Chapter_6_regression_trees_example

Fran Camacho

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Chapter 6 - Regression trees example

Example from the book "Machine Learning with R", by Brett Lantz:

Estimating the quality of wines with regression trees and model trees

Step 1 – collecting data

In this case study, we will use regression trees and model trees to create a system capable of mimicking expert ratings of wine. Because trees result in a model that is readily understood, this could allow winemakers to identify key factors that contribute to better-rated wines.

Step 2 – exploring and preparing the data

The wine data includes 11 features and the quality outcome, as follows:

```
str(wine)
## 'data.frame':
                   4898 obs. of 12 variables:
## $ fixed.acidity
                         : num 6.7 5.7 5.9 5.3 6.4 7 7.9 6.6 7 6.5 ...
## $ volatile.acidity
                         : num 0.62 0.22 0.19 0.47 0.29 0.14 0.12 0.38 0.16 0.37 ...
                         : num 0.24 0.2 0.26 0.1 0.21 0.41 0.49 0.28 0.3 0.33 ...
## $ citric.acid
## $ residual.sugar
                                1.1 16 7.4 1.3 9.65 0.9 5.2 2.8 2.6 3.9 ...
                         : num
                         : num 0.039 0.044 0.034 0.036 0.041 0.037 0.049 0.043 0.043 0.027 ...
## $ chlorides
## $ free.sulfur.dioxide : num 6 41 33 11 36 22 33 17 34 40 ...
## $ total.sulfur.dioxide: num 62 113 123 74 119 95 152 67 90 130 ...
```

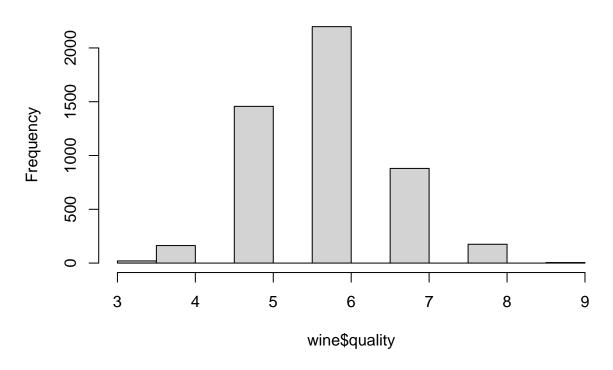
```
##
    $ density
                                  0.993 0.999 0.995 0.991 0.993 ...
                           : num
##
    $ pH
                                  3.41 3.22 3.49 3.48 2.99 3.25 3.18 3.21 2.88 3.28 ...
    $ sulphates
                                  0.32 0.46 0.42 0.54 0.34 0.43 0.47 0.47 0.47 0.39 ...
##
    $ alcohol
                                  10.4 8.9 10.1 11.2 10.9 ...
##
                             num
    $ quality
                             int
                                  5 6 6 4 6 6 6 6 6 7 ...
```

Compared with other types of machine learning models, one of the advantages of trees is that they can handle many types of data without preprocessing. This means we do not need to normalize or standardize the features.

However, a bit of effort to examine the distribution of the outcome variable is needed to inform our evaluation of the model's performance. For instance, suppose that there was very little vari- ation in quality from wine to wine, or that wines fell into a bimodal distribution: either very good or very bad. This may impact the way we design the model. To check for such extremes, we can examine the distribution of wine quality using a histogram:

```
hist(wine$quality)
```





The wine quality values appear to follow a roughly normal, bell-shaped distribution, centered around a value of six. This makes sense intuitively, because most wines are of average quality.

Our last step, then, is to divide the dataset into training and testing sets. Since the wine dataset was already sorted randomly, we can partition it into two sets of contiguous rows as follows:

```
wine_train <- wine[1:3750, ]
wine_test <- wine[3751:4898, ]</pre>
```

Step 3 – training a model on the data

```
#resulting regression tree model object is named m.rpart to distinguish it from the model tree we will
m.rpart <- rpart(quality ~ ., data = wine_train)</pre>
```

For basic information about the tree, simply type the name of the model object:

m.rpart

```
## n= 3750
##
## node), split, n, deviance, yval
##
         * denotes terminal node
##
    1) root 3750 2945.53200 5.870933
##
##
      2) alcohol< 10.85 2372 1418.86100 5.604975
##
        4) volatile.acidity>=0.2275 1611 821.30730 5.432030
##
          8) volatile.acidity>=0.3025 688 278.97670 5.255814 *
          9) volatile.acidity< 0.3025 923
##
                                           505.04230 5.563380 *
##
        5) volatile.acidity< 0.2275 761 447.36400 5.971091 *
##
      3) alcohol>=10.85 1378 1070.08200 6.328737
        6) free.sulfur.dioxide< 10.5 84
##
                                          95.55952 5.369048 *
##
        7) free.sulfur.dioxide>=10.5 1294 892.13600 6.391036
         14) alcohol< 11.76667 629 430.11130 6.173291
##
##
           28) volatile.acidity>=0.465 11
                                             10.72727 4.545455 *
           29) volatile.acidity< 0.465 618 389.71680 6.202265 *
##
         15) alcohol>=11.76667 665 403.99400 6.596992 *
##
```

For each node in the tree, the number of examples reaching the decision point is listed. For instance, all 3,750 examples begin at the root node, of which 2,372 have alcohol < 10.85 and 1,378 have alcohol >= 10.85.

Nodes indicated by * are terminal or leaf nodes, which means that they result in a prediction (listed here as yval). For example, node 5 has a yval of 5.971091. When the tree is used for predictions, any wine samples with alcohol < 10.85 and volatile.acidity < 0.2275 would therefore be predicted to have a quality value of 5.97.

A more detailed summary of the tree's fit:

summary(m.rpart)

```
## Call:
## rpart(formula = quality ~ ., data = wine_train)
##
     n = 3750
##
##
             CP nsplit rel error
                                     xerror
## 1 0.15501053
                     0 1.0000000 1.0002107 0.02445665
## 2 0.05098911
                     1 0.8449895 0.8456859 0.02335357
## 3 0.02796998
                     2 0.7940004 0.8025987 0.02276633
## 4 0.01970128
                     3 0.7660304 0.7779622 0.02156654
## 5 0.01265926
                     4 0.7463291 0.7584318 0.02078557
## 6 0.01007193
                     5 0.7336698 0.7517638 0.02067768
## 7 0.01000000
                     6 0.7235979 0.7456693 0.02065742
```

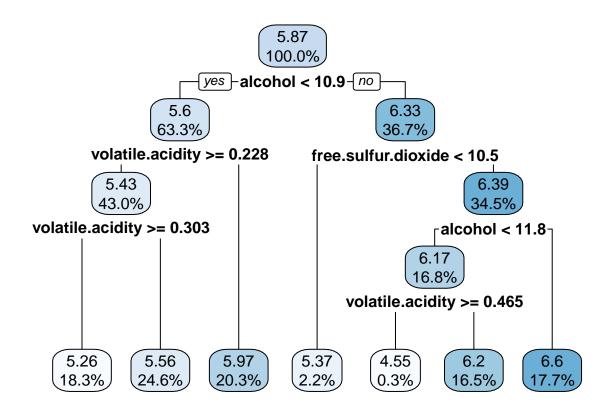
```
##
## Variable importance
##
                alcohol
                                      density
                                                   volatile.acidity
##
                     34
                                           21
                                                                 15
##
              chlorides total.sulfur.dioxide
                                               free.sulfur.dioxide
##
         residual.sugar
##
                                    sulphates
                                                        citric.acid
##
                                            1
##
##
  Node number 1: 3750 observations,
                                         complexity param=0.1550105
##
     mean=5.870933, MSE=0.7854751
##
     left son=2 (2372 obs) right son=3 (1378 obs)
##
     Primary splits:
                               < 10.85
                                          to the left, improve=0.15501050, (0 missing)
##
         alcohol
##
                               < 0.992035 to the right, improve=0.10915940, (0 missing)
         density
##
         chlorides
                               < 0.0395
                                          to the right, improve=0.07682258, (0 missing)
##
                                          to the right, improve=0.04089663, (0 missing)
         total.sulfur.dioxide < 158.5
##
         citric.acid
                               < 0.235
                                          to the left, improve=0.03636458, (0 missing)
##
     Surrogate splits:
##
         density
                               < 0.991995 to the right, agree=0.869, adj=0.644, (0 split)
##
         chlorides
                               < 0.0375
                                          to the right, agree=0.757, adj=0.339, (0 split)
##
         total.sulfur.dioxide < 103.5
                                          to the right, agree=0.690, adj=0.155, (0 split)
                                          to the right, agree=0.667, adj=0.094, (0 split)
##
         residual.sugar
                               < 5.375
                               < 0.345
                                          to the right, agree=0.647, adj=0.038, (0 split)
##
         sulphates
##
## Node number 2: 2372 observations,
                                         complexity param=0.05098911
     mean=5.604975, MSE=0.5981709
##
     left son=4 (1611 obs) right son=5 (761 obs)
##
##
     Primary splits:
##
         volatile.acidity
                              < 0.2275
                                         to the right, improve=0.10585250, (0 missing)
                                         to the left, improve=0.03390500, (0 missing)
##
         free.sulfur.dioxide < 13.5
##
         citric.acid
                             < 0.235
                                         to the left, improve=0.03204075, (0 missing)
##
         alcohol
                              < 10.11667 to the left,
                                                       improve=0.03136524, (0 missing)
##
                              < 0.0585
                                         to the right, improve=0.01633599, (0 missing)
         chlorides
##
     Surrogate splits:
##
                               < 3.485
                                          to the left, agree=0.694, adj=0.047, (0 split)
         Нq
##
         sulphates
                               < 0.755
                                          to the left, agree=0.685, adj=0.020, (0 split)
##
         total.sulfur.dioxide < 105.5
                                          to the right, agree=0.683, adj=0.011, (0 split)
##
         residual.sugar
                               < 0.75
                                          to the right, agree=0.681, adj=0.007, (0 split)
##
         chlorides
                               < 0.0285
                                          to the right, agree=0.680, adj=0.003, (0 split)
##
## Node number 3: 1378 observations,
                                         complexity param=0.02796998
     mean=6.328737, MSE=0.7765472
##
     left son=6 (84 obs) right son=7 (1294 obs)
##
##
     Primary splits:
                                                         improve=0.07699080, (0 missing)
         free.sulfur.dioxide < 10.5</pre>
##
                                          to the left,
##
         alcohol
                               < 11.76667 to the left,
                                                         improve=0.06210660, (0 missing)
##
         total.sulfur.dioxide < 67.5
                                          to the left,
                                                         improve=0.04438619, (0 missing)
##
         residual.sugar
                               < 1.375
                                          to the left,
                                                        improve=0.02905351, (0 missing)
##
         fixed.acidity
                               < 7.35
                                          to the right, improve=0.02613259, (0 missing)
##
     Surrogate splits:
                                          to the left, agree=0.952, adj=0.214, (0 split)
##
         total.sulfur.dioxide < 53.5
##
         volatile.acidity
                               < 0.875
                                          to the right, agree=0.940, adj=0.024, (0 split)
##
```

```
## Node number 4: 1611 observations,
                                         complexity param=0.01265926
     mean=5.43203, MSE=0.5098121
##
     left son=8 (688 obs) right son=9 (923 obs)
##
##
     Primary splits:
##
         volatile.acidity
                             < 0.3025
                                        to the right, improve=0.04540111, (0 missing)
         alcohol
                             < 10.05
                                        to the left, improve=0.03874403, (0 missing)
##
         free.sulfur.dioxide < 13.5
                                        to the left, improve=0.03338886, (0 missing)
##
                                         to the right, improve=0.02574623, (0 missing)
         chlorides
##
                             < 0.0495
##
         citric.acid
                             < 0.195
                                         to the left, improve=0.02327981, (0 missing)
##
     Surrogate splits:
##
         citric.acid
                              < 0.215
                                          to the left, agree=0.633, adj=0.141, (0 split)
                                          to the left, agree=0.600, adj=0.063, (0 split)
##
         free.sulfur.dioxide < 20.5
##
         chlorides
                              < 0.0595
                                          to the right, agree=0.593, adj=0.047, (0 split)
##
                                          to the left, agree=0.583, adj=0.023, (0 split)
         residual.sugar
                              < 1.15
##
         total.sulfur.dioxide < 219.25
                                         to the right, agree=0.582, adj=0.022, (0 split)
##
## Node number 5: 761 observations
     mean=5.971091, MSE=0.5878633
##
##
## Node number 6: 84 observations
##
     mean=5.369048, MSE=1.137613
##
## Node number 7: 1294 observations,
                                         complexity param=0.01970128
     mean=6.391036, MSE=0.6894405
##
     left son=14 (629 obs) right son=15 (665 obs)
##
##
     Primary splits:
##
         alcohol
                              < 11.76667 to the left, improve=0.06504696, (0 missing)
                                         to the right, improve=0.02758705, (0 missing)
##
         chlorides
                              < 0.0395
                                          to the right, improve=0.02750932, (0 missing)
##
                              < 7.35
         fixed.acidity
                                         to the left, improve=0.02307356, (0 missing)
##
                              < 3.055
         рΗ
                                         to the right, improve=0.02186818, (0 missing)
##
         total.sulfur.dioxide < 191.5
##
     Surrogate splits:
##
         density
                              < 0.990885 to the right, agree=0.720, adj=0.424, (0 split)
##
         volatile.acidity
                                         to the left, agree=0.637, adj=0.253, (0 split)
                              < 0.2675
                                         to the right, agree=0.630, adj=0.238, (0 split)
##
         chlorides
                              < 0.0365
##
         residual.sugar
                              < 1.475
                                         to the left, agree=0.575, adj=0.126, (0 split)
##
         total.sulfur.dioxide < 128.5
                                         to the right, agree=0.574, adj=0.124, (0 split)
##
## Node number 8: 688 observations
     mean=5.255814, MSE=0.4054895
##
##
## Node number 9: 923 observations
     mean=5.56338, MSE=0.5471747
##
##
                                         complexity param=0.01007193
## Node number 14: 629 observations,
     mean=6.173291, MSE=0.6838017
##
##
     left son=28 (11 obs) right son=29 (618 obs)
##
     Primary splits:
##
         volatile.acidity
                              < 0.465
                                          to the right, improve=0.06897561, (0 missing)
                                          to the right, improve=0.04223066, (0 missing)
##
         total.sulfur.dioxide < 200
##
                                          to the left, improve=0.03061714, (0 missing)
         residual.sugar
                              < 0.975
                                         to the right, improve=0.02978501, (0 missing)
##
         fixed.acidity
                              < 7.35
##
         sulphates
                              < 0.575
                                         to the left, improve=0.02165970, (0 missing)
##
     Surrogate splits:
```

```
##
         citric.acid
                              < 0.045
                                         to the left, agree=0.986, adj=0.182, (0 split)
##
         total.sulfur.dioxide < 279.25
                                         to the right, agree=0.986, adj=0.182, (0 split)
##
## Node number 15: 665 observations
##
    mean=6.596992, MSE=0.6075098
##
## Node number 28: 11 observations
     mean=4.545455, MSE=0.9752066
##
##
## Node number 29: 618 observations
     mean=6.202265, MSE=0.6306098
```

Visualizing decision trees

```
rpart.plot(m.rpart, digits = 3)
```



Step 4 – evaluating model performance

```
p.rpart <- predict(m.rpart, wine_test)</pre>
```

A quick look at the summary statistics of our predictions suggests a potential problem: the predictions fall into a much narrower range than the true values:

```
summary(p.rpart)
##
                     Median
                                Mean 3rd Qu.
      Min. 1st Qu.
                                                 Max.
##
     4.545
              5.563
                      5.971
                               5.893
                                        6.202
                                                 6.597
summary(wine_test$quality)
##
      Min. 1st Qu.
                                Mean 3rd Qu.
                     Median
                                                  Max.
              5.000
                      6.000
                                                 9.000
     3.000
                               5.901
                                        6.000
```

This finding suggests that the model is not correctly identifying the extreme cases, and in particular, the best and worst wines.

The correlation between the predicted and actual quality values provides a simple way to gauge the model's performance.

```
cor(p.rpart, wine_test$quality)
```

[1] 0.5369525

A correlation of 0.54 is certainly acceptable. However, the correlation only measures how strongly the predictions are related to the true value; it is not a measure of how far off the predictions were from the true values.

Measuring performance with the mean absolute error

```
MAE <- function(actual, predicted) {
   mean(abs(actual - predicted))
}

MAE(p.rpart, wine_test$quality)</pre>
```

```
## [1] 0.5872652
```

This implies that, on average, the difference between our model's predictions and the true quality score was about 0.59. On a quality scale from 0 to 10, this seems to suggest that our model is doing fairly well.

On the other hand, recall that most wines were neither very good nor very bad; the typical quality score was around 5 to 6. Therefore, a classifier that did nothing but predict the mean value may also do fairly well according to this metric.

```
mean(wine_train$quality)
```

```
## [1] 5.870933
```

If we predicted the value 5.87 for every wine sample, we would have a MAE of only about 0.67:

```
MAE(5.87, wine_test$quality)
```

```
## [1] 0.6722474
```

Our regression tree (MAE = 0.59) comes closer on average to the true quality score than the imputed mean (MAE = 0.67), but not by much. In comparison, Cortez reported an MAE of 0.58 for the neural network model and an MAE of 0.45 for the support vector machine. This suggests that there is room for improvement.

Step 5 – improving model performance

To improve the performance of our learner, let's apply a model tree algorithm, which is a more complex application of trees to numeric prediction. Recall that a model tree extends regression trees by replacing the leaf nodes with regression models. This often results in more accurate results than regression trees, which use only a single numeric value for the prediction at the leaf nodes.

The current state-of-the-art in model trees is the **Cubist** algorithm, which itself is an enhance- ment of the M5 model tree algorithm

```
library(Cubist)
## Lade nötiges Paket: lattice
m.cubist <- cubist(x = wine_train[-12], y = wine_train$quality)</pre>
m.cubist
##
## Call:
## cubist.default(x = wine_train[-12], y = wine_train$quality)
## Number of samples: 3750
## Number of predictors: 11
##
## Number of committees: 1
## Number of rules: 25
summary(m.cubist)
##
## Call:
## cubist.default(x = wine_train[-12], y = wine_train$quality)
##
##
## Cubist [Release 2.07 GPL Edition] Wed Feb 12 13:32:56 2025
##
##
##
       Target attribute 'outcome'
##
## Read 3750 cases (12 attributes) from undefined.data
##
## Model:
##
    Rule 1: [21 cases, mean 5.0, range 4 to 6, est err 0.5]
##
##
##
       if
##
   free.sulfur.dioxide > 30
##
    total.sulfur.dioxide > 195
   total.sulfur.dioxide <= 235
##
  sulphates > 0.64
## alcohol > 9.1
```

```
##
##
   outcome = 573.6 + 0.0478 total.sulfur.dioxide - 573 density
##
              - 0.788 alcohol + 0.186 residual.sugar - 4.73 volatile.acidity
##
##
    Rule 2: [28 cases, mean 5.0, range 4 to 8, est err 0.7]
##
##
##
   volatile.acidity > 0.31
##
   citric.acid <= 0.36
## residual.sugar <= 1.45
  total.sulfur.dioxide <= 97
   alcohol > 9.1
##
##
       then
   outcome = 168.2 + 4.75 citric.acid + 0.0123 total.sulfur.dioxide
##
##
              - 170 density + 0.057 residual.sugar - 6.4 chlorides + 0.84 pH
##
              + 0.14 fixed.acidity
##
##
     Rule 3: [171 cases, mean 5.1, range 3 to 6, est err 0.3]
##
##
       if
##
  volatile.acidity > 0.205
   chlorides <= 0.054
##
   density <= 0.99839
##
   alcohol <= 9.1
##
##
       then
##
   outcome = 147.4 - 144 density + 0.08 residual.sugar + 0.117 alcohol
##
              - 0.87 volatile.acidity - 0.09 pH - 0.01 fixed.acidity
##
##
     Rule 4: [37 cases, mean 5.3, range 3 to 6, est err 0.5]
##
##
       if
##
   free.sulfur.dioxide > 30
##
   total.sulfur.dioxide > 235
   alcohol > 9.1
##
##
       then
##
  outcome = 19.5 - 0.013 total.sulfur.dioxide - 2.7 volatile.acidity
##
              - 10 density + 0.005 residual.sugar + 0.008 alcohol
##
##
    Rule 5: [64 cases, mean 5.3, range 5 to 6, est err 0.3]
##
##
       if
##
   volatile.acidity > 0.205
##
   residual.sugar > 17.85
##
       then
   outcome = -23.6 + 0.233 alcohol - 5.2 chlorides - 0.75 citric.acid
##
##
              + 28 density - 0.81 volatile.acidity - 0.19 pH
##
              - 0.002 residual.sugar
##
##
     Rule 6: [56 cases, mean 5.3, range 4 to 7, est err 0.6]
##
##
       if
## fixed.acidity <= 7.1
## volatile.acidity > 0.205
## chlorides > 0.054
```

```
density <= 0.99839
##
   alcohol <= 9.1
##
       then
##
   outcome = 40.6 + 0.374 alcohol - 1.62 volatile.acidity
##
              + 0.026 residual.sugar - 38 density - 0.21 pH
              - 0.01 fixed.acidity
##
##
     Rule 7: [337 cases, mean 5.3, range 3 to 7, est err 0.4]
##
##
##
       if
##
  fixed.acidity <= 7.8
## volatile.acidity > 0.305
## chlorides <= 0.09
## free.sulfur.dioxide <= 82.5
## total.sulfur.dioxide > 130
## total.sulfur.dioxide <= 235
## sulphates <= 0.64
##
   alcohol \leq 10.4
##
       then
##
   outcome = -32.1 + 0.233 alcohol -9.7 chlorides
##
              + 0.0038 total.sulfur.dioxide - 0.0081 free.sulfur.dioxide
##
              + 35 density + 0.81 volatile.acidity
##
##
     Rule 8: [30 cases, mean 5.5, range 3 to 7, est err 0.5]
##
##
## fixed.acidity > 7.1
## volatile.acidity > 0.205
  chlorides > 0.054
## density <= 0.99839
##
   alcohol <= 9.1
##
       then
##
   outcome = 244 - 1.56 fixed.acidity - 228 density
##
              + 0.0252 free.sulfur.dioxide - 7.3 chlorides
##
              - 0.19 volatile.acidity + 0.003 residual.sugar
##
##
    Rule 9: [98 cases, mean 5.5, range 4 to 8, est err 0.5]
##
##
       if
##
  volatile.acidity > 0.155
   chlorides > 0.09
   total.sulfur.dioxide <= 235
##
##
   sulphates <= 0.64
##
       then
   outcome = 55.9 - 3.85 volatile.acidity - 52 density
##
##
              + 0.023 residual.sugar + 0.092 alcohol + 0.35 pH
##
              + 0.05 fixed.acidity + 0.3 sulphates
##
              + 0.001 free.sulfur.dioxide
##
     Rule 10: [446 cases, mean 5.6, range 4 to 8, est err 0.5]
##
##
##
       if
## fixed.acidity <= 7.8
## volatile.acidity > 0.155
```

```
## volatile.acidity <= 0.305
## chlorides <= 0.09
## free.sulfur.dioxide <= 82.5
## total.sulfur.dioxide > 130
## total.sulfur.dioxide <= 235
## sulphates <= 0.64
## alcohol > 9.1
## alcohol <= 10.4
##
       then
   outcome = 15.1 + 0.35 alcohol - 3.09 volatile.acidity - 14.7 chlorides
##
              + 1.16 sulphates - 0.0022 total.sulfur.dioxide
##
              + 0.11 fixed.acidity + 0.45 pH + 0.5 citric.acid - 14 density
##
              + 0.006 residual.sugar
##
##
    Rule 11: [31 cases, mean 5.6, range 3 to 8, est err 0.8]
##
##
##
  volatile.acidity > 0.31
## citric.acid > 0.36
## free.sulfur.dioxide <= 30
## total.sulfur.dioxide <= 97
##
##
   outcome = 3.2 + 0.0584 total.sulfur.dioxide + 7.77 volatile.acidity
##
              + 0.328 alcohol - 9 density + 0.003 residual.sugar
##
##
    Rule 12: [20 cases, mean 5.7, range 3 to 8, est err 0.9]
##
##
  free.sulfur.dioxide > 82.5
##
  total.sulfur.dioxide <= 235
##
   sulphates <= 0.64
##
   alcohol > 9.1
##
       then
##
   outcome = -8.9 + 109.3 chlorides + 0.948 alcohol
##
##
    Rule 13: [331 cases, mean 5.8, range 4 to 8, est err 0.5]
##
##
       if
##
   volatile.acidity > 0.31
## free.sulfur.dioxide <= 30
  total.sulfur.dioxide > 97
## alcohol > 9.1
##
       then
   outcome = 89.8 + 0.0234 free.sulfur.dioxide + 0.324 alcohol
##
              + 0.07 residual.sugar - 90 density - 1.47 volatile.acidity
##
##
              + 0.48 pH
##
##
     Rule 14: [116 cases, mean 5.8, range 3 to 8, est err 0.6]
##
##
       if
## fixed.acidity > 7.8
## volatile.acidity > 0.155
## free.sulfur.dioxide > 30
## total.sulfur.dioxide > 130
```

```
## total.sulfur.dioxide <= 235
## sulphates <= 0.64
##
   alcohol > 9.1
##
       then
##
   outcome = 6 + 0.346 alcohol - 0.41 fixed.acidity - 1.69 volatile.acidity
              - 2.9 chlorides + 0.19 sulphates + 0.07 pH
##
##
     Rule 15: [115 cases, mean 5.8, range 4 to 7, est err 0.5]
##
##
##
       if
   volatile.acidity > 0.205
   residual.sugar <= 17.85
##
   density > 0.99839
   alcohol \leq 9.1
##
##
       then
##
   outcome = -110.2 + 120 density -3.46 volatile.acidity -0.97 pH
##
              - 0.022 residual.sugar + 0.088 alcohol - 0.6 citric.acid
##
              - 0.01 fixed.acidity
##
##
    Rule 16: [986 cases, mean 5.9, range 3 to 9, est err 0.6]
##
##
       if
   volatile.acidity <= 0.31
##
   free.sulfur.dioxide <= 30
##
   alcohol > 9.1
##
##
       then
##
   outcome = 280.4 - 282 density + 0.128 residual.sugar
              + 0.0264 free.sulfur.dioxide - 3 volatile.acidity + 1.2 pH
##
##
              + 0.65 citric.acid + 0.09 fixed.acidity + 0.56 sulphates
              + 0.015 alcohol
##
##
##
    Rule 17: [49 cases, mean 6.0, range 5 to 8, est err 0.5]
##
##
       if
## volatile.acidity > 0.155
## residual.sugar > 8.8
## free.sulfur.dioxide > 30
## total.sulfur.dioxide <= 130
   pH <= 3.26
##
##
   alcohol > 9.1
##
       then
##
   outcome = 173.5 - 169 density + 0.055 alcohol + 0.38 sulphates
##
              + 0.002 residual.sugar
##
    Rule 18: [114 cases, mean 6.1, range 3 to 9, est err 0.6]
##
##
##
       if
## volatile.acidity > 0.31
## citric.acid <= 0.36
## residual.sugar > 1.45
## total.sulfur.dioxide <= 97
## alcohol > 9.1
##
       then
## outcome = 302.3 - 305 density + 0.0128 total.sulfur.dioxide
```

```
##
              + 0.096 residual.sugar + 1.94 citric.acid + 1.05 pH
##
              + 0.17 fixed.acidity - 6.7 chlorides
##
              + 0.0022 free.sulfur.dioxide - 0.21 volatile.acidity
              + 0.013 alcohol + 0.09 sulphates
##
##
    Rule 19: [145 cases, mean 6.1, range 5 to 8, est err 0.6]
##
##
##
       if
##
   volatile.acidity > 0.155
##
  free.sulfur.dioxide > 30
   total.sulfur.dioxide <= 195
   sulphates > 0.64
##
##
       then
   outcome = 206 - 209 density + 0.069 residual.sugar + 0.38 fixed.acidity
##
##
              + 2.79 sulphates + 0.0155 free.sulfur.dioxide
##
              - 0.0051 total.sulfur.dioxide - 1.71 citric.acid + 1.04 pH
##
##
     Rule 20: [555 cases, mean 6.1, range 3 to 9, est err 0.6]
##
##
       if
##
   total.sulfur.dioxide > 130
   total.sulfur.dioxide <= 235
   sulphates <= 0.64
##
   alcohol > 10.4
##
       then
##
##
   outcome = 108 + 0.276 alcohol - 109 density + 0.05 residual.sugar
##
              + 0.77 pH - 1.02 volatile.acidity - 4.2 chlorides
              + 0.78 sulphates + 0.08 fixed.acidity
##
              + 0.0016 free.sulfur.dioxide - 0.0003 total.sulfur.dioxide
##
##
##
     Rule 21: [73 cases, mean 6.2, range 4 to 8, est err 0.4]
##
##
## volatile.acidity > 0.155
## citric.acid <= 0.28
## residual.sugar <= 8.8
## free.sulfur.dioxide > 30
## total.sulfur.dioxide <= 130
   pH <= 3.26
##
## sulphates <= 0.64
  alcohol > 9.1
##
       then
   outcome = 4.2 + 0.147 residual.sugar + 0.47 alcohol + 3.75 sulphates
##
              - 2.5 volatile.acidity - 5 density
##
##
##
     Rule 22: [244 cases, mean 6.3, range 4 to 8, est err 0.6]
##
##
       if
## citric.acid > 0.28
## residual.sugar <= 8.8
## free.sulfur.dioxide > 30
## total.sulfur.dioxide <= 130
## pH <= 3.26
##
       then
```

```
outcome = 40.1 + 0.278 alcohol + 1.3 sulphates - 39 density
##
              + 0.017 residual.sugar + 0.001 total.sulfur.dioxide + 0.17 pH
##
              + 0.03 fixed.acidity
##
##
     Rule 23: [106 cases, mean 6.3, range 4 to 8, est err 0.6]
##
##
##
   volatile.acidity <= 0.155
##
   free.sulfur.dioxide > 30
##
       then
##
   outcome = 139.1 - 138 density + 0.058 residual.sugar + 0.71 pH
              + 0.92 sulphates + 0.11 fixed.acidity - 0.73 volatile.acidity
##
              + 0.055 alcohol - 0.0012 total.sulfur.dioxide
##
              + 0.0007 free.sulfur.dioxide
##
##
##
     Rule 24: [137 cases, mean 6.5, range 4 to 9, est err 0.6]
##
##
       if
## volatile.acidity > 0.155
## free.sulfur.dioxide > 30
## total.sulfur.dioxide <= 130
## pH > 3.26
## sulphates <= 0.64
##
   alcohol > 9.1
##
       then
   outcome = 114.2 + 0.0142 total.sulfur.dioxide - 107 density
##
              - 11.8 chlorides - 1.57 pH + 0.124 alcohol + 1.21 sulphates
              + 1.16 volatile.acidity + 0.021 residual.sugar
##
##
              + 0.04 fixed.acidity
##
##
     Rule 25: [92 cases, mean 6.5, range 4 to 8, est err 0.6]
##
##
##
   volatile.acidity <= 0.205
##
   alcohol \leq 9.1
##
       then
##
   outcome = -200.7 + 210 density + 5.88 volatile.acidity + 23.9 chlorides
##
              - 2.83 citric.acid - 1.17 pH
##
##
## Evaluation on training data (3750 cases):
##
       Average |error|
                                       0.5
##
##
       Relative |error|
                                       0.67
##
       Correlation coefficient
                                       0.66
##
##
   Attribute usage:
##
##
      Conds Model
##
       84%
##
              93%
                     alcohol
##
       80%
              89%
                     volatile.acidity
##
       70%
              61%
                     free.sulfur.dioxide
       63%
              50%
                     total.sulfur.dioxide
##
```

```
44%
              70%
                      sulphates
##
                      chlorides
##
       26%
              44%
       22%
              76%
                      fixed.acidity
##
##
       16%
              87%
                      residual.sugar
##
       11%
              86%
                      Нq
##
       11%
              45%
                      citric.acid
##
        8%
              97%
                      density
##
##
## Time: 0.4 secs
output:
"Rule 1: [21 cases, mean 5.0, range 4 to 6, est err 0.5]
if
free.sulfur.dioxide > 30
total.sulfur.dioxide > 195
total.sulfur.dioxide <= 235
sulphates > 0.64
alcohol > 9.1
then
outcome = **573.6 + 0.0478 total.sulfur.dioxide - 573 density**
          **- 0.788 alcohol + 0.186 residual.sugar - 4.73 volatile.acidity**
Rule 25: [92 cases, mean 6.5, range 4 to 8, est err 0.6]
volatile.acidity <= 0.205
alcohol <= 9.1
outcome = **-200.7 + 210 density + 5.88 volatile.acidity + 23.9 chlorides**
          **- 2.83 citric.acid - 1.17 pH**
Evaluation on training data (3750 cases):
                                 0.5
Average |error|
Relative |error|
                                0.67
Correlation coefficient
                                0.66
Attribute usage:
  Conds Model
   84%
          93%
                 alcohol
   80%
          89%
                 volatile.acidity
                 free.sulfur.dioxide
   70%
          61%
          50%
                 total.sulfur.dioxide
   63%
   44%
          70%
                 sulphates
```

```
26%
       44%
               chlorides
22%
       76%
              fixed.acidity
16%
       87%
              residual.sugar
11%
       86%
              рΗ
11%
       45%
              citric.acid
8%
       97%
              density
```

,,

the if portion of the output is somewhat like the regression tree we built earlier. A series of decisions based on the wine properties of sulfur dioxide, sulphates, and alcohol creates a rule culminating in the final prediction. A key difference between this model tree output and the earlier regression tree output, however, is that **the nodes here terminate not in a numeric prediction**, **but rather in a linear model.**

It is important to note that the regression effects estimated by this model apply only to wine samples reaching this node

To examine the performance of this model, we'll look at how well it performs on the unseen test data. The predict() function gets us a vector of predicted values:

```
p.cubist <- predict(m.cubist, wine_test)
summary(p.cubist)</pre>
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 3.677 5.416 5.906 5.848 6.238 7.393
```

The model tree appears to be predicting a wider range of values than the regression tree

Correlation:

```
cor(p.cubist, wine_test$quality)
```

```
## [1] 0.6201015
```

Furthermore, the model slightly reduced the MAE:

```
MAE(wine_test$quality, p.cubist)
```

```
## [1] 0.5339725
```

Although we did not improve a great deal beyond the regression tree, we surpassed the performance of the neural network model published by Cortez, and we are getting closer to the published MAE value of 0.45 for the support vector machine model, all while using a much simpler learning method.