

# Package ‘meteorits’

July 19, 2019

**Type** Package

**Title** Mixtures-of-experts modeling for complex and non-normal distributions ('MEteorits')

**Version** 0.1.0

**Description** meteorits is an open source toolbox (available in R and in Matlab) containing several original and flexible mixtures-of-experts models to model, cluster and classify heterogeneous data in many complex situations where the data are distributed according to non-normal, possibly skewed distributions, and when they might be corrupted by atypical observations. The toolbox also contains sparse mixture-of-experts models for high-dimensional data.

**URL** <https://github.com/fchamroukhi/MEteorits>

**License** GPL (>= 3)

**Depends** R (>= 2.10)

**Imports** methods,  
stats,  
Rcpp

**Suggests** knitr,  
rmarkdown

**LinkingTo** Rcpp,  
RcppArmadillo

**Collate** meteorits-package.R  
RcppExports.R  
utils.R  
FData.R  
ParamSNMoE.R  
ParamStMoE.R  
ParamTMoE.R  
ParamNMoE.R  
StatSNMoE.R  
StatStMoE.R  
StatTMoE.R  
StatNMoE.R  
ModelSNMoE.R  
ModelStMoE.R  
ModelTMoE.R  
ModelNMoE.R  
emSNMoE.R  
emStMoE.R

```
emTMoE.R
emNMoE.R
```

**VignetteBuilder** knitr

**Encoding** UTF-8

**LazyData** true

**Roxygen** list(markdown = TRUE)

**RoxygenNote** 6.1.1

## R topics documented:

emNMoE . . . . .	2
emSNMoE . . . . .	3
emStMoE . . . . .	4
emTMoE . . . . .	5
FData-class . . . . .	6
ModelNMoE-class . . . . .	7
ModelSNMoE-class . . . . .	7
ModelStMoE-class . . . . .	7
ModelTMoE-class . . . . .	8
ParamNMoE-class . . . . .	8
ParamSNMoE-class . . . . .	9
ParamStMoE-class . . . . .	9
ParamTMoE-class . . . . .	10
StatNMoE-class . . . . .	10
StatSNMoE-class . . . . .	12
StatStMoE-class . . . . .	13
StatTMoE-class . . . . .	14
<b>Index</b>	<b>16</b>

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emNMoE

*emNMoE implements the EM algorithm to fit a NMoE model.*

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## Description

emNMoE implements the maximum-likelihood parameter estimation of a NMoE model by the Expectation-Maximization (EM) algorithm.

## Usage

```
emNMoE(X, Y, K, p = 3, q = 1, n_tries = 1, max_iter = 1500,
        threshold = 1e-06, verbose = FALSE, verbose_IRLS = FALSE)
```

**Arguments**

X	Numeric vector of length $n$ representing the covariates/inputs $x_1, \dots, x_m$ .
Y	Numeric vector of length $n$ representing the observed response/output $y_1, \dots, y_m$ .
K	The number of expert components.
p	The order of the polynomial regression for the expert regressors network.
q	The dimension of the logistic regression for the gating network. For the purpose of segmentation, it must be set to 1.
n_tries	Number of times EM algorithm will be launched with different initializations. The solution providing the highest log-likelihood will be returned.
max_iter	The maximum number of iterations for the EM algorithm.
threshold	A numeric value specifying the threshold for the relative difference of log-likelihood between two steps of the EM as stopping criteria.
verbose	A logical value indicating whether values of the log-likelihood should be printed during EM iterations.
verbose_IRLS	A logical value indicating whether values of the criterion optimized by IRLS should be printed at each step of the EM algorithm.

**Details**

emNMoe function implements the EM algorithm for the NMoe model. This functions starts with an initialization of the parameters done by the method `initParam` of the class [ParamNMoe](#), then it alternates between a E-Step (method of the class [StatNMoe](#)) and a M-Step (method of the class [ParamNMoe](#)) until convergence (until the absolute difference of log-likelihood between two steps of the EM algorithm is less than the `threshold` parameter).

**Value**

The EM algorithm returns an object of class [ModelNMoe](#).

**See Also**

[ModelNMoe](#), [ParamNMoe](#), [StatNMoe](#)

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emSNMoE

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*emSNMoE implements the ECM algorithm to fit a SNMoE model.*


---

**Description**

emSNMoE implements the maximum-likelihood parameter estimation of a SNMoE model by the Expectation Conditional Maximization (ECM) algorithm.

**Usage**

```
emSNMoE(X, Y, K, p = 3, q = 1, n_tries = 1, max_iter = 1500,
        threshold = 1e-06, verbose = FALSE, verbose_IRLS = FALSE)
```

### Arguments

X	Numeric vector of length $n$ representing the covariates/inputs $x_1, \dots, x_m$ .
Y	Numeric vector of length $n$ representing the observed response/output $y_1, \dots, y_m$ .
K	The number of expert components.
p	The order of the polynomial regression for the expert regressors network.
q	The dimension of the logistic regression for the gating network. For the purpose of segmentation, it must be set to 1.
n_tries	Number of times ECM algorithm will be launched with different initializations. The solution providing the highest log-likelihood will be returned.
max_iter	The maximum number of iterations for the ECM algorithm.
threshold	A numeric value specifying the threshold for the relative difference of log-likelihood between two steps of the ECM as stopping criteria.
verbose	A logical value indicating whether values of the log-likelihood should be printed during ECM iterations.
verbose_IRLS	A logical value indicating whether values of the criterion optimized by IRLS should be printed at each step of the ECM algorithm.

### Details

emSNMoE function implements the ECM algorithm for the SNMoE model. This function starts with an initialization of the parameters done by the method `initParam` of the class [ParamSNMoE](#), then it alternates between a E-Step (method of the class [StatSNMoE](#)) and a CM-Step (method of the class [ParamSNMoE](#)) until convergence (until the absolute difference of log-likelihood between two steps of the ECM algorithm is less than the threshold parameter).

### Value

The ECM algorithm returns an object of class [ModelSNMoE](#).

### See Also

[ModelSNMoE](#), [ParamSNMoE](#), [StatSNMoE](#)

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emStMoE

---

*emStMoE implements the ECM algorithm to fit a StMoE model.*


---

### Description

emStMoE implements the maximum-likelihood parameter estimation of a StMoE model by the Expectation Conditional Maximization (ECM) algorithm.

### Usage

```
emStMoE(X, Y, K, p = 3, q = 1, n_tries = 1, max_iter = 1500,
        threshold = 1e-06, verbose = FALSE, verbose_IRLS = FALSE)
```

**Arguments**

X	Numeric vector of length $n$ representing the covariates/inputs $x_1, \dots, x_m$ .
Y	Numeric vector of length $n$ representing the observed response/output $y_1, \dots, y_m$ .
K	The number of expert components.
p	The order of the polynomial regression for the expert regressors network.
q	The dimension of the logistic regression for the gating network. For the purpose of segmentation, it must be set to 1.
n_tries	Number of times ECM algorithm will be launched with different initializations. The solution providing the highest log-likelihood will be returned.
max_iter	The maximum number of iterations for the ECM algorithm.
threshold	A numeric value specifying the threshold for the relative difference of log-likelihood between two steps of the ECM as stopping criteria.
verbose	A logical value indicating whether values of the log-likelihood should be printed during ECM iterations.
verbose_IRLS	A logical value indicating whether values of the criterion optimized by IRLS should be printed at each step of the ECM algorithm.

**Details**

emStMoE function implements the ECM algorithm for the StMoE model. This function starts with an initialization of the parameters done by the method `initParam` of the class [ParamStMoE](#), then it alternates between a E-Step (method of the class [StatStMoE](#)) and a CM-Step (method of the class [ParamStMoE](#)) until convergence (until the absolute difference of log-likelihood between two steps of the ECM algorithm is less than the `threshold` parameter).

**Value**

The ECM algorithm returns an object of class [ModelStMoE](#).

**See Also**

[ModelStMoE](#), [ParamStMoE](#), [StatStMoE](#)

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emTMoE

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*emTMoE implements the ECM algorithm to fit a tMoE model.*


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**Description**

emTMoE implements the maximum-likelihood parameter estimation of a tMoE model by the Expectation Conditional Maximization (ECM) algorithm.

**Usage**

```
emTMoE(X, Y, K, p = 3, q = 1, n_tries = 1, max_iter = 1500,
        threshold = 1e-06, verbose = FALSE, verbose_IRLS = FALSE)
```

**Arguments**

X	Numeric vector of length $n$ representing the covariates/inputs $x_1, \dots, x_m$ .
Y	Numeric vector of length $n$ representing the observed response/output $y_1, \dots, y_m$ .
K	The number of expert components.
p	The order of the polynomial regression for the expert regressors network.
q	The dimension of the logistic regression for the gating network. For the purpose of segmentation, it must be set to 1.
n_tries	Number of times ECM algorithm will be launched with different initializations. The solution providing the highest log-likelihood will be returned.
max_iter	The maximum number of iterations for the ECM algorithm.
threshold	A numeric value specifying the threshold for the relative difference of log-likelihood between two steps of the ECM as stopping criteria.
verbose	A logical value indicating whether values of the log-likelihood should be printed during ECM iterations.
verbose_IRLS	A logical value indicating whether values of the criterion optimized by IRLS should be printed at each step of the ECM algorithm.

**Details**

emTMoE function implements the ECM algorithm for the tMoE model. This function starts with an initialization of the parameters done by the method `initParam` of the class [ParamTMoE](#), then it alternates between a E-Step (method of the class [StatTMoE](#)) and a CM-Step (method of the class [ParamTMoE](#)) until convergence (until the absolute difference of log-likelihood between two steps of the ECM algorithm is less than the `threshold` parameter).

**Value**

The ECM algorithm returns an object of class [ModelTMoE](#).

**See Also**

[ModelTMoE](#), [ParamTMoE](#), [StatTMoE](#)

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FData-class

*A Reference Class to represent a functional data set.*


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**Description**

FData is a reference class which represents general independent and identically distributed (i.i.d.) functional objects. The data can be ordered by time (functional time series). In the last case, the field X represents the time.

**Fields**

- X Numeric vector of length  $m$ .
- Y Matrix of size  $(n, m)$  representing  $n$  functions of X observed at points  $1, \dots, m$ .

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ModelNMoE-class	<i>A Reference Class which represents a fitted NMoE model.</i>
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**Description**

ModelNMoE represents a [NMoE](#) model for which parameters have been estimated.

**Fields**

param A [ParamNMoE](#) object. It contains the estimated values of the parameters.

stat A [StatNMoE](#) object. It contains all the statistics associated to the NMoE model.

**See Also**

[ParamNMoE](#), [StatNMoE](#)

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ModelSNMoE-class	<i>A Reference Class which represents a fitted SNMoE model.</i>
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**Description**

ModelSNMoE represents a [SNMoE](#) model for which parameters have been estimated.

**Fields**

param A [ParamSNMoE](#) object. It contains the estimated values of the parameters.

stat A [StatSNMoE](#) object. It contains all the statistics associated to the SNMoE model.

**See Also**

[ParamSNMoE](#), [StatSNMoE](#)

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ModelStMoE-class	<i>A Reference Class which represents a fitted StMoE model.</i>
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**Description**

ModelStMoE represents a [StMoE](#) model for which parameters have been estimated.

**Fields**

param A [ParamStMoE](#) object. It contains the estimated values of the parameters.

stat A [StatStMoE](#) object. It contains all the statistics associated to the StMoE model.

**See Also**

[ParamStMoE](#), [StatStMoE](#)

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ModelTMoE-class

*A Reference Class which represents a fitted TMoE model.*


---

### Description

ModelTMoE represents a [TMoE](#) model for which parameters have been estimated.

### Fields

param A [ParamTMoE](#) object. It contains the estimated values of the parameters.

stat A [StatTMoE](#) object. It contains all the statistics associated to the TMoE model.

### See Also

[ParamTMoE](#), [StatTMoE](#)

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ParamNMoE-class

*A Reference Class which contains parameters of a NMoE model.*


---

### Description

ParamNMoE contains all the parameters of a NMoE model.

### Fields

fData [FData](#) object representing the sample.

K The number of mixture components.

p The order of the polynomial regression.

q The dimension of the logistic regression. For the purpose of segmentation, it must be set to 1.

nu degree of freedom

alpha is the parameter vector of the logistic model with  $\alpha_K$  being the null vector.

beta is the vector of regression coefficients of component k, the updates for each of the expert component parameters consist in analytically solving a weighted Gaussian linear regression problem.

sigma The variances for the  $K$  mixture components.

delta the skewness parameter lambda (by equivalence delta)

### See Also

[FData](#)



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ParamSNMoE-class	<i>A Reference Class which contains parameters of a SNMoE model.</i>
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**Description**

ParamSNMoE contains all the parameters of a SNMoE model.

**Fields**

fData [FData](#) object representing the sample.  
K The number of mixture components.  
p The order of the polynomial regression.  
q The dimension of the logistic regression. For the purpose of segmentation, it must be set to 1.  
nu degree of freedom  
alpha is the parameter vector of the logistic model with  $\alpha_K$  being the null vector.  
beta is the vector of regression coefficients of component k, the updates for each of the expert component parameters consist in analytically solving a weighted Gaussian linear regression problem.  
sigma The variances for the  $K$  mixture component.  
lambda skewness parameter  
delta the skewness parameter lambda (by equivalence delta)

**See Also**

[FData](#)

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ParamStMoE-class	<i>A Reference Class which contains parameters of a MRHLP model.</i>
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**Description**

ParamMRHLP contains all the parameters of a MRHLP model.

**Fields**

fData [FData](#) object representing the sample.  
K The number of mixture components.  
p The order of the polynomial regression.  
q The dimension of the logistic regression. For the purpose of segmentation, it must be set to 1.  
nu degree of freedom  
alpha is the parameter vector of the logistic model with  $\alpha_K$  being the null vector.  
beta is the vector of regression coefficients of component k, the updates for each of the expert component parameters consist in analytically solving a weighted Gaussian linear regression problem.  
sigma The variances for the  $K$  mixture component.  
lambda skewness parameter  
delta the skewness parameter lambda (by equivalence delta)  
nuk degrees of freedom

**Methods**

`initParam(try_EM, segmental = FALSE)` Method to initialize parameters  $\alpha$ ,  $\beta$  and  $\sigma$ .  
`MStep(statStMoE, verbose_IRLS)` Method used in the EM algorithm to learn the parameters of the StMoE model based on statistics provided by `statStMoE`.

**See Also**

[FData](#)

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ParamTMoE-class	<i>A Reference Class which contains parameters of a TMoE model.</i>
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**Description**

ParamTMoE contains all the parameters of a TMoE model.

**Fields**

`fData` [FData](#) object representing the sample.  
`K` The number of mixture components.  
`p` The order of the polynomial regression.  
`q` The dimension of the logistic regression. For the purpose of segmentation, it must be set to 1.  
`nu` degree of freedom  
`alpha` is the parameter vector of the logistic model with  $\alpha_K$  being the null vector.  
`beta` is the vector of regression coefficients of component  $k$ , the updates for each of the expert component parameters consist in analytically solving a weighted Gaussian linear regression problem.  
`sigma` The variances for the  $K$  mixture component.  
`delta` the skewness parameter  $\lambda$  (by equivalence  $\delta$ )

**See Also**

[FData](#)

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StatNMoE-class	<i>A Reference Class which contains statistics of a NMoE model.</i>
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**Description**

StatNoE contains all the parameters of a [NMoE](#) model.

## Fields

- piik** Matrix of size  $(n, K)$  representing the probabilities  $P(z_i = k; W) = P(z_{ik} = 1; W)$  of the latent variable  $z_i$ ,  $i = 1, \dots, m$ .
- z\_ik** Hard segmentation logical matrix of dimension  $(n, K)$  obtained by the Maximum a posteriori (MAP) rule:  $z_{ik} = 1$  if  $z_{ik} = \arg \max_k P(z_i = k|Y, W, \beta)$ ; 0 otherwise,  $k = 1, \dots, K$ .
- klas** Column matrix of the labels issued from **z\_ik**. Its elements are  $klas(i) = k$ ,  $k = 1, \dots, K$ .
- Wik** Matrix of dimension  $(nm, K)$ .
- Ey\_k** Matrix of dimension  $(n, K)$ .
- Ey** Column matrix of dimension  $n$ .
- Var\_yk** Column matrix of dimension  $K$ .
- Vary** Column matrix of dimension  $n$ .
- log\_lik** Numeric. Log-likelihood of the StMoE model.
- com\_loglik** Numeric. Complete log-likelihood of the StMoE model.
- stored\_loglik** Numeric vector. Stored values of the log-likelihood at each EM iteration.
- BIC** Numeric. Value of the BIC (Bayesian Information Criterion) criterion. The formula is  $BIC = \log\_lik - nu \times \log(n)/2$  with  $nu$  the degree of freedom of the StMoE model.
- ICL** Numeric. Value of the ICL (Integrated Completed Likelihood) criterion. The formula is  $ICL = com\_loglik - nu \times \log(n)/2$  with  $nu$  the degree of freedom of the StMoE model.
- AIC** Numeric. Value of the AIC (Akaike Information Criterion) criterion. The formula is  $AIC = \log\_lik - nu$ .
- log\_piik\_fik** Matrix of size  $(n, K)$  giving the values of the logarithm of the joint probability  $P(Y_i, z_i = k)$ ,  $i = 1, \dots, n$ .
- log\_sum\_piik\_fik** Column matrix of size  $n$  giving the values of  $\sum_{k=1}^K \log P(Y_i, z_i = k)$ ,  $i = 1, \dots, n$ .
- tik** Matrix of size  $(n, K)$  giving the posterior probability that  $Y_i$  originates from the  $k$ -th regression model  $P(z_i = k|Y, W, \beta)$ .

## Methods

**MAP()** calcule une partition d'un echantillon par la regle du Maximum A Posteriori ?? partir des probabilites a posteriori  
 Entrees : post\_probab, Matrice de dimensions [n x K] des probabibiltes a posteriori (matrice de la partition floue)  
 n : taille de l'echantillon  
 K : nombres de classes  
 $klas(i) = \arg \max (post\_probab(i,k))$ , for all  $i=1, \dots, n$   
 $1 \leq k \leq K = \arg \max p(z_i=k|x_i; \theta) p(x_i|z_i=k; \theta) / \sum_{l=1}^K p(z_i=l; \theta) p(x_i|z_i=l; \theta)$   
 $1 \leq k \leq K$   
 Sorties : classes : vecteur collones contenant les classe (1:K)  
 Z : Matrice de dimension [nxK] de la partition dure : ses elements sont zik, avec  $z_{ik}=1$  si  $x_i$  appartient ?? la classe  $k$  (au sens du MAP) et zero sinon.

## See Also

[ParamNMoE](#), [FData](#)

StatSNMoE-class

*A Reference Class which contains statistics of a SNMoE model.***Description**

StatMRHLP contains all the parameters of a [SNMoE](#) model.

**Fields**

**piik** Matrix of size  $(n, K)$  representing the probabilities  $P(z_i = k; W) = P(z_{ik} = 1; W)$  of the latent variable  $z_i$ ,  $i = 1, \dots, m$ .

**z\_ik** Hard segmentation logical matrix of dimension  $(n, K)$  obtained by the Maximum a posteriori (MAP) rule:  $z_{ik} = 1$  if  $z_{ik} = \arg \max_k P(z_i = k | Y, W, \beta)$ ; 0 otherwise,  $k = 1, \dots, K$ .

**klas** Column matrix of the labels issued from **z\_ik**. Its elements are  $klas(i) = k$ ,  $k = 1, \dots, K$ .

**Ey\_k** Matrix of dimension  $(n, K)$ .

**Ey** Column matrix of dimension  $n$ .

**Var\_yk** Column matrix of dimension  $K$ .

**Vary** Column matrix of dimension  $n$ .

**log\_lik** Numeric. Log-likelihood of the SNMoE model.

**com\_loglik** Numeric. Complete log-likelihood of the SNMoE model.

**stored\_loglik** Numeric vector. Stored values of the log-likelihood at each EM iteration.

**BIC** Numeric. Value of the BIC (Bayesian Information Criterion) criterion. The formula is  $BIC = \log\_lik - nu \times \log(n)/2$  with  $nu$  the degree of freedom of the SNMoE model.

**ICL** Numeric. Value of the ICL (Integrated Completed Likelihood) criterion. The formula is  $ICL = com\_loglik - nu \times \log(n)/2$  with  $nu$  the degree of freedom of the SNMoE model.

**AIC** Numeric. Value of the AIC (Akaike Information Criterion) criterion. The formula is  $AIC = \log\_lik - nu$ .

**log\_piik\_fik** Matrix of size  $(n, K)$  giving the values of the logarithm of the joint probability  $P(Y_i, z_i = k)$ ,  $i = 1, \dots, n$ .

**log\_sum\_piik\_fik** Column matrix of size  $n$  giving the values of  $\sum_{k=1}^K \log P(Y_i, z_i = k)$ ,  $i = 1, \dots, n$ .

**tik** Matrix of size  $(n, K)$  giving the posterior probability that  $Y_i$  originates from the  $k$ -th regression model  $P(z_i = k | Y, W, \beta)$ .

**E1ik** To define.

**E2ik** To define.

**Methods**

**EStep(paramSNMoE)** Method used in the EM algorithm to update statistics based on parameters provided by paramSNMoE (prior and posterior probabilities).

**MAP()** calcule une partition d'un echantillon par la regle du Maximum A Posteriori ?? partir des probabilites a posteriori  
 Entrees : post\_probab , Matrice de dimensions [n x K] des probabilites a posteriori (matrice de la partition floue)  
 n : taille de l'echantillon  
 K : nombres de classes  
 klas(i) = arg max (post\_probab(i,k)) , for all i=1,...,n  
 $1 \leq k \leq K = \arg \max p(z_i = k | x_i; \theta)$   
 $1 \leq k \leq K = \arg \max p(z_i = k; \theta) p(x_i | z_i = k; \theta) / \sum_{l=1}^K p(z_i = l; \theta) p(x_i | z_i = l; \theta)$   
 Sorties : classes : vecteur collones contenant les classe (1:K)  
 Z : Matrice de dimension [nxK] de la partition dure : ses elements sont zik, avec zik=1 si xi appartient ?? la classe k (au sens du MAP) et zero sinon.

**See Also**

[ParamSNMoE](#), [FData](#)

---

StatStMoE-class

*A Reference Class which contains statistics of a StMoE model.*


---

**Description**

StatMRHLP contains all the parameters of a [StMoE](#) model.

**Fields**

**piik** Matrix of size  $(n, K)$  representing the probabilities  $P(z_i = k; W) = P(z_{ik} = 1; W)$  of the latent variable  $z_i$ ,  $i = 1, \dots, m$ .

**z\_ik** Hard segmentation logical matrix of dimension  $(n, K)$  obtained by the Maximum a posteriori (MAP) rule:  $z_{ik} = 1$  if  $z_{ik} = \arg \max_k P(z_i = k|Y, W, \beta)$ ; 0 otherwise,  $k = 1, \dots, K$ .

**klas** Column matrix of the labels issued from **z\_ik**. Its elements are  $klas(i) = k$ ,  $k = 1, \dots, K$ .

**Ey\_k** Matrix of dimension  $(n, K)$ .

**Ey** Column matrix of dimension  $n$ .

**Var\_yk** Column matrix of dimension  $K$ .

**Var\_y** Column matrix of dimension  $n$ .

**log\_lik** Numeric. Log-likelihood of the StMoE model.

**com\_loglik** Numeric. Complete log-likelihood of the StMoE model.

**stored\_loglik** Numeric vector. Stored values of the log-likelihood at each EM iteration.

**BIC** Numeric. Value of the BIC (Bayesian Information Criterion) criterion. The formula is  $BIC = \log\_lik - nu \times \log(n)/2$  with  $nu$  the degree of freedom of the StMoE model.

**ICL** Numeric. Value of the ICL (Integrated Completed Likelihood) criterion. The formula is  $ICL = com\_loglik - nu \times \log(n)/2$  with  $nu$  the degree of freedom of the StMoE model.

**AIC** Numeric. Value of the AIC (Akaike Information Criterion) criterion. The formula is  $AIC = \log\_lik - nu$ .

**log\_piik\_fik** Matrix of size  $(n, K)$  giving the values of the logarithm of the joint probability  $P(Y_i, z_i = k)$ ,  $i = 1, \dots, n$ .

**log\_sum\_piik\_fik** Column matrix of size  $n$  giving the values of  $\sum_{k=1}^K \log P(Y_i, z_i = k)$ ,  $i = 1, \dots, n$ .

**tik** Matrix of size  $(n, K)$  giving the posterior probability that  $Y_i$  originates from the  $k$ -th regression model  $P(z_i = k|Y, W, \beta)$ .

**wik** To define.

**dik** To define.

**stme\_pdf** skew-t mixture of experts density

**E1ik** To define.

**E2ik** To define.

**E3ik** To define.

## Methods

EStep(paramStMoE) Method used in the EM algorithm to update statistics based on parameters provided by paramStMoE (prior and posterior probabilities).

MAP() calcule une partition d'un echantillon par la regle du Maximum A Posteriori ?? partir des probabilites a posteriori Entrees : post\_probab, Matrice de dimensions [n x K] des probabilties a posteriori (matrice de la partition floue) n : taille de l'echantillon K : nombres de classes  $klas(i) = \arg \max_k (post\_probab(i,k))$ , for all  $i=1,...,n$   $1 \leq k \leq K = \arg \max_k p(z_i=k|x_i;\theta)$   $1 \leq k \leq K = \arg \max_k p(z_i=k;\theta) p(x_i|z_i=k;\theta) / \sum_{l=1}^K p(z_i=l;\theta) p(x_i|z_i=l;\theta)$   $1 \leq k \leq K$  Sorties : classes : vecteur collones contenant les classe (1:K) Z : Matrice de dimension [nxK] de la partition dure : ses elements sont  $z_{ik}$ , avec  $z_{ik}=1$  si  $x_i$  appartient a la classe  $k$  (au sens du MAP) et zero sinon.

## See Also

[ParamStMoE](#), [FData](#)

---

StatTMoE-class

*A Reference Class which contains statistics of a TMoE model.*

---

## Description

StatTMoE contains all the parameters of a [TMoE](#) model.

## Fields

piik Matrix of size  $(n, K)$  representing the probabilities  $P(z_i = k; W) = P(z_{ik} = 1; W)$  of the latent variable  $z_i$ ,  $i = 1, \dots, m$ .

z\_ik Hard segmentation logical matrix of dimension  $(n, K)$  obtained by the Maximum a posteriori (MAP) rule:  $z_{ik} = 1$  if  $z_{ik} = \arg \max_k P(z_i = k|Y, W, \beta)$ ; 0 otherwise,  $k = 1, \dots, K$ .

klas Column matrix of the labels issued from z\_ik. Its elements are  $klas(i) = k$ ,  $k = 1, \dots, K$ .

Wik Matrix of dimension  $(nm, K)$ .

Ey\_k Matrix of dimension  $(n, K)$ .

Ey Column matrix of dimension  $n$ .

Var\_yk Column matrix of dimension  $K$ .

Vary Column matrix of dimension  $n$ .

log\_lik Numeric. Log-likelihood of the StMoE model.

com\_loglik Numeric. Complete log-likelihood of the StMoE model.

stored\_loglik Numeric vector. Stored values of the log-likelihood at each EM iteration.

BIC Numeric. Value of the BIC (Bayesian Information Criterion) criterion. The formula is  $BIC = log\_lik - nu \times \log(n)/2$  with  $nu$  the degree of freedom of the StMoE model.

ICL Numeric. Value of the ICL (Integrated Completed Likelihood) criterion. The formula is  $ICL = com\_loglik - nu \times \log(n)/2$  with  $nu$  the degree of freedom of the StMoE model.

AIC Numeric. Value of the AIC (Akaike Information Criterion) criterion. The formula is  $AIC = log\_lik - nu$ .

log\_piik\_fik Matrix of size  $(n, K)$  giving the values of the logarithm of the joint probability  $P(Y_i, z_i = k)$ ,  $i = 1, \dots, n$ .

`log_sum_piik_fik` Column matrix of size  $n$  giving the values of  $\sum_{k=1}^K \log P(Y_i, z_i = k)$ ,  $i = 1, \dots, n$ .

`tik` Matrix of size  $(n, K)$  giving the posterior probability that  $Y_i$  originates from the  $k$ -th regression model  $P(z_i = k | Y, W, \beta)$ .

## Methods

`MAP()` calcule une partition d'un echantillon par la regle du Maximum A Posteriori ?? partir des probabilites a posteriori  
 Entrees : `post_probas` , Matrice de dimensions  $[n \times K]$  des probabilites a posteriori (matrice de la partition floue)  
 $n$  : taille de l'echantillon  
 $K$  : nombres de classes  
 $\text{klas}(i) = \arg \max_k (\text{post\_probas}(i,k))$  , for all  $i=1, \dots, n$   
 $1 \leq k \leq K = \arg \max_k p(z_i=k; \theta) p(x_i | z_i=k; \theta) / \sum_{l=1}^K p(z_i=l; \theta) p(x_i | z_i=l; \theta)$   
 $1 \leq k \leq K$   
 Sorties : `classes` : vecteur collones contenant les classe (1:K)  
`Z` : Matrice de dimension  $[n \times K]$  de la partition dure : ses elements sont  $z_{ik}$ , avec  $z_{ik}=1$  si  $x_i$  appartient ?? la classe  $k$  (au sens du MAP) et zero sinon.

## See Also

[ParamStMoE](#), [FData](#)

# Index

emNMoE, [2](#)  
emSNMoE, [3](#)  
emStMoE, [4](#)  
emTMoE, [5](#)  
  
FData, [8–11](#), [13–15](#)  
FData (FData-class), [6](#)  
FData-class, [6](#)  
  
ModelNMoE, [3](#)  
ModelNMoE (ModelNMoE-class), [7](#)  
ModelNMoE-class, [7](#)  
ModelSNMoE, [4](#)  
ModelSNMoE (ModelSNMoE-class), [7](#)  
ModelSNMoE-class, [7](#)  
ModelStMoE, [5](#)  
ModelStMoE (ModelStMoE-class), [7](#)  
ModelStMoE-class, [7](#)  
ModelTMoE, [6](#)  
ModelTMoE (ModelTMoE-class), [8](#)  
ModelTMoE-class, [8](#)  
  
NMoE, [7](#), [10](#)  
  
ParamNMoE, [3](#), [7](#), [11](#)  
ParamNMoE (ParamNMoE-class), [8](#)  
ParamNMoE-class, [8](#)  
ParamSNMoE, [4](#), [7](#), [13](#)  
ParamSNMoE (ParamSNMoE-class), [9](#)  
ParamSNMoE-class, [9](#)  
ParamStMoE, [5](#), [7](#), [14](#), [15](#)  
ParamStMoE (ParamStMoE-class), [9](#)  
ParamStMoE-class, [9](#)  
ParamTMoE, [6](#), [8](#)  
ParamTMoE (ParamTMoE-class), [10](#)  
ParamTMoE-class, [10](#)  
  
SNMoE, [7](#), [12](#)  
StatNMoE, [3](#), [7](#)  
StatNMoE (StatNMoE-class), [10](#)  
StatNMoE-class, [10](#)  
StatSNMoE, [4](#), [7](#)  
StatSNMoE (StatSNMoE-class), [12](#)  
StatSNMoE-class, [12](#)  
StatStMoE, [5](#), [7](#)  
StatStMoE (StatStMoE-class), [13](#)  
StatStMoE-class, [13](#)  
StatTMoE, [6](#), [8](#)  
StatTMoE (StatTMoE-class), [14](#)  
StatTMoE-class, [14](#)  
StMoE, [7](#), [13](#)  
  
TMoE, [8](#), [14](#)