# Final Project – Antibody Response Induced by HIV Vaccines and T-cell Suppression Treatments in Rhesus Macaques – Second Draft

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## Notes/questions

- The resulting dataset from this section is called Data2, and one outlier will be removed in a later section, which results in a final dataset Data3. So Data3 is used for analysis.
- Questions for Kan marked as [Kan...] below.
- Comments for future addition and revisions in [...]
- Instead of looking at average of Binding, look at average of reactivity to see the percentage of reactive. Perhaps use natural log to transform Binding.
- Who can figure out how to put all figures and tables after all text and before supplmental materials?
- Dig deeper into analysis results?
- Not sure what sections the professor wants

## Abstract

#### Introduction

A dominant vaccine development strategy is to induce neutralizing antibodies by immunizing humans with the virus' glycoproteins. However, HIV vaccines that adopted this strategy mostly failed due to the fact that HIV is an RNA virus, which mutates rapidly to escape the inhibition of neutralizing antibodies. By the time the body generates neutralizing antibodies against the glycoproteins of some HIV strains, the RNA virus has already mutated. Thus, the existing neutralizing antibody fails to recognize, bind with, and neutralize the HIV virus. One possible solution is to increase the number of potential neutralizing antibodies that will cycle in the body by releasing a variety of antibodies after glycoprotein immunization.

Our dataset includes measurements of antibodies measured in 20 rhesus macaques after they were given the same HIV vaccine at three different time points and one of three randomly selected anti-Treg treatments. Blood samples were collected two weeks after vaccine dosing, and antibodies were isolated from those samples. A different number of antibodies were collected from each blood sample, limited by assay yield. Each observation contains information about the antibody isolated post the glycoprotein immunization. In the current report, we test if the different Treg treatments and number of vaccine injections cause changes in the antibody characteristics and if the changes are related to immunization/treatment timepoints.

Specifically, we evaluate:

- 1. Do treatments, time points, or isotypes have effects on the mutation frequency or the amino acid count in the third complementarity determining region (CDR3)? This will be evaluated with a three-way MANOVA, followed by further pair-wise analysis of any values found significantly different.
- 2. Do the paired antibody heavy chain and light chain have different mutation rate, CDR3, or binding values? This will be evaluated with paired comparisons by antibody.
- 3. How does the binding strength of the antibodies develop in response to the number of vaccine dosages by treatment? This will be evaluated with a longitudinal analysis by test subject.

## Methodologies

During the experiment, 20 rhesus macaques were given glycoprotein immunization and supplemental antibody doses, as well as one of three treatments (two experimental regulatory T-cell suppression treatments and one control). Regulatory T (Treg) cells prevent autoimmune diseases and suppress allergic reactions by inhibiting adaptive antibody immune response in the germinal center. Theoretically, this adaptive response lowers the effectiveness of vaccines. Thus the experiment used T-cell suppression treatments to investigate the effect on immunization. These drugs are widely used in post transplant immunosuppression treatment to prevent rejection.

For the analysis of mutation frequency and CDR3 count, each antibody within the same treatment is treated as an independent observation. While we might expect different variance within subject vs between subjects, the number of potential antibodies observed is much higher than the number sampled in a blood draw. A human antibody is formed by a heavy chain and light chain. For heavy chain, human has about 51 V-gene segments, 25 D-gene segments and 6 J-gene segment. For light chain (kappa and lambda), there are 71 V-gene segments and 9 J-gene segments[ref.5]. Any heavy chain V-D-J combination and light chain V-J combinations can randomly happen in germline center. Theoretically, there can be  $51 * 25 * 6 * 71 * 9 = 4.88835 \times 10^6$  combinations of gene segments. Considering the frequently happened mutation, insertation, class switching, each individual can have over 10 billion different antibodies. Thus, we decided to follow the convention of vaccine studies and treat each antibody as independent. [Kan – can you identify a reference article or journal here that uses this convention? We don't need to quote it / change the answer, it's just defending our claim that it's a standard practice]

To evaluate the mutation frequency and CDR count vs Treatments, Timepoints, and Isotypes MANOVA, we will be running the [xxx] function from the [xxx] package [package citation]

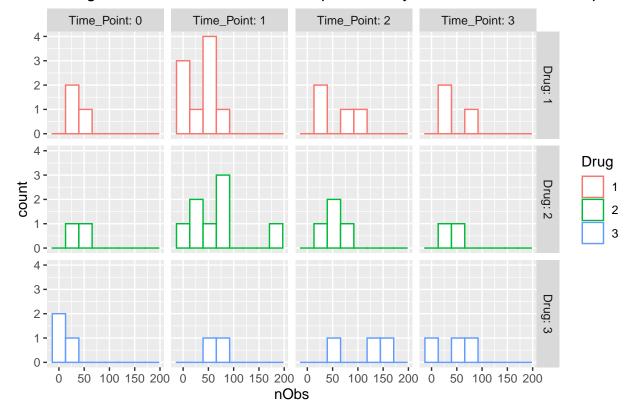
For the longitudinal analysis of binding strength vs number of vaccine doses, we will be using the gls function from the nlme package<sup>[7]</sup>.

## **Data Summaries**

[Feel free to condense any tables or figures or make them look better.]

The dataset has 2465 antibodies collected from 20 rhesus monkeys. We first present our exploratory data analysis and summaries. First an overview of the number of antibodies collected per treatment at each timepoint

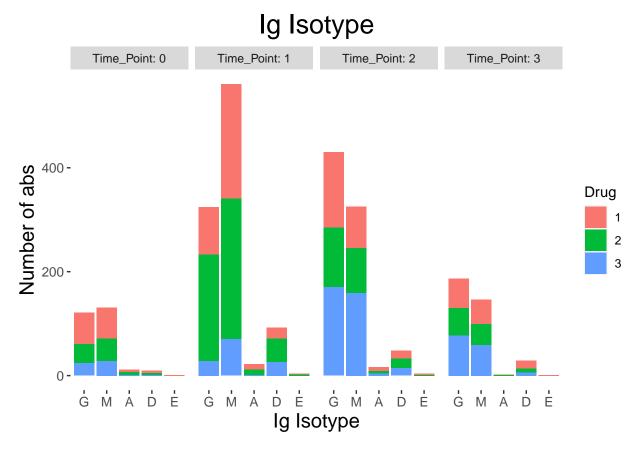
## Histograms of Antibodies Collected per Monkey vs Treatment and Timepoint



There are four time points; time zero was collected before any procedure was done. Times 1,2, and 3 were collected two weeks after an initial and two booster vaccine shots were administered to the macaques. In the treatment groups, groups 1-3 represent different doses of anti T-Reg drug 1, groups 4-6 represent different doses of anti-Treg drug 2, and group 7 represents the control group [We have 20 monkeys, do we need to mention groups at all? Can we just stick to drugs 1,2, and control group 3?].

Next, we'll take a look at the variable Isotype. There are 5 kinds of immunoglobulin isotypes: IgG, IgA,

IgM, IgE, IgD[ref.6]. The two most important kinds are IgG and IgM. IgM occurs in the acute stage of infection and perform an role of primary response. The secondary response IgG appears later in serum with higher binding affinity, and neutralizing potentials against toxins and virus. IgA mostly found in mucosal tissues such as Nasal mucosa. Non-dominant IgD and IgE are typically lower than 1% in blood.



As expected, we see that IgG and IgM occupy the biggest proportion of all antibodies in all time points. Before immunization (time point 0), there are similar weight of IgG and IgM found in blood. After the 1st immunization (time point 1), primary immune response results an increase of IgM, followed with IgG increase at later time point 2 and 3. We'll use the variable Isotype as a grouping covariate later.

For the response variables, we will begin with an outlier check, then review their distributions across treatment and timepoints.

## Histogram of Response Variables

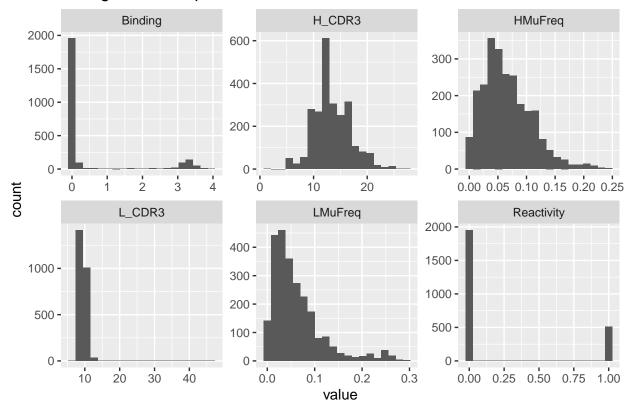


Table 1: Normal Standardized L\_CDR3 Statistics

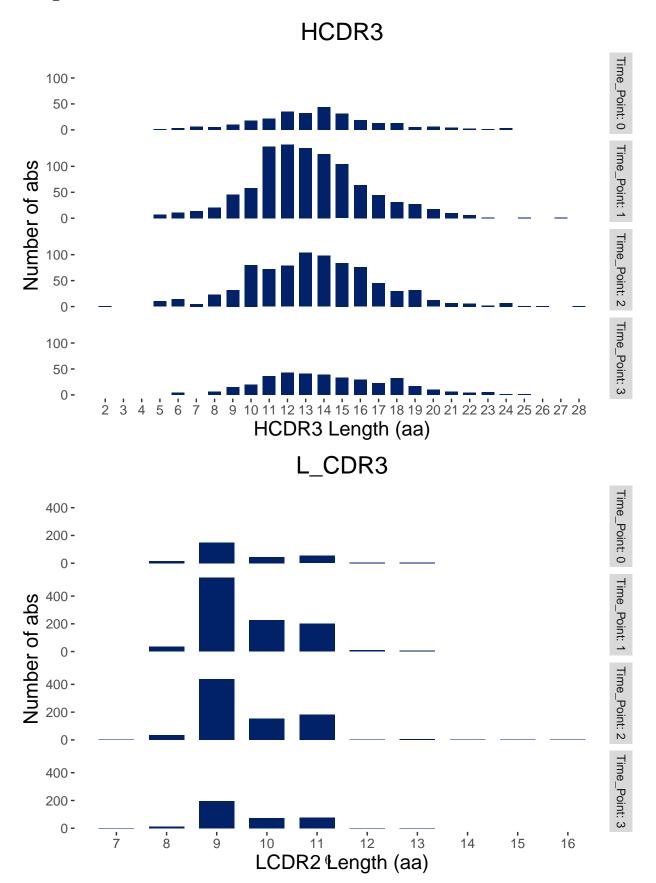
V1	Min. :-2.1860	1st	Median	Mean : $0.0000$	3rd Qu.:	Max. :30.8110
		Qu.:-0.5361	:-0.5361		0.2888	

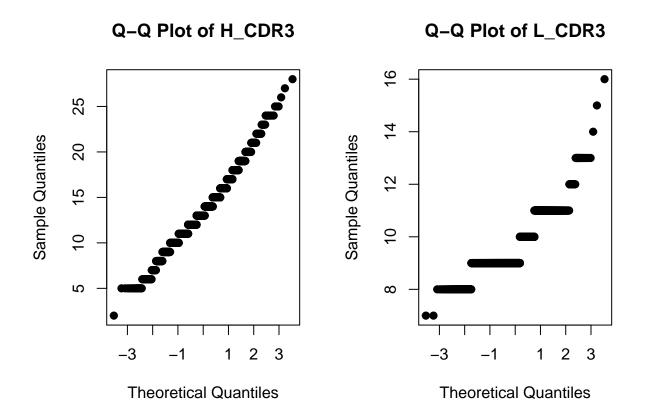
L\_CDR3 appears to have an outlier several standard. This is most likely caused by a laboratory error, so we will exclude it and continue the analysis with the remaining data.

Next we'll examine our responses: H\_CDR3, HMuFreq, L\_CDR3, LMuFreq, Binding, and Reactivity. In each antibody, there are two sets of heavy chain and light chain, all of which forming a Y-shape immunoglobulin. Thus many of the variables start with H or L, indicating which chain the information comes from.

H\_CDR3 and L\_CDR3 indicates the length of the third complementarity-determining region on the variable heavy chain and light chain. The longer they are, the more potential there is to produce diverse antibodies. [Kan, could you check to see if this is correct?] In other words, we want the values to be higher. Below we see that the distributions are roughly normal with the center around 13 for H\_CDR3, with all data points, and slightly centers for different time points.

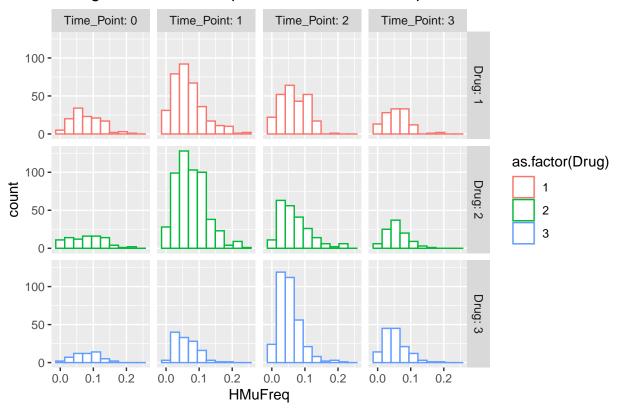
Why does the x-axis label on the L\_CDR3 plot specify LCDR2 Length?



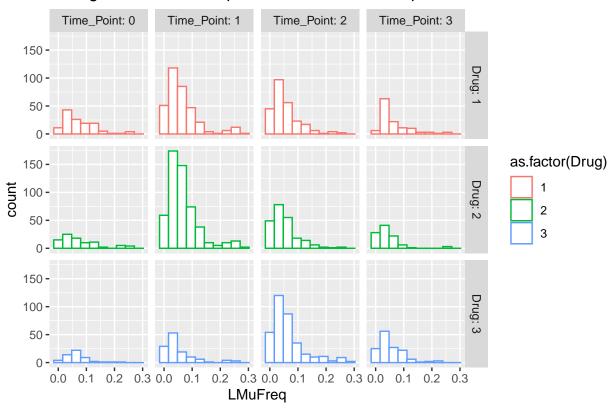


HMuFreq and LMuFreq are calculated by dividing H\_Substitution by H\_VBase for heavy chain and similarly for light chain. These two variables show how much the antibodies mutate. A higher mutation rate is usually indicative of better virus neutralization. Below we see some comparison of mutation rate between heavy chain and light chain. (Kappa and Lambda are two kinds of light chain.) [Kan, is there a reason to split up light chain into Kappa and Lambda? Could we simply plot heavy chain vs. light chain?]

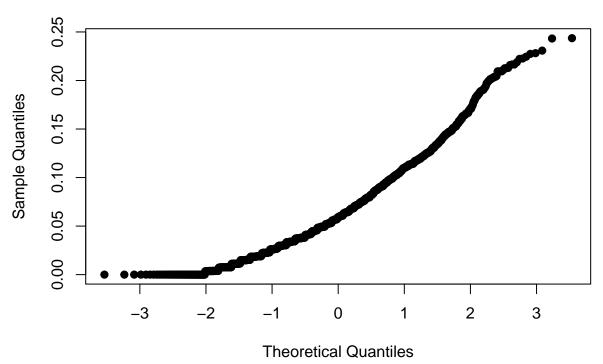
# Histograms of HMuFreq vs Treatment and Timepoint



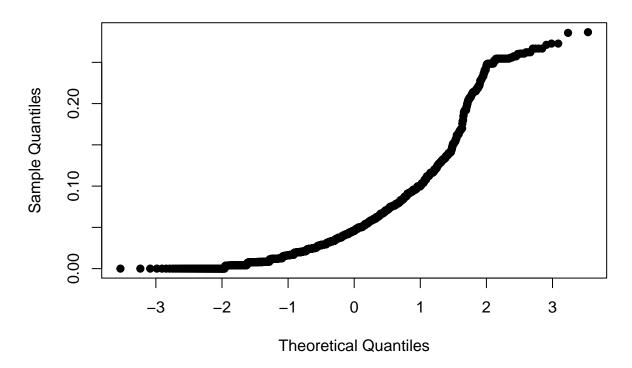
# Histograms of LMuFreq vs Treatment and Timepoint



# Q-Q Plot of HMuFreq



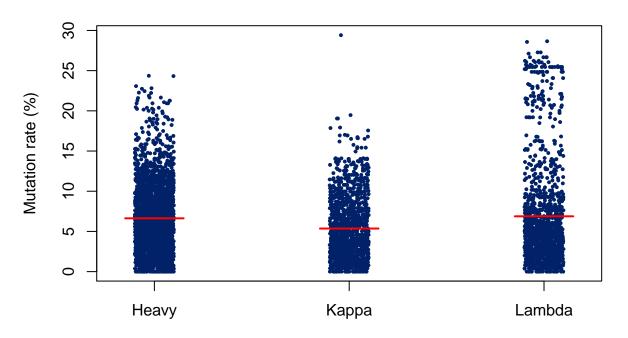
# Q-Q Plot of LMuFreq



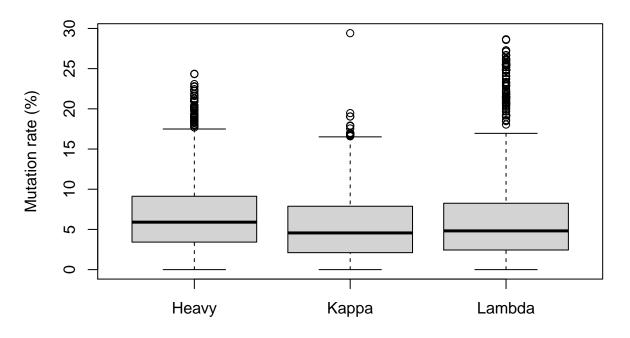
I don't know what Kappa and Lambda Chains are, are we evaluating them for our research questions? We should describe how they fit into the research questions if they are, or otherwise omit them for being extra detail.

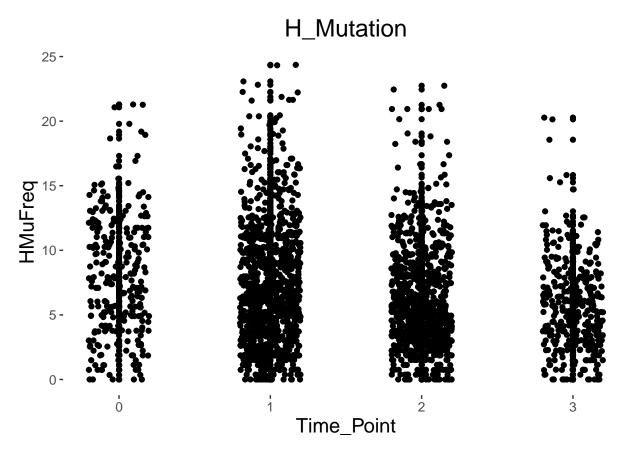
##		H_Mutation%	<pre>K_Mutation%</pre>	L_Mutation%
##	Min.	0.00	0.00	0.00
##	1st Qu.	3.42	2.11	2.44
##	Median	5.90	4.56	4.82
##	Mean	6.63	5.36	6.88
##	3rd Qu.	9.13	7.88	8.25
##	Max.	24.36	29.41	28.65

# H/K/L mutation rate



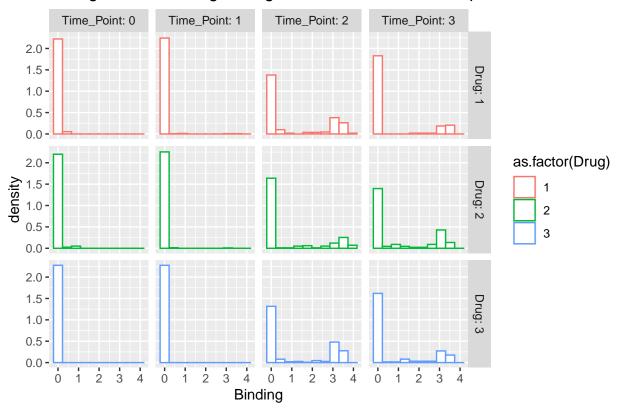
# H/K/L mutation rate



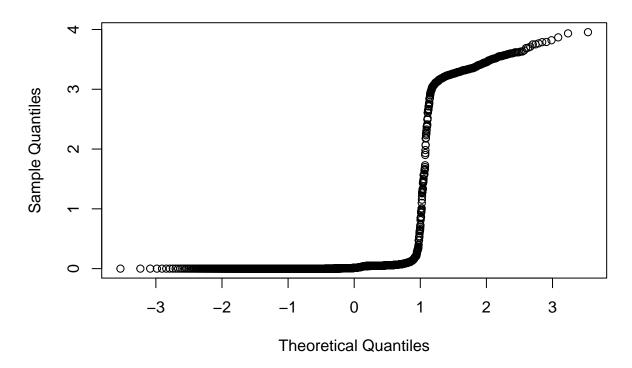


Lastly, Binding indicates the rate of neutralizing, meaning how much the antibodies bind with the virus and thus make the virus ineffective. This is the most important measure of the study. Reactivity turns Binding into a binary variable; Binding rate above 0.1 is considered reactive. In the Q-Q plot of Binding, we can see that it is not normally distributed. However, since our sample size is larger than 2000, we can use the Central Limit Theorem and assume normality.

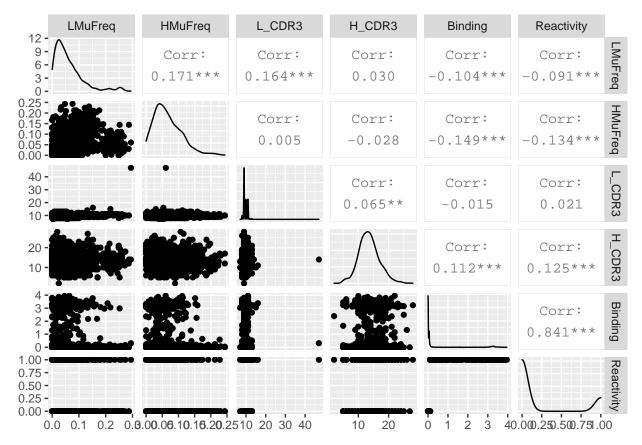
# Histograms of Binding Strength vs Treatment and Timepoint



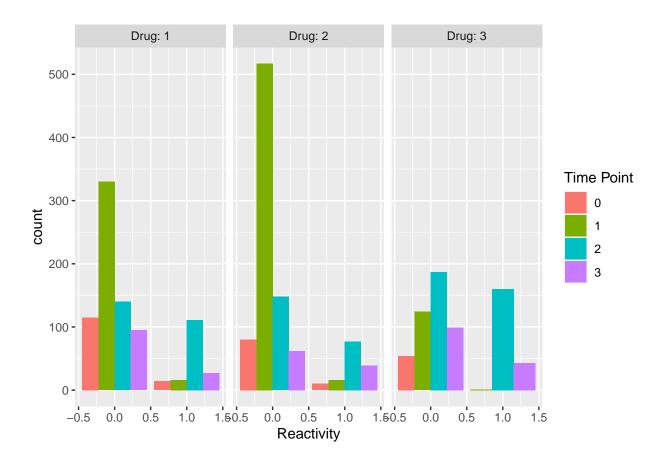
## Normal Q-Q Plot

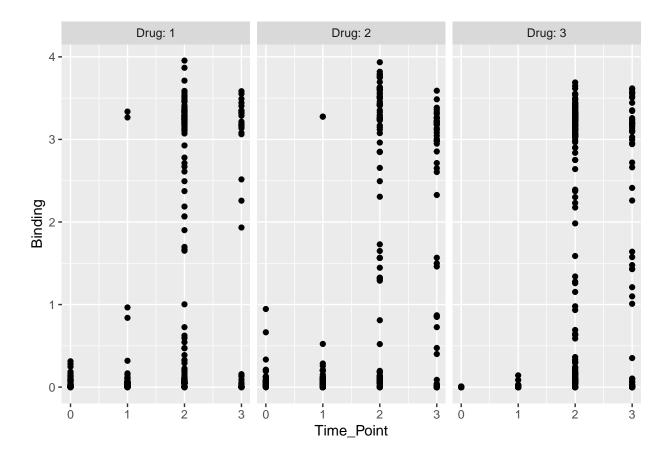


Let's take a look at these response variables and check whether they might be correlated. In the plot below, we can see that none of the response variables are highly correlated, except for Binding and Reactivity, which is expected, because Reactivity is a binary variable derived from Binding. We will only choose one of these two variables in each analysis based on the type of analysis. [What else to point out here?]



<sup>\* [</sup>We should trim this, move to the data analysis section if desired] Now we use some plots to see whether the response variables might be different for different time points, treatment groups or drugs, and grouping covariate (Isotype).

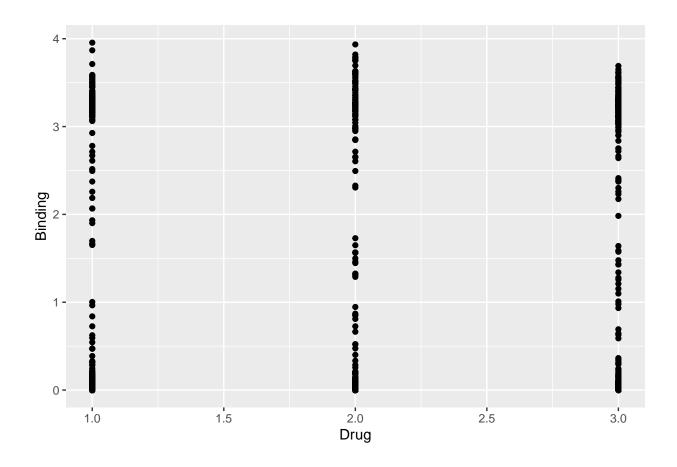


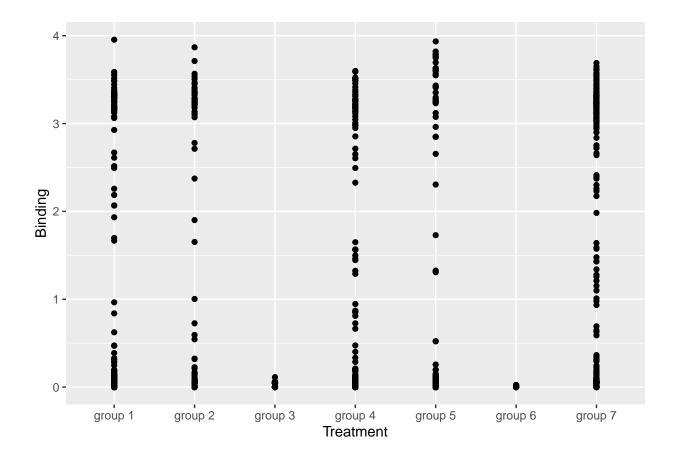


```
##
##
          0
              1
     1 680 168
##
##
     2 807 142
     3 464 204
##
##
##
          0
              1
##
     0 249
             24
##
     1 971
             33
     2 475 348
##
##
     3 256 109
```

Binding or Reactivity do seem to be affected by various predictors, and the boxplots for Binding do appear quite different.

```
## # A tibble: 3 x 6
      {\tt Drug~avgLMuFreq~avgHMuFreq~avgBinding~varBinding~avgReact}
##
##
     <dbl>
                 <dbl>
                             <dbl>
                                         <dbl>
                                                     <dbl>
                                                               <dbl>
## 1
                0.0616
                                                               0.198
         1
                           NA
                                         0.450
                                                     1.14
## 2
         2
                0.0616
                            0.0730
                                         0.334
                                                     0.864
                                                               0.150
## 3
         3
                0.0594
                            0.0559
                                         0.807
                                                     1.81
                                                               0.305
```





# Data Analysis

## Multivariate Data Analysis

Now we want to test whether predictors Drug and Isotype have effects on the five responses: H\_CDR3, HMuFreq, L\_CDR3, LMuFreq, and Binding. We choose Binding here, because all the variables are continuous.

First, we use manova to test effects. Since we have a large same size (n = 2464), we can assume normality. In the output, we can see that the main effects of Drug and Isotype and the interaction effects are all significant.

```
##
                     Pillai approx F num Df den Df
                                                       Pr(>F)
               \mathsf{Df}
## drug
                2 0.058434
                              14.711
                                          10
                                               4888 < 2.2e-16 ***
                 4 0.300048
                              39.672
                                               9784 < 2.2e-16 ***
                                          20
## it
## drug:it
                7 0.069958
                               4.960
                                          35
                                              12235 < 2.2e-16 ***
## Residuals 2447
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
We next use multiple linear regression.
## Response Data3$L_CDR3 :
##
## Call:
## lm(formula = `Data3$L_CDR3` ~ drug * it)
##
## Residuals:
```

```
10 Median
                               3Q
## -2.5872 -0.6634 -0.5696 0.4304 6.3000
## Coefficients: (1 not defined because of singularities)
               Estimate Std. Error t value Pr(>|t|)
                          0.193972 49.406
                                             <2e-16 ***
## (Intercept) 9.583333
                          0.283946 -0.042
                                             0.9666
## drug2
              -0.011905
## drug3
               0.750000
                          0.433735
                                    1.729
                                             0.0839 .
## itD
               0.100877
                          0.231230
                                     0.436
                                             0.6627
## itE
               0.416667
                          0.408198
                                    1.021
                                             0.3075
## itG
               0.116667
                          0.200512
                                    0.582
                                             0.5607
## itM
                                    0.401
               0.080057
                          0.199609
                                             0.6884
                                   -0.543
## drug2:itD
              -0.178972
                          0.329405
                                             0.5870
## drug3:itD
              -0.944849
                          0.472420
                                   -2.000
                                             0.0456 *
## drug2:itE
              -1.321429
                          0.714582
                                   -1.849
                                             0.0645 .
## drug3:itE
                     NA
                                NA
                                        NA
                                                 NA
## drug2:itG
                          0.292246
                                    -0.009
                                             0.9925
              -0.002729
## drug3:itG
              -0.862752
                          0.440155
                                    -1.960
                                             0.0501
## drug2:itM
              -0.028759
                          0.291370
                                   -0.099
                                             0.9214
## drug3:itM
              -0.843770
                          0.439548 - 1.920
                                             0.0550
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9503 on 2447 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.006476, Adjusted R-squared: 0.001198
## F-statistic: 1.227 on 13 and 2447 DF, p-value: 0.2527
##
## Response Data3$LMuFreq :
##
## Call:
## lm(formula = `Data3$LMuFreq` ~ drug * it)
## Residuals:
       Min
                 1Q
                      Median
                                   30
                                           Max
## -0.06859 -0.03658 -0.01446 0.02018
##
## Coefficients: (1 not defined because of singularities)
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.0393431 0.0110147
                                      3.572 0.000361 ***
## drug2
               0.0009367
                          0.0161238
                                      0.058 0.953677
## drug3
              -0.0069529
                          0.0246295
                                     -0.282 0.777738
## itD
                          0.0131304
                                      1.254 0.209981
               0.0164648
## itE
               0.0058906
                          0.0231795
                                      0.254 0.799418
## itG
                          0.0113861
                                      2.212 0.027089 *
               0.0251809
## itM
               0.0216787
                          0.0113348
                                      1.913 0.055918 .
## drug2:itD
               0.0013393
                          0.0187052
                                      0.072 0.942928
## drug3:itD
               0.0197308
                          0.0268263
                                      0.736 0.462105
## drug2:itE
               0.0007513
                          0.0405774
                                      0.019 0.985229
## drug3:itE
                      NA
                                 NΑ
                                         NΑ
                                                  NΑ
## drug2:itG
               0.0017932
                          0.0165951
                                      0.108 0.913962
## drug3:itG
              -0.0043914
                          0.0249941 -0.176 0.860545
## drug2:itM
```

```
## drug3:itM
               0.0096142 0.0249596 0.385 0.700130
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.05396 on 2447 degrees of freedom
    (3 observations deleted due to missingness)
## Multiple R-squared: 0.01073, Adjusted R-squared: 0.005478
## F-statistic: 2.042 on 13 and 2447 DF, p-value: 0.0147
##
##
## Response Data3$H_CDR3 :
##
## Call:
## lm(formula = `Data3$H_CDR3` ~ drug * it)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -9.5829 -2.0000 -0.0933 2.0023 13.7416
## Coefficients: (1 not defined because of singularities)
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 14.7917
                           0.6790 21.783
                           0.9940 -2.282
## drug2
               -2.2679
                                            0.0226 *
## drug3
               -3.2917
                           1.5184 -2.168
                                            0.0303 *
## itD
                           0.8095 -1.455
               -1.1776
                                           0.1458
                                   1.545
## itE
                2.2083
                           1.4290
                                           0.1224
## itG
               -0.2088
                           0.7019 -0.297
                                            0.7661
## itM
                           0.6988 -2.381
               -1.6639
                                           0.0173 *
## drug2:itD
               1.7472
                          1.1531
                                   1.515
                                           0.1299
## drug3:itD
                2.4436
                          1.6538
                                   1.478 0.1397
## drug2:itE
               -2.0655
                           2.5015 -0.826
                                           0.4091
## drug3:itE
                    NA
                               NA
                                       NA
                                                NA
## drug2:itG
                1.5118
                           1.0231
                                    1.478
                                            0.1396
## drug3:itG
                2.9672
                           1.5408
                                   1.926
                                           0.0543 .
## drug2:itM
                2.1378
                           1.0200
                                    2.096
                                            0.0362 *
## drug3:itM
                2.8823
                           1.5387
                                   1.873
                                           0.0612 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.327 on 2447 degrees of freedom
    (3 observations deleted due to missingness)
## Multiple R-squared: 0.04222, Adjusted R-squared: 0.03713
## F-statistic: 8.298 on 13 and 2447 DF, p-value: < 2.2e-16
##
## Response Data3$HMuFreq :
##
## Call:
## lm(formula = `Data3$HMuFreq` ~ drug * it)
## Residuals:
        Min
                   1Q
                         Median
                                       3Q
## -0.091172 -0.028366 -0.006062 0.024649 0.185109
##
```

```
## Coefficients: (1 not defined because of singularities)
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.063852
                           0.008280
                                      7.712 1.79e-14 ***
## drug2
               -0.010070
                           0.012121
                                     -0.831
                                               0.4062
## drug3
                0.015765
                           0.018514
                                      0.852
                                               0.3946
                                    -0.426
## itD
               -0.004201
                           0.009870
                                               0.6704
## itE
                                     -1.228
               -0.021395
                           0.017424
                                               0.2196
## itG
                0.015267
                           0.008559
                                      1.784
                                               0.0746
## itM
               -0.005718
                           0.008521 -0.671
                                               0.5022
## drug2:itD
               0.008037
                           0.014061
                                     0.572
                                               0.5677
## drug3:itD
               -0.025158
                           0.020166
                                     -1.248
                                               0.2123
## drug2:itE
                                      1.491
                0.045493
                           0.030503
                                               0.1360
## drug3:itE
                                 NA
                                          NΑ
                                                   NA
                      NA
                                               0.0763
## drug2:itG
                0.022123
                           0.012475
                                      1.773
## drug3:itG
               -0.036875
                                     -1.963
                                               0.0498 *
                           0.018788
## drug2:itM
                0.011428
                           0.012437
                                      0.919
                                               0.3583
## drug3:itM
               -0.019511
                           0.018763 -1.040
                                               0.2985
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.04056 on 2447 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.1012, Adjusted R-squared: 0.09639
## F-statistic: 21.18 on 13 and 2447 DF, p-value: < 2.2e-16
##
## Response Data3$Binding :
##
## Call:
## lm(formula = `Data3$Binding` ~ drug * it)
##
## Residuals:
##
       Min
                1Q Median
                                        Max
## -1.7208 -0.6290 -0.0707 -0.0147
                                   3.5273
## Coefficients: (1 not defined because of singularities)
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 0.5331
                            0.1989
                                      2.681
                                              0.0074 **
## drug2
                -0.4841
                            0.2911
                                    -1.663
                                              0.0965
## drug3
                 0.4137
                            0.4447
                                      0.930
                                              0.3523
## itD
                -0.4404
                            0.2371
                                    -1.858
                                              0.0633 .
## itE
                -0.4693
                            0.4185
                                    -1.121
                                              0.2623
## itG
                 0.3817
                            0.2056
                                     1.857
                                              0.0634
## itM
                -0.4274
                            0.2047
                                    -2.089
                                              0.0369 *
## drug2:itD
                 0.4918
                            0.3377
                                     1.456
                                              0.1455
## drug3:itD
                -0.4800
                            0.4844
                                     -0.991
                                              0.3218
## drug2:itE
                 0.8512
                            0.7326
                                      1.162
                                              0.2454
## drug3:itE
                     NA
                                NA
                                         NA
                                                  NA
## drug2:itG
                 0.2412
                            0.2996
                                      0.805
                                              0.4210
## drug3:itG
                 0.3922
                            0.4513
                                      0.869
                                              0.3849
                                      1.507
## drug2:itM
                 0.4501
                            0.2987
                                              0.1320
## drug3:itM
                -0.4600
                            0.4507
                                    -1.021
                                              0.3075
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.9743 on 2447 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.2467, Adjusted R-squared: 0.2427
## F-statistic: 61.64 on 13 and 2447 DF, p-value: < 2.2e-16
Finally, we use logistic regression.
All the p-values are large. I am wondering if we should take out the variable Reactivity and just focus on
Binding.
##
## Call:
  lm(formula = Data3$Reactivity ~ drug * it)
## Residuals:
##
        Min
                   1Q
                       Median
                                     30
                                             Max
## -0.60403 -0.25854 -0.06818 -0.05380
                                         0.95238
##
## Coefficients: (1 not defined because of singularities)
##
               Estimate Std. Error t value Pr(>|t|)
                                      2.792 0.00529 **
## (Intercept)
                0.20833
                            0.07463
## drug2
               -0.16071
                            0.10925
                                     -1.471
                                             0.14140
                                      0.749
## drug3
                0.12500
                            0.16688
                                             0.45390
                                     -1.356
## itD
               -0.12061
                            0.08897
                                             0.17531
## itE
               -0.06548
                            0.15705
                                     -0.417
                                             0.67679
## itG
                0.12594
                            0.07713
                                      1.633
                                             0.10261
## itM
               -0.11251
                            0.07680
                                     -1.465
                                             0.14306
                                      0.997
## drug2:itD
                0.12633
                            0.12674
                                             0.31898
## drug3:itD
               -0.12761
                            0.18176
                                     -0.702
                                             0.48270
                            0.27494
## drug2:itE
                0.35119
                                      1.277
                                             0.20160
## drug3:itE
                                         NA
                      NA
                                 NA
                                                   NA
## drug2:itG
                0.08497
                            0.11243
                                      0.756
                                             0.44984
                0.14475
## drug3:itG
                            0.16934
                                      0.855
                                             0.39276
## drug2:itM
                0.13307
                            0.11210
                                      1.187
                                             0.23533
## drug3:itM
               -0.16703
                            0.16912
                                     -0.988
                                             0.32343
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3656 on 2450 degrees of freedom
## Multiple R-squared: 0.1937, Adjusted R-squared: 0.1894
## F-statistic: 45.28 on 13 and 2450 DF, p-value: < 2.2e-16
```

#### Pairwise comparison

To know more details about which groups have different means, we use pairwise comparisons for each treatment group, drug, and Isotype. (We set  $\alpha$  as 0.05, and it is adjusted based on the number of pairs and variables being compared.)

```
[1] "L_CDR3 pairwise CI's"
##
   contrast
                      estimate
                                    SE
                                         df lower.CL upper.CL
##
   group 1 - group 2 0.08842 0.0829 2454
                                             -0.2016
                                                        0.378
   group 1 - group 3 -0.03487 0.1047 2454
                                             -0.4012
                                                        0.331
   group 1 - group 4 0.11097 0.0599 2454
                                             -0.0987
                                                        0.321
##
   group 1 - group 5 -0.01158 0.0630 2454
                                             -0.2321
                                                        0.209
                                             -0.2380
##
   group 1 - group 6 0.08361 0.0919 2454
                                                        0.405
   group 1 - group 7 0.11559 0.0540 2454
                                             -0.0732
                                                        0.304
```

```
group 2 - group 3 -0.12328 0.1213 2454
                                            -0.5477
                                                        0.301
                                                        0.322
##
   group 2 - group 4 0.02255 0.0857 2454
                                            -0.2773
   group 2 - group 5 -0.10000 0.0879 2454
                                            -0.4075
                                                        0.208
   group 2 - group 6 -0.00480 0.1105 2454
                                            -0.3913
                                                        0.382
##
##
    group 2 - group 7 0.02717 0.0816 2454
                                            -0.2584
                                                        0.313
   group 3 - group 4 0.14583 0.1070 2454
##
                                            -0.2283
                                                        0.520
   group 3 - group 5 0.02328 0.1087 2454
                                            -0.3571
                                                        0.404
   group 3 - group 6 0.11848 0.1277 2454
                                            -0.3282
##
                                                        0.565
##
   group 3 - group 7 0.15046 0.1037 2454
                                            -0.2124
                                                        0.513
##
    group 4 - group 5 -0.12255 0.0667 2454
                                            -0.3559
                                                        0.111
   group 4 - group 6 -0.02735 0.0945 2454
                                            -0.3579
                                                        0.303
   group 4 - group 7 0.00462 0.0582 2454
                                                        0.208
##
                                            -0.1990
   group 5 - group 6 0.09520 0.0965 2454
##
                                            -0.2423
                                                        0.433
   group 5 - group 7 0.12717 0.0614 2454
                                            -0.0876
                                                        0.342
   group 6 - group 7 0.03198 0.0908 2454
                                                        0.350
##
                                            -0.2857
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
   [1] "LMuFreq pairwise CI's"
##
   contrast
                       estimate
                                     SE
                                          df lower.CL upper.CL
   group 1 - group 2 0.007328 0.00472 2454 -0.00918
##
   group 1 - group 3 -0.006001 0.00596 2454 -0.02686
                                                       0.01486
##
   group 1 - group 4 0.002551 0.00341 2454 -0.00939
                                                       0.01449
   group 1 - group 5 -0.000993 0.00359 2454 -0.01355
                                                       0.01156
##
   group 1 - group 6 -0.001342 0.00523 2454 -0.01966
                                                       0.01697
   group 1 - group 7 0.003112 0.00307 2454 -0.00764
##
                                                       0.01386
   group 2 - group 3 -0.013330 0.00691 2454 -0.03750
                                                       0.01084
    group 2 - group 4 -0.004778 0.00488 2454 -0.02185
                                                       0.01230
   group 2 - group 5 -0.008322 0.00500 2454 -0.02583
                                                       0.00919
##
    group 2 - group 6 -0.008670 0.00629 2454 -0.03068
                                                       0.01334
##
   group 2 - group 7 -0.004216 0.00465 2454 -0.02048
                                                       0.01205
   group 3 - group 4 0.008552 0.00609 2454 -0.01275
                                                       0.02986
##
   group 3 - group 5 0.005008 0.00619 2454 -0.01665
                                                       0.02667
    group 3 - group 6 0.004659 0.00727 2454 -0.02077
##
   group 3 - group 7 0.009114 0.00591 2454 -0.01155
                                                       0.02978
   group 4 - group 5 -0.003544 0.00380 2454 -0.01683
##
   group 4 - group 6 -0.003893 0.00538 2454 -0.02271
                                                       0.01493
    group 4 - group 7 0.000562 0.00331 2454 -0.01103
##
                                                       0.01216
##
   group 5 - group 6 -0.000349 0.00549 2454 -0.01957
                                                       0.01887
   group 5 - group 7 0.004106 0.00350 2454 -0.00812
                                                       0.01633
   group 6 - group 7 0.004454 0.00517 2454 -0.01364
                                                       0.02254
##
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
## [1] "H_CDR3 pairwise CI's"
##
   contrast
                      estimate
                                  SE
                                       df lower.CL upper.CL
   group 1 - group 2
                        0.5757 0.295 2454 -0.45488
                                                      1.606
##
                        0.9285 0.372 2454 -0.37339
                                                       2.230
   group 1 - group 3
##
                        0.9693 0.213 2454 0.22406
                                                       1.715
   group 1 - group 4
   group 1 - group 5
                        0.3928 0.224 2454 -0.39095
                                                       1.177
##
   group 1 - group 6
                        0.7509 0.327 2454 -0.39208
                                                      1.894
   group 1 - group 7
                        0.6651 0.192 2454 -0.00594
                                                       1.336
```

```
group 2 - group 3
                        0.3528 0.431 2454 -1.15543
                                                      1.861
##
                       0.3936 0.305 2454 -0.67188
                                                      1.459
   group 2 - group 4
   group 2 - group 5
                      -0.1829 0.312 2454 -1.27567
                                                      0.910
   group 2 - group 6
                        0.1753 0.393 2454 -1.19820
##
                                                      1.549
##
   group 2 - group 7
                        0.0894 0.290 2454 -0.92557
                                                      1.104
##
                        0.0408 0.380 2454 -1.28891
                                                      1.371
   group 3 - group 4
   group 3 - group 5 -0.5357 0.386 2454 -1.88738
                                                      0.816
##
   group 3 - group 6 -0.1776 0.454 2454 -1.76477
                                                      1.410
##
   group 3 - group 7
                      -0.2634 0.369 2454 -1.55299
                                                      1.026
##
   group 4 - group 5 -0.5765 0.237 2454 -1.40570
                                                      0.253
   group 4 - group 6 -0.2184 0.336 2454 -1.39301
                                                      0.956
##
   group 4 - group 7 -0.3042 0.207 2454 -1.02780
                                                      0.419
##
   group 5 - group 6
                       0.3581 0.343 2454 -0.84126
                                                      1.558
   group 5 - group 7
                        0.2723 0.218 2454 -0.49084
                                                      1.035
   group 6 - group 7 -0.0858 0.323 2454 -1.21483
                                                      1.043
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
  [1] "HMuFreq pairwise CI's"
##
   contrast
                       estimate
                                     SE
                                          df lower.CL
                                                      upper.CL
   group 1 - group 2 0.001782 0.00367 2454 -0.01105
                                                       0.014613
##
   group 1 - group 3 0.014768 0.00463 2454 -0.00144
                                                       0.030977
   group 1 - group 4 -0.000904 0.00265 2454 -0.01018
                                                       0.008375
   group 1 - group 5 -0.005563 0.00279 2454 -0.01532
##
                                                       0.004195
   group 1 - group 6 -0.009779 0.00407 2454 -0.02401
                                                       0.004452
   group 1 - group 7 0.013055 0.00239 2454 0.00470
##
                                                       0.021410
   group 2 - group 3 0.012986 0.00537 2454 -0.00579
                                                       0.031765
   group 2 - group 4 -0.002686 0.00379 2454 -0.01595
                                                       0.010580
                                                       0.006261
   group 2 - group 5 -0.007345 0.00389 2454 -0.02095
##
   group 2 - group 6 -0.011561 0.00489 2454 -0.02866
                                                       0.005539
   group 2 - group 7 0.011273 0.00361 2454 -0.00136
##
                                                       0.023910
   group 3 - group 4 -0.015672 0.00473 2454 -0.03223
##
   group 3 - group 5 -0.020331 0.00481 2454 -0.03716 -0.003502
    group 3 - group 6 -0.024547 0.00565 2454 -0.04431 -0.004785
##
   group 3 - group 7 -0.001713 0.00459 2454 -0.01777 0.014343
   group 4 - group 5 -0.004659 0.00295 2454 -0.01498 0.005665
##
   group 4 - group 6 -0.008875 0.00418 2454 -0.02350
                                                       0.005750
   group 4 - group 7 0.013959 0.00258 2454 0.00495
##
                                                       0.022968
   group 5 - group 6 -0.004216 0.00427 2454 -0.01915
##
                                                       0.010717
   group 5 - group 7 0.018618 0.00272 2454 0.00912
   group 6 - group 7 0.022834 0.00402 2454 0.00878
                                                      0.036891
##
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
## [1] "Binding pairwise CI's"
##
   contrast
                      estimate
                                   SE
                                        df lower.CL upper.CL
   group 1 - group 2 -0.5394 0.0951 2454
                                           -0.8721
                                                    -0.2066
   group 1 - group 3
                       0.3560 0.1202 2454
                                            -0.0644
                                                      0.7763
                                            -0.2608
##
   group 1 - group 4 -0.0201 0.0688 2454
                                                      0.2205
   group 1 - group 5
                      0.0164 0.0723 2454
                                            -0.2366
                                                      0.2695
##
   group 1 - group 6
                       0.3819 0.1055 2454
                                             0.0129
                                                      0.7510
   group 1 - group 7 -0.4236 0.0619 2454
                                           -0.6403 -0.2070
```

```
group 2 - group 3
                      0.8953 0.1392 2454
                                           0.4083
                                                    1.3823
                                                    0.8633
                      0.5192 0.0983 2454 0.1752
   group 2 - group 4
## group 2 - group 5
                      0.5558 0.1009 2454
                                           0.2029
                                                    0.9086
## group 2 - group 6
                      0.9213 0.1268 2454
                                           0.4778
                                                    1.3648
   group 2 - group 7
                      0.1157 0.0937 2454 -0.2120
                                                    0.4434
   group 3 - group 4 -0.3761 0.1227 2454
                                         -0.8055 0.0532
  group 3 - group 5 -0.3395 0.1248 2454
                                          -0.7760
                                                    0.0969
                                                    0.5384
##
   group 3 - group 6
                      0.0259 0.1465 2454
                                          -0.4866
   group 3 - group 7 -0.7796 0.1190 2454
                                          -1.1960 -0.3632
   group 4 - group 5
                     0.0366 0.0765 2454
                                         -0.2311
                                                    0.3043
## group 4 - group 6
                     0.4021 0.1084 2454
                                           0.0228
                                                    0.7813
   group 4 - group 7 -0.4035 0.0668 2454
                                          -0.6371 -0.1699
   group 5 - group 6 0.3655 0.1107 2454
                                          -0.0218
                                                    0.7528
   group 5 - group 7 -0.4401 0.0704 2454 -0.6865 -0.1937
## group 6 - group 7 -0.8056 0.1042 2454 -1.1701 -0.4410
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
## [1] "L_CDR3 pairwise CI's"
  contrast estimate
                         SE
                             df lower.CL upper.CL
## 1 - 2
             0.0451 0.0450 2458 -0.0870
                                           0.177
## 1 - 3
              0.1018 0.0492 2458 -0.0429
                                            0.246
## 2 - 3
              0.0567 0.0480 2458 -0.0844
                                            0.198
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.996666666666667
## [1] "LMuFreq pairwise CI's"
## contrast estimate
                           SE
                               df lower.CL upper.CL
## 1 - 2
           -0.000176 0.00256 2458 -0.00770 0.00735
## 1 - 3
             0.002320 0.00280 2458 -0.00592 0.01056
## 2 - 3
             0.002496 0.00273 2458 -0.00554 0.01053
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.9966666666666667
## [1] "H_CDR3 pairwise CI's"
## contrast estimate
                        SE
                           df lower.CL upper.CL
## 1 - 2 0.4907 0.160 2458
                                0.0204
                                           0.961
## 1 - 3
             0.4438 0.175 2458 -0.0712
                                           0.959
## 2 - 3
             -0.0469 0.171 2458 -0.5492
                                           0.456
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.99666666666667
## [1] "HMuFreq pairwise CI's"
                          SE df lower.CL upper.CL
  contrast estimate
## 1 - 2
             -0.006 0.00199 2458 -0.01186 -0.000145
##
   1 - 3
              0.011 0.00218 2458 0.00461 0.017432
## 2 - 3
              0.017 0.00213 2458 0.01076 0.023276
## Results are averaged over the levels of: rep.meas
```

```
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.9966666666666667
## [1] "Binding pairwise CI's"
   contrast estimate
                         SE
                               df lower.CL upper.CL
   1 - 2
               0.118 0.0522 2458
                                  -0.0355
                                              0.271
## 1 - 3
                                 -0.5235
                                             -0.188
              -0.356 0.0571 2458
## 2 - 3
              -0.473 0.0557 2458 -0.6372
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.996666666666667
## [1] "L_CDR3 pairwise CI's"
   contrast estimate
                         SE
                              df lower.CL upper.CL
   A - D
              0.1136 0.1510 2456
                                  -0.3838
                                              0.611
##
   A - E
              0.0667 0.3289 2456
                                              1.150
                                  -1.0170
   A - G
              0.0041 0.1364 2456
                                  -0.4451
                                              0.453
##
  A - M
              0.0441 0.1361 2456
                                  -0.4042
                                              0.492
  D - E
             -0.0469 0.3091 2456
                                  -1.0651
                                              0.971
## D - G
             -0.1095 0.0769 2456
                                  -0.3627
                                              0.144
## D - M
             -0.0695 0.0764 2456
                                  -0.3210
                                              0.182
##
  E - G
                                              0.933
             -0.0626 0.3022 2456
                                  -1.0581
  E - M
             -0.0225 0.3021 2456
                                  -1.0177
                                              0.973
## G - M
              0.0400 0.0404 2456
                                 -0.0931
                                              0.173
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
## [1] "LMuFreq pairwise CI's"
   contrast estimate
                            SE
                                df lower.CL upper.CL
  A - D
##
            -0.021206 0.00858 2456 -0.04947 0.00705
##
   A - E
            -0.006829 0.01869 2456 -0.06840
                                              0.05475
##
   A - G
            -0.023476 0.00775 2456 -0.04900
                                             0.00205
   A - M
            -0.021669 0.00773 2456 -0.04714
                                              0.00380
## D - E
             0.014376 0.01756 2456 -0.04348
                                              0.07223
## D - G
            -0.002270 0.00437 2456 -0.01666
                                              0.01212
## D - M
            -0.000463 0.00434 2456 -0.01476
                                             0.01383
  E - G
            -0.016647 0.01717 2456 -0.07321
                                             0.03992
## E - M
            -0.014839 0.01716 2456 -0.07138
                                              0.04170
##
             0.001807 0.00230 2456 -0.00576 0.00937
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
## [1] "H_CDR3 pairwise CI's"
   contrast estimate
                         SE
                             df lower.CL upper.CL
##
   A - D
               0.297 0.530 2456
                                  -1.448
                                             2.043
   A - E
##
              -2.229 1.154 2456
                                  -6.032
                                             1.574
##
  A - G
              -0.728 0.479 2456
                                  -2.304
                                             0.849
##
  A - M
                                  -1.070
               0.503 0.478 2456
                                             2.076
## D - E
              -2.527 1.085 2456
                                  -6.100
                                            1.046
## D - G
              -1.025 0.270 2456
                                  -1.914
                                            -0.137
  D - M
               0.206 0.268 2456
                                  -0.677
                                            1.089
## E - G
               1.502 1.060 2456
                                             4.995
                                  -1.992
```

```
2.733 1.060 2456
                                   -0.760
                                             6.225
## G - M
                1.231 0.142 2456
                                    0.764
                                              1.698
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
## [1] "HMuFreq pairwise CI's"
   contrast estimate
                           SE
                                df lower.CL upper.CL
   A - D
              0.00523 0.00659 2456
                                    -0.0165
                                            0.02693
##
   A - E
                                    -0.0388
              0.00848 0.01435 2456
                                            0.05576
   A - G
             -0.01628 0.00595 2456
                                    -0.0359
                                            0.00332
  A - M
##
              0.00393 0.00594 2456
                                    -0.0156
                                             0.02349
   D - E
              0.00325 0.01349 2456
                                    -0.0412 0.04768
##
   D - G
             -0.02151 0.00335 2456
                                    -0.0326 -0.01046
   D - M
             -0.00130 0.00333 2456
                                    -0.0123
                                             0.00968
   E - G
##
             -0.02476 0.01319 2456
                                    -0.0682
                                             0.01868
##
   E - M
                                    -0.0480
             -0.00455 0.01318 2456
                                             0.03888
##
   G - M
              0.02021 0.00176 2456
                                     0.0144 0.02602
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
## [1] "Binding pairwise CI's"
   contrast estimate
                          SE
                               df lower.CL upper.CL
   A - D
##
                                    -0.227
                                              0.834
              0.30395 0.1610 2456
   A - E
              0.20847 0.3508 2456
                                    -0.947
                                              1.364
##
  A - G
             -0.66527 0.1454 2456
                                    -1.144
                                              -0.186
   A - M
              0.30220 0.1451 2456
                                    -0.176
                                              0.780
##
  D - E
             -0.09548 0.3296 2456
                                    -1.181
                                              0.990
   D - G
             -0.96922 0.0820 2456
                                    -1.239
                                             -0.699
  D - M
##
             -0.00175 0.0814 2456
                                    -0.270
                                              0.267
##
   E - G
             -0.87374 0.3223 2456
                                    -1.936
                                              0.188
##
   E - M
              0.09373 0.3222 2456
                                    -0.968
                                               1.155
   G - M
##
              0.96747 0.0431 2456
                                     0.825
                                               1.109
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
```

Here are the pairs that have significant differences:

#### • Treatment

```
L_CDR3: none
LMuFreq: none
H_CDR3:
    * group 1 > group 4
HMuFreq:
    * group 3 < group 5
    * group 3 < group 6
    * group 5 > group 7
    * group 6 > group 7
Binding:
    * group 1 < group 2
    * group 5 > group 6
```

```
* group 2 > \text{group } 3
          * group 2 > \text{group } 4
          * group 2 > \text{group } 5
          * group 2 > \text{group } 6
          * group 3 < \text{group } 7
          * group 4 > \text{group } 6
          * group 4 < \text{group } 7
          * group 5 < \text{group } 7
          * group 6 < \text{group } 7
• Drug
     - L CDR3: none
     - LMuFreq: none
     - H CDR3:
          * 1 > 2
     - HMuFreq:
          * 1 < 2
          * 1 > 3
          * 2 > 3
     - Binding:
          *1 < 3
          * 2 < 3

    Isotype

     - L_CDR3: none

    LMuFreq: none

     − H CDR3:
          * IgD < IgG
     - HMuFreq:
          * IgD < IgG
          * IgG > IgM
     - Binding:
          * IgA < IgG
          * IgD < IgG
          * IgG > IgM
```

In short, L\_CDR3 and LMuFreq do not have significant paired differences.

For H\_CDR3, treatment group 1 (drug 1) is higher than treatment group 7 (control), and IgG has a longer H\_CDR3 length than IgD.

For HMuFreq, drug 2 has the highest mean, followed by drug 1 and control. More specifically, treatment groups 5 and 6 (two doses in drug 2) have the highest mutation rates. IgG has higher mutation rate than IgD.

For Binding, drug 3 has the highest mean, but drug 1 and drug 2 do not have significant differences. IgG has higher binding rate than IgA, IgD, and IgM.

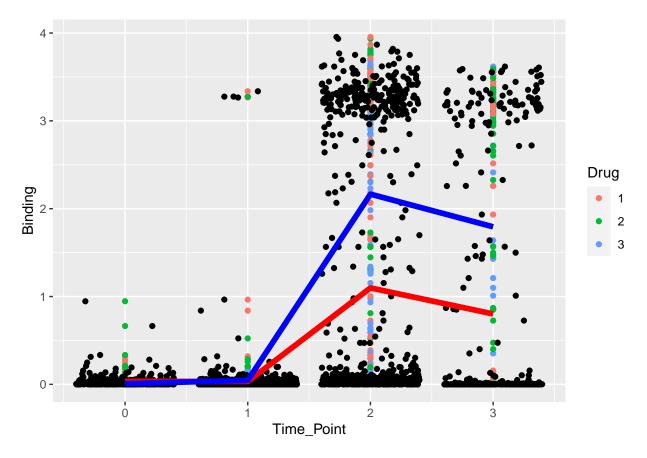
We could conclude that the drugs/treatment groups do increase mutation rate; however, they do not increase binding rate. That is to say, although the treatments do help increase the diversity of antibodies, they are not specific to the HIV antigens and thus do not increase binding.

## Longitudinal Data Analysis

This section probably needs some more revisions, since we still have three more lectures.

First we don't consider treatments but only plot the mean trend over time. The plot shows that bindign does vary over time. The red line shows the mean trend over time, and the blue line shows the variance over time. The variance does not seem equal over time, so we use unequal variance over time for the covariance structure.

$$Y_{ij} = \beta_0 + \beta_1 Time_{ij} + e_{ij}$$



Here we use Binding as the response, Time\_Point as the time factor, and Drug as the covariates. Random effect for both intercept and slope. Now we want to add one covariate: Drug. We use two indicator variables: D1 and D2, where

$$D1 = \begin{cases} 1 & \text{if Drug} = 1\\ 0 & \text{otherwise} \end{cases}$$

$$D2 = \begin{cases} 1 & \text{if Drug} = 2\\ 0 & \text{otherwise} \end{cases}$$

Assuming that the random effects are the same for each drug, our full model is:

$$Y_{ij} = \beta_0 + \beta_1 Time_{ij} + D1_i(\beta_2 + \beta_3 Time_{ij}) + D2_i(\beta_4 + \beta_5 Time_{ij}) + b_{0i} + b_{1i} Time_{ij} + e_{ij}$$

$$\mathbf{b_i} \sim N \left( 0, \mathbf{D} = \begin{bmatrix} D_{11} & D_{12} \\ D_{12} & D_{22} \end{bmatrix} \right)$$

Drug 1:  $Y_{ij} = \beta_0 + \beta_1 Time_{ij} + \beta_2 + \beta_3 Time_{ij} + b_{0i} + b_{1i} Time_{ij} + e_{ij}$ Drug 2:  $Y_{ij} = \beta_0 + \beta_1 Time_{ij} + \beta_4 + \beta_5 Time_{ij} + b_{0i} + b_{1i} Time_{ij} + e_{ij}$ Drug 3:  $Y_{ij} = \beta_0 + \beta_1 Time_{ij} + b_{0i} + b_{1i} Time_{ij} + e_{ij}$ 

```
## Linear mixed-effects model fit by REML
##
   Data: dataLDA
##
          AIC
                   BIC
                          logLik
##
     3673.651 3749.144 -1823.826
##
## Random effects:
   Formula: ~Time Point | id
   Structure: General positive-definite, Log-Cholesky parametrization
##
               StdDev
                         Corr
## (Intercept) 0.6893734 (Intr)
## Time_Point 0.6524155 -0.999
## Residual
               0.2169511
##
## Variance function:
  Structure: Different standard deviations per stratum
   Formula: ~1 | Time_Point
##
   Parameter estimates:
##
           1
                     0
## 1.0000000 0.3827704 7.1563614 6.5754859
## Fixed effects: binding ~ Time_Point + D1 + D1:Time_Point + D2 + D2:Time_Point
##
                      Value Std.Error
                                        DF
                                              t-value p-value
## (Intercept)
                 -0.0432994 0.3982221 2441 -0.1087318 0.9134
## Time_Point
                  0.1772970 0.3772249 2441 0.4700034 0.6384
## D1
                 -0.3162408 0.5043030
                                        17 -0.6270850
                                                       0.5389
## D2
                 -0.8725346 0.5123761
                                        17 -1.7029181
                                                       0.1068
## Time_Point:D1 0.2407466 0.4811398 2441
                                           0.5003672 0.6169
## Time_Point:D2 0.7867662 0.4891206 2441
                                            1.6085323 0.1078
##
   Correlation:
##
                 (Intr) Tm_Pnt D1
                                      D2
                                             T_P:D1
## Time_Point
                 -0.998
## D1
                 -0.790 0.788
## D2
                 -0.777 0.775 0.614
## Time_Point:D1 0.782 -0.784 -0.998 -0.608
## Time_Point:D2 0.769 -0.771 -0.608 -0.998
                                              0.605
## Standardized Within-Group Residuals:
                                                Q3
                                                            Max
## -1.18636862 -0.29361355 -0.10681754 0.02325697 15.04537744
##
## Number of Observations: 2464
## Number of Groups: 20
```

The p-values for Drug and the interaction of Drug and Time\_Point are large. So we try another model with Time\_Point as the only predictor.

$$Y_{ij} = \beta_0 + \beta_1 Time_{ij} + b_{0i} + b_{1i} Time_{ij} + e_{ij}$$

$$\underbrace{\begin{bmatrix} Y_{i1} \\ \vdots \\ Y_{im_i} \end{bmatrix}}_{\mathbf{Y}_{:}} = \underbrace{\begin{bmatrix} 1 & Time_{i1} \\ \vdots & \vdots \\ 1 & Time_{im_i} \end{bmatrix}}_{\mathbf{Y}_{:}} \underbrace{\begin{bmatrix} \beta_0 \\ \beta_1 \end{bmatrix}}_{\beta} + \underbrace{\begin{bmatrix} 1 & Time_{i1} \\ \vdots & \vdots \\ 1 & Time_{im_i} \end{bmatrix}}_{\mathbf{Z}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{b}_{i}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} b_{0i} \\ b_{1i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\ e_{im_i} \end{bmatrix}}_{\mathbf{e}_{:}} + \underbrace{\begin{bmatrix} e_{i1} \\ \vdots \\$$

$$\mathbf{b_i} \sim N \left( 0, \mathbf{D} = \begin{bmatrix} D_{11} & D_{12} \\ D_{12} & D_{22} \end{bmatrix} \right)$$
$$\mathbf{e}_{ij} \sim N(0, \mathbf{R}_i = \sigma^2 I_{mi})$$

[need to consider whether time point 2 is the optimal point]

```
## Linear mixed-effects model fit by REML
##
    Data: dataLDA
##
          AIC
                  BIC
                         logLik
##
     3661.551 3713.83 -1821.776
##
## Random effects:
    Formula: ~Time_Point | id
##
##
    Structure: General positive-definite, Log-Cholesky parametrization
                         Corr
##
               StdDev
   (Intercept) 0.6628601 (Intr)
## Time_Point 0.6255252 -0.998
## Residual
               0.2163048
##
  Variance function:
##
##
    Structure: Different standard deviations per stratum
    Formula: ~1 | Time_Point
##
    Parameter estimates:
##
           1
                                2
  1.0000000 0.3842252 7.1971216 6.6106513
  Fixed effects: binding ~ Time_Point
##
##
                    Value Std.Error
                                       DF
                                            t-value p-value
  (Intercept) -0.5031390 0.1871486 2443 -2.688447 0.0072
## Time_Point
                0.5695081 0.1798267 2443 3.166983 0.0016
    Correlation:
##
##
## Time_Point -0.998
##
## Standardized Within-Group Residuals:
##
           Min
                        Q1
                                    Med
                                                 Q3
  -1.15655984 -0.26620653 -0.11153392 0.02881313 15.06729096
##
##
## Number of Observations: 2464
## Number of Groups: 20
```

This simpler model has lower AIC and BIC, as shown below. So we prefer the model with Time\_Point as the predictor and, with the low p-values of the slope of Time\_Point, conclude that the binding rates vary over time. In other words, the number of HIV vaccines given do affect the binding rate, but the drugs given do not have significant effects.

```
## df AIC df.1 BIC
## lda 13 3673.651 13 3749.144
## lda2 9 3661.551 9 3713.830
```

## Discussion

In this study we used both multivariate and longitudinal data analysis to examine the effects of HIV vaccines and Treg suppression treatments. Although the study provides evidence to support the concept of using

immunosuppressing treatments to increase diversity, the added diversity does not seem to improve the binding rate. In other words, this study does not provide evidence to show that the added treatments can enhance the effects of HIV vaccines.

## List of variables

- Treatment: Treatment A is the mock control, and treatment B and C are two different kinds of Treg inhibitor treatments.
- Time Points: 0 represents before immunization; 1 represents 2 weeks post 1st immunization; 2 represents 2 weeks post 2nd immunization; and 3 represents 2 weeks post 3rd immunization, respectively.
- Isotype: the category of antibody type
- H ID and L ID: heavy chain and light chain IDs for the particular observation
- H\_V, H\_D and H\_J: the gene segments used in heavy chain VDJ recombination in that antibody. The same applies to L\_V and L\_J
- H VBase: the number of nucleotide of the heavy chain variable region
- H Substitutions, H Insertions, H Deletions: the number of relative nucleotide mutations.
- HMuFreq: calculated by H\_Substitutions / H\_VBase
- H\_CDR3: the number of amino acid of the heavy chain's third complementarity determining region
- Binding: affinity of antibodies against a selected HIV glycoprotein. The larger value indicates stronger binding

## Reference

The dataset, which can be found here, was provided by Kan Luo, as he was one of authors for the following four publications that used the dataset:

- 1. Luo K, Liao HX, Zhang R, et al. Tissue memory B cell repertoire analysis after ALVAC/AIDSVAX B/E gp120 immunization of rhesus macaques. *JCI Insight*. 2016;1(20):e88522. Published 2016 Dec 8. doi:10.1172/jci.insight.88522
- 2. Bradley, T., Kuraoka, M., Yeh, C.-H., Tian, M., Chen, H., Cain, D. W., . . . Haynes, B. F. (2020). Immune checkpoint modulation enhances HIV-1 antibody induction. *Nature Communications*, 11(1), 948. doi:10.1038/s41467-020-14670-w
- 3. Easterhoff, D., Pollara, J., Luo, K., Tolbert, W. D., Young, B., Mielke, D., . . . Ferrari, G. (2020). Boosting with AIDSVAX B/E Enhances Env Constant Region 1 and 2 Antibody-Dependent Cellular Cytotoxicity Breadth and Potency. *Journal of Virology*, 94(4), e01120-01119. doi:10.1128/jvi.01120-19
- 4. Wiehe, K., Easterhoff, D., Luo, K., Nicely, N. I., Bradley, T., Jaeger, F. H., Dennison, S. M., Zhang, R., Lloyd, K. E., Stolarchuk, C., Parks, R., Sutherland, L. L., Scearce, R. M., Morris, L., Kaewkungwal, J., Nitayaphan, S., Pitisuttithum, P., Rerks-Ngarm, S., Sinangil, F., Phogat, S., ... Haynes, B. F. (2014). Antibody light-chain-restricted recognition of the site of immune pressure in the RV144 HIV-1 vaccine trial is phylogenetically conserved. *Immunity*, 41(6), 909–918. https://doi.org/10.1016/j.immuni.2014.11.014
  - 5.Lefranc MP, Giudicelli V, Ginestoux C, Bodmer J, Muller W, Bontrop R, Lemaitre M, Malik A, Barbie V, Chaume D. IMGT, the international ImMunoGeneTics database. *Nucleic Acids Res.* 1999;27:209–212. doi: 10.1093/nar/27.1.209.
  - 6.Jenny M Woof, Dennis R Burton, Human antibody-Fc receptor interactions illuminated by crystal structures. Nat Rev Immunol. 2004 Feb;4(2):89-99. doi: 10.1038/nri1266. 7.Pinheiro J, Bates D, DebRoy S, Sarkar D, R Core Team (2020). nlme: Linear and Nonlinear Mixed Effects Models. R package version 3.1-150, <URL: https://CRAN.R-project.org/package=nlme>.