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Temporal comprehension in autonomous drone racing: infer navigation decisions from current and past raw sensor data with a recurrent convolutional neural network

Master Thesis

am Fachgebiet Agententechnologien in betrieblichen Anwendungen und der
Telekommunikation (AOT)

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Abstract

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- one paragraph on the motivation to your topic
- one paragraph on what approach you have chosen
- and one paragraph on your results which may be presented in comparison to other approaches that try to solve the same or a similar problem.

Abstract should not exceed one page (aubrey's opinion)

Zusammenfassung

DELETEME: translate to German to Englisch or vice-versa.

Acknowledgements

DELETEME: Thank you for the music, the songs I am singing

Yacine Zahidi: Paris Pytorch Lukas Kilian: Computer Unity Administratives HU:
RÄ¼cken freigehalten, immer unterstÄ¼tzt

Contents

List of Figures	viii
List of Tables	ix
1 Introduction	1
1.1 Motivation	1
1.2 Approach and Goals	2
1.3 Structure of the Thesis	3
2 Background	4
2.1 Topic 1	5
2.2 Imitation Learning with Dataset Aggregation	5
2.3 Gated recurrent unit	8
3 Autonomous Navigation Method	21
3.1 Reference systems	21
3.2 ANN module	25
3.3 Planning module	32
3.4 Control stack	35
3.5 Expert system	36
3.6 Racing vs. Training Data Generation	42
4 Experiments in Simulation	43
4.1 Simulation Setup	43
4.2 Imitation learning process of the ANN Module	47
4.3 Racing Tests	49
4.4 Experiment 1	50
5 Evaluation	56
5.1 Results	56
5.2 Discussions	56

6	Conclusion and Future Work	61
6.1	Summary	61
6.2	Conclusion	61
6.3	Future Work	61
	Bibliography	62
	Appendices	68
	Appendix A: Abbreviations	69
	Appendix B: L ^A T _E X Help	70

List of Figures

2.1	Folded and unfolded RNN	9
2.2	The non-linear activation functions deployed within a standard GRU . .	14
2.3	Time-unfolded computation graph of a GRU layer operating in many- to-one mode.	15
3.1	The local and the image reference system	23
3.2	Information flow of the navigation decision making	26
3.3	The control stack in simulation.	35
3.4	Update of the projection state index	40
4.1	Implementation concept of the simulation	43
4.2	Scenes available in simulation	44
4.3	Race gates available in simulation	45
4.4	Racetrack randomization and redirection	55
5.1	???	57
5.2	???	58
5.3	???	59
5.4	???	60
6.1	Including an Image	74
6.2	Short caption for list of figures	74
6.3	Placing images side by side	74

List of Tables

4.1	Available options for the simulation configuration	45
4.2	Deterministic gate poses	46
4.3	Learning configuration	47
4.4	Testing configuration	49
4.5	ANN Module Variants of Experiment 1	51
4.6	Learning configuration of Experiment 1	52
4.7	Numbers of trainable parameters and multiply-accumulate operations of the ANN module variants of experiment 1	53
6.1	Simple table using vertical lines. Note that the caption is always above the table! Please check code for finding the right place for the table label.	75
6.2	Table using vertical and horizontal lines	75
6.3	Table with column width specification on last column	75
6.4	Table using multi-column and multirow	76

Chapter 1

Introduction

1.1 Motivation

Advances in drone technology in recent years have opened the door to many civilian application possibilities, especially in the commercial sector [12]. Today, drones are already standard in aerial inspection services [11, 1, 3]. In the near future, the areas of infrastructure, transport, insurance, media and entertainment, telecommunication, agriculture, safety and mining are considered to be particularly promising [36]. In contrast, real breakthroughs of more visionary applications, such as drone delivery or drone taxis are, if at all, only expected in the more distant future [48]. Reasons for this are strict regulations, skeptical public attitudes and technical problems [48]. With regard to the latter, autonomous navigation methods are not yet robust enough for the reliable deployment in open-world environments of high uncertainty such as densely populated urban areas [7]. This makes the autonomous navigation of drones of great importance in current research. Loquercio and Scaramuzza [35] categorize existing autonomous navigation methods for drones into classical methods and modern, machine learning based methods.

Classical autonomous navigation methods follow the scheme of mapping-localization-planning-tracking. Simple approaches track pre-programmed waypoints based on GNSS and are thus limited to flight environments that first, have a reliable GNSS signal (which often is not the case for urban areas, mountains, indoor sites, caves, etc.) and second, are free of obstacles, since functions to cope with them are absent. More complex approaches use SLAM algorithms to generate a map of the flight environment and localize in it based on the drone's visual or range sensors. [42] Path planning algorithms (e.g., [5], [10]) are applied to generate collision-free trajectories through the generated maps, which are tracked while estimating the drone state based on data from the drone's inertial measurement unit (IMU) and the output of SLAM algorithms (e.g., [33], [53], [51], [34]). Theoretically, these approaches can be deployed

in uncontrolled environments with unknown obstacles and other agents. Practically, the mapping coerces global consistency which likely makes the computation too complex to be run in real-time onboard drones, especially for non-static environments.

Modern autonomous navigation methods use machine learning to replace the classical mapping-localization (or even the planning and tracking for more end-to-end methods) with the perception of the drone’s onboard sensors (e.g., visual, range, IMU) and the decisions making of an ANN. These methods can be further subdivided by their way of learning into reinforcement learning (RL) and imitation learning (IL). RL has the advantage that they are not affected by the ”distributional mismatch” [2] between training and testing as the ANN learns with ”trial-and-error” [52] from direct environmental interaction. However, this comes with the expense of a substantially higher sample complexity compared to IL. [61] This disadvantage is severe for drones because their limited flight endurance makes the learning process inefficient and collisions are uncontrolled and hence costly and dangerous. [52]

A popular research playground is autonomous drone racing (e.g., [40], [25], [56]) due to the controlled flight environment, the straightforward definition of goals and the measureability and comparability of performance. Methods for autonomous drone racing usually integrate feedforward convolutional neural networks (CNN) to map the current color or depth image to action (e.g., [47], [28], [26]). CNNs already achieve a high, spatial comprehension of how the drone’s sensors perceive the immediate environment, however, this alone may not be enough for the long-term objective of safely applying autonomous drones in open-world environments. As humans are able to safely navigate there, it seems promising to learn human-like abilities. Temporal comprehension, besides spatial comprehension, has an important function in human navigation. For example, after entering a room through a door, a person can leave the room knowing that the door is behind him and does not need to keep the door in sight to do so. Further, a person requires to observe a sequence of images to estimate the velocity and motion direction of herself or himself, obstacles or other agents. In machine learning, recurrent neural networks can establish temporal connections. It is interesting to research the effect of using a recurrent neural networks in autonomous drone racing.

1.2 Approach and Goals

This thesis aims to investigate the question whether temporal comprehension induced by a recurrent neural network can be beneficial for the autonomous navigation in drone racing. To do this, the thesis uses the vision-based autonomous navigation method proposed by Kaufmann et al. [29] as a baseline. In the tests conducted by the authors, the baseline method stood out from the compared methods with high reliability and agility along dynamic flight curves through the racetrack. The baseline method has a hybrid structure: an artificial neural network inferring navigation decisions from the images of

the drone’s onboard camera and a planning-control stack translating these decisions into flight movement. The baseline ANN is a serial connection of a convolutional neural network (CNN) and fully-connected (FC) layers. The CNN extracts visual features from imagery, thereby enabling the baseline method to spatially comprehend what is in the field of view of the drone’s onboard camera.

This thesis extends the baseline ANN with a multi-layer gated recurrent unit (GRU). Theoretically, this recurrent neural network variant enables the autonomous navigation method to remember and to establish temporal connections. Specifically, this means that navigation decisions would be made based on both current and past sensor data. Considering that, first, navigation can be seen as sequentially making decisions regarding how to move through space, and second, the thereby resulting trajectories are 4D objects in space and time, the CNN-GRU approach of this thesis, by incorporating both spatial and temporal understanding, is expected to improve the racing performance. This hypothesis is investigated in simulated drone races. Different variants of ANNs are tested for their robustness at different maximum speeds and for their ability to cope with intermediate target loss. The latter refers to the event that the next race gate intermediately leaves the FOV of the drone’s camera (e.g., due to a sharp turn between two race gates) and the drone can only make meaningful navigation decisions based on the memory induced by the GRU.

1.3 Structure of the Thesis

This thesis is structured as follows. Chapter 2 provides background information on the thesis topic. This includes the machine learning field of imitation learning, in particular with dataset aggregation, and recurrent neural networks, in particular the gated recurrent unit. Chapter 3 presents the applied autonomous drone racing navigation method, which consists of the ANN, planning and control submodules. Special attention is paid here to the ANN submodule, as it is the part that enables temporal comprehension and therewith distinguishes this thesis from the original method. Chapter 4 presents the experiments of the thesis. Racing tests for the navigation method with different ANN submodule variants are carried out in simulation. Thereby, the performance of the variants are measured. Chapter 5 evaluates the results of the racing experiments. The focus lies on the question, whether temporal comprehension is beneficial to the racing performance. Chapter 6 is the conclusion of this thesis. At last, Chapter 6.3 gives additional related information on the topic of this thesis.

Chapter 2

Background

DELETEME: This chapter will cover all of your background information and related work. Background and related work are directly related to your thesis. Please do not place irrelevant content here which is a common mistake. Citing will be handled in the appendices.

DELETEME: Background represents underlying knowledge that is required to understand your work. The expected knowledge level of your readers can be set to the one of a bachelor or master student who just finished his studies (depending on what kind of thesis you are writing). This means that you do not need to describe how computers work, unless your thesis topic is about this. Everything that an average alumni from your field of studies should now does not need to be described. In turn, background information that is very complex and content-wise very near to your problem, can be placed in the main parts. Everything else should be written here. Note: it is important to connect each presented topic to your thesis. E.g. if you present the ISO/OSI layer model you should also write that this is needed to understand the protocols you plan to develop in the main parts.

DELETEME: Related work represents results from work that handled the same or a similar problem that you are addressing. This work might have used a different approach or might not have been that successful. Finding a paper / work that solved your problem in the same way you were planning to do is not good and you should contact your supervisor for solving this issue. Again, each paper / work has to be connected to your approach: other papers might have not chosen an optimal solution; they might not have been taking care of essential aspects; they might have chosen a different approach and you believe, yours will work better ...

2.1 Topic 1

2.2 Imitation Learning with Dataset Aggregation

Imitation learning is an area of machine learning that considers the task of learning to imitate (i.e., behave like) an expert in a sequential decision-making problem. It is a potential solution to learning problems where it is easier to demonstrate the desired behavior of attaining a goal than to define intermediate goals and rewards (as in supervised and reinforcement learning, respectively) that lead to the desired behavior. In terms of supervision, imitation learning is therefore located between supervised learning and reinforcement learning. [43] Imitation learning tends to apply successfully on tasks related to human intent/behaviour, e.g., pedestrian avoidance [62], speech animation [57], sport analytics [30] and gaming [58]. With respect to planning and control in autonomous navigation, imitation learning has become state-of-the-art. [38] The methods of imitation learning can be divided by their approach into direct policy learning and inverse reinforcement learning. [2] Direct policy learning optimizes a policy class to approximate the expert's behaviour by reducing the imitation learning problem to a single or a sequence of supervised learning problems. Inverse reinforcement learning optimizes a reward function to approximate the expert's underlying intent and deploys reinforcement learning methods to optimize a policy class to maximize the identified reward.

In this thesis, the training of the ANN module of the autonomous navigation method (see section 3.2) is considered an imitation learning problem. In the experiments (see section 4.2), direct policy learning with dataset aggregation is applied to solve this problem. Therefore this section introduces the core concept of dataset aggregation, which was proposed as DAgger by Ross et al. [49]. Prior to this, the general imitation learning problem is defined and behavioural cloning, the simplest form of direct policy learning is presented.

Problem definition

An imitation learning problem includes: a system, an expert, a policy class, a loss function, and a learning algorithm. The goal is to find the policy within the policy class that approximates the expert's decision making as closely as possible. [60]

The system interacts with its real or simulated environment. At time step t , the system is in the state $\underline{x}_t \in \mathcal{X}$ and executes the action $\underline{u}_t \in \mathcal{U}$ where \mathcal{X} and \mathcal{U} are the spaces of all possible system states and actions, respectively. The system is considered a MDP (Markov decision process) whose initial state is sampled from the distribution $p(\underline{x}_0)$. The system dynamics can be described with a probabilistic transition model, which provides the conditional probability distribution over the system state given the

system state and action from the previous time step

$$p(\underline{x}_t | \underline{x}_{t-1}, \underline{u}_{t-1}). \quad (2.1)$$

The expert is a human or a computer program that makes state-based action decisions, which cause the system to act as desired. This decision making process is described by the expert policy which maps system states to expert actions

$$\pi^* : \mathcal{X} \rightarrow \mathcal{U}; \quad \underline{x}_t \mapsto \underline{u}_t^*. \quad (2.2)$$

Applying the expert policy on a system state yields a demonstration, i.e., the state-action pair $(\underline{x}_t, \underline{u}_t^*)$.

The policy class defines the search space the optimal policy, i.e., the policy that most closely imitates the expert policy. In the following, the policy class is considered to be an ANN (artificial neural network)

$$\pi_{\underline{\theta}} : \mathcal{X} \rightarrow \mathcal{U}; \quad \underline{x}_t \mapsto \pi_{\underline{\theta}}(\underline{x}_t) \quad (2.3)$$

where the vector $\underline{\theta}$ contains the trainable parameters of the ANN.

Both, the expert policy and members of the policy class, can be rolled out. The rollout of a general policy $\pi : \mathcal{X} \rightarrow \mathcal{U}$ denotes the process, in which the system, starting from the initial state $\underline{x}_0 \sim p(\underline{x}_0)$, interacts with the environment based on the actions inferred by that policy for a certain number of time steps

$$p(\underline{x}_t | \underline{x}_{t-1}, \pi(\underline{x}_{t-1})), \quad t \in \{0, \dots, T\}. \quad (2.4)$$

A rollout produces a trajectory, which is the sequence of the state-action pairs visited during rollout

$$\tau = (\underline{x}_t, \pi(\underline{x}_t))_{t \in \{0, \dots, T\}}. \quad (2.5)$$

The state distribution of a policy rollout, i.e., the probability that a state is visited during the rollout of the policy and becomes therewith part of the corresponding trajectory, is induced by the policy itself. It is calculated by averaging the state distributions over the time steps of the rollout

$$p(\underline{x} | \pi) = \frac{1}{T+1} \sum_{t=0}^T p(\underline{x}_t | \pi). \quad (2.6)$$

The loss function quantifies how closely a policy π imitates the expert policy π^* . For a state, it measures the deviation of the action predicted by the general policy from the action demonstrated by the expert

$$L_{\pi} : \mathcal{X} \rightarrow \mathbb{R}; \quad \underline{x}_t \mapsto L_{\pi}(\pi(\underline{x}_t), \pi^*(\underline{x}_t)). \quad (2.7)$$

The learning algorithm finds the policy $\hat{\pi}^*$ within the policy class that is closest to the expert policy. For this purpose, the algorithm minimizes the total imitation loss evaluated for states sampled from the distribution induced by the identified policy itself. In machine learning, the optimization is realized with the training of the ANN, whereby its trainable parameters are updated according to the evaluated loss

$$\hat{\pi}^* = \underset{\underline{\theta}}{\operatorname{argmin}} \sum_{\underline{x} \sim p(\underline{x}|\pi_{\underline{\theta}})} L_{\pi_{\underline{\theta}}}(\underline{x}). \quad (2.8)$$

The above optimization corresponds to a "non-i.i.d. supervised learning problem" [49]. Note that, as generally the system dynamics are unknown or too complex, the training data cannot be computed to be independent and identically distributed (i.i.d.) across the state space \mathcal{X} . In fact, the only way to generate training data is to sample it during policy rollouts. General optimization learning takes the most reliable, available option of generating training data from rollouts of the identified policy itself. This has the advantage, that the state distributions at training and testing (rollout) do not differ and thus, a low training loss is likely to transfer to good test performance. On the downside, the interdependence of the ANN and the training state distribution renders the optimization to be non-convex and thus complex in contrast to common supervised learning.

Behavioural cloning

Behavioural cloning reduces the imitation learning problem to a single standard supervised learning problem on a precollected training dataset of expert trajectories

$$D = \{\tau_i^*\}_{i \in \{1,2,\dots\}}, \quad \tau_i^* = (\underline{x}_{i,t}, \underline{u}_{i,t}^*)_{t \in \{0,1,\dots\}}. \quad (2.9)$$

Each trajectory is the product of an expert policy rollout and contains the thereby demonstrated state-action pairs. The state distribution of an expert rollout is

$$p(\underline{x}|\pi^*) = \frac{1}{T+1} \sum_{t=0}^T p(\underline{x}_t|\pi^*). \quad (2.10)$$

The optimization problem of BC is thus to minimize the accumulated imitation loss of all demonstrations $(\underline{x}_t, \underline{u}_t^*)$ of all trajectories τ_i within the dataset D precollected

$$\begin{aligned} \hat{\pi}^* &= \underset{\underline{\theta}}{\operatorname{argmin}} \sum_{\tau_i \in D} \sum_{(\underline{x}_t, \underline{u}_t^*) \in \tau_i} L(\pi_{\underline{\theta}}(\underline{x}_t), \underline{u}_t^*) \\ &= \underset{\underline{\theta}}{\operatorname{argmin}} \sum_{\underline{x} \sim p(\underline{x}|\pi^*)} L_{\pi_{\underline{\theta}}}(\underline{x}). \end{aligned} \quad (2.11)$$

In comparison to general imitation learning, behavioural cloning generally exhibits different distributions at training and testing

$$p(\underline{x}|\pi^*) \neq p(\underline{x}|\pi_{\underline{\theta}}). \quad (2.12)$$

This plus the fact that the training data is generally not iid across the state space makes it likely that the ANN is confronted with states not seen during training. As a result, a good test performance cannot be generally inferred from a low training loss. This is especially true for a long task horizon T of a rollout. The above optimization can be interpreted as minimizing the one-step loss of the trained ANN along the expert trajectories. However, as the trained ANN rolls out at testing, these one-step errors, even though minimized, accumulate along the ANN trajectory and will likely cause non-negligible deviation from the expert’s behaviour. In fact, on a ANN trajectory the upper bound of the error grows quadratically with the number of timesteps. [60]

Dagger

Dagger[49] is an iterative method for direct policy learning that reduces the imitation learning problem to a sequence of convex supervised learning problems:

1. Roll out the expert policy to generate a dataset. Train the initial ANN $\pi_{\theta,0}$ with behavioural cloning on that dataset.
2. For $i = 1, 2, \dots$
 - (a) Rollout the initial/intermediate ANN $\pi_{\theta,i-1}$ to generate trajectories.
 - (b) Label the trajectories using the expert policy and add them to the training dataset.
 - (c) Train the next intermediate ANN $\pi_{\theta,i}$ on the aggregated dataset.

In contrast to behavioural cloning, DAgger requires an interactive expert, that provides feedback on the state distributions induced by the ANN, and access on the system to execute ANN rollouts. The DAgger algorithm makes sure that mistakes made by the ANN during rollout become part of the aggregated dataset. Ideally, this training converges to the optimal ANN parameters for the general IL problem.

2.3 Gated recurrent unit

The artificial neural network (ANN) of the autonomous navigation method of this thesis integrates the PyTorch implementation¹ of the gated recurrent unit (GRU) with the objective to involve temporal comprehension in the navigation decision making. The GRU, published in 2014 by Cho et al. [8], is a variant of the ANN class of recurrent neural networks (RNN). This section shortly introduces the RNN class and justifies the design choice for the GRU in light of standard RNNs and the more prevalent RNN

¹<https://pytorch.org/docs/stable/generated/torch.nn.GRU.html>, visited on 09/07/2022

variant, the long short-term memory (LSTM). Moreover, it provides an insight into the mechanisms of the GRU that make temporal comprehension available as well as how the GRU trains its temporal comprehension by backpropagating loss through time.

Recurrent neural networks

RNNs contrasts with classical feedforward ANNs, which forward information exclusively towards subsequent layers, by featuring dynamic properties that stem from the implementation of feedback connections [22] (see fig. 2.1a). As previously inferred states re-enter the network, the output of an RNN depends not only on the current but also on prior inputs. In this sense, an RNN is qualified to process and reason on entire sequences of data points. In case of time-series data, this can be interpreted as temporal comprehension and memory [23]. RNNs train on sequential data with backpropagation through time (BPTT) [45] which is basically the application of standard backpropagation (e.g., [46]) on the unfolded representation of the RNN (see figure 2.1b). The unfolded representation exhibits a layer for each data point in the given input sequence and can be construed as a feedforward ANN that shares its trainable parameters across its layers. The longer the input sequences, the deeper the unfolded representation of an RNN becomes. The training of RNNs on long sequences is hence prone to the vanishing gradient problem [20], which manifests itself in the premature slowdown or standstill of the convergence of the RNN. As a result, standard RNNs have difficulties learning to connect to information from inputs deep in the past [4].

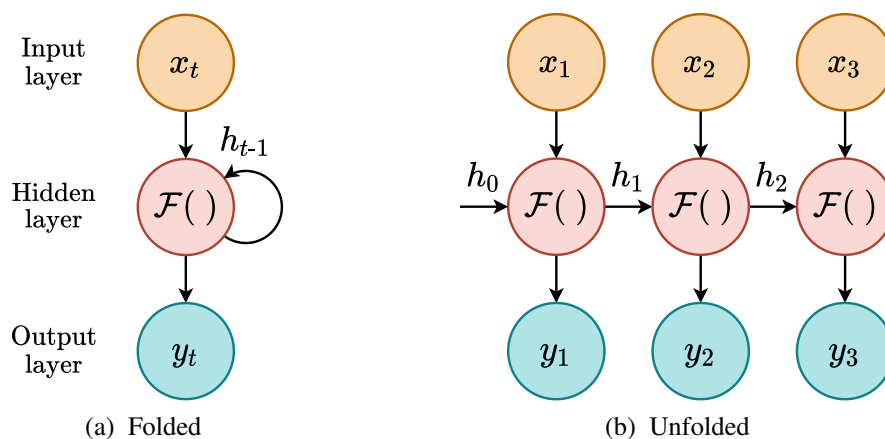


Figure 2.1: Folded schematic RNN with a single hidden layer that feeds the previous h_{t-1} (or initial h_0) state back to the inference at the current time step t and its time-unfolded representation when processing the input of a time-series consisting of the three data points $(x_i)_{i \in \{1,2,3\}}$.

In 1997, Hochreiter and Schmidhuber [21] introduced the long short-term memory

(LSTM), which is today's predominant [54] RNN variant. A standard LSTM layer (see, e.g., the PyTorch implementation²) recurrently maintains a cell and a hidden state. This means that, in addition to the current data point of the input sequence, the layer re-inputs the fed back cell and hidden state from the previous sequential step. Furthermore, the LSTM layer implements three gating mechanism that control the information flow within the layer. A gating mechanism is basically the Hadamard product of a state and a gate, which is a vector whose entries are within the interval from zero to one. Consequently, a gate applied on a state, controls the flow of the elements of the state within the range from zero to full flow. The forget gate of the LSTM layer controls the flow from the previous to the current cell state. The input gate controls the flow from the previous hidden state and the current data point of the input sequence to the current cell state. And the output gate controls the flow from the current cell state to current hidden state. By this design of recurrent states with gated information flow, the training of the LSTM is essentially robust to the vanishing gradient problem [45]. As a result, the LSTM is, compared to standard RNNs, essentially more capable of learning to remember long-term dependencies within input sequences.

The GRU, which was proposed 17 years after the LSTM by Cho et al. [8], can be seen as a lighter version of the LSTM. It refrains from the cell state and therewith the output gate of the LSTM and maintains only a hidden state and two gating mechanisms. Therewith, the GRU has less trainable parameters than the LSTM and is less memory efficient during inference. Nevertheless, it preserves the robustness with respect to the vanishing gradient problem that affects most standard RNNs [23]. Various empirical studies show that the GRU, compared to the LSTM, performs equally well or even slightly better. Greff et al. [17] evaluated the "vanilla" LSTM and the GRU, among other LSTM variants, on speech and handwritten text recognition as well as music representation and could not detect substantial differences in performance. Chung et al. [9] applied LSTM and GRU on raw speech and polyphonic music data and empirically observed that both performed equally well. In the comparative study of Yin et al. [59], the GRU slightly outperforms the LSTM on five of seven natural language processing tasks. In the field of algorithm learning, Kaiser and Sutskever [27] achieved notably better results with a network based on GRU than with a network based on LSTM. In consideration of these findings and the fact that the GRU has less trainable parameters and occupies less memory during inference, the GRU is chosen over the LSTM for the deployment in the ANN module of the autonomous navigation method of this thesis.

Inference

The following presents the mathematics of a single GRU layer during inference in ac-

²<https://pytorch.org/docs/stable/generated/torch.nn.LSTM.html>, visited on 03/07/2022

cordance with the PyTorch implementation³. This includes the GRU layer's two gating mechanisms as well as its computations of the candidate and the hidden state.

Without loss of generality, let the sequential data to be processed by the GRU layer be a batch of time series of data points

$$\left(\underline{x}_t \in \mathbb{R}^{N^{\text{in}}} \right)_{t \in \{1, \dots, N^{\text{seq}}\}, i}, \quad i \in \{1, \dots, N^{\text{batch}}\} \quad (2.13)$$

with the batch size N^{batch} , the sequence length N^{seq} and the dimensionality N^{in} of the data points. Let the initial batch of hidden states be

$$\underline{h}_{0,i} \in [-1, 1]^{N^{\text{hidden}}}, \quad i \in \{1, \dots, N^{\text{batch}}\} \quad (2.14)$$

with the dimensionality N^{hidden} of the hidden state, which is a design parameter of the GRU layer. The values of the initial hidden states $\underline{h}_{0,i}$, are typically initialized with zeros or noise [63] but can also be learned by the network, e.g., [15]. The GRU layer processes the time series included in the batch parallelly and the data points of the individual time series successively. At the current time step t , the layer's input consists of the batch of the current data points and the fed back batch of previously outputted, hidden states

$$(\underline{x}_{t,i}, \underline{h}_{t-1,i}), \quad i \in \{1, \dots, N^{\text{batch}}\}. \quad (2.15)$$

For reasons of simplification, the following text only refers to the parallelly computed, individual elements of the processed batch. However, the following equations yet explicitly refer to the entire batch.

At every incoming input, the GRU layer at first computes its two gates. The current reset gate

$$\underline{g}_{t,i}^r = \mathcal{F}^r(\underline{x}_{t,i}, \underline{h}_{t-1,i}), \quad i \in \{1, \dots, N^{\text{batch}}\} \quad (2.16)$$

is obtained by the mapping

$$\begin{aligned} \mathcal{F}^r : \left(\mathbb{R}^{N^{\text{in}}}, [-1, 1]^{N^{\text{hidden}}} \right) &\rightarrow [0, 1]^{N^{\text{hidden}}} \\ (\underline{x}, \underline{h}) &\mapsto \sigma \left(\underline{A}_x^r \underline{x} + \underline{b}_x^r + \underline{A}_h^r \underline{h} + \underline{b}_h^r \right). \end{aligned} \quad (2.17)$$

The above mapping to the reset gate can be divided into two steps. First, the current data point and the previous hidden state are linearly transformed with the corresponding matrices of trainable weights and vectors of trainable biases

$$\begin{aligned} \underline{A}_x^r &\in \mathbb{R}^{N^{\text{hidden}} \times N^{\text{in}}}, & \underline{b}_x^r &\in \mathbb{R}^{N^{\text{hidden}}}, \\ \underline{A}_h^r &\in \mathbb{R}^{N^{\text{hidden}} \times N^{\text{hidden}}}, & \underline{b}_h^r &\in \mathbb{R}^{N^{\text{hidden}}}. \end{aligned} \quad (2.18)$$

³<https://pytorch.org/docs/stable/generated/torch.nn.GRU.html>, visited on 09/07/2022

The user has the design option to disable all biases of the GRU layer. This is tantamount to set the above and the still upcoming biases of the layer to zero and consider them not trainable. Second, the standard sigmoid function [18] (see figure 2.2)

$$\sigma : \mathbb{R} \rightarrow [0, 1]; x \mapsto \frac{1}{1 + e^{-x}} \quad (2.19)$$

is applied element-wise (denoted with the accent \odot) on the sum of these two linear transformations. The sigmoid function forces the values of the reset gate to be in the interval between zero and one. This is characteristic for a gating mechanism since the gating of a state, which is in fact the calculation of the Hadamard product of the state and the gate, targets at only damping not amplifying or reversing the individual values of the state.

The current update gate

$$\underline{g}_{t,i}^u = \mathcal{F}^u(\underline{x}_{t,i}, \underline{h}_{t-1,i}), \quad i \in \{1, \dots, N^{\text{batch}}\} \quad (2.20)$$

is obtained with the mapping

$$\begin{aligned} \mathcal{F}^u : (\mathbb{R}^{N^{\text{in}}}, [-1, 1]^{N^{\text{hidden}}}) &\rightarrow [0, 1]^{N^{\text{hidden}}} \\ (\underline{x}, \underline{h}) &\mapsto \sigma \left(\underline{A}_x^u \underline{x} + \underline{b}_x^u + \underline{A}_h^u \underline{h} + \underline{b}_h^u \right). \end{aligned} \quad (2.21)$$

The above mapping to the update gate differs from the mapping to the reset gate only in the fact that the occurring linear transformations rely on their separate, trainable weights and biases

$$\begin{aligned} \underline{A}_x^u &\in \mathbb{R}^{N^{\text{hidden}} \times N^{\text{in}}}, & \underline{b}_x^u &\in \mathbb{R}^{N^{\text{hidden}}}, \\ \underline{A}_h^u &\in \mathbb{R}^{N^{\text{hidden}} \times N^{\text{hidden}}}, & \underline{b}_h^u &\in \mathbb{R}^{N^{\text{hidden}}}. \end{aligned} \quad (2.22)$$

With the knowledge of the current reset gate, the GRU layer calculates the candidate for the current hidden state, hereinafter referred to as candidate state

$$\underline{h}_{t,i}^c = \mathcal{F}^c(\underline{x}_{t,i}, \underline{h}_{t-1,i}), \quad i \in \{1, \dots, N^{\text{batch}}\}. \quad (2.23)$$

The mapping to the candidate state

$$\begin{aligned} \mathcal{F}^c : (\mathbb{R}^{N^{\text{in}}}, [-1, 1]^{N^{\text{hidden}}}) &\rightarrow [-1, 1]^{N^{\text{hidden}}} \\ (\underline{x}, \underline{h}) &\mapsto \tanh \left[\underline{A}_x^c \underline{x} + \underline{b}_x^c + \mathcal{F}^r(\underline{x}, \underline{h}) \odot \left(\underline{A}_h^c \underline{h} + \underline{b}_h^c \right) \right] \end{aligned} \quad (2.24)$$

contains the trainable weight matrices and bias vectors

$$\begin{aligned} \underline{A}_x^c &\in \mathbb{R}^{N^{\text{hidden}} \times N^{\text{in}}}, & \underline{b}_x^c &\in \mathbb{R}^{N^{\text{hidden}}}, \\ \underline{A}_h^c &\in \mathbb{R}^{N^{\text{hidden}} \times N^{\text{hidden}}}, & \underline{b}_h^c &\in \mathbb{R}^{N^{\text{hidden}}}. \end{aligned} \quad (2.25)$$

The above mapping to the candidate state resembles the mappings to the reset and update gate by subjecting the current data point and the previous hidden state to a separate, biased linear transformation. It differs in two aspects. First, before the two transformations are added together, the current reset gate is applied on the transformed, previous hidden state (\odot denotes the Hadamard product). The function of the reset gate is, consequently, to mitigate the contribution of the previous hidden state to the candidate state. Second, instead of the sigmoid function, the hyperbolic tangent [50] (see figure 2.2)

$$\tanh : \mathbb{R} \rightarrow [-1, 1]; x \mapsto \frac{e^x - e^{-x}}{e^x + e^{-x}} \quad (2.26)$$

is applied element-wise on the sum of the linearly transformed data point and the gated, linearly transformed, previous hidden state. The hyperbolic tangent bounds the values of the candidate state to the interval from minus to plus one.

Finally, the GRU layer computes the current hidden state

$$h_{t,i} = \mathcal{F}^h(\underline{x}_{t,i}, \underline{h}_{t-1,i}), \quad i \in \{1, \dots, N^{\text{batch}}\} \quad (2.27)$$

on the basis of the mapping

$$\begin{aligned} \mathcal{F}^h : \left(\mathbb{R}^{N^{\text{in}}}, [-1, 1]^{N^{\text{hidden}}} \right) &\rightarrow [-1, 1]^{N^{\text{hidden}}} \\ \chi := (\underline{x}, \underline{h}) &\mapsto [\underline{1} - \mathcal{F}^u(\chi)] \odot \mathcal{F}^c(\chi) + \mathcal{F}^u(\chi) \odot \underline{h}. \end{aligned} \quad (2.28)$$

The above mapping to the hidden state is basically a weighted arithmetic mean. Before the previous hidden state and the current candidate state are averaged, they are weighted by the current update gate and counter-update gate, respectively. In other words, the update gate, whose values are between zero and one, controls the element-wise percentage proportions of both states on the current hidden state. Due to the fact that the hyperbolic tangent normalizes the elements of the candidate state to the interval from minus to plus one (equation 2.24) and the values of the initial hidden state are typically initialized to be also within this interval (equation 2.14), the values of the current hidden state are also bounded to the interval from minus to plus one.

Backpropagation through time

The following presents the application of backpropagation through time on a single integrated GRU layer operating in many-to-one mode in order to calculate the gradients of the loss with respect to the GRU layer's trainable parameters. During training, these gradients are required by gradient-based methods which update the trainable parameters with the target to minimize the loss.

Let a single GRU layer, integrated into any superior ANN, operate in many-to-one mode. With biases enabled, the set of all structures that contain trainable parameters of

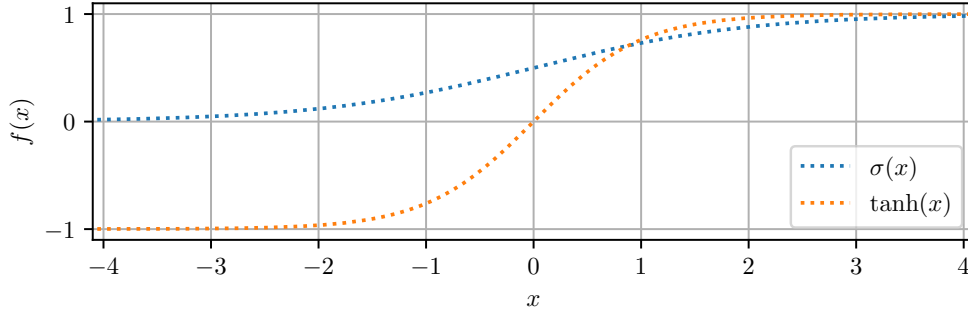


Figure 2.2: The non-linear activation functions deployed within a standard GRU. The standard sigmoid function $\sigma(x) = (1 + e^{-x})^{-1}$ normalizes the values of the reset and update gate to the interval from zero to one (equation 2.17 and 2.21). The hyperbolic tangent $\tanh(x) = (e^x - e^{-x}) / (e^x + e^{-x})$ normalizes the values of the candidate and, consequently, the hidden state to the interval from minus to plus one (equation 2.24 and 2.28).

the GRU layer is aggregated from equation 2.18, 2.22 and 2.25

$$\Theta = \left\{ \underline{A}_x^r, \underline{b}_x^r, \underline{A}_h^r, \underline{b}_h^r, \underline{A}_x^u, \underline{b}_x^u, \underline{A}_h^u, \underline{b}_h^u, \underline{A}_x^c, \underline{b}_x^c, \underline{A}_h^c, \underline{b}_h^c \right\}. \quad (2.29)$$

The addition of the sizes of the structures in the set Θ yields the total number of trainable parameters of the GRU layer

$$N^{\text{param}} = \begin{cases} 3N^{\text{hidden}} (N^{\text{in}} + N^{\text{hidden}} + 2), & \text{if biases enabled} \\ 3N^{\text{hidden}} (N^{\text{in}} + N^{\text{hidden}}), & \text{else.} \end{cases} \quad (2.30)$$

At a single inference, the GRU layer receives a batch of sequences of feature vectors from the previous layer of the ANN

$$(\underline{x}_t)_{t \in \{1, \dots, N^{\text{seq}}\}, i}, \quad i \in \{1, \dots, N^{\text{batch}}\}. \quad (2.31)$$

The GRU layer in many-to-one mode maps each incoming batch of sequences to a batch of single outputs, whereby a single output is the hidden state lastly inferred from a sequence

$$\underline{y}_i = \underline{h}_{N^{\text{seq}}, i}, \quad i \in \{1, \dots, N^{\text{batch}}\}. \quad (2.32)$$

The time-unfolded computation graph of the integrated GRU layer for a single batch element is shown in figure 2.3. The batches of single GRU outputs are forwarded to the subsequent layer of the ANN. Whenever a batch has passed all the output layer of the ANN, the loss L of the batch is computed by averaging the losses of the individual

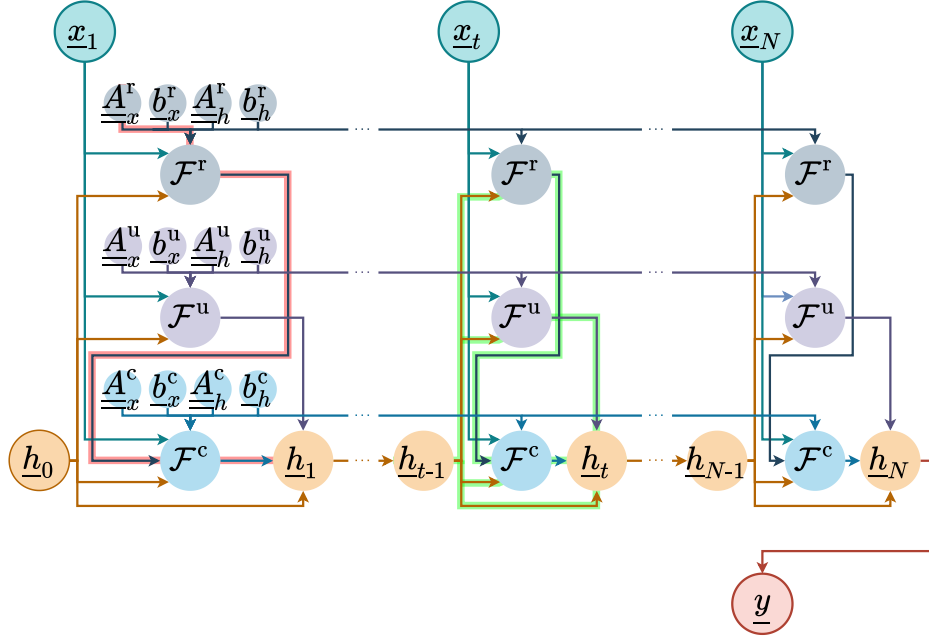


Figure 2.3: Time-unfolded computation graph of a GRU layer operating in many-to-one mode. The input sequence $(x_t)_{t \in \{1, \dots, N\}}$ is mapped to the single output y which is equal to the lastly inferred, hidden state \underline{h}_N . Equation 2.17, 2.21 and 2.24 define the mapping to the reset gate \mathcal{F}^r , update gate \mathcal{F}^u and candidate state \mathcal{F}^c , respectively. The hidden states $(h_t)_{t \in \{1, \dots, N\}}$ are obtained with the mapping \mathcal{F}^h defined by equation 2.28 whereas the initial hidden state \underline{h}_0 (equation 2.14) is defined by the user. The trainable parameters $\underline{A}_{\square}^{\square}, \underline{b}_{\square}^{\square}$ of the GRU layer are shared across all unfolded time steps. The backpropagation path of the intra-gradient with respect to $\underline{A}_{\square}^{\square}$ (equation 2.36) is highlighted in red for the first time step $t = 1$. The backpropagation paths of the inter-gradient (equation 2.39) is highlighted in green for the time step t .

elements of the batch. Because the separate losses depend on their corresponding single GRU output, the loss of the batch is a function of all of these outputs.

$$L(\underline{y}_1, \dots, \underline{y}_{N^{\text{batch}}}) = \frac{1}{N^{\text{batch}}} \sum_{i=1}^{N^{\text{batch}}} L_i(\underline{y}_i). \quad (2.33)$$

Gradient-based methods update the trainable parameters of the ANN with the goal to minimize the loss of the batch. For this, they require the knowledge of the gradients of the loss with respect to the trainable parameters. The update of the trainable parameters of the integrated GRU layer complies with

$$\underset{\Theta}{\operatorname{argmin}} L(\underline{y}_1, \dots, \underline{y}_{N^{\text{batch}}}). \quad (2.34)$$

In conformity with Li [32], the gradient of the batch loss with respect to a single element $\theta \in \Theta$ of the set of structures containing trainable parameters (equation 2.29) is computed based on backpropagation through time

$$\begin{aligned} & \frac{\partial}{\partial \theta} L(\underline{y}_1, \dots, \underline{y}_{N^{\text{batch}}}) \\ & \stackrel{(1)}{=} \frac{1}{N^{\text{batch}}} \sum_{i=1}^{N^{\text{batch}}} \frac{\partial}{\partial \theta} L_i(\underline{y}_i) \\ & \stackrel{(2)}{=} \frac{1}{N^{\text{batch}}} \sum_{i=1}^{N^{\text{batch}}} \left(\frac{\partial L_i}{\partial \underline{y}_i} \frac{\partial \underline{y}_i}{\partial \theta} \right) \\ & \stackrel{(3)}{=} \frac{1}{N^{\text{batch}}} \sum_{i=1}^{N^{\text{batch}}} \left[\frac{\partial L_i}{\partial \underline{y}_i} \sum_{j=1}^{N^{\text{seq}}} \left(\frac{\partial \underline{y}_i}{\partial \underline{h}_{j,i}} \widehat{\frac{\partial \underline{h}_{j,i}}{\partial \theta}} \right) \right] \\ & \stackrel{(4)}{=} \frac{1}{N^{\text{batch}}} \sum_{i=1}^{N^{\text{batch}}} \left\{ \frac{\partial L_i}{\partial \underline{y}_i} \sum_{j=1}^{N^{\text{seq}}} \left[\prod_{k=j+1}^{N^{\text{seq}}} \left(\frac{\partial \underline{h}_{k,i}}{\partial \underline{h}_{k-1,i}} \right) \widehat{\frac{\partial \underline{h}_{j,i}}{\partial \theta}} \right] \right\}. \end{aligned} \quad (2.35)$$

(1) Loss of a batch (equ. 2.33)

(2) Chain rule

(3) Backpropagation through time (gradient $\widehat{}$ considers previous hidden states constant)

(4) Many-to-one output (equ. 2.32); chain rule applied on $\partial \underline{y}_i / \partial \underline{h}_{j,i}$

In the above formula, the gradient $\widehat{\partial \underline{h}_{j,i} / \partial \theta}$, hereinafter referred to as intra-gradient, treats all previous hidden states $\underline{h}_{\tilde{j}, \dots, i}$, $\tilde{j} \in \{0, j-1\}$ as constants. In doing so, the intra-gradient only covers the backpropagation path from the hidden state $\underline{h}_{j,i}$ to the parameter structure θ within the same time step j . In order to compute the full gradient covering all

backpropagation paths to θ , all intra-backpropagation paths are connected through time to the GRU layer's output \underline{y}_i by multiplying the intra-gradients with their corresponding chain of time step inter-gradients $\partial \underline{h}_{k,i} / \partial \underline{h}_{k-1,i}$. For demonstration purposes, the intra-gradient with respect to $\theta = \underline{A}_x^r$ (the corresponding backpropagation path is highlighted for the first time step in figure 2.3) is exemplarily derived as

$$\begin{aligned} \widehat{\frac{\partial \underline{h}_{t,i}}{\partial \underline{A}_x^r}} &\stackrel{(1)}{=} \widehat{\frac{\partial}{\partial \underline{A}_x^r}} \{ [\underline{1} - \mathcal{F}^u(\chi)] \odot \mathcal{F}^c(\chi) + \mathcal{F}^u(\chi) \odot \underline{h}_{t-1,i} \} \\ &\stackrel{(2)}{=} \text{diag} [\underline{1} - \mathcal{F}^u(\chi)] \frac{\widehat{\frac{\partial \mathcal{F}^c(\chi)}{\partial \underline{A}_x^r}}}{\partial \underline{A}_x^r} \end{aligned} \quad (2.36)$$

(1) Mapping to hidden state (equ. 2.27, 2.28); $\chi := (\underline{x}_{t,i}, \underline{h}_{t-1,i})$

(2) Sum rule of differentiation;

Mapping to update gate (equ. 2.21): $\partial \mathcal{F}^u / \partial \underline{A}_x^r = 0$

Consider previous hidden states constant: $\partial \underline{h}_{t-1,i} / \partial \underline{A}_x^r = 0$;

Hadamard product of two vectors (equ. 2.45)

with

$$\begin{aligned} \widehat{\frac{\partial \mathcal{F}^c(\chi)}{\partial \underline{A}_x^r}} &\stackrel{(1)}{=} \widehat{\frac{\partial}{\partial \underline{A}_x^r}} \left\{ \tanh \left[\underbrace{\underline{A}_x^c \underline{x}_{t,i} + \underline{b}_x^c + \mathcal{F}^r(\underline{x}_{t,i}, \underline{h}_{t-1,i}) \odot (\underline{A}_h^c \underline{h}_{t-1,i} + \underline{b}_h^c)}_{:=\chi^c} \right] \right\} \\ &\stackrel{(2)}{=} \text{diag} \left[\frac{\partial}{\partial \chi^c} \tanh(\chi^c) \right] \cdot \widehat{\frac{\partial \chi^c}{\partial \underline{A}_x^r}} \\ &\stackrel{(3)}{=} \text{diag} \left[1 - \tanh^2(\chi^c) \right] \cdot \text{diag} \left(\underline{A}_h^c \underline{h}_{t-1,i} + \underline{b}_h^c \right) \frac{\partial \mathcal{F}^r(\underline{x}_{t,i}, \underline{h}_{t-1,i})}{\partial \underline{A}_x^r} \end{aligned} \quad (2.37)$$

(1) Mapping to candidate state (equ. 2.24); $\chi := (\underline{x}_{t,i}, \underline{h}_{t-1,i})$

(2) Chain rule of differentiation;

Derivative of function applied element-wise on vector (equ. 2.47)

(3) Derivative of hyperbolic tangent (equ. 2.43);

Hadamard product of two vectors (equ. 2.45)

and

$$\begin{aligned}
\frac{\partial \mathcal{F}^r(\underline{x}_{t,i}, \underline{h}_{t-1,i})}{\partial \underline{A}_x^r} &\stackrel{(1)}{=} \frac{\widehat{\partial}}{\partial \underline{A}_x^r} \left[\overset{\circ}{\sigma} \left(\underbrace{\underline{A}_x^r \underline{x}_{t,i} + \underline{b}_x^r + \underline{A}_h^r \underline{h}_{t-1,i} + \underline{b}_h^r}_{:=\chi^r} \right) \right] \\
&\stackrel{(2)}{=} \text{diag} \left[\frac{\partial}{\partial \chi^r} \overset{\circ}{\sigma}(\chi^r) \right] \cdot \frac{\widehat{\partial \chi^u}}{\partial \underline{A}_x^r} \\
&\stackrel{(3)}{=} \text{diag} \left\{ \overset{\circ}{\sigma}(\chi^r) \odot [1 - \overset{\circ}{\sigma}(\chi^r)] \right\} \cdot \frac{\partial \underline{A}_x^r \underline{x}_{t,i}}{\partial \underline{A}_x^r}. \tag{2.38}
\end{aligned}$$

(1) Mapping to reset gate (equ. 2.17)

(2) Chain rule of differentiation;

Derivative of function applied element-wise on vector (equ. 2.47)

(3) Derivative of sigmoid function (equ. 2.44)

For the computation of the gradient $\partial (\underline{A}_x^r \underline{x}_{t,i}) / \partial \underline{A}_x^r$, which is a 3-dimensional matrix whose information content is only 2-dimensional, refer to [31], for example.

The in equation 2.35 required inter-gradient (the corresponding backpropagation path is highlighted in figure 2.3) , i.e., the gradient of the current hidden state with respect to the previous hidden state, is derived as

$$\begin{aligned}
\frac{\partial \underline{h}_{t,i}}{\partial \underline{h}_{t-1,i}} &\stackrel{(1)}{=} \frac{\partial}{\partial \underline{h}_{t-1,i}} \{ [1 - \mathcal{F}^u(\chi)] \odot \mathcal{F}^c(\chi) + \mathcal{F}^u(\chi) \odot \underline{h}_{t-1,i} \} \\
&\stackrel{(2)}{=} \frac{\partial}{\partial \underline{h}_{t-1,i}} \{ [1 - \mathcal{F}^u(\chi)] \odot \mathcal{F}^c(\chi) \} + \frac{\partial}{\partial \underline{h}_{t-1,i}} \{ \mathcal{F}^u(\chi) \odot \underline{h}_{t-1,i} \} \\
&\stackrel{(3)}{=} -\text{diag}[\mathcal{F}^c(\chi)] \frac{\partial \mathcal{F}^u(\chi)}{\partial \underline{h}_{t-1,i}} + \text{diag}[1 - \mathcal{F}^u(\chi)] \frac{\partial \mathcal{F}^c(\chi)}{\partial \underline{h}_{t-1,i}} \\
&\quad + \text{diag}(\underline{h}_{t-1,i}) \frac{\partial \mathcal{F}^u(\chi)}{\partial \underline{h}_{t-1,i}} + \text{diag}[\mathcal{F}^u(\chi)]. \tag{2.39}
\end{aligned}$$

(1) Mapping to current hidden state (equ. 2.27, 2.28); $\chi := (\underline{x}_{t,i}, \underline{h}_{t-1,i})$

(2) Sum rule of differentiation

(3) Differentiation of Hadamard product of two vectors (equ. 2.46)

The in equation 2.39 required gradient of the current update gate with respect to the

previous hidden state is derived as

$$\begin{aligned}
\frac{\partial \mathcal{F}^u(x_{t,i}, \underline{h}_{t-1,i})}{\partial \underline{h}_{t-1,i}} &\stackrel{(1)}{=} \frac{\partial}{\partial \underline{h}_{t-1,i}} \left[\overset{\odot}{\sigma} \left(\underbrace{\underline{A}_x^u x_{t,i} + \underline{b}_x^u + \underline{A}_h^u \underline{h}_{t-1,i} + \underline{b}_h^u}_{:=\chi^u} \right) \right] \\
&\stackrel{(2)}{=} \text{diag} \left[\frac{\partial}{\partial \chi^u} \overset{\odot}{\sigma}(\chi^u) \right] \cdot \frac{\partial}{\partial \underline{h}_{t-1,i}} \chi^u \\
&\stackrel{(3)}{=} \text{diag} \left\{ \overset{\odot}{\sigma}(\chi^u) \odot \left[1 - \overset{\odot}{\sigma}(\chi^u) \right] \right\} \cdot \underline{A}_h^u. \tag{2.40}
\end{aligned}$$

(1) Mapping to update gate (equ. 2.21)

(2) Chain rule of differentiation;

Derivative of function applied element-wise on vector (equ. 2.47)

(3) Derivative of sigmoid function (equ. 2.44)

The in equation 2.39 required gradient of the current candidate state with respect to the previous hidden state is derived as

$$\begin{aligned}
&\frac{\partial}{\partial \underline{h}_{t-1,i}} \mathcal{F}^c(x_{t,i}, \underline{h}_{t-1,i}) \\
&\stackrel{(1)}{=} \frac{\partial}{\partial \underline{h}_{t-1,i}} \left\{ \tanh \left[\underbrace{\underline{A}_x^c x_{t,i} + \underline{b}_x^c + \mathcal{F}^r(x_{t,i}, \underline{h}_{t-1,i}) \odot (\underline{A}_h^c \underline{h}_{t-1,i} + \underline{b}_h^c)}_{:=\chi^c} \right] \right\} \\
&\stackrel{(2)}{=} \text{diag} \left[\frac{\partial}{\partial \chi^c} \tanh(\chi^c) \right] \cdot \frac{\partial}{\partial \underline{h}_{t-1,i}} \chi^c \\
&\stackrel{(3)}{=} \text{diag} \left[1 - \tanh^2(\chi^c) \right] \\
&\quad \cdot \left\{ \text{diag} \left(\underline{A}_h^c \underline{h}_{t-1,i} + \underline{b}_h^c \right) \frac{\partial \mathcal{F}^r(x_{t,i}, \underline{h}_{t-1,i})}{\partial \underline{h}_{t-1,i}} + \text{diag} [\mathcal{F}^r(x_{t,i}, \underline{h}_{t-1,i})] \underline{A}_h^c \right\}. \tag{2.41}
\end{aligned}$$

(1) Mapping to candidate state (equ. 2.24)

(2) Chain rule of differentiation;

Derivative of function applied element-wise on vector (equ. 2.47)

(3) Derivative of hyperbolic tangent (equ. 2.43);

Differentiation of Hadamard product of two vectors (equ. 2.46)

The in equation 2.41 required gradient of the current reset gate with respect to the previous hidden state shares the same structure with the gradient of equation 2.40 and is

hence derived as

$$\frac{\partial}{\partial \underline{h}_{t-1,i}} \mathcal{F}^r(\underline{x}_{t,i}, \underline{h}_{t-1,i}) = \text{diag} \left\{ \overset{\circ}{\sigma}(\chi^r) \odot \left[1 - \overset{\circ}{\sigma}(\chi^r) \right] \right\} \cdot \underline{\underline{A}}_h^r$$

with $\chi^r := \underline{\underline{A}}_x^r \underline{x}_{t,i} + \underline{b}_x^r + \underline{\underline{A}}_h^r \underline{h}_{t-1,i} + \underline{b}_h^r$. (2.42)

The above derivations revert to the following equations. Equations (4.5.73) and (4.5.17) of Abramowitz and Stegun [50] yield the derivative of the hyperbolic tangent as

$$\frac{d}{dx} \tanh(x) = 1 - \tanh^2(x). \quad (2.43)$$

The derivative of the sigmoid function (e.g., [39]) is given by

$$\frac{d}{dx} \sigma(x) = \sigma(x) [1 - \sigma(x)]. \quad (2.44)$$

The hadamard product of two vectors can be reformulated as the matrix product of a diagonal matrix and a vector [6]

$$\underline{x}_1 \odot \underline{x}_2 = \text{diag}(\underline{x}_1) \underline{x}_2 = \text{diag}(\underline{x}_2) \underline{x}_1. \quad (2.45)$$

Together with the product rule of differentiation, the derivative of the Hadamard product of two vectors is therewith identified as

$$\frac{\partial}{\partial t} (\underline{x}_1 \odot \underline{x}_2) = \text{diag}(\underline{x}_2) \frac{\partial \underline{x}_1}{\partial t} + \text{diag}(\underline{x}_1) \frac{\partial \underline{x}_2}{\partial t}. \quad (2.46)$$

The derivative of a function $f : \mathbb{R} \rightarrow \mathbb{R}$, that is applied element-wise on a vector \underline{x} , is the diagonal matrix built from the derivative of the function applied element-wise on the vector

$$\frac{\partial}{\partial \underline{x}} \overset{\circ}{f}(\underline{x}) = \text{diag} \left[\overset{\circ}{f}'(\underline{x}) \right]. \quad (2.47)$$

The above statement can be derived from the calculation of the differential of the function

$$\frac{d}{d\underline{x}} \overset{\circ}{f}(\underline{x}) \cdot d\underline{x} \stackrel{(1)}{=} d\overset{\circ}{f}(\underline{x}) \stackrel{(2)}{=} \left[\overset{\circ}{f}'(\underline{x}) \right] \odot d\underline{x} \stackrel{(3)}{=} \text{diag} \left[\overset{\circ}{f}'(\underline{x}) \right] \cdot d\underline{x}. \quad (2.48)$$

(1) Relation of differential and derivative

(2) Chain rule element-wise applied

(3) Hadamard product of two vectors (equ. 2.45) (2.49)

Chapter 3

Autonomous Navigation Method

DELETEME: In this chapter you start addressing your actual problem. Therefore, it makes often sense to make a detailed problem analysis first (if not done in introduction). You should be sure about what to do and how. As writtin in the background part, it might also make sense to include complex background information or papers you are basing on in this analysis. If you are solving a software problem, you should follow the state of the art of software development which basically includes: problem analysis, design, implementation, testing, and deployment. Maintenance is often also described but I believe this will not be required for most theses. Code should be placed in the appendix unless it is solving an essential aspect of your work.

In order to investigate the effect of temporal comprehension in machine-learning-based, autonomous navigation of drones, this master thesis extends the navigation method of Kaufmann, Loquercio et. al [?] is minimally adjusted and extended with a recurrent convolutional neural network. This chapter ...

3.1 Reference systems

In this thesis, the coordinates of a point \underline{p} relate to either the global, the local or the image reference system

$$\mathbf{G}\underline{p} = \begin{bmatrix} \mathbf{G}^x \\ \mathbf{G}^y \\ \mathbf{G}^z \end{bmatrix} \in \mathbb{R}^3, \quad \mathbf{L}\underline{p} = \begin{bmatrix} \mathbf{L}^x \\ \mathbf{L}^y \\ \mathbf{L}^z \end{bmatrix} \in \mathbb{R}^3, \quad \mathbf{I}\underline{p} = \begin{bmatrix} \mathbf{I}^x \\ \mathbf{I}^y \end{bmatrix} \in [-1, 1]^2. \quad (3.1)$$

The 3D global reference system is fixed to an arbitrary point on earth and is hence quasi inertial. It is spanned by the orthonormal basis which, related to the global refer-

ence system, equates to the standard basis of \mathbb{R}^3

$$\{\underline{e}_x^G, \underline{e}_y^G, \underline{e}_z^G\} \quad \text{with} \quad \mathbf{G}\underline{e}_x^G = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, \quad \mathbf{G}\underline{e}_y^G = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}, \quad \mathbf{G}\underline{e}_z^G = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}. \quad (3.2)$$

The local reference system (see figure 3.1a) is fixed to the moving drone. It is spanned by the orthonormal basis, whose origin is located at the optical center of the drone's onboard camera,

$$\{\underline{e}_x^L, \underline{e}_y^L, \underline{e}_z^L\} \quad \text{with} \quad \mathbf{L}\underline{e}_x^L = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, \quad \mathbf{L}\underline{e}_y^L = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}, \quad \mathbf{L}\underline{e}_z^L = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}. \quad (3.3)$$

The unit vector \underline{e}_x^L points along the optical axis of the camera in the flight direction of the drone. The unit vector \underline{e}_z^L points in the direction of the forces generated by the drone's rotors and is parallel to the vertical axis of the image plane of the drone's onboard camera. The unit vector \underline{e}_y^L points to the left of the drone and parallels the horizontal axis of the image plane.

The image reference system (see figure 3.1b) is superimposed on the images of the drone's onboard camera. This 2-dimensional system is spanned by the orthonormal basis

$$\{\underline{e}_x^I, \underline{e}_y^I\} \quad \text{with} \quad \mathbf{I}\underline{e}_x^I = \begin{bmatrix} 1 \\ 0 \end{bmatrix}, \quad \mathbf{I}\underline{e}_y^I = \begin{bmatrix} 0 \\ 1 \end{bmatrix}. \quad (3.4)$$

The origin of the image reference system is located at the center of the image plane. The unit vector \underline{e}_x^I points rightwards along the vertical axis of the image plane. The unit vector \underline{e}_y^I points upwards along the horizontal axis of the image plane. A point on the image plane is bounded by the left and right $-1 \leq \mathbf{I}x \leq 1$ as well as the lower and upper $-1 \leq \mathbf{I}y \leq 1$ border of the image plane.

Transformation between the global and the local reference system

The drone's position $\mathbf{G}\underline{p}^d$ and quaternion orientation $\mathbf{G}\underline{q}^d$ with respect to the global reference system are the parameters that determine the bidirectional transformation between the global and the local reference system. The following bases on quaternion mathematics, for which one can consult, e.g., [44]. A point given in the coordinates of the global reference system can be expressed in the coordinates of the local reference system with the transformation

$$T_{\mathbf{LG}} : \mathbb{R}^3 \rightarrow \mathbb{R}^3; \quad \mathbf{G}\underline{p} \mapsto \mathbf{L}\underline{p} = \mathcal{P} \left[\text{inv} \left(\mathbf{G}\underline{q}^d \right) * \mathcal{Q} \left(\mathbf{G}\underline{p} - \mathbf{G}\underline{p}^d \right) * \mathbf{G}\underline{q}^d \right], \quad (3.5)$$

Reversely, a point given in the coordinates of the local reference system can be expressed in the coordinates of the global reference system with the transformation

$$T_{\mathbf{GL}} : \mathbb{R}^3 \rightarrow \mathbb{R}^3; \quad \mathbf{L}\underline{p} \mapsto \mathbf{G}\underline{p} = \mathcal{P} \left[\mathbf{G}\underline{q}^d * \mathcal{Q} \left(\mathbf{L}\underline{p} \right) * \text{inv} \left(\mathbf{G}\underline{q}^d \right) \right] + \mathbf{G}\underline{p}^d, \quad (3.6)$$

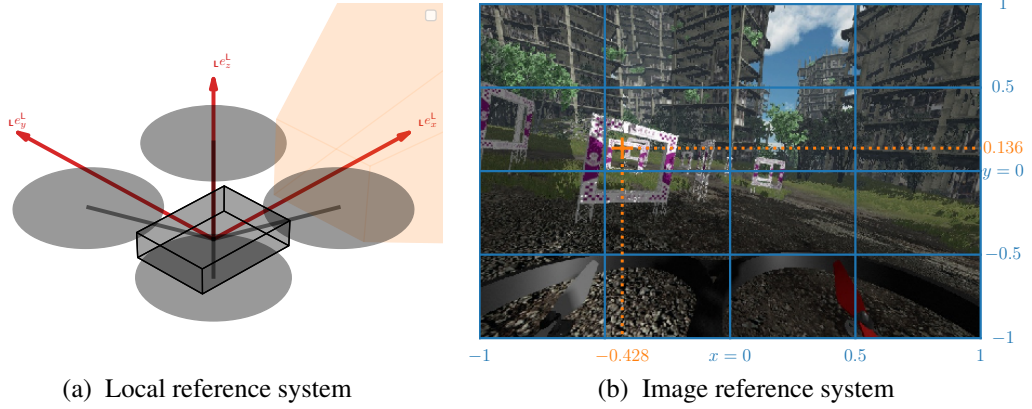


Figure 3.1: The local and the image reference system. The local reference system (red) is aligned with the drone's onboard camera. The image reference system (blue) is superimposed on the images from the onboard camera. The pictured, exemplary waypoint $\underline{p}^{\text{wp}} = [-0.428 \ 0.136]^T$ (orange) with respect to the image reference system is part of the label for the underlying image.

In the two above transformations, the mapping \mathcal{Q} of a point to its quaternion representation and the reverse mapping \mathcal{P} of a quaternion representation to its point are given by

$$\begin{aligned} \mathcal{Q} : \mathbb{R}^3 &\rightarrow \mathbb{R}^4; \underline{p} = \begin{bmatrix} x \\ y \\ z \end{bmatrix} \mapsto \underline{q} = \begin{bmatrix} w \\ \underline{p} \end{bmatrix} \text{ with } w = 0 \\ \mathcal{P} : \mathbb{R}^4 &\rightarrow \mathbb{R}^3; \underline{q} = \begin{bmatrix} w \\ \underline{p} \end{bmatrix} \mapsto \underline{p} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}. \end{aligned} \quad (3.7)$$

Moreover, the operator $*$ denotes the multiplication of two quaternions which is given by

$$\underline{q}_1 * \underline{q}_2 = \begin{bmatrix} w_1 w_2 - \underline{p}_1^T \underline{p}_2 \\ w_1 \underline{p}_2 + w_2 \underline{p}_1 + \underline{p}_1 \times \underline{p}_2 \end{bmatrix}. \quad (3.8)$$

Finally, the inversion of a quaternion is given by

$$\text{inv}(\underline{q}) = \frac{1}{\|\underline{q}\|_2} \begin{bmatrix} w \\ -\underline{p} \end{bmatrix}. \quad (3.9)$$

The two above transformations are the inversion of each other. Therefore, points can be transformed between the global and local reference system without information loss

$$T_{\text{GL}} \circ T_{\text{LG}}(\underline{g}\underline{p}) = \underline{g}\underline{p}, \quad T_{\text{LG}} \circ T_{\text{GL}}(\underline{l}\underline{p}) = \underline{l}\underline{p}. \quad (3.10)$$

In the above equations, the operator \circ denotes the composition of two functions.

Transformation between the local and the image reference system

The horizontal $\check{\phi}_h^{\text{cam}}$ and the vertical $\check{\phi}_v^{\text{cam}}$ angle of view of the drone's onboard camera are the parameters that determine the bidirectional transformation between the local and the image reference system. A point given in the coordinates of the local reference system is expressed in the coordinates of the image reference system with the transformation

$$T_{\text{IL}} : \mathbb{R}^3 \rightarrow [-1, 1]^2; \quad \underline{\mathbf{L}}p \mapsto \underline{\mathbf{I}}p = \begin{bmatrix} \max\left(-1, \min\left(\frac{-2}{\check{\phi}_h^{\text{cam}}} \text{atan2}(\underline{\mathbf{L}}y, \underline{\mathbf{L}}x), 1\right)\right) \\ \max\left(-1, \min\left(\frac{2}{\check{\phi}_v^{\text{cam}}} \text{atan2}\left(\underline{\mathbf{L}}z, \|\underline{\mathbf{L}}p\|_2\right), 1\right)\right) \end{bmatrix}. \quad (3.11)$$

The above transformation can be interpreted as the projection of a point onto the image plane of the drone's onboard camera. It can be divided into three steps. First, the vector from the optical center of the camera to the point to be transformed is mapped to its yaw $\text{atan2}(\underline{\mathbf{L}}y, \underline{\mathbf{L}}x)$ and pitch $\text{atan2}\left(\underline{\mathbf{L}}z, \|\underline{\mathbf{L}}p\|_2\right)$ angle, both, with respect to the image reference system. Second these angles are normalized by the half of the horizontal $\check{\phi}_h^{\text{cam}}$ and the half of the vertical $\check{\phi}_v^{\text{cam}}$ angle of view of the camera, respectively. Third, these normalized angles are bounded to be in the interval from minus to plus one. This boundary takes into account that an artificial neural network, which inputs images, has no basis for predictions that relate to objects that are not within the camera's field of view. As a projection from 3D to 2D, the above transformation is accompanied by information loss and is hence not bijective.

A point given in the coordinates of the image reference system is expressed in the coordinates of the local reference system with the reverse transformation

$$T_{\text{LI}} : \mathbb{R}_{\geq 0}, [-1, 1]^2 \rightarrow \mathbb{R}^3; \quad d, \underline{\mathbf{I}}p \mapsto \underline{\mathbf{L}}p = d \begin{bmatrix} \cos(\underline{\mathbf{L}}\phi_y) \\ \cos(\underline{\mathbf{L}}\phi_y) \\ \sin(\underline{\mathbf{L}}\phi_y) \end{bmatrix} \odot \begin{bmatrix} \cos(\underline{\mathbf{L}}\phi_z) \\ \sin(\underline{\mathbf{L}}\phi_z) \\ 1 \end{bmatrix}$$

with $\underline{\mathbf{L}}\phi_z = -\frac{\check{\phi}_h^{\text{cam}}}{2} \cdot \underline{\mathbf{I}}x, \quad \underline{\mathbf{L}}\phi_y = \frac{\check{\phi}_v^{\text{cam}}}{2} \cdot \underline{\mathbf{I}}y.$ (3.12)

In the above transformation, the operator \odot denotes the Hadamard product, i.e., the element-wise product of two equally dimensioned matrices. Because the 2D coordinates of the image reference system can only contain information about the direction of a point, the above transformation to 3D requires the additional input of a backprojection length d .

In contrast to the transformations T_{LG} and T_{GL} between the global and the local reference system, the transformations T_{IL} and T_{LI} between the local and the image

reference system are not invertible. However, for relevant points located within the camera's field of view and a well chosen backprojection length, it is assumed that the transformations approximately invert each other

$$T_{\mathbf{LI}} \left[d, T_{\mathbf{IL}} \left(\mathbf{l}\underline{p} \right) \right] \approx \mathbf{l}\underline{p}, \quad T_{\mathbf{IL}} \circ T_{\mathbf{LI}} \left(d, \mathbf{l}\underline{p} \right) \approx \mathbf{l}\underline{p}. \quad (3.13)$$

Transformation between the global and the image reference system

The bidirectional transformations of points between the global and the image reference frame are the compositions of the transformations via the intermittent local reference system

$$\begin{aligned} T_{\mathbf{IG}} &= T_{\mathbf{IL}} \circ T_{\mathbf{LG}} : \mathbb{R}^3 \rightarrow [-1, 1]^2 \\ T_{\mathbf{GI}} &= T_{\mathbf{GL}} \circ T_{\mathbf{LI}} : \mathbb{R}_{\geq 0}, [-1, 1]^2 \rightarrow \mathbb{R}^3. \end{aligned} \quad (3.14)$$

Due to the fact that $T_{\mathbf{LG}}$ and $T_{\mathbf{GL}}$ are the inverse of each other and the assumption that $T_{\mathbf{IL}}$ and $T_{\mathbf{LI}}$ approximately invert each other within a relevant range, the above compositions are expected to also approximately invert each other within this relevant range

$$T_{\mathbf{GI}} \left[d, T_{\mathbf{IG}} \left(\mathbf{g}\underline{p} \right) \right] \approx \mathbf{g}\underline{p}, \quad T_{\mathbf{IG}} \circ T_{\mathbf{GI}} \left(d, \mathbf{l}\underline{p} \right) \approx \mathbf{l}\underline{p}. \quad (3.15)$$

3.2 ANN module

The ANN module performs the function of making navigation decisions within the autonomous navigation method. Figure 3.2 shows the information flow of this decision making process. The ANN module infers its decisions exclusively on the basis of pre-processed data from sensors onboard the drone. It comprises the five submodules named CNN, CAT, GRU, FC and HEAD. This modular design enables a high flexibility for the experiments with the different ANN module variants in chapter 4. All variants have in common that, first, the order of the submodules is fixed and, second, the outer submodules (CNN and HEAD) are always activated. The latter ensures the minimum functionality of the ANN module of extracting visual features of the preprocessed RGB images from the drone's onboard camera and mapping them to navigation decisions. The variants can differ in that the user specifies the design parameters of the (inner and outer) individual submodules. This can include the deactivation (reduction to the identity map) of the individual inner submodules (CAT, GRU and FC). The inner submodules perform the functions of inputting optional features (CAT), extracting temporal features (GRU) and increasing the general complexity of the ANN module (FC).

The ANN module learns by imitation with dataset aggregation (see section 2.2 for background). Thereby, the dataset is aggregated from samples demonstrated by the expert system (see section 3.5). Each sample is a pair of an input sequence and a single

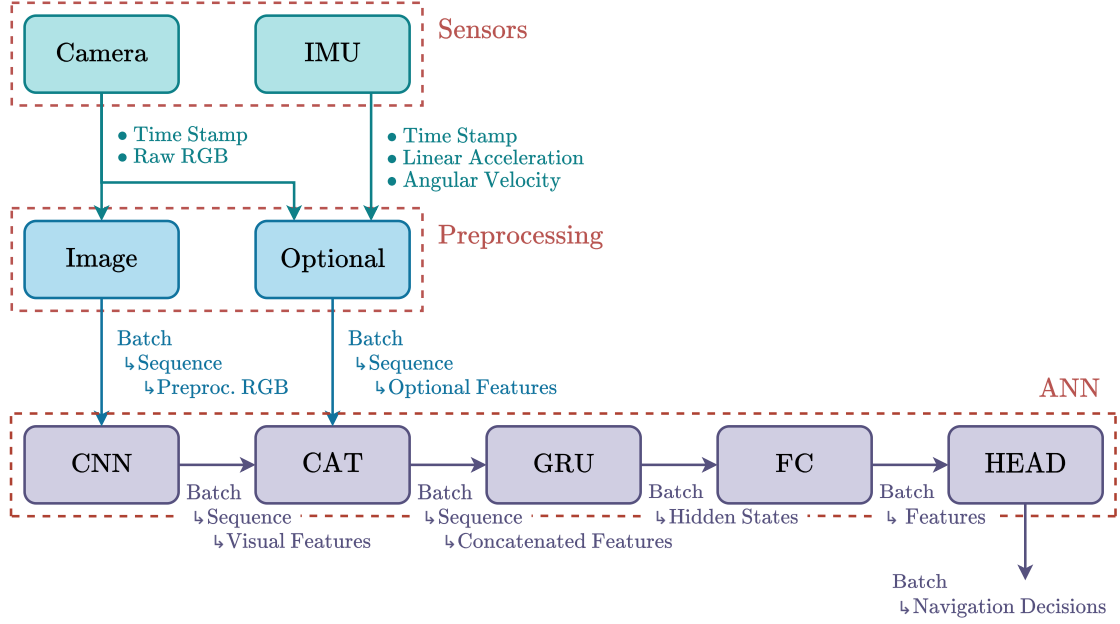


Figure 3.2: Information flow of the navigation decision making

lable. For the individual ANN variant, the user specifies the sequence length of the samples

$$\check{N}^{\text{seq}} \in \mathbb{N}_{>0}. \quad (3.16)$$

The ANN module is trained on batches of the aggregated dataset with supervised learning. The user specifies the batch size

$$\check{N}^{\text{batch}} \in \mathbb{N}_{>0}. \quad (3.17)$$

The submodules prior to the GRU submodule (CNN and CAT) have no sequential awareness and, thus, process sequence elements in parallel like batch elements. In contrast, the GRU submodule operates in many-to-one mode, whereby each input sequence of feature vectors is mapped to a single non-sequential output feature vector. The subsequent submodules (FC and HEAD) then process batches of non-sequential data, as is common in conventional feedforward networks. In this sense, the GRU submodule is mandatory in case the user specifies $\check{N}^{\text{seq}} > 1$ for the samples of the training dataset.

At racing, when the autonomous navigation method flies the drone through the race-track, the ANN module makes navigation decisions in real-time at the user-specified frequency f^{main} with the batch size and sequence length of the input $\check{N}^{\text{batch}} = \check{N}^{\text{seq}} = 1$. The GRU submodule (if activated in the specific variant) hence operates in one-to-one mode, i.e., each single non-sequential input feature vector is mapped to a single non-sequential output feature vector. Since the single input feature vectors trace back to the

sensor data coming in at a fixed frequency, they, as a whole, constitute a time series, on which the GRU submodule can build up memory as learned during the training on the sequences of the specified length. As a result, both, the current and past sensor data, influence the current navigation decision.

Input preprocessing

The drone's onboard camera outputs raw RGB images

$$\underline{\underline{x}}^{\text{cam}} \in \{0, \dots, N_{\text{max}}^{\text{cam}}\}^{3 \times N_{\text{height}}^{\text{cam}} \times N_{\text{width}}^{\text{cam}}} \quad (3.18)$$

where $N_{\text{max}}^{\text{cam}}$ (usually = 255) is the full pixel intensity and $N_{\text{height}}^{\text{cam}} \times N_{\text{width}}^{\text{cam}}$ is the image size. The latest raw RGB image is preprocessed in two steps before being fed to the CNN submodule. First, the pixel intensities are normalized by the full intensity $N_{\text{max}}^{\text{cam}}$ with the aim to accelerate the convergence of the loss during training. Second, the image is sized down preserving its aspect ratio with the user-specified factor $s_{\text{resize}}^{\text{cnn}}$. Besides significantly accelerating the training, this step makes training on longer sequences possible in the first place by reducing GPU memory usage. The resulting preprocessed RGB image is

$$\underline{\underline{x}}^{\text{preproc}} \in \left\{ \frac{i}{N_{\text{max}}^{\text{cam}}} \right\}_{i \in \{0, \dots, N_{\text{max}}^{\text{cam}}\}}^{3 \times \lfloor s_{\text{resize}}^{\text{cnn}} \cdot N_{\text{height}}^{\text{cam}} \rfloor \times \lfloor s_{\text{resize}}^{\text{cnn}} \cdot N_{\text{width}}^{\text{cam}} \rfloor} \quad (3.19)$$

where $\lfloor \square \rfloor$ denotes the operation of rounding down to the nearest integer.

The available optional input features are

- the time step t_{Δ}^{cam} between the stamps of the raw RGB images processed at the previous and the current inference
- the latest estimate from the drone's onboard IMU (inertial measurement unit) comprising the drone's linear acceleration $\mathbf{L}\hat{\underline{a}}^{\text{imu}} \in \mathbb{R}^3$ and angular velocity $\mathbf{L}\hat{\underline{\omega}}^{\text{imu}} \in \mathbb{R}^3$ in the local reference system
- the time step t_{Δ}^{imu} between the stamps of the IMU estimates processed at the previous and the current inference.

The user-activated optional inputs are stacked into the optional input vector before being fed to the CAT submodule. For example, the fully activated optional input vector is

$$\underline{\underline{x}}^{\text{opt}} = \begin{bmatrix} t_{\Delta}^{\text{cam}} \\ \mathbf{L}\hat{\underline{a}}^{\text{imu}} \\ \mathbf{L}\hat{\underline{\omega}}^{\text{imu}} \\ t_{\Delta}^{\text{imu}} \end{bmatrix}. \quad (3.20)$$

CNN

The CNN (convolutional neural network) submodule extracts visual features of images. This submodule is implemented with the backbone of any user-selected TorchVision classification model¹, which is obtained by removing the last layer of the model. In addition, the user specifies whether the backbone initializes with pretrained weights and whether the weights of the backbone are trainable. Since CNN backbones are only applied in this thesis, their corresponding mapping is regarded as a black box

$$\check{\mathcal{F}}^{\text{cnn}} : \mathbb{R}^{N_{\text{channel}}^{\text{cnn}} \times N_{\text{height}}^{\text{cnn}} \times N_{\text{width}}^{\text{cnn}}} \rightarrow \mathbb{R}^{N_{\text{out}}^{\text{cnn}}}; \quad \underline{x} \mapsto \underline{x}^{\text{vis}}. \quad (3.21)$$

The backbone implementation adapts to the inputted image in terms of the the number of channels $N_{\text{channel}}^{\text{cnn}}$, height $N_{\text{height}}^{\text{cnn}}$ and width $N_{\text{width}}^{\text{cnn}}$. The backbone's output dimensionality $N_{\text{out}}^{\text{cnn}}$ is fixed by the design of its last layer. The user specifies

The CNN submodule inputs a batch of sequences of preprocessed RGB images (equ. 3.19)

$$\left(\underline{x}_t^{\text{preproc}} \right)_{t \in \{1, \dots, \check{N}_{\text{seq}}\}, i}, \quad i \in \{1, \dots, \check{N}^{\text{batch}}\}. \quad (3.22)$$

As it processes the individual sequence elements unrelated in parallel like batch elements, the CNN submodule maps each image of the input batch to an individual visual feature vector in the output batch

$$\left(\underline{x}_t^{\text{vis}} \right)_{t \in \{1, \dots, \check{N}_{\text{seq}}\}, i}, \quad i \in \{1, \dots, \check{N}^{\text{batch}}\}. \quad (3.23)$$

The number of trainable parameters $N_{\text{params}}^{\text{cnn}}$ of the CNN submodule depends on the user-selected TorchVision model.

CAT

The CAT submodule concatenates two feature vectors

$$\mathcal{F}^{\text{cat}} : \left(\mathbb{R}^{N_1^{\text{cat}}}, \mathbb{R}^{N_2^{\text{cat}}} \right) \rightarrow \mathbb{R}^{N_1^{\text{cat}} + N_2^{\text{cat}}}; \quad (\underline{x}_1, \underline{x}_2) \mapsto \begin{bmatrix} \underline{x}_1 \\ \underline{x}_2 \end{bmatrix} \quad (3.24)$$

where the input dimensionalities $\mathbb{R}^{N_1^{\text{cat}}}$ and $\mathbb{R}^{N_2^{\text{cat}}}$ adapt to the number of features of the input. This submodule applies to each visual feature vector outputted by the CNN submodule (see equ. 3.23) and optional input feature vector

$$\left(\underline{x}_t^{\text{opt}} \right)_{t \in \{1, \dots, \check{N}_{\text{seq}}\}, i}, \quad i \in \{1, \dots, \check{N}^{\text{batch}}\}. \quad (3.25)$$

that correspond to the same position in batch and sequence. Hence the CAT submodule outputs a batch of sequences of concatenated feature vectors

$$\left(\begin{bmatrix} \underline{x}_t^{\text{vis}} \\ \underline{x}_t^{\text{opt}} \end{bmatrix} \right)_{t \in \{1, \dots, \check{N}_{\text{seq}}\}, i}, \quad i \in \{1, \dots, \check{N}^{\text{batch}}\}. \quad (3.26)$$

¹<https://pytorch.org/vision/stable/models.html>, visited on 23/08/2022

If the user deactivates all optional inputs, the CAT submodule also deactivates and re-cedes to the identity map of the the CNN submodule output. Either way, the CAT submodule has zero trainable parameters

$$N_{\text{params}}^{\text{cat}} = 0. \quad (3.27)$$

GRU

The GRU (gated recurrent unit) submodule is implemented using the PyTorch multi-layer GRU², which integrates the GRU [8] introduced in section 2.3 on each layer. As a quick reminder, the single layer GRU has the ability to comprehend temporal relations within sequences. Each layer $l \in \{1, \dots, \check{N}_{\text{layer}}^{\text{gru}}\}$ processes an input sequence by iterating through it $t \in \{1, \dots, \check{N}_{\text{seq}}\}$ mapping the current sequence element and the layer's previous hidden state to the current hidden state (see equ. 2.27)

$$\mathcal{F}_t^{\text{gru}} : \left(\mathbb{R}^{N_{\text{in},l}^{\text{gru}}}, [-1, 1]^{\check{N}_{\text{hidden}}^{\text{gru}}} \right) \rightarrow [-1, 1]^{\check{N}_{\text{hidden}}^{\text{gru}}} ; \quad \left(\underline{x}_t^{(l)}, \underline{h}_{t-1}^{(l)} \right) \mapsto \underline{h}_t^{(l)}. \quad (3.28)$$

Thereby, $\underline{h}_0^{(l)}$ is either initialized with zeros or corresponds to the last computed hidden state from the last inference. In the multi-layer GRU, each layer maintains its own hidden state. The user specifies the number of layers $\check{N}_{\text{layer}}^{\text{gru}}$ and the hidden size $\check{N}_{\text{hidden}}^{\text{gru}}$ (i.e., dimensionality) shared by all hidden states. While the first GRU layer inputs the elements of the given input sequence, all subsequent layers input the hidden state from the previous layer subject to dropout

$$\begin{aligned} \mathcal{F}^{\text{gru}} : & \left(\mathbb{R}^{N_{\text{in},1}^{\text{gru}}}, [-1, 1]^{\check{N}_{\text{hidden}}^{\text{gru}} \times \check{N}_{\text{layer}}^{\text{gru}}} \right) \rightarrow [-1, 1]^{\check{N}_{\text{hidden}}^{\text{gru}}} \\ & \left(\underline{x}_t, \underline{h}_{t-1}^{(1)}, \dots, \underline{h}_{t-1}^{(\check{N}_{\text{layer}}^{\text{gru}})} \right) \mapsto \underline{h}_t^{(\check{N}_{\text{layer}}^{\text{gru}})} = \dots \\ & \dots \mathcal{F}_{\check{N}_{\text{layer}}^{\text{gru}}}^{\text{gru}} \left(\underline{\delta} \odot \mathcal{F}_{\check{N}_{\text{layer}}^{\text{gru}}-1}^{\text{gru}} \left(\underline{\delta} \odot \dots \mathcal{F}_1^{\text{gru}} \left(\underline{x}_t, \underline{h}_{t-1}^{(1)} \right), \underline{h}_{t-1}^{(\check{N}_{\text{layer}}^{\text{gru}}-1)} \right), \underline{h}_{t-1}^{(\check{N}_{\text{layer}}^{\text{gru}})} \right). \end{aligned} \quad (3.29)$$

Dropout is a measure that prevents ANNs from overfitting to their provided training data. At training, it randomly sets entries of a feature vector to zero while maintaining the vector's signal strength on average in order to force the ANN to learn the extraction of stand-alone features whose informative value is independent from the other extracted features [19]. Mathematically, dropout applied on a hidden state (or feature vector) is calculated with the Hadamard product (denoted with \odot) of that hidden state and the vector $\underline{\delta}$ of same dimensionality whose entries, for every calculation, are random

²<https://pytorch.org/docs/stable/generated/torch.nn.GRU.html>, visited on 24/08/2022

variables resampled from a Bernoulli distribution with a user-specified probability

$$P(\delta_i = 0) = \check{p}^{\text{gru}}, \quad P\left(\delta_i = \frac{1}{1 - \check{p}^{\text{gru}}}\right) = 1 - \check{p}^{\text{gru}}. \quad (3.30)$$

At racing, the dropout probability is null whereby the dropout is deactivated.

As the l -th GRU layer has $3\check{N}_{\text{hidden}}^{\text{gru}}(N_{\text{in},l}^{\text{gru}} + \check{N}_{\text{hidden}}^{\text{gru}} + 2)$ trainable parameters (see equ. 2.30), the total number of trainable parameters of the GRU submodule is

$$N_{\text{params}}^{\text{gru}} = 3\check{N}_{\text{hidden}}^{\text{gru}} \left((N_{\text{in},1}^{\text{gru}} + \check{N}_{\text{hidden}}^{\text{gru}} + 2) + (\check{N}_{\text{layer}}^{\text{gru}} - 1)(2\check{N}_{\text{hidden}}^{\text{gru}} + 2) \right). \quad (3.31)$$

The GRU submodule operates in many-to-one mode at training or one-to-one mode at racing where the length of the input sequences is one. Either way, the GRU submodule maps its input batch (see equ. 3.26) to a batch of last hidden states of the last layer

$$\underline{h}_{\check{N}_{\text{seq},i}}^{(\check{N}_{\text{layer}}^{\text{gru}})}, \quad i \in \{1, \dots, \check{N}^{\text{batch}}\}. \quad (3.32)$$

FC

The FC submodule performs the function of increasing the general complexity of the ANN module. It consists of multiple fully connected layers. Each layer $l \in \{1, \dots, \check{N}_{\text{layer}}^{\text{fc}}\}$ applies an activation, dropout and a biased linear transformation on the input feature vector

$$\mathcal{F}_l^{\text{fc}} : \mathbb{R}^{N_{\text{in},l}^{\text{fc}}} \rightarrow \mathbb{R}^{\check{N}_{\text{width}}^{\text{fc}}}; \quad \underline{x} \mapsto \underline{A}_l^{\text{fc}} \cdot \underline{\delta}^{\text{fc}} \odot \check{f}^{\text{fc}}(\underline{x}) + \underline{b}_l^{\text{fc}}. \quad (3.33)$$

In the multi-layer FC submodule, the first layer inputs the given input feature vector, whereas all subsequent layers input the output from the previous layer

$$\mathcal{F}^{\text{fc}} : \mathbb{R}^{N_{\text{in},1}^{\text{fc}}} \rightarrow \mathbb{R}^{\check{N}_{\text{width}}^{\text{fc}}}; \quad \underline{x} \mapsto \mathcal{F}_{\check{N}_{\text{layer}}^{\text{fc}}}^{\text{fc}} \left(\mathcal{F}_{\check{N}_{\text{layer}}^{\text{fc}}-1}^{\text{fc}} (\dots \mathcal{F}_1^{\text{fc}}(\underline{x})) \right). \quad (3.34)$$

For the FC submodule, the user specifies:

- the number of layers $\check{N}_{\text{layer}}^{\text{fc}}$
- the width $\check{N}_{\text{width}}^{\text{fc}}$, i.e., output dimensionality shared by all layers
- the activation function $\check{f}^{\text{fc}} : \mathbb{R} \rightarrow \mathbb{R}$ from the non-linear activations implemented in PyTorch³, which applies element-wise on the input feature vector (denoted with the overset \odot)

³<https://pytorch.org/docs/stable/nn.html>, visited on 03/07/2022

- the dropout probability $\check{p}^{\text{fc}} \in [0, 1]$, i.e., the probability to resample an entry of the vector $\underline{\delta}^{\text{fc}}$ with zero

The input dimensionality of a layer adapts to the number of features in the given input vector. For the first layer, it adapts to the feature vector forwarded to the FC submodule $N_{\text{in},1}^{\text{fc}} = \dim(\underline{x})$. For all subsequent layers $l \geq 2$, it adapts to the width of the FC submodule $N_{\text{in},l}^{\text{fc}} = \check{N}_{\text{width}}^{\text{fc}}$. The biased linear transformation of the l -th layer consists of the multiplication with the matrix of trainable weights and the addition of the vector of trainable biases

$$\underline{A}_l^{\text{fc}} \in \mathbb{R}^{N_{\text{in},l}^{\text{fc}} \times \check{N}_{\text{width}}^{\text{fc}}}, \quad \underline{b}_l^{\text{fc}} \in \mathbb{R}^{\check{N}_{\text{width}}^{\text{fc}}}. \quad (3.35)$$

As a single layer therewith has $(N_{\text{in},l}^{\text{fc}} + 1) \check{N}_{\text{width}}^{\text{fc}}$ trainable parameters, the total number of trainable parameters of the FC submodule is

$$N_{\text{params}}^{\text{fc}} = \left(N_{\text{in},1}^{\text{fc}} + 1 + \left(\check{N}_{\text{layer}}^{\text{fc}} - 1 \right) \left(\check{N}_{\text{width}}^{\text{fc}} + 1 \right) \right) \check{N}_{\text{width}}^{\text{fc}}. \quad (3.36)$$

The FC submodule maps the batch of hidden states outputted by the GRU submodule to the batch of feature vectors

$$\mathcal{F}^{\text{fc}}(\underline{h})_i, \quad i \in \{1, \dots, \check{N}^{\text{batch}}\}. \quad (3.37)$$

HEAD

The mandatory HEAD submodule performs the function of mapping to the final output of the ANN module. Depending on the user's selection, the final output is either a navigation decision or a control command. A navigation decision

$$(\tilde{v}_{\text{des}}^{\text{d}}, \underline{\mathbf{I}}p^{\text{wp}}) \quad (3.38)$$

comprises a normalized desired speed $\tilde{v}_{\text{des}}^{\text{d}} \in [0, 1]$ of the drone and a waypoint $\underline{\mathbf{I}}p^{\text{wp}} \in [-1, 1]$ in the image reference system (see fig. 3.1b). A control command

$$(\underline{\mathbf{L}}\underline{\omega}_{\text{des}}^{\text{d}}, \underline{\mathbf{L}}\underline{\dot{\omega}}_{\text{des}}^{\text{d}}, c_{\text{des}}^{\text{d}}) \quad (3.39)$$

comprises the desired angular velocity $\underline{\mathbf{L}}\underline{\omega}_{\text{des}}^{\text{d}}$ and acceleration $\underline{\mathbf{L}}\underline{\dot{\omega}}_{\text{des}}^{\text{d}}$ of the drone in the local reference system (see fig. 3.1a) as well as the desired collective thrust $c_{\text{des}}^{\text{d}}$ of the drone's rotors. In the limited scope of this master's thesis, the control command output option, which is a shortcut to the position controller output (see section 3.4), is only partly implemented and not examined in the experiments in section 4.

The head submodule corresponds to a single layer of the FC submodule without dropout (see equ. 3.33) as it applies an activation and a biased linear transformation on the input feature vector

$$\mathcal{F}^{\text{head}} : \mathbb{R}^{N_{\text{in}}^{\text{head}}} \rightarrow \mathbb{R}^{N_{\text{out}}^{\text{head}}}; \quad \underline{x} \mapsto \underline{A}^{\text{head}} \cdot \overset{\odot}{f}^{\text{head}}(\underline{x}) + \underline{b}^{\text{head}}. \quad (3.40)$$

For the HEAD submodule, the user selects the activation function $\check{f}^{\text{fc}} : \mathbb{R} \rightarrow \mathbb{R}$ from the non-linear activations implemented in PyTorch⁴, which applies element-wise on the input feature vector (denoted with the overset \odot). The input dimensionality adapts to the number of features of the given input vector

$$N_{\text{in}}^{\text{head}} = \dim(\underline{x}), \quad (3.41)$$

whereas the output dimensionality adapts to the user-selected output option

$$N_{\text{out}}^{\text{head}} = \begin{cases} 3, & \text{if navigation decision} \\ 7, & \text{if control command.} \end{cases} \quad (3.42)$$

The total number of trainable parameters of the HEAD submodule is

$$N_{\text{params}}^{\text{head}} = (N_{\text{in}}^{\text{head}} + 1) N_{\text{out}}^{\text{head}}. \quad (3.43)$$

Output

3.3 Planning module

The planning module performs the task of path planning within the autonomous navigation method. At the user-specified main frequency \check{f}^{main} , the planning module samples states from its local trajectory and forwards them as reference to the control module. Every \check{N}^{plan} -th (user-specified) iteration, the planning module re-computes its local trajectory on the basis of its input, i.e., the latest navigation decision and the latest drone state estimate.

The latest navigation decision stems from either the ANN module (see equ. 3.38) or, if it has intervened at training data generation, the expert system (see equ. ??). A navigation decision comprises the normalized desired speed and the waypoint in the image reference system

$$(\tilde{v}_{\text{des}}^{\text{d}}, \underline{\mathbf{p}}^{\text{wp}}). \quad (3.44)$$

The latest drone state estimate stems from the state estimation system. In simulation, the estimate may correspond to the ground-truth state. A drone state estimate includes position, velocity and acceleration with respect to the global reference system

$$\underline{\mathbf{g}}\underline{\mathbf{p}}^{\text{d}}, \underline{\mathbf{g}}\underline{\mathbf{v}}^{\text{d}}, \underline{\mathbf{g}}\underline{\mathbf{a}}^{\text{d}}. \quad (3.45)$$

At a fraction of the main frequency, i.e., $\check{f}^{\text{main}} / \check{N}^{\text{plan}}$, the planning module takes the following 5 steps to re-compute its local trajectory.

⁴<https://pytorch.org/docs/stable/nn.html>, visited on 03/07/2022

1. Compute the desired speed

$$v_{\text{des}}^{\text{d}} = \max \left(\check{v}_{\text{min}}^{\text{d}}, \check{v}_{\text{max}}^{\text{d}} \cdot \tilde{v}_{\text{des}}^{\text{d}} \right). \quad (3.46)$$

The normalized, desired speed $\tilde{v}_{\text{des}}^{\text{d}} \in [0, 1]$ of the navigation decision is rescaled by its upper bound, the user-specified drone's maximum speed $\check{v}_{\text{max}}^{\text{d}}$. The user-specified drone's minimum speed $\check{v}_{\text{min}}^{\text{d}}$ lower-bounds the desired speed.

2. Compute the drone's distance to the waypoint

$$d^{\text{d-wp}} = \max \left(\check{d}_{\text{min}}^{\text{d-wp}}, \min \left(v_{\text{des}}^{\text{d}} \cdot \check{t}_{\Delta}^{\text{d-wp}}, \check{d}_{\text{max}}^{\text{d-wp}} \right) \right). \quad (3.47)$$

The desired speed $v_{\text{des}}^{\text{d}}$ is integrated over the user-specified duration $\check{t}_{\Delta}^{\text{d-wp}}$. The result is bounded to the interval spanned by the user-specified minimum $\check{d}_{\text{min}}^{\text{d-wp}}$ and maximum $\check{d}_{\text{max}}^{\text{d-wp}}$ distance.

3. Compute the waypoint with respect to the global reference system

$$\mathbf{g}\underline{p}^{\text{wp}} = T_{\mathbf{GI}} \left(d^{\text{d-wp}}, \mathbf{i}\underline{p}^{\text{wp}} \right). \quad (3.48)$$

The transformation $T_{\mathbf{GI}}$ (see equ. 3.14) backprojects the waypoint $\mathbf{i}\underline{p}^{\text{wp}}$ of the navigation decision from the 2D image to the 3D global reference system. Thereby, the drone's distance $d^{\text{d-wp}}$ to the waypoint constitutes the backprojection length.

4. Set the starting time of the local trajectory to the current time

$$t_0^{\text{lt}} = t \quad (3.49)$$

and compute the duration of the local trajectory

$$t_{\Delta}^{\text{lt}} = \frac{d^{\text{d-wp}}}{\min \left(v_{\text{des}}^{\text{d}}, \|\mathbf{g}\underline{v}^{\text{d}}\|_2 + \check{v}_{\Delta}^{\text{d}} \right)}. \quad (3.50)$$

The drone's distance $d^{\text{d-wp}}$ to the waypoint is divided by the slower of either the desired speed $v_{\text{des}}^{\text{d}}$ or the latest drone speed estimate $\|\mathbf{g}\underline{v}^{\text{d}}\|_2$ plus a user-specified speed increment $\check{v}_{\Delta}^{\text{d}}$. By relating the desired to the estimated speed, excessive speed increases potentially violating the drone's dynamic limitations can be prevented.

5. Compute the local trajectory

$$\mathbf{g}\underline{p}^{\text{lt}} : [0, t_{\Delta}^{\text{lt}}] \rightarrow \mathbb{R}^3; \quad t \mapsto \mathbf{g}\underline{p}^{\text{lt}}(t) \quad (3.51)$$

starting in the latest drone state estimate $\mathbf{g}\underline{p}^d$, $\mathbf{g}\underline{v}^d$, $\mathbf{g}\underline{a}^d$ and ending in the global waypoint $\mathbf{g}\underline{p}^{wp}$ with unconstrained velocity and acceleration. The implementation⁵ of the algorithm of Mueller et. al. [41] is deployed to find the polynomial trajectory with minimum jerk (third time derivative of position) by solving the optimization problem

$$\begin{aligned} & \min \int_0^{t_\Delta^{lt}} \left\| \mathbf{g}\ddot{\underline{p}}^{lt}(t) \right\|_2^2 dt \\ \text{s.t. } & \mathbf{g}\underline{p}^{lt}(0) = \mathbf{g}\underline{p}^d & \mathbf{g}\underline{p}^{lt}(t_\Delta^{lt}) = \mathbf{g}\underline{p}^{wp} \\ & \mathbf{g}\underline{\dot{p}}^{lt}(0) = \mathbf{g}\underline{v}^d & \mathbf{g}\underline{\dot{p}}^{lt}(t_\Delta^{lt}) \text{ free} \\ & \mathbf{g}\underline{\ddot{p}}^{lt}(0) = \mathbf{g}\underline{a}^d & \mathbf{g}\underline{\ddot{p}}^{lt}(t_\Delta^{lt}) \text{ free.} \end{aligned} \quad (3.52)$$

The drone's dynamic limitations are only taken into account in subsequent feasibility checks and are exempt from the above optimization problem. This allows the algorithm to solve the optimization problem in closed form which is characterized by low computational effort. The algorithm therewith qualifies to run at the relatively high frequencies required by the autonomous navigation method.

At the main frequency \check{f}^{main} , the planning module takes the following 2 steps to sample a reference state from its local trajectory.

1. Compute the time point of the reference state

$$t^{lt} = t - t_0^{lt} + 1/\check{f}^{main}. \quad (3.53)$$

The actual time t is related to the starting time t_0^{lt} of the local trajectory, whose time domain starts at zero. The addition of the main period $1/\check{f}^{main}$ ensures that the sampled reference state remains prospective at all times.

2. Sample the current reference state from the local trajectory

$$\begin{aligned} \mathbf{g}\underline{p}^{ref} &= \mathbf{g}\underline{p}^{lt}(t^{lt}) \\ \mathbf{g}\underline{v}^{ref} &= \mathbf{g}\underline{\dot{p}}^{lt}(t^{lt}) \\ \mathbf{g}\underline{a}^{ref} &= \mathbf{g}\underline{\ddot{p}}^{lt}(t^{lt}) \\ \mathbf{g}\underline{j}^{ref} &= \mathbf{g}\underline{\ddot{\dot{p}}}^{lt}(t^{lt}) \\ \phi_z^{ref} &= \text{atan2}(\mathbf{g}v_y^{ref}, \mathbf{g}v_x^{ref}). \end{aligned} \quad (3.54)$$

The reference yaw ϕ_z^{ref} is set so that the drone and therewith its onboard camera point in the direction of flight movement.

⁵<https://github.com/markwmuller/RapidQuadrocopterTrajectories>, visited on 17/08/2022

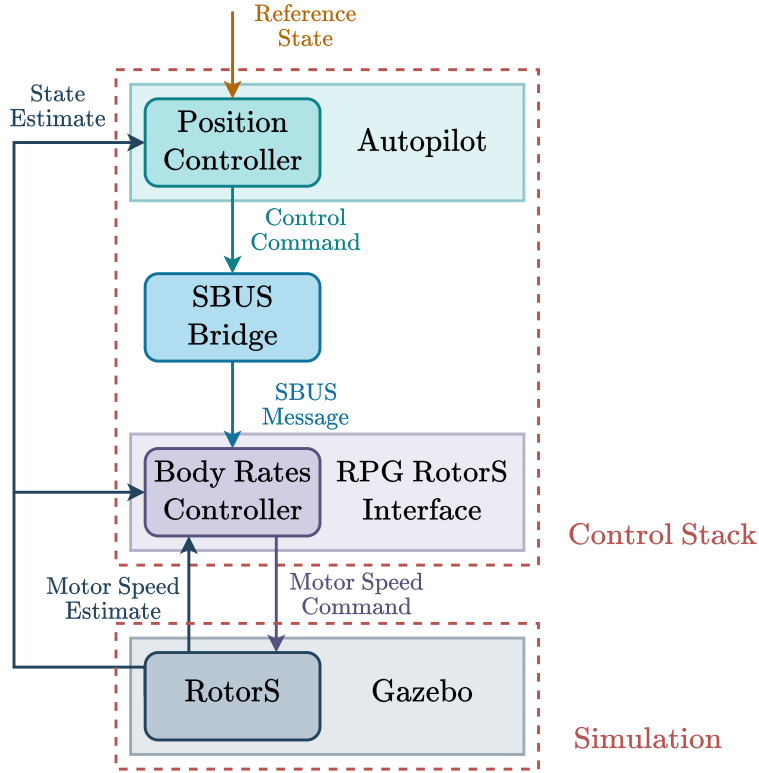


Figure 3.3: The control stack in simulation.

3.4 Control stack

Within the autonomous navigation method, the control stack takes on the task of flying the drone as planned. To do this, the control stack generates the inputs for the motors attached to the drone’s rotors, which consequently track the latest reference state (equ. 3.54) from the planning module. In the simulations of this thesis, the control stack is realized with the RPG Quadrotor Control ⁶ implementation (see figure 3.3). Since this thesis centers on the reasoning aspect of autonomous navigation, only an overview of the deployed control stack is presented here. The reader may consult the provided references for more details on the control.

The RPG Quadrotor Control implementation, which includes the autopilot, the SBUS bridge and the RPG RotorS interface, basically executes two feedback control loops in a cascade. The autopilot integrates the position controller that runs the control algorithm of Faessler et al. proposed in [14]. Based on the latest reference state and the fed back drone state estimates, the position controller generates high-level control commands. A control command comprises the collective thrust of the drone’s

⁶https://github.com/uzh-rpg/rpg_quadrotor_control, visited on 17/08/2022

rotors as well as the drone’s angular velocity and acceleration. The SBUS bridge converts each incoming control command into an SBUS message and forwards this message to the RPG RotorS interface. The RPG RotorS interface integrates the body-rate controller that runs the control algorithm of Faessler et al. proposed in [13]. Based on the latest high-level control command as well as the fed back drone state and motor speed estimates, the body-rate controller generates low-level motor speed commands. These commands are forwarded to RotorS for execution. RotorS, developed by Furrer et al. [16], is plugged into the Gazebo ⁷ simulator to model the drone’s physics and to provide the controllers with drone state and motor speed estimates.

In real-world, the drone’s flight controller would replace the RPG RotorS interface in order to generate hardware-specific low-level motor commands based on the latest SBUS message from the SBUS bridge.

3.5 Expert system

In the context of machine learning, an expert system is a program that imitates a human expert in order to solve a problem. It comprises a knowledge base, which stores known facts and rules, and an inference engine, which infers new facts by applying the rules to the known facts [24].

Problem

This thesis implements the expert system by Kaufmann et al. [29] in order to solve the problem of automated navigation decision making during the generation of training data for the ANN module. The training dataset is extended with new samples while the drone runs the autonomous navigation method to fly through a racetrack. The expert system checks the latest navigation decision made by the yet partially trained ANN module. If it does not meet certain requirements, the expert system intervenes with its own navigation decision. This, first, keeps the drone on course and, second, triggers the generation of a new training sample labeled with the expert system’s navigation decision.

Knowledge base

While the ANN module infers navigation decisions from onboard sensor data, the expert system makes navigation decisions based on its knowledge which includes the following known facts (**F***) and rules (**R***).

F1 The planning module’s waypoint

$$G_{wp}^{ann} \tag{3.55}$$

⁷<https://gazebo.org/home>, visited on 18/08/2022

with respect to the global reference system (see equ. 3.48) that was computed based on the ANN module's latest navigation decision (see equ. 3.38).

- F2** The drone's latest position and quaternion orientation estimate, which are provided by the drone's state estimation system and may correspond to ground truth in the simulation

$$\mathbf{G}\underline{p}^d, \quad \mathbf{G}\underline{q}^d. \quad (3.56)$$

- F3** The center points of the gates of the racetrack

$$\left(\mathbf{G}\underline{p}_i^{\text{gate}} \right)_{i \in \{0, \dots, N^{\text{gate}} - 1\}} \quad (3.57)$$

and the initial index to the currently targeted gate to be passed next

$$i_{\text{target}}^{\text{gate}} \in \{0, \dots, N^{\text{gate}} - 1\}. \quad (3.58)$$

- R1** Compute the global trajectory of the current racetrack

$$\mathbf{G}\underline{p}^{\text{gt}} : \left[t_0^{\text{gate}}, t_{N^{\text{gate}}}^{\text{gate}} \right] \rightarrow \mathbb{R}^3; \quad t \mapsto \mathbf{G}\underline{p}^{\text{gt}}(t). \quad (3.59)$$

The algorithm of Mellinger and Kumar [37] finds the minimum snap (fourth time derivative of position) spline trajectory

$$\mathbf{G}\underline{p}^{\text{gt}}(t) = \sum_{i=0}^{N^{\text{gate}}-1} \begin{cases} \mathbf{G}\underline{p}_i^{\text{gt}}(t), & t \in [t_i^{\text{gate}}, t_{i+1}^{\text{gate}}] \\ 0, & \text{else} \end{cases} \quad (3.60)$$

that, traverses through all gate center points (**F3**), each at its corresponding gate time t_i^{gate} , and reconnects to itself at $t = t_{N^{\text{gate}}}^{\text{gate}}$ at gate $i = 0$. The entries of the pieces $\mathbf{G}\underline{p}_i^{\text{gt}}(t)$ of the spline are polynomials. The user specifies the polynomial order $\check{N}_{\text{poly}}^{\text{gt}}$ of the pieces and the continuity order $\check{N}_{\text{cont}}^{\text{gt}}$ of the spline. However, since the goal is to minimize snap, it is required that $\check{N}_{\text{poly}}^{\text{gt}} \geq \check{N}_{\text{cont}}^{\text{gt}} \geq 4$. The algorithm performs the following two-step iterative optimization.

First, the optimal polynomial coefficients of the spline pieces are found for fixed gate arrival times t_i^{gate} by solving the optimization problem

$$\begin{aligned} & \underset{\mathbf{G}\underline{p}^{\text{gt}}}{\text{argmin}} \int_{t_0^{\text{gate}}}^{t_{N^{\text{gate}}}^{\text{gate}}} \left\| \mathbf{G}\ddot{\ddot{p}}^{\text{gt}}(t) \right\|_2^2 dt \\ \text{s.t.} \quad & \mathbf{G}\underline{p}^{\text{gt}}(t_i^{\text{gate}}) = \mathbf{G}\underline{p}_i^{\text{gate}}, & \frac{d^j \mathbf{G}\underline{p}^{\text{gt}}}{dt^j}(t_i^{\text{gate}}) \text{ defined,} \\ & i \in \{0, \dots, N^{\text{gate}}\}, & j \in \{1, \dots, \check{N}_{\text{cont}}^{\text{gt}}\}. \end{aligned} \quad (3.61)$$

Note that, as the spline is closed, the first and last gate equate $\mathbf{g}_{N^{\text{gate}}}^{\text{gate}} = \mathbf{g}_0^{\text{gate}}$. Moreover, the gate times of the very first iteration are approximated with the distances between the gate center points divided by the user-specified maximum speed $\check{v}_{\text{max}}^{\text{gt}}$ of the trajectory. The above optimization problem is temporally and spatially dedimensionalized to increase numeric stability and reformulated as quadratic program, which is solved with the Gurobi⁸ optimizer.

Second, the polynomial coefficients of the spline pieces are fixed and the inner gate times t_i^{gate} are optimized relatively to each other. The corresponding optimization problem

$$\begin{aligned} & \underset{t_i^{\text{gate}}}{\text{argmin}} \int_{t_0^{\text{gate}}}^{t_{N^{\text{gate}}}^{\text{gate}}} \left\| \mathbf{g} \ddot{\underline{p}}^{\text{gt}}(t) \right\|_2^2 dt \\ \text{s.t. } & t_i^{\text{gate}} < t_{i+1}^{\text{gate}}, \quad t_0^{\text{gate}}, t_{N^{\text{gate}}}^{\text{gate}} \text{ fixed}, \quad i \in \{0, \dots, N^{\text{gate}} - 1\} \end{aligned} \quad (3.62)$$

is solved by gradient descent with backtracking line search.

The two optimization steps are executed iteratively until the cost of the first optimization problem converges. Then, the trajectory is temporally and spatially redimensionalized and temporally scaled to adhere to the user-specified maximum values in terms of speed $\check{v}_{\text{max}}^{\text{gt}}$, thrust $\check{a}_{\text{max}}^{\text{gt}}$ and roll-pitch rate $\check{\omega}_{\text{max}}^{\text{gt}}$ along the trajectory. For later use, the expert system samples the positions and speeds of the global trajectory

$$\left(\mathbf{g}_{\underline{p}}^{\text{gt}} \right)_{i \in \{0, \dots, N^{\text{gt}} - 1\}}, \quad \left(\mathbf{g}_{\underline{v}}^{\text{gt}} \right)_{i \in \{0, \dots, N^{\text{gt}} - 1\}} \quad (3.63)$$

with $\mathbf{g}_{\underline{v}}^{\text{gt}} = \left\| \mathbf{g} \dot{\underline{p}}^{\text{gt}} \right\|_2$. The sampling occurs at the user-specified frequency \check{f}^{gt} , which results in $N^{\text{gt}} = \check{f}^{\text{gt}} \cdot (t_{N^{\text{gate}}}^{\text{gate}} - t_0^{\text{gate}})$ samples.

R2 If the drone is closer to the currently targeted gate than a user-specified distance

$$\left\| \mathbf{g}_{\underline{p}_{i_{\text{target}}^{\text{gate}}}}^{\text{gate}} - \mathbf{g}_{\underline{p}}^{\text{d}} \right\|_2 < d^{\text{d-gate}}, \quad (3.64)$$

increment the index to the currently targeted gate

$$i^{\text{gate}} \leftarrow (i^{\text{gate}} + 1) \bmod N^{\text{gate}}. \quad (3.65)$$

R3 If the planning module's waypoint (**F1**) computed based on the ANN module's latest navigation decision, is more distant from the global trajectory (**R1**) than a

⁸<https://www.gurobi.com/>, visited on 20/08/2022

user-specified margin scaled by the the user-specified drone's maximum speed, i.e.,

$$\operatorname{argmin}_{i \in \{0, \dots, N^{\text{gt}} - 1\}} \left\| \mathbf{G}\underline{p}_{\text{wp}}^{\text{ann}} - \mathbf{G}\underline{p}_i^{\text{gt}} \right\|_2 > \check{d}_{\text{max}}^{\text{wp-gt}} \cdot \frac{\check{v}_{\text{max}}^{\text{d}} + 1}{5}, \quad (3.66)$$

the expert system is required to intervene with its own navigation decision.

R4 Update the index $i_{\text{proj}}^{\text{gt}} \in \{0, \dots, N^{\text{gt}} - 1\}$ to the projection state, i.e., the state of the global trajectory onto which the drone's latest position estimate is projected, with the following iterative method. Figure 3.4 schematically illustrates the method with a 2D example.

1. Compute the index to the previous state of the global trajectory, by decrementing the index to the projection state

$$i_{\text{prev}}^{\text{gt}} = (i_{\text{proj}}^{\text{gt}} - 1 + N^{\text{gt}}) \bmod N^{\text{gt}}. \quad (3.67)$$

2. Starting from the previous state, compute the vector to the projection state

$$\mathbf{G}\underline{a} = \mathbf{G}\underline{p}_{i_{\text{proj}}^{\text{gt}}}^{\text{gt}} - \mathbf{G}\underline{p}_{i_{\text{prev}}^{\text{gt}}}^{\text{gt}} \quad (3.68)$$

and the vector to the current drone position

$$\mathbf{G}\underline{b} = \mathbf{G}\underline{p}^{\text{d}} - \mathbf{G}\underline{p}_{i_{\text{prev}}^{\text{gt}}}^{\text{gt}}. \quad (3.69)$$

3. If the scalar product of the vectors $\mathbf{G}\underline{a}$ and $\mathbf{G}\underline{b}$, both normalized by the length of $\mathbf{G}\underline{a}$, is less than 1

$$\frac{\mathbf{G}\underline{a} \cdot \mathbf{G}\underline{b}}{\mathbf{G}\underline{a} \cdot \mathbf{G}\underline{a}} < 1, \quad (3.70)$$

go to the next step. Else, increment the index to the projection state

$$i_{\text{proj}}^{\text{gt}} \leftarrow (i_{\text{proj}}^{\text{gt}} + 1) \bmod N^{\text{gt}} \quad (3.71)$$

and go back to step 1.

4. If the drone is within a user-specified distance to the projection state

$$\left\| \mathbf{G}\underline{p}^{\text{d}} - \mathbf{G}\underline{p}_{i_{\text{proj}}^{\text{gt}}}^{\text{gt}} \right\|_2 \leq \check{d}^{\text{d-proj}}, \quad (3.72)$$

the index $i_{\text{proj}}^{\text{gt}}$ to the projection state is found. Else, set the index to the state of the global trajectory which has the minimum distance to the current drone position

$$\operatorname{argmin}_{i_{\text{proj}}^{\text{gt}}} \left\| \mathbf{G}\underline{p}^{\text{d}} - \mathbf{G}\underline{p}_{i_{\text{proj}}^{\text{gt}}}^{\text{gt}} \right\|_2. \quad (3.73)$$

Due to this step, the expert system does not require to know the initial index to the projection state.

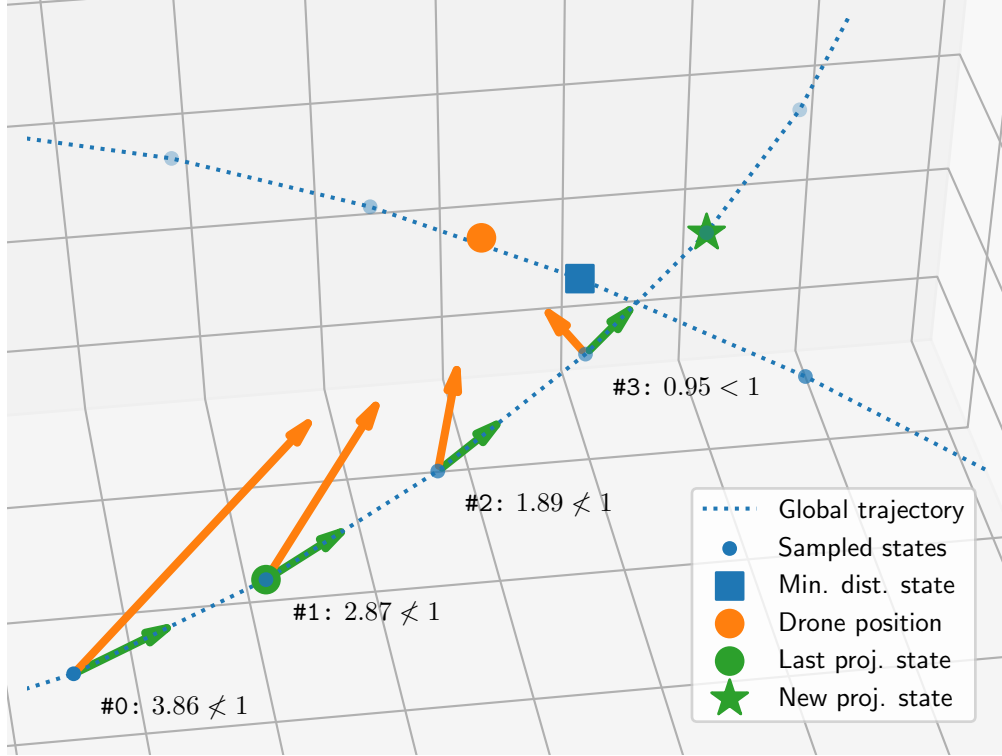


Figure 3.4: Schematic example of the update of the projection state index (**R4**). Known are: the positions (blue points) sampled from the global trajectory (blue dotted line), the last index to the projection state (green circle) and the current position of the drone (orange circle). At an iteration, the vector from the previous to the projection state (green arrows, equ. 3.68) and the vector from the previous to the drone position (orange arrows, equ. 3.69) are computed. Then, the normalized dot product criterion (annotations, equ. 3.70) is checked. For iteration #0-2, the criterion is not met. Thus, the index to the projection state is incremented and another iteration is started. At iteration #3 the criterion is met and the new index to the projection state (green star) is identified (assuming the distance criterion (equ. 3.72) is also met). Note that finding the index to the projection state only with minimum distance (equ. 3.73) would have failed here, since the so indexed state (blue square) belongs to a later or earlier part of the global trajectory which only intersects the current part.

R5 Update the index $i_v^{\text{gt}} \in \{0, \dots, N^{\text{gt}} - 1\}$ to the speed state, i.e., the state of the global trajectory that is the reference for the normalized speed $\tilde{v}_{\text{des}}^{\text{exp}}$ component of the expert system's navigation decision, by finding the first state of the global trajectory that follows the projection state with a specific distance.

1. Initialize the searched index with the index to the projection state

$$i_v^{\text{gt}} = i_{\text{proj}}^{\text{gt}}. \quad (3.74)$$

2. Increment the searched index

$$i_v^{\text{gt}} \leftarrow (i_v^{\text{gt}} + 1) \bmod N^{\text{gt}}. \quad (3.75)$$

3. If the speed state is further from the projection state than a user-specified distance

$$\left\| \mathbf{G}\underline{p}_{i_v^{\text{gt}}}^{\text{gt}} - \mathbf{G}\underline{p}_{i_{\text{proj}}^{\text{gt}}}^{\text{gt}} \right\|_2 > \check{d}^{\text{proj-v}}. \quad (3.76)$$

the searched index is found. Else, go back to step 2.

R6 Update the index $i_{\text{wp}}^{\text{gt}} \in \{0, \dots, N^{\text{gt}} - 1\}$ to the waypoint state, i.e., the state of the global trajectory that is the reference for the image waypoint $\mathbf{l}_{\text{wp}}^{\text{exp}}$ component of the expert system's navigation decision, by finding the first state of the global trajectory that follows the projection state with a distance to be computed.

1. Set the distance from the projection to the waypoint state to the distance from the drone to the closer of either the currently or lastly targeted gate. However, a user-specified distance constitutes the lower limit

$$d^{\text{proj-wp}} = \max \left(\check{d}_{\min}^{\text{proj-wp}}, \argmin_i \left\| \mathbf{G}\underline{p}_i^{\text{gate}} - \mathbf{G}\underline{p}^{\text{d}} \right\|_2 \right), \quad (3.77)$$

$$i \in \{i_{\text{target}}^{\text{gate}}, (i_{\text{target}}^{\text{gate}} - 1 + N^{\text{gate}}) \bmod N^{\text{gate}}\}. \quad (3.78)$$

2. Initialize the searched index with the index to the projection state

$$i_{\text{wp}}^{\text{gt}} = i_{\text{proj}}^{\text{gt}}. \quad (3.79)$$

3. Increment the searched index

$$i_{\text{wp}}^{\text{gt}} \leftarrow (i_{\text{wp}}^{\text{gt}} + 1) \bmod N^{\text{gt}}. \quad (3.80)$$

4. If the waypoint state is further from the projection state than the distance computed in step 1

$$\left\| \mathbf{G}\underline{p}_{i_{\text{wp}}^{\text{gt}}}^{\text{gt}} - \mathbf{G}\underline{p}_{i_{\text{proj}}^{\text{gt}}}^{\text{gt}} \right\|_2 > d^{\text{proj-wp}}, \quad (3.81)$$

the searched index is found. Else, go back to step 3.

R7 Compute the normalized speed component of the expert system's navigation decision as the sampled speed of the speed state normalized by the maximum speed of the global trajectory

$$\tilde{v}_{\text{des}}^{\text{exp}} = \frac{\mathbf{G}v_{i_v}^{\text{gt}}}{\underset{i \in \{0, \dots, N^{\text{gt}}-1\}}{\text{argmax}} \left\| \mathbf{G}v_i^{\text{gt}} \right\|_2} \in [0, 1]. \quad (3.82)$$

R8 Compute the image waypoint component of the expert system's navigation decision by applying the transformation from the global to the image reference system (see equ. 3.14) on the sampled position of the waypoint state

$$\mathbf{p}_{\text{wp}}^{\text{exp}} = T_{\text{IG}} \left(\mathbf{p}_{i_{\text{wp}}}^{\text{gt}} \right). \quad (3.83)$$

Inference Engine

The inference engine of the expert system is only activated during training data generation. Figure ?? shows the related interaction of the inference engine within the autonomous navigation method. Internally, the inference engine runs the following schedule.

Before the drone starts to fly, the inference engine pre-computes the global trajectory (**R1**) and samples the position and speeds. During the flight, it constantly update the currently targeted gate index (**R2**). Whenever the planning module has computed a global waypoint on the basis of the latest ANN navigation decision, the inference engine checks whether it must intervene (**R3**). If so, the engine updates its indices to relevant states of the global trajectory (**R4-6**) and makes its own navigation decision (**R7-8**). Finally the engine sends its navigation decision to the planning module for processing.

3.6 Racing vs. Training Data Generation

Chapter 4

Experiments in Simulation

4.1 Simulation Setup

The experiments in this thesis are conducted in a drone racing simulation, which includes the environment, the racetrack consisting of race gates and the drone. The implementation of the simulation (see figure 4.1) is separated into physics modeling and image rendering.

For a physics modeling of high accuracy, the Gazebo¹ simulator with the RotorS [16] plugin is deployed. The modeling includes the dynamics of the drone under the actuation with inputted motor speed commands and possible collisions of the drone with the racetrack gates. Further, the RotorS plugin provides the drone state estimate, the motor speeds estimate and the data from the onboard IMU as output.

For an almost photo-realistic image rendering, the Flightmare [55] simulator is de-

¹<https://gazebo-sim.org/home>, visited on 18/08/2022

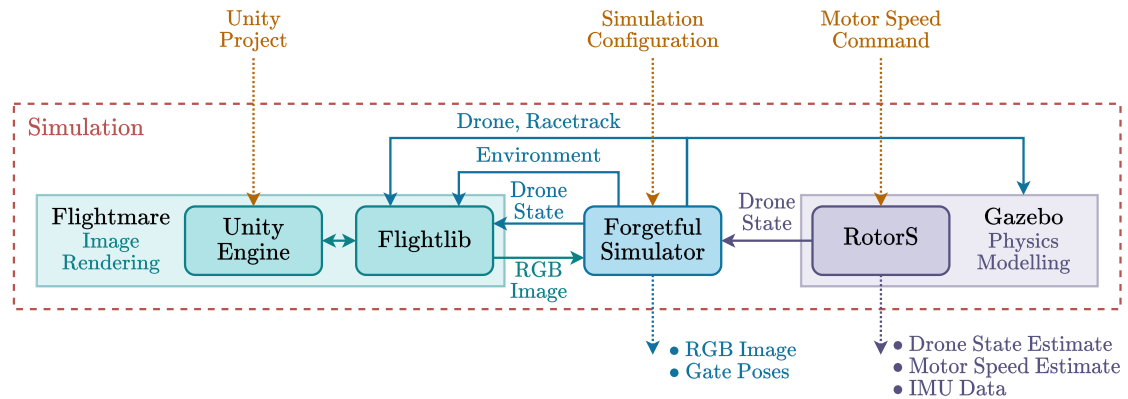


Figure 4.1: Implementation concept of the simulation

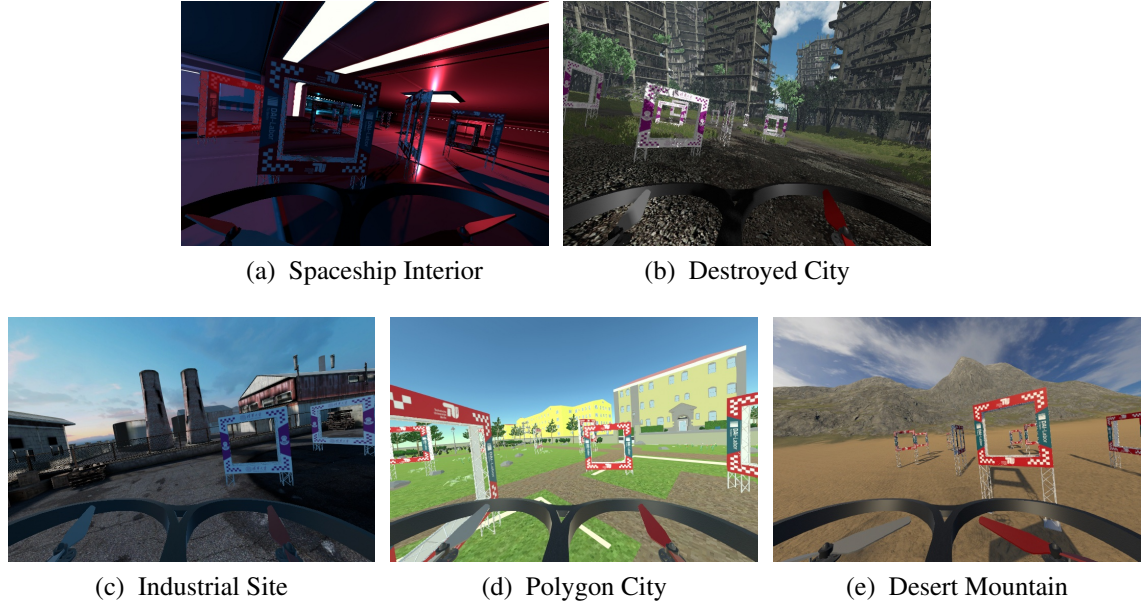


Figure 4.2: Scenes available in simulation

ployed. Upon request, the Flightlib interface updates the drone pose within the Unity² Engine and fetches an RGB image from the drone’s onboard camera. Before running the simulation, the Unity Engine is built from a Unity project that bases on the RPG Flightmare Unity Project³. The Unity project of this thesis entails five scenes named spaceship interior⁴, destroyed city⁵, industrial site⁶, polygon city⁷ and desert mountain⁸ (see figure 4.2). Within each scene, there are three sites (A, B, C) to place a racetrack. For the racetrack, two different gate types are provided: the first with TU Berlin/DAI-Labor logos and the second with Tsinghua University/DME logos (see figure 4.3).

The Forgetful Simulator node takes on two tasks. First, it synchronizes the drone state in the Flightmare simulator with the ground-truth state in the Gazebo simulator and provides the RGB images fetched from the Flightmare simulator as as output. Second, the node sets up the simulation according to the inputted simulation configuration.

A simulation configuration includes the environment and the racetrack configuration. The environment configuration specifies the scene and the site. The racetrack configuration specifies the racetrack type, the racetrack generation, the racetrack direc-

²<https://unity.com/>, visited on 20/08/2022

³https://github.com/uzh-rpg/flightmare_unity, visited on 20/08/2022

⁴based on "3D Free Modular Kit" from the Unity Asset Store

⁵based on "Destroyed City FREE" from the Unity Asset Store

⁶based on "RPG/FPS Game Assets for PC/Mobile (Industrial Set v2.0)" from the Unity Asset Store

⁷based on "CITY package" from the Unity Asset Store

⁸based on "Free Island Collection" from the Unity Asset Store

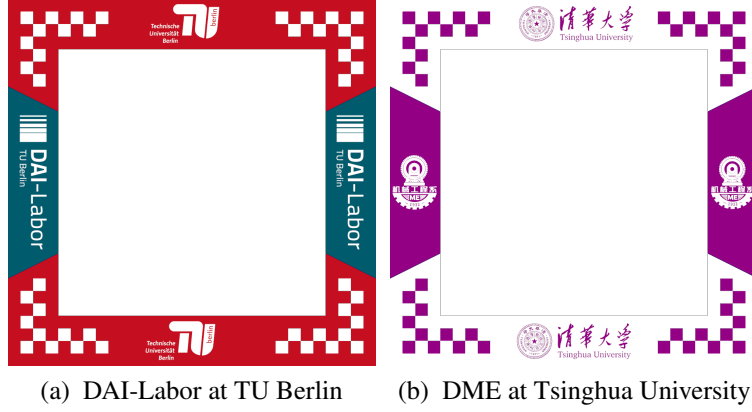


Figure 4.3: Race gates available in simulation

tion and the racetrack gates. Table 4.1 shows all available options for the simulation configuration. The Forgetful Simulator node stores the gate poses for both deterministic

Table 4.1: Available options for the simulation configuration

Simulation	Environment	Scenes	Spaceship interior, destroyed city, industrial site, polygon city, desert mountain
		Sites	A, B, C
	Racetrack	Types	Figure-8, gap
		Generations	Deterministic, randomized
		Directions	Counterclockwise, clockwise
		Gates	TUB-DAI, THU-DME

and counterclockwise racetrack types (see table 4.2). If specified, these poses are randomized and redirected from counterclockwise to clockwise as illustrated in figure 4.4. The racetrack randomization includes the following steps.

1. Sample the y -position values of the gates #3-6 from the uniform real distribution over the intervals specified in table 4.2. This step only applies to the gap racetrack type as it explicitly randomizes the gap distance.
2. Shift the gate positions along the x -, y - and z -axis by a value, which is sampled independently for each gate and axis from the uniform real distribution over the user-specified interval $[-\check{d}_{\text{shift,max}}^{\text{sim}}, \check{d}_{\text{shift,max}}^{\text{sim}}]$.
3. Scale the gate positions by a value, which is sampled once for all gates from the uniform real distribution over the user-specified interval $[\check{d}_{\text{shift,min}}^{\text{sim}}, \check{d}_{\text{shift,max}}^{\text{sim}}]$.

4. Twist the gate yaw-orientations by a value, which is sampled independently for each gate from the uniform real distribution over the user-specified interval $\left[-\check{d}_{\text{twist,max}}^{\text{sim}}, \check{d}_{\text{twist,max}}^{\text{sim}}\right]$.

After processing the racetrack configuration, the Forgetful Simulator node computes the start position of the drone so that the drone is located between the second last and the last gate and faces towards the last gate. Then, the node loads the environment configuration in the Flightmare Simulator and spawns the drone model and the race gate models of the specified type at the computed poses in both, the Flightmare and the Gazebo simulator. Finally, the node outputs the computed gate poses. This information is required to compute the global trajectory of the expert system (see section 3.5) and to automatically update the drone's progress on the racetrack whenever the drone has passed the currently targeted race gate.

Table 4.2: Deterministic gate poses

Racetrack	Gate	x	y	z	yaw
Figure-8	0	-20.45	-8.65	2.0	1.13
	1	-12.55	-11.15	2.0	-1.57
	2	-4.15	-5.35	2.0	-0.60
	3	3.45	4.25	2.0	-0.63
	4	11.95	11.15	2.0	-1.21
	5	21.85	6.85	2.0	0.99
	6	24.25	-1.75	2.0	0.00
	7	19.25	-9.55	2.0	-1.03
	8	10.55	-10.65	2.0	1.53
	9	2.85	-5.95	2.0	0.57
	10	-4.95	4.65	2.0	0.67
	11	-12.95	9.65	2.0	-1.53
	12	-21.05	6.65	2.0	-0.77
	13	-24.25	-1.00	2.0	0.07
Gap	0	-20.45	-8.65	2.0	1.13
	1	-12.55	-11.15	2.0	-1.57
	2	-4.15	-9.35	2.0	-1.0
	3	4.85	[-4.95, -5.95]	2.0	-1.4
	4	16.95	[-2.25, -5.25]	2.0	1.57
	5	16.95	[2.25, 5.25]	2.0	1.57
	6	5.45	[4.45, 5.45]	2.0	1.4
	7	-4.95	7.95	2.0	1.2
	8	-12.95	9.65	2.0	-1.53
	9	-21.05	6.65	2.0	-0.77
	10	-24.25	-1.0	2.0	0.07

4.2 Imitation learning process of the ANN Module

The ANN module of the autonomous navigation method must first learn to make meaningful navigation decisions. In this thesis as well as in the baseline work, this task is viewed as an imitation learning problem. The goal is that the ANN module learns to mimic the navigation decision making demonstrated by the expert system of section 3.5. The problem is addressed with dataset aggregation, which is a type of interactive direct policy learning (see section 2.2). In the learning process, rollouts to generate additional training data alternate with supervised trainings of the ANN module on the aggregated dataset. During a rollout, the drone navigates through a racetrack based on the navigation decisions of the ANN module. Whenever the ANN module makes a navigation decision that would cause the drone to deviate too far from the expert’s global trajectory through the racetrack, the interactive expert system intervenes and provides an expert navigation decision that is executed instead. Also, a training sample labeled with the expert navigation decision is added to the training dataset so that, during training, the ANN module can learn from the mistakes made during rollout.

The user specifies the learning configuration for the individual ANN module variant, which includes the rollout and the training configuration. The rollout configuration comprises a set \mathcal{S} of simulation configurations (see table 4.1), a set \mathcal{V} of maximum drone speeds (see equ. 3.46) and a set \mathcal{E} of pairs of margins and thresholds for the expert intervention share (hereafter referred to as margin-threshold pairs). A margin determines the distance of the drone from the global trajectory above which the expert intervenes. The threshold determines the share of expert navigation decisions in the total navigation decisions of a rollout, below which a rollout configuration is considered sufficiently learned. The training configuration comprises the sequence length of the training samples aggregated during rollout (which must be one if the individual ANN module is not recurrent), the number of epochs after each rollout, the batch size, the loss function, the optimizer type and the scheduling of the learning rate.

Table 4.3: Learning configuration

Learning	Rollout	Simulation configurations \mathcal{S}
		Max. drone speeds \mathcal{V}
		Margin-threshold pairs \mathcal{E}
	Training	Sequence length \tilde{N}^{seq}
		Number of Epochs \tilde{N}^{epoch}
		Batch size \tilde{N}^{batch}
		Loss
		Optimizer
		Learning rate

In detail, the learning process proceeds in the following steps.

- For every margin-threshold pair (M, T) in \mathcal{E}
 - For every simulation configuration S in \mathcal{S}
 - For every maximum drone speed V in \mathcal{V}
1. Process and load S in the simulation.
 2. Set the maximum drone speed $\check{v}_{\max}^d = v$ of the planning module.
 3. Compute the expert's global trajectory through the racetrack.
 4. Roll out the ANN module with the interactive expert system for one round on the racetrack. At the user-specified main frequency \check{f}^{main} , the following steps are taken.
 - (a) The latest data from the onboard sensors is preprocessed to a single (non-sequential) input. (Which sensor data is included depends on the configuration of the individual ANN module.)
 - (b) The ANN module processes the single input to make a navigation decision. (If the individual ANN module is recurrent, it can still make temporal connections because the single inputs incoming at the frequency \check{f}^{main} constitute a time series.)
 - (c) The planning module computes the local trajectory for the ANN navigation decision.
 - (d) If the end position of the local trajectory is more distant from the expert's global trajectory than M :
 - i. The expert system intervenes by making a navigation decision based on its knowledge.
 - ii. The planning module re-computes the local trajectory for the expert navigation decision.
 - (e) The local trajectory is forwarded to the control stack, which tracks it at a higher frequency than \check{f}^{main} .
 5. For every expert intervention of the latest rollout, add a sample to the training dataset. A sample comprises an expert navigation decision as a label and the corresponding sequence of inputs for the individual ANN module variant. The sequence starts \check{N}^{seq} timesteps of duration $1/\check{f}^{\text{main}}$ back in time and ends at the time step where the expert made the navigation decision. Record the share of the expert navigation decisions in the total (expert and ANN) navigation decisions made during the rollout.

6. Train the ANN module on the aggregated training dataset with supervised learning. The number of epochs \check{N}^{epoch} , the batch size \check{N}^{batch} , the loss function, the optimizer and the learning rate scheduling are specified in the training configuration. (For a recurrent ANN module, the samples of the training dataset are usually sequential. The ANN module then operates in many-to-one mode, whereby only the navigation decision from the processing of the last input of the input sequence is used to calculate the loss.)
7. If the recorded expert intervention share (from step 5) is greater than T , go back to step 1. Else the current (M, T) - S - V combination in the rollout configuration is considered as sufficiently learned by the ANN module.

4.3 Racing Tests

After an ANN module variant completed the imitation learning process, its racing performance is tested. To do this, the ANN module variant is rolled out with the expert system deactivated. From records made during the rollout, the variant's racing performance is evaluated.

The user specifies the testing configuration (see table 4.4), which includes a set of simulation configurations, a set of maximum drone speeds, and the number \check{N}^{rep} of rollout repetitions for a given combination of simulation configuration and maximum drone speed. In order to ensure comparability of the racing performance of different ANN module variants while also using randomized racetracks, \check{N}^{rep} randomized race-tracks are pre-computed for every possible simulation configuration (see table 4.1).

Table 4.4: Testing configuration

Testing	Simulation configurations \mathcal{S}
	Max. drone speeds \mathcal{V}
	number of repetitions \check{N}^{rep}

In detail, the racing tests are conducted as follows.

- For every simulation configuration S in \mathcal{S}
 - For every maximum drone speed V in \mathcal{V}
 - For every repetition N in \mathcal{N}
1. Load S with the N -th pre-computed racetrack for S in the simulation.
 2. Set the maximum drone speed $\check{v}_{\text{max}}^{\text{d}} = v$ of the planning module.

3. Roll out the ANN module for one round on the racetrack. At the user-specified main frequency \check{f}^{main} , the following steps are taken.
 - (a) Record the time-stamped position of the drone.
 - (b) The latest data from the onboard sensors is preprocessed to a single (non-sequential) input. (Which sensor data is included depends on the configuration of the individual ANN module.)
 - (c) The ANN module processes the single input to make a navigation decision. (If the individual ANN module is recurrent, it can still make temporal connections because the single inputs incoming at the frequency \check{f}^{main} constitute a time series.)
 - (d) The planning module computes the local trajectory for the ANN navigation decision.
 - (e) The local trajectory is forwarded to the control stack, which tracks it at a higher frequency than \check{f}^{main} .
4. Record if the drone, during the latest rollout, completed the racetrack by traversing all gates without crashing.

The recordings allow the race performance of an ANN module variant to be evaluated. On the basis of the racetrack completion records, a variant's racetrack completion share, on a set of simulation configurations depending on the maximum drone speed can be calculated. The racetrack completion share quantifies the robustness of a variant's navigation decision making for a given setup. The time-stamped drone position records of the rollouts reproduce the flight trajectories induced by a variant. The optimality with respect to jerk and snap of these trajectories and therewith the variant's navigation decision making can be quantified with the loss functions of the optimization problem formulations of the global and the local trajectory (see equ. 3.61 and 3.52).

4.4 Experiment 1

Experiment 1 studies the racing performance of several feedforward and recurrent ANN module variants on the randomized, counterclockwise figure-8 racetrack for varying maximum drone speeds. Table 4.5 shows the configurations of the variants examined in this experiment. Table 4.6 shows the learning configuration for the variants examined in this experiment. The variant's learning process **and the racing tests** of this experiment **are** limited to a single simulation environment, i.e., spaceship interior - A,

for the learning process is limited to a single site in a single scene, i.e., spaceship interior - A, due to the high time expenditure of the process. Thus, this experiment only compares the variants in terms of their ability to generalize to the randomized

Table 4.5: ANN Module Variants of Experiment 1

			Feedforward		Recurrent		
			F1	F2	R1	R2	R3
ANN	CNN	Input	240x160 RGB				
		Model	Resnet8	Resnet14			
		Pretrained	No				Yes
		Trainable	Yes				Partly
	CAT	Opt. Input	None			All	None
	GRU	# Layers	None		3		
		Hidden size			64		
		Dropout			0.00346		
	FC	# Layers	3		None		
		Width	256				
		dropout	0.206299				
		Activation	ReLU				
	HEAD	Activation	ReLU				
		Output	Navigation decision				

figure-8 racetrack located in a fixed simulation environment. It does not provide insights regarding the generalization to simulation environments not seen in the learning process.

Table 4.7 shows the variants' number of trainable parameters and number of multiply-accumulate (MAC) operations performed during a single inference, both obtained with torchinfo⁹.

All variants have in common that first, the CNN submodule inputs 240x160 preprocessed RGB images from the drone's onboard camera. Second, the HEAD submodule is a ReLU-activated, fully-connected layer that outputs navigation decisions. And third, the resultant dropout probability is 50 %. For a variant that during inference applies dropout x times with the same dropout probability and that trains on samples with the input sequence length y , the dropout probability at a single application is

$$p = 1 - \sqrt[x]{0.5}. \quad (4.1)$$

The two feedforward variants are characterized by their deactivated GRU submodule and their FC submodule, which consists of three ReLU-activated, dropout-subjected, fully-connected layers with a width of 256 neurons. The first feedforward variant (F1) is a slightly extended version of the ANN deployed in the baseline autonomous navigation method of Kaufmann et. al. [29]. The CNN submodule of the F1 variant is, like the baseline, implemented with an 8-layer Resnet. Unlike the baseline, its FC submodule

⁹<https://github.com/TylerYep/torchinfo>, visited on 18/08/2022

Table 4.6: Learning configuration of Experiment 1

				Feedforward		Recurrent		
				F1	F2	R1	R2	R3
Learning	Rollout	Environ-ments	Scenes	Spaceship interior				
			Sites	A				
		Race-tracks	Types	Figure-8				
			Generations	Randomized				
			Directions	Counterclockwise				
			Gates	TUB-DAI, THU-DME				
		Max. drone speeds		4, 5, 6, 7, 8, 9, 10 m/s				
		Margin-threshold pairs		(0.5, 10), (0.75, 5), (1.0 m, 1 %)				
	Training	Sequence length		1		25		
		# Epochs		10		3		
		Batch size		256	32	8		
		Loss		SmoothL1Loss				
		Optimizer		ADAM				
		Learning rate		Exponential: $0.0001 * 0.95^{\text{epoch}}$				

has three instead of one layer. This extension adjusts the F1 variant to the other examined variants in terms of the number of trainable parameters of the FC/GRU submodule in order to increase the variants' comparability. The second feedforward variant (F2) differs from the F1 variant only in the CNN submodule as it uses a 14-layer instead of a 8-layer Resnet. Preliminary experiments (not documented here) suggested that more complex Resnets than the one used in the baseline work yield significantly better results. The Resnet14 was chosen for the F2 variant because it represents a good compromise in terms of the increase in trainable parameters, thus keeping the variant's memory occupation and training duration within tolerable limits. In this experiment, the comparison between the F1 and F2 variant aims to investigate the influence of the CNN complexity on a variant's racing performance.

The three recurrent variants are characterized by their deactivated FC submodule and their GRU submodule, which consist of three layers with a hidden size of 64, of which the second and the third layer are subjected to dropout. All three variants use the Resnet14 because the F2 variant performs significantly stronger (see results in section ??). **recurrent with resnet8 not converged** For a resultant dropout probability of 50 % at inference, equation ?? with $x = 2$ and $y = 25$ yields the dropout probability at single application shown in table 4.5. The first recurrent variant (R1) is the recurrent equivalent of the feedforward F2 variant. The comparison between the F2 and R1 variant, thus, aims to investigate the impact of the GRU submodule's temporal comprehension on a variant's racing performance. The second recurrent variant (R2) differs from the R1

Table 4.7: Numbers of trainable parameters (TP) and multiply-accumulate operations (MAC) of the ANN module variants of experiment 1 in the format $men = m \times 10^n$. Note that, the table for the R3 variant does not reflect the negligible number of single trainings in the learning process where the CNN parameters are momentarily trainable.

ANN	#	F1	F2	R1	R2	R3
CNN	TP	309e3	2.78e6	2.78e6	2.78e6	0
	MAC	52.9e6	1.07e9	1.07e9	1.07e9	1.07e9
GRU	TP	0	0	112e3	113e3	112e3
	MAC	0	0	112e3	112e3	112e3
FC	TP	164e3	197e3	0	0	0
	MAC	164e3	197e3	0	0	0
HEAD	TP	771	771	195	195	195
	MAC	771	771	195	195	195
Total	TP	474e3	2.98e6	2.89e6	2.90e6	112e3
	MAC	53.1e6	1.07e9	1.07e9	1.07e9	1.07e9

variant with respect to the CAT submodule. While the CAT submodule for R1 is deactivated, for R2 it introduces all available optional inputs (see section) into the variant’s decision making. The comparison of R1 and R2, thus, aims to investigate the impact of the optional inputs on a variant’s racing performance. The third recurrent variant (R3) differs from R1 with respect to the CNN submodule. While the CNN submodule for R1 is trainable and not pretrained, for R2 it is pretrained and only partly trainable. **imagenet classifier not converged** The CNN submodule of R2 is pretrained with preliminary final layer on training data from preliminary experiments (**not documented here**) and only trainable at the single trainings whenever a margin-threshold pair is completed in the learning process. This significantly speeds up the training of R3.

To summarize: F1 represents the feedforward ANN of the baseline work. F2 integrates a 14-layer instead of an 8-layer Resnet. R1 is the recurrent counterpart of F2. R2 additionally uses the optional inputs. The CNN submodule of R3 is pretrained and trainable only partly in time.

Table 4.7 shows the number of trainable parameters and the number of multiply-accumulate (MAC) operations performed during a single inference, both obtained with torchinfo¹⁰. The number of trainable parameters determines the degree of freedom of a variant’s architecture to fit the training data, which can correlate with how well the variant performs at training and eventually at racing. Furthermore, it is a platform-independent indicator of how memory- and time-consuming the training of a variant is. The number of MAC operations is a platform-independent indicator of how time-

¹⁰<https://github.com/TylerYep/torchinfo>, visited on 18/08/2022

consuming the single inference of a variant is. As drones are highly limited in computation power and navigation decisions must be made at a relatively high frequency, the inference time of a variant is critical at racing. However, since the experiments of this thesis are only conducted in simulation on a desktop computer, whether a variant has a sufficiently small inference time cannot be examined.

Using the 8-layer or the 14-layer Resnet has by far the largest impact on the total number of both, parameters and MAC operations, of a variant. Compared to Resnet8, Resnet14 has approximately 9 times more parameters and performs approximately 20 times more MAC operations during a single inference. The F1 variant (from the baseline work) is the only variant using Resnet8 and has thus by far the lowest MAC number.

The CAT submodule is not listed in the table because it neither has parameters nor performs MAC operations. Care was taken to ensure that the GRU submodule of the three recurrent variants has fewer trainable parameters than the FC submodule of the two feedforward variants, in order to rule out the possibility that the recurrent variants perform better only because of a higher number of trainable parameters.

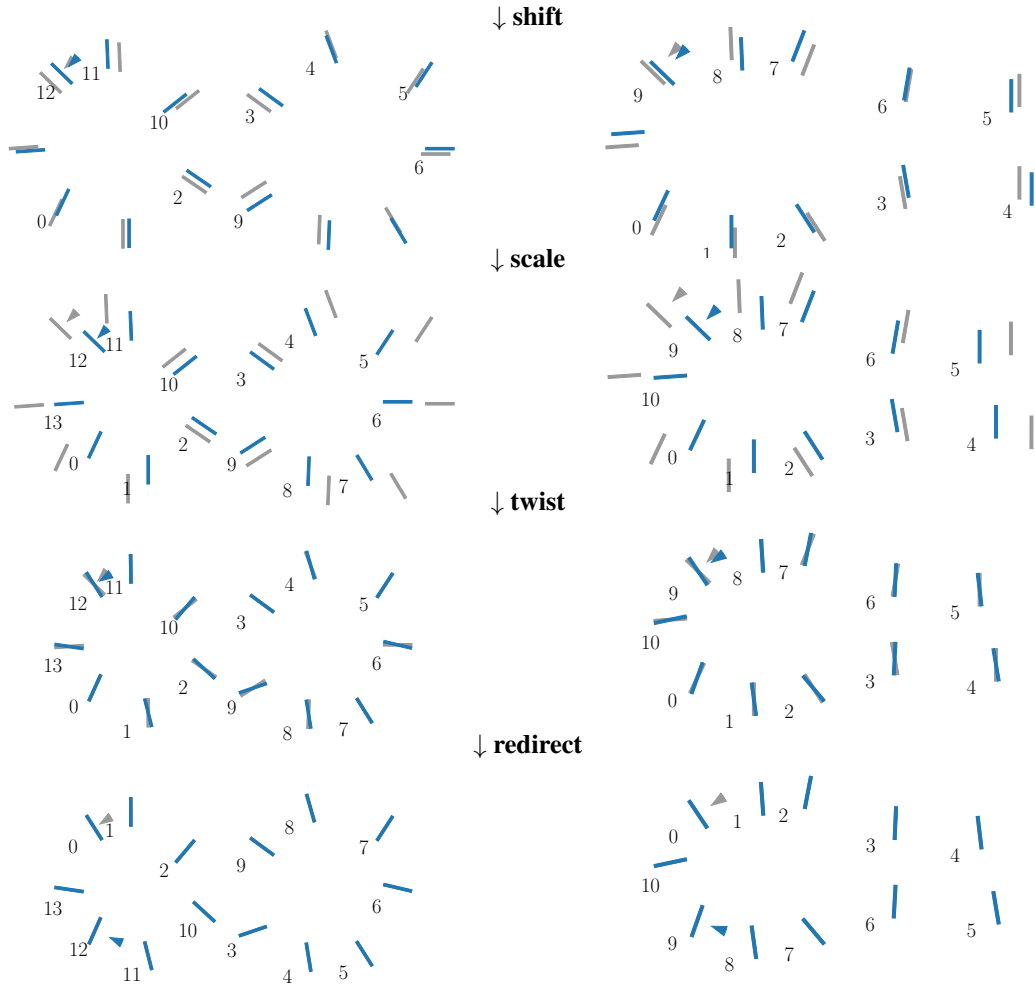


Figure 4.4: Racetrack randomization and redirection for the figure-8 (left) and the gap (right) racetrack type. In the xy-plane, the drone starting pose (arrow) and the gate poses (numbered bars) are shown before (grey) and after (blue) the individual processing step. The first randomization step, which is exclusive to the gap racetrack type, is not depicted.

Chapter 5

Evaluation

DELETEME: The evaluation chapter is one of the most important chapters of your work. Here, you will prove usability/efficiency of your approach by presenting and interpreting your results. You should discuss your results and interpret them, if possible. Drawing conclusions on the results will be one important point that your estimators will refer to when grading your work.

In a first step, this chapter presents the results of this thesis, i.e., the performance of the examined ANN submodule variants in the racing tests (see section ...). In a second step, the results are discussed.

5.1 Results

In order to compare the examined ANN module variants, the results of the imitation learning process and the racing tests are presented here.

5.2 Discussions

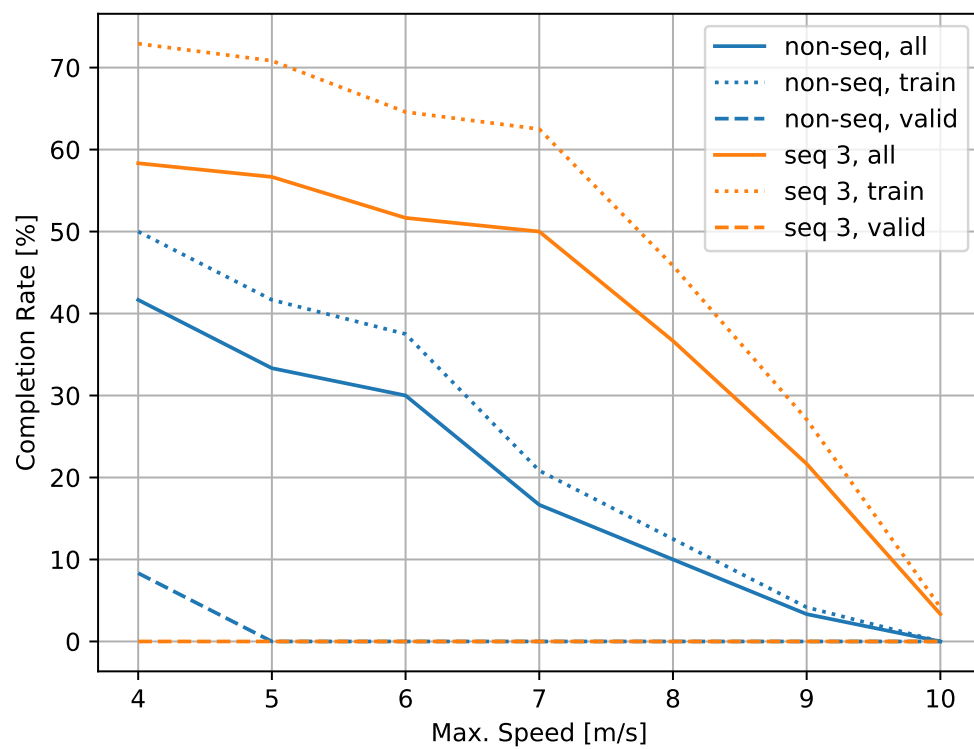


Figure 5.1: ???

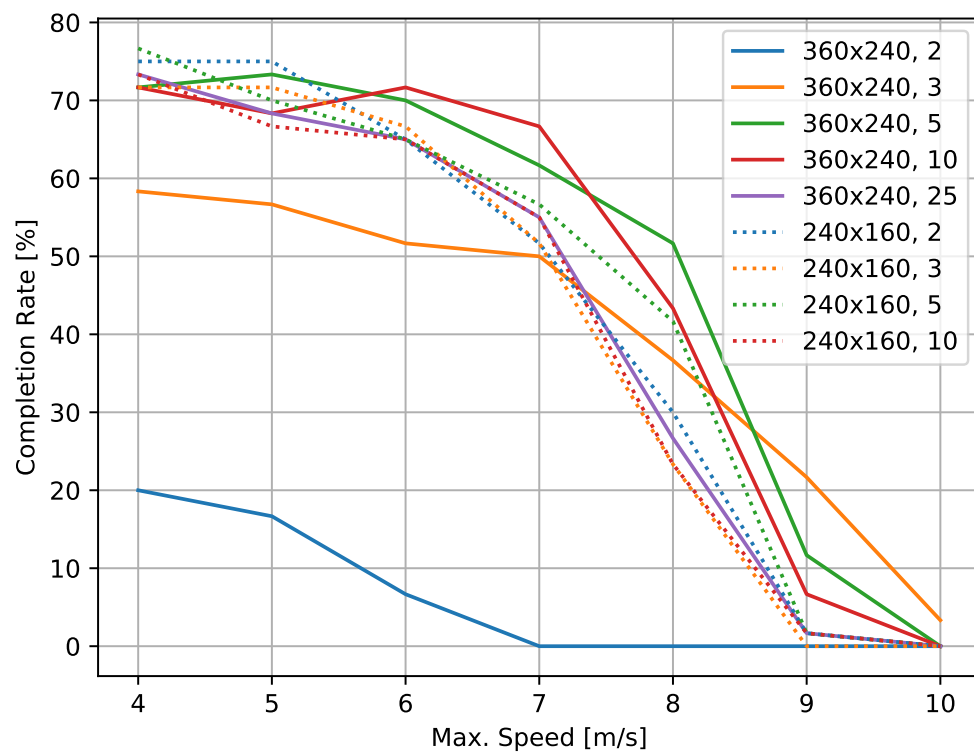


Figure 5.2: ???

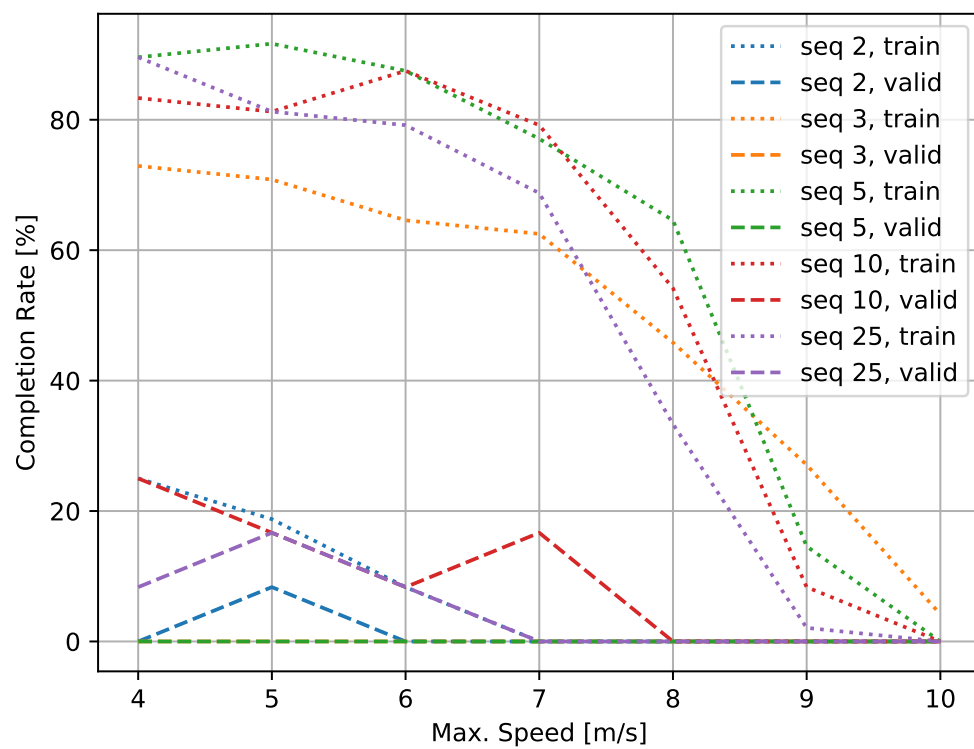


Figure 5.3: ???

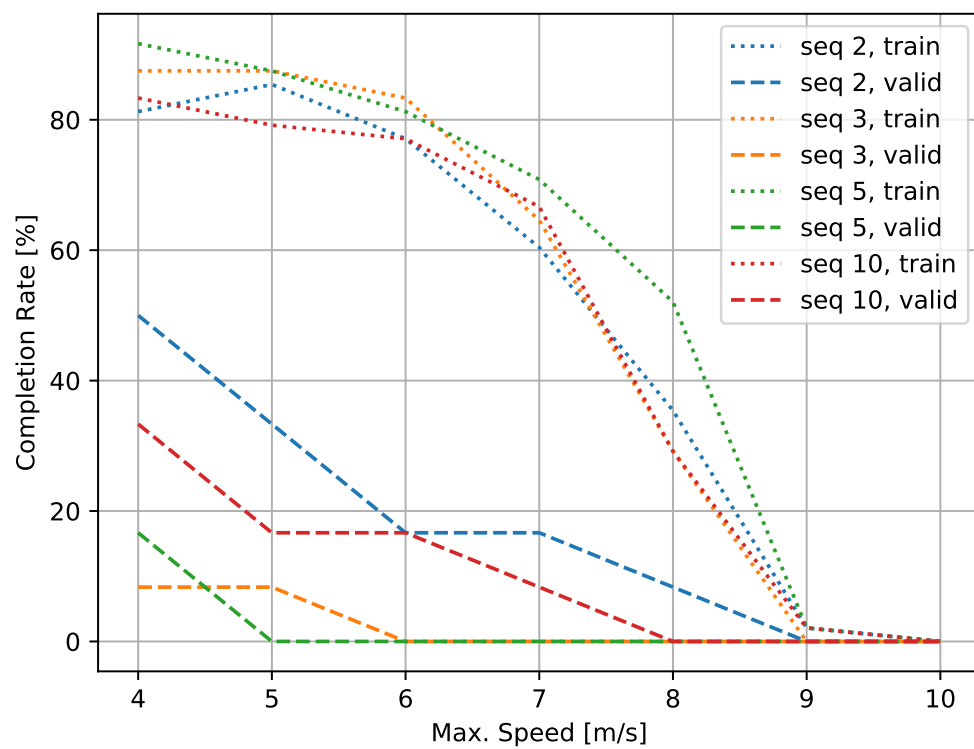


Figure 5.4: ???

Chapter 6

Conclusion and Future Work

6.1 Summary

DELETEME: put a plain summary of your work here. Summaries should be made of each Chapter beginning with Chapter 2 and ending with you evaluation. Just write down what you did and describe the corresponding results without reflecting on them.

6.2 Conclusion

DELETEME: do not summarize here. Reflect on the results that you have achieved. What might be the reasons and meanings of these? Did you make improvements in comparison to the state of the art? What are the good points about your results and work? What are the drawbacks?

6.3 Future Work

DELETEME: Regarding your results - which problems did you not solve? Which questions are still open? Which new questions arised? How should someone / would you continue working in your thesis field basing on your results?

- https://en.wikipedia.org/wiki/Gated_recurrent_unit#Content-Adaptive_Recurrent_Unit
- https://en.wikipedia.org/wiki/Gated_recurrent_unit#Architecture

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Appendices

DELETEME: everything that does not fit into your work, e.g. a 5 page table that breaks the reading flow, should be placed here

Appendix A: Abbreviations

AES	Advanced Encryption Standard (Symmetrisches Verschlüsselungsverfahren)
ASCII	American Standard Code for Information Interchange (Computer-Textstandard)
dpi	dots per inch (Punkte pro Zoll; Maß für Auflösung von Bilddateien)
HTML	Hypertext Markup Language (Textbasierte Webbeschreibungssprache)
JAP	Java Anon Proxy
JPEG	Joint Photographic Experts Group (Grafikformat)
JPG	Joint Photographic Experts Group (Grafikformat; Kurzform)
LED	Light Emitting Diode (lichtemittierende Diode)
LSB	Least Significant Bit
MD5	Message Digest (Kryptographisches Fingerabdruckverfahren)
MPEG	Moving Picture Experts Group (Video- einschließlich Audiokompression)
MP3	MPEG-1 Audio Layer 3 (Audiokompressionsformat)
PACS	Picture Archiving and Communication Systems
PNG	Portable Network Graphics (Grafikformat)
RSA	Rivest, Shamir, Adleman (asymmetrisches Verschlüsselungsverfahren)
SHA1	Security Hash Algorithm (Kryptographisches Fingerabdruckverfahren)
WAV	Waveform Audio Format (Audiokompressionsformat von Microsoft)

Appendix B: L^AT_EX Help

How to Use This Template

- Remove all of my text which is mostly labeled with DELETEME
- Change the information in the 00a_title_page.tex file
- Use the information written in this section
- Ask you supervizor to help you
- If I am not your supervizor and noone else can help you, write me an email (aubrey.schmidt@dai-labor.de)

Citations

Citing is one of the essential points you need to do in you thesis. Statements not basing on results of your own research¹ not being cited represent a breach on the rules of scientific working. Therefore, you every statement needs to be cited basing on information that other people can cross-check. A common way of citing in technical papers is:

- Oberheide et al. [?] state that the average time for an anti-virus enginge to be updated with a signature to detect an unknown threat is 48 days.

Note: et al. is used when the paper was written by more than two people. Check the code of this section to learn how to cite from a technical perspective.

Note: you can change the citation style in the `thesis.tex` file, e.g. to harvard style citations. Instructions on this can also be found in this file.

You should not cite anything that can be changed, e.g. it is not that good citing web pages since they might get updated changing the cited content. There are no clear quality measures on citing sources but aubrey believes that the following list is true for several cases, starting with highest quality:

1. Journal article or book
2. Conference paper
3. Workshop paper
4. Technical report
5. Master thesis

¹in what ever context

6. Bachelor thesis

7. General Web reference

There might be workshop papers that have a higher quality than some journal papers. Therefore this list only gives you a hint on possible quality measures. Another measure can be whether a paper was indexed by ACM/IEEE, although this is not a strong indicator.

Finding and Handling Citation Sources

Following resources are required for finding and handling articles, books, papers and sources.

- your primary resource will be `http://scholar.google.com`
- `http://www.google.com` might also be used
- `wikipedia.com` can be a good start for finding relevant papers on your topic
- you should download and install JabRef or a similar tool `http://jabref.sourceforge.net/`
- you should point JabRef to the `mybib.bib` file
- you should immediately enter a relevant paper to JabRef, additionally, you should write a short summary on it; else, you will do this work at least twice.

General Advices

- Do not take care of design, \LaTeX will do this for you. If you still feel that you need to take care of this, do this when you have finished writing, else you will end up in a lot of double and triple work.
- \LaTeX will do exactly that you will tell it to do. If you have problems with this, go for google or ask your supervisor
- use labels in order to be able to reference to chapters, section, subsections, figures, tables, etc. ...

General Commands

- `check` <http://en.wikibooks.org/wiki/LaTeX>
- `check` <http://www.uni-giessen.de/hrz/tex/cookbook/cookbook.html> **German**

Please also check the following source [?].

Code

This section shows you how to get your code into a \LaTeX document. See code for options.

```
1 class Beispiel{
2
3   public static void main(String args[]){
4
5     System.out.println("Hello_World");
6
7   }
8
9 }
```

```
1 class Beispiel{
2
3   public static void main(String args[]){
4
5     System.out.println("Hello World");
6
7   }
8
9 }
```

Listing 6.1: Example code is presented here

Figures

This section describes how to include images to your document. Information was taken from http://en.wikibooks.org/wiki/LaTeX/Floats,_Figures_and_Captions, visited on 05/08/2011. Please make sure to use original vector graphics as basis since image quality might be used as weak indicator for thesis quality. For this, try to find files in .SVG or .PDF format. Exporting a .PNG or .JPG to .PDF will not work since data was already lost while exporting it to these formats. This is the case for most Web graphics. Wikipedia startet entering most in images in .SVG which easily can be transformed to .PDF, but please do not forget proper citations.



Figure 6.1: Including an image; in this case a PDF. Please note that the caption is placed below the image.



Figure 6.2: See code for caption options: this is a long caption which is printed in the Text. Additionally, image size was increased



Figure 6.3: Placing images side by side using the subfig package. Space between the images can be adjusted.

Tables

Here, you will find some example tables. The tables were taken from <http://en.wikibooks.org/wiki/LaTeX/Tables>, visited on 05/08/2011. Table environment was added plus caption and label. For code, check `__help/latex_hinweise.tex`.

Table 6.1: Simple table using vertical lines. Note that the caption is always above the table! Please check code for finding the right place for the table label.

1	2	3
4	5	6
7	8	9

Table 6.2: Table using vertical and horizontal lines

7C0	hexadecimal
3700	octal
11111000000	binary
1984	decimal

Table 6.3: Table with column width specification on last column

Day	Min Temp	Max Temp	Summary
Monday	11C	22C	A clear day with lots of sunshine. However, the strong breeze will bring down the temperatures.
Tuesday	9C	19C	Cloudy with rain, across many northern regions. Clear spells across most of Scotland and Northern Ireland, but rain reaching the far northwest.

Table 6.4: Table using multi-column and multirow

Team sheet		
Goalkeeper	GK	Paul Robinson
Defenders	LB	Lucus Radebe
	DC	Michael Duberry
	DC	Dominic Matteo
	RB	Didier Domi
Midfielders	MC	David Batty
	MC	Eirik Bakke
	MC	Jody Morris
Forward	FW	Jamie McMaster
Strikers	ST	Alan Smith
	ST	Mark Viduka