### Final Project – Second Draft

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### Questions/next steps

- Questions for Kan marked as [Kan...] below.
- Comments for future addition and revisions in [...]
- Instead of looking at average of Binding, look at average of reactivity to see the percentage of reactive
- Variances can be very different in different cells
- How to hide message from API?
- The resulting dataset from this section is called Data2, and one outlier will be removed in a later section, which results in a final dataset Data3. So Data3 is used for analysis.
- Who can figure out how to put all figures and tables after all text and before supplmental materials?
- Use the caret package to do training and predition?
- Please do condense any tables or figures if you see a way to do so.
- Longitudinal analysis: consider how to show whether time point 2 is the peak and if the difference is significant
- ## Response [https://raw.githubusercontent.com/luokan1227/537P1/master/Data.xlsx]
- ## Date: 2020-10-25 05:18

```
##
     Status: 200
##
     Content-Type: application/octet-stream
##
  <ON DISK>
             C:\Users\shihn\AppData\Local\Temp\RtmpeSTpzF\file39d87e646098.xlsx
##
## Response [https://raw.githubusercontent.com/luokan1227/537P1/master/MonkeyID.xlsx]
    Date: 2020-10-25 05:18
##
##
     Status: 200
##
     Content-Type: application/octet-stream
##
     Size: 50.1 kB
  <ON DISK> C:\Users\shihn\AppData\Local\Temp\RtmpeSTpzF\file39d8384a78.xlsx
```

#### Abstract

### Introduction

A dominant vaccine development strategy is to induce neutralizing antibodies by immunizing humans with the virus' glycoproteins. However, HIV vaccines that adopted this strategy mostly failed due to the fact that HIV is an RNA virus, which mutates rapidly to escape the inhibition of neutralizing antibodies. In other words, by the time the body generates neutralizing antibodies against the glycoproteins of some HIV strains, the RNA virus has already mutated. Thus, the existing neutralizing antibody fails to recognize, bind with, and neutralize the HIV virus. One possible solution is to increase the number of potential neutralizing antibodies that will cycle in the body by releasing a variety of antibodies after glycoprotein immunization.

Our dataset includes 23 variables (measurements of antibodies) after 20 rhesus macaques were given the same HIV vaccine at three different time points and one of three randomly selected anti-Treg treatments. Although only 20 animals were in the study, antibodies are viewed as independent in the study of vaccines, and therefore we treat these 2,239 observations as independent. Blood samples were collected two weeks after vaccine dosing, and antibodies were isolated from those samples. A different number of antibodies were collected from each blood sample, limited by assay yield. Each observation contains information about the antibody isolated post the glycoprotein immunization. For our final project, we plan to determine if the different Treg treatments and number of vaccine injections cause changes in the antibody characteristics and if the changes are related to immunization/treatment timepoints.

### Methodologies

During the experiment, monkeys (rhesus macaques) were given glycoprotein immunization and supplemental antibody doses, as well as one of three treatments (two experimental regulatory T-cell suppression treatments and one control). Regulatory T (Treg) cells prevent autoimmune diseases and suppress allergic reactions by inhibiting adaptive antibody immune response in the germinal center. Theoretically, this adaptive response lowers the effectiveness of vaccines. Thus the experiment used T-cell suppression treatments to investigate the effect on immunization. These drugs are widely used in post transplant immunosuppression treatment to prevent rejection.

#### **Data Summaries**

Our data came from a vaccine study, in which 20 rhesus marcaque was given HIV vaccines as well as immunosuppressing treatments that can inhibit human body's mechanism to suppress antibodies and, in theory, enhance the effect of vaccines. The dataset has 2465 data points, 20 rhesus monkeys.

```
6104 6105 6107 6117 6118 6119 6125 6132 6160 6193 6199 6200 6201 6202 6203 6204
  35
      228
           239
                243
                       7
                            55
                               216
                                    251
                                          183
                                              117
                                                     48
                                                         191
                                                               73
                                                                     78
                                                                         238
```

```
## 6205 6209 6210 6214
## 5 46 50 6
```

In the current analysis, each row represents one antibody and its measurements. While it is possible to treat the 20 rhesus macaques as the observational units, the analysis will become quite complex. We would have to use information from gene segments of the heavy and light chains of the antibodies to classify each antibody. There are five such segments, and each has 6 to 11 subtypes. (In total, there can be  $7*7*6*11*6=1.9404\times10^4$  combinations of gene segments.) Thus, we decided to follow the convention of vaccine studies and treat each antibody as independent.

The main goal of the study is to test whether any procedures can incease the diversity of antibodies and thus enhance the effectiveness of vaccines. Our predictors are time points, which indicates time and the number of vaccines given up to that point, treatment or drug, and Isotype. We first take a look at these variables.

There are four time points; one before any procedure was done, and three after vaccine shots were administered to the macaques. In the treatment groups, groups 1-3 represent different doses of drug 1, groups 4-6 represent different doses of drug 2, and group 7 represents the control group. Later we'll look at the effect made by different drugs first and then different doses.

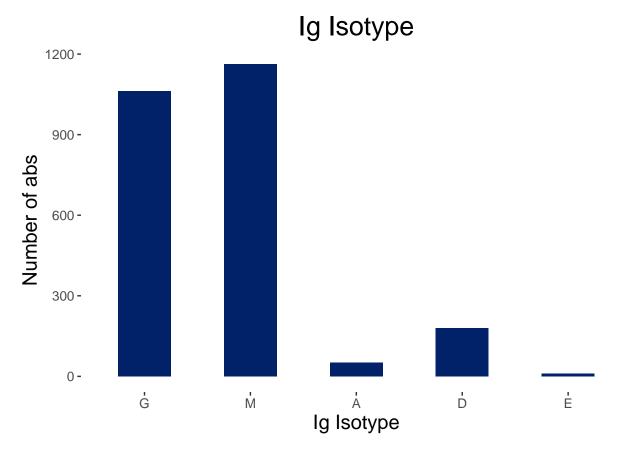
	group 1	group 2	group 3	group 4	group 5	group 6	group 7
0	129	0	0	90	0	0	54
1	190	60	96	105	297	131	125
2	141	110	0	148	77	0	347
3	122	0	0	101	0	0	142
	group 1	group 2	group 3	group 4	group 5	group 6	group 7
1	582	170	96	0	0	0	0
2	0	0	0	444	374	131	0
3	0	0	0	0	0	0	668
	group 1	group 2	group 3	group 4	group 5	group 6	group 7
1	582	170	96	0	0	0	0
2	0	0	0	444	374	131	0
3	0	0	0	0	0	0	668
	1 2 3 1 2 3	0 129 1 190 2 141 3 122 group 1 1 582 2 0 3 0 group 1 1 582 2 0	0 129 0 1 190 60 2 141 110 3 122 0 group 1 group 2 1 582 170 2 0 0 3 0 0 group 1 group 2 1 582 170 2 1 582 170 2 0 0	0 129 0 0 0 1 190 60 96 2 141 110 0 3 122 0 0  group 1 group 2 group 3 1 582 170 96 2 0 0 0 0 3 0 0 0  group 1 group 2 group 3 1 582 170 96 2 1 582 170 96 2 0 0 0 0	0 129 0 0 90 1 190 60 96 105 2 141 110 0 148 3 122 0 0 101  group 1 group 2 group 3 group 4 1 582 170 96 0 2 0 0 0 444 3 0 0 0 0 0  group 1 group 2 group 3 group 4 1 582 170 96 0 2 0 0 0 444 1 582 170 96 0 2 0 0 0 444	0 129 0 0 90 0 1 190 60 96 105 297 2 141 110 0 148 77 3 122 0 0 101 0 group 1 group 2 group 3 group 4 group 5 1 582 170 96 0 0 2 0 0 0 444 374 3 0 0 0 0 444 374 3 1 582 170 96 0 0 group 1 group 2 group 3 group 4 group 5 1 582 170 96 0 0 2 0 0 0 444 374	1 190 60 96 105 297 131 2 141 110 0 148 77 0 3 122 0 0 101 0 0  group 1 group 2 group 3 group 4 group 5 group 6 1 582 170 96 0 0 0 2 0 0 0 444 374 131 3 0 0 0 0 0 0 0 0  group 1 group 2 group 3 group 4 group 5 group 6 1 582 170 96 0 0 0 2 0 0 0 444 374 131

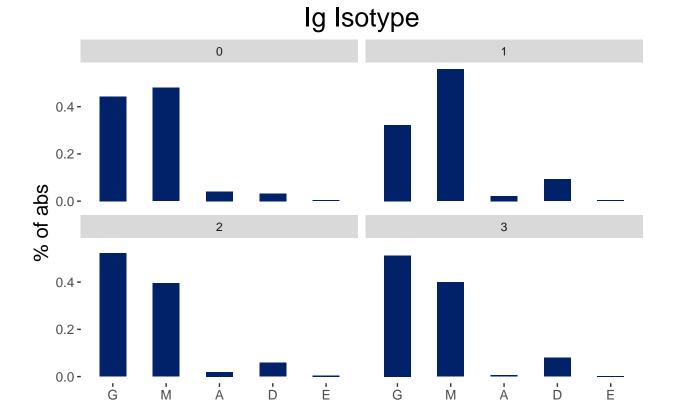
Each marcaque only received one kind of treatment.

##								
##		group 1	group 2	group 3	group 4	group 5	group 6	group 7
##	6104	0	0	35	0	0	0	0
##	6105	0	0	0	228	0	0	0
##	6107	0	0	0	0	0	0	239
##	6117	243	0	0	0	0	0	0
##	6118	0	7	0	0	0	0	0
##	6119	0	0	55	0	0	0	0
##	6125	0	0	0	216	0	0	0
##	6132	0	0	0	0	251	0	0
##	6160	183	0	0	0	0	0	0
##	6193	0	117	0	0	0	0	0
##	6199	0	0	0	0	0	48	0
##	6200	0	0	0	0	0	0	191
##	6201	0	0	0	0	73	0	0
##	6202	0	0	0	0	0	78	0
##	6203	0	0	0	0	0	0	238
##	6204	156	0	0	0	0	0	0

##	6205	0	0	0	0	0	5	0
##	6209	0	46	0	0	0	0	0
##	6210	0	0	0	0	50	0	0
##	6214	0	0	6	0	0	0	0

Next, we'll take a look at the variable Isotype. There are 5 kinds of heavy chain for antibodies: IgG, IgA, IgM, IgE, IgD. The two most important kinds are IgG and IgM. IgM mostly occurs in the acute stage of infection, and IgM appears later in blood with better neutralizing potentials.





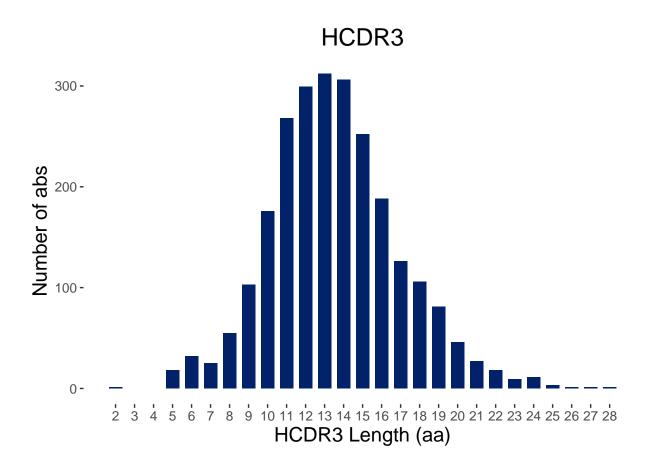
```
##
     Isotype Ab # Ab %
## 1
            Α
                51
                     2.1
## 2
            D
               179
                    7.3
## 3
            Ε
                10
                    0.4
            G 1062 43.1
## 4
## 5
            M 1163 47.2
```

As expected, we see that IgG and IgM occupy the biggest proportion of all antibodies in all time points. We'll use the variable Isotype as a grouping covariate later.

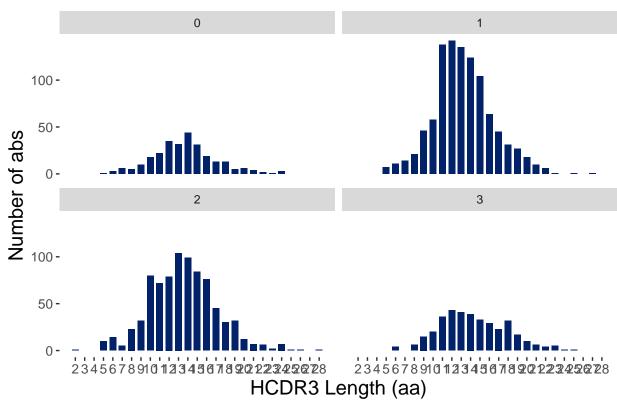
Ig Isotype

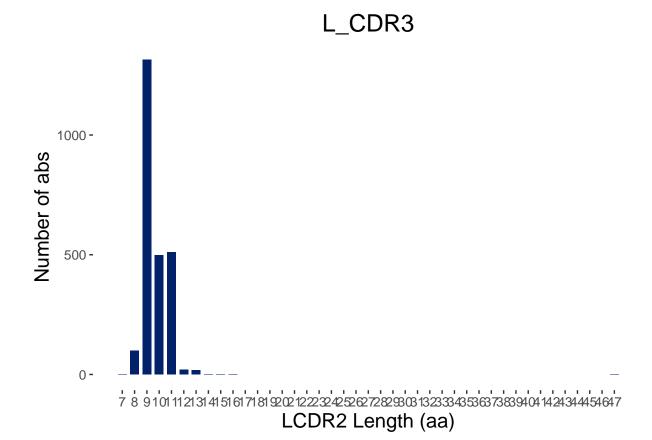
Next we'll examine our responses: H\_CDR3, HMuFreq, L\_CDR3, LMuFreq, Binding, and Reactivity. In each antibody, there are two sets of heavy chain and light chain, all of which forming a Y-shape immunoglobulin. Thus many of the variables start with H or L, indicating which chain the information comes from.

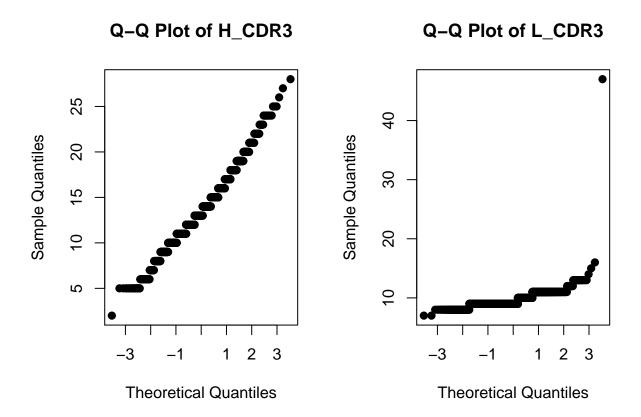
H\_CDR3 and L\_CDR3 indicates the length of the third complementarity-determining region on the variable heavy chain and light chain. The longer they are, the more potential there is to produce diverse antibodies. [Kan, could you check to see if this is correct?] In other words, we want the values to be higher. Below we see that the distributions are roughly normal with the center around 13 for H\_CDR3, with all data points, and slightly centers for different time points. For the Q-Q plot for L\_CDR3, we can see that there is one outlier. Without it, the distribution is likely normal. (We'll get to this soon.)



# HCDR3

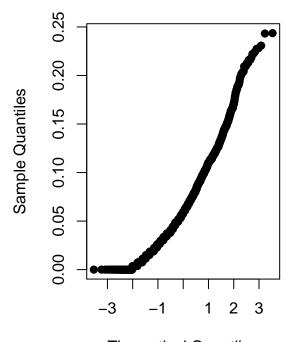




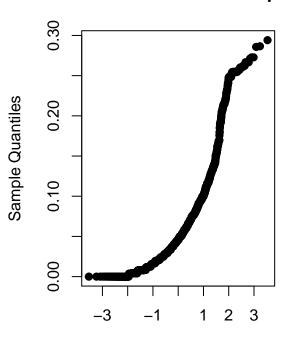


HMuFreq and LMuFreq are calculated by dividing H\_Substitution by H\_VBase for heavy chain and similarly for light chain. These two variables show how much the antibodies mutate. For the purpose of the study, the higher the mutation rate is, the better. Below we see some comparison of mutation rate between heavy chain and light chain. (Kappa and Lambda are two kinds of light chain.) [Kan, is there a reason to split up light chain into Kappa and Lambda? Could we simply plot heavy chain vs. light chain?]

## Q-Q Plot of HMuFreq



## Q-Q Plot of LMuFreq



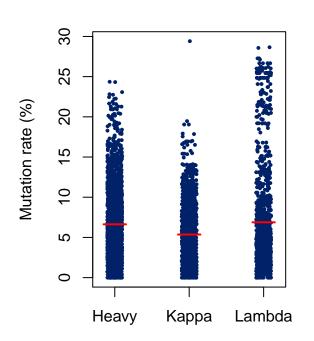
Theoretical Quantiles

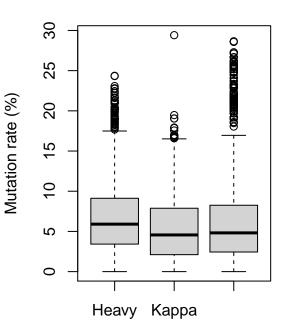
Theoretical Quantiles

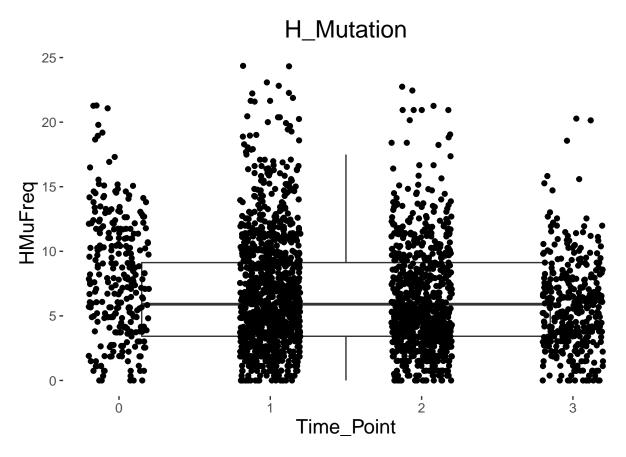
##		H_Mutation%	$K\_Mutation\%$	L_Mutation%
##	Min.	0.00	0.00	0.00
##	1st Qu.	3.42	2.11	2.44
##	Median	5.90	4.56	4.82
##	Mean	6.63	5.36	6.88
##	3rd Qu.	9.13	7.88	8.25
##	Max.	24.36	29.41	28.65



## H/K/L mutation rate

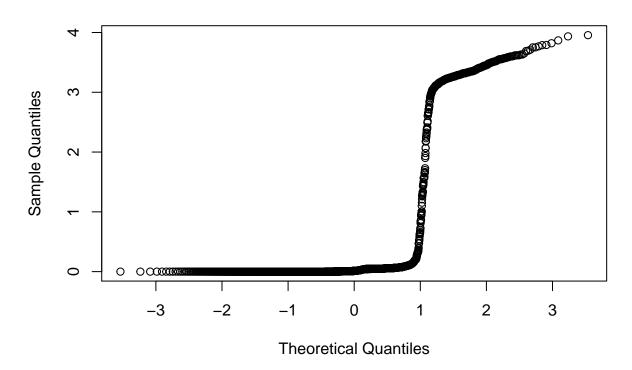






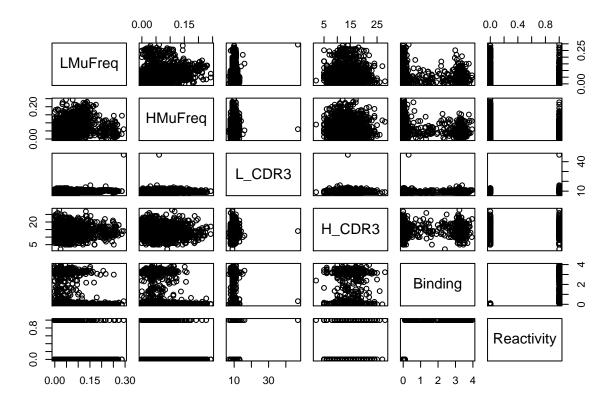
Lastly, Binding indicates the rate of neutralizing, meaning how much the antibodies bind with the virus and thus make the virus ineffective. This is the most important measure of the study. Reactivity turns Binding into a binary variable; Binding rate above 0.1 is considered reactive. In the Q-Q plot of Binding, we can see that it is not normally distributed. Thus the Reactivity measure might be a better response to use. However, since our sample size is larger than 2000, we can use the Central Limit Theorem and assume normality.

## Normal Q-Q Plot

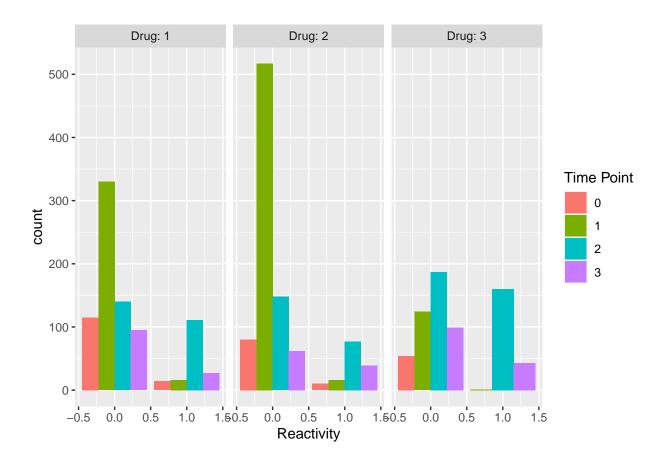


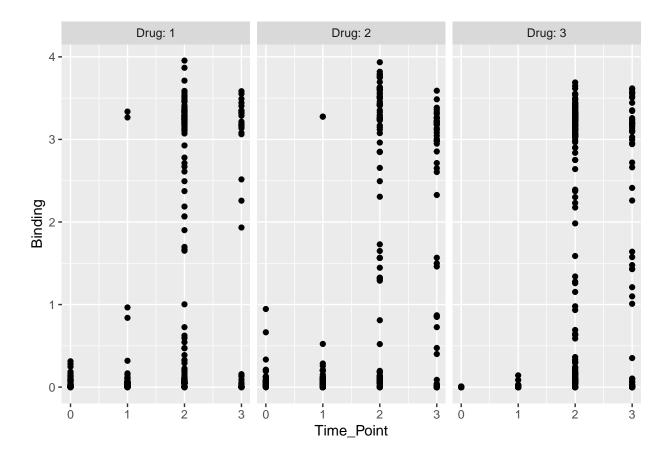
## 0 1 ## 1951 514

Let's take a look at these response variables and check whether they might be correlated.



Now we use some plots to see whether the response variables might be different for different time points, treatment groups or drugs, and grouping covariate (Isotype).

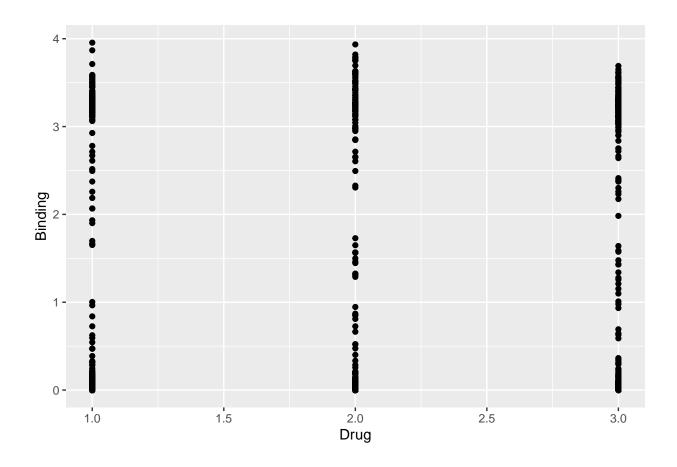


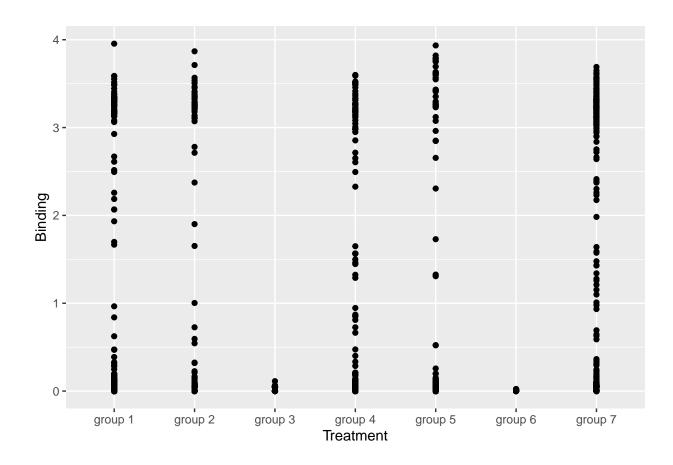


```
##
##
          0
              1
     1 680 168
##
##
     2 807 142
     3 464 204
##
##
##
          0
              1
##
     0 249
             24
##
     1 971
             33
     2 475 348
##
##
     3 256 109
```

Binding or Reactivity do seem to be affected by various predictors. Different drugs appear to have different boxplots in terms of the Binding variable.

```
## # A tibble: 3 x 6
      {\tt Drug\ avgLMuFreq\ avgHMuFreq\ avgBinding\ varBinding\ avgReact}
##
##
     <dbl>
                  <dbl>
                              <dbl>
                                          <dbl>
                                                      <dbl>
                                                                <dbl>
                0.0616
                                          0.450
                                                      1.14
                                                                0.198
## 1
                           NA
## 2
          2
                0.0616
                             0.0730
                                          0.334
                                                      0.864
                                                                0.150
## 3
          3
                0.0594
                             0.0559
                                          0.807
                                                      1.81
                                                                0.305
```

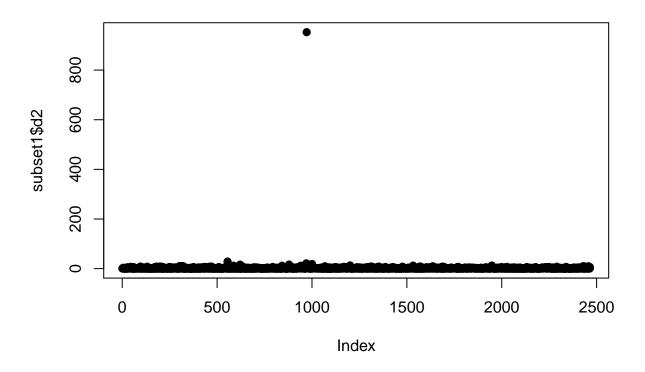


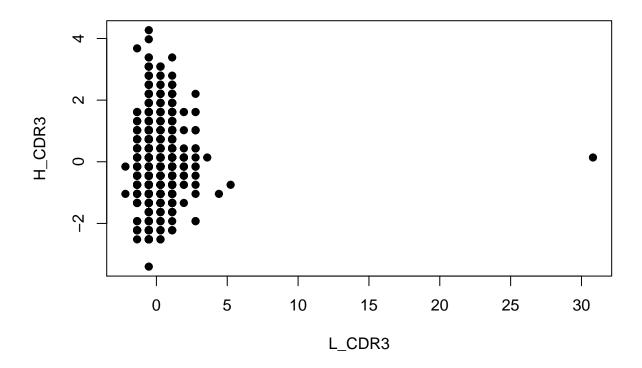


### Outlier detection

Before we go into analyses, notice may have outlier in LCDR3 variable.

## Min. 1st Qu. Median Mean 3rd Qu. Max. ## 7.00 9.00 9.00 9.65 10.00 47.00





```
# A tibble: 1 x 4
                        d2 Z[,"L_CDR3"] [,"H_CDR3"]
##
     L_CDR3 H_CDR3
                                                       [,"d2"]
      <dbl>
##
              <dbl> <dbl>
                                   <dbl>
                                                <dbl>
                                                         <dbl>
                                    30.8
                                                          49.4
## 1
         47
                 14
                     953.
                                                0.139
## [1] 972
```

Row 972 from Data2 is in fact an outlier, as shown in the summary and plots above. The value for L\_CDR3 is quite unlikely. Since we can't go back to the original data, we remove the data point and will use the new dataset Data3.

```
## # A tibble: 1 x 19
##
     MonkeyID Drug Treatment Time_Point Isotype H_VBase H_Substitutions
##
        <dbl> <dbl> <chr>
                                    <dbl> <chr>
                                                    <dbl>
                                                                     <dbl>
## 1
         6107
                  3 group 7
                                        2 G
                                                      263
                                                                        16
    ... with 12 more variables: H_Insertions <dbl>, H_Deletions <dbl>,
       HMuFreq <dbl>, H_CDR3 <dbl>, L_VBase <dbl>, L_Substitutions <dbl>,
## #
       L_Insertions <dbl>, L_Deletions <dbl>, LMuFreq <dbl>, L_CDR3 <dbl>,
       Binding <dbl>, Reactivity <dbl>
```

### Multivariate Data Analysis

Now we want to test whether predictors Drug and Isotype have effects on the five responses: H\_CDR3, HMuFreq, L\_CDR3, LMuFreq, and Binding. We choose Binding here, because all the variables are continuous. We will use Reactivity separately when we use logistic regression. Although Time\_Point is also one of the predictors, we will use it for longitudinal analysis in the next section.

First, we use manova to test effects. Since we have a large same size (n = 2464), we can assume normality.

In the output, we can see that the main effects of Drug and Isotype and the interaction effects are all significant.

```
Pillai approx F num Df den Df
                                                     Pr(>F)
## drug
                2 0.058434
                             14.711
                                        10
                                             4888 < 2.2e-16 ***
## it
                4 0.300048
                             39.672
                                        20
                                             9784 < 2.2e-16 ***
                7 0.069958
                              4.960
## drug:it
                                        35 12235 < 2.2e-16 ***
## Residuals 2447
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
We next use multiple linear regression.
## Response Data3$L CDR3 :
##
## Call:
## lm(formula = `Data3$L_CDR3` ~ drug * it)
## Residuals:
       Min
                10 Median
                                30
                                       Max
## -2.5872 -0.6634 -0.5696 0.4304
                                   6.3000
##
## Coefficients: (1 not defined because of singularities)
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 9.583333
                           0.193972 49.406
                                              <2e-16 ***
               -0.011905
                           0.283946 -0.042
                                              0.9666
## drug2
## drug3
                0.750000
                           0.433735
                                     1.729
                                              0.0839 .
## itD
                0.100877
                           0.231230
                                      0.436
                                              0.6627
## itE
                0.416667
                           0.408198
                                      1.021
                                              0.3075
## itG
                                      0.582
                                              0.5607
               0.116667
                           0.200512
## itM
               0.080057
                           0.199609
                                      0.401
                                              0.6884
## drug2:itD
                                    -0.543
               -0.178972
                           0.329405
                                              0.5870
## drug3:itD
               -0.944849
                           0.472420
                                     -2.000
                                              0.0456 *
## drug2:itE
               -1.321429
                                    -1.849
                                              0.0645
                           0.714582
## drug3:itE
                      NA
                                 NA
                                         NA
                                                  NA
## drug2:itG
                                              0.9925
               -0.002729
                           0.292246
                                     -0.009
## drug3:itG
               -0.862752
                           0.440155
                                     -1.960
                                              0.0501 .
## drug2:itM
               -0.028759
                           0.291370
                                    -0.099
                                              0.9214
## drug3:itM
               -0.843770
                           0.439548 - 1.920
                                              0.0550 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9503 on 2447 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.006476,
                                    Adjusted R-squared: 0.001198
## F-statistic: 1.227 on 13 and 2447 DF, p-value: 0.2527
##
##
## Response Data3$LMuFreq :
## Call:
## lm(formula = `Data3$LMuFreq` ~ drug * it)
##
## Residuals:
##
        Min
                  1Q
                                    3Q
                       Median
                                            Max
```

```
## -0.06859 -0.03658 -0.01446 0.02018 0.22777
##
## Coefficients: (1 not defined because of singularities)
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.0393431 0.0110147
                                   3.572 0.000361 ***
## drug2
              0.0009367 0.0161238
                                  0.058 0.953677
## drug3
             -0.0069529 0.0246295 -0.282 0.777738
## itD
              0.0164648 0.0131304
                                   1.254 0.209981
## itE
              0.0058906 0.0231795
                                   0.254 0.799418
## itG
              0.0251809 0.0113861
                                  2.212 0.027089 *
## itM
              0.0216787 0.0113348
                                  1.913 0.055918 .
## drug2:itD
              ## drug3:itD
              0.0007513 0.0405774 0.019 0.985229
## drug2:itE
## drug3:itE
                     NA
                               NA
                                      NA
## drug2:itG
              0.0017932 0.0165951
                                    0.108 0.913962
## drug3:itG
             -0.0043914 0.0249941
                                  -0.176 0.860545
## drug2:itM
             ## drug3:itM
              0.0096142 0.0249596 0.385 0.700130
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.05396 on 2447 degrees of freedom
    (3 observations deleted due to missingness)
## Multiple R-squared: 0.01073,
                                 Adjusted R-squared: 0.005478
## F-statistic: 2.042 on 13 and 2447 DF, p-value: 0.0147
##
## Response Data3$H_CDR3 :
##
## Call:
## lm(formula = `Data3$H_CDR3` ~ drug * it)
##
## Residuals:
              1Q Median
                             3Q
## -9.5829 -2.0000 -0.0933 2.0023 13.7416
## Coefficients: (1 not defined because of singularities)
             Estimate Std. Error t value Pr(>|t|)
                         0.6790 21.783
## (Intercept) 14.7917
                                         <2e-16 ***
## drug2
              -2.2679
                          0.9940 -2.282
                                         0.0226 *
## drug3
              -3.2917
                          1.5184 -2.168
                                         0.0303 *
                         0.8095 -1.455
## itD
              -1.1776
                                         0.1458
## itE
               2.2083
                         1.4290
                                 1.545
                                         0.1224
## itG
                         0.7019 -0.297
              -0.2088
                                         0.7661
                         0.6988 -2.381
## itM
              -1.6639
                                         0.0173 *
## drug2:itD
               1.7472
                         1.1531
                                  1.515
                                         0.1299
## drug3:itD
               2.4436
                         1.6538
                                 1.478
                                         0.1397
## drug2:itE
              -2.0655
                          2.5015
                                 -0.826
                                         0.4091
## drug3:itE
                   NA
                             NA
                                    NA
                                             NA
                                 1.478
## drug2:itG
                         1.0231
                                         0.1396
               1.5118
## drug3:itG
               2.9672
                         1.5408
                                 1.926
                                         0.0543 .
## drug2:itM
               2.1378
                         1.0200
                                  2.096
                                         0.0362 *
## drug3:itM
               2.8823
                         1.5387
                                  1.873
                                         0.0612 .
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.327 on 2447 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.04222,
                                   Adjusted R-squared: 0.03713
## F-statistic: 8.298 on 13 and 2447 DF, p-value: < 2.2e-16
##
##
## Response Data3$HMuFreq :
## lm(formula = `Data3$HMuFreq` ~ drug * it)
##
## Residuals:
##
         Min
                    1Q
                          Median
                                        3Q
                                                 Max
## -0.091172 -0.028366 -0.006062 0.024649 0.185109
## Coefficients: (1 not defined because of singularities)
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.063852
                          0.008280
                                    7.712 1.79e-14 ***
## drug2
              -0.010070
                          0.012121 -0.831
                                              0.4062
## drug3
                                     0.852
                                              0.3946
               0.015765
                          0.018514
## itD
                          0.009870 -0.426
                                              0.6704
              -0.004201
## itE
              -0.021395
                          0.017424 - 1.228
                                              0.2196
## itG
               0.015267
                          0.008559
                                    1.784
                                              0.0746
## itM
              -0.005718
                          0.008521 -0.671
                                              0.5022
                                    0.572
## drug2:itD
               0.008037
                          0.014061
                                              0.5677
## drug3:itD
              -0.025158
                          0.020166 -1.248
                                              0.2123
## drug2:itE
               0.045493
                           0.030503
                                    1.491
                                              0.1360
## drug3:itE
                      NA
                                         NA
                                                  NA
## drug2:itG
               0.022123
                           0.012475
                                     1.773
                                              0.0763
## drug3:itG
              -0.036875
                           0.018788
                                    -1.963
                                              0.0498 *
## drug2:itM
               0.011428
                           0.012437
                                     0.919
                                              0.3583
## drug3:itM
              -0.019511
                           0.018763 -1.040
                                              0.2985
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.04056 on 2447 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.1012, Adjusted R-squared: 0.09639
## F-statistic: 21.18 on 13 and 2447 DF, p-value: < 2.2e-16
##
## Response Data3$Binding :
##
## Call:
## lm(formula = `Data3$Binding` ~ drug * it)
##
## Residuals:
                1Q Median
                                3Q
      Min
                                       Max
## -1.7208 -0.6290 -0.0707 -0.0147
                                   3.5273
## Coefficients: (1 not defined because of singularities)
```

```
Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            0.1989
                 0.5331
                                      2.681
                                              0.0074 **
                                    -1.663
## drug2
                -0.4841
                            0.2911
                                              0.0965
## drug3
                 0.4137
                            0.4447
                                     0.930
                                              0.3523
## itD
                -0.4404
                            0.2371
                                    -1.858
                                              0.0633
## itE
                -0.4693
                            0.4185
                                    -1.121
                                              0.2623
## itG
                 0.3817
                            0.2056
                                     1.857
                                              0.0634 .
## itM
                -0.4274
                            0.2047
                                    -2.089
                                              0.0369 *
## drug2:itD
                 0.4918
                            0.3377
                                      1.456
                                              0.1455
## drug3:itD
                -0.4800
                            0.4844
                                    -0.991
                                              0.3218
## drug2:itE
                 0.8512
                            0.7326
                                     1.162
                                              0.2454
## drug3:itE
                     NA
                                NA
                                         NA
                                                  NA
## drug2:itG
                 0.2412
                            0.2996
                                      0.805
                                              0.4210
                                      0.869
                                              0.3849
## drug3:itG
                 0.3922
                            0.4513
## drug2:itM
                 0.4501
                            0.2987
                                      1.507
                                              0.1320
## drug3:itM
                -0.4600
                            0.4507 -1.021
                                              0.3075
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.9743 on 2447 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.2467, Adjusted R-squared: 0.2427
## F-statistic: 61.64 on 13 and 2447 DF, p-value: < 2.2e-16
Finally, we use logistic regression.
##
## Call:
## lm(formula = Data3$Reactivity ~ drug * it)
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -0.60403 -0.25854 -0.06818 -0.05380
                                        0.95238
##
## Coefficients: (1 not defined because of singularities)
               Estimate Std. Error t value Pr(>|t|)
                           0.07463
                                      2.792 0.00529 **
## (Intercept) 0.20833
## drug2
               -0.16071
                           0.10925
                                    -1.471 0.14140
## drug3
                0.12500
                                      0.749 0.45390
                           0.16688
## itD
                           0.08897
                                    -1.356 0.17531
               -0.12061
## itE
                                    -0.417 0.67679
               -0.06548
                           0.15705
## itG
               0.12594
                           0.07713
                                     1.633 0.10261
               -0.11251
                           0.07680
                                    -1.465 0.14306
## itM
## drug2:itD
                0.12633
                           0.12674
                                     0.997 0.31898
## drug3:itD
               -0.12761
                                    -0.702 0.48270
                           0.18176
## drug2:itE
                0.35119
                           0.27494
                                      1.277 0.20160
## drug3:itE
                     ΝA
                                NA
                                        NA
                                                  NA
## drug2:itG
                0.08497
                           0.11243
                                      0.756
                                            0.44984
## drug3:itG
                0.14475
                           0.16934
                                      0.855
                                            0.39276
## drug2:itM
                0.13307
                           0.11210
                                      1.187
                                             0.23533
## drug3:itM
               -0.16703
                           0.16912
                                    -0.988 0.32343
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3656 on 2450 degrees of freedom
```

```
## Multiple R-squared: 0.1937, Adjusted R-squared: 0.1894
## F-statistic: 45.28 on 13 and 2450 DF, p-value: < 2.2e-16</pre>
```

#### Pairwise comparison

To know more details about which groups have different means, we use pairwise comparisons for each treatment group, drug, and Isotype. (We set  $\alpha$  as 0.05, and it is adjusted based on the number of pairs and variables being compared.)

```
[1] "L_CDR3 pairwise CI's"
##
   contrast
                      estimate
                                   SE
                                         df lower.CL upper.CL
##
    group 1 - group 2 0.08842 0.0829 2454
                                             -0.2016
                                                        0.378
##
   group 1 - group 3 -0.03487 0.1047 2454
                                             -0.4012
                                                        0.331
    group 1 - group 4 0.11097 0.0599 2454
##
                                             -0.0987
                                                        0.321
##
   group 1 - group 5 -0.01158 0.0630 2454
                                             -0.2321
                                                        0.209
   group 1 - group 6 0.08361 0.0919 2454
                                             -0.2380
                                                        0.405
   group 1 - group 7 0.11559 0.0540 2454
##
                                             -0.0732
                                                        0.304
    group 2 - group 3 -0.12328 0.1213 2454
##
                                             -0.5477
                                                        0.301
##
   group 2 - group 4 0.02255 0.0857 2454
                                             -0.2773
                                                        0.322
##
   group 2 - group 5 -0.10000 0.0879 2454
                                             -0.4075
                                                        0.208
##
   group 2 - group 6 -0.00480 0.1105 2454
                                             -0.3913
                                                        0.382
##
   group 2 - group 7 0.02717 0.0816 2454
                                             -0.2584
                                                        0.313
   group 3 - group 4 0.14583 0.1070 2454
##
                                             -0.2283
                                                        0.520
##
   group 3 - group 5 0.02328 0.1087 2454
                                             -0.3571
                                                        0.404
##
   group 3 - group 6 0.11848 0.1277 2454
                                             -0.3282
                                                        0.565
   group 3 - group 7 0.15046 0.1037 2454
##
                                             -0.2124
                                                        0.513
##
    group 4 - group 5 -0.12255 0.0667 2454
                                             -0.3559
                                                        0.111
   group 4 - group 6 -0.02735 0.0945 2454
##
                                             -0.3579
                                                        0.303
##
    group 4 - group 7
                       0.00462 0.0582 2454
                                             -0.1990
                                                        0.208
##
                                             -0.2423
   group 5 - group 6 0.09520 0.0965 2454
                                                        0.433
   group 5 - group 7 0.12717 0.0614 2454
                                             -0.0876
                                                        0.342
##
   group 6 - group 7 0.03198 0.0908 2454
                                                        0.350
                                             -0.2857
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
##
  [1] "LMuFreq pairwise CI's"
##
   contrast
                                           df lower.CL upper.CL
                       estimate
                                      SE
   group 1 - group 2 0.007328 0.00472 2454 -0.00918
                                                        0.02384
##
   group 1 - group 3 -0.006001 0.00596 2454 -0.02686
                                                        0.01486
##
   group 1 - group 4 0.002551 0.00341 2454 -0.00939
                                                        0.01449
##
    group 1 - group 5 -0.000993 0.00359 2454 -0.01355
                                                        0.01156
##
   group 1 - group 6 -0.001342 0.00523 2454 -0.01966
                                                        0.01697
    group 1 - group 7 0.003112 0.00307 2454 -0.00764
##
                                                        0.01386
##
   group 2 - group 3 -0.013330 0.00691 2454 -0.03750
                                                        0.01084
##
   group 2 - group 4 -0.004778 0.00488 2454 -0.02185
                                                        0.01230
##
   group 2 - group 5 -0.008322 0.00500 2454 -0.02583
                                                        0.00919
    group 2 - group 6 -0.008670 0.00629 2454 -0.03068
##
                                                        0.01334
##
   group 2 - group 7 -0.004216 0.00465 2454 -0.02048
                                                        0.01205
   group 3 - group 4 0.008552 0.00609 2454 -0.01275
                                                        0.02986
##
   group 3 - group 5 0.005008 0.00619 2454 -0.01665
                                                        0.02667
##
   group 3 - group 6 0.004659 0.00727 2454 -0.02077
                                                        0.03009
##
   group 3 - group 7 0.009114 0.00591 2454 -0.01155
                                                        0.02978
   group 4 - group 5 -0.003544 0.00380 2454 -0.01683
                                                        0.00974
   group 4 - group 6 -0.003893 0.00538 2454 -0.02271
```

```
group 4 - group 7 0.000562 0.00331 2454 -0.01103 0.01216
   group 5 - group 6 -0.000349 0.00549 2454 -0.01957
                                                      0.01887
   group 5 - group 7 0.004106 0.00350 2454 -0.00812 0.01633
   group 6 - group 7 0.004454 0.00517 2454 -0.01364 0.02254
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
## [1] "H_CDR3 pairwise CI's"
##
   contrast
                      estimate
                                  SE
                                       df lower.CL upper.CL
   group 1 - group 2
                        0.5757 0.295 2454 -0.45488
                                                      1.606
                                                      2.230
##
   group 1 - group 3
                        0.9285 0.372 2454 -0.37339
##
   group 1 - group 4
                        0.9693 0.213 2454 0.22406
                                                      1.715
                                                      1.177
##
   group 1 - group 5
                        0.3928 0.224 2454 -0.39095
                        0.7509 0.327 2454 -0.39208
##
   group 1 - group 6
                                                      1.894
##
    group 1 - group 7
                        0.6651 0.192 2454 -0.00594
                                                      1.336
##
                        0.3528 0.431 2454 -1.15543
                                                      1.861
   group 2 - group 3
                        0.3936 0.305 2454 -0.67188
                                                      1.459
   group 2 - group 4
   group 2 - group 5
                      -0.1829 0.312 2454 -1.27567
                                                      0.910
   group 2 - group 6
                        0.1753 0.393 2454 -1.19820
                                                      1.549
##
   group 2 - group 7
                        0.0894 0.290 2454 -0.92557
                                                      1.104
   group 3 - group 4
                        0.0408 0.380 2454 -1.28891
                                                      1.371
##
   group 3 - group 5 -0.5357 0.386 2454 -1.88738
                                                      0.816
##
   group 3 - group 6 -0.1776 0.454 2454 -1.76477
                                                      1.410
   group 3 - group 7 -0.2634 0.369 2454 -1.55299
##
                                                      1.026
   group 4 - group 5 -0.5765 0.237 2454 -1.40570
                                                      0.253
   group 4 - group 6 -0.2184 0.336 2454 -1.39301
                                                      0.956
##
##
   group 4 - group 7
                      -0.3042 0.207 2454 -1.02780
                                                      0.419
   group 5 - group 6
                      0.3581 0.343 2454 -0.84126
                                                      1.558
   group 5 - group 7
                        0.2723 0.218 2454 -0.49084
                                                      1.035
##
    group 6 - group 7 -0.0858 0.323 2454 -1.21483
                                                      1.043
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
  Confidence level used: 0.999523809523809
  [1] "HMuFreq pairwise CI's"
##
   contrast
                       estimate
                                     SE
                                          df lower.CL
                                                      upper.CL
##
   group 1 - group 2 0.001782 0.00367 2454 -0.01105
                                                       0.014613
   group 1 - group 3 0.014768 0.00463 2454 -0.00144
                                                       0.030977
##
   group 1 - group 4 -0.000904 0.00265 2454 -0.01018
                                                       0.008375
   group 1 - group 5 -0.005563 0.00279 2454 -0.01532
   group 1 - group 6 -0.009779 0.00407 2454 -0.02401
##
                                                       0.004452
##
   group 1 - group 7 0.013055 0.00239 2454 0.00470
                                                       0.021410
##
   group 2 - group 3 0.012986 0.00537 2454 -0.00579
                                                       0.031765
   group 2 - group 4 -0.002686 0.00379 2454 -0.01595
                                                       0.010580
   group 2 - group 5 -0.007345 0.00389 2454 -0.02095
##
                                                       0.006261
                                                       0.005539
##
   group 2 - group 6 -0.011561 0.00489 2454 -0.02866
   group 2 - group 7 0.011273 0.00361 2454 -0.00136
                                                       0.023910
   group 3 - group 4 -0.015672 0.00473 2454 -0.03223
                                                      0.000884
    group 3 - group 5 -0.020331 0.00481 2454 -0.03716 -0.003502
##
   group 3 - group 6 -0.024547 0.00565 2454 -0.04431 -0.004785
   group 3 - group 7 -0.001713 0.00459 2454 -0.01777 0.014343
   group 4 - group 5 -0.004659 0.00295 2454 -0.01498 0.005665
   group 4 - group 6 -0.008875 0.00418 2454 -0.02350 0.005750
```

```
group 4 - group 7 0.013959 0.00258 2454 0.00495 0.022968
   group 5 - group 6 -0.004216 0.00427 2454 -0.01915 0.010717
   group 5 - group 7 0.018618 0.00272 2454 0.00912 0.028120
## group 6 - group 7 0.022834 0.00402 2454 0.00878 0.036891
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
## [1] "Binding pairwise CI's"
   contrast
                     estimate
                                  SE
                                       df lower.CL upper.CL
   group 1 - group 2 -0.5394 0.0951 2454
                                           -0.8721 -0.2066
                      0.3560 0.1202 2454
                                           -0.0644
                                                     0.7763
   group 1 - group 3
   group 1 - group 4 -0.0201 0.0688 2454
                                           -0.2608
                                                     0.2205
##
                     0.0164 0.0723 2454
   group 1 - group 5
                                           -0.2366
                                                     0.2695
   group 1 - group 6
                       0.3819 0.1055 2454
                                           0.0129
                                                     0.7510
   group 1 - group 7 -0.4236 0.0619 2454
##
                                           -0.6403 -0.2070
##
                                            0.4083
   group 2 - group 3
                       0.8953 0.1392 2454
                                                     1.3823
   group 2 - group 4
                       0.5192 0.0983 2454
                                            0.1752
                                                     0.8633
                       0.5558 0.1009 2454
   group 2 - group 5
                                            0.2029
                                                     0.9086
   group 2 - group 6
                       0.9213 0.1268 2454
                                            0.4778
                                                     1.3648
##
   group 2 - group 7
                       0.1157 0.0937 2454
                                          -0.2120
                                                    0.4434
  group 3 - group 4 -0.3761 0.1227 2454
                                           -0.8055
                                                     0.0532
##
   group 3 - group 5 -0.3395 0.1248 2454
                                           -0.7760
                                                     0.0969
                       0.0259 0.1465 2454
                                           -0.4866
   group 3 - group 6
                                                     0.5384
   group 3 - group 7 -0.7796 0.1190 2454
                                          -1.1960 -0.3632
  group 4 - group 5
                       0.0366 0.0765 2454
                                           -0.2311
                                                     0.3043
##
   group 4 - group 6
                      0.4021 0.1084 2454
                                            0.0228
                                                     0.7813
   group 4 - group 7 -0.4035 0.0668 2454
                                           -0.6371 -0.1699
   group 5 - group 6 0.3655 0.1107 2454
                                          -0.0218
                                                     0.7528
   group 5 - group 7 -0.4401 0.0704 2454
                                           -0.6865 -0.1937
##
   group 6 - group 7 -0.8056 0.1042 2454 -1.1701 -0.4410
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999523809523809
## [1] "L_CDR3 pairwise CI's"
   contrast estimate
                         SE
                              df lower.CL upper.CL
## 1 - 2
              0.0451 0.0450 2458 -0.0870
                                             0.177
## 1 - 3
              0.1018 0.0492 2458
                                 -0.0429
                                             0.246
## 2 - 3
              0.0567 0.0480 2458 -0.0844
                                             0.198
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.99666666666667
## [1] "LMuFreq pairwise CI's"
  contrast estimate
                           SE
                                df lower.CL upper.CL
            -0.000176 0.00256 2458 -0.00770 0.00735
## 1 - 2
##
  1 - 3
             0.002320 0.00280 2458 -0.00592 0.01056
##
             0.002496 0.00273 2458 -0.00554 0.01053
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.996666666666667
```

```
## [1] "H_CDR3 pairwise CI's"
  contrast estimate
                        SE
                            df lower.CL upper.CL
## 1 - 2
              0.4907 0.160 2458
                                  0.0204
## 1 - 3
                                            0.959
              0.4438 0.175 2458 -0.0712
## 2 - 3
             -0.0469 0.171 2458 -0.5492
                                            0.456
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.9966666666666667
## [1] "HMuFreq pairwise CI's"
   contrast estimate
                          SE
                               df lower.CL upper.CL
## 1 - 2
              -0.006 0.00199 2458 -0.01186 -0.000145
               0.011 0.00218 2458 0.00461 0.017432
## 1 - 3
## 2 - 3
               0.017 0.00213 2458 0.01076 0.023276
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.996666666666667
## [1] "Binding pairwise CI's"
   contrast estimate
                         SE
                              df lower.CL upper.CL
## 1 - 2
              0.118 0.0522 2458 -0.0355
                                             0.271
## 1 - 3
              -0.356 0.0571 2458 -0.5235
                                            -0.188
## 2 - 3
              -0.473 0.0557 2458 -0.6372
                                            -0.310
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.996666666666667
## [1] "L_CDR3 pairwise CI's"
   contrast estimate
                         SE
                              df lower.CL upper.CL
  A - D
              0.1136 0.1510 2456
##
                                  -0.3838
                                             0.611
##
   A - E
              0.0667 0.3289 2456
                                  -1.0170
                                             1.150
##
   A - G
                                  -0.4451
              0.0041 0.1364 2456
                                             0.453
   A - M
                                  -0.4042
              0.0441 0.1361 2456
                                             0.492
## D - E
             -0.0469 0.3091 2456
                                  -1.0651
                                             0.971
## D - G
                                  -0.3627
             -0.1095 0.0769 2456
                                             0.144
## D - M
             -0.0695 0.0764 2456
                                 -0.3210
                                             0.182
  E - G
             -0.0626 0.3022 2456
                                  -1.0581
                                             0.933
## E - M
             -0.0225 0.3021 2456
                                             0.973
                                 -1.0177
##
              0.0400 0.0404 2456 -0.0931
                                             0.173
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
## [1] "LMuFreq pairwise CI's"
  contrast estimate
                           SE
                                df lower.CL upper.CL
##
   A - D
            -0.021206 0.00858 2456 -0.04947 0.00705
   A - E
##
            -0.006829 0.01869 2456 -0.06840
                                            0.05475
##
  A - G
            -0.023476 0.00775 2456 -0.04900
                                             0.00205
  A - M
##
            -0.021669 0.00773 2456 -0.04714
                                             0.00380
## D - E
             0.014376 0.01756 2456 -0.04348
                                             0.07223
## D - G
            -0.002270 0.00437 2456 -0.01666
                                             0.01212
  D - M
            -0.000463 0.00434 2456 -0.01476
## E - G
            -0.016647 0.01717 2456 -0.07321 0.03992
```

```
-0.014839 0.01716 2456 -0.07138 0.04170
## G - M
             0.001807 0.00230 2456 -0.00576 0.00937
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
## [1] "H_CDR3 pairwise CI's"
  contrast estimate
                        SE
                             df lower.CL upper.CL
   A - D
               0.297 0.530 2456
                                  -1.448
                                            2.043
## A - E
                                  -6.032
                                            1.574
              -2.229 1.154 2456
## A - G
              -0.728 0.479 2456
                                  -2.304
                                            0.849
## A - M
               0.503 0.478 2456
                                  -1.070
                                            2.076
## D - E
                                  -6.100
              -2.527 1.085 2456
                                            1.046
## D - G
                                           -0.137
              -1.025 0.270 2456
                                  -1.914
## D - M
               0.206 0.268 2456
                                  -0.677
                                            1.089
## E - G
               1.502 1.060 2456
                                  -1.992
                                            4.995
## E - M
               2.733 1.060 2456
                                  -0.760
                                            6.225
## G - M
               1.231 0.142 2456
                                   0.764
                                            1.698
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
## [1] "HMuFreq pairwise CI's"
   contrast estimate
                          SE
                               df lower.CL upper.CL
             0.00523 0.00659 2456 -0.0165 0.02693
## A - D
## A - E
             0.00848 0.01435 2456 -0.0388 0.05576
## A - G
            -0.01628 0.00595 2456 -0.0359 0.00332
## A - M
             0.00393 0.00594 2456 -0.0156 0.02349
## D - E
             0.00325 0.01349 2456 -0.0412 0.04768
                                   -0.0326 -0.01046
## D - G
            -0.02151 0.00335 2456
## D - M
            -0.00130 0.00333 2456
                                   -0.0123 0.00968
## E - G
            -0.02476 0.01319 2456
                                   -0.0682 0.01868
## E - M
            -0.00455 0.01318 2456
                                   -0.0480 0.03888
## G - M
             0.02021 0.00176 2456
                                    0.0144 0.02602
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
## [1] "Binding pairwise CI's"
## contrast estimate
                         SE
                              df lower.CL upper.CL
             0.30395 0.1610 2456
                                   -0.227
                                             0.834
## A - E
             0.20847 0.3508 2456
                                   -0.947
                                             1.364
## A - G
            -0.66527 0.1454 2456
                                   -1.144
                                            -0.186
## A - M
                                   -0.176
             0.30220 0.1451 2456
                                             0.780
## D - E
            -0.09548 0.3296 2456
                                   -1.181
                                             0.990
## D - G
            -0.96922 0.0820 2456
                                   -1.239
                                            -0.699
## D - M
            -0.00175 0.0814 2456
                                   -0.270
                                             0.267
##
  E - G
            -0.87374 0.3223 2456
                                   -1.936
                                             0.188
  E - M
             0.09373 0.3222 2456
                                   -0.968
                                             1.155
##
   G - M
             0.96747 0.0431 2456
                                    0.825
                                             1.109
##
## Results are averaged over the levels of: rep.meas
## Note: contrasts are still on the [.: scale
## Confidence level used: 0.999
```

Here are the pairs that have significant differences:

```
• Treatment
     - L CDR3: none
     - LMuFreq: none
     - H_CDR3:
          * group 1 > \text{group } 4
     - HMuFreq:
          * group 1 > \text{group } 7
          * group 3 < \text{group } 5
          * group 3 < group 6
          * group 5 > \text{group } 7
          * group 6 > \text{group } 7
     - Binding:
          * group 1 < \text{group } 2
          * group 1 > \text{group } 6
          * group 2 > \text{group } 3
          * group 2 > \text{group } 4
          * group 2 > \text{group } 5
          * group 2 > \text{group } 6
          * group 3 < \text{group } 7
          * group 4 > \text{group } 6
          * group 4 < \text{group } 7
          * group 5 < \text{group } 7
          * group 6 < \text{group } 7
• Drug
     - L_CDR3: none
     - LMuFreq: none
     - H_CDR3:
          *1 > 2
     - HMuFreq:
          * 1 < 2
          * 1 > 3
          * 2 > 3
     - Binding:
          * 1 < 3
          * 2 < 3
• Isotype
     - L_CDR3: none
     - LMuFreq: none
     - H CDR3:
          * \ \mathrm{IgD} < \mathrm{IgG}
     - HMuFreq:
          * IgD < IgG
          * IgG > IgM
     - Binding:
          * IgA < IgG
          * IgD < IgG
          * IgG > IgM
```

In short, L\_CDR3 and LMuFreq do not have significant paired differences.

For H\_CDR3, treatment group 1 (drug 1) is higher than treatment group 7 (control), and IgG has a longer H\_CDR3 length than IgD.

For HMuFreq, drug 2 has the highest mean, followed by drug 1 and control. More specifically, treatment

groups 5 and 6 (two doses in drug 2) have the highest mutation rates. IgG has higher mutation rate than IgD.

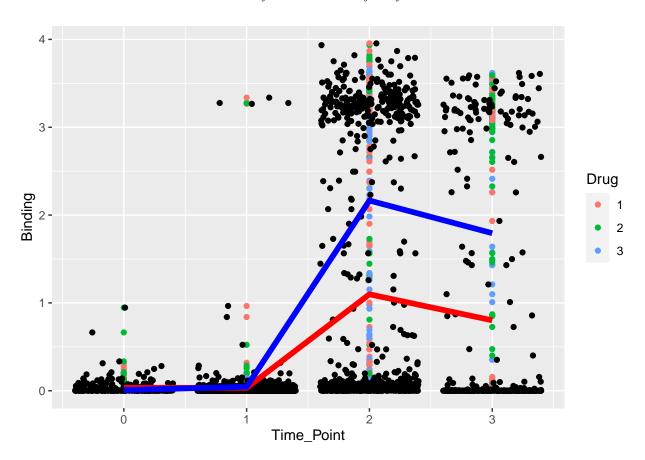
For Binding, drug 3 has the highest mean, but drug 1 and drug 2 do not have significant differences. IgG has higher binding rate than IgA, IgD, and IgM.

We could conclude that the drugs/treatment groups do increase mutation rate; however, they do not increase binding rate. That is to say, although the treatments do help increase the diversity of antibodies, they are not specific to the HIV antigens and thus do not increase binding.

### Longitudinal Data Analysis

First we don't consider treatments but only plot the mean trend over time. The plot shows that bindign does vary over time. The red line shows the mean trend over time, and the blue line shows the variance over time. The variance does not seem equal over time, so we will have to use unequal variance for the covariance structure.

$$Y_{ij} = \beta_0 + \beta_1 Time_{ij} + e_{ij}$$



Here we use Binding as the response, Time\_Point as the time factor, and Drug as the covariates. Random effect for both intercept and slope. Now we want to add one covariate: Drug. We use two indicator variables: D1 and D2, where

$$D1 = \begin{cases} 1 & \text{if Drug} = 1\\ 0 & \text{otherwise} \end{cases}$$

$$D2 = \begin{cases} 1 & \text{if Drug} = 2\\ 0 & \text{otherwise} \end{cases}$$

 $Y_{ij} = \beta_0 + \beta_1 Time_{ij} + D1_i(\beta_2 + \beta_3 Time_{ij}) + D2_i(\beta_4 + \beta_5 Time_{ij}) + b_{0i} + b_{1i} Time_{ij} + e_{ij}$ 

Assuming that the random effects are the same for each drug, our full model is:

```
Drug 1: Y_{ij} = \beta_0 + \beta_1 Time_{ij} + \beta_2 + \beta_3 Time_{ij} + b_{0i} + b_{1i} Time_{ij} + e_{ij}
Drug 2: Y_{ij} = \beta_0 + \beta_1 Time_{ij} + \beta_4 + \beta_5 Time_{ij} + b_{0i} + b_{1i} Time_{ij} + e_{ij}
Drug 3: Y_{ij} = \beta_0 + \beta_1 Time_{ij} + b_{0i} + b_{1i} Time_{ij} + e_{ij}
[need to list D and \Sigma]
## Linear mixed-effects model fit by REML
    Data: dataLDA
##
           AIC
                     BIC
                              logLik
##
     6743.422 6801.493 -3361.711
##
## Random effects:
    Formula: ~Time_Point | ID
##
    Structure: General positive-definite, Log-Cholesky parametrization
##
                 StdDev
                            Corr
## (Intercept) 0.6371528 (Intr)
## Time_Point
                 0.6428851 -0.976
## Residual
                 0.9329905
##
## Fixed effects: binding ~ Time_Point + D1 + D1:Time_Point + D2 + D2:Time_Point
##
                         Value Std.Error
                                             DF
                                                    t-value p-value
## (Intercept)
                   -0.3892858 0.3791678 2441 -1.0266848
                                                               0.3047
## Time_Point
                    0.6688464 0.3740370 2441
                                                  1.7881825
                                                               0.0739
## D1
                    0.0804698 0.5026261
                                              17
                                                  0.1600986
                                                               0.8747
## D2
                   -0.2777354 0.5044149
                                              17 -0.5506090
                                                               0.5891
## Time_Point:D1 -0.2012380 0.4958255 2441 -0.4058645
                                                               0.6849
## Time Point:D2
                    0.0816835 0.4987194 2441
                                                 0.1637866
    Correlation:
                   (Intr) Tm_Pnt D1
##
                                           D2
                                                   T_P:D1
## Time Point
                   -0.967
## D1
                   -0.754 0.730
                   -0.752 0.727 0.567
## Time_Point:D1 0.730 -0.754 -0.972 -0.549
  Time_Point:D2 0.725 -0.750 -0.547 -0.973
##
##
   Standardized Within-Group Residuals:
##
              Min
                                Q1
                                               Med
                                                                Q3
                                                                               Max
   -3.5180965300 -0.5157029350 -0.1075302008 -0.0007237661
##
## Number of Observations: 2464
## Number of Groups: 20
```

The p-values for Drug and the interaction of Drug and Time\_Point are large. So we try another model with Time\_Point as the only predictor.

$$Y_{ij} = \beta_0 + \beta_1 Time_{ij} + b_{0i} + b_{1i} Time_{ij} + e_{ij}$$

[need to list **D** and  $\Sigma$ ] [need to consider whether time point 2 is the optimal point]

```
## Linear mixed-effects model fit by REML
##
    Data: dataLDA
##
          AIC
                   BIC
                           logLik
##
     6733.537 6768.389 -3360.769
##
## Random effects:
    Formula: ~Time_Point | ID
##
##
    Structure: General positive-definite, Log-Cholesky parametrization
##
               StdDev
                         Corr
## (Intercept) 0.5926928 (Intr)
               0.5902261 -0.971
## Time_Point
## Residual
               0.9330387
##
## Fixed effects: binding ~ Time_Point
##
                    Value Std.Error
                                       DF
                                            t-value p-value
## (Intercept) -0.4805707 0.1856332 2443 -2.588819 0.0097
## Time Point
                0.6295635 0.1814510 2443 3.469606 0.0005
##
    Correlation:
##
              (Intr)
  Time_Point -0.973
##
##
## Standardized Within-Group Residuals:
##
                                                             Max
## -3.53555423 -0.50930841 -0.08770458 0.02706098 3.60996805
##
## Number of Observations: 2464
## Number of Groups: 20
```

This simpler model has lower AIC and BIC, as shown below. So we prefer the model with Time\_Point as the predictor and, with the low p-values of the slope of Time\_Point, conclude that the binding rates vary over time. In other words, the number of HIV vaccines given do affect the binding rate, but the drugs given do not have significant effects.

```
## df AIC df.1 BIC
## lda 10 6743.422 10 6801.493
## lda2 6 6733.537 6 6768.389
```

#### Discussion

### Conclusion

Although the study provides evidence to support the concept of using immunosuppressing treatments to increase diversity, the added diversity does not seem to improve the binding rate. In other words, this study does not provide evidence to show that the added treatments can enhance the effects of HIV vaccines.

#### List of variables

- Treatment: Treatment A is the mock control, and treatment B and C are two different kinds of Treg inhibitor treatments.
- Time Points: 0 represents before immunization; 1 represents 2 weeks post 1st immunization; 2 represents 2 weeks post 2nd immunization; and 3 represents 2 weeks post 3rd immunization, respectively.

- Isotype: the category of antibody type
- H\_ID and L\_ID: heavy chain and light chain IDs for the particular observation
- H\_V, H\_D and H\_J: the gene segments used in heavy chain VDJ recombination in that antibody. The same applies to L\_V and L\_J
- H VBase: the number of nucleotide of the heavy chain variable region
- H Substitutions, H Insertions, H Deletions: the number of relative nucleotide mutations.
- HMuFreq: calculated by H Substitutions / H VBase
- H CDR3: the number of amino acid of the heavy chain's third complementarity determining region
- Binding: affinity of antibodies against a selected HIV glycoprotein. The larger value indicates stronger binding

### Reference

The dataset, which can be found here, was provided by Kan Luo, as he was one of authors for the following four publications that used the dataset:

- 1. Luo K, Liao HX, Zhang R, et al. Tissue memory B cell repertoire analysis after ALVAC/AIDSVAX B/E gp120 immunization of rhesus macaques. *JCI Insight*. 2016;1(20):e88522. Published 2016 Dec 8. doi:10.1172/jci.insight.88522
- 2. Bradley, T., Kuraoka, M., Yeh, C.-H., Tian, M., Chen, H., Cain, D. W., . . . Haynes, B. F. (2020). Immune checkpoint modulation enhances HIV-1 antibody induction. *Nature Communications*, 11(1), 948. doi:10.1038/s41467-020-14670-w
- 3. Easterhoff, D., Pollara, J., Luo, K., Tolbert, W. D., Young, B., Mielke, D., . . . Ferrari, G. (2020). Boosting with AIDSVAX B/E Enhances Env Constant Region 1 and 2 Antibody-Dependent Cellular Cytotoxicity Breadth and Potency. *Journal of Virology*, 94(4), e01120-01119. doi:10.1128/jvi.01120-19
- 4. Wiehe, K., Easterhoff, D., Luo, K., Nicely, N. I., Bradley, T., Jaeger, F. H., Dennison, S. M., Zhang, R., Lloyd, K. E., Stolarchuk, C., Parks, R., Sutherland, L. L., Scearce, R. M., Morris, L., Kaewkungwal, J., Nitayaphan, S., Pitisuttithum, P., Rerks-Ngarm, S., Sinangil, F., Phogat, S., ... Haynes, B. F. (2014). Antibody light-chain-restricted recognition of the site of immune pressure in the RV144 HIV-1 vaccine trial is phylogenetically conserved. *Immunity*, 41(6), 909–918. https://doi.org/10.1016/j.immuni.2014.11.014