

ch1: Hypergraph

理解:

$$\mathcal{G} = (\mathcal{V}, \mathcal{E}, W)$$

\mathcal{G} : hypergraph

\mathcal{V} : vertices

U: Vertex Weight Matrix

X: Vertex Feature Matrix

Y: Vertex Label Matrix

\mathcal{E} : hyperedges

W: Hyperedge Weight Matrix

$$H \in |\mathcal{V}| * |\mathcal{E}| \quad H(v, e) = \begin{cases} 1 & \text{if } v \in e \\ 0 & \text{if } v \notin e \end{cases}$$

$$d(v) = \sum_{e \in \mathcal{E}} H(v, e) * w(e) \quad D_v$$

$$d(e) = \sum_{v \in \mathcal{V}} H(v, e) \quad D_e$$

$$\Delta = D_v - H W D_e^{-1} H^T$$

$$\Delta = I - D_v^{-1/2} H W D_e^{-1} H^T D_v^{-1/2}$$

ch2: Hypergraph Learning Architecture

(1) Features

$$X \in R^{|V| \times d} \quad Y \in R^{|E| \times d'}$$

External + Internal(local+global) + Identity

(2) Transformation

Reductive Transformation

$$(E, X, Y) \Rightarrow A \quad \text{hyperedges to edges}$$

clique expansion + adaptive expansion

Non-reductive Transformation

star/line/tensor expansion