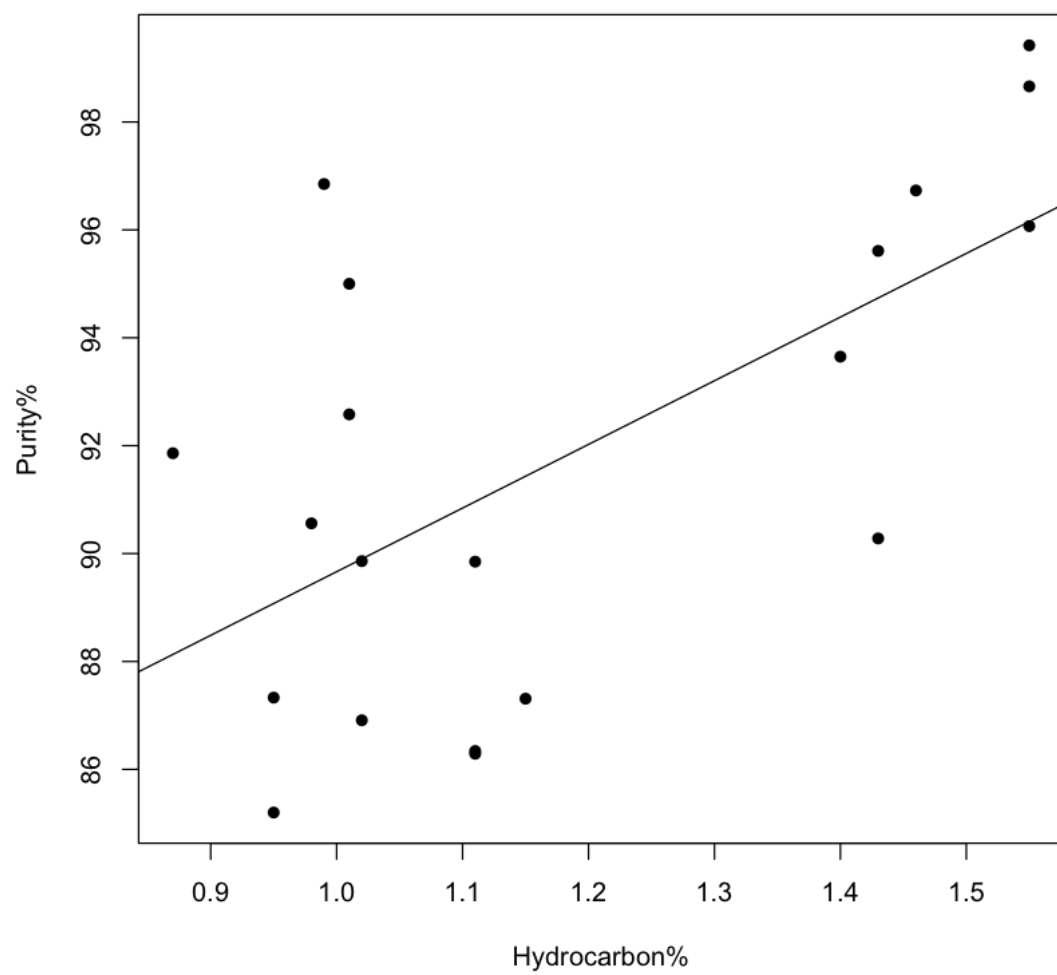


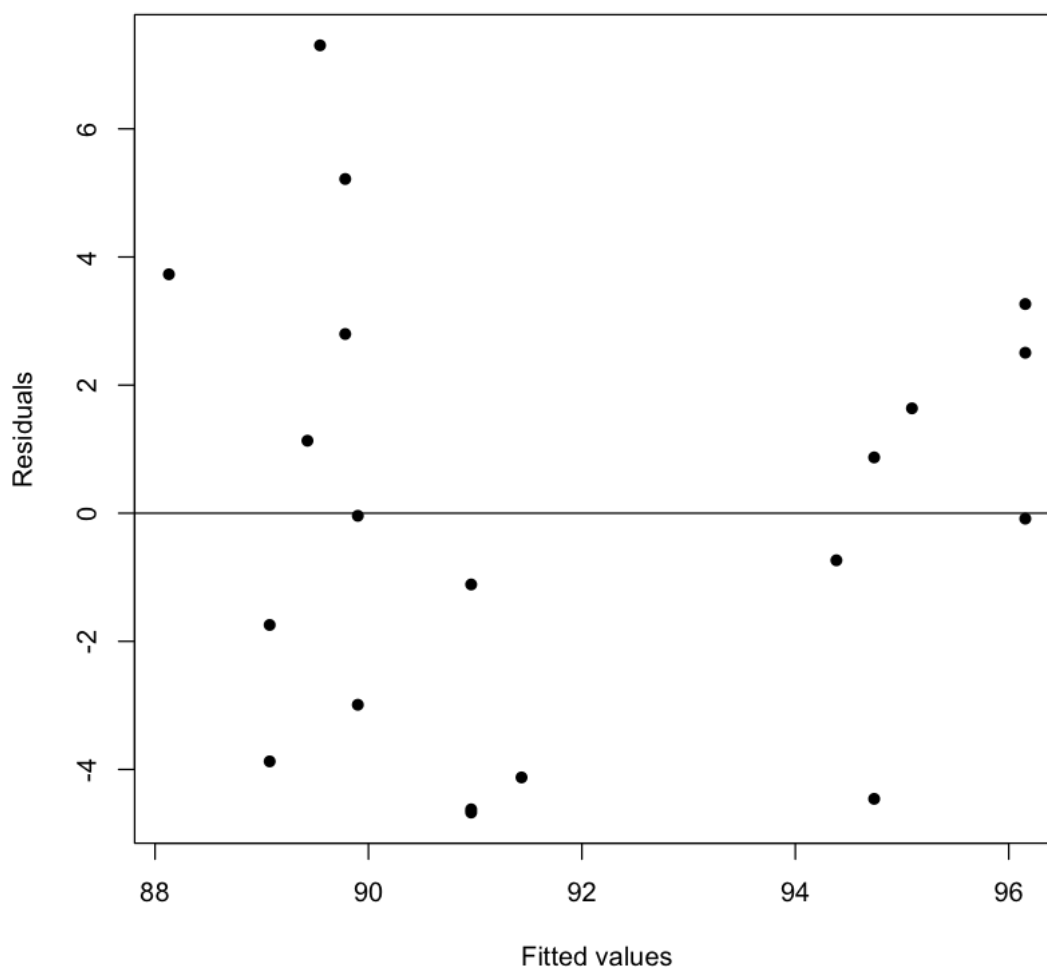
P1

September 11, 2021

```
[37]: df <- read.csv("problem1-oxygenpurity (1).csv")
hydrocarbon<-df$hydro
purity<-df$purity
```

```
[38]: fit = lm(purity~hydrocarbon)
#scatterplot with regression line superimposed
plot(hydrocarbon,purity,xlab = "Hydrocarbon%",ylab = "Purity%",pch=16)
abline(fit)
#residual plot
# Residual plot
plot(fitted(fit),residuals(fit),pch=16,
xlab="Fitted values",ylab="Residuals")
abline(h=0)
#QQ plot
resid<-residuals(fit)
qqnorm(resid);qqline(resid)
#Find coefficient estimate
summary(fit)
#ANOVA table
anova(fit)
```





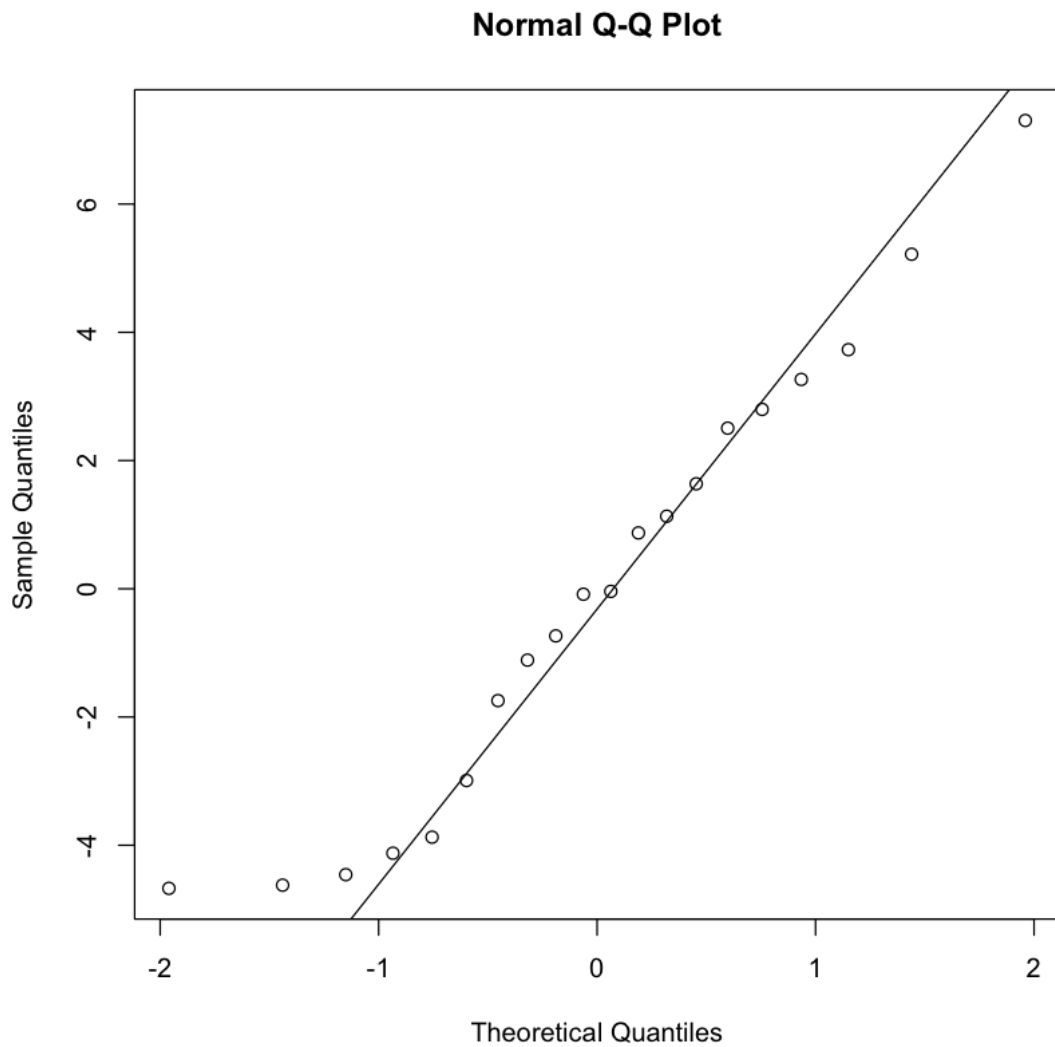
```
Call:
lm(formula = purity ~ hydrocarbon)
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-4.6724 -3.2113 -0.0626  2.5783  7.3037
```

```
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)   77.863     4.199   18.544 3.54e-13 ***
hydrocarbon    11.801     3.485    3.386 0.00329 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 3.597 on 18 degrees of freedom
Multiple R-squared: 0.3891, Adjusted R-squared: 0.3552
F-statistic: 11.47 on 1 and 18 DF, p-value: 0.003291

A anova: 2 × 5		Df	Sum Sq	Mean Sq	F value	Pr(>F)
		<int>	<dbl>	<dbl>	<dbl>	<dbl>
	hydrocarbon	1	148.3130	148.31296	11.4658	0.003291122
	Residuals	18	232.8344	12.93524	NA	NA



(a)

$$S_{yy} = \sum y^2 - \frac{(\sum y)^2}{n} = 381.1473 \quad S_{xx} = \sum x^2 - \frac{(\sum x)^2}{n} = 1.0650 \quad S_{xy} = \sum xy - \frac{(\sum x)(\sum y)}{n} = 12.5678$$

Slope of the regression equation is

$$b_1 = \frac{S_{xy}}{S_{xx}} = 11.8010$$

and intercept of the equation will be

$$b_0 = \frac{1}{n} \left(\sum y - b_1 \sum x \right) = 77.8633$$

So the regression equation will be $y' = 77.8633 + 11.801x$

(b)

Let us find SSE first :

$$SSE = \sum y^2 - b_0 \sum y - b_1 \sum xy = 232.8344$$

So standard error of estimate will be

$$S_e = \sqrt{\frac{SSE}{n-2}} = 3.5966$$

$$s_{b_1} = \frac{S_e}{\sqrt{S_{xx}}} = 3.4851$$

T-statistics is

$$t = \frac{b_1 - 0}{s_{b_1}} = 3.386$$

Degree of freedom of test is $df = n - 2 = 20 - 2 = 18$ P -value of the test: 0.0033 Since p -value is less than 0.05 so we reject the null hypothesis.

(c)

The coefficient of correlation is :

$$r = \frac{S_{xy}}{\sqrt{S_{xx}S_{yy}}} = 0.6238$$

The coefficient of determination is: $r^2 = 0.6238 \cdot 0.6238 = 0.3891$

(d)

For $df = 18$ critical value of t for 95% confidence interval is 2.101. So confidence interval is

$$b_1 \pm t_c s_{b_1} = 11.801 \pm 2.101 \cdot 3.4851 = 11.801 \pm 7.322 = (4.479, 19.123)$$

(e)

```
[39]: predict(fit,data.frame(hydrocarbon=1.05),level=0.95,interval="confidence")
```

	fit	lwr	upr
A matrix: 1 × 3 of type dbl	90.25436	88.30605	92.20268

(f)

The coefficient of correlation is :

$$\text{Cov}(Y, X) = r = \frac{S_{xy}}{\sqrt{S_{xx}S_{yy}}} = 0.6238$$

(g)

from (b), $t_{\{1\}} = 3.386$

p-value: $0.003291 < \alpha$

Therefore, reject the H_0