

Knowledge Representation and Reasoning Project 2

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1. Implementing the Back/Forward-Chaining Procedures

1.1. Formulation of the Rules

For this task the following rules were used:

$$\text{KB} \left\{ \begin{array}{l} 1. \text{ In Romania it is a crime for civilians to own guns.} \\ 2. \text{ Criminals break laws.} \\ 3. \text{ Lawbreakers get sent to jail.} \end{array} \right.$$

This knowledge base can be converted into the conjunctive normal form like so:

$$\text{CNF} \left\{ \begin{array}{l} 1. \neg \text{Romanian}(x) \vee \neg \text{Civilian}(x) \vee \neg \text{GunOwner}(x) \vee \text{Criminal}(x) \\ 2. \neg \text{Criminal}(x) \vee \text{LawBreaker}(x) \\ 3. \neg \text{LawBreaker}(x) \vee \text{SentToJail}(x) \end{array} \right.$$

1.2. The Back-Chaining procedure

The back-chaining procedure is an algorithm that can be used to decide whether a full set of sentences can be entailed or not from a given KB. It is expressed in pseudocode below [1].

Algorithm 1 $\text{SOLVE}(q_1, \dots, q_n)$

Input: a finite list of atomic sentences q_1, \dots, q_n

Output: "yes" or "no" depending on whether a given KB entails all of the q_i

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if  $n = 0$  then
    return yes
end if
for each clause  $c \in KB$  do
    if  $c = [q_1, \neg p_1, \dots, \neg p_m]$  and  $\text{SOLVE}[p_1, \dots, p_m, q_2, \dots, q_n]$  then
        return yes
    end if
end for
return no
```

This algorithm was implemented in Prolog following this way of thinking:

- The knowledge base (the rules from the previous subsection) is read from an external file and the following three questions are asked by the program: "Is the person Romanian?", "Is the person a civilian?" and "Does the person own a gun?" (typing "stop." in the console will interrupt this and proceed with the answers gathered up to that point).
- The back-chaining procedure is implemented as a predicate called `backchaining/2`, which takes the KB and a list of atomic clauses (Q) that are based on the answers given by the user. For example, should the user answer "yes", "yes" and "no", the program would assign the values a, b and not(c) to Q.
- If Q is empty, the predicate returns true
- If Q is not empty, the predicate `foreach/2` is used to iterate through KB, in conjuncture with a custom predicate, `do_loop/3`, which takes a clause from the KB, the KB itself and Q.
- The `do_loop` predicate simulates the for-block from Algorithm 1. It first sorts the KB Clause from the respective iteration, since doing that to a positive horn clause arranges the elements in such a way that the positive atomic sentence is placed first ($q_1, \neg p_1, \dots, \neg p_m$).
- Finally, another custom predicate called `if_condition/4`, is used to compare the heads of the sorted KB Clause and of the Q list and to call the backchaining predicate recursively with the respective parameters from the algorithm presented above. If the condition is met, the procedure returns false (in order to stop further execution), and the message "yes" is displayed.

References

- [1] Ronald Brachman, Hector Levesque, “Knowledge Representation and Reasoning,” *Morgan Kaufmann*, p. 92, 2004

```

n(not(A), A).
n(A, not(A)).

head([H|_], H).
tail([_|T], T).

neg_list([], []).
neg_list([Head|Tail], [NegHead|NegTail]) :-
    n(Head, NegHead),
    neg_list(Tail, NegTail), !.

if_condition(KB, Q, QClause, KBClause_Head) :-
    QClause == KBClause_Head,
    backchaining(KB, Q).

backchaining(_, Q) :-member([], Q).
backchaining(KB, Q) :-
    foreach(
        member(KBClause, KB),
        do_loop(KBClause, KB, Q)
    ) .

do_loop(KBClause, KB, Q) :-
    sort(KBClause, KBClause_Sorted),
    head(KBClause_Sorted, KBClause_Sorted_Head),
    head(Q, QClause),
    tail(KBClause_Sorted, KBClause_Sorted_Tail),
    neg_list(KBClause_Sorted_Tail, KBClause_Sorted_Tail_Pos),
    tail(Q, QTail),
    append(KBClause_Sorted_Tail_Pos, QTail, NewQ),
    if_condition(KB, NewQ, QClause, KBClause_Sorted_Head) -> fail; !.

read_KB_and_output_answer_bc(Str, _, []) :-
    at_end_of_stream(Str), !.

read_KB_and_output_answer_bc(Str, Q, [_|T]) :-
    not(at_end_of_stream(Str)),
    read(Str, X),
    backchaining(X, Q) ->
        write(no), nl,
        read_KB_and_output_answer_bc(Str, Q, T)
    ;
        write(yes), nl,
        read_KB_and_output_answer_bc(Str, Q, T).

main :-
    open('data.in', read, Str),
    Questions = [
        'Is the person Romanian?',
        'Is the person a civilian?',
        'Does the person own a gun?'
    ],
    In = [a, b, c],
    read_answers(Questions, In, Q),
    read_KB_and_output_answer_bc(Str, Q, _).

```

```
read_answers(_, [], _).
read_answers([H|T], [In_H|In_T], Out) :-
    writeln(H),
    read(Input),
    (
        Input == 'stop'
    ->
        writeln('Program stopped')
    ;
        Input == 'yes'
    ->
        append([In_H], [], Out),
        read_answers(T, In_T, Out)
    ;
        Input == 'no'
    ->
        n(In_H, In_H_Neg),
        append([In_H_Neg], [], Out),
        read_answers(T, In_T, Out)
    )
    .
```

Listing 1: Resolution Implementation in Prolog