

# THE OPTIMAL DELAUNAY TRIANGULATION OF CHEESY SONGS

A thesis submitted to the Delft University of Technology in partial fulfillment  
of the requirements for the degree of

Master of Science in Geomatics

by

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May 2015

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## ABSTRACT

*[Should fit on one page.]*

Bacon ipsum dolour sit amet porchetta beef turkey, bacon turducken boudin hamburger venison ball tip. Brisket pork loin bresaola short loin ground round leberkas pastrami tongue jerky cow turducken beef ribs. Pork ribeye landjaeger prosciutto pig venison tenderloin. Swine beef ribs kielbasa, porchetta tenderloin salami venison pork belly tail. Bacon ipsum dolour sit amet porchetta beef turkey, bacon turducken boudin hamburger venison ball tip. Brisket pork loin bresaola short loin ground round leberkas pastrami tongue jerky cow turducken beef ribs. Pork ribeye landjaeger prosciutto pig venison tenderloin. Swine beef ribs kielbasa, porchetta tenderloin salami venison pork belly tail. Bacon ipsum dolour sit amet porchetta beef turkey, bacon turducken boudin hamburger venison ball tip. Brisket pork loin bresaola short loin ground round leberkas pastrami tongue jerky cow turducken beef ribs. Pork ribeye landjaeger prosciutto pig venison tenderloin. Swine beef ribs kielbasa, porchetta tenderloin salami venison pork belly tail.



## ACKNOWLEDGEMENTS

Thanks to everyone, especially to my supervisors and my mum. And obviously to the ones who made that great template.

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## ACRONYMS

DT	Delaunay triangulation.....	5
GIS	geographical information system.....	4
TIN	triangular irregular network.....	5





# 1 | INTRODUCTION

This is a complete template for the MSc Geomatics thesis. It contains all the parts that are required and is structured in such a way that most/all supervisors expect. Observe that the MSc Geomatics at TU Delft has no formal requirements (except the reflection part, which is put here as an Appendix, but it can also be submitted as a separate document), how the document looks like (fonts, margins, headers, etc) is entirely up to you. We basically took the template `arsclassica` (by Lorenzo Pantieri), which is an adaption of the original `classicthesis` package from André Miede, added the front/back matters (cover page, copyright, abstract, etc.), and gave examples for the insertion of figures, tables and algorithms.

*It is not an official template and it is not mandatory to use it.*

But we hope it will encourage everyone to use  $\text{\LaTeX}$  for writing their thesis, and we also hope that it will *discourage* some from using Word.

If you run into mistakes/problems/issues, please report them on the GitHub page, and if you fix an error, then please submit a pull request.

<https://github.com/tudelft3d/MScGeomaticsThesisTemplate>.

## 1.1 HOW TO GET STARTED WITH $\text{\LaTeX}$ ?

Basically everything you need to know—from installation to details—is there:

<http://en.wikibooks.org/wiki/LaTeX>

To compile this template, you need a full installation of **MiKTeX** (Windows) or **TeXLive** (cross-platform) or **MacTeX** (OSX).

## 1.2 CROSS-REFERENCES

The command `autoref` can be used for chapters, sections, subsections, figures, tables, etc.

**Chapter 1** is what you are currently reading, and its name is **INTRODUCTION**. **Section 1.8** is about pseudo-code, and **Section 1.3.1** is about something else. The next chapter (**RELATED WORK; TITLE WHICH CAN SPAN MULTIPLE LINES**), is on page 7.

## 1.3 FIGURES

Figures **1.1** is a simple figure. Notice that all figures in your thesis should be referenced to in the main text. The same applies to tables and algorithms.

It is recommended *not* to force-place your figures (e.g. with commands such as: `\newpage` or by forcing a figure to be at the top of a page).  $\text{\LaTeX}$  usually places the figures automatically rather well. Only if at the end of your thesis you have small problem then can you solve them.

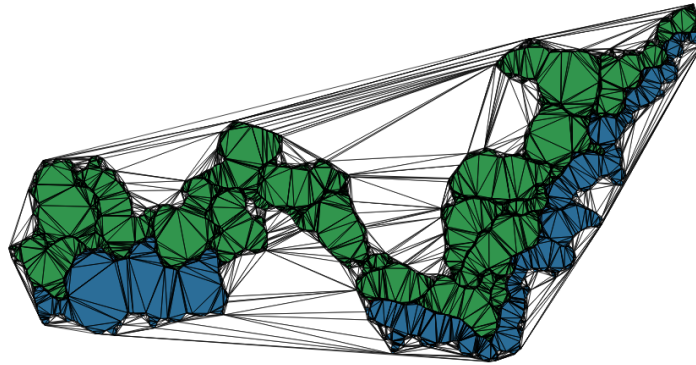


Figure 1.1: One nice figure

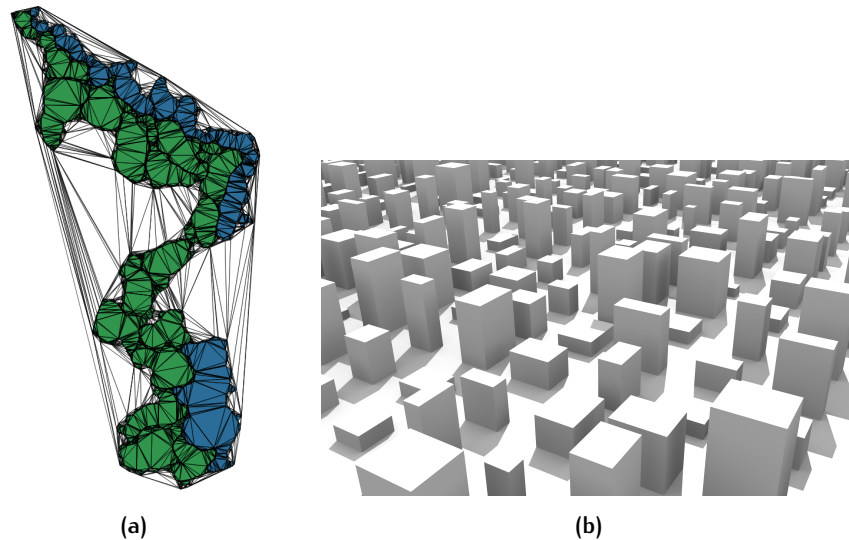


Figure 1.2: Two figures side-by-side. (a) A triangulation of 2 polygons. (b) Something not related at all.

As shown in [Figure 1.2](#), it is possible to have two figures (or more) side by side. You can also refer to a subfigure: see [Figure 1.2b](#).

#### 1.3.1 Figures in PDF are possible and even encouraged!

If you use Adobe Illustrator or **Ipe** you can make your figures vectorial and save them in PDF.

You include a PDF the same way as you do for a PNG, see [Figure 1.3](#),

## 1.4 HOW TO ADD REFERENCES?

References are best handled using Bib $\TeX$ . See the `myreferences.bib` file. A good cross-platform reference manager is **JabRef**.

[Descartes \[1637\]](#) wrote this and that [[Voronoi, 1908](#); [Delaunay, 1934](#)]. Instead of citing the whole paper [[Delaunay, 1934](#)], it is also possible to cite only the authors (e.g. [Delaunay](#)).

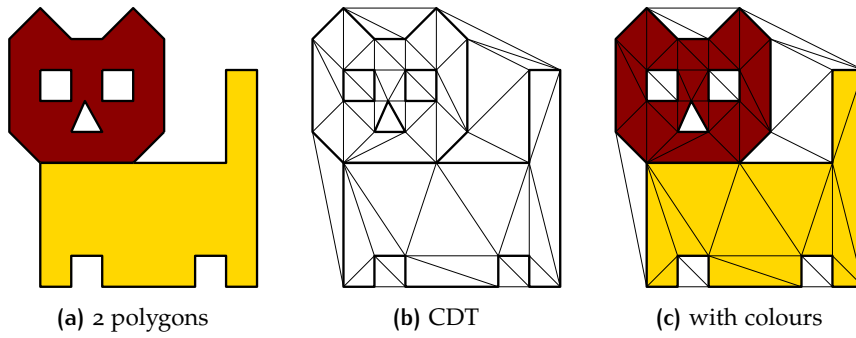


Figure 1.3: Three PDF figures.

	3D model		input	
	solids	faces	vertices	constraints
<b>campus</b>	370	4 298	5 970	3 976
<b>kvz</b>	637	6 549	8 951	13 571
<b>engelen</b>	1 629	15 870	23 732	15 868

Table 1.1: Details concerning the datasets used for the experiments.

## 1.5 FOOTNOTES

Footnotes are a good way to write text that is not essential for the understanding of the text<sup>1</sup>.

## 1.6 TABLES

The package `booktabs` permits you to make nicer tables than the basic ones in  $\text{\LaTeX}$ . See for instance [Table 1.1](#).

## 1.7 PLOTS

The best way is to use `matplotlib`, or its more beautiful version (`seaborn`). With these, you can use Python to generate nice PDF plots, such as that in [Figure 1.4](#).

In the folder `./plots/`, there is an example of a CSV file of the temperature of Delft, taken somewhere. From this CSV, the plot is generated with the script `createplot.py`.

## 1.8 PSEUDO-CODE

Please avoid putting code (Python, C++, Fortran) in your thesis. Small excerpt are probably fine (for some cases), but do not put all the code in an appendix. Instead, put your code somewhere online (e.g. GitHub) and put *pseudo-code* in your thesis. The package `algorithm2e` is pretty handy, see for instance the [Algorithm 1.1](#). All your algorithms will be automatically added

<sup>1</sup> but please do not overuse them

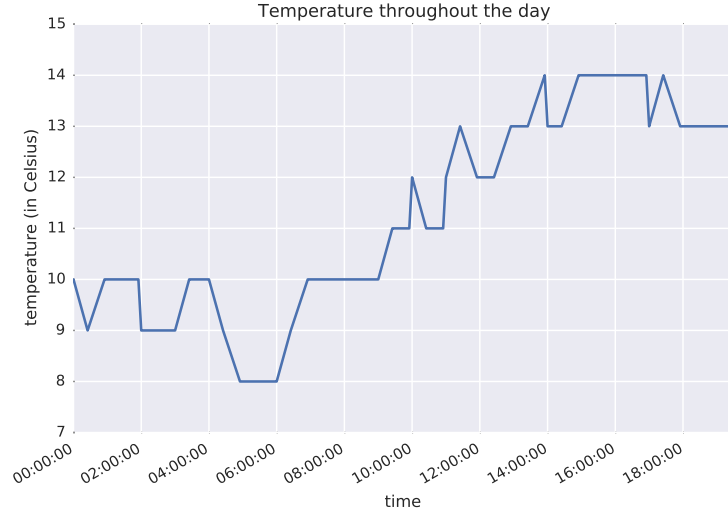


Figure 1.4: A super plot

to the list of algorithms at the beginning of the thesis. Observe that you can

---

**Algorithm 1.1:**  $\text{WALK}(\mathcal{T}, \tau, p)$ 


---

**Input:** A Delaunay tetrahedralization  $\mathcal{T}$ , a starting tetrahedron  $\tau$ , and a query point  $p$

**Output:**  $\tau_r$ : the tetrahedron in  $\mathcal{T}$  containing  $p$

---

```

1 while  $\tau_r$  not found do
2   for  $i \leftarrow 0$  to 3 do
3      $\sigma_i \leftarrow$  get face opposite vertex  $i$  in  $\tau$ ;
4     if  $\text{Orient}(\sigma_i, p) < 0$  then
5        $\tau \leftarrow$  get neighbouring tetrahedron of  $\tau$  incident to  $\sigma_i$ ;
6       break;
7   if  $i = 3$  then
8     // all the faces of  $\tau$  have been tested
9     return  $\tau_r = \tau$ 

```

---

put labels on certain lines (with ) and then reference to them: on line 4 of the Algorithm 1.1 this is happening.

If you want to put some code (or XML for instance), use the package listings, e.g. you can wrap it in a Figure so that it does not span over multiple pages.

## 1.9 ACRONYMS

If you want to have a list of acronyms you use in your thesis, use the acronym package. The first time you speak about geographical information system (GIS), it will be spelled out. Further use, GIS, you'll get the acronym plus a hyperlink to the list in the preamble of the thesis.

```

<gml:Solid>
  <gml:exterior>
    <gml:CompositeSurface>
      <gml:surfaceMember>
        <gml:Polygon>
          <gml:exterior>
            <gml:LinearRing>
              <gml:pos>0.000000 0.000000 1.000000</gml:pos>
              <gml:pos>1.000000 0.000000 1.000000</gml:pos>
              <gml:pos>1.000000 1.000000 1.000000</gml:pos>
              <gml:pos>0.000000 1.000000 1.000000</gml:pos>
              <gml:pos>0.000000 0.000000 1.000000</gml:pos>
            </gml:LinearRing>
          </gml:exterior>
          <gml:interior>
            ...
          </gml:surfaceMember>
        </gml:CompositeSurface>
      </gml:interior>
    </gml:Solid>

```

Figure 1.5: Some GML for a `gml:Solid`.

Add yours to `front/acronyms.tex`. Notice that only these used are printed, e.g. Delaunay triangulation ([DT](#)) and triangular irregular network ([TIN](#)).



## 2

## RELATED WORK; TITLE WHICH CAN SPAN MULTIPLE LINES

Bacon ipsum dolour sit amet porchetta beef turkey, bacon turducken boudin hamburger venison ball tip. Brisket pork loin bresaola short loin ground round leberkas pastrami tongue jerky cow turducken beef ribs. Pork ribeye landjaeger prosciutto pig venison tenderloin. Swine beef ribs kielbasa, porchetta tenderloin salami venison pork belly tail. Bacon ipsum dolour sit amet porchetta beef turkey, bacon turducken boudin hamburger venison ball tip. Brisket pork loin bresaola short loin ground round leberkas pastrami tongue jerky cow turducken beef ribs. Pork ribeye landjaeger prosciutto pig venison tenderloin. Swine beef ribs kielbasa, porchetta tenderloin salami venison pork belly tail. Bacon ipsum dolour sit amet porchetta beef turkey, bacon turducken boudin hamburger venison ball tip. Brisket pork loin bresaola short loin ground round leberkas pastrami tongue jerky cow turducken beef ribs. Pork ribeye landjaeger prosciutto pig venison tenderloin. Swine beef ribs kielbasa, porchetta tenderloin salami venison pork belly tail.

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- Descartes, R. (1637). *Discours de la méthode*. Jan Maire, Leyde.
- Voronoi, G. M. (1908). Nouvelles applications des paramètres continus à la théorie des formes quadratiques. *Journal für die Reine und Angewandte Mathematik*, 134:198–287.



# A | REFLECTION

At P4 a draft reflection must be handed in. A final version of the reflection must be included as a distinct part of the thesis (a separate chapter) or as a separate document at the P4. In this reflection the student uses a short substantiated explanation to account for the results of the research in the graduation phase (product, process, planning). Depending on the research, reflection on a number of the following aspects should be included (you may choose in which order). The reflection should be in the form of a text, with diagrams and sketches for purposes of illustration and clarification.

**ASPECT 1** The relationship between the methodical line of approach of the Master Geomatics and the method chosen by the student in this framework.

**ASPECT 2** The relationship between the conducted research and application of the field geomatics.

**ASPECT 3** The relationship between the project and the wider social context.



# B | SOME UML DIAGRAMS

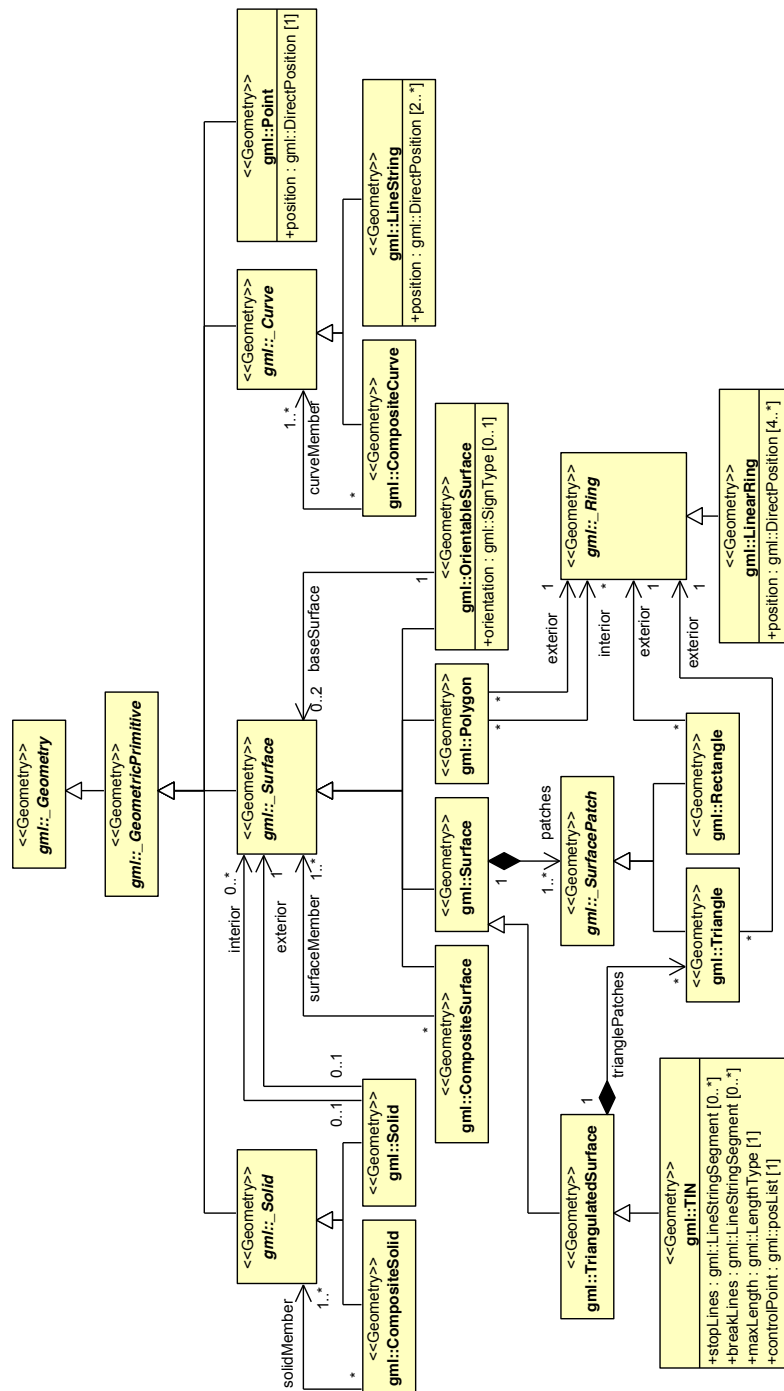


Figure B.1: The UML diagram of CityGML

## COLOPHON

This document was typeset using  $\text{\LaTeX}$ . The document layout was generated using the `arsclassica` package by Lorenzo Pantieri, which is an adaption of the original `classicthesis` package from André Miede.