

## ch1: Hypergraph

理解:

$$\mathcal{G} = (\mathcal{V}, \mathcal{E}, W)$$

$\mathcal{G}$  : hypergraph

$\mathcal{V}$  : vertices

U: Vertex Weight Matrix

X: Vertex Feature Matrix

Y: Vertex Label Matrix

$\mathcal{E}$  : hyperedges

W: Hyperedge Weight Matrix

$$H \in |\mathcal{V}| * |\mathcal{E}| \quad H(v, e) = \begin{cases} 1 & \text{if } v \in e \\ 0 & \text{if } v \notin e \end{cases}$$

$$d(v) = \sum_{e \in \mathcal{E}} H(v, e) * w(e) \quad D_v$$

$$d(e) = \sum_{v \in \mathcal{V}} H(v, e) \quad D_e$$

$$\Delta = D_v - H W D_e^{-1} H^T$$

$$\Delta = I - D_v^{-1/2} H W D_e^{-1} H^T D_v^{-1/2}$$

## ch2: Spectral Hypergraph Theory

$$g \star x = \phi((\phi^T g) \odot (\phi^T x)) = \phi g(\wedge)(\phi^T x)$$

$$g(\wedge) = \text{diag}(g(\lambda_1), \dots, g(\lambda_n))$$

$$g \star x \approx \sum_{k=0}^K \theta_k T_k(\tilde{\Delta}) x$$

$$\tilde{\Delta} = \frac{2}{\lambda_{max}} \Delta - I$$

$$K = 2 \qquad \lambda_{max} = 2$$

$$g \star x \approx \theta_0 x - \theta_1 D_v^{-1/2} H W D_e^{-1} H^T D_v^{-1/2} x$$

## ch3: Hypergraph Generation and Transformation

理解:

隐式: 距离、特征

显式: 属性、网络

## ch3: Hypergraph Learning Architecture

理解:

超图游走

(1) Features

$$X \in R^{|V| \times d} \quad Y \in R^{|E| \times d'}$$

External + Internal(local+global) + Identity

(2) Transformation

Reductive Transformation

$(E, X, Y) \Rightarrow A$  hyperedges to edges

clique expansion + adaptive expansion

Non-reductive Transformation

star/line/tensor expansion

(3) Message

whose: v-v v-e e-v

what : e-consistent + e-dependent

how : fixed-pooling + learnable-pooling

(4) Training