

You are comparing two linear models, m_1 and m_2 , and are told that the first model has an R^2 of 0.815, and the second model has an R^2 of 0.765. Which of the two models do you prefer?

- ☒ a. There is insufficient information to prefer either model

$\{R^2\}$ alone is not enough to prefer one model over another, for example, if you find out that the first model has 10,000 covariates, whilst the other has only 6 covariates, then the $\{R^2\}$ differential does not seem very impressive. Recall that $\{R^2\}$ tends to increase as new variables are included in the model, even if those variables are useless.

- ☐ b. m_2
- ☐ c. m_1
- ☐ d. Both models are equivalent

Which of the following is **not** an assumption of the univariate linear regression model with feature vector x , target output y , and predictions \hat{y} ?

I. y is normally distributed for any fixed value of x .

II. x has a linear relationship with y

III. The variance of the residual $e = y - \hat{y}$ is constant for any value x

IV. All observations (x_i, y_i) are independent of each other

- ☐ a. I
- ☒ b. II
- ☐ c. III
- ☐ d. IV

Compute the derivative of $f(x) = x^3 \ln(x) + \frac{3}{x^3}$.

- ☐ a. $f'(x) = 3x^2 \ln(x) + x^2 - \frac{3}{x^4}$
- ☐ b. $f'(x) = 3x^2 - \frac{9}{x^4}$
- ☒ c. $f'(x) = 3x^2 \ln(x) + x^2 - \frac{9}{x^4}$
- ☐ d. $f'(x) = 6x^2 \ln(x) + x^2 - \frac{9}{x^4}$

Compute the derivative of $f(x) = (x - 4)(2x + x^2)^2$

- ☐ a. $f'(x) = 5x^4 - 18x^2 - 32x$
- ☐ b. $f'(x) = x^4 - 36x^2 - 16x$
- ☐ c. $f'(x) = x^4 - 36x^2 - 32x$
- ☒ d. $f'(x) = 5x^4 - 36x^2 - 32x$

Consider the following 3 datasets:

Dataset 1	
x	y
1	2
2	3
3	6
4	8
5	11

Dataset 2	
x	y
1	3
2	3
3	3
4	3
5	3

Dataset 3	
x	y
1	3
2	2
3	2
4	1
5	-4

Which of the following most accurately describes the correlations r_1, r_2, r_3 between x and y across datasets 1, 2, 3 respectively?

- ☐ a. $r_1 > 0, r_2 = 0, r_3 > 0$
- ☐ b. $r_1 > 0, r_2 = 0, r_3$
- ☒ c. $r_1 > 0, r_2 = \text{undefined}, r_3$
- ☐ d. $r_1 > 0, r_2 = \text{undefined}, r_3 > 0$

Compute the derivative of $f(x) = \frac{\ln x + 1}{x^2}$

- ☐ a. $f'(x) = -\frac{1}{2x}$
- ☒ b. $f'(x) = -\frac{2 \ln(x) + 1}{x^3}$
- ☐ c. $f'(x) = -\frac{2 \ln(x) + 1}{x^4}$
- ☐ d. $f'(x) = \frac{1}{2x}$

A new COVID19 home-testing kit is developed and administered to 100 individuals who are known to have the virus. Out of 100, the test returns 72 positive results.

- ☐ a. The test has precision of 72%
- ☐ b. The test has recall of 28%
- ☐ c. The test has recall of 28%
- ☒ d. The test has recall of 72%

Consider the following data: $X = ((1, 1), (3, 1), (1, -1), (2, -2))$ with corresponding labels $y = (1, 1, -1, -1)$. The basic linear classifier is described by the equation $\langle x, w \rangle = t$ where:

- ☐ a. $w = (5/2, 1/2)$ and $t = 1/8$
- ☐ b. $w = (5/2, -1/2)$ and $t = -1/4$
- ☒ c. $w = (1/2, 5/2)$ and $t = 1/4$
- ☐ d. $w = (-5/2, 1/2)$ and $t = -1/4$

Which of the following is **not** an assumption of the univariate linear regression model with feature vector x , target output y , and predictions \hat{y} ?

- I. y is normally distributed for any fixed value of x .
- II. x has a linear relationship with y
- III. The variance of the residual $e = y - \hat{y}$ is constant for any value x
- IV. All observations (x_i, y_i) are independent of each other

- ☐ a. I
- ☒ b. II
- ☐ c. III
- ☐ d. IV

Assume we have two classes A and B , and we wish to classify a new document d . We have the following training data:

document	class	cosine distance to d
1	A	1
2	B	0.95
3	B	0.94
4	A	0.45
5	A	0.4
6	B	0.39

Where we are using the cosine distance as a measure of distance (the higher the value, the closer the two documents). What class would be assigned to d using a k -NN classifier where we take $k = 3$ then $k = 5$.

- ☐ a. Class A for both $k = 3$ and $k = 5$
- ☐ b. Class A for $k = 3$ and Class B for $k = 5$
- ☐ c. Class B for both $k = 3$ and $k = 5$
- ☒ d. Class B for $k = 3$ and Class A for $k = 5$

