near this location, which led us to ask whether the same locus affects both traits. The two traits show a correlation of -0.15 (Figure S1).

QTL analysis with the LOCO method, and using sex as an additive covariate, showed multiple suggestive QTL for each phenotype (Figure S2; Table S2). For our investigation of pleiotropy, we focused on the interval 53–64 cM on Chromosome 8. The univariate QTL results for this region are shown in Figure 2.

The estimated QTL allele effects for the two traits are quite different (Figure 3). With the QTL placed at 55 cM, for “percent time in light”, the WSB and PWK alleles are associated with large phenotypes and NOD with low phenotypes. For “hot plate latency”, on the other hand, CAST and NZO show low phenotypes and NOD and PWK are near the center.

In applying our test for pleiotropy, we performed a two-dimensional, two-QTL scan for the pair of phenotypes. With these results, we created a profile LOD plot (Figure 4). The profile LOD for “percent time in light” (in brown) peaks near 55 cM, as was seen in the univariate analysis. The profile LOD for “hot plate latency” (in blue) peaks near 57 cM, also similar to the univariate analysis. The pleiotropy trace (in gray) peaks near 55 cM.

The likelihood ratio test statistic for the test of pleiotropy was 1.2. Based on a parametric bootstrap with 1,000 bootstrap replicates, the estimated p-value was 0.11, indicating weak evidence for distinct QTL for the two traits.

Discussion

We developed a test of pleiotropy vs. separate QTL for multiparental populations, extending the work of [Jiang and Zeng \(1995\)](#) for multiple alleles and with a linear mixed model to account for population structure ([Kang et al. 2010](#); [Yang et al. 2014](#)). Our simulation studies indicate that the test has power to detect presence of separate loci, especially when univariate trait associations are strong (Figure 1). Type I error rates indicate that our test is slightly conservative (Table 1).

In the application of our method to two behavioral phenotypes in a study of 261 Diversity Outbred mice ([Recla et al. 2014](#); [Logan et al. 2013](#)), we obtained weak evidence ($p=0.11$) for the presence of two distinct QTL, with one QTL (which contained the *Hydin* gene) affecting only “hot plate latency” and a second QTL affecting “percent time in light” (Figure 4).

Founder allele effects plots provide further evidence for the presence of two distinct loci. As [Macdonald and Long \(2007\)](#) and [King et al. \(2012\)](#) have demonstrated in their analyses of multiparental *Drosophila* populations, a biallelic pleiotropic QTL would result in allele effects plots that have similar patterns. While we don’t know that “percent time in light” and “hot plate latency” arise from biallelic QTL, the dramatic differences that we observe in allele effects patterns further support the argument for two distinct loci.

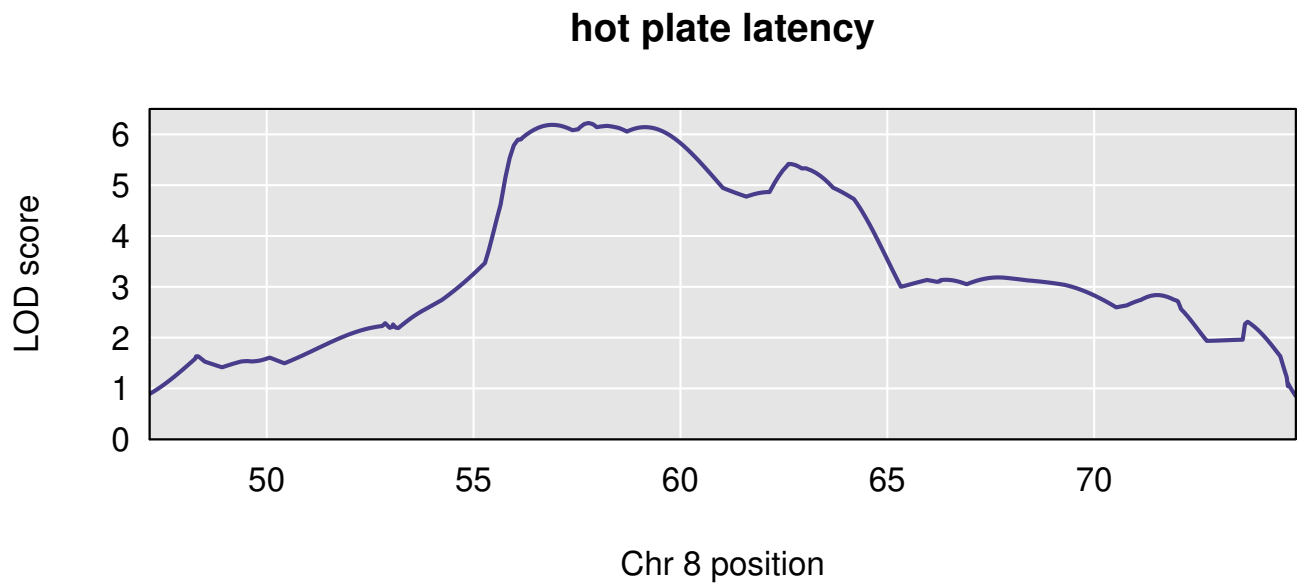
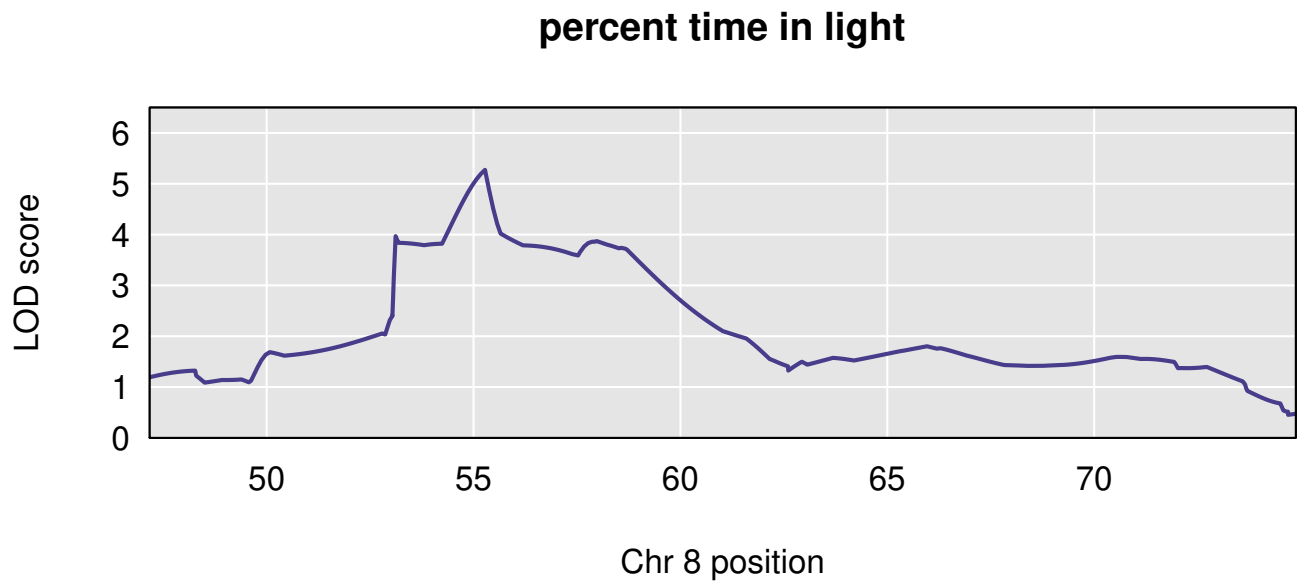


Figure 2 Chromosome 8 univariate LOD scores for percent time in light and hot plate latency reveal broad, overlapping peaks between 53 cM and 64 cM. The peak for percent time in light spans the region from approximately 53 cM to 60 cM, with a maximum near 55 cM. The peak for hot plate latency begins near 56 cM and ends about 64 cM.

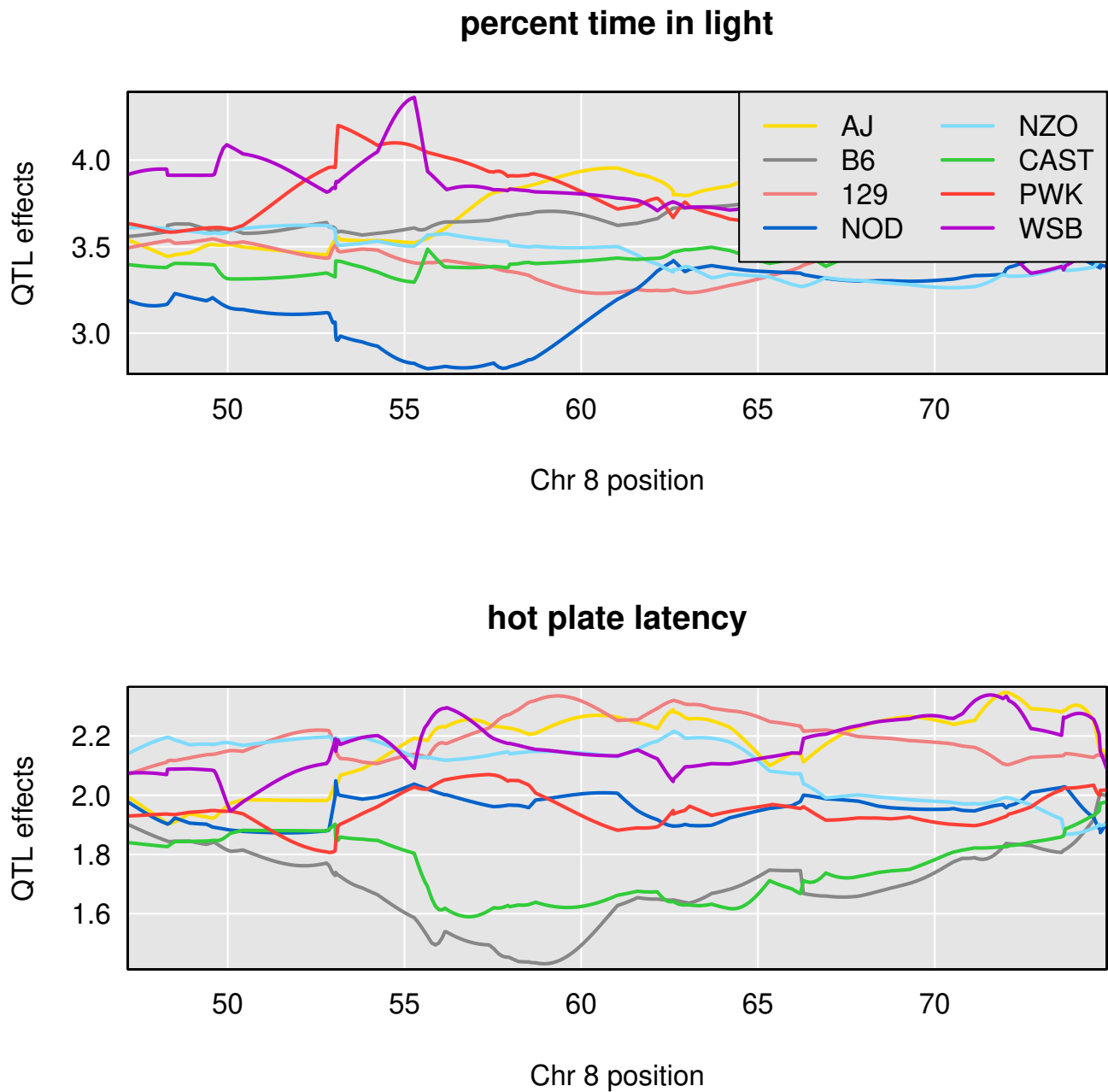


Figure 3 Chromosome 8 univariate LOD scores for percent time in light and hot plate latency reveal broad, overlapping peaks between 53 cM and 64 cM. The peak for percent time in light spans the region from approximately 53 cM to 60 cM, with a maximum near 55 cM. The peak for hot plate latency begins near 56 cM and ends about 64 cM.

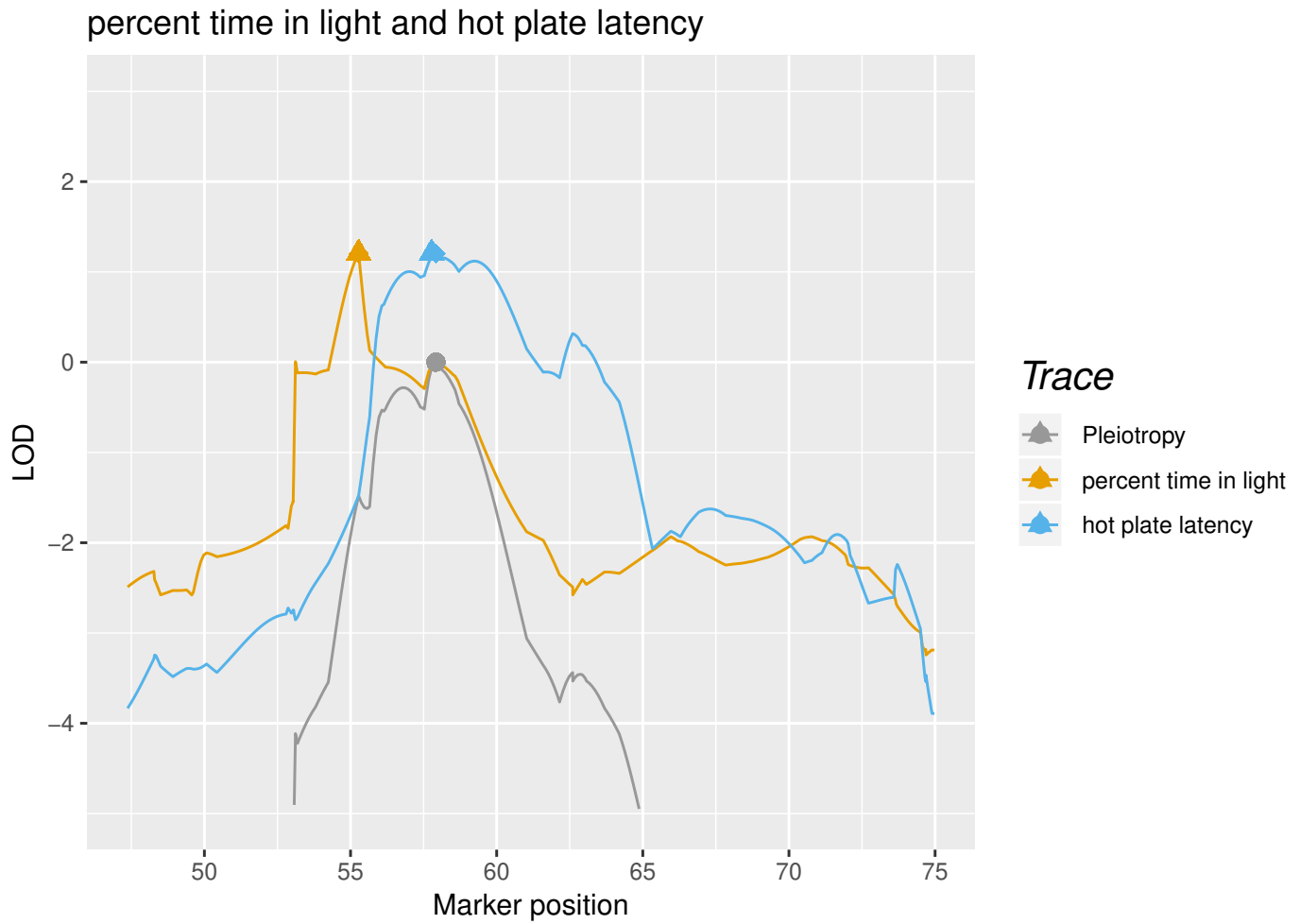


Figure 4 Profile LOD curves for the pleiotropy vs. separate QTL hypothesis test for “percent time in light” and “hot plate latency”. Gray trace denotes pleiotropy LOD values. Triangles denote the univariate LOD maxima, while diamonds denote the profile LOD maxima. For “percent time in light”, the brown triangle obscures the smaller brown diamond. Likelihood ratio test statistic value corresponds to the height of the blue and brown traces at their maxima.

We have implemented our methods in an R package `qt12pleio`, but analyses can be computationally intensive and time consuming. `qt12pleio` is written mostly in R, and so we could likely obtain improved computational speed by porting parts of the calculations to a compiled language such as C or C++. To accelerate our multi-dimensional QTL scans, we have integrated C++ code into `qt12pleio`, using the Rcpp package (Eddelbuettel *et al.* 2011).

Another computational bottleneck is the estimation of the variance components V_g and V_e . To accelerate this procedure, especially for the joint analysis of more than two traits, we will consider other strategies for variance component estimation, including that described by Meyer *et al.* (2018). Meyer *et al.* (2018), in joint analysis of dozens of traits, implement a bootstrap strategy to estimate variance components for lower-dimensional phenotypes before combining bootstrap estimates into valid covariance matrices for the full multivariate phenotype. Such an approach may ease some of the computational burdens that we encountered.

We view tests of pleiotropy as complementary to mediation tests and related methods that have become popular for inferring biomolecular causal relationships (Chick *et al.* 2016; Schadt *et al.* 2005; Baron and Kenny 1986). A mediation test proceeds by including a putative mediator as a covariate in the regression analysis of phenotype and QTL genotype; a substantial reduction in the association between genotype and phenotype corresponds to evidence of mediation.

Mediation analyses and our pleiotropy test ask distinct, but related, questions. Mediation analysis seeks to establish causal relationships among traits, including molecular traits, or dependent biological and behavioral processes. Pleiotropy tests examine whether two traits share a single source of genetic variation, which may act in parallel or in a causal network. Pleiotropy is required for causal relations among traits. In many cases, the pleiotropy hypothesis is the only reasonable one.

Schadt *et al.* (2005) argued that both pleiotropy tests and causal inference methods may contribute to gene network reconstruction. They developed a model selection strategy, based on the Akaike Information Criterion (Akaike 1974), to determine which causal model is most compatible with the observed data. Schadt *et al.* (2005) extended the methods of Jiang and Zeng (1995) to consider more complicated alternative hypotheses, such as the possibility of two QTL, one of which associates with both traits, and one of which associates with only one trait. As envisioned by Schadt *et al.* (2005), we foresee complementary roles emerging for our pleiotropy test and mediation tests in the dissection of complex trait genetic architecture.

CAPE (Combinatorial Analysis of Pleiotropy and Epistasis) is a strategy for identifying higher-order relationships among traits and marker genotypes (Tyler *et al.* 2013). Tyler *et al.* (2017) used CAPE to identify epistatic gene networks in Diversity Outbred mice. Tyler *et al.* (2016) found evidence for weak epistasis in a large intercross population.

CAPE uses linear models that are distinct from those in our pleiotropy test. A CAPE starts with founder allele dosages at all markers and a collection of two or more traits (Tyler *et al.* 2017). After eigendecomposition to get two or more eigentraits, univariate QTL scans are performed and founder allele effects are estimated at all markers (or a subset of all markers). Next, one identifies markers with sufficiently strong effects of at least one founder allele. Resulting (eigenscore, marker, founder allele) triples are then subjected to a second model fitting. This second round of modeling involves two (eigenscore, marker, founder allele) triples that share an eigenscore. The shared (univariate) eigenscore is modeled as a linear function of the two founder allele dosages and their interaction.

In comparing CAPE and our pleiotropy test, it's important to recognize that the two methods ask different questions. CAPE enables assessment of interactions among specific founder allele dosages at two (possibly identical) markers while examining one eigenscore at a time. Our pleiotropy test, on the other hand, jointly models two phenotypes and quantifies the evidence against the pleiotropy hypothesis by performing a two-dimensional QTL scan over a genomic region. One limitation of

CAPE is its inability to account for population structure. Incorporation of a polygenic random effect into CAPE's linear models may improve its performance in multiparental populations. CAPE's methods also highlight a current limitation of our pleiotropy test. While our multivariate linear models accommodate interactions between founder allele dosages at two markers, we haven't yet incorporated this functionality into our software. It is one direction for future research.

Technological advances in mass spectrometry and RNA sequencing have enabled the acquisition of high-dimensional biomolecular phenotypes (Ozsolak and Milos 2011; Han *et al.* 2012). Multiparental populations in *Arabidopsis*, maize, wheat, oil palm, rice, *Drosophila*, yeast, and other organisms enable high-precision QTL mapping (Yu *et al.* 2008; Tisné *et al.* 2017; Stanley *et al.* 2017; Raghavan *et al.* 2017; Mackay *et al.* 2012; Kover *et al.* 2009; Cubillos *et al.* 2013). The need to analyze high-dimensional phenotypes in multiparental populations compels the scientific community to develop tools to study genotype-phenotype relationships and complex trait architecture. Our test, and its future extensions, will contribute to these ongoing efforts.

Acknowledgments

The authors thank Lindsay Traeger, Julia Kemis, Qiongshi Lu, and Rene Welch for valuable suggestions to improve the manuscript. This work was supported in part by National Institutes of Health grant R01GM070683 (to K.W.B.). The research made use of compute resources and assistance of the UW-Madison Center For High Throughput Computing (CHTC) in the Department of Computer Sciences at UW-Madison, which is supported by the Advanced Computing Initiative, the Wisconsin Alumni Research Foundation, the Wisconsin Institutes for Discovery, and the National Science Foundation, and is an active member of the Open Science Grid, which is supported by the National Science Foundation and the U.S. Department of Energy's Office of Science.

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Table S1 Eight founder lines and their one-letter abbreviations.

| Founder allele | One-letter abbreviation |
|----------------|-------------------------|
| A/J | A |
| C57BL/6J | B |
| 129S1/SvImJ | C |
| NOD/ShiLtJ | D |
| NZO/H1LTJ | E |
| Cast/EiJ | F |
| PWK/PhJ | G |
| WSB/EiJ | H |

Table S2 Both “hot plate latency” and “percent time in light” demonstrate multiple QTL peaks with LOD scores above 5.

| phenotype | chr | pos | LOD score |
|-----------------------|-----|-------|-----------|
| percent time in light | 8 | 55.28 | 5.27 |
| hot plate latency | 8 | 57.77 | 6.22 |
| percent time in light | 9 | 36.70 | 5.42 |
| hot plate latency | 9 | 46.85 | 5.22 |
| percent time in light | 11 | 63.39 | 6.46 |
| hot plate latency | 12 | 43.52 | 5.13 |
| percent time in light | 15 | 15.24 | 5.67 |
| hot plate latency | 19 | 47.80 | 5.48 |

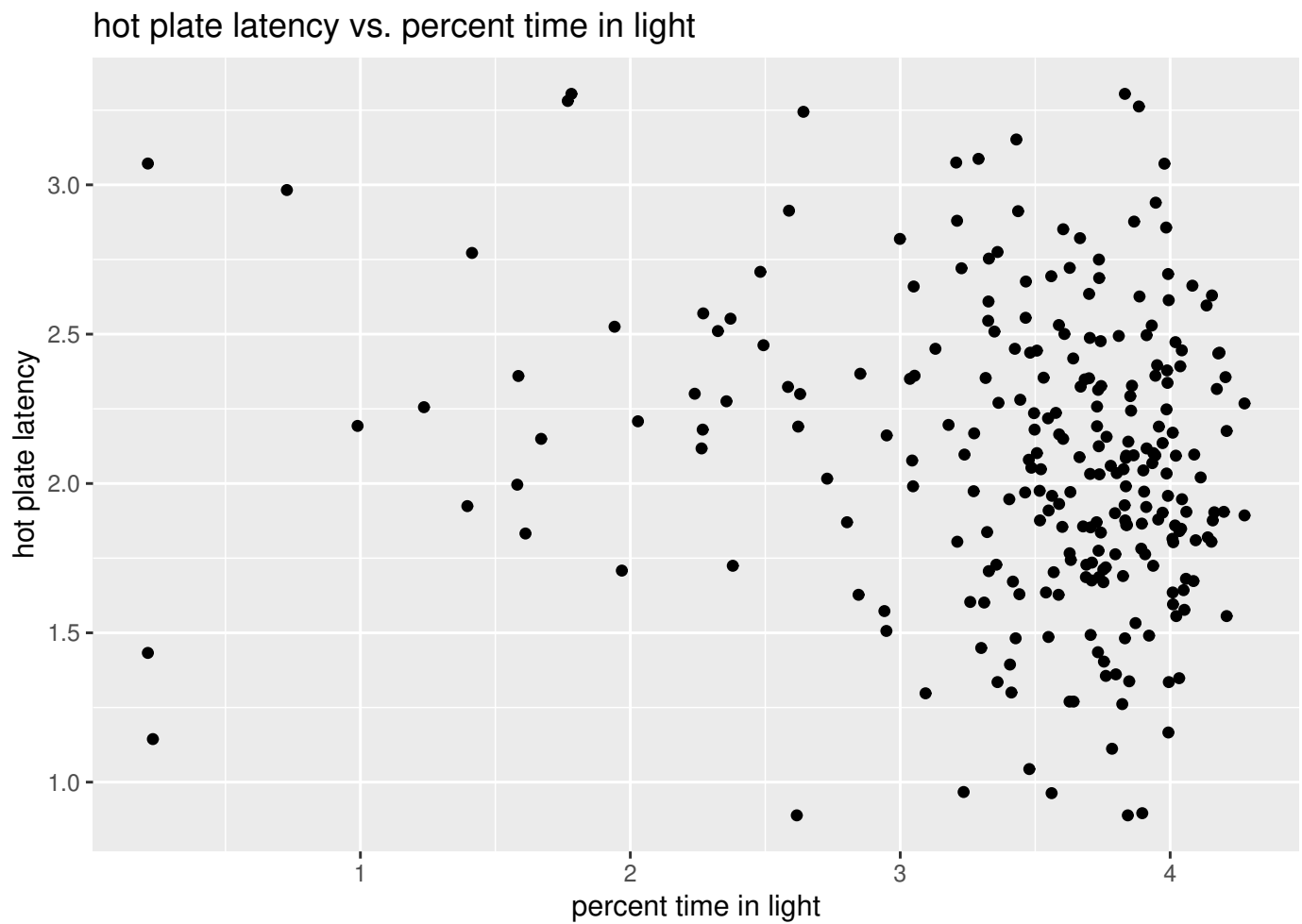


Figure S1 Scatter plot of “hot plate latency” against “percent time in light”, after applying logarithm transformations and winsorizing both traits.

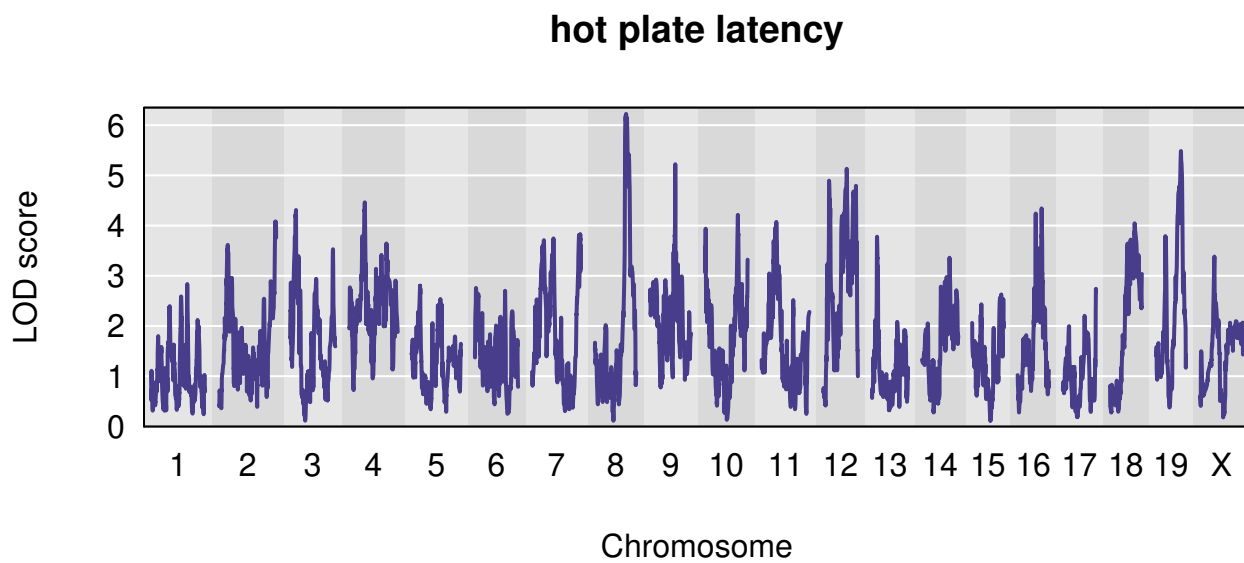
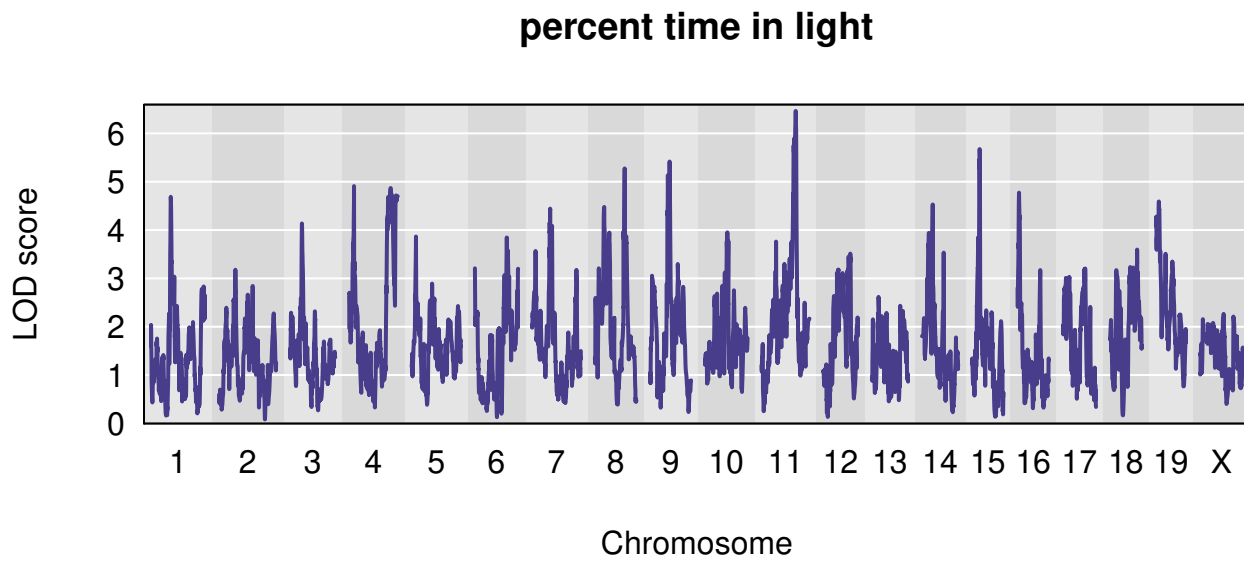


Figure S2 Genome-wide QTL scan for percent time in light reveals multiple QTL, including one on Chromosome 8.