



# Capturing Factorized Provenance (FDB 2022)

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## Outline

- **Overview & Motivation**
- Provenance Graph Model
- Capturing Provenance
- Factorization
- Experiments
- Conclusions & Future work

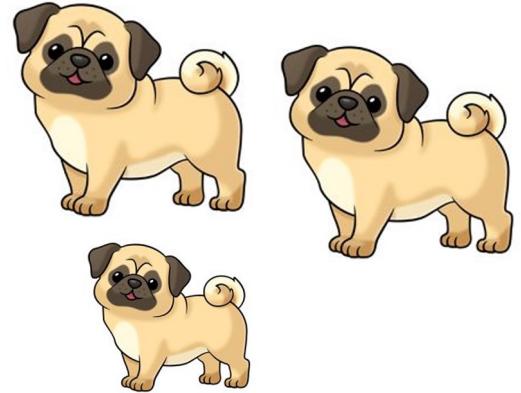
# Debugging Datalog

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- **Datalog has seen a resurgence in academia & industry**
  - Programming distributed systems
  - Complex data-intensive computations
  - Analytics & ML over query results
- **Urgent need for debugging Datalog programs**
  - Why did my program produce this unexpected result?
  - Why did my program not produce this expected result?
  - Which rules are responsible for deriving this result?
  - Why did this rule derivation fail?
  - Would deleting & inserting a tuple change the result?



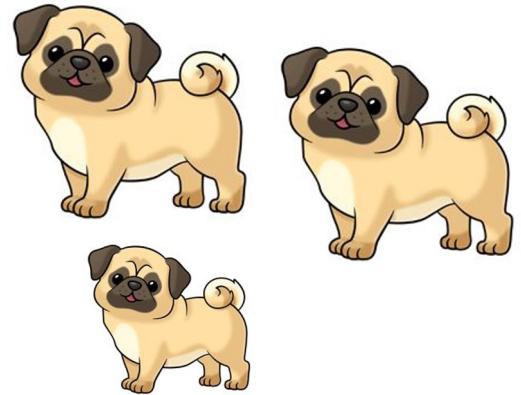
## PUG + PUGS



***Efficient capture and summarization for why and why-not provenance through a provenance model developed for queries with negation***



## PUG + PUGS



***Efficient capture*** and ***summarization*** for ***why and why-not*** provenance through a ***provenance model developed***  
*for queries with negation*

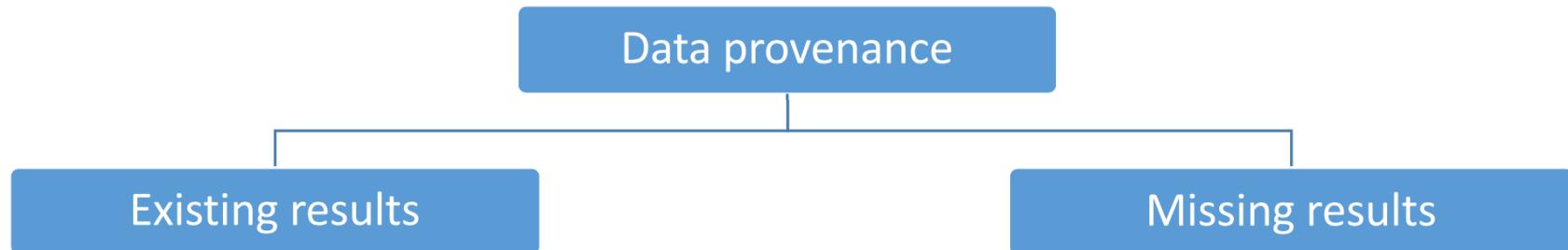
***This is FDB!***



*PUG utilizes a flat-relational encoding of provenance graphs which essentially corresponds to a factorized representation of provenance*

# Schism between Why / Why-not

- How the rules of a program did derive / failed to derive an existing / missing output from the input data

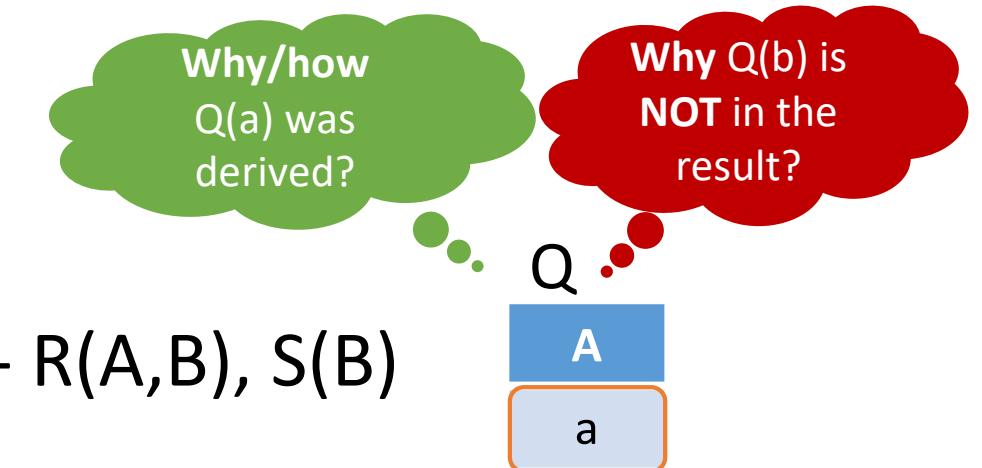


Why

| R | S |   |
|---|---|---|
| A | B | B |
| b | a | b |
| a | b |   |

$Q(A) :- R(A,B), S(B)$

Why-not



## Unifying Why / Why-not

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- **Why** (provenance) and **why-not** (missing answers) have been mostly treated in isolation
- Why and why-not questions can be reduced to each other for a query language **L** if ...
  - for any query **Q**, its complement **Q<sup>C</sup>** is in **L**

$$t \notin Q(D) \equiv t \in Q^C(D)$$

$Q(A) :- R(A, B)$

$Q^C(A) :- R(A, B), \text{adom}(A), \text{adom}(B)$

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# Requirements

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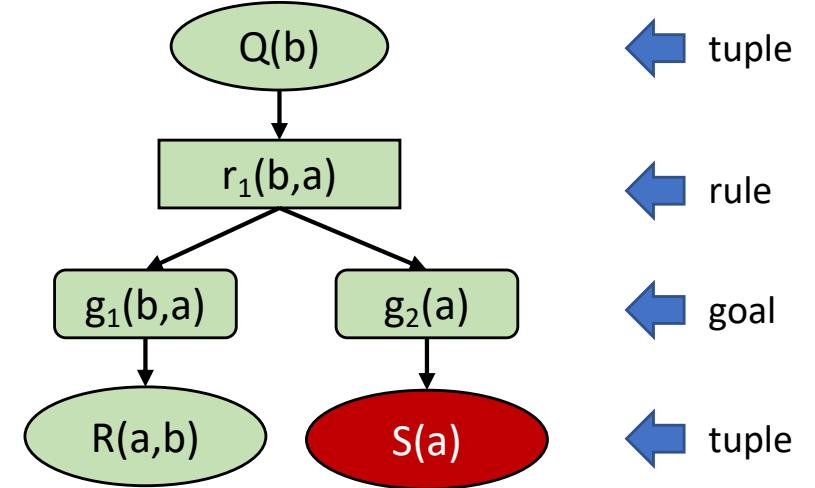
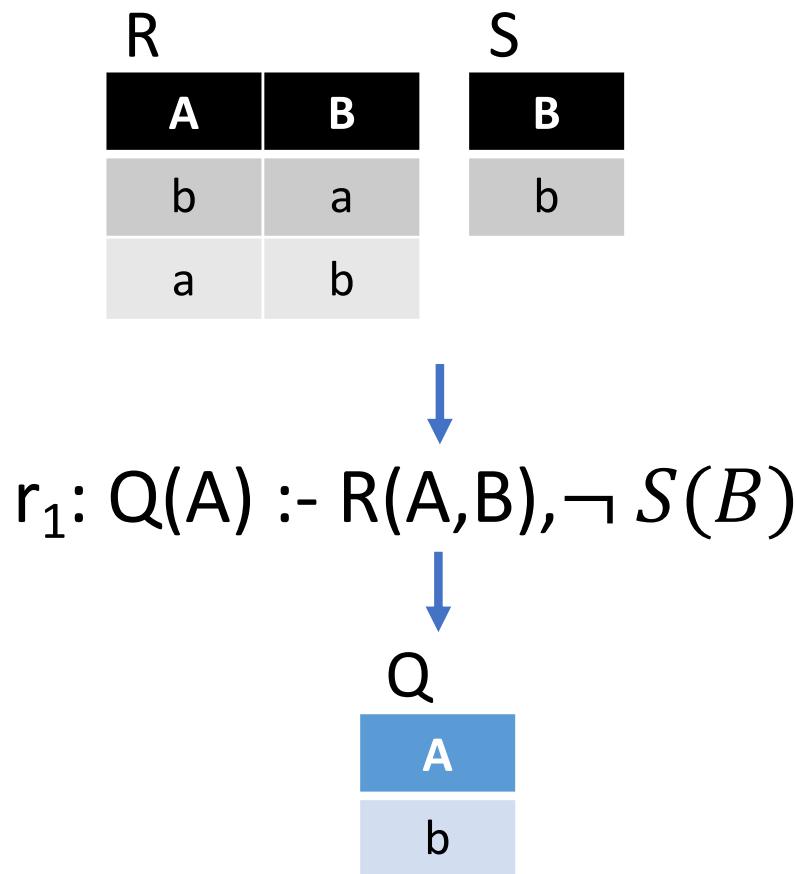


- **Syntax-driven**
  - Provenance structure aligns with program structure
- **Compatible with well-established provenance models**
  - Provenance polynomials for positive queries [1]
  - Dual polynomials [2]
- **Build-in support for sharing common subexpressions**

[1] T. Green, G. Karvounarakis, and V. Tannen. Provenance semirings. In PODS, pages 31–40, 2007.

[2] E.Grädel and V.Tannen.Semiring provenance for first-order model checking. arXiv preprint arXiv:1712.01980, 2017.

# Provenance Graph Model



Green: success / existence  
 Red: failure / absence

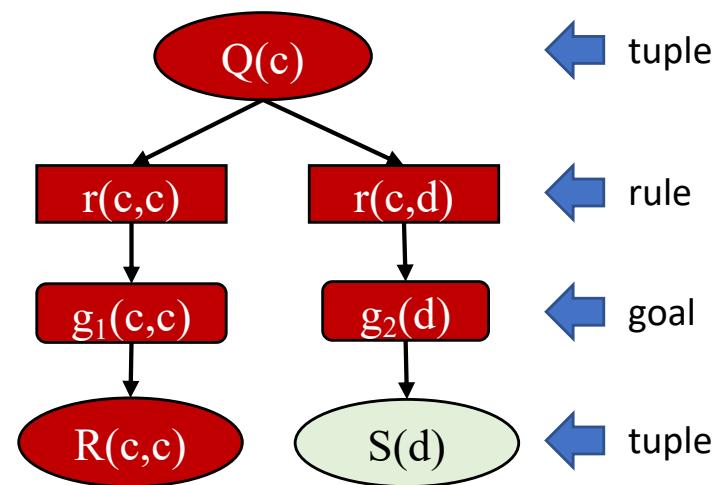
# Provenance Graph Model

| R |   | S |
|---|---|---|
| A | B | B |
| d | c | d |
| c | d |   |

r:  $Q(A) :- R(A,B), \neg S(B)$

|   |
|---|
| A |
| d |

Why  $Q(c)$  is NOT  
in the output?



Green: success / existence  
Red: failure / absence

# Provenance Graph Model

| R |   | S |
|---|---|---|
| A | B | B |
| d | c | d |
| c | d |   |

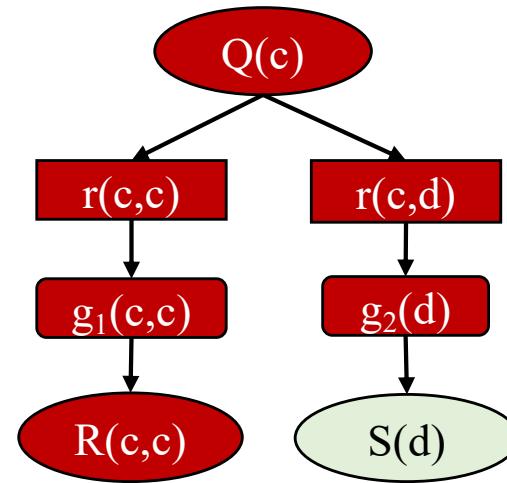


r:  $Q(A) :- R(A,B), \neg S(B)$



| Q |     |
|---|-----|
| A | ... |
| d |     |

Why  $Q(c)$  is NOT  
in the output?



# Provenance Graph Model

| R |   | S |  |
|---|---|---|--|
| A |   | B |  |
| d | c | d |  |
| c | d |   |  |

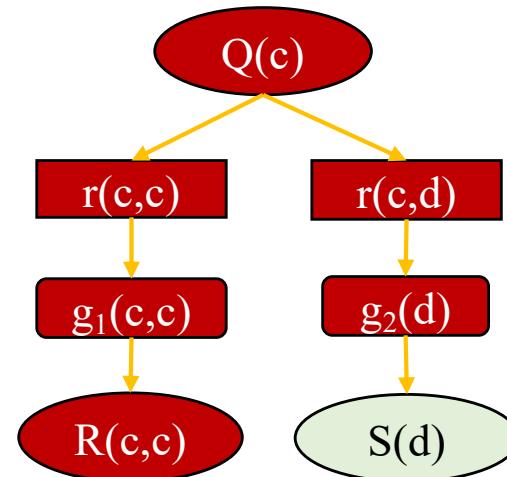
↓

r:  $Q(A) :- R(A,B), \neg S(B)$

↓

|   |
|---|
| A |
| d |

... Why  $Q(c)$  is NOT in the output?



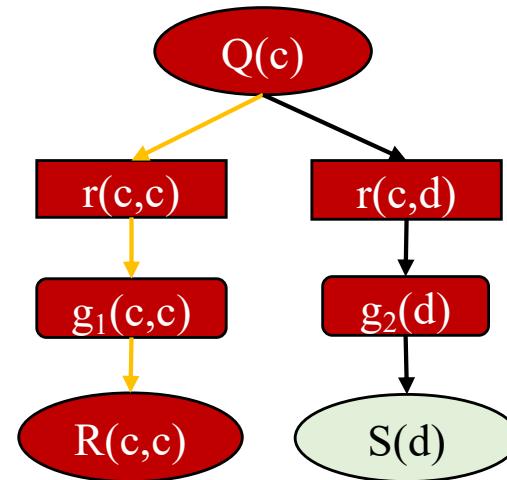
# Provenance Graph Model

| R |   | S |
|---|---|---|
| A | B | B |
| d | c | d |
| c | d |   |

$r: Q(c) :- R(c,c), \neg S(c)$

|   |
|---|
| A |
| d |

Why  $Q(c)$  is NOT  
in the output?



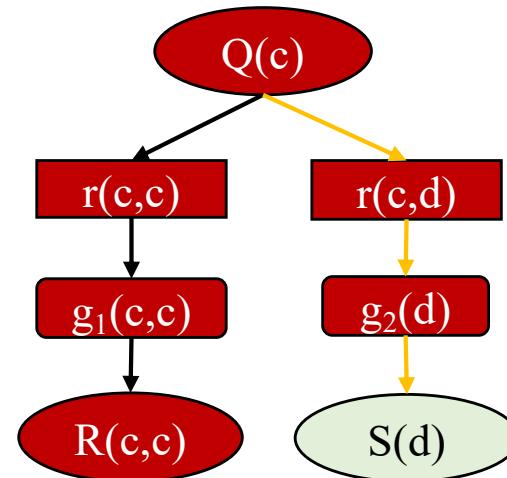
# Provenance Graph Model

| R |   | S |
|---|---|---|
| A | B | B |
| d | c | d |
| c | d |   |

r:  $Q(c) :- R(c,d), \neg S(d)$

|   |
|---|
| A |
| d |

Why  $Q(c)$  is NOT  
in the output?

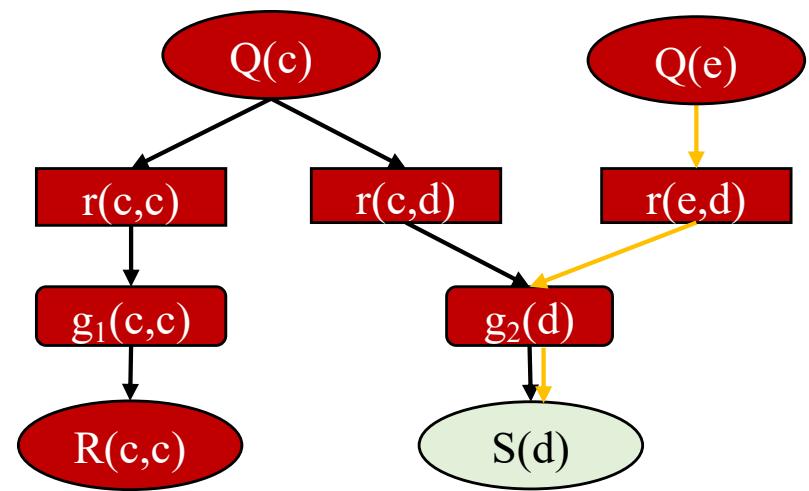


# Provenance Graph Model

| R |   | S |
|---|---|---|
| A | B | B |
| d | c | d |
| c | d |   |
| e | d |   |

r:  $Q(e) :- R(e,d), \neg S(d)$

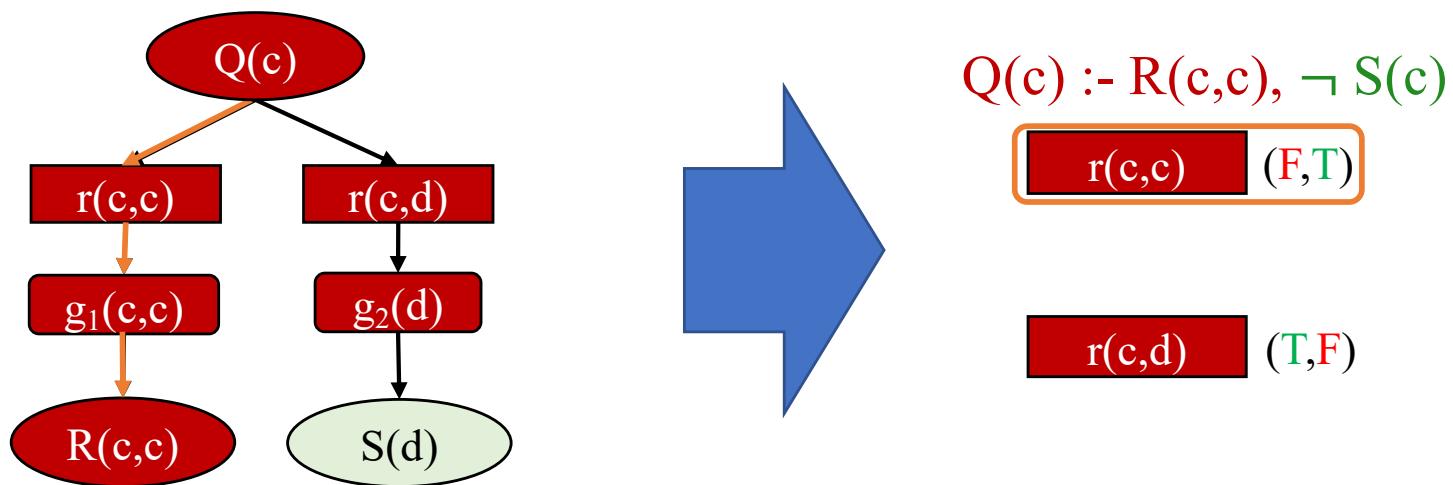
|   |   |
|---|---|
| Q | A |
|   | d |



Why  $Q(c)$  is NOT  
in the output?

# Provenance Graph Model

- Equivalent model (annotated rule derivations)



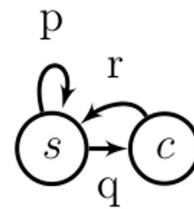
# Extracting Provenance Polynomials

$$r_2 : Q_{3\text{hop}}(X, Y) :- T(X, A), T(A, B), T(B, Y)$$

Relation Train

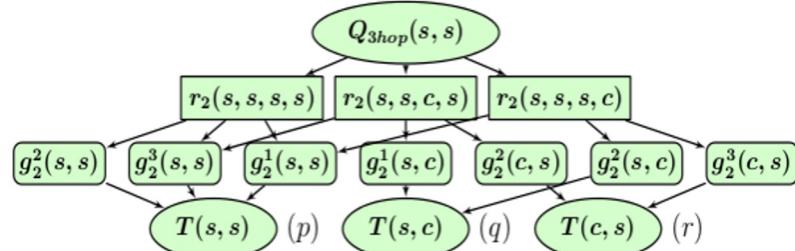
| fromCity | toCity  |
|----------|---------|
| seattle  | seattle |
| seattle  | chicago |
| chicago  | seattle |

$$\begin{array}{c} \mathbb{N}[X] \\ \hline p \\ q \\ r \end{array}$$

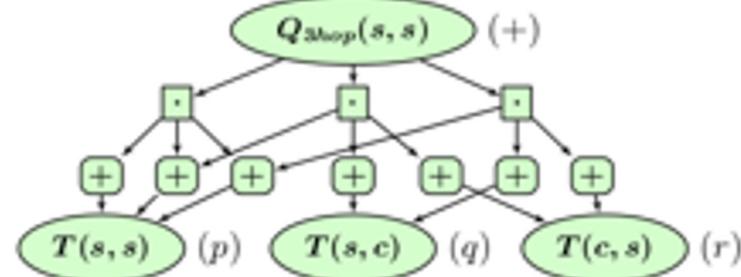


Result of query  $Q_{3\text{hop}}$

| X       | Y       | $\mathbb{N}[X]$ |
|---------|---------|-----------------|
| seattle | seattle | $p^3 + 2pqr$    |



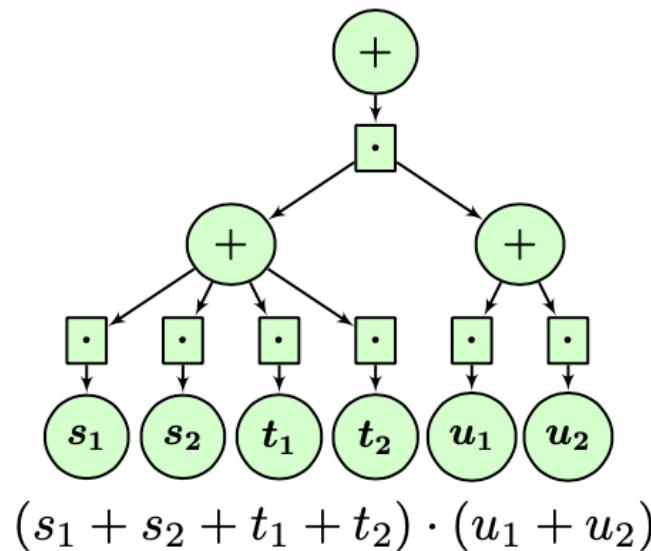
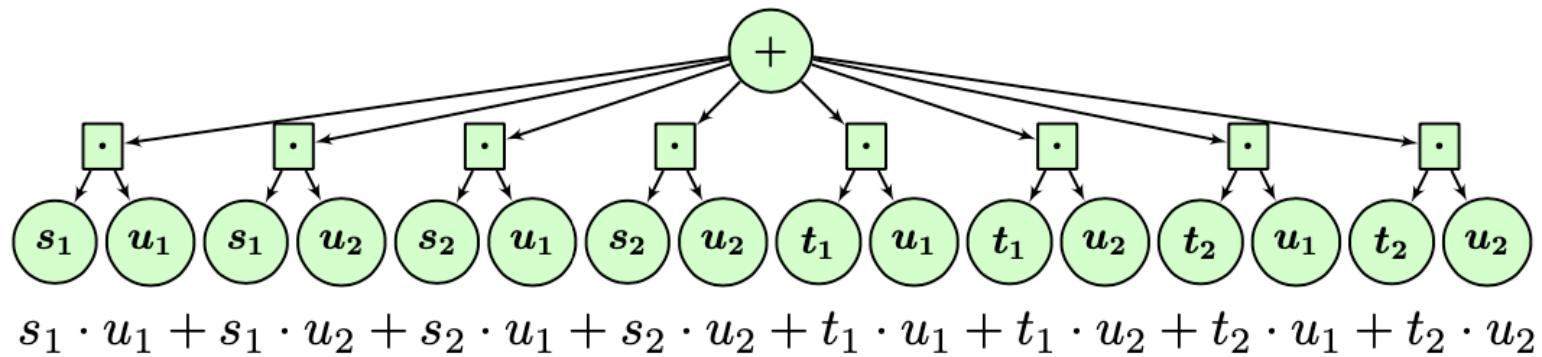
$$\begin{aligned} & r_2(g_1(p) \cdot g_2(p) \cdot g_3(p)) + r_2(g_1(q) \cdot g_2(r) \cdot g_3(p)) \\ & + r_2(g_1(p) \cdot g_2(q) \cdot g_3(r)) \end{aligned}$$



$$p^3 + 2 \cdot (p \cdot q \cdot r)$$

$$[[p, p, p], [p, q, r], [p, q, r]]$$

# Factorized Provenance Graphs



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## Problem definition

**input:** (missing) answers of interest

**output:** relevant subgraph for all answers of interest

## Instrumentation of the input Datalog program

- Use **firing rules** to capture rule derivations
- **Goal-oriented** approach
  - Limit the provenance based on the user question
  - Efficient bottom-up evaluation using relational engines
  - Compiling rewritten program into SQL

# Overview

---

## Rewriting steps

- **Unifying** the program with specification of outputs of interest
- **Statically annotate** program to indicate interest in success / failure
- Creating **firing rules**
- Checking **connectivity with joins**
- **Computing** the **edge** relation of the provenance graph

## Example query and provenance question

$$r_1 : Q(X, Y) : \neg \text{Train}(X, Z), \text{Train}(Z, Y), \neg \text{Train}(X, Y)$$

WHY  $Q(n, s)$ ?



## Rewriting steps

- **Unifying** the program with specification of outputs of interest
- **Statically annotate** program to indicate interest in success / failure
- Creating **firing rules**
- Checking **connectivity with joins**
- **Computing** the **edge** relation of the provenance graph

# Computing Explanations



## Step 1: Unifying the program with the question

- **Limit computation** by binding variables to constants
- Propagating constants in the question throughout the program

### Example

- Binding variables:  $X = n$  (New York) and  $Y = s$  (Seattle)

$r_1 : Q(X, Y) :- \neg \text{Train}(X, Z), \text{Train}(Z, Y), \neg \text{Train}(X, Y)$

+

WHY  $Q(n, s)$



$r_1^{(X=n, Y=s)} : Q(\underline{n}, \underline{s}) :- T(\underline{n}, Z), T(Z, \underline{s}), \neg T(\underline{n}, \underline{s})$

# Computing Explanations



## Step 2: Annotating rule with success / failure

- To determine the state of nodes
- The question provides information about success / failure
  - True = Success / Exist
  - False = Failed / Not Exist
- Propagate annotations throughout the unified program

### Example

- ▷ WHY Q(n,s) implies only successful goals need to be captured

$$r_1^{(X=n, Y=s)} : Q(n, s) :- T(n, Z), T(Z, s), \neg T(n, s)$$

+

WHY Q(n,s)


$$r_1^{(X=n, Y=s), T} : Q(n, s)^T :- T(n, Z)^T, T(Z, s)^T, \neg T(n, s)^T$$

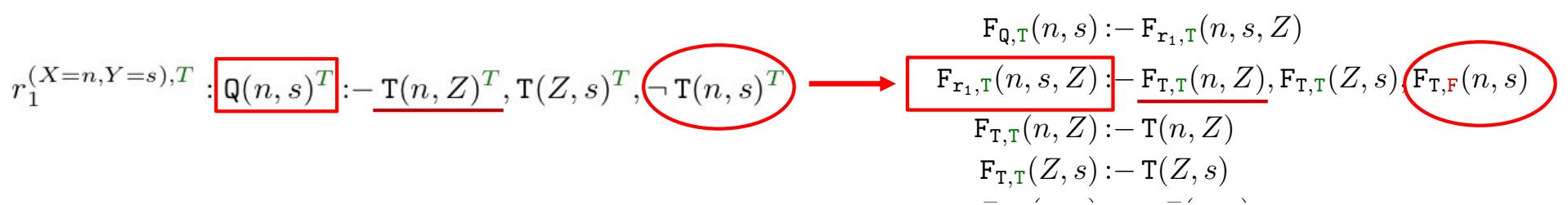
# Computing Explanations

## Step 3: Create firing rules

- Capture successful / failed derivations for the variable binding

### Example

- Create new head by adding the variable Z and use firing versions
- Invert the annotation  $\textcolor{red}{T}$  for the goal  $\neg T(n,s)$  in the firing version



# Computing Explanations

## Step 4: Connectivity joins

- Firing rules are **not sufficient to determine** which **subgraphs** of the provenance explain the outputs of interest
- Filter derivations by checking whether connectivity
- Check connectivity from the question node one hop at a time

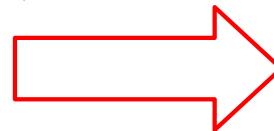
## Example

- No guarantees for the nodes in the red box
- Tuple node  $T(n, c)$  is only connected iff  $T(c, s)$  exists

$$F_{Q,T}(n, s) :- F_{r_1,T}(n, s, Z)$$

$$F_{r_1,T}(n, s, Z) :- F_{T,T}(n, Z), F_{T,T}(Z, s), F_{T,F}(n, s)$$

$F_{T,T}(n, Z) :- T(n, Z)$

$$F_{T,T}(Z, s) :- T(Z, s)$$


$$F_{Q,T}(n, s) :- F_{r_1,T}(n, s, Z)$$

$$F_{r_1,T}(n, s, Z) :- F_{T,T}(n, Z), F_{T,T}(Z, s), F_{T,F}(n, s)$$

$FC_{r_2,r_1,T}(n, Z) :- T(n, Z), F_{r_1,T}(n, s, Z)$

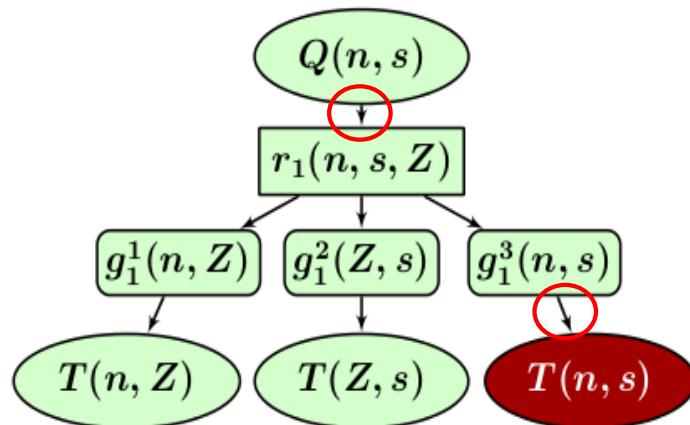
$FC_{r_2,r_1,T}(Z, s) :- T(Z, s), F_{r_1,T}(n, s, Z)$

$$F_{T,F}(n, s) :- \neg T(n, s)$$

# Computing Explanations

## Step 5: Computing provenance subgraph edge relation

- Create edges for the provenance graph (explanation)
- Generate rules for the edge relation based on the rule binding information
- Use node identifier  $f_{r_1}^T(n, s, Z)$
- Type of the node, assignments to constants, success/failure state
- Each rule corresponds to a pattern in the graph



- Provenance graph structure -

```

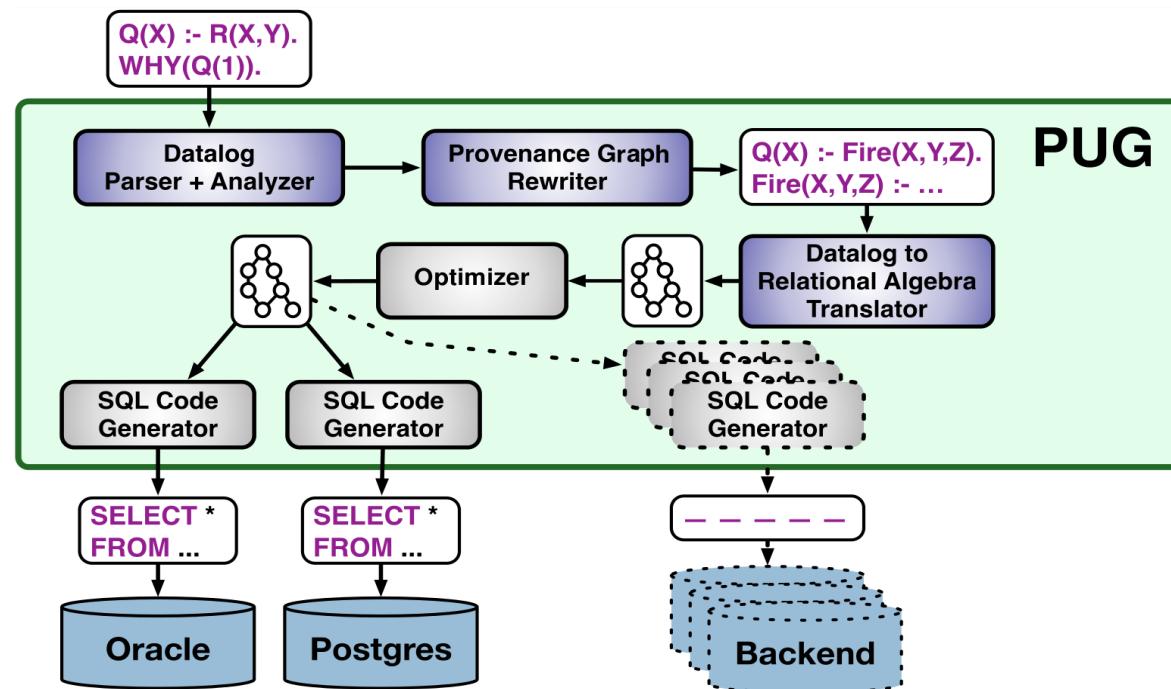
edge(f_Q^T(n, s), f_{r_1}(n, s, Z)) :- F_{r_1,T}(n, s, Z)
edge(f_{r_1}(n, s, Z), f_{g_1^1}(n, Z)) :- F_{r_1,T}(n, s, Z)
edge(f_{g_1^1}(n, Z), f_T^T(n, Z)) :- F_{r_1,T}(n, s, Z)
edge(f_{g_1^3}(n, s), f_T^F(n, s)) :- F_{r_1,T}(n, s, Z)
  
```

Example (partial) rules deriving the edge relation

# Implementation

## PUG (Provenance Unification through Graphs) architecture

- Extension of GProM supporting Datalog provenance
- GProM is a SQL+X – to – SQL optimizing compiler
- Relational algebra as IR



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# Recap

## Our provenance graphs can encode factorized polynomials

- What factorization we get is determined by the structure of the program

$Q() :- S(X), U(X, Y)$

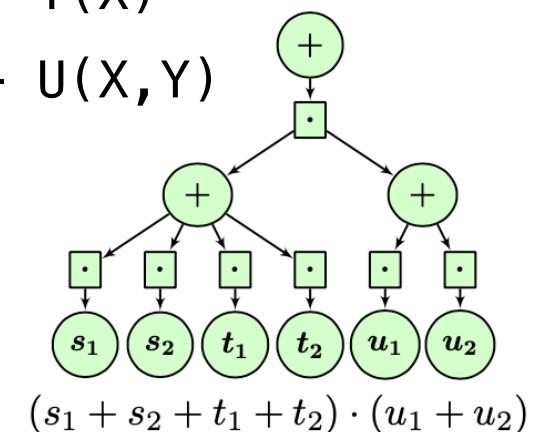
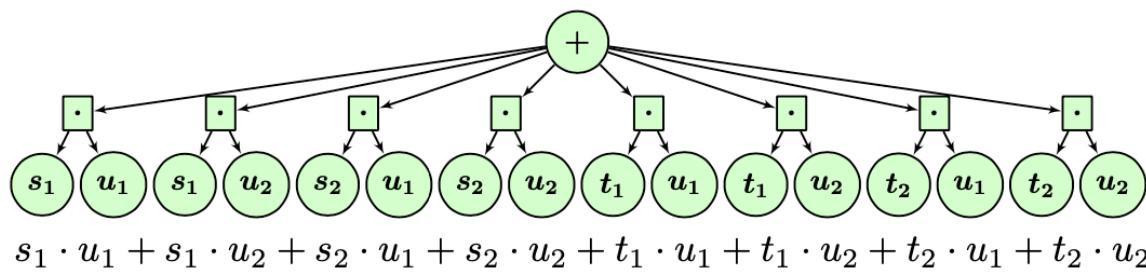
$Q() :- T(X), U(X, Y)$

$Q() :- Q2(X), Q1(X)$

$Q1(X) :- S(X)$

$Q1(X) :- T(X)$

$Q2(X) :- U(X, Y)$

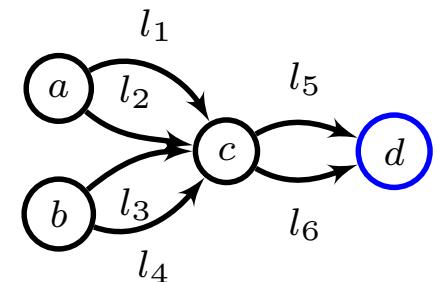


## Approach

- Determine worst-case optimal d-tree factorization
- Rewrite input query to produce this factorization
- Apply capture rewriting

D. Olteanu and J. Závodny. Size bounds for factorised representations of query results. ACM Transactions on Database Systems (TODS), 40(1):2, 2015.

$r_3 : Q_{2\text{hop}}(X) :- \text{H}(Y, L_1, Z), \text{H}(Z, L_2, X)$



# Utilizing work on factorization

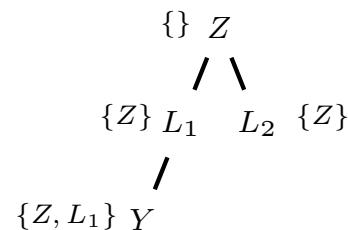
## Approach

- Determine worst-case optimal d-tree factorization
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$r_5 : Q_{2\text{hop}}() :- Q_{L_1}(Z), Q_{L_2}(Z)$

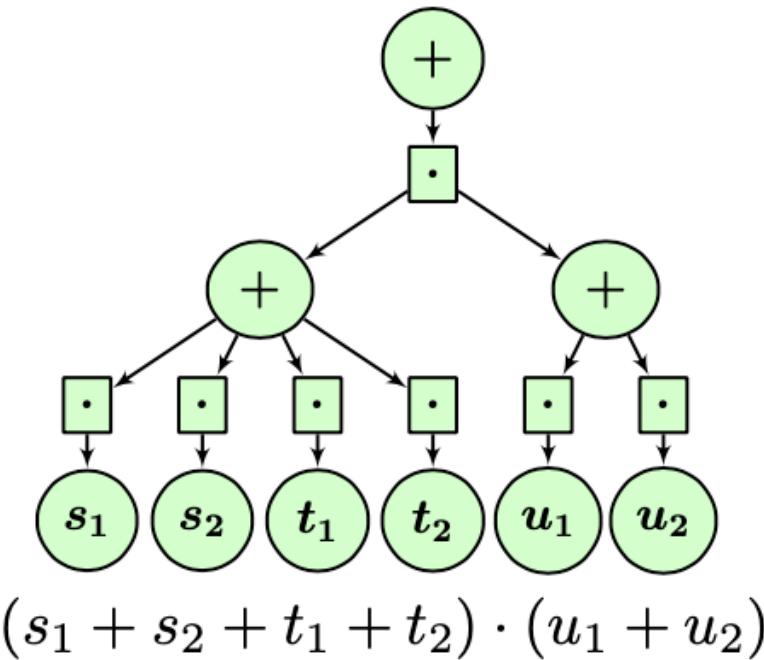
$r_{5'} : Q_{L_1}(Z) :- H(Y, L_1, Z)$

$r_{5''} : Q_{L_2}(Z) :- H(Z, L_2, d)$



Relation H

| S | L     | E |       |
|---|-------|---|-------|
| a | $l_1$ | c | $s_1$ |
| a | $l_2$ | c | $s_2$ |
| b | $l_3$ | c | $t_1$ |
| b | $l_4$ | c | $t_2$ |
| c | $l_5$ | d | $u_1$ |
| c | $l_6$ | d | $u_2$ |



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# Experiments

- TPC-H

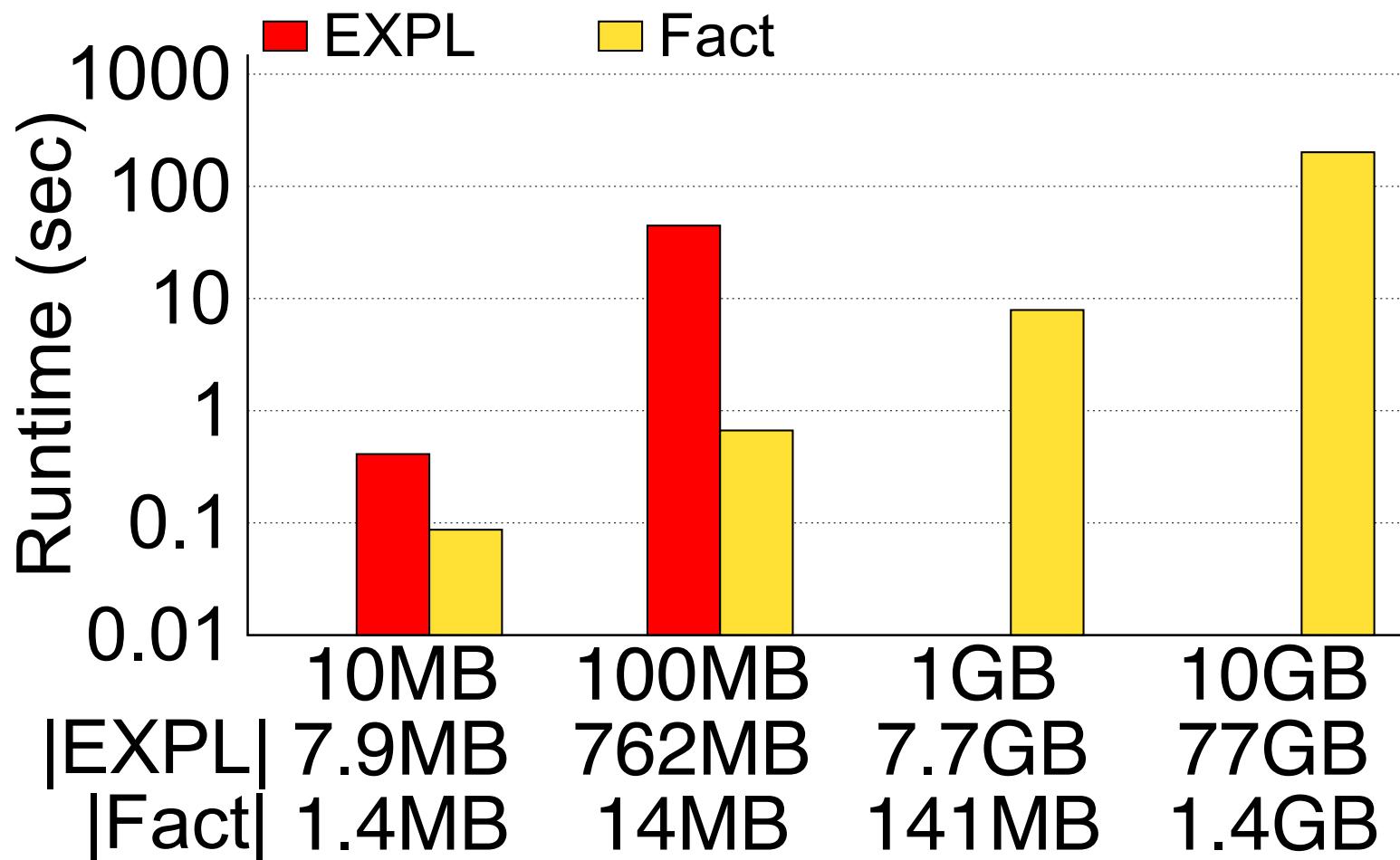
```
ordDisc(X,Y) :- CUSTOMER(A,X,B,C,D,E,F,G),
                ORDERS(H,A,I,J,K,L,M,O,P),
                LINEITEM(H,Q,R,S,T,U,V,Y,W,Z,A',B',C',D',E',F')
```



# Experiments

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- TPC-H  $\text{suppCust}(N) :- \text{SUPPLIER}(A, B, C, N, D, E, F), \text{CUSTOMER}(G, H, I, N, J, K, L, M)$



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# Conclusions

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- **Provenance graph model**

- Provenance structure aligns with program structure
- Compatible with well-established provenance models
- Provenance polynomials for positive queries + dual polynomials
- Build-in support for sharing common subexpressions
- Flat relational encoding as edge relation

- **Capturing Provenance**

- Incorporate user's provenance interest into the capture query
- Filter successful / failed assignments upfront (static analysis)
- Output is a query returning the edge relation of the graph

# Conclusions

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- **Factorization**
  - Program structure determines factorization
- **Approximate Summarization of Why-not Provenance**
  - Use patterns to summarize provenance
  - Use sampling to generate such summaries for very large why-not provenance graphs

## Future work

- **Expressiveness**
  - Support aggregation and recursion
- **Efficiency**
  - Leverage factorized DB techniques for aggregates?
  - Factorizing missing answers (complement representations)?
- **Going beyond SQL / Datalog as the target language**
  - What specialized algorithms & data structures would be beneficial?

*Questions?*



## Seokki Lee

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Grouppage: <https://sites.google.com/view/ucdbg>

PUG: <https://github.com/IITDBGroup/PUG>



# *Summarizing Provenance*

# Motivation (Example)

- Airbnb (bed and breakfast)

Listing (input)

| <b>Id</b> | <b>Name</b>      | <b>Ptype</b> | <b>Rtype</b> | <b>NGroup</b> | <b>Neighbor</b> |
|-----------|------------------|--------------|--------------|---------------|-----------------|
| 8403      | central place    | apt          | shared       | queen anne    | east            |
| 9211      | plum             | apt          | entire       | ballard       | adams           |
| 2445      | cozy homebase    | house        | private      | queen anne    | west            |
| 8575      | near SpaceNeedle | apt          | shared       | queen anne    | lower           |
| 4947      | seattle couch    | condo        | shared       | downtown      | first hill      |
| 2332      | modern view      | house        | entire       | queen anne    | west            |

Availability (input)

| <b>Id</b> | <b>Date</b> | <b>Price</b> |
|-----------|-------------|--------------|
| 9211      | 2016-11-09  | 130          |
| 2445      | 2016-11-09  | 45           |
| 2332      | 2016-11-09  | 350          |
| 4947      | 2016-11-10  | 40           |



$r_1: AL(N,R) :- L(I, N, T, R, queen\ anne, E), A(I, 2016-11-09, P)$

“ What are available listings and the room types in Queen Anne on Nov 9<sup>th</sup>, 2016? ”



| AvailableListings (output) |              |
|----------------------------|--------------|
| <b>Name</b>                | <b>Rtype</b> |
| cozy homebase              | private      |
| modern view                | entire       |

Why no shared room exists?

## Motivation (Example)

Why-not provenance  
(instance-based)

All derivations

Why-not [Huang et al. VLDB 2008]  
Artemis [Herschel et al. VLDB 2009]

Single derivation

Y! [Wu et al. SIGCOMM 2014]

**Not scalable**

**Not comprehensive**

# Motivation (Example)

Listing (input)

| <b>Id</b> | <b>Name</b>      | <b>Ptype</b> | <b>Rtype</b> | <b>NGroup</b> | <b>Neighbor</b> |
|-----------|------------------|--------------|--------------|---------------|-----------------|
| 8403      | central place    | apt          | shared       | queen anne    | east            |
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Availability (input)

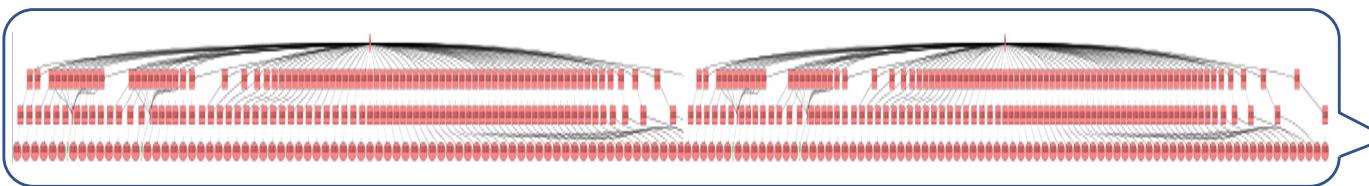
| <b>Id</b> | <b>Date</b> | <b>Price</b> |
|-----------|-------------|--------------|
| 9211      | 2016-11-09  | 130          |
| 2445      | 2016-11-09  | 45           |
| 2332      | 2016-11-09  | 350          |
| 4947      | 2016-11-10  | 40           |

Why no shared room exists?

r<sub>1</sub>: AL(N,R) :- L(I,N,T,R) queen anne, E), A(I, 2016-11-09, P)

| Attribute        | Id | Name | Ptype | Rtype | NGroup | Neighbor | Date | Price |
|------------------|----|------|-------|-------|--------|----------|------|-------|
| #Distinct Values | 6  | 6    | 3     | 3     | 3      | 5        | 2    | 4     |

= 2160



~ $15 \cdot 10^{20}$  derivations over full dataset (~ 1.4M)

# Motivation (Example)

Listing (input)

| <b>Id</b> | <b>Name</b>   | <b>Ptype</b> | <b>Rtype</b> | <b>NGroup</b> | <b>Neighbor</b> |
|-----------|---------------|--------------|--------------|---------------|-----------------|
| 8403      | central place | apt          | shared       | queen anne    | east            |

Availability (input)

| <b>Id</b> | <b>Date</b> | <b>Price</b> |
|-----------|-------------|--------------|
|           |             |              |

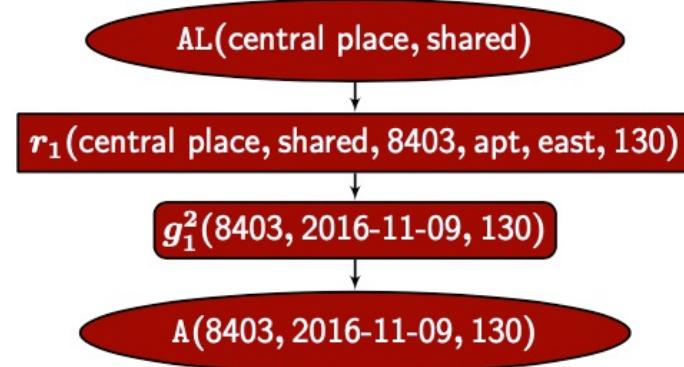
$r_1: AL(N,R) :- L(I, N, T, R, queen\ anne, E), A(I, 2016-11-09, P)$

AvailableListings (output)

| <b>Name</b>   | <b>Rtype</b> |
|---------------|--------------|
| cozy homebase | private      |
| modern view   | entire       |

Why no shared room exists?

The listing 'central place' has a shared room which is not available at \$130



# Motivation (Example)

Listing (input)

| <b>Id</b> | <b>Name</b>      | <b>Ptype</b> | <b>Rtype</b> | <b>NGroup</b> | <b>Neighbor</b> |
|-----------|------------------|--------------|--------------|---------------|-----------------|
| 8403      | central place    | apt          | shared       | queen anne    | east            |
| 9211      | plum             | apt          | entire       | ballard       | adams           |
| 2445      | cozy homebase    | house        | private      | queen anne    | west            |
| 8575      | near SpaceNeedle | apt          | shared       | queen anne    | lower           |
| 4947      | seattle couch    | condo        | shared       | downtown      | first hill      |
| 2332      | modern view      | house        | entire       | queen anne    | west            |

Availability (input)

| <b>Id</b> | <b>Date</b> | <b>Price</b> |
|-----------|-------------|--------------|
| 9211      | 2016-11-09  | 130          |
| 2445      | 2016-11-09  | 45           |
| 2332      | 2016-11-09  | 350          |
| 4947      | 2016-11-10  | 40           |

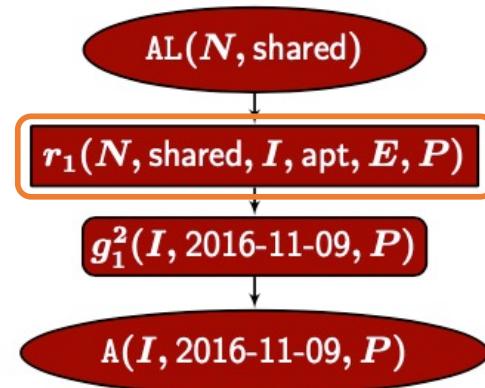
$r_1: AL(N,R) :- L(I, N, T, R, queen\ anne, E), A(I, 2016-11-09, P)$

AvailableListings (output)

| <b>Name</b>   | <b>Rtype</b> |
|---------------|--------------|
| cozy homebase | private      |
| modern view   | entire       |

Why no shared room exists?

“ All shared rooms of apartments in Queen Anne are not available at any price on Nov 9th, 2016 ”



# Summarizing Provenance

---

- Goals

- **Concise** (small size of explanations)
- **Complete** (covering all provenance)
- **Informative** (providing new insights)

- Challenge

- **Fullfilling all 3 elements** at the same time
- **Computing** summaries using **full why-not provenance**

# Summarizing Provenance

---



- Computing **top- $k$**  summaries using patterns
  - Concise explanations
  - Meaningful (semantically)
- Integrating **sampling** into provenance capture process
  - Unbiased
  - Computing representative patterns
  - Calculating close enough approximate completeness of patterns

# Summarizing Provenance

---



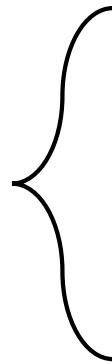
- What are patterns?

$r_1(N, \text{shared}, I, \text{apt}, E, P)$  | (T,F)

# Summarizing Provenance

- What are patterns?

$r_1(N, \text{shared}, I, \text{apt}, E, P)$  (T,F)



|  |       |
|--|-------|
| $r_1(\text{central place, shared, 8403, apt, east, } 130)$     | (T,F) |
| $r_1(\text{near SpaceNeedle, shared, 8575, apt, lower, } 40)$  | (T,F) |
| $r_1(\text{central place, shared, 8403, apt, east, } 40)$      | (T,F) |
| $r_1(\text{near SpaceNeedle, shared, 8575, apt, lower, } 350)$ | (T,F) |
| $r_1(\text{central place, shared, 8403, apt, east, } 350)$     | (T,F) |
| $r_1(\text{central place, shared, 8403, apt, east, } 45)$      | (T,F) |

.....

# Summarizing Provenance

- What are patterns?

$r_1(N, \text{shared}, I, \text{apt}, E, P)$  (T,F)



|  |       |
|--|-------|
| $r_1(\text{central place, shared, } 8403, \text{apt, east, } 130)$     | (T,F) |
| $r_1(\text{near SpaceNeedle, shared, } 8575, \text{apt, lower, } 40)$  | (T,F) |
| $r_1(\text{central place, shared, } 8403, \text{apt, east, } 40)$      | (T,F) |
| $r_1(\text{near SpaceNeedle, shared, } 8575, \text{apt, lower, } 350)$ | (T,F) |
| $r_1(\text{central place, shared, } 8403, \text{apt, east, } 350)$     | (T,F) |
| $r_1(\text{central place, shared, } 8403, \text{apt, east, } 45)$      | (T,F) |

.....

# Summarizing Provenance

- What are provenance summaries?

| Summary   |       |       |
|---|-------|-------|
| $r_1(N, \text{shared}, I, \text{apt}, E, P)$                    | (T,F) | ..... |
| $r_1(\text{central place}, \text{shared}, I, \text{apt}, E, P)$ | (T,F) | ..... |
| $r_1(N, \text{shared}, I, \text{condo}, E, P)$                  | (T,F) | ..... |
| $r_1(N, \text{shared}, I, \text{apt}, E, 130)$                  | (F,T) | ..... |
| $r_1(N, \text{shared}, I, \text{house}, \text{east}, P)$        | (F,F) | ..... |
| $r_1(N, \text{shared}, I, \text{house}, E, 350)$                | (T,F) | ..... |

# Summarizing Provenance



- Quality metrics
  - Completeness (cp): fraction of provenance covered by a pattern

$r_1(\text{central place, shared, 8403, apt, east, 130})$

$(T,F)$

$\leqslant$

$r_1(N, \text{shared, I, apt, E, P})$

$(T,F)$

# Summarizing Provenance

- Quality metrics
  - Completeness (cp): fraction of provenance covered by a pattern
  - Informativeness (info): degree of new information from a pattern

Why no shared  
room exists?

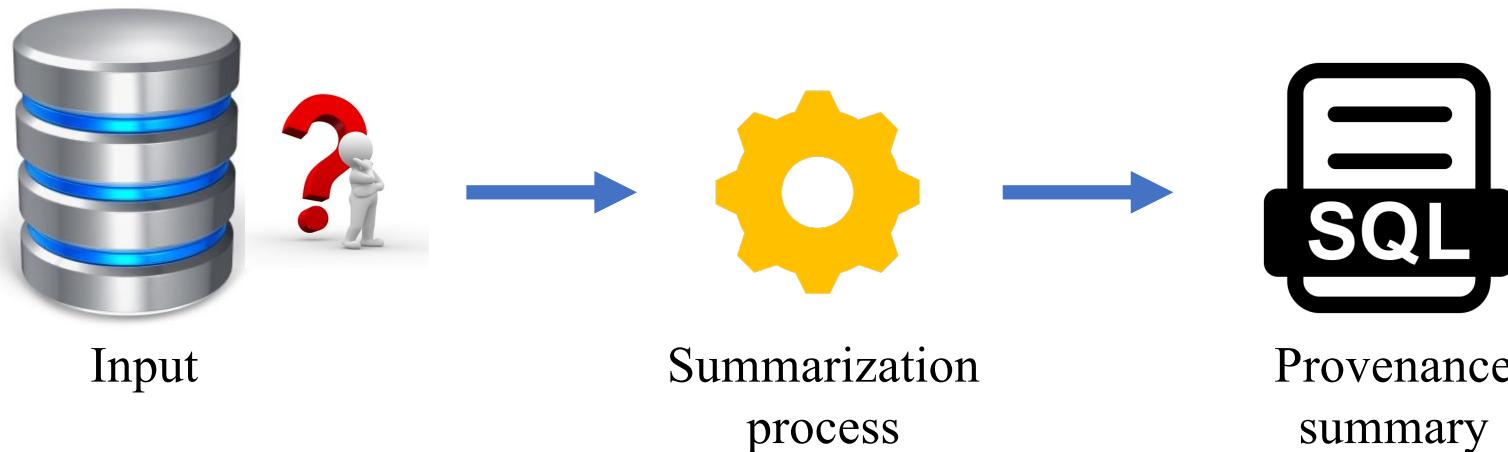
$$r_1(N, \text{shared}, I, \text{apt}, E, P) \quad (\text{T}, \text{F}) \quad > \quad r_1(N, \text{shared}, I, R, E, P) \quad (\text{T}, \text{F})$$

# Summarizing Provenance

- How to compute summaries
  - Heuristic using a sample of why-not provenance

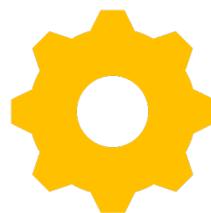
Size of the summary ( $k$ )

$Q(A) :- R(A,B), \neg S(B)$

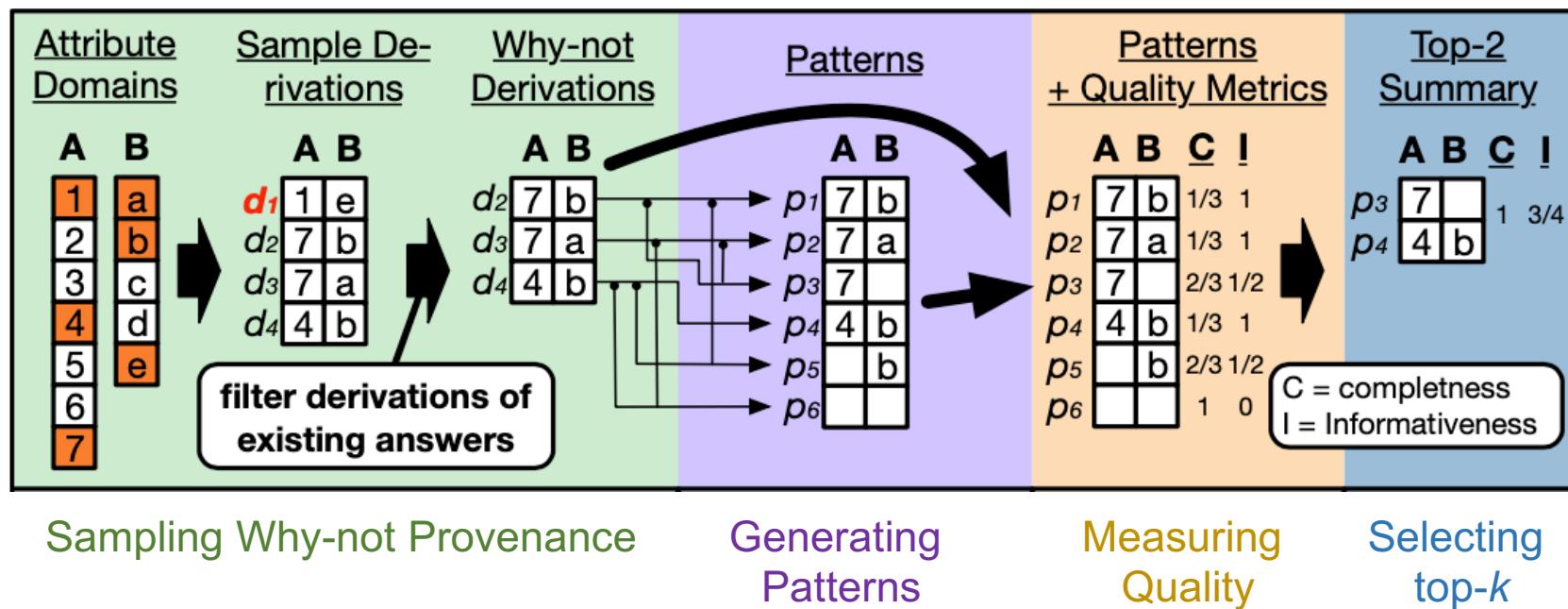


# Summarizing Provenance

- How to compute summaries

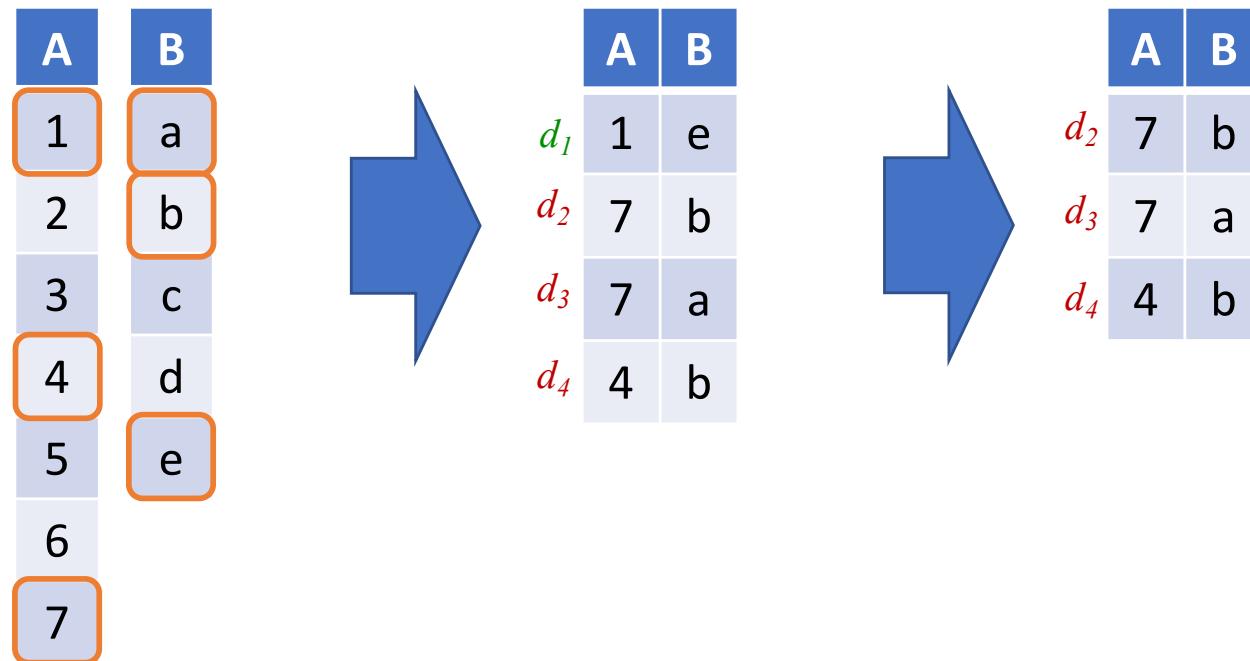


Summarization process



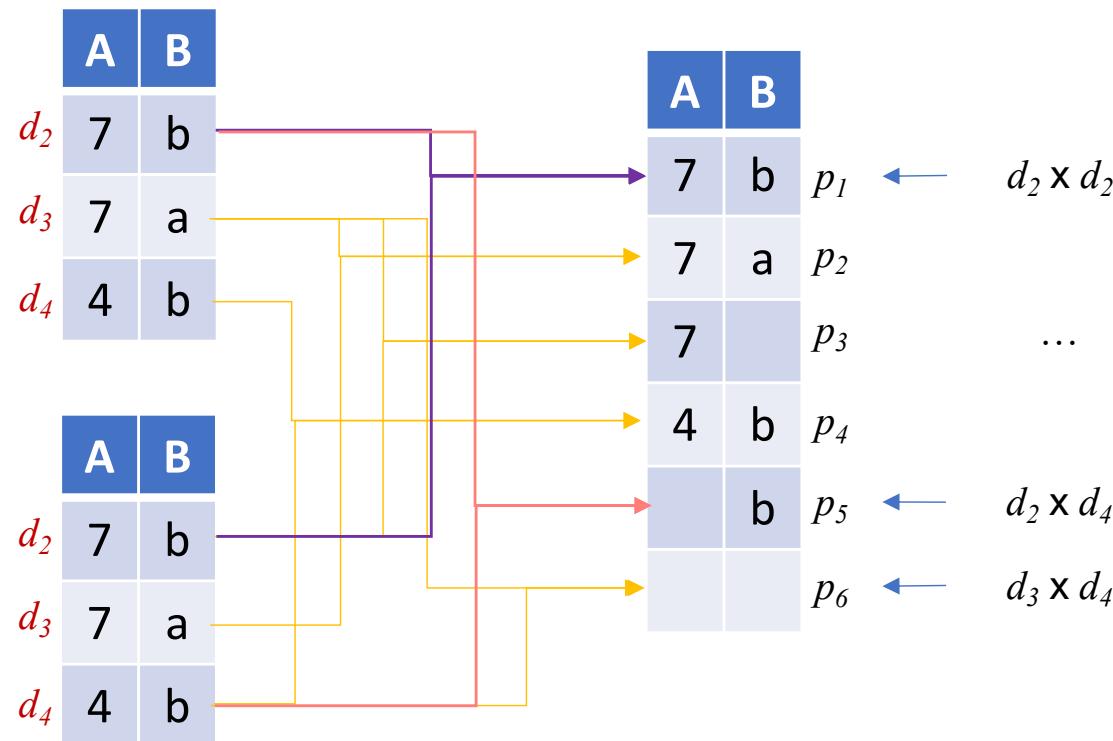
# Summarizing Provenance

- Sampling why-not provenance
  - Generating a sample that is equivalent to uniform random sample
    - Without computing full why-not provenance
  - Batch sampling: generating a query that returns an unbiased sample



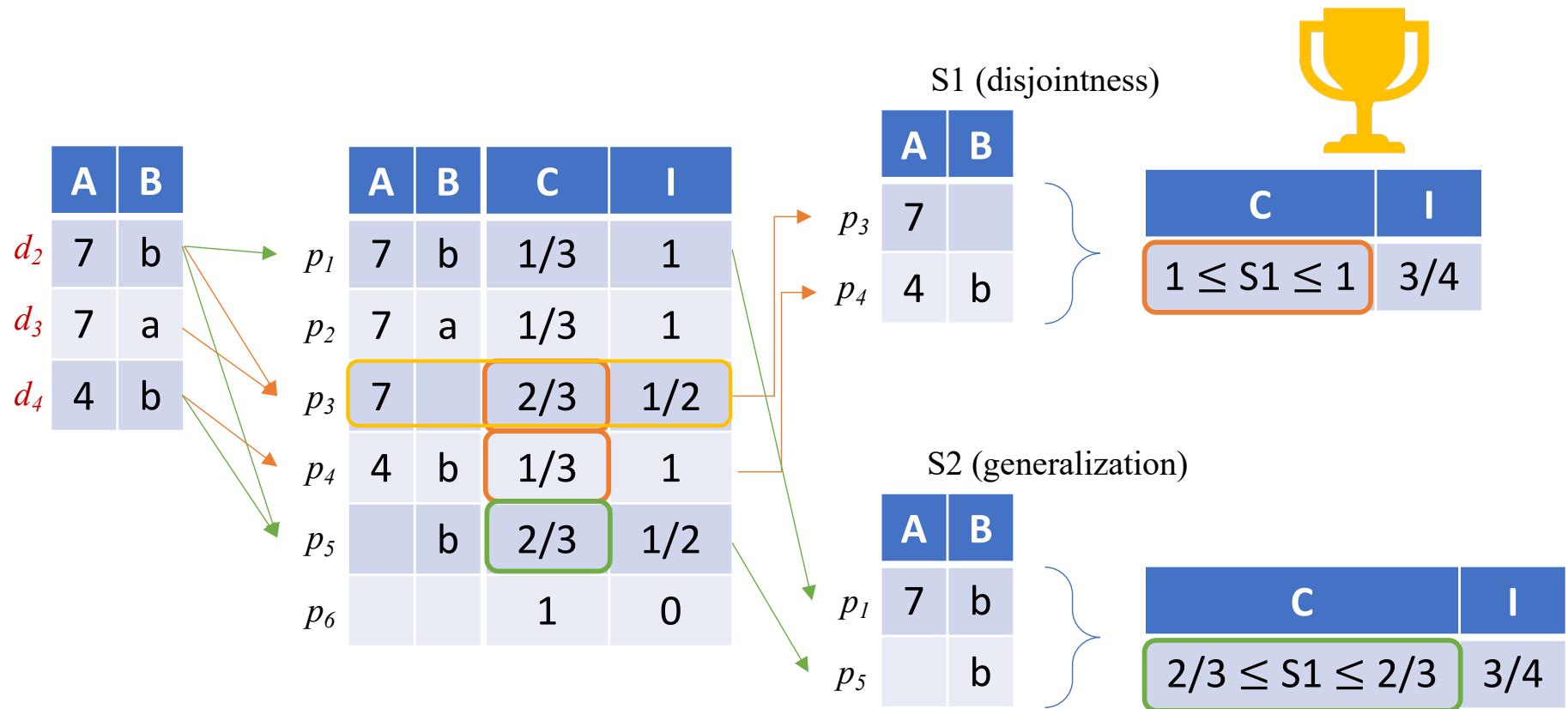
# Summarizing Provenance

- Generating patterns
  - LCA (Lowest Common Ancestor)



# Summarizing Provenance

- Measuring quality and selecting top- $k$  patterns



C: completeness

I: Informativeness

# *Experiments*

# Experiments

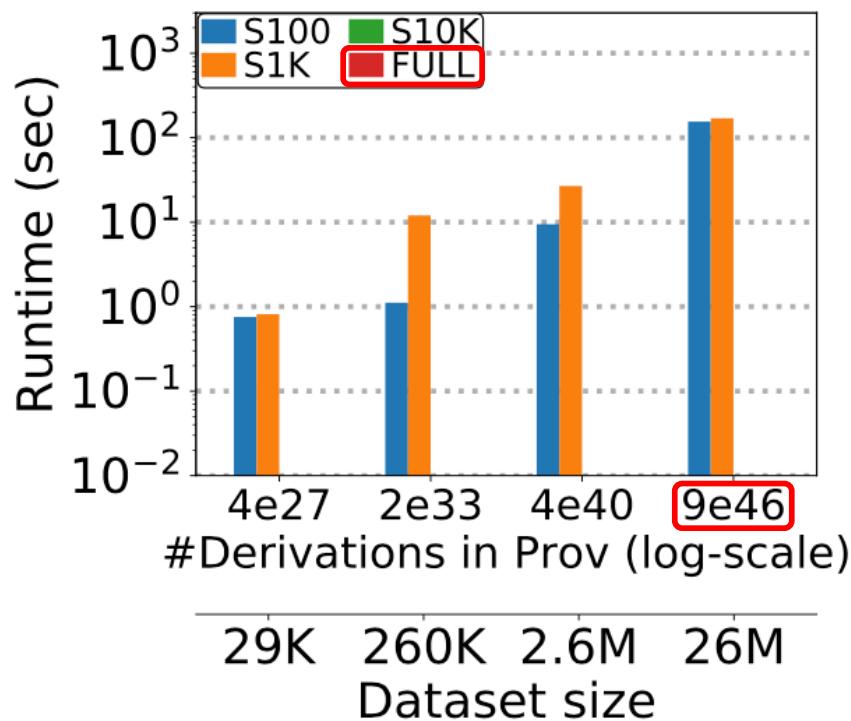
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- Performance of computing summaries
- Quality of summaries
- Comparison with other approaches
- Datasets
  - 4 real-world datasets
  - TPCH
- Queries
  - Single rule through multiple rules
  - Negation and comparisons

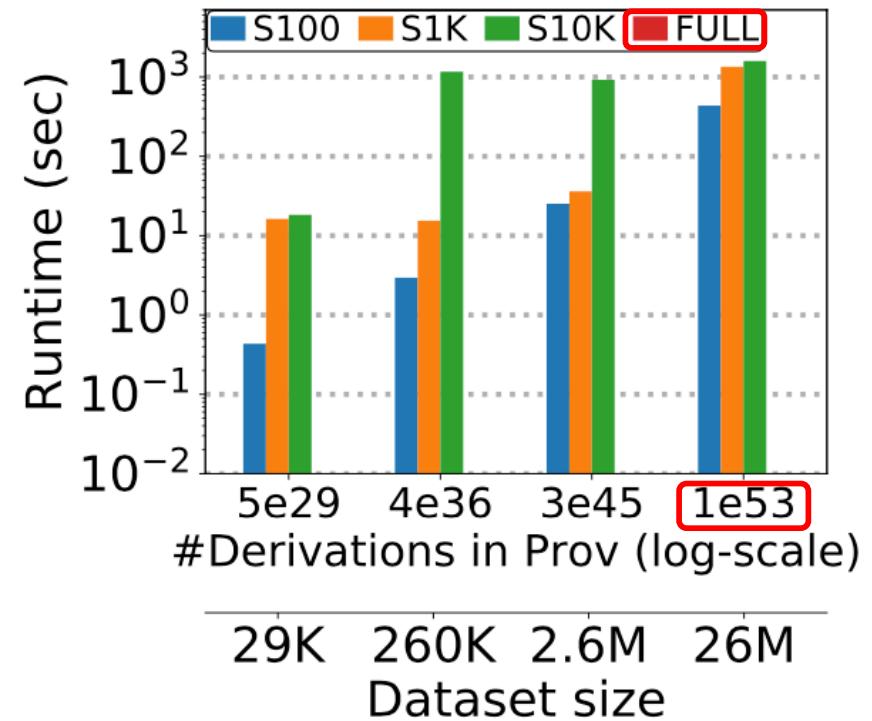
# Experiments

- Computing summaries for  $\sim 10^{50}$  derivations

12 variables + 6 goals + negation

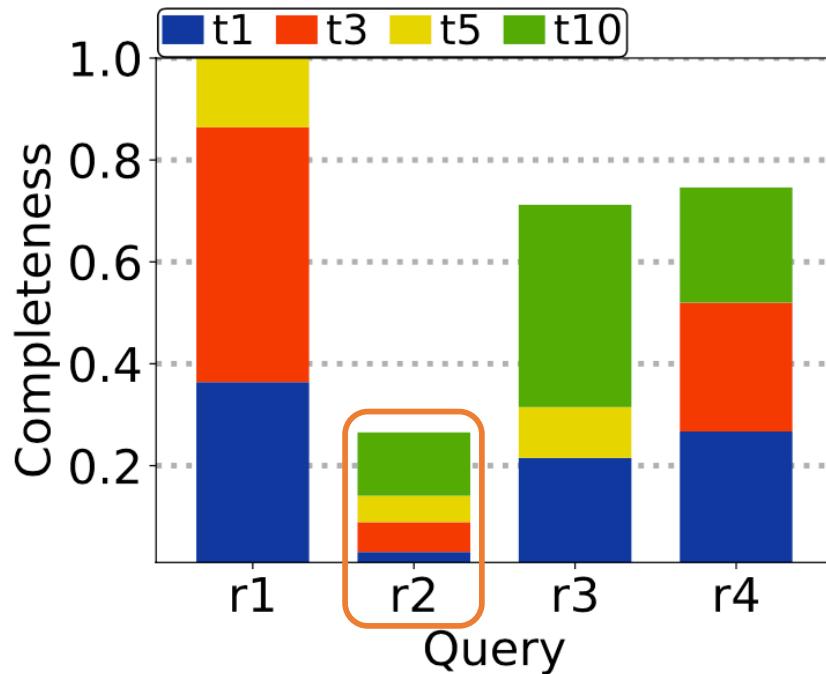


13 variables + 4 goals + multiple rules

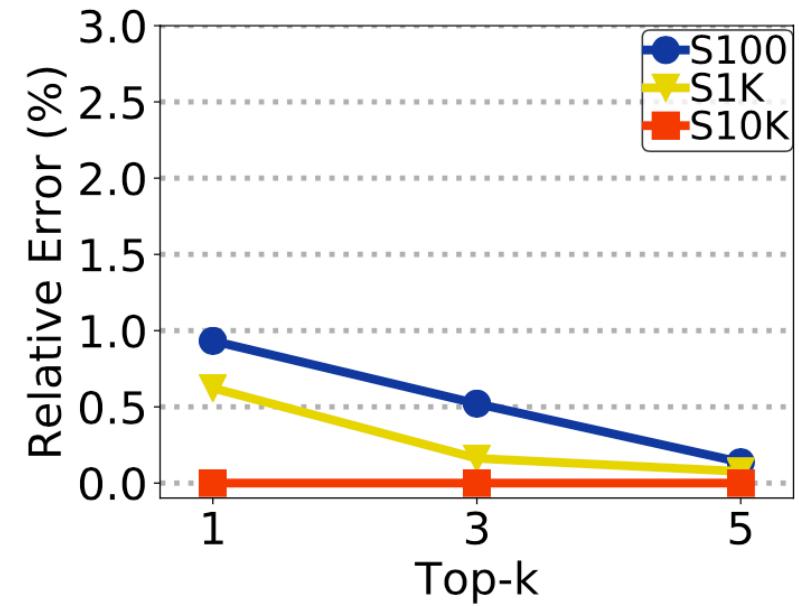


# Experiments

- Generating high-quality summaries



[Completeness comparison]



[Quality metric error caused by sampling]