TA Session 3

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1 Introduction

1.1 TA Information

TA: Chi-Yuan Fang

TA sessions: Tuesday 1:20 – 3:10 PM (SS 501)

Email: r09323017@ntu.edu.tw

Office hours: Friday 2:00 – 3:30 PM or by appointments (SS 643)

Class group on Facebook: Statistics (Fall 2020) and Econometrics (Spring 2021)

https://www.facebook.com/groups/452292659024369/

Because screens are not clear in SS 501, I will provide the link of live streaming in the group.

1.2 TA Sessions Schedule

Week	TA Sessions	Quiz	Content	Remind
1	02/23: No class			
2	03/02: Class 1		Function, Confidence Interval, T test	03/10 Turn in HW1
3	03/09: Class 2		Loops, Linear Model	03/10 Turn in HW1, 03/16 Quiz 1
4	03/16: Class 3	Quiz 1	OLS	03/24 Turn in HW2
5	03/23: Class 4			03/24 Turn in HW2, $03/30$ Quiz 2
6	03/30: Class 5	Quiz 2		04/14 Turn in HW3
7	04/06: No class			04/14 Turn in HW3
8	04/13: Class 6			04/14 Turn in HW3, $04/20$ Quiz 3
9	04/20: Class 7	Quiz 3		$04/28 \; \mathrm{Midterm}$
10	04/27: Class 8		Review and Q&A	04/28 Midterm , 05/05 Turn in HW4
11	05/04: Class 9			05/05 Turn in HW4, $05/11$ Quiz 4
12	05/11: Class 10	$\mathrm{Quiz}\ 4$		05/19 Turn in HW5

Week	TA Sessions	Quiz	Content	Remind
13	05/18: Class 11			05/19 Turn in HW5, 05/25 Quiz 5
14	05/25: Class 12	Quiz 5		06/02 Turn in HW6
15	06/01: Class 13			06/02 Turn in HW6, $06/08$ Quiz 6
16	06/08: Class 14	Quiz 6	Review and Q&A	06/16 Final Exam
17	06/15: No class			06/16 Final Exam
18	06/22: No class			,

1.3 Reference

Introduction to Econometrics with R

https://www.econometrics-with-r.org

R for Data Science

https://r4ds.had.co.nz

R Markdown

https://rmarkdown.rstudio.com

Introduction to R Markdown

https://rpubs.com/brandonkopp/RMarkdown

What is a good book on learning R with examples?

https://www.quora.com/What-is-a-good-book-on-learning-R-with-examples

2 Empirical Exercise 4.2

On the text website, http://www.pearsonglobaleditions.com, you will find the data file **Earnings_and_Height**, which contains data on earnings, height, and other characteristics of a random sample of U.S. workers. A detailed description is given in **Earnings_and_Height_Description**, also available on the website. In this exercise, you will investigate the relationship between earnings and height.

a. What is the median value of height in the sample?

Solution

```
# import data
#install.packages("readxl")
library(readxl)
Earnings_and_Height <- read_xlsx("Earnings_and_Height/Earnings_and_Height.xlsx")
median(Earnings_and_Height$height)</pre>
```

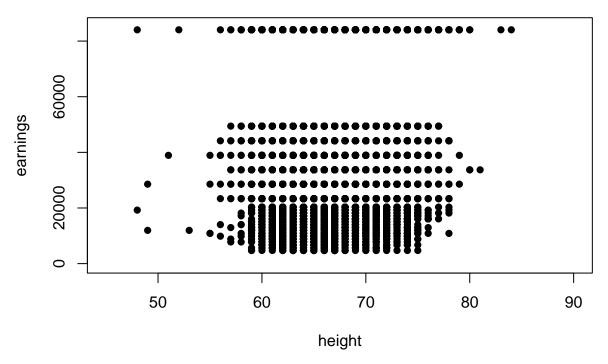
[1] 67

- b. i. Estimate average earnings for workers whose height is at most 67 inches.
 - ii. Estimate average earnings for workers whose height is greater than 67 inches.
 - iii. On average, do taller workers earn more than shorter workers? How much more? What is a 95% confidence interval for the difference in average earnings?

```
# create "group" variable
group <- c()</pre>
for (i in 1:length(Earnings_and_Height$height)){
  if (Earnings_and_Height$height[i] <= 67){</pre>
    # group 0: height <= 67
    group[i] <- c(0)
  } else {
    # group 1: height > 67
    group[i] \leftarrow c(1)
}
Earnings_and_Height <- cbind(Earnings_and_Height, group)</pre>
E42b <- function(x){
  # sample mean
  mu \leftarrow mean(x)
  # sample standard deviation (standard error)
  se <- sd(x)/sqrt(length(x))</pre>
  # test
  test <- t.test(x,
                  alternative = c("two.sided"),
                  mu = 0, # HO
                  conf.level = 0.95) # alpha = 0.05
  # 95% confidence interval
  lower <- round(test$conf.int[1], digit = 4)</pre>
  upper <- round(test$conf.int[2], digit = 4)</pre>
  CI <- paste(lower, "-" ,upper)</pre>
  Table <- data.frame(mu, se, CI)</pre>
  colnames(Table) <- c("Mean", "Standard Error", "95% Confidence Interval")</pre>
  Table
}
# i. # ii.
tapply(Earnings_and_Height$earnings, Earnings_and_Height$group, E42b)
## $`0`
         Mean Standard Error 95% Confidence Interval
                     265.4948 43968.0133 - 45008.8585
## 1 44488.44
##
## $`1`
         Mean Standard Error 95% Confidence Interval
## 1 49987.88
                     305.4062 49389.1973 - 50586.5544
# height <= 67
Earnings_and_Height_i <- Earnings_and_Height[Earnings_and_Height$height <= 67, ]</pre>
```

```
# height > 67
Earnings_and_Height_ii <- Earnings_and_Height[Earnings_and_Height$height > 67, ]
# iii. 95% CI for difference
t.test(Earnings_and_Height_ii$earnings, Earnings_and_Height_i$earnings,
       alternative = c("two.sided"),
       mu = 0, # HO
       var.equal = FALSE,
       conf.level = 0.95) \# \ alpha = 0.05
##
##
   Welch Two Sample t-test
##
## data: Earnings_and_Height_ii$earnings and Earnings_and_Height_i$earnings
## t = 13.59, df = 16624, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 4706.237 6292.643
## sample estimates:
## mean of x mean of y
## 49987.88 44488.44
       c. Construct a scatterplot of annual earnings (Earnings) on height (Height). Notice that the
         points on the plot fall along horizontal lines. (There are only 23 distinct values of Earnings).
         Why? (Hint: Carefully read the detailed data description.)
```

```
plot(x = Earnings_and_Height$height,
    y = Earnings_and_Height$earnings,
    pch = 16, # filled circle
    col = "black",
    xlim = c(45, 90),
    ylim = c(0, 85000),
    xlab = "height",
    ylab = "earnings",
    main = "E4.2 (c)")
```



The data documentation reports that individual earnings were reported in 23 brackets, and a single average value is reported for earnings in the same bracket. Thus, the dataset contains 23 distinct values of earnings.

- d. Run a regression of Earnings on Height.
 - i. What is the estimated slope?
 - ii. Use the estimated regression to predict earnings for a worker who is 67 inches tall, for a worker who is 70 inches tall, and for a worker who is 65 inches tall.

```
# regression
E42d <- lm(formula = earnings ~ height, data = Earnings_and_Height)
# i. estimated intercept, estimated slope
summary(E42d)
##
## Call:
## lm(formula = earnings ~ height, data = Earnings_and_Height)
##
## Residuals:
##
     Min
              1Q Median
                            3Q
                                  Max
   -47836 -21879 -7976
                         34323
                                50599
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                -512.73
                           3386.86
                                    -0.151
                                               0.88
## height
                 707.67
                             50.49
                                   14.016
                                             <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 26780 on 17868 degrees of freedom
## Multiple R-squared: 0.01088,
                                      Adjusted R-squared: 0.01082
## F-statistic: 196.5 on 1 and 17868 DF, p-value: < 2.2e-16
# predict value
E42d_predict <- function(x){</pre>
  E42d$coefficients %*% matrix(c(1, x), ncol = 1)
}
# ii. predict value: height = 67
E42d_predict(67)
##
            [,1]
## [1,] 46901.26
# ii. predict value: height = 70
E42d_predict(70)
##
            [,1]
## [1,] 49024.28
# ii. predict value: height = 65
E42d_predict(65)
##
## [1,] 45485.92
       e. Suppose height were measured in centimeters instead of inches. Answer the following
         questions about the Earnings on Height (in cm) regression.
           i. What is the estimated slope of the regression?
          ii. What is the estimated intercept?
          iii. What is the R^2?
          iv. What is the standard error of the regression?
Solution
# translates from inches to cm
height_cm <- cm(Earnings_and_Height$height)
Earnings_and_Height <- cbind(Earnings_and_Height, height_cm)</pre>
# regression
E42e <- lm(formula = earnings ~ height_cm, data = Earnings_and_Height)
# i. estimated slope # ii. estimated intercept
# iii. R^2 # iv. SE
summary(E42e)
##
## Call:
## lm(formula = earnings ~ height_cm, data = Earnings_and_Height)
##
## Residuals:
      Min
              10 Median
                             30
                                    Max
## -47836 -21879 -7976 34323 50599
##
```

Coefficients:

```
##
              Estimate Std. Error t value Pr(>|t|)
                          3386.86 -0.151
## (Intercept) -512.73
                                             0.88
## height cm
                278.61
                            19.88 14.016
                                           <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 26780 on 17868 degrees of freedom
                                  Adjusted R-squared: 0.01082
## Multiple R-squared: 0.01088,
## F-statistic: 196.5 on 1 and 17868 DF, p-value: < 2.2e-16
```

- f. Run a regression of Earnings on Height, using data for female workers only.
 - i. What is the estimated slope?
 - ii. A randomly selected woman is 1 inch taller than the average woman in the sample. Would you predict her earnings to be higher or lower than the average earnings for women in the sample? By how much?

Solution

```
# female
Earnings_and_Height_f <- Earnings_and_Height[Earnings_and_Height$sex == 0, ]
# regression
E42f <- lm(formula = earnings ~ height, data = Earnings_and_Height_f)
# i. estimated slope # ii.
summary(E42f)
##
## Call:
## lm(formula = earnings ~ height, data = Earnings_and_Height_f)
##
## Residuals:
##
     Min
             1Q Median
                            3Q
                                 Max
## -42748 -22006 -7466 36641 46865
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 12650.9
                           6383.7
                                    1.982
                                            0.0475 *
                                    5.169 2.4e-07 ***
## height
                 511.2
                             98.9
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 26800 on 9972 degrees of freedom
## Multiple R-squared: 0.002672,
                                   Adjusted R-squared: 0.002572
## F-statistic: 26.72 on 1 and 9972 DF, p-value: 2.396e-07
```

A women who is one inch taller than average is predicted to have earnings that are \$511.2 per year higher than average.

g. Repeat (f) for male workers.

```
# male
Earnings_and_Height_g <- Earnings_and_Height[Earnings_and_Height$sex == 1, ]
# regression
E42g <- lm(formula = earnings ~ height, data = Earnings_and_Height_g)</pre>
```

```
# i. estimated slope # ii.
summary(E42g)
##
## Call:
## lm(formula = earnings ~ height, data = Earnings_and_Height_g)
##
## Residuals:
##
     Min
              1Q Median
                            3Q
                                 Max
## -50158 -22373 -8118
                        33091
                               59228
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -43130.3
                           7068.5
                                  -6.102 1.1e-09 ***
## height
                 1306.9
                            100.8 12.969 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 26670 on 7894 degrees of freedom
## Multiple R-squared: 0.02086,
                                   Adjusted R-squared:
## F-statistic: 168.2 on 1 and 7894 DF, p-value: < 2.2e-16
```

A man who is one inch taller than average is predicted to have earnings that are \$1306.9 per year higher than average.

h. Do you think that height is uncorrelated with other factors that cause earning? That is, do you think that the regression error term, ui has a conditional mean of 0 given $Height(X_i)$? (You will investigate this more in the Earnings and Height exercises in later chapters.)

Solution

Height may be correlated with other factors that cause earnings. For example, height may be correlated with "strength," and in some occupations, stronger workers may by more productive. There are many other potential factors that may be correlated with height and cause earnings and we will investigate of these in future exercises.

3 Empirical Exercise 5.1

Use the data set **Earnings_and_Height** described in Empirical Exercise 4.2 to carry out the following exercises.

- a. Run a regression of Earnings on Height.
 - i. Is the estimated slope statistically significant?
 - ii. Construct a 95% confidence interval for the slope coefficient.

Solution

i.

• Prepare

```
H_0: \beta_{height} = 0 v.s. H_1: \beta_{height} \neq 0
```

Let the significance level be 0.05.

Calculate

```
# import data
library(readxl)
Earnings_and_Height <- read_xlsx("Earnings_and_Height/Earnings_and_Height.xlsx")</pre>
E51a_model <- lm(earnings ~ height, data = Earnings_and_Height)
summary(E51a_model)
##
## Call:
## lm(formula = earnings ~ height, data = Earnings_and_Height)
##
## Residuals:
##
     Min
             1Q Median
                            ЗQ
                                 Max
## -47836 -21879 -7976 34323 50599
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -512.73
                          3386.86 -0.151
                                              0.88
## height
                707.67
                            50.49 14.016
                                            <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 26780 on 17868 degrees of freedom
## Multiple R-squared: 0.01088,
                                   Adjusted R-squared: 0.01082
## F-statistic: 196.5 on 1 and 17868 DF, p-value: < 2.2e-16
```

• Conclude

Because p-value < 0.05, we reject H_0 . The estimated slope is statistically significant different from 0.

ii.

In simple regression model

$$Y_i = \beta_0 + \beta_1 X_i + u_i, \tag{1}$$

we know

$$\widehat{\beta}_{1} = \frac{\sum_{i=1}^{n} (X_{i} - \overline{X}) (Y_{i} - \overline{Y})}{\sum_{i=1}^{n} (X_{i} - \overline{X})^{2}}$$

$$\widehat{\beta}_{0} = \overline{Y} - \widehat{\beta}_{1} \overline{X}$$
(2)

$$\widehat{\beta}_0 = \overline{Y} - \widehat{\beta}_1 \overline{X} \tag{3}$$

$$ESS = \sum_{i=1}^{n} \left(\widehat{Y}_i - \overline{Y} \right)^2 \tag{4}$$

$$TSS = \sum_{i=1}^{n} (Y_i - \overline{Y})^2 \tag{5}$$

$$SSR = \sum_{i=1}^{n} \widehat{u}_i^2 = \sum_{i=1}^{n} \left(Y_i - \widehat{Y}_i \right)^2$$
 (6)

$$R^2 = \frac{ESS}{TSS} = 1 - \frac{SSR}{TSS} \tag{7}$$

$$\widehat{\sigma}^2 = \frac{\sum_{i=1}^n \widehat{u}_i^2}{n-2} \tag{8}$$

$$SE\left(\widehat{\beta}_{1}\right) = \sqrt{\frac{\widehat{\sigma}^{2}}{\sum_{i=1}^{n} \left(X_{i} - \overline{X}\right)^{2}}}$$

$$(9)$$

$$SE\left(\widehat{\beta}_{0}\right) = \sqrt{\widehat{\sigma}^{2}\left(\frac{1}{n} + \frac{\overline{X}^{2}}{\sum_{i=1}^{n}\left(X_{i} - \overline{X}\right)^{2}}\right)}$$

$$(10)$$

```
E51a \leftarrow function(x, y){
  # numbers of sample
  n <- length(y)</pre>
  # sample mean
  xbar <- mean(x)
  ybar <- mean(y)</pre>
  # OLS coefficient
  b1hat <-cov(x,y)/var(x)
  b0hat <- ybar - b1hat*xbar
  yhat <- b0hat + b1hat*x</pre>
  # explained sum of squares (ESS)
  ESS <- sum((yhat - ybar)^2)
  # total sum of squares (TSS)
  TSS <- sum((y - ybar)^2)
  # sum of squared residuals (SSR)
  SSR \leftarrow sum((y - yhat)^2)
  # coefficient of determination
  Rsqure <- ESS/TSS
  # standard error of the regression
  SER <- sqrt(SSR/(n-2))
  # standard error of coefficient
  se_b1hat <- sqrt(SER^2/sum((x - xbar)^2))</pre>
```

```
se_b0hat \leftarrow sqrt(SER^2* (1/n + xbar^2/sum((x - xbar)^2)))
  # 95% CI for b1hat
  lower_b1hat <- round(b1hat - qnorm(0.975, mean = 0, sd = 1)*se_b1hat, digit = 4)
  upper_b1hat <- round(b1hat + qnorm(0.975, mean = 0, sd = 1)*se_b1hat, digit = 4)
  CI_b1hat <- paste(lower_b1hat, "-" ,upper_b1hat)</pre>
  # 95% CI for b0hat
  lower_b0hat <- round(b0hat - qnorm(0.975, mean = 0, sd = 1)*se_b0hat, digit = 4)</pre>
  upper_b0hat <- round(b0hat + qnorm(0.975, mean = 0, sd = 1)*se_b0hat, digit = 4)
  CI_b0hat <- paste(lower_b0hat, "-" ,upper_b0hat)</pre>
  # coefficient
  coef <- matrix(c(b0hat, se_b0hat, CI_b0hat, b1hat, se_b1hat, CI_b1hat), ncol = 3, byrow = TRUE)</pre>
  rownames(coef) <- c("Intercept", "Slope")</pre>
  colnames(coef) <- c("Estimate", "Standard Error", "95% Confidence Interval")</pre>
  result <- list(coef, Rsqure)</pre>
  names(result) <- c("Coefficients", "R-squared")</pre>
  result
}
E51a(Earnings_and_Height$height, Earnings_and_Height$earnings)
## $Coefficients
##
             Estimate
                                    Standard Error
                                                        95% Confidence Interval
## Intercept "-512.733592001881" "3386.85615092263" "-7150.8497 - 6125.3825"
              "707.671558437266" "50.4892245961979" "608.7145 - 806.6286"
##
## $`R-squared`
## [1] 0.0108753
       b. Repeat (a) for women.
Solution
  i.
   • Prepare
H_0: \beta_{height}^{women} = 0 \text{ v.s. } H_1: \beta_{height}^{women} \neq 0
Let the significance level be 0.05.

    Calculate

# data: woman
Earnings_and_Height_women <- Earnings_and_Height[Earnings_and_Height$sex == 0,]</pre>
E51b_model <- lm(earnings ~ height, data = Earnings_and_Height_women)
summary(E51b_model)
##
## Call:
## lm(formula = earnings ~ height, data = Earnings_and_Height_women)
##
```

```
## Residuals:
##
      Min
              1Q Median
                             30
                                   Max
## -42748 -22006 -7466 36641 46865
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 12650.9
                             6383.7 1.982 0.0475 *
                                       5.169 2.4e-07 ***
## height
                  511.2
                               98.9
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 26800 on 9972 degrees of freedom
## Multiple R-squared: 0.002672, Adjusted R-squared: 0.002572
## F-statistic: 26.72 on 1 and 9972 DF, p-value: 2.396e-07
   • Conclude
Because p-value < 0.05, we reject H_0. The estimated slope is statistically significant different from 0.
E51a(Earnings_and_Height_women$height, Earnings_and_Height_women$earnings)
## $Coefficients
                                                     95% Confidence Interval
             Estimate
                                 Standard Error
## Intercept "12650.8577295031" "6383.74100734725" "138.9553 - 25162.7602"
             "511.222170015359" "98.8963075918224" "317.389 - 705.0554"
## Slope
## $`R-squared`
## [1] 0.002672482
       c. Repeat (a) for men.
Solution
  i.
   • Prepare
H_0: \beta_{height}^{men} = 0 v.s. H_1: \beta_{height}^{women} \neq 0
Let the significance level be 0.05.

    Calculate

# data: woman
Earnings and Height men <- Earnings and Height (Earnings and Height $\$sex == 1,]
E51c_model <- lm(earnings ~ height, data = Earnings_and_Height_men)
summary(E51c_model)
##
## lm(formula = earnings ~ height, data = Earnings_and_Height_men)
##
## Residuals:
##
      Min
              1Q Median
                             3Q
                                    Max
## -50158 -22373 -8118 33091 59228
```

##

```
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) -43130.3    7068.5   -6.102   1.1e-09 ***
## height    1306.9    100.8   12.969    < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 26670 on 7894 degrees of freedom
## Multiple R-squared: 0.02086, Adjusted R-squared: 0.02074
## F-statistic: 168.2 on 1 and 7894 DF, p-value: < 2.2e-16</pre>
```

Conclude

Because p-value < 0.05, we reject H_0 . The estimated slope is statistically significant different from 0.

ii.

```
E51a(Earnings_and_Height_men$height, Earnings_and_Height_men$earnings)
```

```
## $Coefficients
## Estimate Standard Error 95% Confidence Interval
## Intercept "-43130.3423470527" "7068.48053034493" "-56984.3096 - -29276.3751"
## Slope "1306.85990584335" "100.766159761487" "1109.3619 - 1504.3579"
##
## $`R-squared`
## [1] 0.02086292
```

d. Test the null hypothesis that the effect of height on earnings is the same for men and women. (Hint: See Exercise 5.15.)

Solution

• Prepare

```
H_0: \beta_{height}^{men} - \beta_{height}^{women} = 0 \text{ v.s. } H_1: \beta_{height}^{men} - \beta_{height}^{women} \neq 0
```

Let the significance level be 0.05.

• Calculate

```
E51d <- function(x1, y1, x2, y2){
  # numbers of sample
  n1 <- length(y1); n2 <- length(y2)</pre>
  # sample mean
  x1bar \leftarrow mean(x1); x2bar \leftarrow mean(x2)
  y1bar <- mean(y1); y2bar <- mean(y2)</pre>
  # OLS coefficient
  b1hat1 \leftarrow cov(x1, y1)/var(x1); b1hat2 \leftarrow cov(x2, y2)/var(x2)
  b0hat1 <- y1bar - b1hat1*x1bar; b0hat2 <- y2bar - b1hat2*x2bar
  y1hat1 <- b0hat1 + b1hat1*x1; y2hat2 <- b0hat2 + b1hat2*x2
  # explained sum of squares (ESS)
  ESS1 \leftarrow sum((y1hat1 - y1bar)^2); ESS2 \leftarrow sum((y2hat2 - y2bar)^2)
  # total sum of squares (TSS)
  TSS1 \leftarrow sum((y1 - y1bar)^2); TSS2 \leftarrow sum((y2 - y2bar)^2)
  # sum of squared residuals (SSR)
  SSR1 \leftarrow sum((y1 - y1hat1)^2); SSR2 \leftarrow sum((y2 - y2hat2)^2)
```

```
# standard error of the regression
  SER1 <- sqrt(SSR1/(n1-2)); SER2 <- sqrt(SSR2/(n2-2))
  # standard error of coefficient
  se_b1hat1 \leftarrow sqrt(SER1^2/sum((x1 - x1bar)^2))
  se_b1hat2 \leftarrow sqrt(SER2^2/sum((x2 - x2bar)^2))
  est <- b1hat1 - b1hat2
  se <- sqrt(se_b1hat1^2 + se_b1hat2^2)</pre>
  # 95% CI for difference
  lower <- round(est - qnorm(0.975, mean = 0, sd = 1)*se, digit = 4)
  upper <- round(est + qnorm(0.975, mean = 0, sd = 1)*se, digit = 4)
  CI <- paste(lower, "-", upper)
  # output table
  Table <- data.frame(est, se, CI)
  colnames(Table) <- c("Estimate", "Standard Error", "95% Confidence Interval")</pre>
  Table
}
E51d(Earnings_and_Height_men$height, Earnings_and_Height_men$earnings, Earnings_and_Height_women$height
```

```
##
     Estimate Standard Error 95% Confidence Interval
## 1 795.6377
                    141.1889
                                518.9126 - 1072.3628
```

• Conclude

Because $0 \notin 95\%$ confidence interval, we reject H_0 . The estimated slope is statistically significant different from 0.

e. One explanation for the effect of height on earnings is that some professions require strength, which is correlated with height. Does the effect of height on earnings disappear when the sample is restricted to occupations in which strength is unlikely to be important?

```
E51e <- function(x, y){
  # numbers of sample
  n <- length(y)
  # sample mean
  xbar <- mean(x)
  ybar <- mean(y)</pre>
  # OLS coefficient
  b1hat <- cov(x,y)/var(x)
  b0hat <- ybar - b1hat*xbar
  yhat <- b0hat + b1hat*x</pre>
  # explained sum of squares (ESS)
  ESS <- sum((yhat - ybar)^2)
  # total sum of squares (TSS)
```

```
TSS <- sum((y - ybar)^2)
  # sum of squared residuals (SSR)
  SSR \leftarrow sum((y - yhat)^2)
  # coefficient of determination
  #Rsqure <- ESS/TSS
  # standard error of the regression
  SER \leftarrow sqrt(SSR/(n-2))
  # standard error of coefficient
  se_b1hat <- sqrt(SER^2/sum((x - xbar)^2))</pre>
  # 95% CI for b1hat
  lower_b1hat \leftarrow round(b1hat \rightarrow qnorm(0.975, mean = 0, sd = 1)*se_b1hat, digit = 4)
  upper_b1hat \leftarrow round(b1hat + qnorm(0.975, mean = 0, sd = 1)*se_b1hat, digit = 4)
  CI_b1hat <- paste(lower_b1hat, "-" ,upper_b1hat)</pre>
  Table <- matrix(c(b1hat, se_b1hat, CI_b1hat), nrow = 1)
  colnames(Table) <- c("Estimate", "Standard Error", "95% Confidence Interval")</pre>
  Table
}
E51e output <- matrix(nrow = 15, ncol = 3)
rownames(E51e_output) <- c(1:15)</pre>
colnames(E51e_output) <- c("Estimate", "Standard Error", "95% Confidence Interval")</pre>
for (i in 1:15){
 data <- Earnings_and_Height[Earnings_and_Height$occupation == i,]</pre>
 x <- data$height
 y <- data$earnings
 E51e_output[i,] \leftarrow E51e(x, y)
}
E51e_output
##
      Estimate
                           Standard Error
                                               95% Confidence Interval
## 1 "469.458070315024" "155.197956234637" "165.2757 - 773.6405"
## 2 "622.755176016371"
                           "117.270342579588" "392.9095 - 852.6008"
## 3 "649.721773596878" "214.630174152533" "229.0544 - 1070.3892"
## 4 "1372.384840781"
                           "148.798366501132" "1080.7454 - 1664.0243"
     "201.215856644732" "133.739773995006" "-60.9093 - 463.341"
## 5
## 6 "-172.893730327361" "680.403429299889" "-1506.4599 - 1160.6725"
## 7 "1503.03853605894"
                           "403.078327473455" "713.0195 - 2293.0575"
## 8 "62.8574693717754"
                           "128.266422708668" "-188.5401 - 314.255"
                           "308.815799047297" "443.9334 - 1654.4691"
## 9 "1049.20129254131"
```

"331.525682080739" "-78.5552 - 1221.0015"

"286.488509387146" "518.8141 - 1641.8284"

"150.635402614451" "677.6696 - 1268.1495"

"268.02788099113" "613.0886 - 1663.7386"

11 "967.009049351859" "306.481847438174" "366.3157 - 1567.7024"

15 "549.115247105915" "249.240665896231" "60.6125 - 1037.618"

10 "571.223149958568"

12 "1080.32127574574"

13 "972.909550457317"

14 "1138.41360943808"