# cryptohack Symmetric Ciphers 部分wp by crumbling

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## SYMMETRIC CIPHERS

### **HOW AES WORKS**

当时似乎是看了这个视频帮助理解,可能没那么牛逼,但总而言之帖上来了:

https://www.bilibili.com/video/BV1i341187fK/?vd\_source=230d5993c02c8821538d172f6b14bc0d

### **Keyed Permutations**

一些基础知识的介绍

flag: bijection

#### **Resisting Bruteforce**

一些基础知识的介绍

**Biclique Cryptanalysis** 

flag: crypto{Biclique}

#### **Structure of AES**

```
def matrix2bytes(matrix):
    """ Converts a 4x4 matrix into a 16-byte array. """
    # 实现了将4*4的矩阵转化为16字节的字符串
    s=""
    for i in range(4):
        for j in range(4):
        s+=chr(matrix[i][j])
    return s
```

```
matrix = [
    [99, 114, 121, 112],
    [116, 111, 123, 105],
    [110, 109, 97, 116],
    [114, 105, 120, 125],
]
print(matrix2bytes(matrix))
```

## **Round Keys**

其实是对add round key 环节的简单体验

```
state = [
    [206, 243, 61, 34],
    [171, 11, 93, 31],
    [16, 200, 91, 108],
    [150, 3, 194, 51],
]
round_key = [
    [173, 129, 68, 82],
    [223, 100, 38, 109],
   [32, 189, 53, 8],
    [253, 48, 187, 78],
]
def add_round_key(s, k):
   m=""
    for i in range(4):
        for j in range(4):
            m+=chr(s[i][j]^k[i][j])
    return m
print(add_round_key(state, round_key))
```

#### **Confusion through Substitution**

利用s-box进行字节替代,是AES的环节之一

```
0xD0, 0xEF, 0xAA, 0xFB, 0x43, 0x4D, 0x33, 0x85, 0x45, 0xF9, 0x02, 0x7F,
0x50, 0x3C, 0x9F, 0xA8,
    0x51, 0xA3, 0x40, 0x8F, 0x92, 0x9D, 0x38, 0xF5, 0xBC, 0xB6, 0xDA, 0x21,
0x10, 0xFF, 0xF3, 0xD2,
    0xCD, 0xOC, 0x13, 0xEC, 0x5F, 0x97, 0x44, 0x17, 0xC4, 0xA7, 0x7E, 0x3D,
0x64, 0x5D, 0x19, 0x73,
    0x60, 0x81, 0x4F, 0xDC, 0x22, 0x2A, 0x90, 0x88, 0x46, 0xEE, 0xB8, 0x14,
OxDE, Ox5E, Ox0B, OxDB,
    0xE0, 0x32, 0x3A, 0x0A, 0x49, 0x06, 0x24, 0x5C, 0xC2, 0xD3, 0xAC, 0x62,
0x91, 0x95, 0xE4, 0x79,
    0xE7, 0xC8, 0x37, 0x6D, 0x8D, 0xD5, 0x4E, 0xA9, 0x6C, 0x56, 0xF4, 0xEA,
0x65, 0x7A, 0xAE, 0x08,
    0xBA, 0x78, 0x25, 0x2E, 0x1C, 0xA6, 0xB4, 0xC6, 0xE8, 0xDD, 0x74, 0x1F,
0x4B, 0xBD, 0x8B, 0x8A,
    0x70, 0x3E, 0xB5, 0x66, 0x48, 0x03, 0xF6, 0x0E, 0x61, 0x35, 0x57, 0xB9,
0x86, 0xC1, 0x1D, 0x9E,
    0xE1, 0xF8, 0x98, 0x11, 0x69, 0xD9, 0x8E, 0x94, 0x9B, 0x1E, 0x87, 0xE9,
0xCE, 0x55, 0x28, 0xDF,
    0x8C, 0xA1, 0x89, 0x0D, 0xBF, 0xE6, 0x42, 0x68, 0x41, 0x99, 0x2D, 0x0F,
0xB0, 0x54, 0xBB, 0x16,
)
inv_s_box = (
    0x52, 0x09, 0x6A, 0xD5, 0x30, 0x36, 0xA5, 0x38, 0xBF, 0x40, 0xA3, 0x9E,
0x81, 0xF3, 0xD7, 0xFB,
    0x7C, 0xE3, 0x39, 0x82, 0x9B, 0x2F, 0xFF, 0x87, 0x34, 0x8E, 0x43, 0x44,
0xC4, 0xDE, 0xE9, 0xCB,
    0x54, 0x7B, 0x94, 0x32, 0xA6, 0xC2, 0x23, 0x3D, 0xEE, 0x4C, 0x95, 0x0B,
0x42, 0xFA, 0xC3, 0x4E,
    0x08, 0x2E, 0xA1, 0x66, 0x28, 0xD9, 0x24, 0xB2, 0x76, 0x5B, 0xA2, 0x49,
0x6D, 0x8B, 0xD1, 0x25,
    0x72, 0xF8, 0xF6, 0x64, 0x86, 0x68, 0x98, 0x16, 0xD4, 0xA4, 0x5C, 0xCC,
0x5D, 0x65, 0xB6, 0x92,
    0x6c, 0x70, 0x48, 0x50, 0xFD, 0xED, 0xB9, 0xDA, 0x5E, 0x15, 0x46, 0x57,
0xA7, 0x8D, 0x9D, 0x84,
    0x90, 0xD8, 0xAB, 0x00, 0x8C, 0xBC, 0xD3, 0x0A, 0xF7, 0xE4, 0x58, 0x05,
0xB8, 0xB3, 0x45, 0x06,
    0xD0, 0x2C, 0x1E, 0x8F, 0xCA, 0x3F, 0x0F, 0x02, 0xC1, 0xAF, 0xBD, 0x03,
0x01, 0x13, 0x8A, 0x6B,
    0x3A, 0x91, 0x11, 0x41, 0x4F, 0x67, 0xDC, 0xEA, 0x97, 0xF2, 0xCF, 0xCE,
0xF0, 0xB4, 0xE6, 0x73,
    0x96, 0xAC, 0x74, 0x22, 0xE7, 0xAD, 0x35, 0x85, 0xE2, 0xF9, 0x37, 0xE8,
0x1C, 0x75, 0xDF, 0x6E,
    0x47, 0xF1, 0x1A, 0x71, 0x1D, 0x29, 0xC5, 0x89, 0x6F, 0xB7, 0x62, 0x0E,
0xAA, 0x18, 0xBE, 0x1B,
    0xFc, 0x56, 0x3E, 0x4B, 0xC6, 0xD2, 0x79, 0x20, 0x9A, 0xDB, 0xC0, 0xFE,
0x78, 0xCD, 0x5A, 0xF4,
    0x1F, 0xDD, 0xA8, 0x33, 0x88, 0x07, 0xC7, 0x31, 0xB1, 0x12, 0x10, 0x59,
0x27, 0x80, 0xEC, 0x5F,
    0x60, 0x51, 0x7F, 0xA9, 0x19, 0xB5, 0x4A, 0x0D, 0x2D, 0xE5, 0x7A, 0x9F,
0x93, 0xC9, 0x9C, 0xEF,
   0xA0, 0xE0, 0x3B, 0x4D, 0xAE, 0x2A, 0xF5, 0xB0, 0xC8, 0xEB, 0xBB, 0x3C,
0x83, 0x53, 0x99, 0x61,
   0x17, 0x2B, 0x04, 0x7E, 0xBA, 0x77, 0xD6, 0x26, 0xE1, 0x69, 0x14, 0x63,
0x55, 0x21, 0x0C, 0x7D,
```

```
state = [
    [251, 64, 182, 81],
    [146, 168, 33, 80],
    [199, 159, 195, 24],
    [64, 80, 182, 255],
]

def sub_bytes(s, sbox=s_box):
    enc=b''
    for i in range(4):
        for j in range(4):
            enc+=long_to_bytes(sbox[s[i][j]])
    return enc

print(sub_bytes(state, sbox=inv_s_box))
```

#### **Diffusion through Permutation**

行位移与列混合,同样是AES加密的其中两个环节。

比较复杂的列混合解密inv\_mix\_columns已经完成,只需要实现对行位移的解密,即inv\_shift\_rows,比较简单。

```
def shift_rows(s): #AES中最简单的变换 行位移
    s[0][1], s[1][1], s[2][1], s[3][1] = s[1][1], s[2][1], s[3][1], s[0][1]
    s[0][2], s[1][2], s[2][2], s[3][2] = s[2][2], s[3][2], s[0][2], s[1][2]
    s[0][3], s[1][3], s[2][3], s[3][3] = s[3][3], s[0][3], s[1][3], s[2][3]
def inv_shift_rows(s):
    s[1][1], s[2][1], s[3][1], s[0][1] = s[0][1], s[1][1], s[2][1], s[3][1]
    s[2][2], s[3][2], s[0][2], s[1][2] = s[0][2], s[1][2], s[2][2], s[3][2]
    s[3][3], s[0][3], s[1][3], s[2][3] = s[0][3], s[1][3], s[2][3], s[3][3]
    return s
# learned from http://cs.ucsb.edu/~koc/cs178/projects/JT/aes.c
xtime = lambda a: (((a << 1) ^{\circ} 0x1B) & 0xFF) if (a & 0x80) else (a << 1)
def mix_single_column(a):
    # see Sec 4.1.2 in The Design of Rijndael
    t = a[0] \wedge a[1] \wedge a[2] \wedge a[3]
    u = a[0]
    a[0] \wedge = t \wedge xtime(a[0] \wedge a[1])
    a[1] \wedge = t \wedge xtime(a[1] \wedge a[2])
    a[2] \wedge = t \wedge xtime(a[2] \wedge a[3])
    a[3] \wedge = t \wedge xtime(a[3] \wedge u)
def mix_columns(s):
    for i in range(4):
        mix_single_column(s[i])
```

```
def inv_mix_columns(s):
    # see Sec 4.1.3 in The Design of Rijndael
    for i in range(4):
        u = xtime(xtime(s[i][0] \land s[i][2]))
        v = xtime(xtime(s[i][1] \land s[i][3]))
        s[i][0] \wedge = u
        s[i][1] ^= v
        s[i][2] \wedge = u
        s[i][3] \wedge = v
    mix_columns(s)
    return s
state = [
    [108, 106, 71, 86],
    [96, 62, 38, 72],
    [42, 184, 92, 209],
    [94, 79, 8, 54],
]
state=inv_shift_rows(inv_mix_columns(state))
flag=""
for i in range(4):
    for j in range(4):
        flag+= chr(state[i][j])
print(flag)
```

#### **Bringing It All Together**

前面4个小题结合起来,这里就是一个简化版AES的加密与解密。

```
from Crypto.Util.number import long_to_bytes
N_ROUNDS = 10
def matrix2bytes(matrix):
    """ Converts a 4x4 matrix into a 16-byte array. """
    s=b""
    for i in range(4):
       for j in range(4):
            s+=long_to_bytes(matrix[i][j])
    return s
s_box = (
   0x63, 0x7c, 0x77, 0x7B, 0xF2, 0x6B, 0x6F, 0xC5, 0x30, 0x01, 0x67, 0x2B,
0xFE, 0xD7, 0xAB, 0x76,
   0xCA, 0x82, 0xC9, 0x7D, 0xFA, 0x59, 0x47, 0xF0, 0xAD, 0xD4, 0xA2, 0xAF,
0x9C, 0xA4, 0x72, 0xC0,
   0xB7, 0xFD, 0x93, 0x26, 0x36, 0x3F, 0xF7, 0xCC, 0x34, 0xA5, 0xE5, 0xF1,
0x71, 0xD8, 0x31, 0x15,
   0x04, 0xc7, 0x23, 0xc3, 0x18, 0x96, 0x05, 0x9A, 0x07, 0x12, 0x80, 0xe2,
0xEB, 0x27, 0xB2, 0x75,
   0x09, 0x83, 0x2C, 0x1A, 0x1B, 0x6E, 0x5A, 0xAO, 0x52, 0x3B, 0xD6, 0xB3,
0x29, 0xE3, 0x2F, 0x84,
```

```
0x53, 0xD1, 0x00, 0xED, 0x20, 0xFC, 0xB1, 0x5B, 0x6A, 0xCB, 0xBE, 0x39,
0x4A, 0x4C, 0x58, 0xCF,
    0xD0, 0xEF, 0xAA, 0xFB, 0x43, 0x4D, 0x33, 0x85, 0x45, 0xF9, 0x02, 0x7F,
0x50, 0x3C, 0x9F, 0xA8,
    0x51, 0xA3, 0x40, 0x8F, 0x92, 0x9D, 0x38, 0xF5, 0xBC, 0xB6, 0xDA, 0x21,
0x10, 0xFF, 0xF3, 0xD2,
    0xCD, 0xOC, 0x13, 0xEC, 0x5F, 0x97, 0x44, 0x17, 0xC4, 0xA7, 0x7E, 0x3D,
0x64, 0x5D, 0x19, 0x73,
    0x60, 0x81, 0x4F, 0xDC, 0x22, 0x2A, 0x90, 0x88, 0x46, 0xEE, 0xB8, 0x14,
0xDE, 0x5E, 0x0B, 0xDB,
    0xE0, 0x32, 0x3A, 0x0A, 0x49, 0x06, 0x24, 0x5C, 0xC2, 0xD3, 0xAC, 0x62,
0x91, 0x95, 0xE4, 0x79,
    0xE7, 0xC8, 0x37, 0x6D, 0x8D, 0xD5, 0x4E, 0xA9, 0x6C, 0x56, 0xF4, 0xEA,
0x65, 0x7A, 0xAE, 0x08,
    0xBA, 0x78, 0x25, 0x2E, 0x1C, 0xA6, 0xB4, 0xC6, 0xE8, 0xDD, 0x74, 0x1F,
0x4B, 0xBD, 0x8B, 0x8A,
    0x70, 0x3E, 0xB5, 0x66, 0x48, 0x03, 0xF6, 0x0E, 0x61, 0x35, 0x57, 0xB9,
0x86, 0xC1, 0x1D, 0x9E,
    0xE1, 0xF8, 0x98, 0x11, 0x69, 0xD9, 0x8E, 0x94, 0x9B, 0x1E, 0x87, 0xE9,
0xCE, 0x55, 0x28, 0xDF,
    0x8C, 0xA1, 0x89, 0x0D, 0xBF, 0xE6, 0x42, 0x68, 0x41, 0x99, 0x2D, 0x0F,
0xB0, 0x54, 0xBB, 0x16,
)
inv_s_box = (
    0x52, 0x09, 0x6A, 0xD5, 0x30, 0x36, 0xA5, 0x38, 0xBF, 0x40, 0xA3, 0x9E,
0x81, 0xF3, 0xD7, 0xFB,
    0x7c, 0xE3, 0x39, 0x82, 0x9B, 0x2F, 0xFF, 0x87, 0x34, 0x8E, 0x43, 0x44,
0xC4, 0xDE, 0xE9, 0xCB,
    0x54, 0x7B, 0x94, 0x32, 0xA6, 0xC2, 0x23, 0x3D, 0xEE, 0x4C, 0x95, 0x0B,
0x42, 0xFA, 0xC3, 0x4E,
    0x08, 0x2E, 0xA1, 0x66, 0x28, 0xD9, 0x24, 0xB2, 0x76, 0x5B, 0xA2, 0x49,
0x6D, 0x8B, 0xD1, 0x25,
    0x72, 0xF8, 0xF6, 0x64, 0x86, 0x68, 0x98, 0x16, 0xD4, 0xA4, 0x5C, 0xCC,
0x5D, 0x65, 0xB6, 0x92,
    0x6C, 0x70, 0x48, 0x50, 0xFD, 0xED, 0xB9, 0xDA, 0x5E, 0x15, 0x46, 0x57,
0xA7, 0x8D, 0x9D, 0x84,
    0x90, 0xD8, 0xAB, 0x00, 0x8C, 0xBC, 0xD3, 0x0A, 0xF7, 0xE4, 0x58, 0x05,
0xB8, 0xB3, 0x45, 0x06,
    0xD0, 0x2C, 0x1E, 0x8F, 0xCA, 0x3F, 0x0F, 0x02, 0xC1, 0xAF, 0xBD, 0x03,
0x01, 0x13, 0x8A, 0x6B,
    0x3A, 0x91, 0x11, 0x41, 0x4F, 0x67, 0xDC, 0xEA, 0x97, 0xF2, 0xCF, 0xCE,
0xF0, 0xB4, 0xE6, 0x73,
    0x96, 0xAC, 0x74, 0x22, 0xE7, 0xAD, 0x35, 0x85, 0xE2, 0xF9, 0x37, 0xE8,
0x1C, 0x75, 0xDF, 0x6E,
    0x47, 0xF1, 0x1A, 0x71, 0x1D, 0x29, 0xC5, 0x89, 0x6F, 0xB7, 0x62, 0x0E,
0xAA, 0x18, 0xBE, 0x1B,
    0xFC, 0x56, 0x3E, 0x4B, 0xC6, 0xD2, 0x79, 0x20, 0x9A, 0xDB, 0xC0, 0xFE,
0x78, 0xCD, 0x5A, 0xF4,
    0x1F, 0xDD, 0xA8, 0x33, 0x88, 0x07, 0xC7, 0x31, 0xB1, 0x12, 0x10, 0x59,
0x27, 0x80, 0xEC, 0x5F,
   0x60, 0x51, 0x7F, 0xA9, 0x19, 0xB5, 0x4A, 0x0D, 0x2D, 0xE5, 0x7A, 0x9F,
0x93, 0xC9, 0x9C, 0xEF,
   0xA0, 0xE0, 0x3B, 0x4D, 0xAE, 0x2A, 0xF5, 0xB0, 0xC8, 0xEB, 0xBB, 0x3C,
0x83, 0x53, 0x99, 0x61,
```

```
0x17, 0x2B, 0x04, 0x7E, 0xBA, 0x77, 0xD6, 0x26, 0xE1, 0x69, 0x14, 0x63,
0x55, 0x21, 0x0C, 0x7D,
def inv_sub_bytes(s, sbox=inv_s_box):
    for i in range(4):
        for j in range(4):
             s[i][j]=sbox[s[i][j]]
    return s
def inv_shift_rows(s):
    s[1][1], s[2][1], s[3][1], s[0][1] = s[0][1], s[1][1], s[2][1], s[3][1]
    s[2][2], s[3][2], s[0][2], s[1][2] = s[0][2], s[1][2], s[2][2], s[3][2]
    s[3][3], s[0][3], s[1][3], s[2][3] = s[0][3], s[1][3], s[2][3], s[3][3]
    return s
xtime = lambda a: (((a << 1) ^{\land} 0x1B) & 0xFF) if (a & 0x80) else (a << 1)
def mix_single_column(a):
    # see Sec 4.1.2 in The Design of Rijndael
    t = a[0] \wedge a[1] \wedge a[2] \wedge a[3]
    u = a[0]
    a[0] \wedge = t \wedge xtime(a[0] \wedge a[1])
    a[1] \wedge = t \wedge xtime(a[1] \wedge a[2])
    a[2] \wedge = t \wedge xtime(a[2] \wedge a[3])
    a[3] \wedge = t \wedge xtime(a[3] \wedge u)
def mix_columns(s):
    for i in range(4):
        mix_single_column(s[i])
def inv_mix_columns(s):
    # see Sec 4.1.3 in The Design of Rijndael
    for i in range(4):
         u = xtime(xtime(s[i][0] \land s[i][2]))
        v = xtime(xtime(s[i][1] \land s[i][3]))
        s[i][0] \wedge = u
         s[i][1] \wedge = v
         s[i][2] \wedge = u
         s[i][3] \wedge = v
    mix_columns(s)
    return s
            = b'\xc3,\\xa6\xb5\x80^\x0c\xdb\x8d\xa5z*\xb6\xfe\'
ciphertext = b'\xd10\x14j\xa4+0\xb6\xa1\xc4\x08B)\x8f\x12\xdd'
def add_round_key(s, k):
    for i in range(4):
         for j in range(4):
             s[i][j]=s[i][j]^k[i][j]
    return s
def bytes2matrix(text):
    return [list(text[i:i+4]) for i in range(0, len(text), 4)]
def expand_key(master_key):
```

```
Expands and returns a list of key matrices for the given master_key.
    # Round constants
https://en.wikipedia.org/wiki/AES_key_schedule#Round_constants
    r\_con = (
        0x00, 0x01, 0x02, 0x04, 0x08, 0x10, 0x20, 0x40,
        0x80, 0x1B, 0x36, 0x6C, 0xD8, 0xAB, 0x4D, 0x9A,
        0x2F, 0x5E, 0xBC, 0x63, 0xC6, 0x97, 0x35, 0x6A,
        0xD4, 0xB3, 0x7D, 0xFA, 0xEF, 0xC5, 0x91, 0x39,
    )
    # Initialize round keys with raw key material.
    key_columns = bytes2matrix(master_key)
    iteration_size = len(master_key) // 4
    # Each iteration has exactly as many columns as the key material.
    while len(key_columns) < (N_ROUNDS + 1) * 4:
        # Copy previous word.
        word = list(key_columns[-1])
        # Perform schedule_core once every "row".
        if len(key_columns) % iteration_size == 0:
            # Circular shift.
            word.append(word.pop(0))
            # Map to S-BOX.
            word = [s_box[b] for b in word]
            # XOR with first byte of R-CON, since the others bytes of R-CON are
0.
            word[0] \land = r\_con[i]
            i += 1
        elif len(master_key) == 32 and len(key_columns) % iteration_size == 4:
            # Run word through S-box in the fourth iteration when using a
            # 256-bit key.
            word = [s_box[b] for b in word]
        # XOR with equivalent word from previous iteration.
        word = bytes(i^j for i, j in zip(word, key_columns[-iteration_size]))
        key_columns.append(word)
    # Group key words in 4x4 byte matrices.
    return [key_columns[4*i : 4*(i+1)] for i in range(len(key_columns) // 4)]
def decrypt(key, ciphertext):
    round_keys = expand_key(key) # Remember to start from the last round key and
work backwards through them when decrypting
    exciphertext= bytes2matrix(ciphertext)# Convert ciphertext to state matrix
    exciphertext= add_round_key(exciphertext, round_keys[10])
    # Initial add round key step
    for i in range(N_ROUNDS - 1, 0, -1):
        """range(start, stop[, step])"""
        exciphertext=inv_shift_rows(exciphertext)
```

```
exciphertext=inv_sub_bytes(exciphertext)
    exciphertext=add_round_key(exciphertext,round_keys[i])
    exciphertext=inv_mix_columns(exciphertext)
    exciphertext = inv_shift_rows(exciphertext)
    exciphertext = inv_sub_bytes(exciphertext)
    exciphertext = add_round_key(exciphertext,round_keys[0])
# Run final round (skips the InvMixColumns step)
plaintext=matrix2bytes(exciphertext)
# Convert state matrix to plaintext
return plaintext
print(decrypt(key, ciphertext))
```

## SYMMETRIC STARTER

## **Modes of Operation Starter**

题目会根据flag生成一个加密后的信息,根据网页中显示的源代码,flag经历了encode编码和ECB模式的AES加密,并且给出了解密函数(虽然全程看不到key的具体数据,但解密函数显然使用了和加密过程相同的key,所以解密函数不会出现问题)。

那么求解过程只需要解密后decode解码就行。

网页上可以解密,贴一下他的代码:

```
from Crypto.Cipher import AES
KEY = ?
FLAG = ?
@chal.route('/block_cipher_starter/decrypt/<ciphertext>/')
def decrypt(ciphertext):
    ciphertext = bytes.fromhex(ciphertext)
    cipher = AES.new(KEY, AES.MODE_ECB)
        decrypted = cipher.decrypt(ciphertext)
    except ValueError as e:
        return {"error": str(e)}
    return {"plaintext": decrypted.hex()}
@chal.route('/block_cipher_starter/encrypt_flag/')
def encrypt_flag():
    cipher = AES.new(KEY, AES.MODE_ECB)
    encrypted = cipher.encrypt(FLAG.encode())
    return {"ciphertext": encrypted.hex()}
```