P4

September 11, 2021

[1]: #4

$$\begin{aligned} \operatorname{Var}[\hat{Y}_h] &= \operatorname{Var}[\hat{\beta}_0 \bar{x} + \hat{\beta}_1 x_h] \\ &= \operatorname{Var}[\bar{y} - \hat{\beta}_1 \bar{x} + \hat{\beta}_1 x_h] \\ &= \operatorname{Var}[\bar{y} + \hat{\beta}_1 (x_h - \bar{x})] \\ &= \operatorname{Var}[\bar{y}] + \operatorname{Var}[\hat{\beta}_1 (x_h - \bar{x})] \\ &= \frac{\sigma^2}{n} + \operatorname{Var}[\hat{\beta}_1 (x_h - \bar{x})] \end{aligned}$$