## Package 'BBMV'

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BBMV-package Models for continuous traits evolving in macroevolutionary land-

scapes of any shape

#### **Description**

This package provides a set of functions to fit general macroevolutionary models for continuous traits evolving in adaptive landscapes of any shape. The model is based on bounded Brownian motion (BBM), in which a continuous trait evolves along a phylogenetic tree under constant-rate diffusion between two reflective bounds. In addition to this random component, the trait evolves in a potential and is thus subject to a force that pulls it towards specific values - this force can be of any shape.

#### **Details**

Package: BBMV Type: Package

Title: Models for continuous traits evolving in macroevolutionary landscapes of any shape

Version: 1.0

Date: 2016-04-28 Author: Florian C. Boucher

Maintainer: Florian C. Boucher <flofloboucher@gmail.com>

Depends: R (>= 3.1.0), ape Suggests: coda, geiger

Description: This package provides a set of functions to fit general macroevolutionary models for continuous traits evol-

License: GPL-2

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#### Author(s)

Florian C. Boucher Maintainer: Florian C. Boucher <flofloboucher@gmail.com>

#### References

Inferring bounded evolution in phenotypic characters from phylogenetic comparative data. F.C. Boucher and V. Demery. Systematic Biology, 65, 651-661, 2016

A general model for estimating macroevolutionary landscapes from phylogenetic comparative data. F.C. Boucher, V. Demery, E. Conti, L. J. Harmon and J. Uyeda. Submitted

charac\_time

Characteristic time measurement

#### **Description**

Calculate the characteristic time it takes for the BBM+V process to reach its stationary distribution.

#### Usage

```
charac_time(Npts, model)
```

## Arguments

Npts The number of points used in the discretization procedure.

model A BBM+V model fit, as returned by fit\_BBMV.

#### Value

The function returns the characteristic time of the process as a numeric value.

#### Author(s)

F. C. Boucher

```
# Simulate data: tree + continuous trait
library(geiger)
tree=sim.bdtree(stop='taxa',n=10) # tree with few tips for quick tests
tree$edge.length=100*tree$edge.length/max(branching.times(tree)) # rescale the tree
# Simulate trait evolving on the tree with a linear trend towards small values
TRAIT= Sim_BBMV(tree,x0=0,V=seq(from=0,to=5,length.out=50),sigma=10,bounds=c(-5, 5))
# fit a model with a linear potential:
BBM_x=fit_BBMV(tree,TRAIT,Npts=10,method='Nelder-Mead',verbose=TRUE,V_shape='linear')
# measure time to reach stationarity
```

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```
charac_time(Npts=10, BBM_x)
# compare it with tree depth
max(branching.times(tree))
```

ConvProp\_bounds

Convolution of the diffusion matrix with the trait density vector.

## Description

Internal function used for likelihood calculation and simulation.

## Usage

```
ConvProp_bounds(X, t, prep_mat)
```

#### **Arguments**

X A trait density vector.

t The time over which to do the convolution (usually the length of one branch).

prep\_mat The diagonalized diffusion matrix.

#### Author(s)

F. C. Boucher

DiffMat\_backwards

Diffusion matrix building

#### **Description**

Internal function that builds the discretized diffusion matrix of the BBM+V process going backwards in time (for likelihood calculations)

#### Usage

```
DiffMat_backwards(V)
```

## **Arguments**

٧

A vector giving the values of the evolutionary potential (V) at each point in the gridded trait interval.

#### Author(s)

DiffMat\_forward 5

## Description

Internal function that builds the discretized diffusion matrix of the BBM+V process going forward in time (for simulations)

#### Usage

DiffMat\_forward(V)

#### **Arguments**

V A vector giving the values of the evolutionary potential (V) at each point in the

gridded trait interval.

#### Author(s)

F.C. Boucher

fit_BBMV	Main function to fit the BBM+V model	

## Description

Fits various forms of the BBM+V model to trait data and a phylogeny, using maximum likelihood.

## Usage

```
fit_BBMV(tree, trait, Npts = 50, method = "Nelder-Mead", verbose = T, V_shape, bounds = "estimate";
```

## Arguments

tree	A phylogenetic tree in phylo format
trait	A named vector of trait values for the tips of the tree. It should match tip labels in the phylogeny.
Npts	The number of points used in the discretization procedure.
method	The optimization routine used.
verbose	If TRUE, prints progress to the screen.
V_shape	The shape of the evolutionary potential. This should be one of 'flat', 'linear', 'quadratic', or 'full'. Alternatively, a given potential can be specified using a vector of values for V, along with bounds.
bounds	Describes how to treat the bounds. If set to 'estimate' (the default), bounds will be estimated along with other parameters. Alternatively, you can fix two bounds by specifying a numeric vector containing the minimum and maximum bound of the trait interval as the first and second element, respectively.
init.optim	A parameter combination from which to start the optimization procedure, specified as a numeric vector. Default to NULL should work in most of the cases.

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#### **Details**

Only 'Nelder-Mead' (the default, which we found to be more reliable) and 'L-BFGS-B' are supported as optimization methods. For further details on both methods see the help of the optim function.

The different values for V\_shape refer to the following shapes of the evolutionary potential: (1) 'flat' is a flat potential as in BBM, i.e. V(x)=0; (2) 'linear' is a linear potential, i.e. V(x)=c.x; (3) 'quadratic' is a quadratic potential, i.e.  $V(x)=b.x^2+c.x$ ; (4) 'full' is a potential with three polynomial terms, i.e.  $V(x)=a.x^4+b.x^2+c.x$ .

#### Value

A list with the following elements:

par The ML estimates of model parameters: the two bounds of the trait interval

(\$bounds), the diffusion rate (\$sigsq), the coefficients of the evolutionary potential (\$a, \$b, and \$c, depending on the shape fitted), and the value of the trait at

the root of the tree (\$root\_value).

InL The log-likelihood of the model.

k The number of parameters of the model.

aic The AIC of the model.

aicc The AICc of the model.

method The optimization method used to fit the model.

convergence Convergence code returned by optim. 0 indicates successful convergence. For

other values see the help of the optim function.

message Convergence message returned by optim. See the help of the optim function.

root\_density A vector giving the density of probability of the trait at the root of the tree. Each

element corresponds to one point in the discretized trait grid, from left (lower

bound) to right (upper bound).

ACE A list of tables, one for each node of the phylogeny. Each table has the position

of the points in the trait grid as its first column, and their associated probabilities

in the second column.

## Author(s)

F. C. Boucher

```
# Simulate data: tree + continuous trait
library(geiger)
tree=sim.bdtree(stop='taxa',n=10) # tree with few tips for quick tests
tree$edge.length=100*tree$edge.length/max(branching.times(tree)) # rescale the tree
# Simulate trait evolving on the tree with a linear trend towards small values
TRAIT= Sim_BBMV(tree,x0=0,V=seq(from=0,to=5,length.out=50),sigma=10,bounds=c(-5, 5))
# fit a model with a linear potential:
BBM_x=fit_BBMV(tree,TRAIT,Npts=10,method='Nelder-Mead',verbose=TRUE,V_shape='linear')
```

FormatTree\_bounds 7

## Description

Internal function used for likelihood calculation and simulation.

#### Usage

```
FormatTree_bounds(tree, trait, V, bounds)
```

## Arguments

tree	A phylogenetic tree in phylo format.
trait	A vector of traits at the tips of the tree
٧	A vector giving the evolutionary potential.
bounds	A vector of bounds of the trait interval.

#### Author(s)

F. C. Boucher

get.landscape.BBMV Pa
-----------------------

## **Description**

Plot the adaptive landscape estimated in a BBM+V model.

## Usage

```
get.landscape.BBMV(model, Npts = 50, main = "Macroevolutionary landscape", ylab = "-V", xlab = "Traget.multiple.landscapes.BBMV(models, Npts = 50, xlim = NULL, ylim = NULL, main = "Macroevolutionary")
```

## Arguments

model	A BBM+V model fit, as returned by fit_BBMV.
models	A list of BBM+V model fits, as returned by fit_BBMV.
landscape	If TRUE (the default), plots the adaptive landscape. If FALSE, plots the evolutionary potential instead.
Npts	The number of points used to discretize the trait interval for plotting.
main	A title for the plot.
ylim	The upper limit of the plotting region when multiple adaptive landscapes are plotted together.
xlim	The limits of thex-axis.
ylab	Label of the y-axis.
xlab	Label of the x-axis.

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#### Value

A plot of the adaptive landscape (or alternatively the evolutionary potential) across the trait interval.

#### Author(s)

F. C. Boucher

#### **Examples**

```
# Simulate data: tree + continuous trait
library(geiger)
tree=sim.bdtree(stop='taxa',n=10) # tree with few tips for quick tests
tree$edge.length=100*tree$edge.length/max(branching.times(tree)) # rescale the tree
# Simulate trait evolving on the tree with a linear trend towards small values
TRAIT= Sim_BBMV(tree,x0=0,V=seq(from=0,to=5,length.out=50),sigma=10,bounds=c(-5, 5))
# fit a model with a linear potential:
BBM_x=fit_BBMV(tree,TRAIT,Npts=10,method='Nelder-Mead',verbose=TRUE,V_shape='linear')
# plot the macroevolutionary landscape
get.landscape.BBMV(model=BBM_x,Npts=100)
```

LogLik\_bounds

Likelihood calculations for the BBM+V model

#### **Description**

Internal functions that calculate the log-likelihood of various versions of the BBM+V model, used in ML and MCMC estimation.

#### Usage

```
LogLik_bounds(tree_formatted, dCoeff, dMat, bounds)
LogLik_bounds_est(tree, trait, dCoeff, V, bounds)
LogLik_bounds_est_root(tree, trait, dCoeff, V, x0_pos, bounds)
bBM_loglik_0_flex_points(tree, trait, Npts)
bBM_loglik_bounds(tree_formatted, dMat, bounds)
bBM_loglik_linear_bounds(tree_formatted, Npts = 100, bounds)
bBM_loglik_quadra_bounds(tree_formatted, Npts = 100, bounds)
bBM_loglik_x_flex_points(tree, trait, Npts)
bBM_loglik_x2x_flex_points(tree, trait, Npts)
bBM_loglik_x4x2x_bounds(tree_formatted, Npts = 100, bounds)
bBM_loglik_x4x2x_flex_pts(tree, trait, Npts)
```

#### **Arguments**

tree\_formatted A formatted tree as returned by FormatTree\_bounds.

dCoeff The diffusion coefficient.

dMat The discretized diffusion matrix.

V A numeric vector giving the value of the evolutionary potential in each point of

the trait grid.

Talle and the second	A		41 1 1.	. C 41	trait interval.
bounds	A VECTOR	anvina	the notings	OT THE	trait interval
Doulius	A VCCIOI	ZIVIIIZ I	me bounds	or uic	trait mitti var.

 $x0_pos$  The value of the trait at the root of the tree.

tree A phylogenetic tree in phylo format.

trait A trait vector for tip taxa.

Npts The number of points used for discretizing the trait interval.

#### Author(s)

F. C. Boucher

```
\label{log_prior_7pars_root_bounds} Prior\ function.
```

## **Description**

Internal function that calculates the log prior, used in MCMC estimation of the BBM+V model.

## Usage

```
log_prior_7pars_root_bounds(type = c(rep("Normal", 4), rep("Uniform", 3)), shape = list(c(0, 10), c(0, 10), c(0, 10), c(0, 10), NA, 10, 10), pars, Npts_int, trait)
```

## Arguments

type A vector giving the type of prior for each parameter.

shape A list giving the shape of the prior for each parameter.

pars The parameter values at which the prior should be evaluated.

Npts\_int The number of points on the grid between min(trait) and max(trait).

trait A named vector of trait values for the tips of the tree.

## Author(s)

```
MH_MCMC_V_ax4bx2cx_root_bounds 
 MCMC estimation
```

#### **Description**

The function estimates the parameters of the BBM+V model using an MCMC chain with the Metropolis Hastings algorithm and a Gibbs sampler.

#### Usage

#### **Arguments**

٦	,	
	tree	A phylogenetic tree in phylo format.
	trait	A named vector of trait values for the tips of the tree. It should match tip labels in the phylogeny.
	Nsteps	The number of generations in the MCMC chain.
	record_every	The frequency used for sampling the MCMC chain.
	plot_every	The frequency at which the chain is plotted (if plot=TRUE).
	Npts_int	The number of points on the grid between min(trait) and max(trait).
	pars_init	A vector giving the initial parameters for starting the algorithm, which correspond to the following: $c(\log(sig^2/2),a,b,c,x0,Bmin,Bmax)$ .
	prob_update	A vector giving the relative frequencies of update of the different parameters of the model.
	verbose	If TRUE, will print some generations of the chain to the screen.
	plot	If TRUE, the chain is plotted from time to time.
	save_to	The path to the file where the chain is saved (can be useful in case the chain crashes).
	save_every	Sets how often the chain is saved.
	type_priors	A character vector specifying the type of priors used. Either 'Uniform' or 'Normal'. See Details.
	shape_priors	A list that gives the shape for each prior. See Details.
	proposal_type	The type of proposal function, only 'Uniform' is available (the default).
	proposal_sensit	·
		A numeric vector specifying the width of the uniform proposal for each parameter. See Details.
	prior.only	Default to FALSE for estimation of the posterior. If TRUE, the likelihood is not

evaluated: this is mostly useful for internal test of the Gibbs sampler.

#### **Details**

When specifying intial parameters yourself, be careful since x0 is actually the index of the point on the grid (between 1 and Npts\_int), not the actual root value. Also the fist parameter (log(sig^2/2)) is the diffusion coefficient, not the evolutionary rate (sig^2). Finally, be careful that the intial bounds you propose actually contain all trait values in you dataset.

Priors can be either 'Normal' (preferred) or 'Uniform' for log(sig^2/2), a, b and c. The only option for bounds and x0 is discrete uniform priors, specified by 'Uniform'.

Each element of the shape\_priors list should be a vector giving c(mean,sd) for normal priors and c(min,max) for continuous uniform priors. The shape is not specified for the root prior (it is set as 'NA' by default), since it is fixed to be discrete uniform on the grid. Values for the priors on the bounds (forced to be discrete uniform) are a single numeric value giving the maximum number of points that can be added on the trait grid outside of the observed trait interval, with a default value of 10 points.

Elements of the proposal\_sensitivity vector can be any positive number for continuously varying parameters: c(log(sig^2/2),a,b,c). Default values should often be a good start. Only integer numbers are possible for x0, Bmin, and Bmax and give how many steps at a time can be travelled on the trait grid when updating these parameters. It is recommended to keep it to 1, as it is by default.

#### Value

A matrix of numeric values giving values of all parameters, the likelihood, prior and posterior at each generation sampled in the MCMC chain (one row per sample taken). The matrix has the following columns:

step	The number of the generation sampled.
sigsq	The evolutionary rate.
а	The coefficient of the $x^4$ term of the evolutionary potential.
b	The coefficient of the $x^2$ term of the evolutionary potential.
С	The coefficient of the x term of the evolutionary potential.
root	The value of the trait at the root of the tree.
bmin	The value of the lower bound of the trait interval.
bmax	The value of the upper bound of the trait interval.
lnprior	The logarithm of the prior.
lnlik	The logarithm of the likelihood.

The logarithm of the (unnormalized) posterior.

Which parameter was updated in this generation.

Whether the proposed MCMC move was accepted (1) or not (0).

#### Author(s)

F. C. Boucher

quasi-lnpost

Acceptance

Par\_updated

```
Optim_bBM_0_flex_pts_multiple_starts

Maximum-likelihood estimation
```

#### **Description**

Set of internal functions that are used for ML optimization of various forms of the BBM+v model.

#### Usage

```
Optim_bBM_0_flex_pts_multiple_starts(tree, trait, Npts = 50, method = "Nelder-Mead", verbose = T)
Optim_bBM_x4x2x(tree, trait, Npts = 100, bounds = NULL, method = "L-BFGS-B", init.optim = NULL)
Optim_bBM_x4x2x_flex_pts_start(tree, trait, Npts = 50, method = "Nelder-Mead",
start.point=c(log(var(trait)/(2*max(branching.times(tree)))),0,0,0,
min(trait)-0.5*(max(trait) - min(trait)),
max(trait)+0.5*(max(trait) - min(trait))))
Optim_bBM_x4x2x_flex_pts_multiple_starts(tree, trait, Npts = 50,
method = "Nelder-Mead", verbose = T)
Optim_bBM_x2x_flex_pts_start(tree, trait, Npts = 50, method = "Nelder-Mead",
start.point = c(log(var(trait)/(2 * max(branching.times(tree)))), 0, 0,
min(trait)-0.5*(max(trait)-min(trait)), max(trait)+0.5*(max(trait)-min(trait))))
Optim_bBM_x2x_flex_pts_multiple_starts(tree, trait, Npts = 50,
method = "Nelder-Mead", verbose = T)
Optim_bBM_x_flex_pts_start(tree, trait, Npts = 50, method = "Nelder-Mead",
start.point = c(log(var(trait)/(2 * max(branching.times(tree)))), 0,
min(trait)-0.5*(max(trait)-min(trait)), max(trait)+0.5*(max(trait)-min(trait))))
Optim_bBM_x_flex_pts_multiple_starts(tree, trait, Npts = 50,
method = "Nelder-Mead", verbose = T)
Optim_bBM_quadratic(tree, trait, Npts = 100, bounds = NULL, method = "L-BFGS-B", init.optim = NULL
Optim_bBM_linear(tree, trait, Npts = 100, bounds = NULL, method = "L-BFGS-B", init.optim = NULL)
Optim_bBM_bounds_fixed_potential(tree, trait, V, bounds = NULL, init.optim = NULL)
Optim_bBM_0_flex_pts_start(tree, trait, Npts = 50, method = "Nelder-Mead",
start.point = c(log(var(trait)/(2 * max(branching.times(tree)))),
min(trait)-0.5*(max(trait)-min(trait)), max(trait)+0.5*(max(trait)-min(trait))))
```

#### **Arguments**

tree	A phylogenetic tree in phylo format
trait	A named vector of trait values for the tips of the tree. It should match tip labels in the phylogeny.
Npts	The number of points used in the discretization procedure.
method	The optimization routine used.
verbose	If TRUE, prints progress to the screen.
bounds	A vector giving the bounds of the trait interval.
init.optim	A parameter combination from which to start the optimization procedure, specified as a numeric vector. Default to NULL should work in most of the cases.
start.point	A parameter combination from which to start the optimization procedure, specified as a numeric vector.
٧	A numeric vector giving the potential.

prep\_mat\_exp 13

#### Author(s)

F. C. Boucher

<pre>prep_mat_exp</pre>	Matrix exponential.	

#### **Description**

Internal function used for likelihood calculation and simulation.

#### Usage

```
prep_mat_exp(dCoeff, dMat, bounds)
```

#### **Arguments**

dCoeff The diffusion coefficient.

dMat The diffusion matrix.

bounds A vector of bounds of the trait interval.

#### Author(s)

F. C. Boucher

#### **Description**

Internal function that proposes parameter updates used in MCMC estimation of the BBM+V model.

#### Usage

```
proposal_7pars_root_bounds(type = "Uniform", sensitivity, pars, trait, Npts_int)
```

## **Arguments**

type The type of proposal function, only 'Uniform' is available (the default).

sensitivity A numeric vector specifying the width of the uniform proposal for each param-

eter.

pars The current parameters in the MCMC chain.

trait A named vector of trait values for the tips of the tree. It should match tip labels

in the phylogeny.

Npts\_int The number of points on the grid between min(trait) and max(trait).

## Author(s)

14 Sim\_BBMV

Sim_BBMV	Simulation of the BBM+V process.	

## Description

The function simulates a continuous trait evolving according to the BBM+V process along the branches of a phylogenetic tree.

#### Usage

```
Sim_BBMV(tree, x0 = 0, V = rep(0, 100), sigma, bounds)
```

## Arguments

tree	A phylogenetic tree in phylo format.
x0	The value of the trait at the root of the tree.
V	A vector giving the values of the evolutionary potential at each point of the discretized trait grid. Default is a flat potential, i.e. bounded Brownian Motion.
sigma	The square root of the diffusion rate.
bounds	A vector giving the values of the bounds of the trait interval.

## Value

A numeric vector with values of the trait at the tips of the tree. Names correspond to tip labels in the tree.

#### Author(s)

F. C. Boucher

```
# Simulate data: tree + continuous trait
library(geiger)
tree=sim.bdtree(stop='taxa',n=20) # tree with few tips for quick tests
tree$edge.length=100*tree$edge.length/max(branching.times(tree)) # rescale the tree
# Simulate a trait evolving on the tree with a linear trend towards small values
TRAIT= Sim_BBMV(tree,x0=0,V=seq(from=0,to=5,length.out=50),sigma=10,bounds=c(-5, 5))
hist(TRAIT)
```

Uncertainty\_BBMV 15

Uncertainty_BBMV Measure uncertainty in paramater estimation	
--	--

#### **Description**

This function measures the uncertainty associated with ML paramater estimates, returning plots as well as confidence intervals

#### Usage

```
Uncertainty_BBMV(model, tree, trait, Npts = 50, effort_uncertainty = 100)
```

#### **Arguments**

model A BBM+V model fit, as returned by fit\_BBMV.

tree A phylogenetic tree, in phylo format.

trait A named vector of trait values for the tips of the tree. It should match tip labels in the phylogeny.

Npts The number of points used to discretize the trait interval.

effort\_uncertainty

The number of values of each peremeter that should be tried to essess uncer-

The number of values of each parameter that should be tried to assess uncertainty

#### Author(s)

F. C. Boucher

```
# Simulate data: tree + continuous trait
library(geiger)
tree=sim.bdtree(stop='taxa',n=10) # tree with few tips for quick tests
tree$edge.length=100*tree$edge.length/max(branching.times(tree)) # rescale the tree
# Simulate trait evolving on the tree with a linear trend towards small values
TRAIT= Sim_BBMV(tree,x0=0,V=seq(from=0,to=5,length.out=50),sigma=10,bounds=c(-5, 5))
# fit a model with a linear potential:
BBM_x=fit_BBMV(tree,TRAIT,Npts=10,method='Nelder-Mead',verbose=TRUE,V_shape='linear')
# Measure uncertainty around ML estimates of parameters
# Uncertainty_BBMV(BBM_x,tree,trait= TRAIT,Npts=10,effort_uncertainty= 20)
```

VectorPos\_bounds

VectorPos\_bounds

Discretization of a continuous trait value into a probability vector.

## Description

Internal function used for likelihood calculation and simulation.

## Usage

```
VectorPos_bounds(x, V, bounds)
```

## **Arguments**

x A numeric value of the trait.V The evolutionary potential used

bounds A vector with the values of both bounds.

## Author(s)

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