



A Monte-Carlo investigation of the nematic-isotropic phase transition

Félix Bunel & Hadrien Vergnet

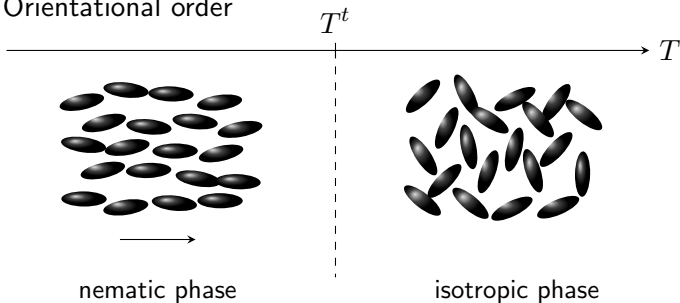
16/01/2017





Nematic phase:

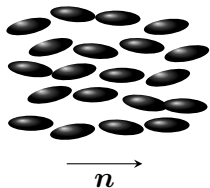
- No positional order
- Orientational order



- 1 The order parameter
- 2 Numerical methods
 - Lebwohl Lasher Model
 - Monte-Carlo Algorithm
 - Equilibration
- 3 Nematic Isotropic Phase Transitions
 - Direct visualisation
 - Energy
 - Order Parameter
 - Histograms
- 4 Influence of an Electric Field
 - Lebwohl Lasher Model
 - Critical point
 - Phase diagram
- 5 Liquid Crystal Display
 - Fréedericksz transition
 - Molecular Orientation

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The Order Parameter



$$\mathbf{n} = \langle \mathbf{a} \rangle$$

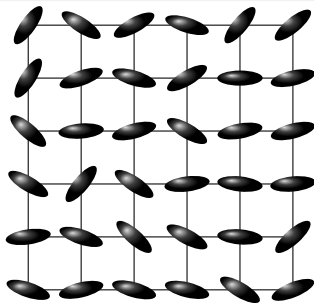


$$S = \frac{3\langle (\mathbf{a} \cdot \mathbf{n})^2 \rangle - 1}{2}$$

Nematic phase : $S = 1$

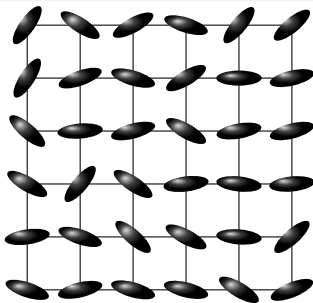
Isotropic phase : $S = 0$

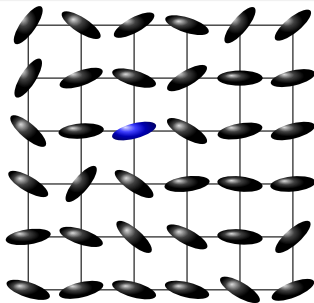
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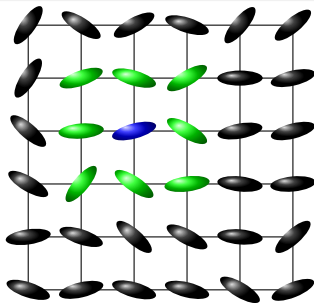
Size : $30 \times 30 \times 30$

$$E = -\epsilon \sum_{\langle i,j \rangle} \frac{3 \cos^2 \alpha_{i,j} - 1}{2}$$

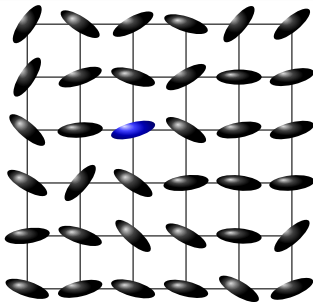




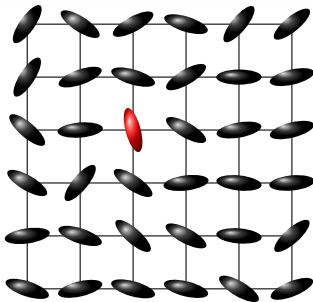
- We select a random site



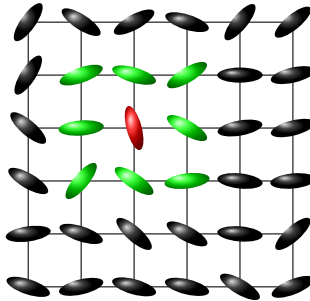
- We select a random site
- We compute the energy with the neighbors : E_{old}



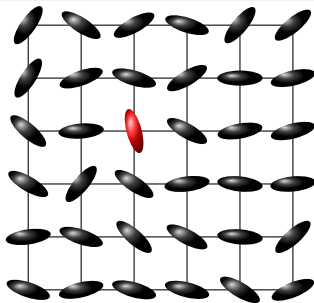
- We select a random site
- We compute the energy with the neighbors : E_{old}
- We try to swap the chosen site



- We select a random site
- We compute the energy with the neighbors : E_{old}
- We try to swap the chosen site

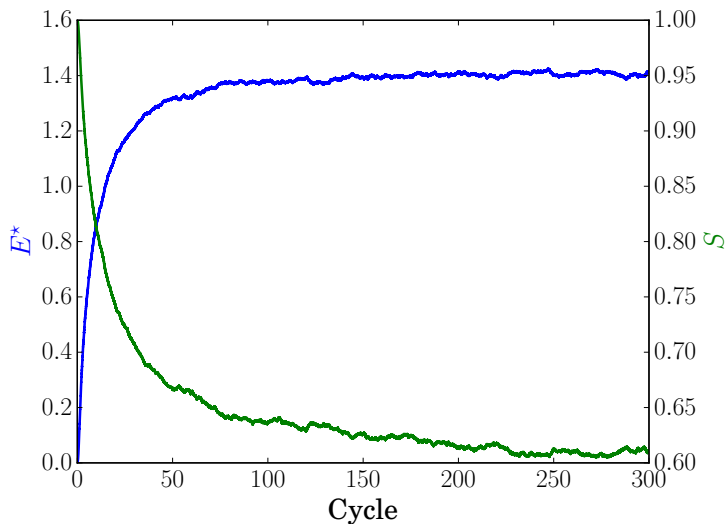


- We select a random site
- We compute the energy with the neighbors : E_{old}
- We try to swap the chosen site
- We compute the energy with the neighbors : E_{new}



- We select a random site
- We compute the energy with the neighbors : E_{old}
- We try to swap the chosen site
- We compute the energy with the neighbors : E_{new}
- We accept the swap with a probability :

$$p = e^{-\frac{E_{old} - E_{new}}{k_B T}}$$

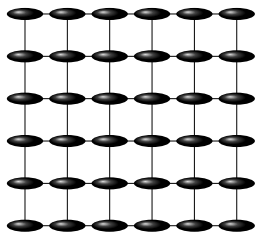


Equilibration at $T^* = 1$

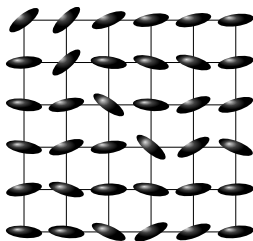
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Nematic Isotropic Phase Transitions

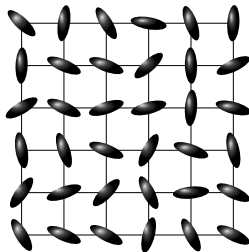
Direct visualisation



$$T^* = 0.05$$



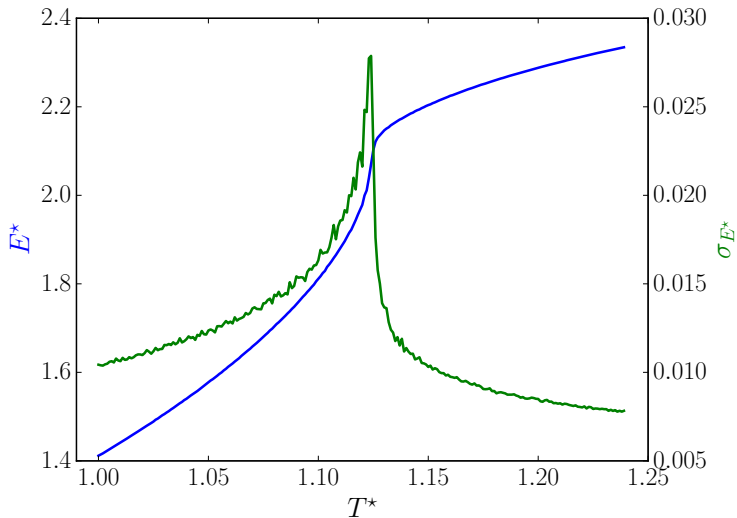
$$T^* = 0.9$$



$$T^* = 1.5$$

Nematic Isotropic Phase Transitions

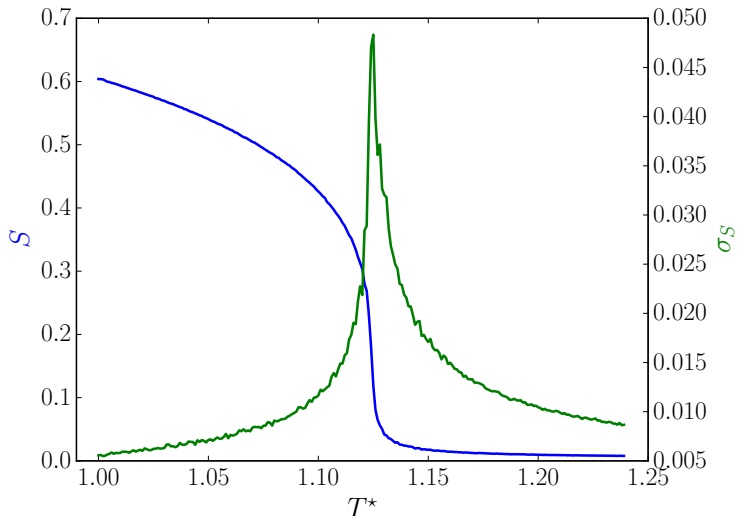
Energy



Energy and its variance.

Nematic Isotropic Phase Transitions

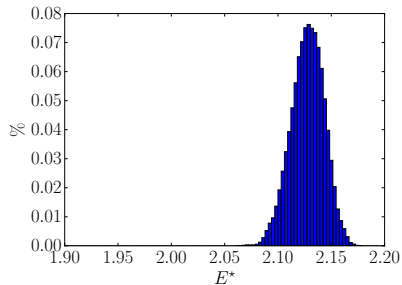
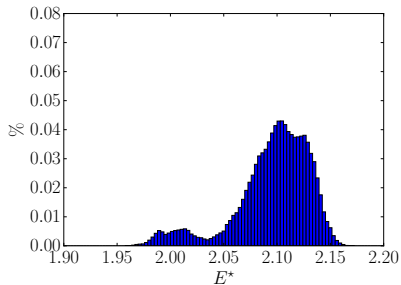
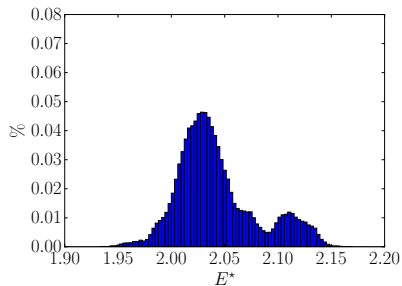
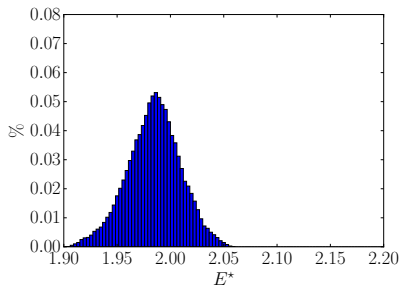
Order Parameter



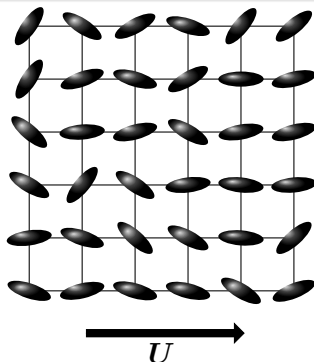
Order parameter and its variance.

Nematic Isotropic Phase Transitions

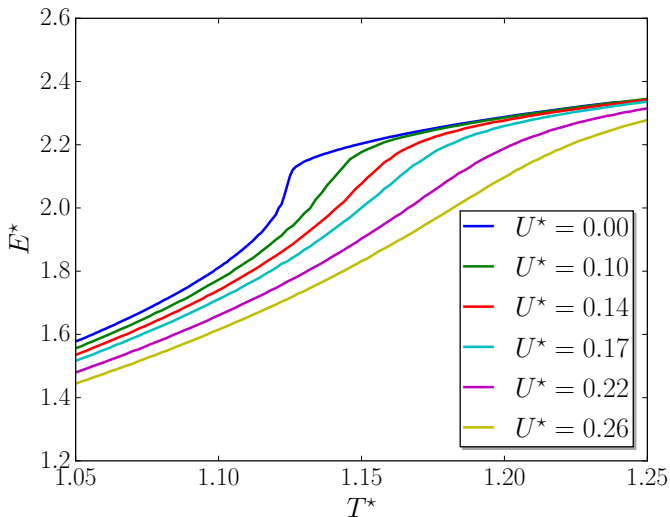
Energy Histograms



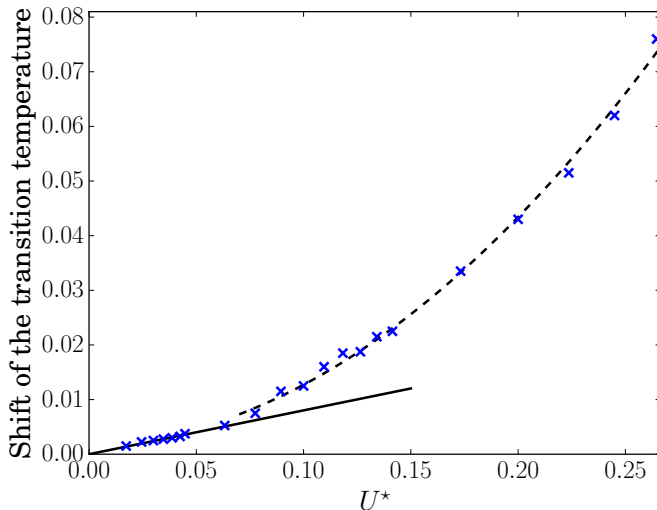
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$$E = -\epsilon \sum_{\langle i,j \rangle} \frac{3 \cos^2 \alpha_{i,j} - 1}{2} - \epsilon \xi U^2 \sum_i \frac{3 \cos^2 \beta_i - 1}{2}$$



Energy for different electric fields.

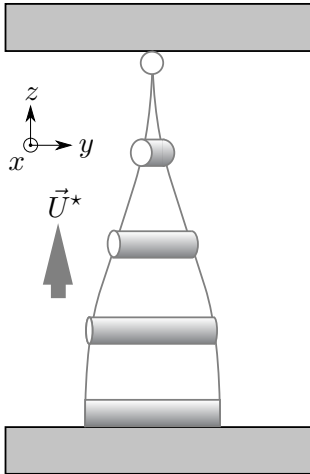


Transition temperature as a function of the electric field.

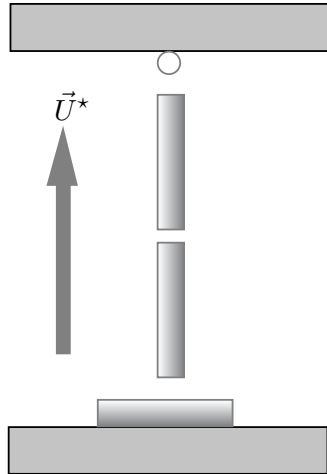
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Liquid Crystal Display

Fréedericksz transition



(a) Pixel "off" state

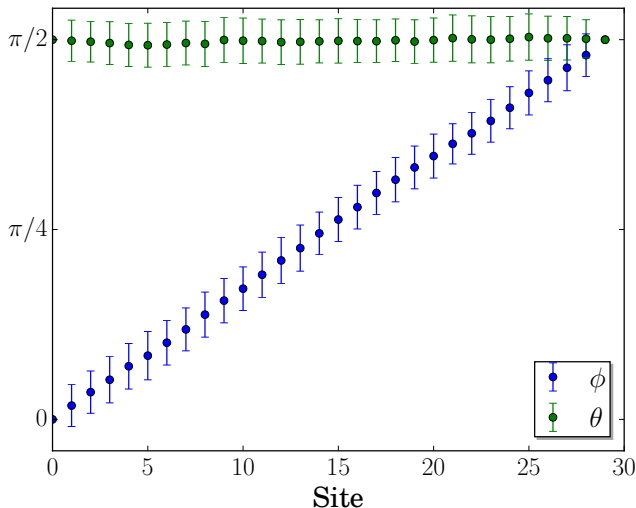


(b) Pixel "on" state

Diagram of a LCD pixel using *twisted nematic* technology.

Liquid Crystal Display

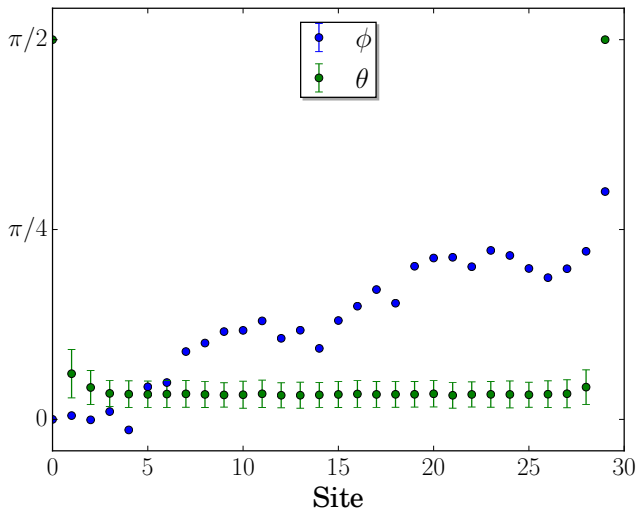
Molecule Orientation



Molecule orientation **without** electric field

Liquid Crystal Display

Molecule Orientation



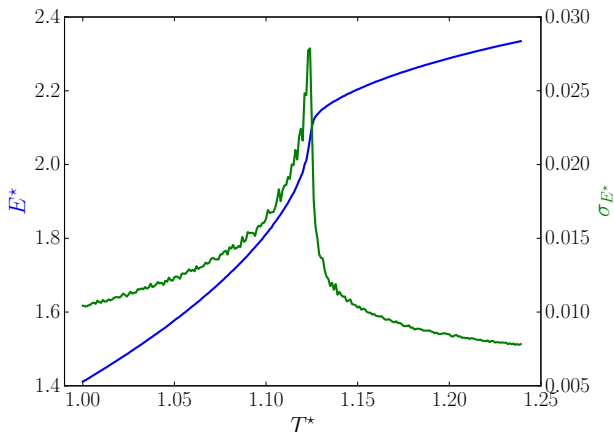
Molecule orientation **with** electric field

Conclusion

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Detailed study of nematic-isotropic transition with Lebwohl-Laser model :

- first order transition at $T^* = 1.1232 \pm 0.0005$

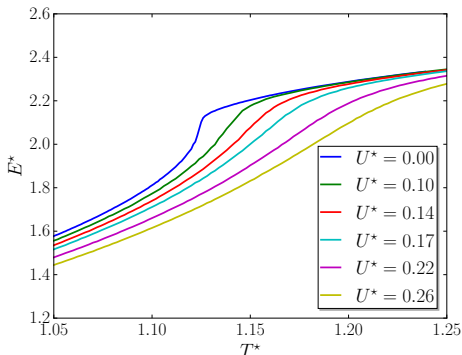


Detailed study of nematic-isotropic transition with Lebwohl-Laser model :

- first order transition at $T^* = 1.1232 \pm 0.0005$

Electric field influence :

- shifts transition temperature and critical point for strong fields



Detailed study of nematic-isotropic transition with Lebwohl-Laser model :

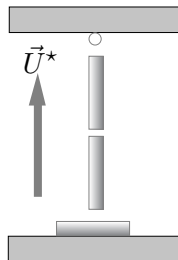
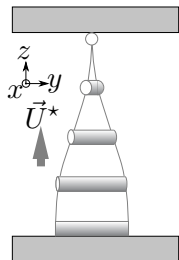
- first order transition at $T^* = 1.1232 \pm 0.0005$

Electric field influence :

- shifts transition temperature and critical point for strong fields

LCD and Fréedericksz :

- Lebwohl-Laser model can be used to model a LCD pixel



Perspectives :

- Find the value of the critical field in that Fréedericksz transition
- Study the temperature dependence of that transition

Thank you for your attention