Using the Illinois Report Card Data to Teach Statistics

MMC Conference of Workshops

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1 Variables

The ISBE raw data file rx17.txt contains 1,471 variables. The variable definitions are in the Excel file RC17_layout.xlsx and have been categorized into the groups shown below. The first number represents available variables in each group while the second is the number actually imported into the processed data file. The import script produces 316 variables from 20 of the 21 categories for all 3,796 Illinois public schools. (None of the NAEP variables were imported.) Usable files will be discussed in section 3.

```
School information (13 variables; 12 imported)
                                                              AP courses (168;42)
Student demographics (396;71)
                                                              IB courses (168;42)
ACT (44;11)
                                                              Dual credit (168;42)
Instructional setting (92;2)
                                                              AP exams (36;12)
Teacher and admin statistics (78;26)
                                                              Post secondary remediation (4;1)
District financial (67;40)
                                                              Response rate (5E survey) (4;2)
Region and legislative (3;2)
                                                              Health and wellness (3;1)
National Assmnt. of Educ. Progress (NAEP) (184;0)
                                                              Teacher Attendance (4;1)
College and Career readiness (16;3) CTE (4;1)
                                                              Teacher Evaluation (2;1)
Advanced coursework (12:3)
                                                              School District Count (3;1)
```

2 Descriptive Statistics via State Demographics

2.1 Categorical Count (Raw)

```
school_type <- rc17 %>%
  count(SCHOOL_TYPE_NAME, sort = TRUE) %>%
 mutate(rel_freq = n/sum(n))
school_type
## # A tibble: 4 x 3
     SCHOOL_TYPE_NAME
##
                           n rel_freq
##
     <chr>>
                       <int>
                                <dbl>
## 1 ELEMENTARY
                        2406
                               0.634
## 2 HIGH SCHOOL
                         644
                               0.170
## 3 MIDDLE SCHL
                         604
                               0.159
## 4 CHARTER SCH
                         142
                               0.0374
```

2.2 Categorical Count (Formatted)

```
kable(school_type) %>%
kable_styling(bootstrap_options = "striped", full_width = F)
```

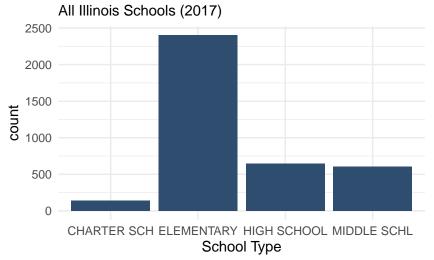
SCHOOL_TYPE_NAME	n	rel_freq
ELEMENTARY	2406	0.6338251
HIGH SCHOOL	644	0.1696523
MIDDLE SCHL	604	0.1591149
CHARTER SCH	142	0.0374078

2.3 Categorical Plot

```
ggplot(rc17, aes(x=factor(SCHOOL_TYPE_NAME)))+
geom_bar(fill="#2F4E6F")+
```

```
labs(title = "Type of School", x = "School Type", subtitle = "All Illinois Schools (2017)") +
theme_minimal()
```

Type of School



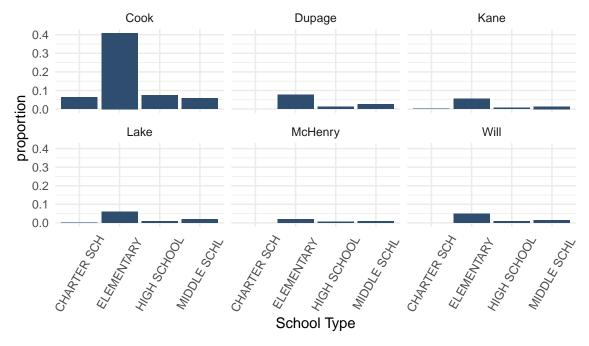
2.4 Categorical Analysis I

Write a short analysis for the types of schools in the state of Illinois.

2.5 Categorical Analysis II

Type of School by County

Six Counties in the Chicago Metropolitan Region (2017)



Write a short analysis for the types of schools in the six county region.

3 Data Import

3.1 Data Files

- ISBE Report Card Data Library [https://www.isbe.net/Pages/Illinois-State-Report-Card-Data.aspx]
 - rc17.txt
 - six_county
- Import script
 - define variables
 - fix issues i.e. "\$" and ","
 - load libraries
 - available here

Creating the six county subset:

```
sixco <- rc17 %>%
filter(COUNTY %in% c("Cook", "Lake", "Will", "Kane", "McHenry", "Dupage"))
```

4 Numeric Summaries (REORDER THESE SECTIONS)

4.1 Lists

phs_value <- function(unk) {</pre>

x <- rc17 %>%

4.1.1 Number of High Schools in the Six County Region

```
sixco %>%
  filter(SCHOOL_TYPE_NAME == "HIGH SCHOOL") %>%
  group_by(COUNTY) %>%
 summarise(count = n())
## # A tibble: 6 x 2
     COUNTY count
##
##
     <chr>
            <int>
## 1 Cook
               151
## 2 Dupage
## 3 Kane
               16
## 4 Lake
                21
## 5 McHenry
                14
## 6 Will
                17
4.1.2 Single List of Scores
mchenry_act <- rc17%>% filter(COUNTY == "McHenry", is.na(ACT_COMP_SCHOOL) == FALSE )
mchenry_act$ACT_COMP_SCHOOL
    [1] 22.4 19.7 18.1 23.1 22.6 23.8 22.7 24.0 21.1 19.9 22.9 22.9 21.4 21.2
4.1.3 Single Values (MAYBE MOVE TO DATA IMPORT SECTION)
4.1.3.1 Finding a School
rc17 %>%
  filter(str_detect(SCHOOL_NAME, "Morton")) %>%
  select(SCHOOL_ID, SCHOOL_NAME, ACT_COMP_SCHOOL)
## # A tibble: 7 x 3
                                                     ACT_COMP_SCHOOL
##
     SCHOOL_ID
                     SCHOOL_NAME
##
     <chr>
                     <chr>>
                                                                <dbl>
## 1 060162010170001 J Sterling Morton East High Sch
                                                                18.4
## 2 060162010170002 J Sterling Morton West High Sch
                                                                18.7
## 3 060162010170003 J Sterling Morton Freshman Cntr
                                                                NA
## 4 070161450022004 Morton Gingerwood Elem School
                                                                NA
## 5 150162990252844 Morton Elem Career Academy
                                                                NA
## 6 530907090260006 Morton High School
                                                                23.3
## 7 530907090261005 Morton Jr High School
                                                                NA
4.1.3.2 Using a Filter
prospect <- rc17 %>%
  filter(str_detect(SCHOOL_NAME, "Prospect High School"))
prospect_act <- prospect$ACT_COMP_SCHOOL</pre>
prospect_act
## [1] 25
4.1.3.3 Using a Function
```

```
filter(SCHOOL_ID == "050162140170005")
    x[unk]
}

phs_value("ACT_COMP_SCHOOL")

## # A tibble: 1 x 1

## ACT_COMP_SCHOOL

## <dbl>
## 1 25
```

4.1.4 Lake County ACT Scores (Ordered and Formatted)

```
lake_ACT <- rc17 %>%
filter(SCHOOL_TYPE_NAME == "HIGH SCHOOL", COUNTY == "Lake") %>%
arrange(desc(ACT_COMP_SCHOOL)) %>%
select(COUNTY, SCHOOL_NAME, ACT = ACT_COMP_SCHOOL)
kable(lake_ACT)
```

COUNTY	SCHOOL_NAME	ACT
Lake	Adlai E Stevenson High School	26.9
Lake	Deerfield High School	26.4
Lake	Lake Forest High School	26.3
Lake	Libertyville High School	25.9
Lake	Highland Park High School	25.2
Lake	Vernon Hills High School	25.1
Lake	Lake Zurich High School	24.9
Lake	Barrington High School	24.8
Lake	Grayslake Central High School	23.3
Lake	Lakes Community High School	22.6
Lake	Grayslake North High School	22.4
Lake	Warren Township High School	22.1
Lake	Wauconda High School	21.8
Lake	Antioch Comm High School	21.7
Lake	Mundelein Cons High School	21.4
Lake	Grant Community High School	21.3
Lake	New Tech High - Zion-Benton East	20.1
Lake	Zion-Benton Twnshp Hi Sch	18.6
Lake	Waukegan High School	17.9
Lake	Round Lake Senior High School	17.8
Lake	North Chicago Community High Sch	17.5

Create a boxplot for Lake County ACT scores. How could you compare to DuPage county?

4.2 Two-Way Tables

```
district_type <- rc17 %>%
  filter(COUNTY == "Lake" | COUNTY == "Dupage") %>%
  group_by(COUNTY)

two_way <- with(district_type, table(DISTRICT_SIZE_NAME, COUNTY))

kable(two_way, caption = "Types of School Districts") %>%
  kable_styling(bootstrap_options = "striped", full_width = F)
```

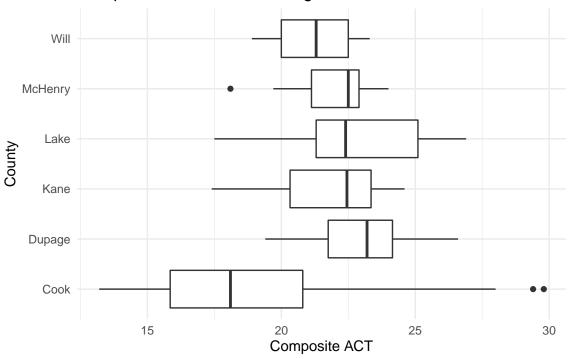
Table 1: Types of School Districts

	Dupage	Lake
LARGE	182	150
MEDIUM	52	38
SMALL	0	4

4.3 Resistant Measures

Warning: Removed 4 rows containing non-finite values (stat_boxplot).

Composite ACT Scores for High Schools



4.4 Mean vs Median

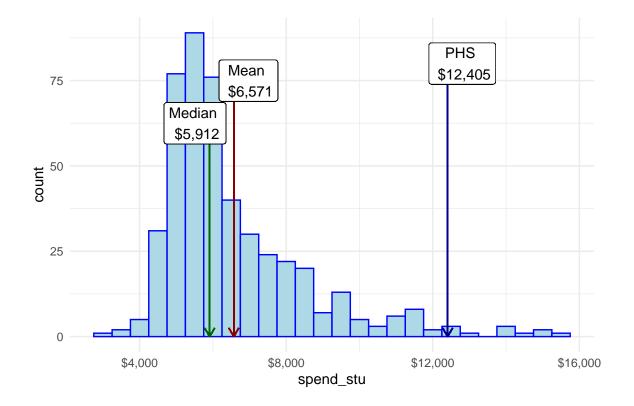
4.4.1 Instructional Spending per Pupil by District

4.4.1.1 Numeric Summary

```
rc17 %>%
filter(SCH00L_TYPE_NAME == "HIGH SCH00L") %>%
group_by(DISTRICT_NAME) %>%
summarise(spend_stu = mean(INSTRUCT_EXPEND_PER_PUPIL_DISTRICT201516, na.rm = TRUE)) %>%
summary()
```

```
DISTRICT_NAME
##
                         spend_stu
##
   Length: 473
                       Min. : 2975
##
   Class : character
                       1st Qu.: 5263
##
   Mode :character
                       Median: 5912
                       Mean : 6571
##
                       3rd Qu.: 7315
##
                       Max.
                              :15535
##
##
                       NA's
                              :1
```

4.4.1.2 Plot



5 Correlation and Regression

5.1 Guess the Correlation

- ACT Composite vs Student Mobility Guess:_____ Actual:____
- ACT Composite vs Attendance rate (%) Guess:______ Actual:____

5.2 Predicting ACT Scores

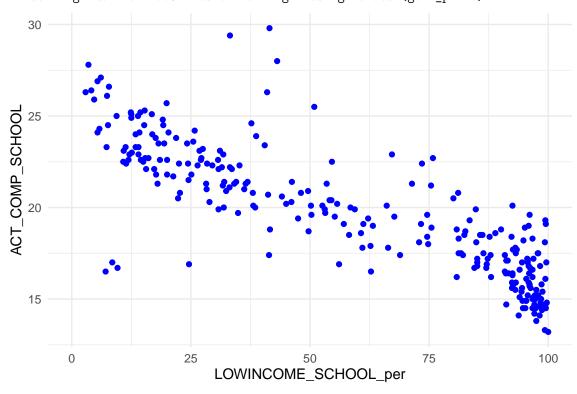
Suppose you choose 3 variables (Composite ACT Score, Enrollment and Attendance Rate) for all schools in the Six County region. What question(s) and display(s) would you explore?

5.3 Scatterplot Analysis

5.3.1 Outliers and Influential

```
ACTvLI <- sixco %>%
    ggplot(mapping = aes(x = LOWINCOME_SCHOOL_per, y = ACT_COMP_SCHOOL)) +
    geom_point(color="Blue") +
    theme_minimal()
ACTvLI
```

Warning: Removed 1779 rows containing missing values (geom_point).



Add some labels using the ggrepel package. (Also notice the layering of information.)

```
library(ggrepel)
```

```
ACTvLI +

geom_text(aes(label=ifelse(SCHOOL_ID =="050162140170005",

as.character(SCHOOL_NAME),'')),hjust=0,vjust=0) +

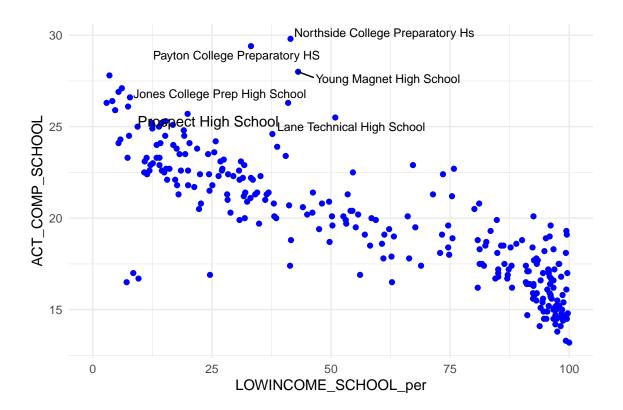
geom_text_repel(aes(LOWINCOME_SCHOOL_per, ACT_COMP_SCHOOL,

label = ifelse(ACT_COMP_SCHOOL_>25 &

LOWINCOME_SCHOOL_per>25,

SCHOOL_NAME, "")), size = 3)
```

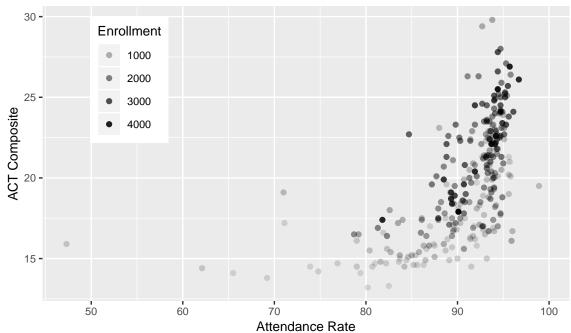
- ## Warning: Removed 1779 rows containing missing values (geom_point).
- ## Warning: Removed 1779 rows containing missing values (geom_text).
- ## Warning: Removed 1779 rows containing missing values (geom_text_repel).



5.3.2 Adding a Third Variable

Predicting ACT from Attendance

Six County High Schools



5.4 Regression Output

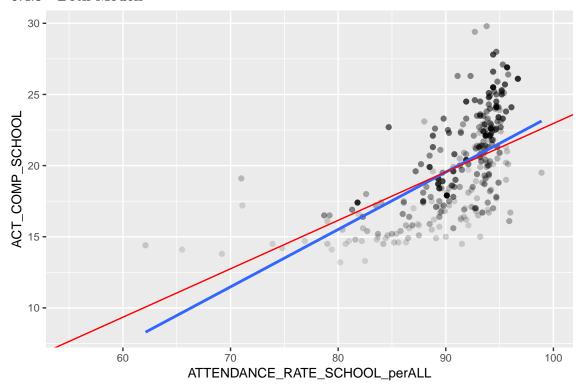
5.4.1 All Schools

summary(lm(sixco\$ACT_COMP_SCHOOL~sixco\$ATTENDANCE_RATE_SCHOOL_perALL))

##

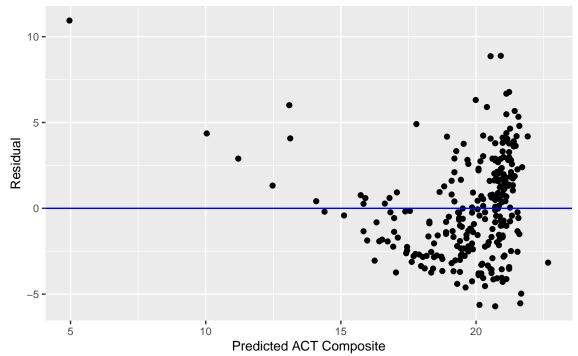
```
## Call:
## lm(formula = sixco$ACT_COMP_SCHOOL ~ sixco$ATTENDANCE_RATE_SCHOOL_perALL)
##
## Residuals:
      Min
               1Q Median
                               30
##
                                      Max
## -5.7088 -2.2108 -0.2343 1.8209 10.9398
##
## Coefficients:
                                       Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                      -11.26875 2.61192 -4.314 2.25e-05
                                                   0.02887 11.886 < 2e-16
## sixco$ATTENDANCE_RATE_SCHOOL_perALL
                                       0.34311
##
## (Intercept)
## sixco$ATTENDANCE_RATE_SCHOOL_perALL ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.844 on 268 degrees of freedom
    (1779 observations deleted due to missingness)
## Multiple R-squared: 0.3452, Adjusted R-squared: 0.3427
## F-statistic: 141.3 on 1 and 268 DF, p-value: < 2.2e-16
5.4.2 Influential Removed
sixco removed <- sixco %>%
 filter(ATTENDANCE_RATE_SCHOOL_perALL>50)
 summary(lm(sixco_removed$ACT_COMP_SCHOOL~sixco_removed$ATTENDANCE_RATE_SCHOOL_perALL))
##
## Call:
## lm(formula = sixco_removed$ACT_COMP_SCHOOL ~ sixco_removed$ATTENDANCE_RATE_SCHOOL_perALL)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
## -5.8340 -2.1147 -0.1728 1.6627 8.7676
##
## Coefficients:
##
                                               Estimate Std. Error t value
## (Intercept)
                                              -16.74644
                                                           2.81182 -5.956
## sixco_removed$ATTENDANCE_RATE_SCHOOL_perALL
                                                0.40322
                                                           0.03104 12.993
##
                                              Pr(>|t|)
                                              8.13e-09 ***
## (Intercept)
## sixco_removed$ATTENDANCE_RATE_SCHOOL_perALL < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.75 on 267 degrees of freedom
## (1778 observations deleted due to missingness)
## Multiple R-squared: 0.3873, Adjusted R-squared: 0.385
## F-statistic: 168.8 on 1 and 267 DF, p-value: < 2.2e-16
```

5.4.3 Both Models



5.4.4 Residual Plot





6 Random Selection and Simulation

6.1 Rolling a die

```
set.seed(2020)
one_die <- sample(1:6, 10, replace = TRUE)
one_die
## [1] 4 4 6 1 1 4 2 6 1 5</pre>
```

6.2 Random Selection

```
four_schools <- sample_n(rc17, 4)</pre>
four_schools[c("SCHOOL_NAME", "SCHOOL_TOTAL_ENROLLMENT")]
## # A tibble: 4 x 2
     SCHOOL_NAME
                                   SCHOOL_TOTAL_ENROLLMENT
##
     <chr>
                                                      <dbl>
## 1 South Side Elementary School
                                                        312
## 2 Coventry Elem School
                                                        565
## 3 Plano High School
                                                        714
## 4 Wanda Kendall Elem School
                                                        236
```

6.3 Stratified Sample

```
strat_samp <- sixco %>%
  filter(SCHOOL_TYPE_NAME == "HIGH SCHOOL") %>%
  group_by(COUNTY) %>%
  sample_n(3)
strat_samp[c("SCHOOL_NAME", "COUNTY", "SCHOOL_TOTAL_ENROLLMENT")]
```

```
## # A tibble: 18 x 3
## # Groups:
               COUNTY [6]
                                                 SCHOOL_TOTAL_ENROLLMENT
      SCHOOL_NAME
                                         COUNTY
##
##
      <chr>>
                                         <chr>
                                                                    <dbl>
##
   1 Marshall Metropolitan High School Cook
                                                                      358
## 2 Proviso West High School
                                                                     1850
                                         Cook
## 3 Chicago Vocational Career Acad HS Cook
                                                                      901
## 4 Westmont High School
                                                                     449
                                         Dupage
## 5 Glenbard East High School
                                         Dupage
                                                                     2244
## 6 Hinsdale South High School
                                         Dupage
                                                                     1507
## 7 Kaneland Senior High School
                                         Kane
                                                                     1342
## 8 East High School
                                         Kane
                                                                     3848
## 9 St Charles North High School
                                         Kane
                                                                     1985
                                                                     2040
## 10 Highland Park High School
                                         Lake
## 11 Libertyville High School
                                         Lake
                                                                     1935
## 12 Zion-Benton Twnshp Hi Sch
                                         Lake
                                                                     2263
## 13 Woodstock North High School
                                                                     942
                                         McHenry
## 14 Huntley High School
                                                                     2996
                                         McHenry
## 15 Crystal Lake South High School
                                                                     1527
                                         McHenry
## 16 Bolingbrook High School
                                         Will
                                                                     3469
## 17 Lincoln-Way Central High School
                                         Will
                                                                     2157
## 18 Wilmington High School
                                         Will
                                                                      465
```

6.4 Binomial

5 10 27 53 94 68 33

A basketball player claims he makes 70% of his free throws. During a recent game he made only 4 of 10. Does this cast doubt on his 70% claim or could making only 4 of 10 happen to a 70% shooter?

```
free_throws <- rbinom(300, 10, .7)
free_throws
                                                                                                3
##
      [1]
                7
                        6
                           6
                               8
                                   7
                                       8
                                           5
                                              7
                                                  6
                                                    10
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     [24]
            7
                6
                    8
                        7
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                                   7
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##
            7
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##
     [47]
                6
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                        6
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                                              7
                                                      8
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     [70]
            5
                9
                    7
                        8
                           7
                               6
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                                       4
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     [93]
                                           9
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   [116]
            6
                6
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##
    [139]
           10
                6
                    6
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                    7
                           4
                               8
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                                                                         6
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##
   [162]
            8
                        6
                                   9
                                       8
                                           6
                                               5
                                                  6
                                                                  4
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                                                                                     6
                                                                                         5
                                                                                            9
   [185]
            7
                6
                    8
                        6
                           9
                               7
                                   9
                                       8
                                           7
                                               5
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                                                          8
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   [208]
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##
            3
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##
   [231]
            9
                7
                    3
                        6
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                               6
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   [254]
                              10
                                   8
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##
                        7
                                                  5
                                                          7
##
   [277]
            6
                9
                    8
                           6
                               7
                                   7
                                       6 10
                                              6
                                                    10
                                                              6
                                                                  8
                                                                     7
                                                                             8
                                                                                         5
## [300]
            8
sort(free_throws)
##
      [1]
            2
                3
                    3
                        3
                           3
                               3
                                   4
                                       4
                                           4
                                              4
                                                  4
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                                                          4
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##
     [24]
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     [47]
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