

# Factorized Machine Learning: Paths and Roadblocks

Arun Kumar



**UC San Diego**  
**JACOBS SCHOOL OF ENGINEERING**  
Computer Science and Engineering

**UC San Diego**  
**HALİCİOĞLU DATA SCIENCE INSTITUTE**

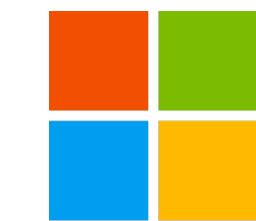
Factorized Databases Workshop

Aug 3, 2022

# Golden Age of ML Analytics



FACEBOOK

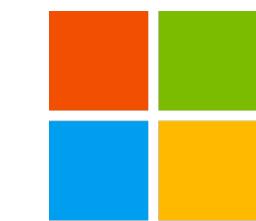


Microsoft

# Golden Age of ML Analytics



FACEBOOK



Microsoft



Insurance



Retail

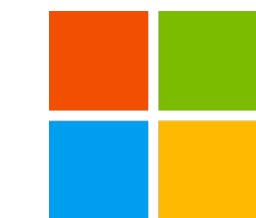


Sciences

# Golden Age of ML Analytics



FACEBOOK



Microsoft



Healthcare



Insurance



Retail



Sciences

\$ 38 billion  
in 2019\*



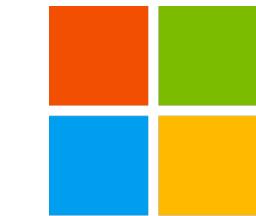
\$ 500 billion  
by 2025\*

\*International Data Corporation

# Golden Age of ML Analytics



FACEBOOK



Healthcare



Insurance



Retail



Sciences

\$ 38 billion  
in 2019\*



\$ 500 billion  
by 2025\*

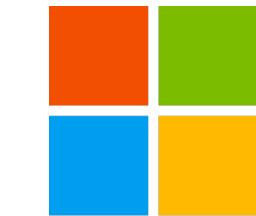


\*International Data Corporation

# Golden Age of ML Analytics



FACEBOOK



Healthcare



Insurance



Retail



Sciences

\$ 38 billion  
in 2019\*



\$ 500 billion  
by 2025\*



PyTorch



\*International Data Corporation

# Golden Age of ML Analytics



FACEBOOK



Healthcare



Insurance



Retail



Sciences

\$ 38 billion  
in 2019\*



\$ 500 billion  
by 2025\*

Still, fundamental efficiency and usability bottlenecks in the  
end-to-end process of building and deploying ML applications

\*International Data Corporation

# My Research

New abstractions, algorithms, and software systems  
to “*democratize*” ML-based data analytics from  
a data management/systems standpoint

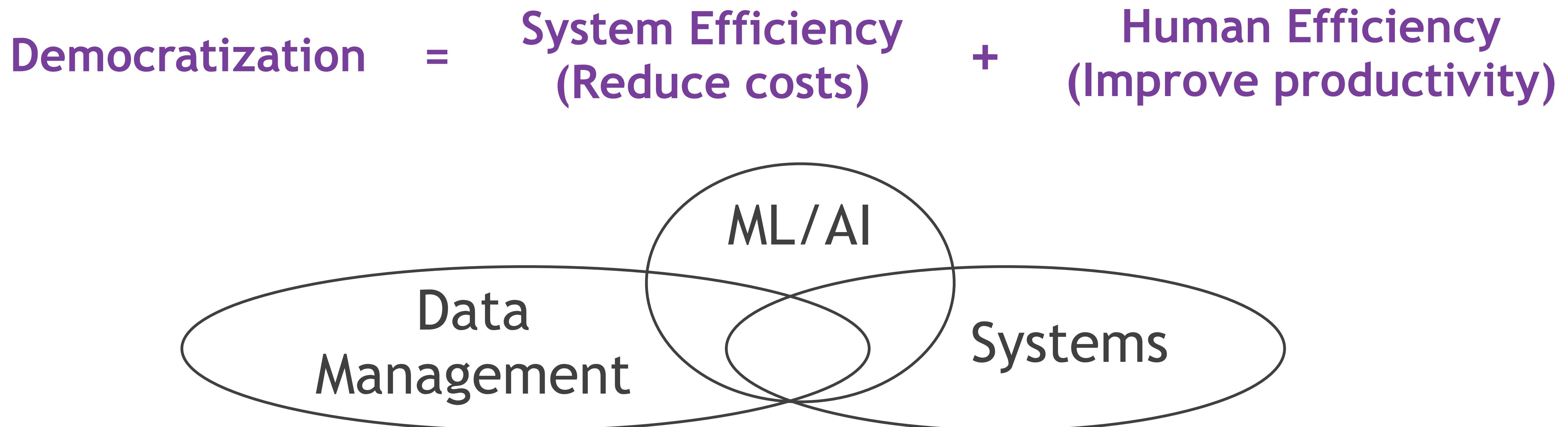
# My Research

New abstractions, algorithms, and software systems  
to “*democratize*” ML-based data analytics from  
a data management/systems standpoint

$$\text{Democratization} = \text{System Efficiency (Reduce costs)} + \text{Human Efficiency (Improve productivity)}$$

# My Research

New abstractions, algorithms, and software systems  
to “*democratize*” ML-based data analytics from  
a data management/systems standpoint



# My Research

New abstractions, algorithms, and software systems  
to “*democratize*” ML-based data analytics from  
a data management/systems standpoint

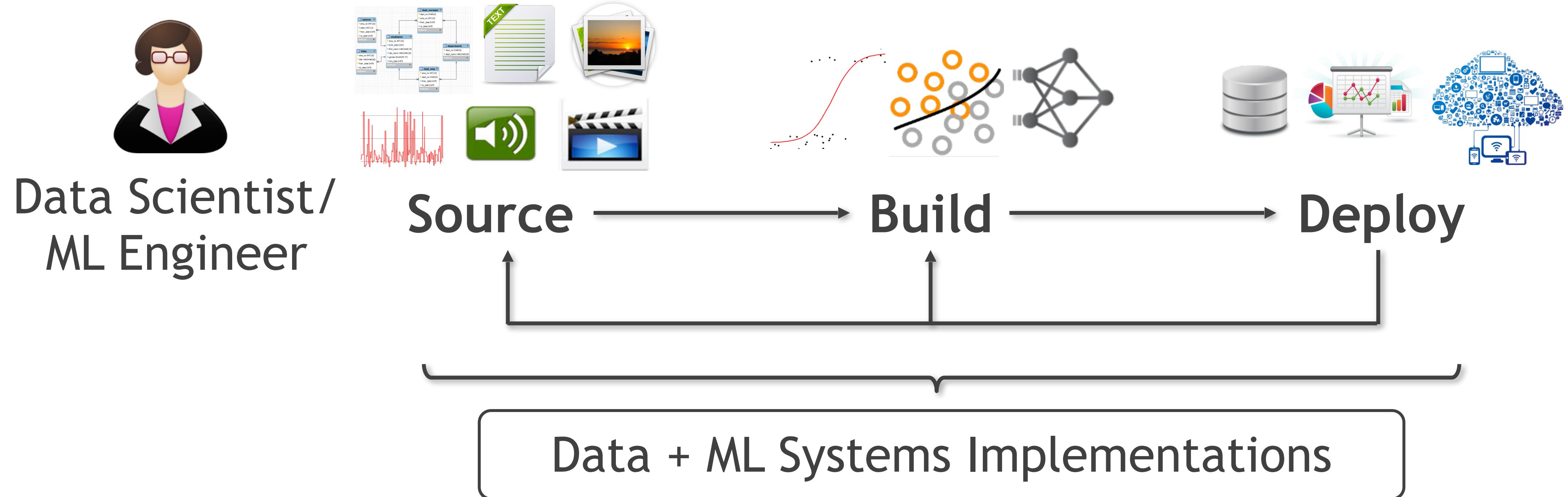
$$\text{Democratization} = \text{System Efficiency} \quad (\text{Reduce costs}) + \text{Human Efficiency} \quad (\text{Improve productivity})$$

Practical and scalable data systems for ML analytics

Inspired by *relational database systems* principles

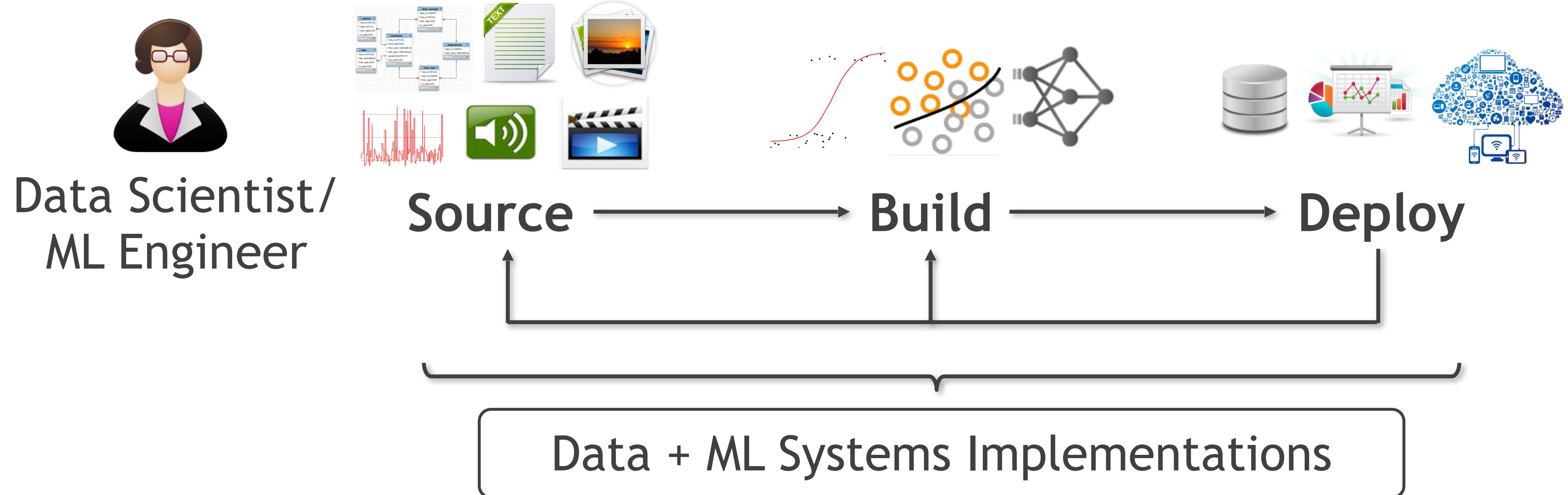
Exploit insights from *learning theory* and *optimization theory*

# End-to-End ML Application Lifecycle



<https://ADALabUCSD.github.io>

# End-to-End ML Application Lifecycle



**Research Approach :** *Abstract* key steps + *Formalize* computation + *Automate* grunt work + *Optimize* execution

<https://ADALabUCSD.github.io>

# Outline

■ Introducing ML over Joins

■ Orion: Factorized ML

■ Morpheus and Extensions

■ Roadblocks and Musings

# Outline

4m

Introducing ML over Joins

4m

Orion: Factorized ML

10m

Morpheus and Extensions

4m

Roadblocks and Musings

# ML after Joins: The Problem

# ML after Joins: The Problem

A fundamental bottleneck in feature engineering on structured data:

Many datasets  
are multi-table



ML toolkits assume  
single-table inputs

# ML after Joins: The Problem

A fundamental bottleneck in feature engineering on structured data:

Many datasets  
are multi-table



ML toolkits assume  
single-table inputs



Materialize  
join output

# ML after Joins: The Problem

A fundamental bottleneck in feature engineering on structured data:

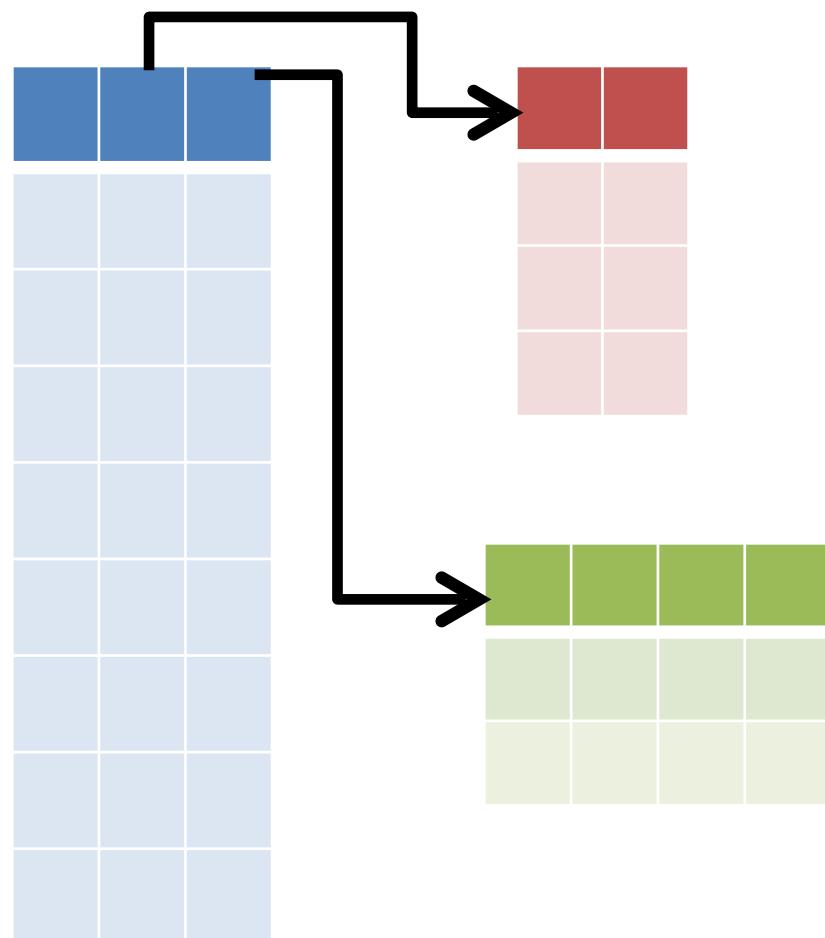
Many datasets  
are multi-table



ML toolkits assume  
single-table inputs



Materialize  
join output



# ML after Joins: The Problem

A fundamental bottleneck in feature engineering on structured data:

Many datasets  
are multi-table       $\longleftrightarrow$       ML toolkits assume  
single-table inputs       $\Rightarrow$       Materialize  
join output



# ML after Joins: The Problem

A fundamental bottleneck in feature engineering on structured data:

Many datasets  
are multi-table

ML toolkits assume  
single-table inputs

Materialize  
join output



# ML after Joins: The Problem

A fundamental bottleneck in feature engineering on structured data:

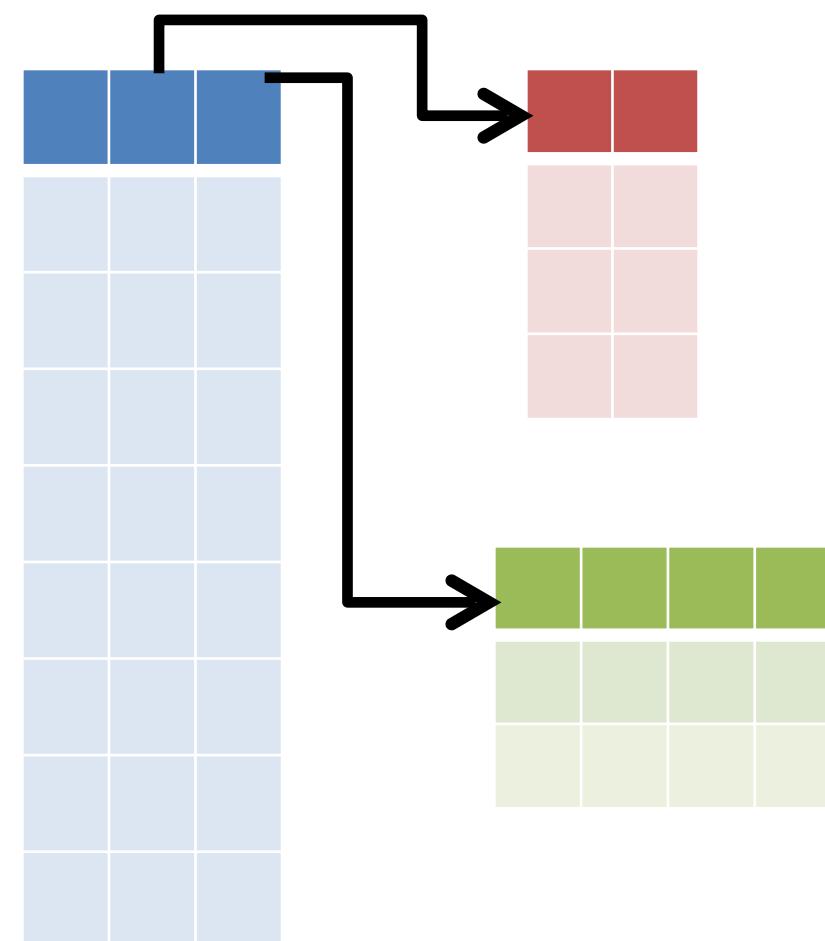
Many datasets  
are multi-table



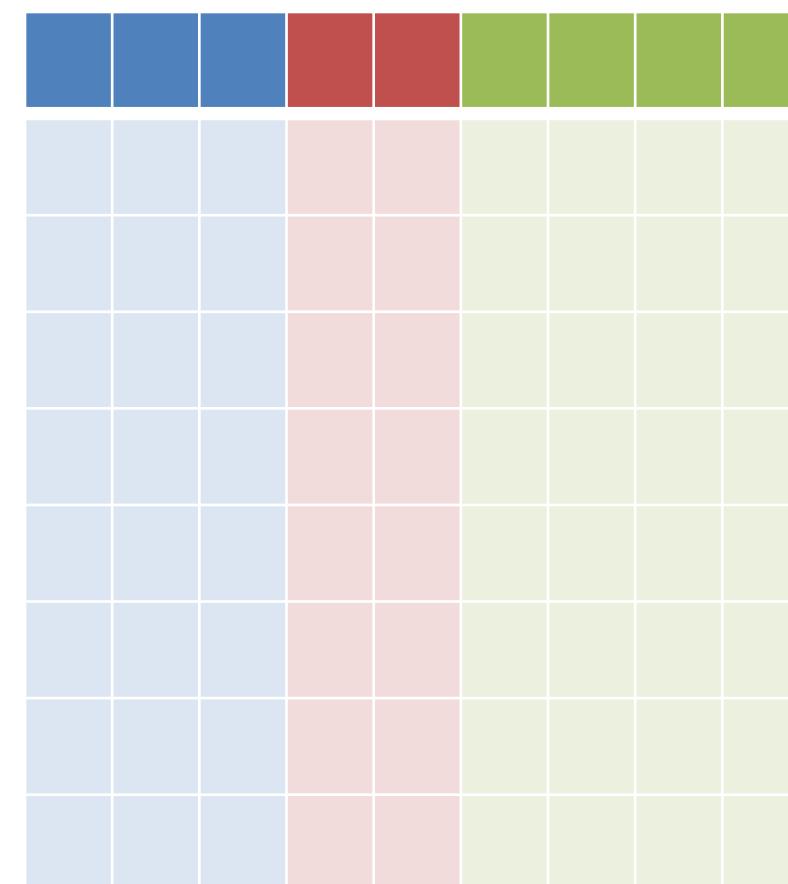
ML toolkits assume  
single-table inputs



Materialize  
join output



Key-Foreign  
Key (KFK) Joins



✗ System efficiency



# ML after Joins: The Problem

A fundamental bottleneck in feature engineering on structured data:

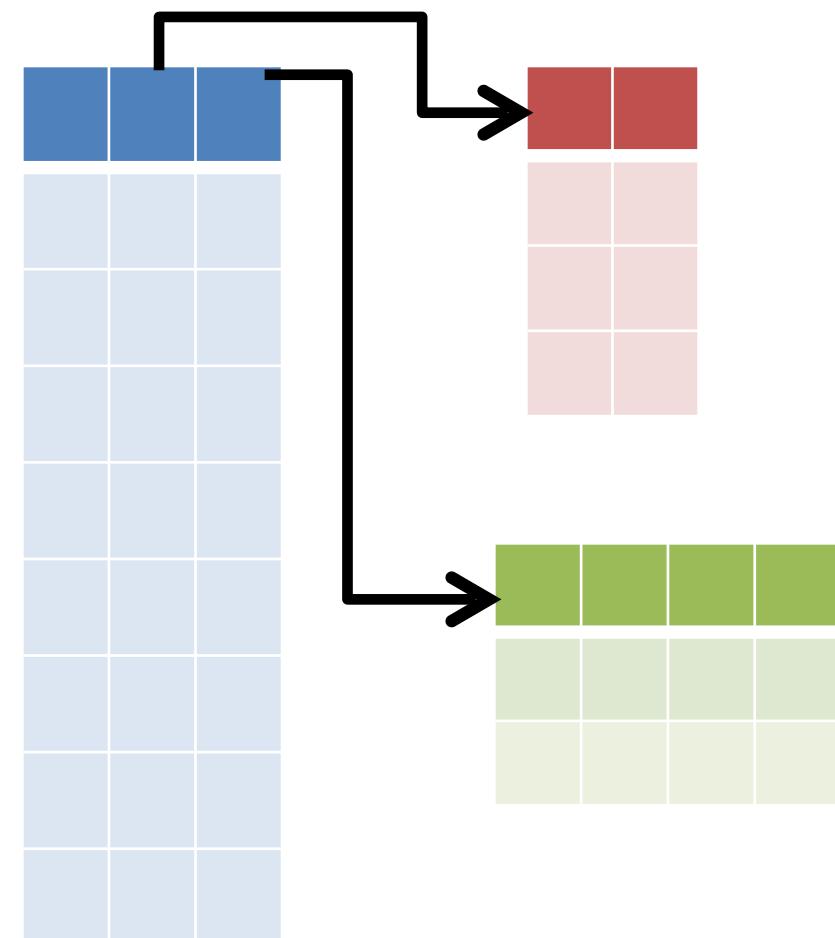
Many datasets  
are multi-table



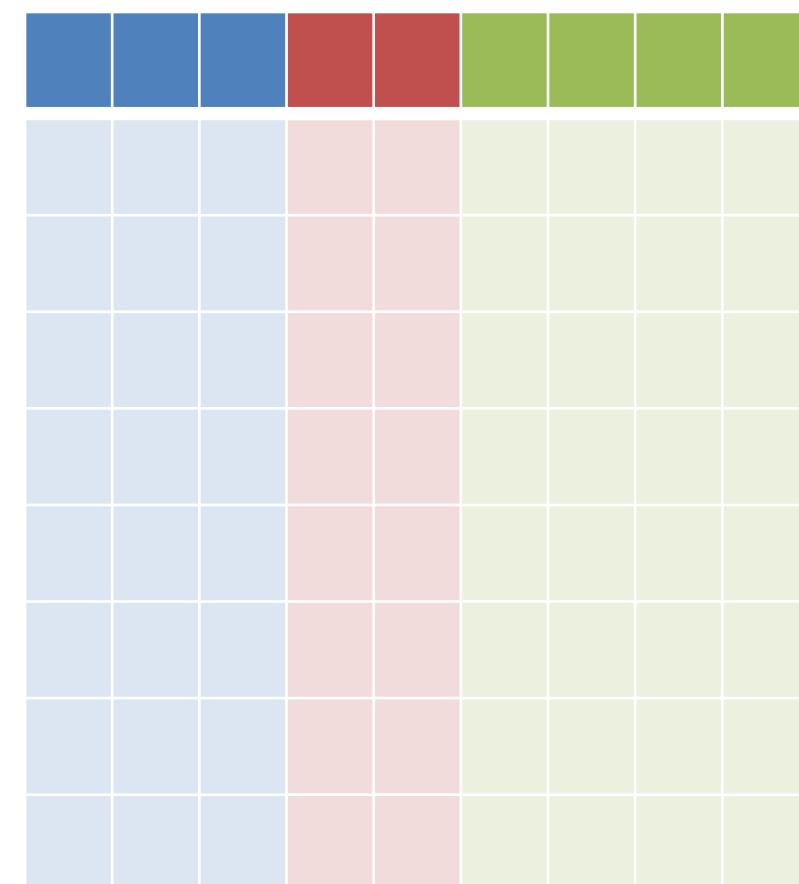
ML toolkits assume  
single-table inputs



Materialize  
join output



Key-Foreign  
Key (KFK) Joins



✗ System efficiency



✗ Human efficiency



# ML after Joins: The Problem

A fundamental bottleneck in feature engineering on structured data:

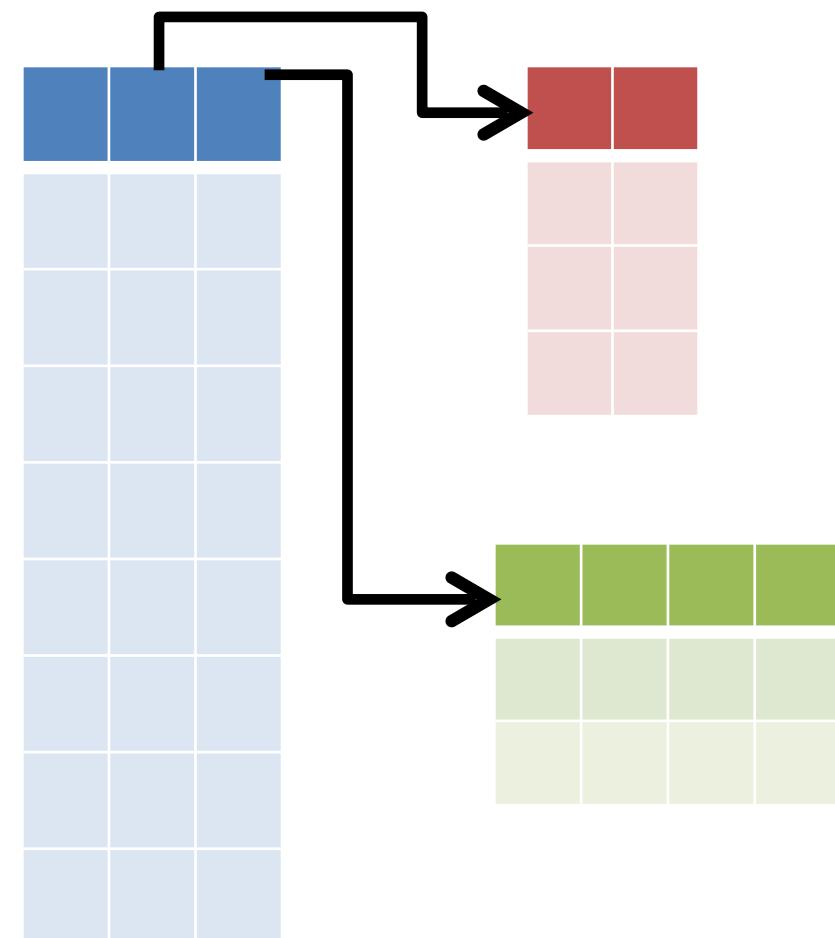
Many datasets  
are multi-table



ML toolkits assume  
single-table inputs



Materialize  
join output



Key-Foreign  
Key (KFK) Joins



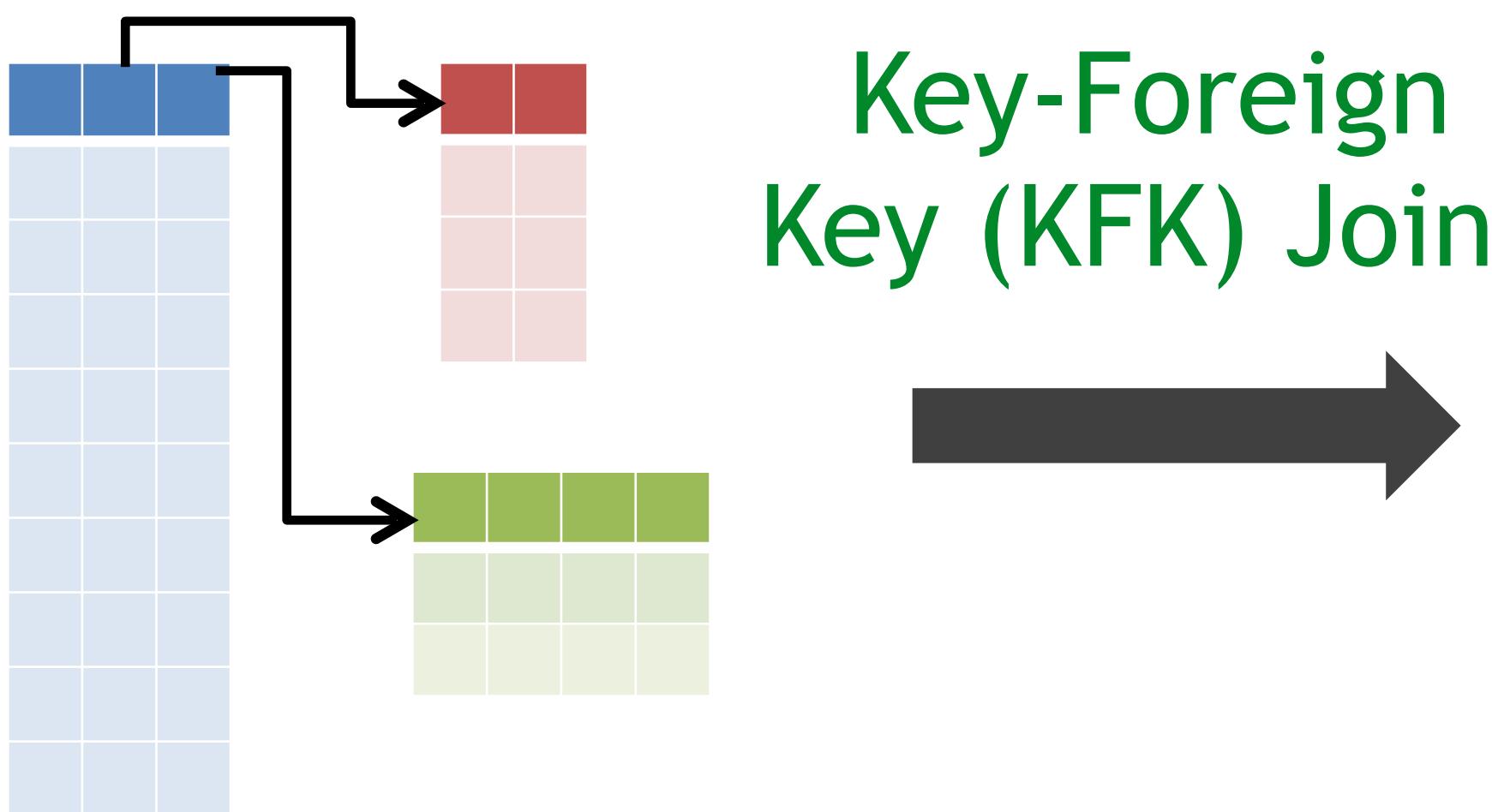
✗ System efficiency



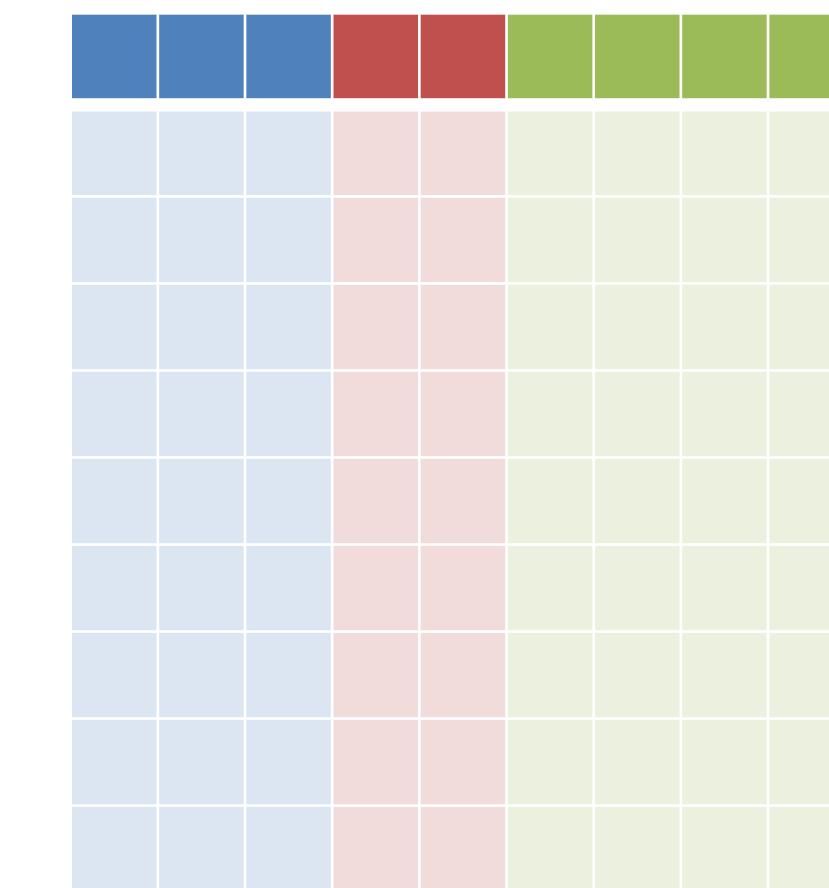
✗ Human efficiency



# ML over Joins: Overview



Key-Foreign  
Key (KFK) Joins



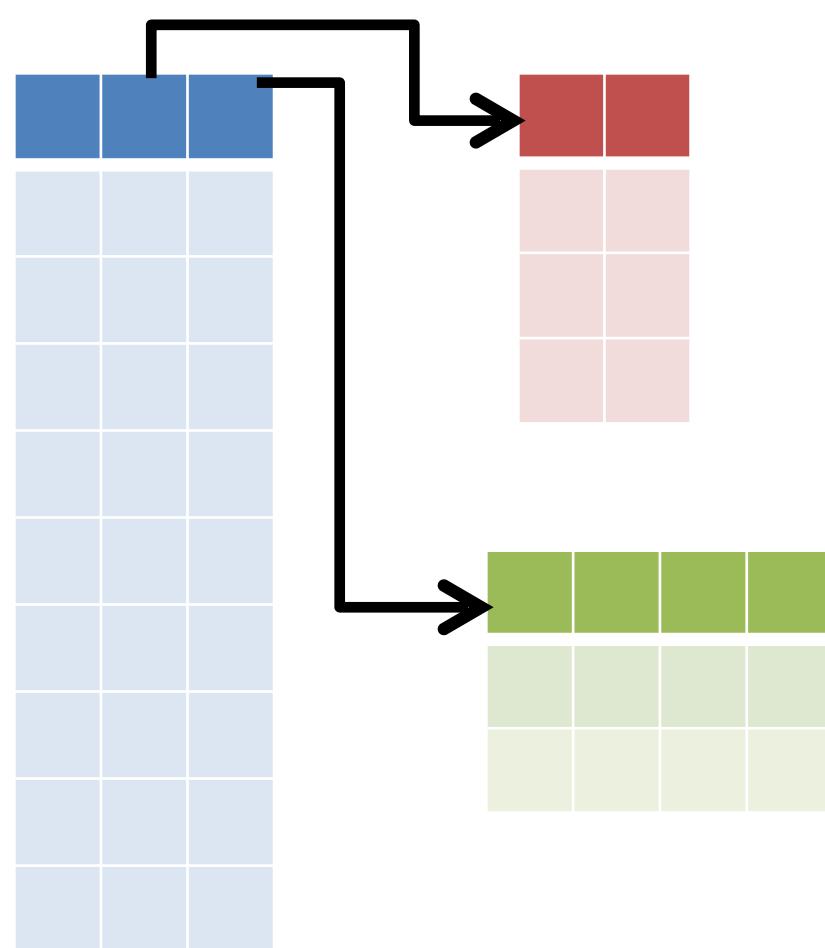
✖ System efficiency

✖ Human efficiency

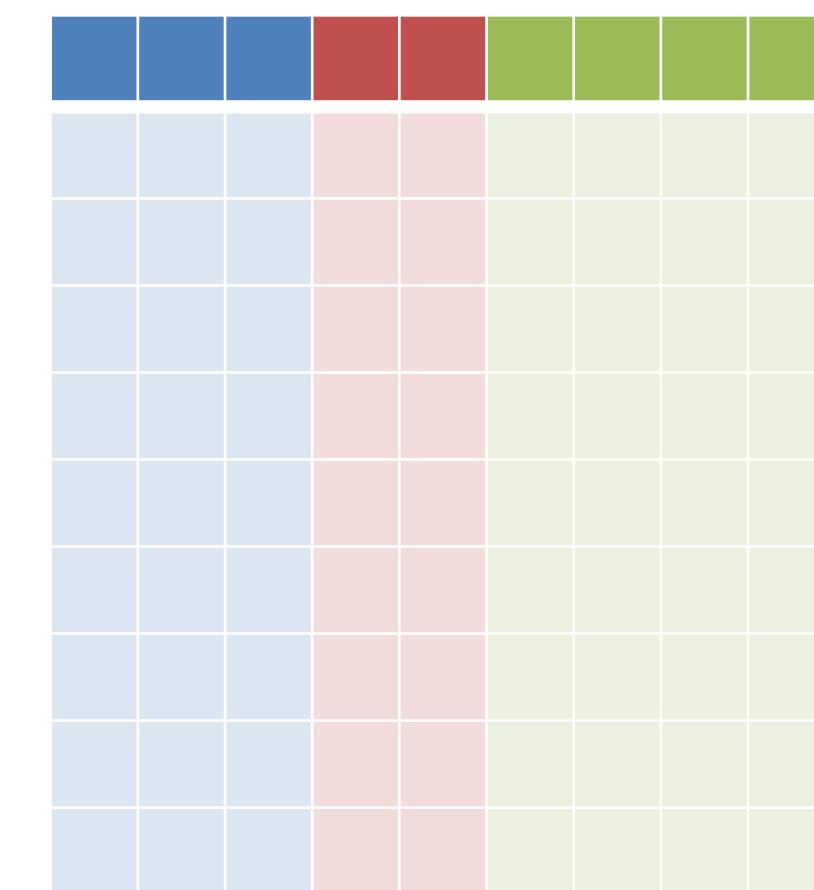
# ML over Joins: Overview

Avoid Joins Physically

ORION, MORPHEUS



Key-Foreign  
Key (KFK) Joins



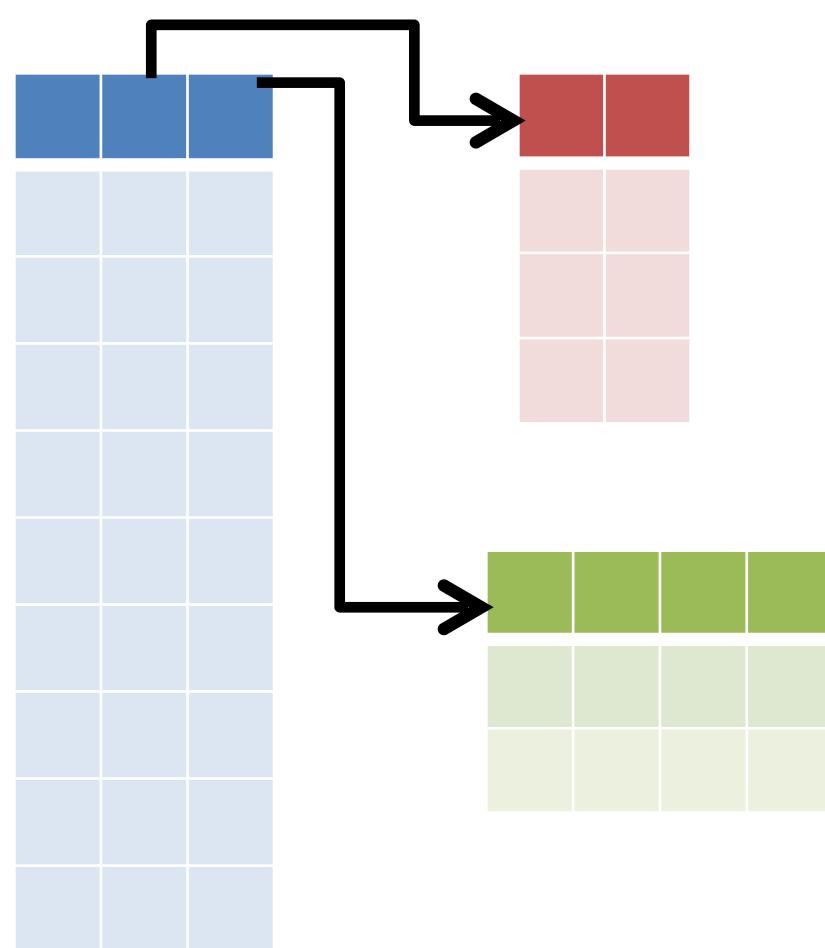
✗ System efficiency

✗ Human efficiency

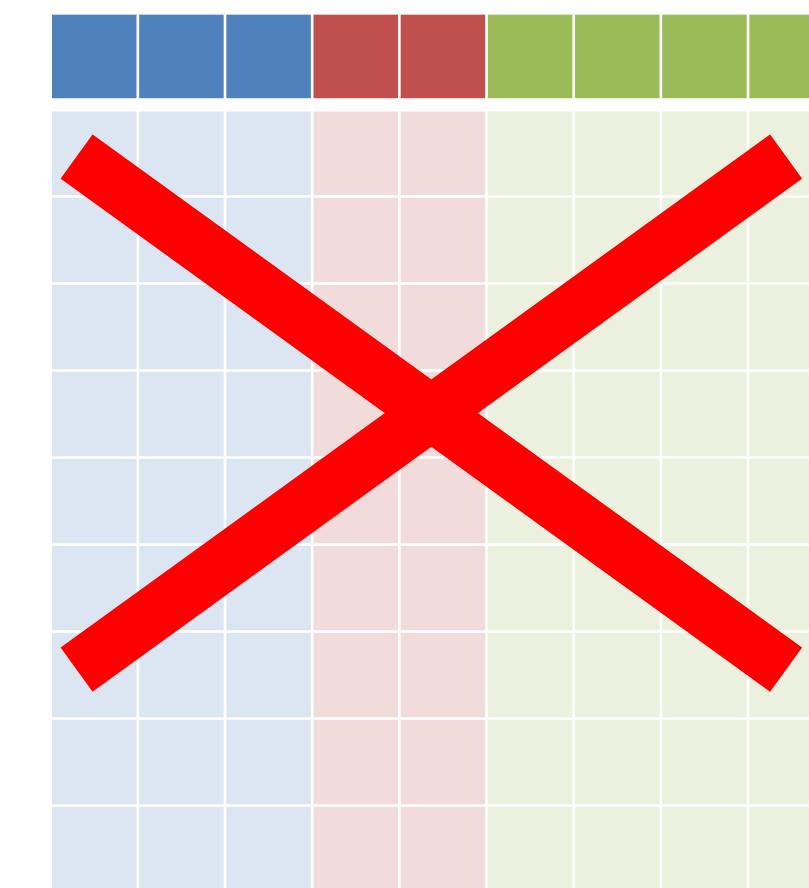
# ML over Joins: Overview

Avoid Joins Physically

ORION, MORPHEUS



Key-Foreign  
Key (KFK) Joins



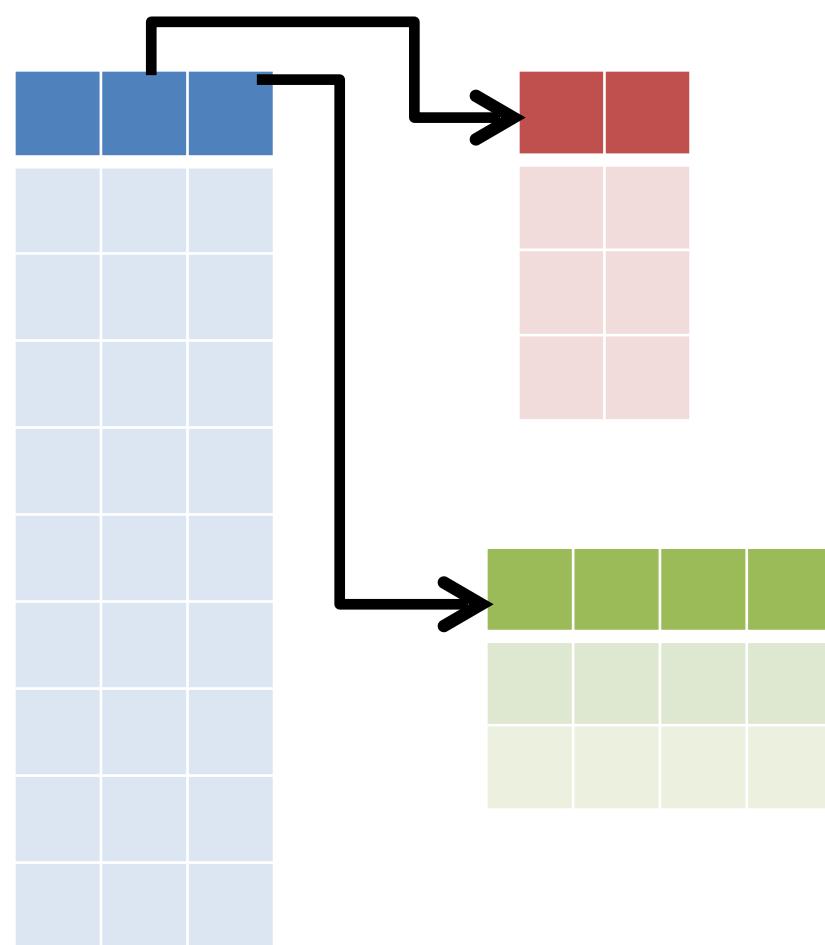
✗ System efficiency

✗ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

ORION, MORPHEUS



✖ System efficiency

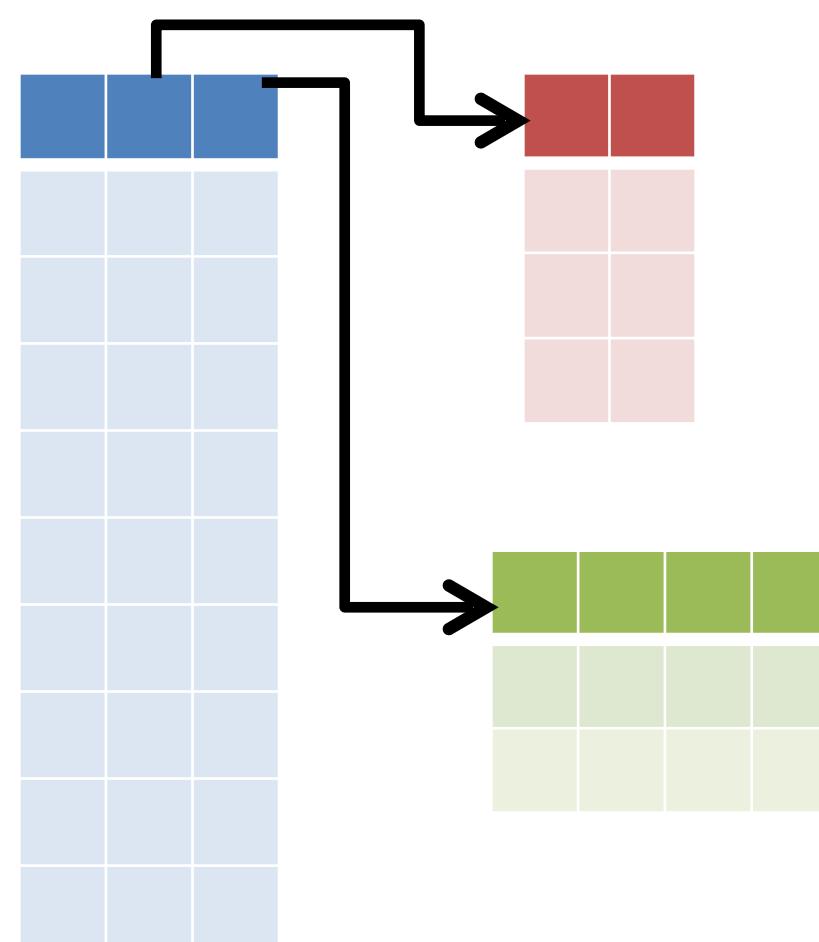
✖ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

ORION, MORPHEUS

*Runs faster,  
same accuracy*



✖ System efficiency

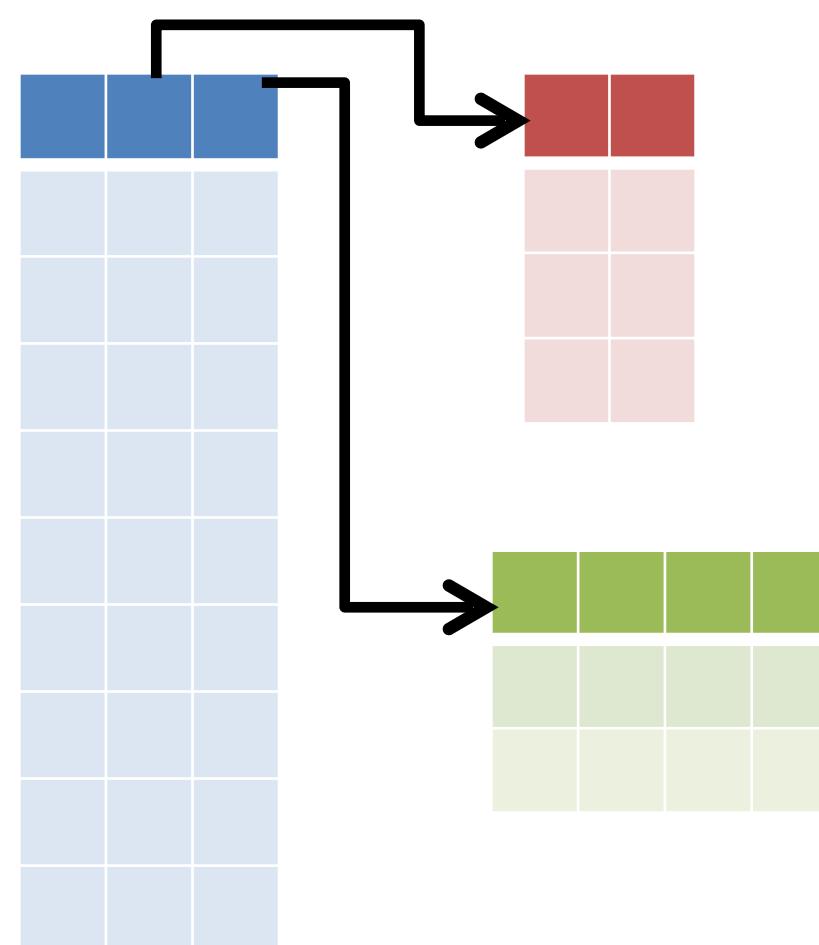
✖ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

ORION, MORPHEUS

*Runs faster,  
same accuracy*



✖ System efficiency

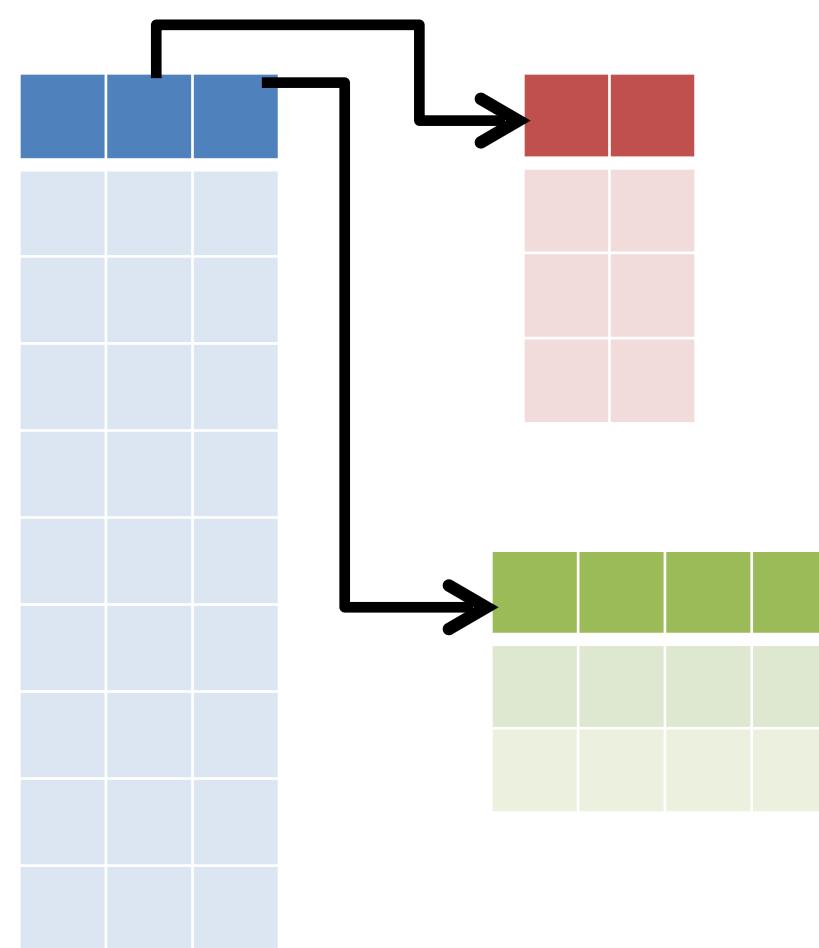
+ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

ORION, MORPHEUS

*Runs faster,  
same accuracy*



+ System efficiency

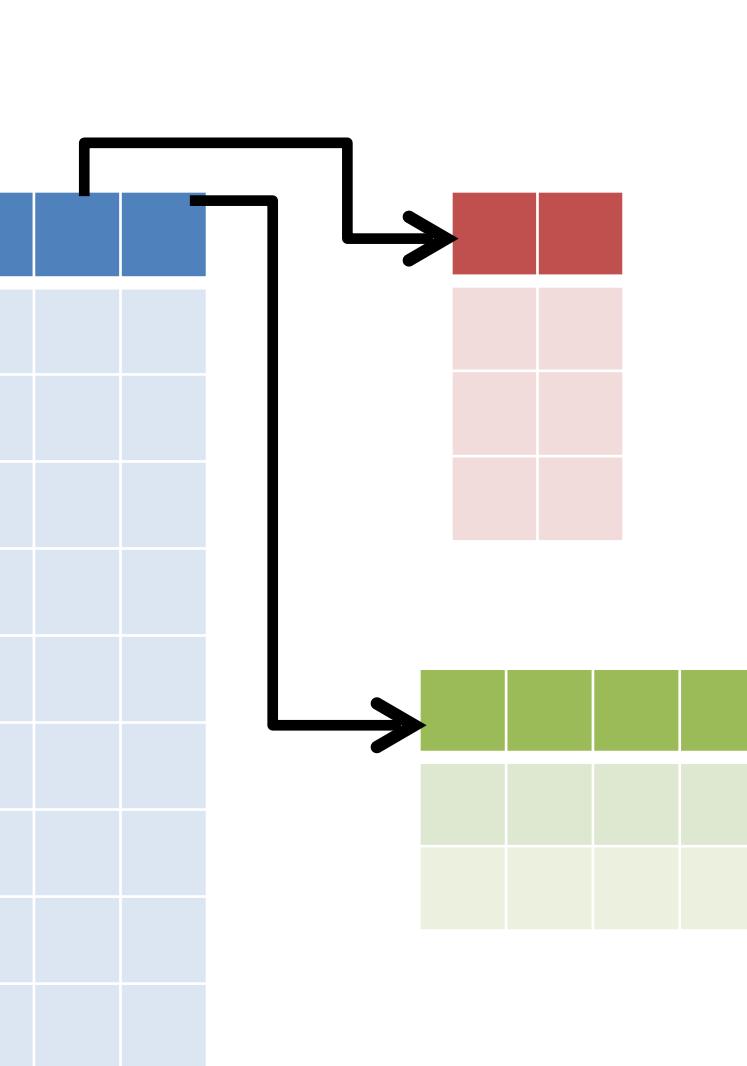
+ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

ORION, MORPHEUS

*Runs faster,  
same accuracy*



Avoid Joins Logically

HAMLET, HAMLET++

+ System efficiency

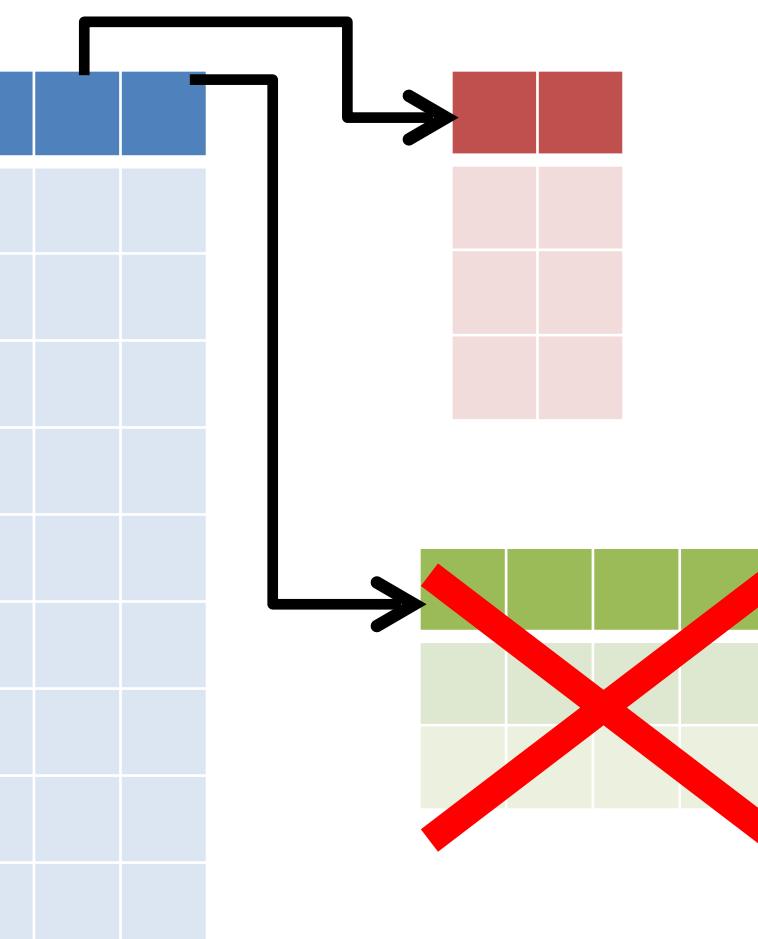
+ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

ORION, MORPHEUS

*Runs faster,  
same accuracy*



Avoid Joins Logically

HAMLET, HAMLET++

+ System efficiency

+ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

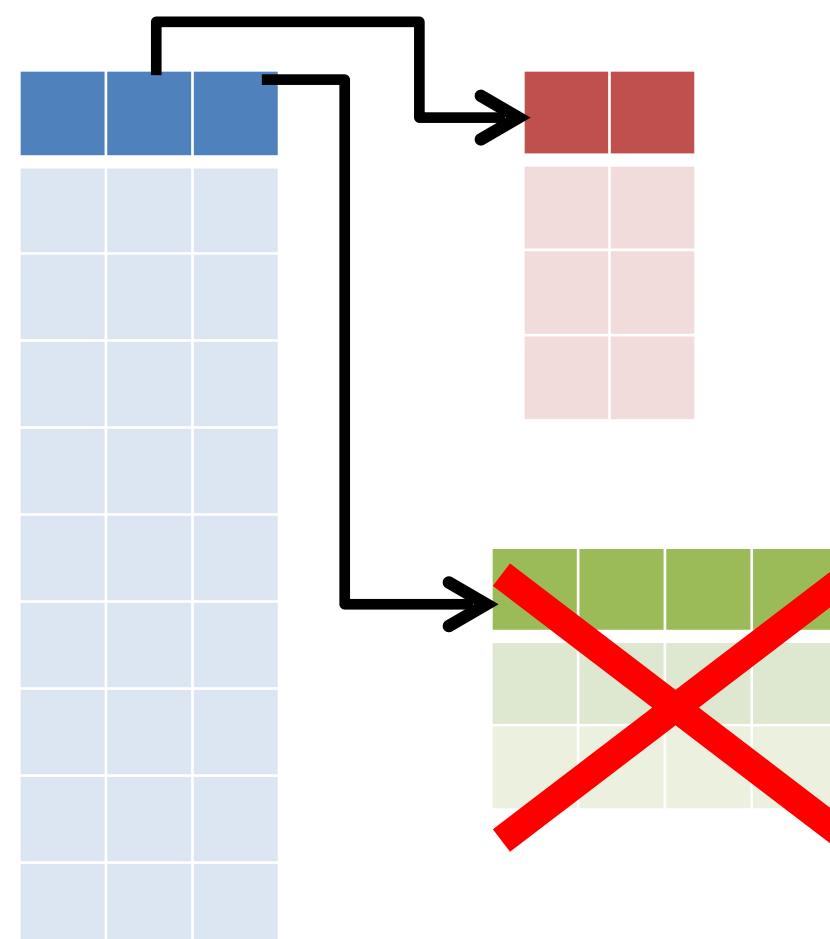
ORION, MORPHEUS

*Runs faster,  
same accuracy*

Avoid Joins Logically

HAMLET, HAMLET++

*Even faster,  
similar accuracy*



+ System efficiency

+ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

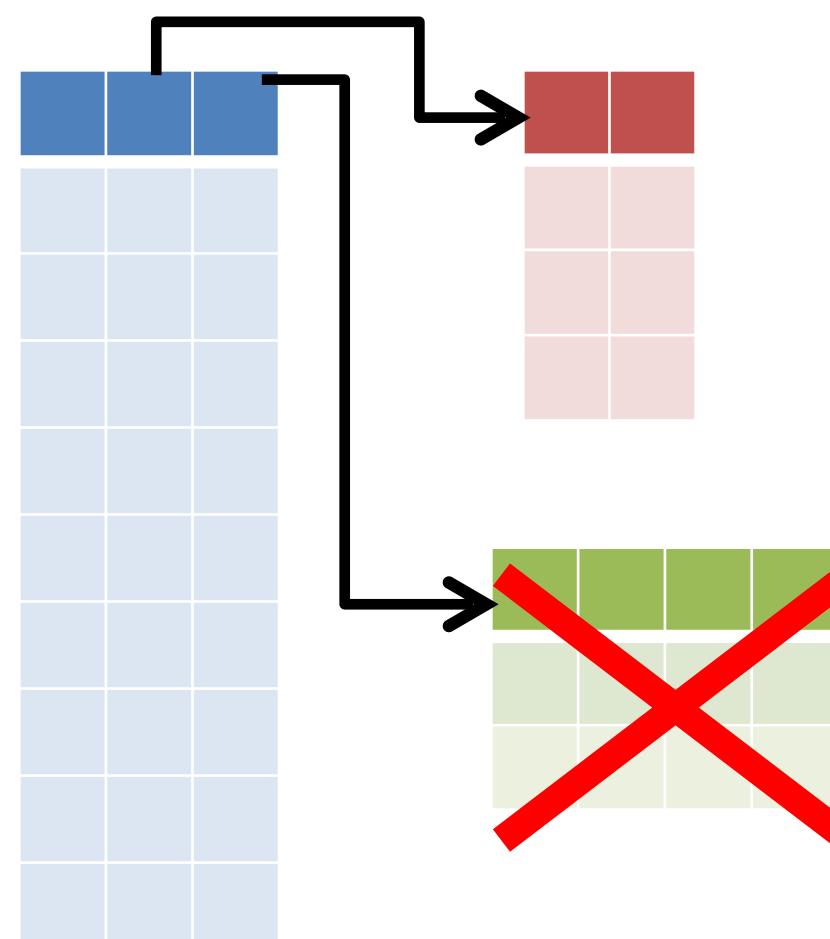
ORION, MORPHEUS

*Runs faster,  
same accuracy*

Avoid Joins Logically

HAMLET, HAMLET++

*Even faster,  
similar accuracy*



++ System efficiency

++ Human efficiency

# ML over Joins: Overview

Avoid Joins Physically

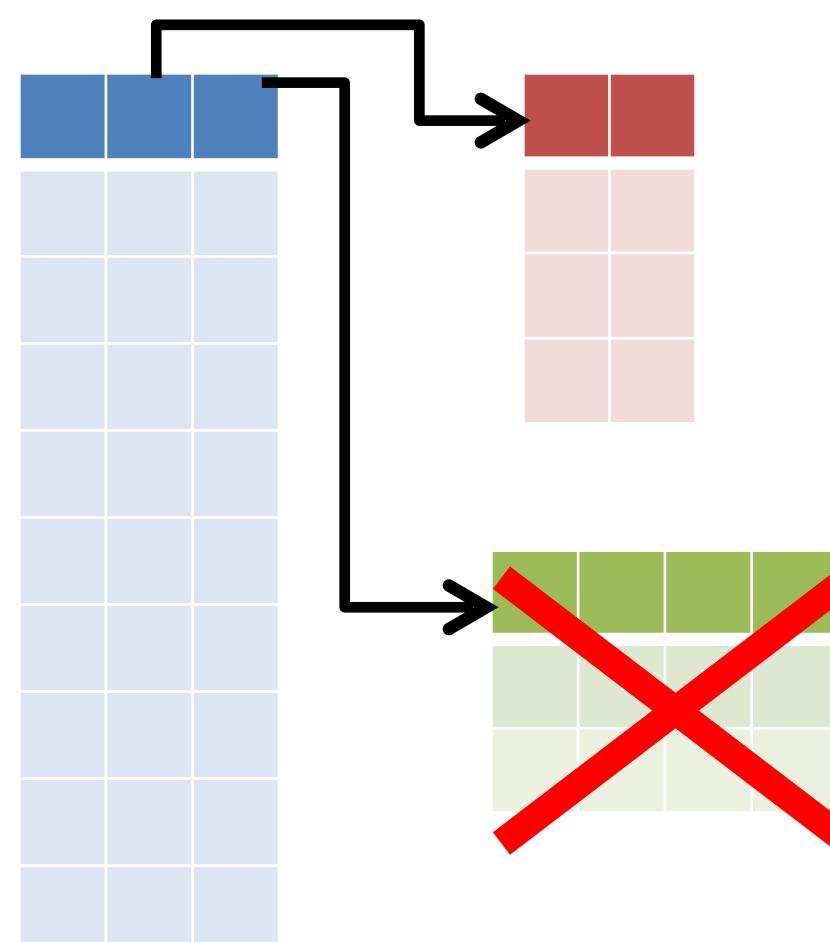
**ORION, MORPHEUS**

*Runs faster,  
same accuracy*

Avoid Joins Logically

**HAMLET, HAMLET++**

*Even faster,  
similar accuracy*



**++ System efficiency**

**++ Human efficiency**

# Running Example for ML over Joins

ML Task: Classify if a customer will *churn* or not



CID	Customers				EmplID	Foreign Key			Employers		
	Churn?	Gender	Age			EmplID	EmplID	State	Revenue		
1	Yes	Female	33	AMZN	AMZN	AMZN	WA	136b			
2	No	Male	51	GOOG	GOOG	GOOG	CA	89b			
3	Yes	Other	46	GOOG	GOOG	MSFT	WA	85b			
4	No	Female	27	MSFT	MSFT	...	...	...			
...	...	...	...	...	...	...	...	...			

# Running Example for ML over Joins

ML Task: Classify if a customer will *churn* or not



CID	Customers				EmplID	Foreign Key			Employers		
	Churn?	Gender	Age			EmplID	EmplID	State	Revenue		
1	Yes	Female	33	AMZN	AMZN	AMZN	WA	136b			
2	No	Male	51	GOOG	GOOG	GOOG	CA	89b			
3	Yes	Other	46	GOOG	GOOG	MSFT	WA	85b			
4	No	Female	27	MSFT	MSFT	...	...	...			
...	...	...	...	...	...	...	...	...			

More features!

# Running Example for ML over Joins

ML Task: Classify if a customer will *churn* or not



Customers					Foreign Key	Employers		
CID	Churn?	Gender	Age	EmplID	EmplID	State	Revenue	
1	Yes	Female	33	AMZN	AMZN	WA	136b	
2	No	Male	51	GOOG	GOOG	CA	89b	
3	Yes	Other	46	GOOG	MSFT	WA	85b	
4	No	Female	27	MSFT	...	...	...	
...	...	...	...	...	More features!			

More joins possible, e.g., with neighborhood data, weather data, etc.

*Materializing such joins can blow up the data, even by over 10x!*

# Outline

4m

Introducing ML over Joins

4m

Orion: Factorized ML

10m

Morpheus and Extensions

4m

Roadblocks and Musings

# ORION: Factorized ML

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

**Focus:**

Generalized Linear Models (GLMs) solved  
using (batch) gradient descent methods

$$\mathbf{X} \equiv [\mathbf{X}_C \ \mathbf{X}_E]$$

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

**Focus:**

Generalized Linear Models (GLMs) solved  
using (batch) gradient descent methods

$$\nabla L(\mathbf{w}) = \sum_{i=1}^N g(\mathbf{w}^T \mathbf{x}_i, y_i) \mathbf{x}_i \quad \mathbf{X} \equiv [\mathbf{X}_C \mathbf{X}_E]$$

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

**Focus:**

Generalized Linear Models (GLMs) solved  
using (batch) gradient descent methods

$$\nabla L(\mathbf{w}) = \sum_{i=1}^N g(\mathbf{w}^T \mathbf{x}_i, y_i) \mathbf{x}_i \quad \mathbf{X} \equiv [\mathbf{X}_C \mathbf{X}_E]$$

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

**Focus:**

Generalized Linear Models (GLMs) solved  
using (batch) gradient descent methods

$$\nabla L(\mathbf{w}) = \sum_{i=1}^N g(\mathbf{w}^T \mathbf{x}_i, y_i) \mathbf{x}_i \quad \mathbf{X} \equiv [\mathbf{X}_C \mathbf{X}_E]$$

$$\mathbf{w}^T \mathbf{x} = [\mathbf{w}_C^T \mathbf{w}_E^T] \begin{bmatrix} \mathbf{x}_C \\ \mathbf{x}_E \end{bmatrix} = \mathbf{w}_C^T \mathbf{x}_C + \mathbf{w}_E^T \mathbf{x}_E$$

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

**Focus:**

Generalized Linear Models (GLMs) solved  
using (batch) gradient descent methods

$$\nabla L(\mathbf{w}) = \sum_{i=1}^N g(\mathbf{w}^T \mathbf{x}_i, y_i) \mathbf{x}_i \quad \mathbf{X} \equiv [\mathbf{X}_C \mathbf{X}_E]$$

$$\mathbf{w}^T \mathbf{x} = [\mathbf{w}_C^T \mathbf{w}_E^T] \begin{bmatrix} \mathbf{x}_C \\ \mathbf{x}_E \end{bmatrix} = \mathbf{w}_C^T \mathbf{x}_C + \boxed{\mathbf{w}_E^T \mathbf{x}_E}$$

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

**Focus:**

Generalized Linear Models (GLMs) solved  
using (batch) gradient descent methods

$$\nabla L(\mathbf{w}) = \sum_{i=1}^N g(\mathbf{w}^T \mathbf{x}_i, y_i) \mathbf{x}_i \quad \mathbf{X} \equiv [\mathbf{X}_C \mathbf{X}_E]$$

$$\mathbf{w}^T \mathbf{x} = [\mathbf{w}_C^T \mathbf{w}_E^T] \begin{bmatrix} \mathbf{x}_C \\ \mathbf{x}_E \end{bmatrix} = \mathbf{w}_C^T \mathbf{x}_C + \mathbf{w}_E^T \mathbf{x}_E$$

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

**Focus:**

Generalized Linear Models (GLMs) solved  
using (batch) gradient descent methods

$$\nabla L(\mathbf{w}) = \sum_{i=1}^N g(\mathbf{w}^T \mathbf{x}_i, y_i) \mathbf{x}_i \quad \mathbf{X} \equiv [\mathbf{X}_C \mathbf{X}_E]$$

$$\mathbf{w}^T \mathbf{x} = [\mathbf{w}_C^T \mathbf{w}_E^T] \begin{bmatrix} \mathbf{x}_C \\ \mathbf{x}_E \end{bmatrix} = \mathbf{w}_C^T \mathbf{x}_C + \mathbf{w}_E^T \mathbf{x}_E$$

1 full iteration requires 2 scans of Employers, 1 scan of Customers

# ORION: Factorized ML

**Insight:** Decompose ML computations and push them down through joins

**Focus:**

Generalized Linear Models (GLMs) solved  
using (batch) gradient descent methods

$$\nabla L(\mathbf{w}) = \sum_{i=1}^N g(\mathbf{w}^T \mathbf{x}_i, y_i) \mathbf{x}_i \quad \mathbf{X} \equiv [\mathbf{X}_C \mathbf{X}_E]$$

$$\mathbf{w}^T \mathbf{x} = [\mathbf{w}_C^T \mathbf{w}_E^T] \begin{bmatrix} \mathbf{x}_C \\ \mathbf{x}_E \end{bmatrix} = \mathbf{w}_C^T \mathbf{x}_C + \mathbf{w}_E^T \mathbf{x}_E$$

1 full iteration requires 2 scans of Employers, 1 scan of Customers

**Challenges Tackled:** Scalability; developability

# ORION: Implementations

*Learning Generalized Linear Models over Normalized Data. SIGMOD 2015*  
*Demonstration of Santoku: Optimizing Machine Learning over Normalized Data. VLDB 2015*

# ORION: Implementations

Prototyped on PostgreSQL with UDAFs (MADlib style)

Distributed prototype with MapReduce on Hive & Spark (MLlib style)

Extended to Naive Bayes, k-means clustering, decision trees as R package

*Learning Generalized Linear Models over Normalized Data.* **SIGMOD 2015**

*Demonstration of Santoku: Optimizing Machine Learning over Normalized Data.* **VLDB 2015**

# ORION: Implementations

Prototyped on PostgreSQL with UDAFs (MADlib style)

Distributed prototype with MapReduce on Hive & Spark (MLlib style)

Extended to Naive Bayes, k-means clustering, decision trees as R package

Explored for  
production use cases:



Microsoft  
(Web security)



(Retail)



(Ads)

*Learning Generalized Linear Models over Normalized Data. SIGMOD 2015*  
*Demonstration of Santoku: Optimizing Machine Learning over Normalized Data. VLDB 2015*

***Q: Can we avoid manual rewriting of each ML algorithm  
and “automate” factorized ML on top of ML tools?***

# Outline

4m

Introducing ML over Joins

4m

Orion: Factorized ML

10m

Morpheus and Extensions

4m

Roadblocks and Musings

# MORPHEUS: Generalizing ORION

# MORPHEUS: Generalizing ORION

**Goal:** *Automate* factorized ML to many ML algorithms in a unified way

# MORPHEUS: Generalizing ORION

**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

# MORPHEUS: Generalizing ORION

**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

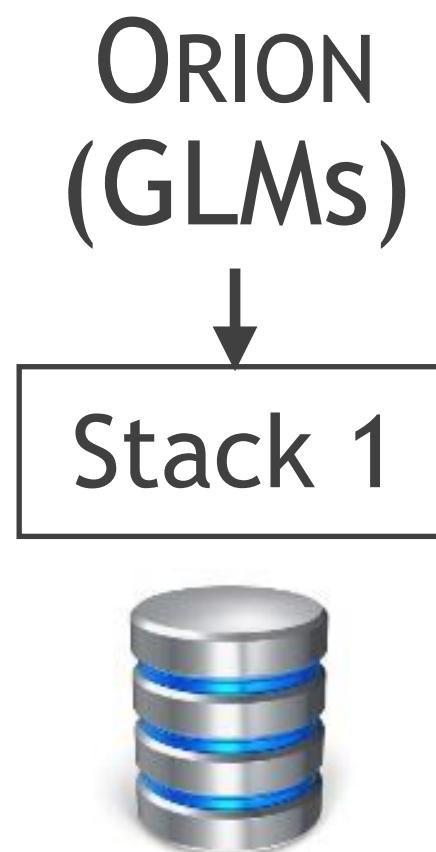
## Factorized ML: Prior Work

# MORPHEUS: Generalizing ORION

**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

## Factorized ML: Prior Work

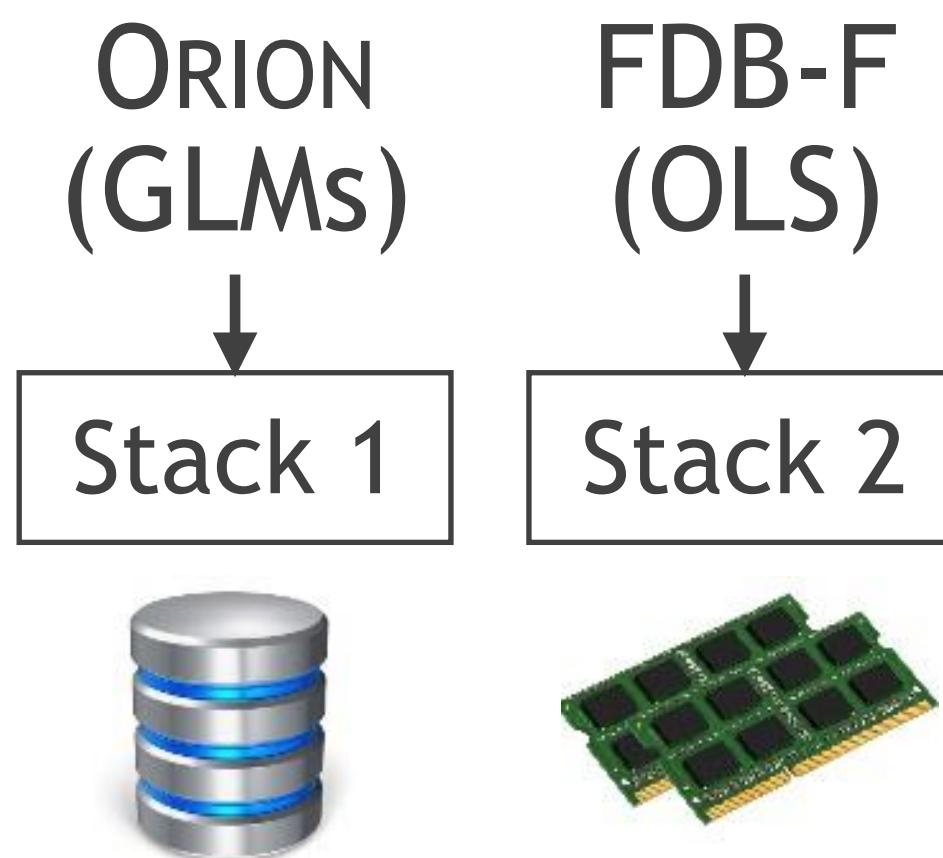


# MORPHEUS: Generalizing ORION

**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

## Factorized ML: Prior Work

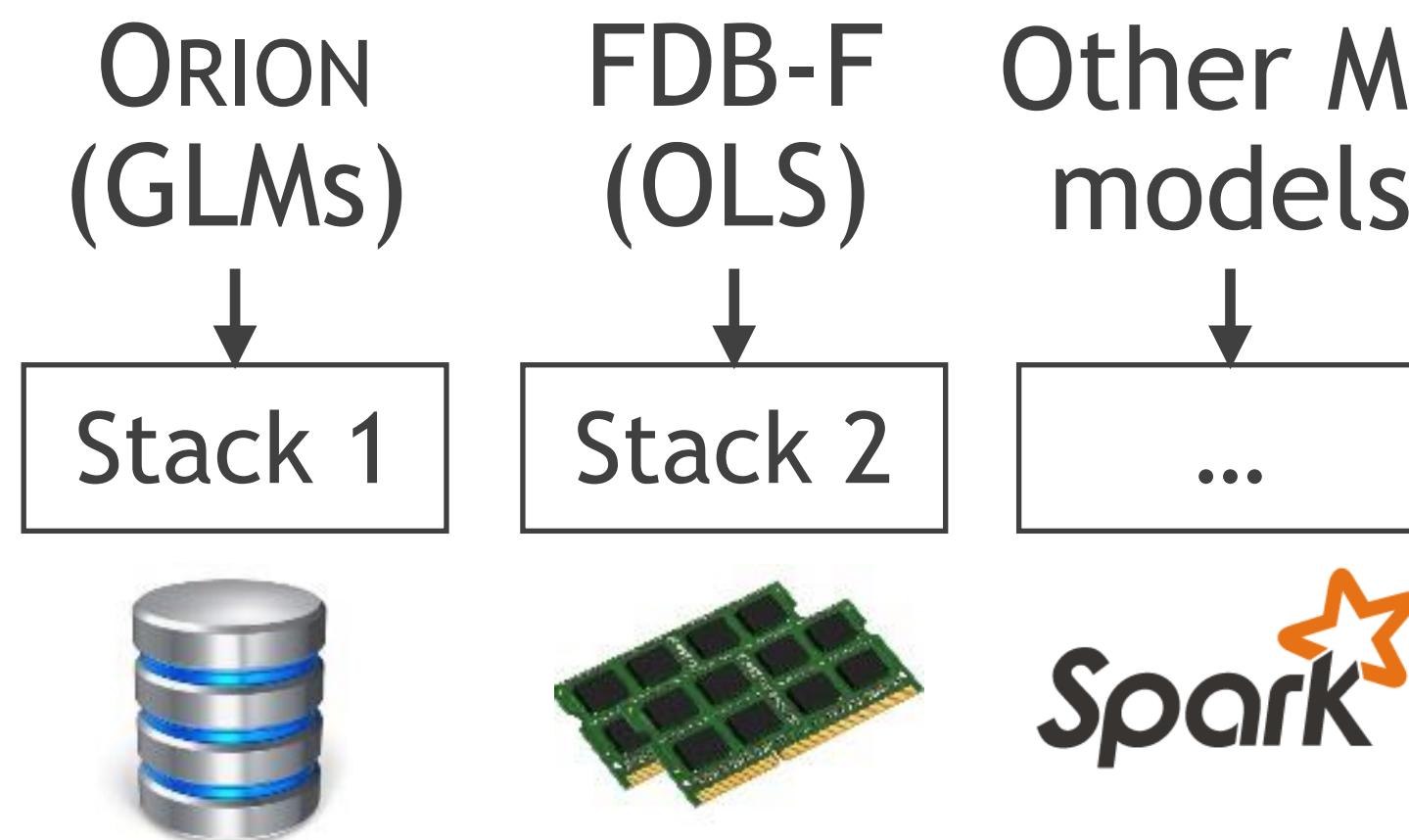


# MORPHEUS: Generalizing ORION

**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

## Factorized ML: Prior Work

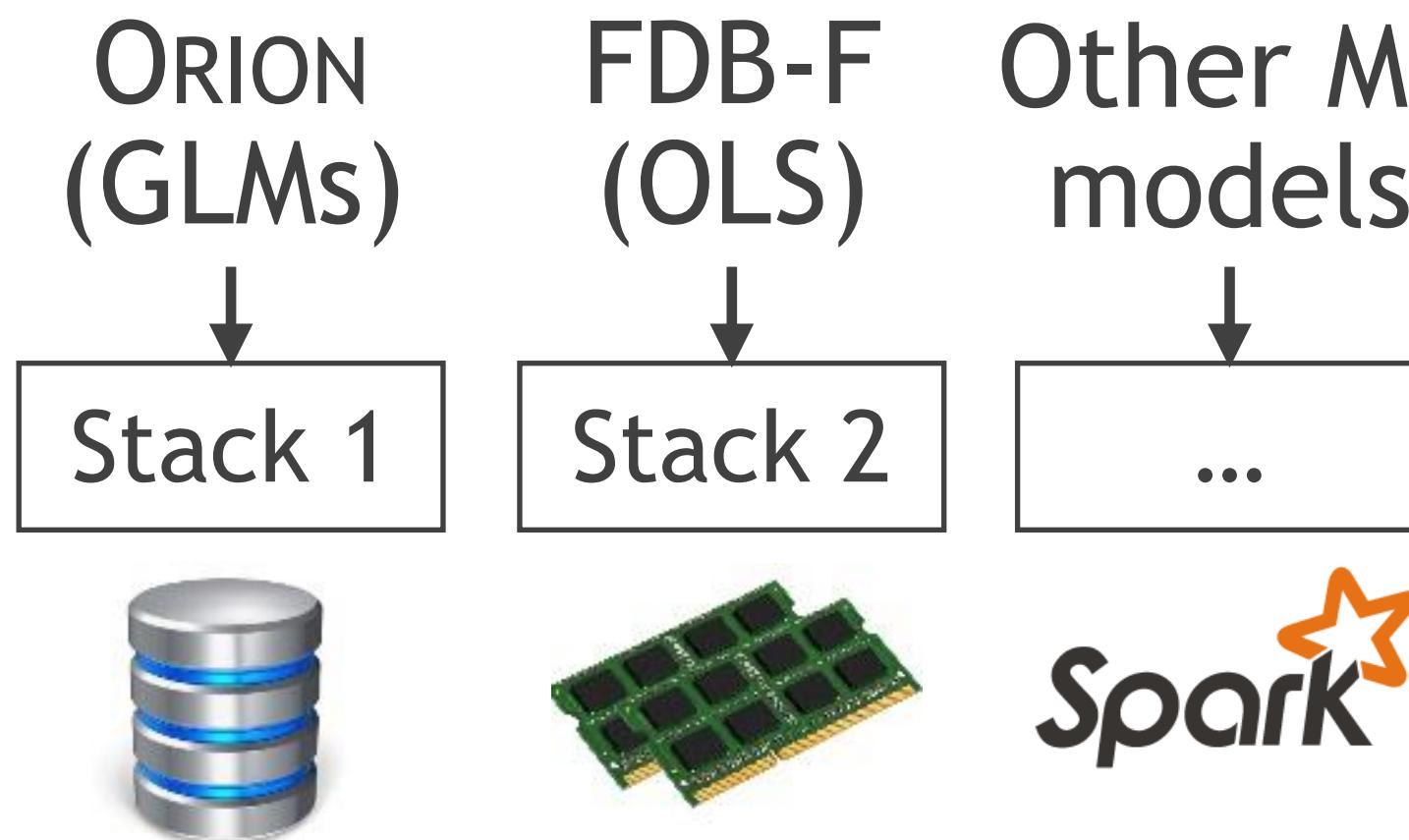


# MORPHEUS: Generalizing ORION

**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

## Factorized ML: Prior Work



## The MORPHEUS Approach

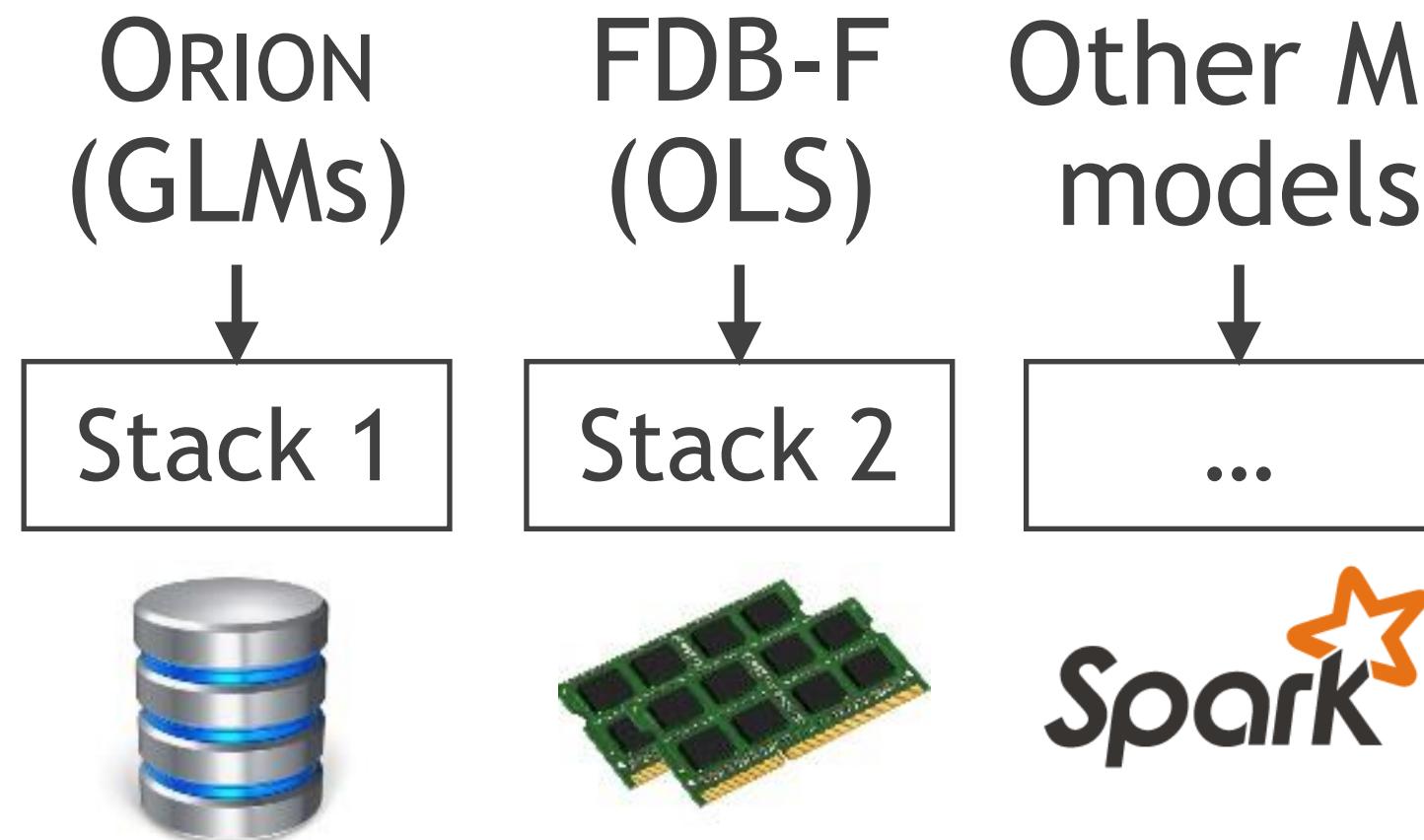
Towards Linear Algebra over Normalized Data. VLDB 2017

# MORPHEUS: Generalizing ORION

**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

## Factorized ML: Prior Work



## The MORPHEUS Approach

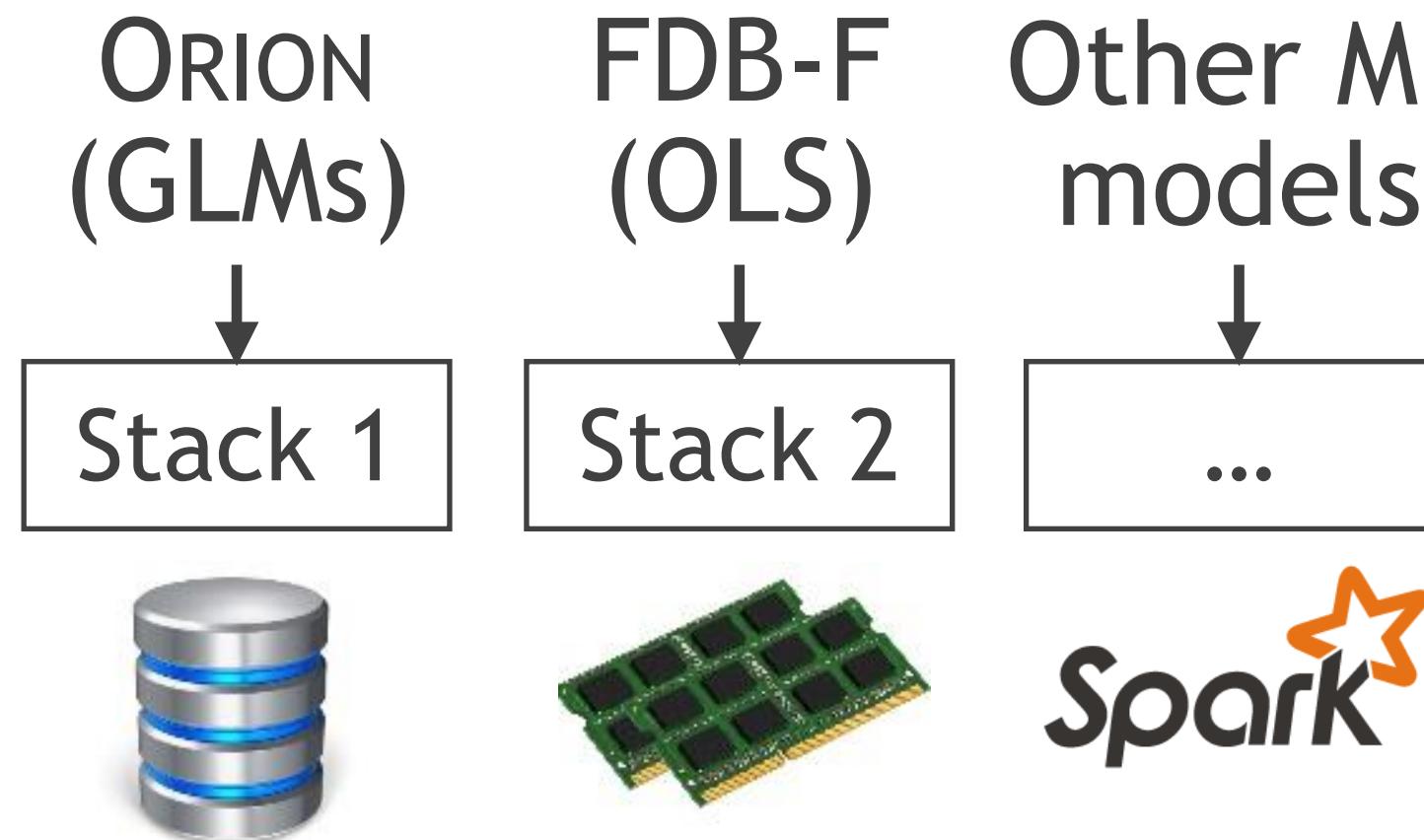
GLMs      OLS      K-Means      NMF      ...

# MORPHEUS: Generalizing ORION

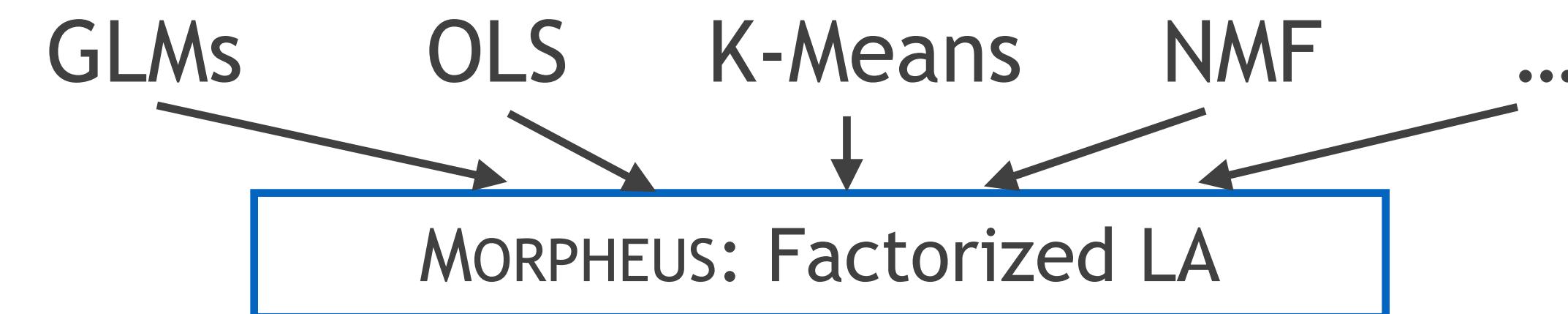
**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

## Factorized ML: Prior Work



## The MORPHEUS Approach

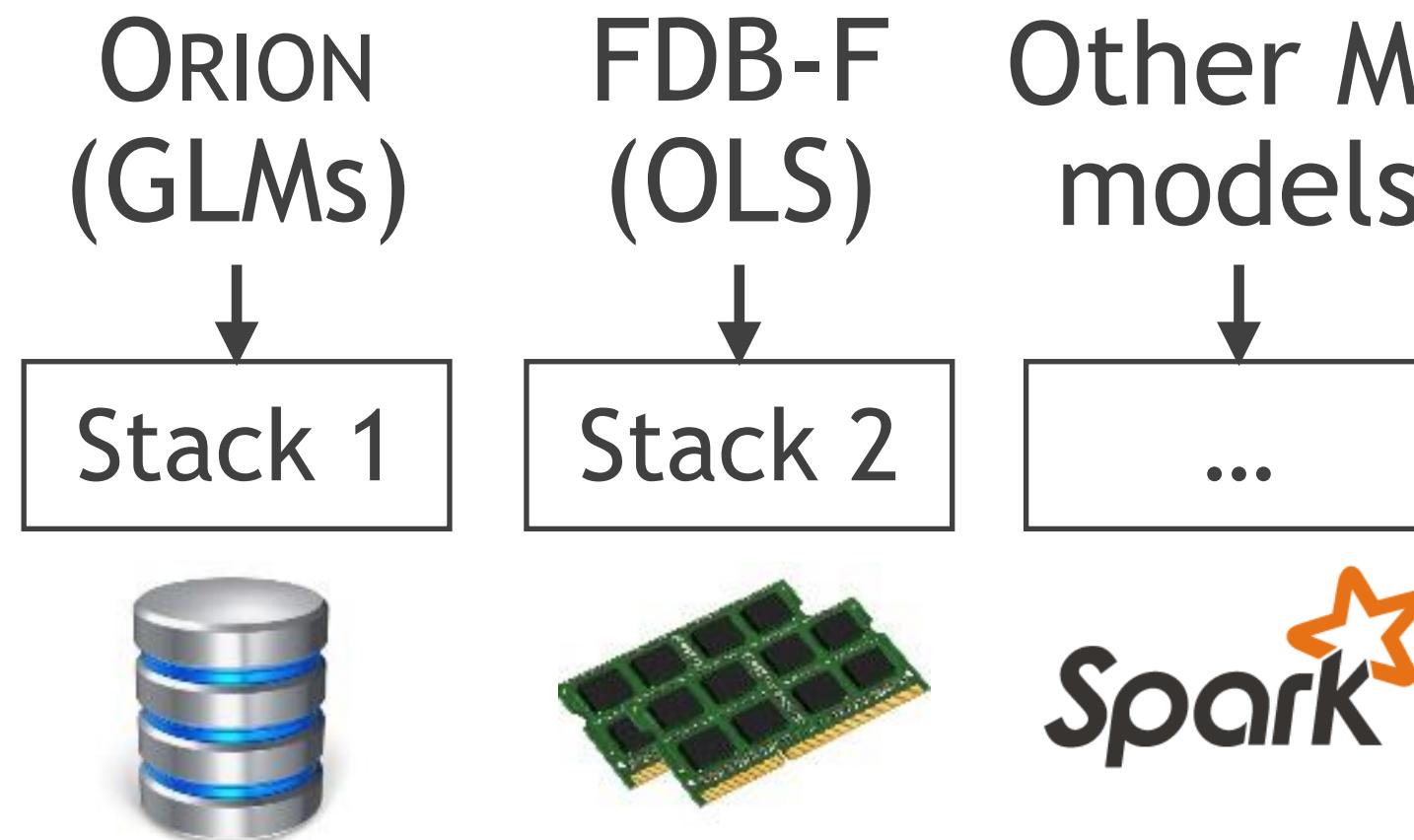


# MORPHEUS: Generalizing ORION

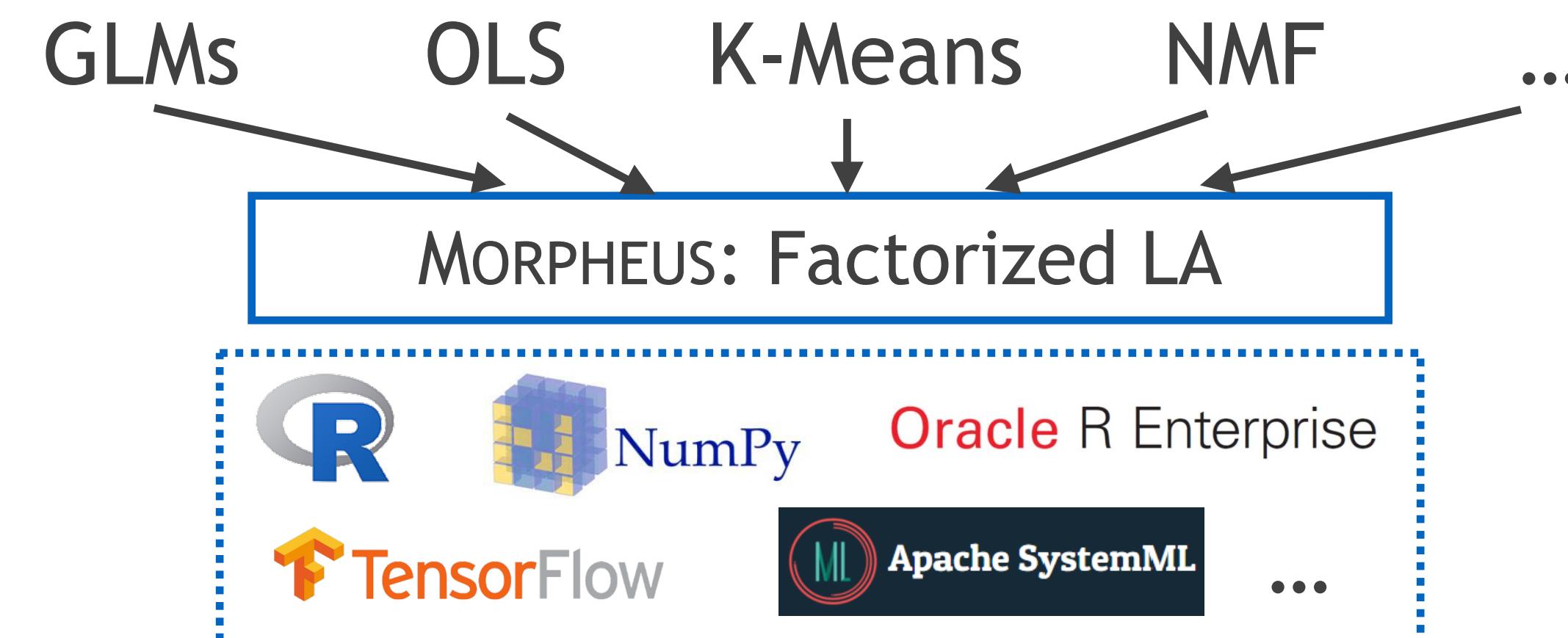
**Goal:** Automate factorized ML to many ML algorithms in a unified way

**Idea:** Many ML algorithms are bulk *linear algebra* (LA) programs  
Create a framework for rewrite rules for LA ops

## Factorized ML: Prior Work



## The MORPHEUS Approach



# Bulk LA-based ML Algorithms

# Bulk LA-based ML Algorithms

Ordinary Least Squares linear regression with normal equations

**Input:** Regular matrix  $T, Y, w$

$$w = ginv(crossprod(T))(T^\top Y)$$

# Bulk LA-based ML Algorithms

Ordinary Least Squares linear regression with normal equations

```
Input: Regular matrix  $T$ ,  $Y$ ,  $w$ 
 $w = ginv(crossprod(T))(T^\top Y)$ 
```

Logistic regression with BGD; works for L-BFGS and Conjugate Gradient too

```
Input: Regular matrix  $T$ ,  $Y$ ,  $w$ ,  $\alpha$ 
for  $i$  in  $1 : max\_iter$  do
|  $w = w + \alpha * (T^\top(Y/(1 + \exp(Tw))))$ 
end
```

# MORPHEUS: High-level Architecture

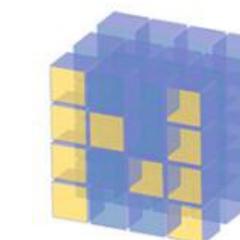
# MORPHEUS: High-level Architecture

MORPHEUS

Rewrite Rules for  
Factorized LA ops  
on an LA tool



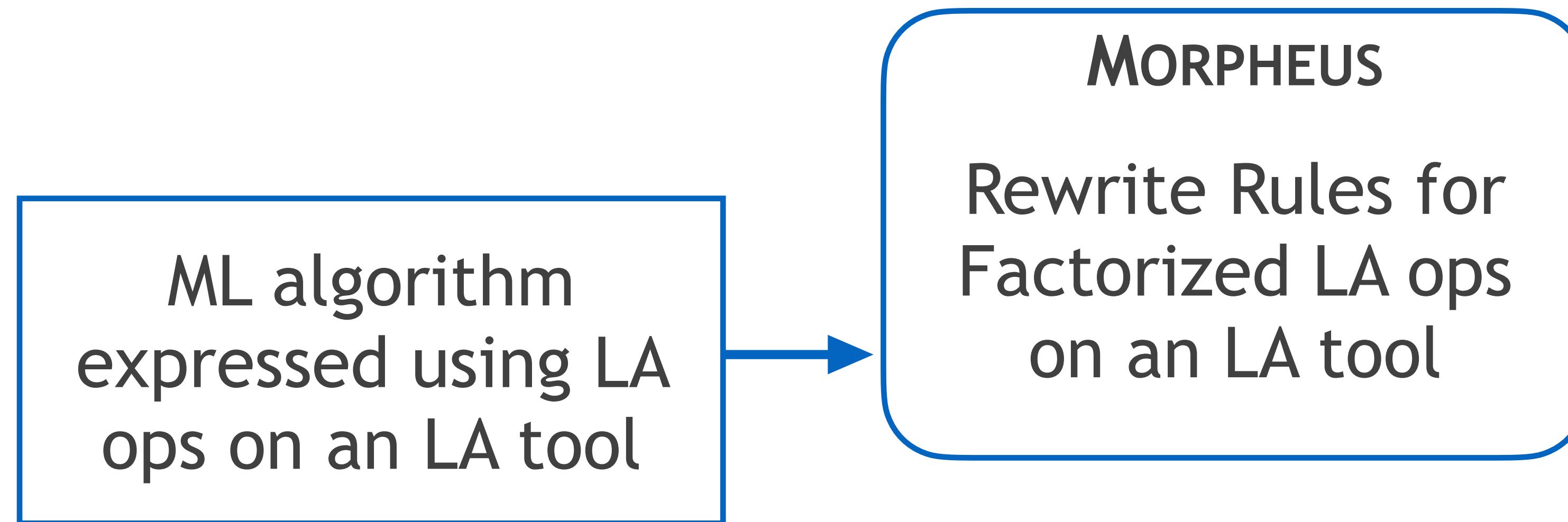
Oracle R Enterprise



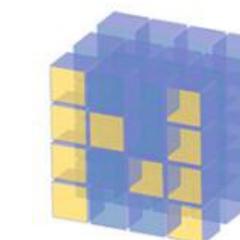
NumPy



# MORPHEUS: High-level Architecture



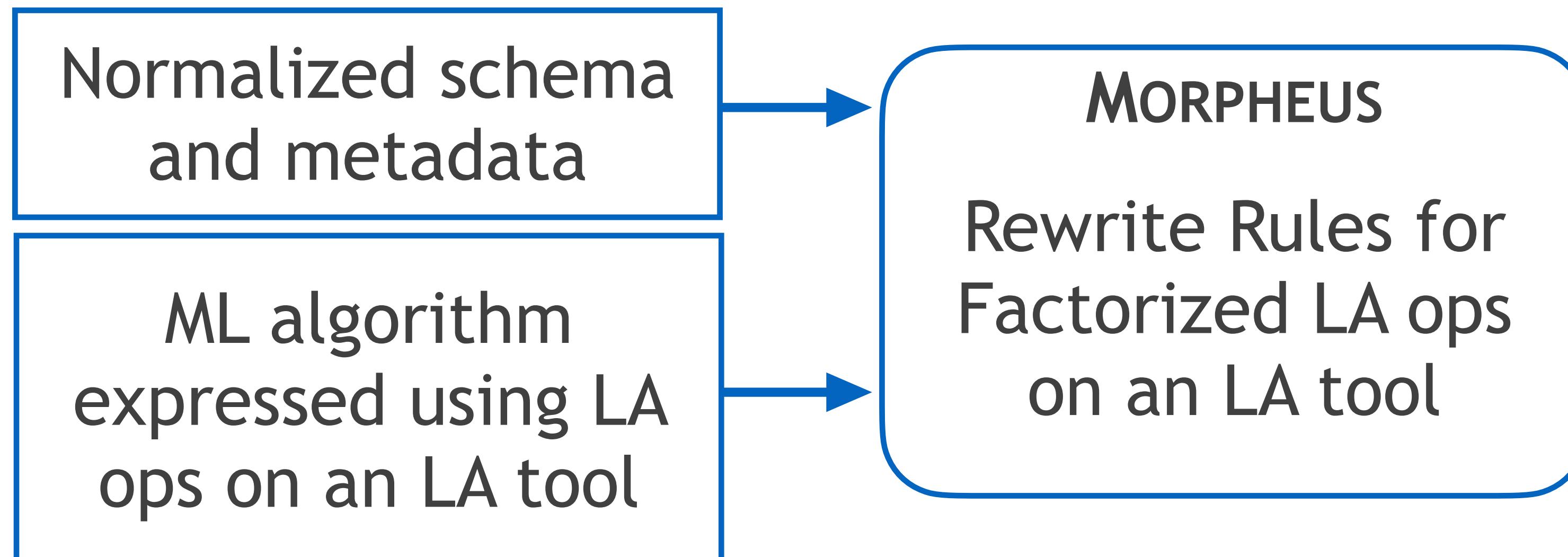
Oracle R Enterprise



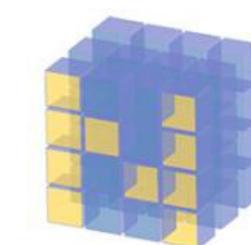
NumPy



# MORPHEUS: High-level Architecture



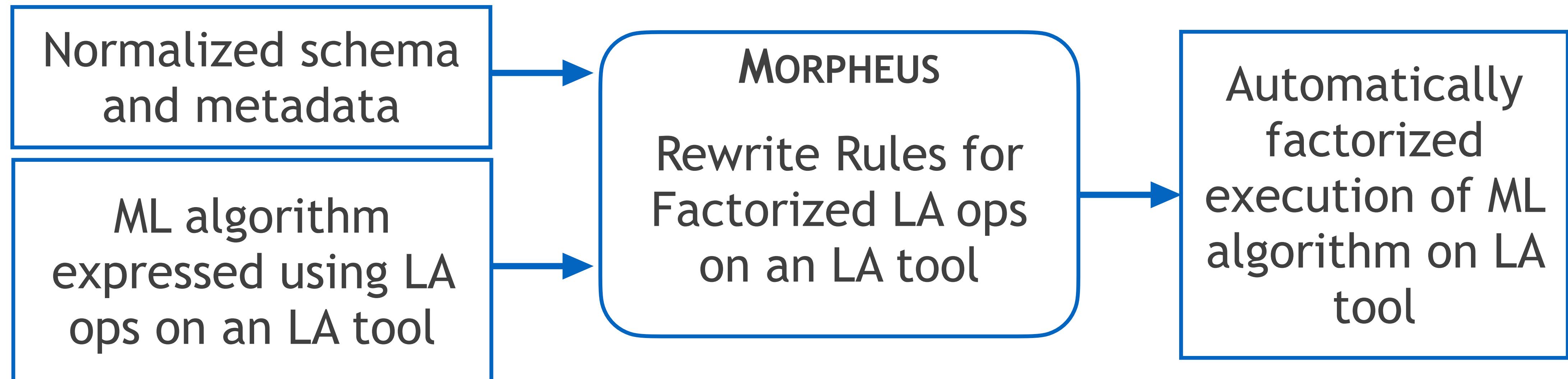
Oracle R Enterprise



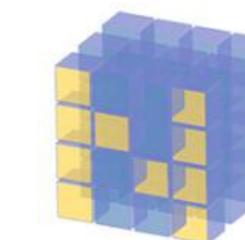
NumPy



# MORPHEUS: High-level Architecture



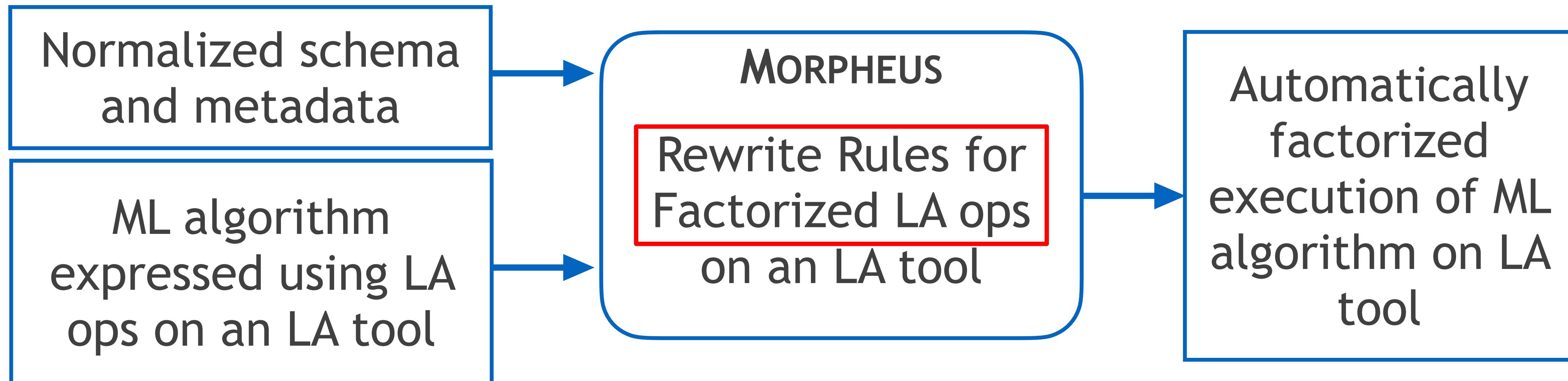
Oracle R Enterprise



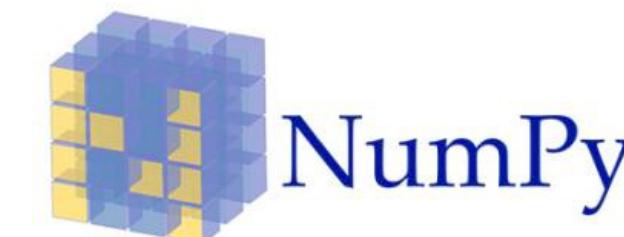
NumPy



# MORPHEUS: High-level Architecture



Oracle R Enterprise



# MORPHEUS: Factorized LA Rewrite Rules

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

Employers

# MORPHEUS: Factorized LA Rewrite Rules

# New Abstraction: “Normalized Matrix” to represent join in LA

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$       Customers      Employers

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$       Customers      Employers  
 $S_{n \times d_S}$

# MORPHEUS: Factorized LA Rewrite Rules

# New Abstraction: “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$       Customers      Employers  
 $S_{n \times d_S}$        $R_{n_R \times d_R}$

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, \boxed{X}) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$$X \equiv [X_S \ X_R]$$

$$T_{n \times d}$$

Customers  
 $S_{n \times d_S}$

Employers  
 $R_{n_R \times d_R}$

# MORPHEUS: Factorized LA Rewrite Rules

# New Abstraction: “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$       Customers      Employers  
 $T_{n \times d}$        $S_{n \times d_S}$        $R_{n_R \times d_R}$

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$	Customers $S_{n \times d_S}$	Employers $K_{n \times n_R}$	$R_{n_R \times d_R}$
------------------------	---------------------------------	---------------------------------	----------------------

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$	$S_{n \times d_S}$ Customers	$K_{n \times n_R}$	$R_{n_R \times d_R}$ Employers
$T_{n \times d}$			

$$K[i, j] = \begin{cases} 1, & \text{if } \mathbf{S}[i].FK = j \\ 0, & \text{o/w} \end{cases}$$

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$$X \equiv [X_S \ X_R] \quad \begin{array}{c} \text{Customers} \\ S_{n \times d_S} \end{array} \quad \begin{array}{c} \text{Employers} \\ K_{n \times n_R} \end{array} \quad R_{n_R \times d_R}$$

$$T = [S \ KR] \quad K[i, j] = \begin{cases} 1, & \text{if } \mathbf{S}[i].FK = j \\ 0, & \text{o/w} \end{cases}$$

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$	Customers	Employers	
$T_{n \times d}$	$S_{n \times d_S}$	$K_{n \times n_R}$	$R_{n_R \times d_R}$
$T = [S \ KR]$	$K[i, j] = \begin{cases} 1, & \text{if } \mathbf{S}[i].FK = j \\ 0, & \text{o/w} \end{cases}$		

Framework of algebraic rewrite rules for many LA operations

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$	Customers	Employers
$T_{n \times d}$	$S_{n \times d_S}$	$K_{n \times n_R}$
$T = [S \ KR]$	$K[i, j] = \begin{cases} 1, & \text{if } \mathbf{S}[i].FK = j \\ 0, & \text{o/w} \end{cases}$	$R_{n_R \times d_R}$

Framework of algebraic rewrite rules for many LA operations

Left Matrix Multiplication:

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$	$S_{n \times d_S}$	$K_{n \times n_R}$	$R_{n_R \times d_R}$
$T_{n \times d}$	<b>Customers</b>	<b>Employers</b>	
$T = [S \ KR]$	$K[i, j] = \begin{cases} 1, & \text{if } \mathbf{S}[i].FK = j \\ 0, & \text{o/w} \end{cases}$		

Framework of algebraic rewrite rules for many LA operations

Left Matrix Multiplication:  $Tw \rightarrow Sw_S + K(Rw_R)$

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$	Customers	Employers
$T_{n \times d}$	$S_{n \times d_S}$	$K_{n \times n_R}$
$T = [S \ KR]$	$K[i, j] = \begin{cases} 1, & \text{if } \mathbf{S}[i].FK = j \\ 0, & \text{o/w} \end{cases}$	$R_{n_R \times d_R}$

Framework of algebraic rewrite rules for many LA operations

Left Matrix Multiplication:  $Tw \rightarrow Sw_S + K(Rw_R)$

# MORPHEUS: Factorized LA Rewrite Rules

**New Abstraction:** “Normalized Matrix” to represent join in LA

$$\mathbf{T}(ID, X) \leftarrow \pi(\mathbf{S}(ID, X_S, FK) \bowtie_{FK=RID} \mathbf{R}(RID, X_R))$$

$X \equiv [X_S \ X_R]$	Customers	Employers
$T_{n \times d}$	$S_{n \times d_S}$	$K_{n \times n_R}$
$T = [S \ KR]$	$K[i, j] = \begin{cases} 1, & \text{if } \mathbf{S}[i].FK = j \\ 0, & \text{o/w} \end{cases}$	$R_{n_R \times d_R}$

Framework of algebraic rewrite rules for many LA operations

Left Matrix Multiplication:  $Tw \rightarrow Sw_S + K(Rw_R)$

GLMs, K-means clustering, NMF, etc. *automatically* factorized

# Automatically Factorized ML in MORPHEUS

# Automatically Factorized ML in MORPHEUS

```
Input: Regular matrix  $T$ ,  $Y$ ,  $w$ ,  $\alpha$ 
for  $i$  in  $1 : max\_iter$  do
|  $w = w + \alpha * (T^\top(Y/(1 + \exp(Tw))))$ 
end
```

# Automatically Factorized ML in MORPHEUS

```
Input: Regular matrix  $T, Y, w, \alpha$ 
for  $i$  in  $1 : max\_iter$  do
|  $w = w + \alpha * (T^\top(Y/(1 + \exp(Tw))))$ 
end
```

$T \equiv (S, K, R)$   MORPHEUS

# Automatically Factorized ML in MORPHEUS

```
Input: Regular matrix  $T, Y, w, \alpha$ 
for  $i$  in  $1 : max\_iter$  do
|  $w = w + \alpha * (T^\top(Y/(1 + \exp(Tw))))$ 
end
```

$T \equiv (S, K, R)$   MORPHEUS

```
Input: Normalized matrix  $(S, K, R), Y, w, \alpha$ 
for  $i$  in  $1 : max\_iter$  do
|  $P = (Y/(1 + \exp(Sw[1 : d_S,] +
| \quad \quad \quad K(Rw[d_S + 1 : d_S + d_R,]))))^\top$ 
|  $w = w + \alpha * [PS, (PK)R]^\top$ 
end
```

# LA Operations Factorized in MORPHEUS

Table 1: Operators and functions of linear algebra handled in this paper over a normalized matrix  $T$ .

Op Type	Name	Expression	Output Type	Parameter X or x	Factorizable
Element-wise Scalar Op	Arithmetic Op ( $\otimes = +, -, *, /, \hat{,}$ , etc)	$T \otimes x$ or $x \otimes T$	Normalized Matrix	A scalar	Yes
	Transpose	$T^\top$		N/A	
	Scalar Function $f$ (e.g., log, exp, sin)	$f(T)$		Parameters for $f$	
Aggregation	Row Summation	$\text{rowSums}(T)$	Column Vector	N/A	Yes
	Column Summation	$\text{colSums}(T)$	Row Vector		
	Summation	$\text{sum}(T)$	Scalar		
Multiplication	Left Multiplication	$TX$	Regular Matrix	$(d_S + d_R) \times d_X$ matrix	No
	Right Multiplication	$X T$		$n_X \times n_S$ matrix	
	Cross-product	$\text{crossprod}(T)$		N/A	
Inversion	Pseudoinverse	$\text{ginv}(T)$	Regular Matrix	$n_S \times (d_S + d_R)$ matrix	No
Element-wise Matrix Op	Arithmetic Op ( $\otimes = +, -, *, /, \hat{,}$ , etc)	$X \otimes T$ or $T \otimes X$			

# Snapshot of Empirical Results

# Snapshot of Empirical Results

Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine

# Snapshot of Empirical Results

Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine

S: Ratings



R<sub>1</sub>: Users

R<sub>2</sub>: Businesses

# Snapshot of Empirical Results

Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine



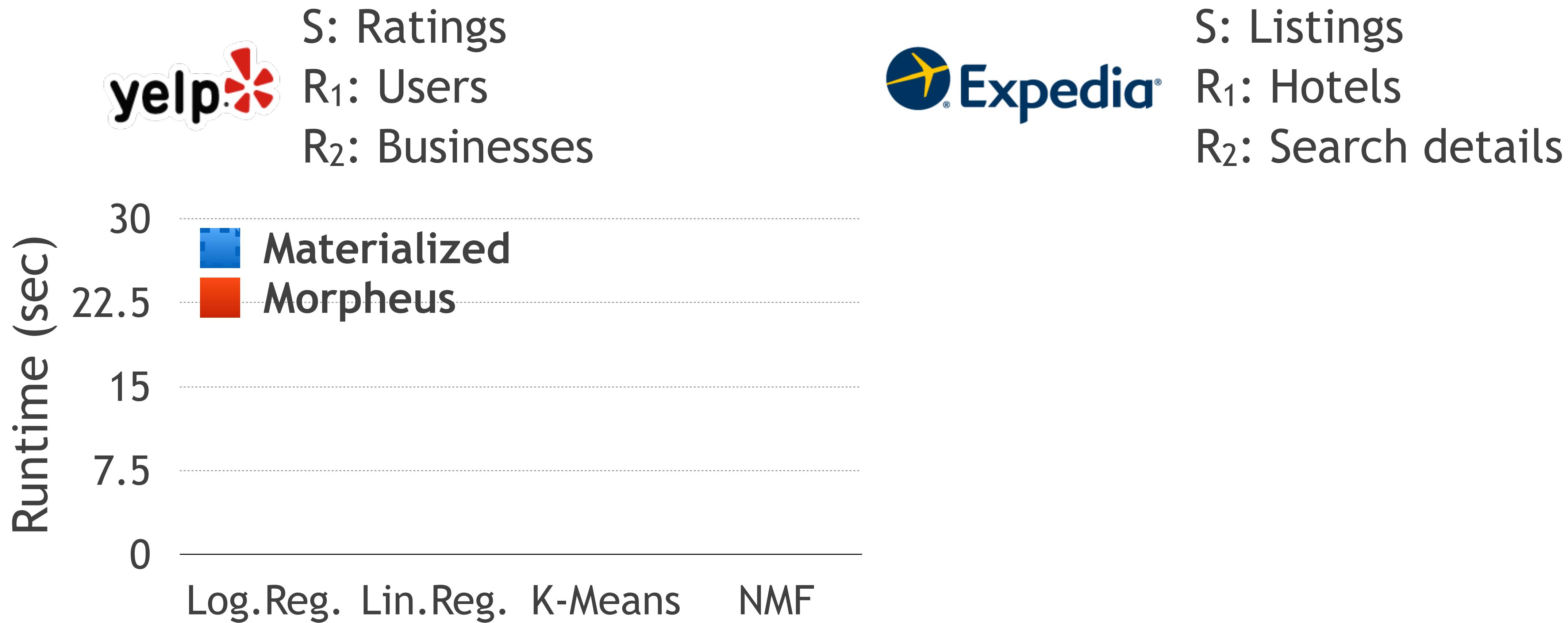
S: Ratings  
R<sub>1</sub>: Users  
R<sub>2</sub>: Businesses



S: Listings  
R<sub>1</sub>: Hotels  
R<sub>2</sub>: Search details

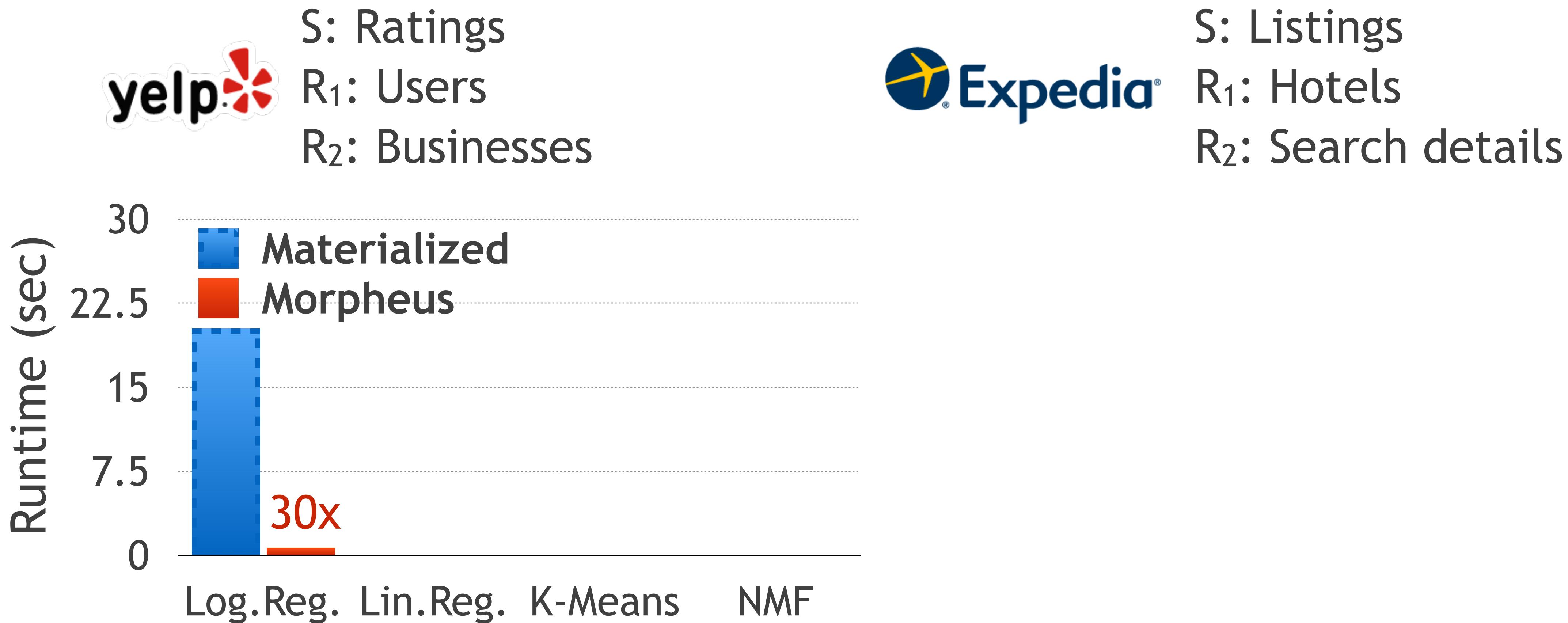
# Snapshot of Empirical Results

Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine



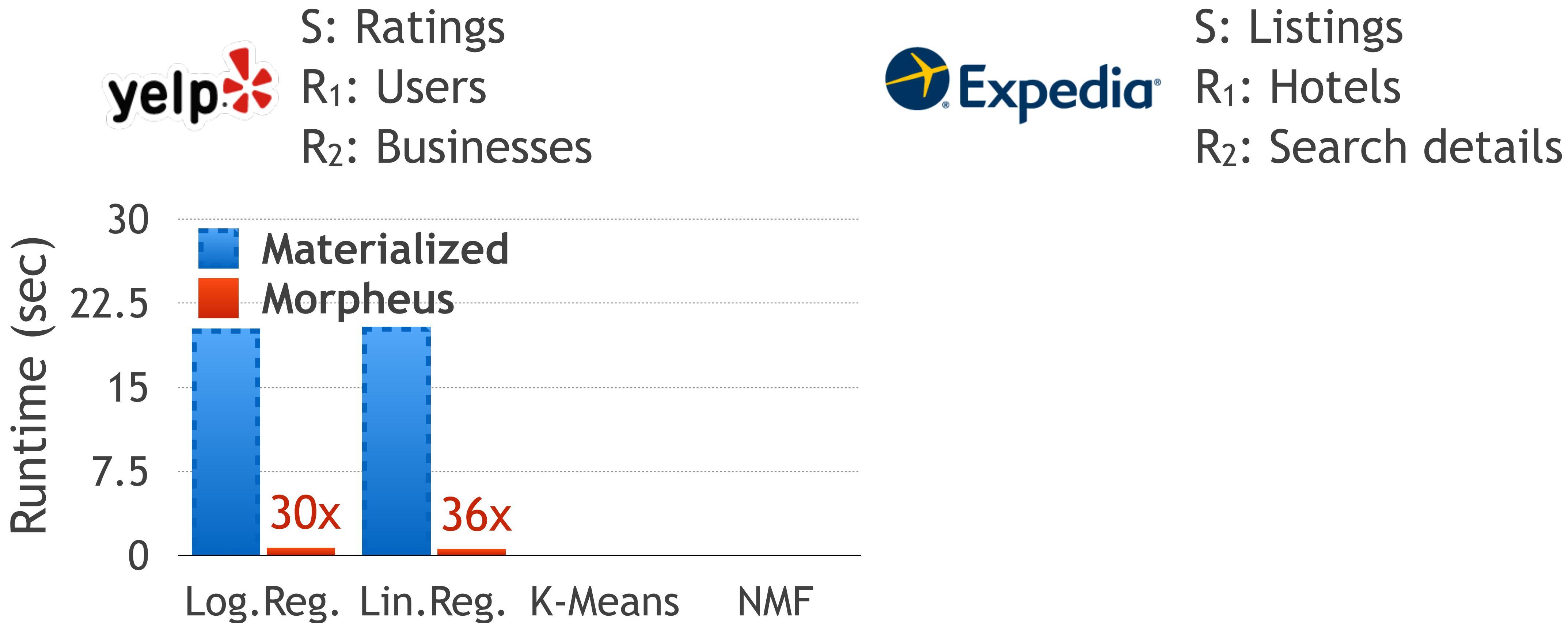
# Snapshot of Empirical Results

Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine



# Snapshot of Empirical Results

Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine



# Snapshot of Empirical Results

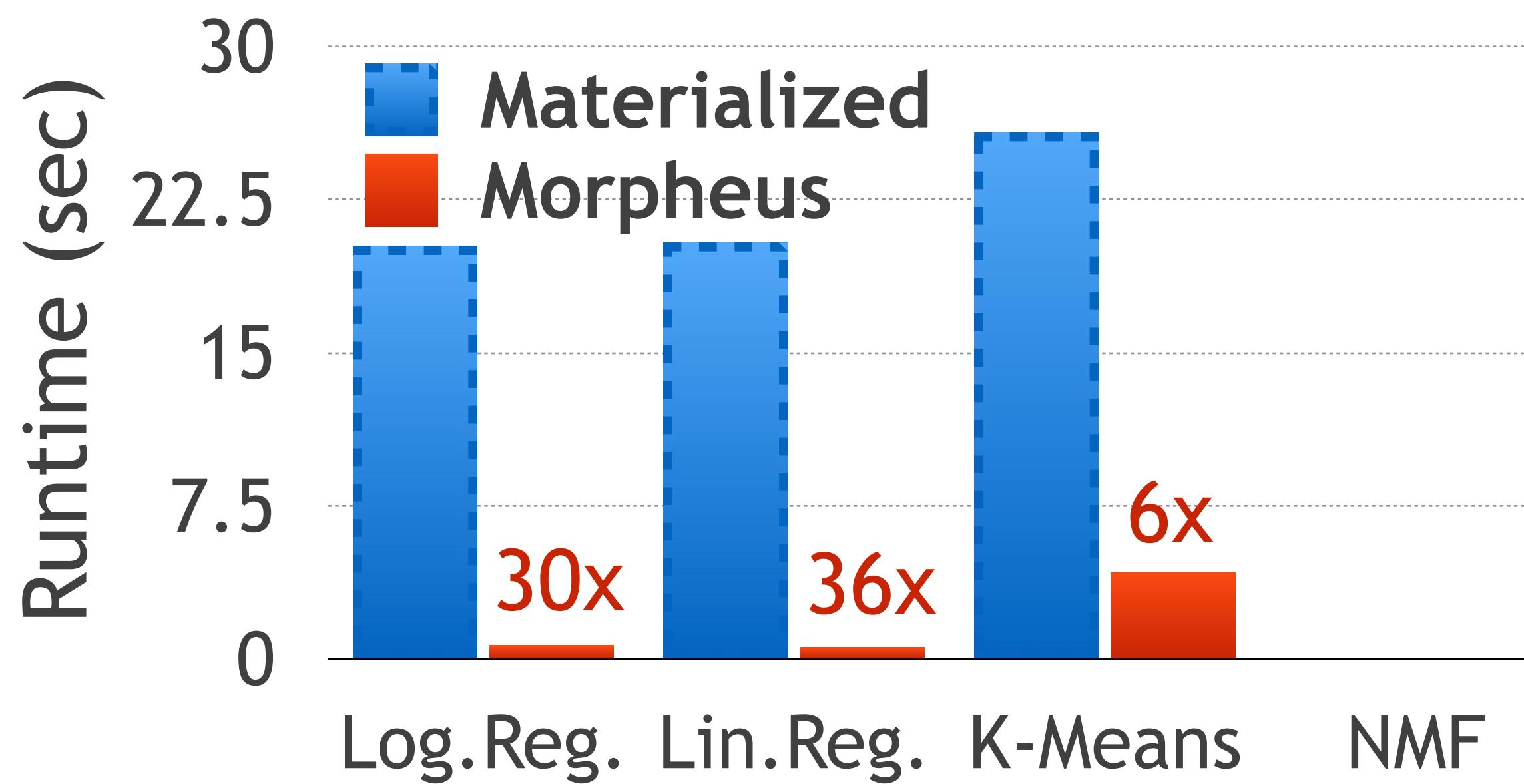
Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine



S: Ratings  
R<sub>1</sub>: Users  
R<sub>2</sub>: Businesses



S: Listings  
R<sub>1</sub>: Hotels  
R<sub>2</sub>: Search details



# Snapshot of Empirical Results

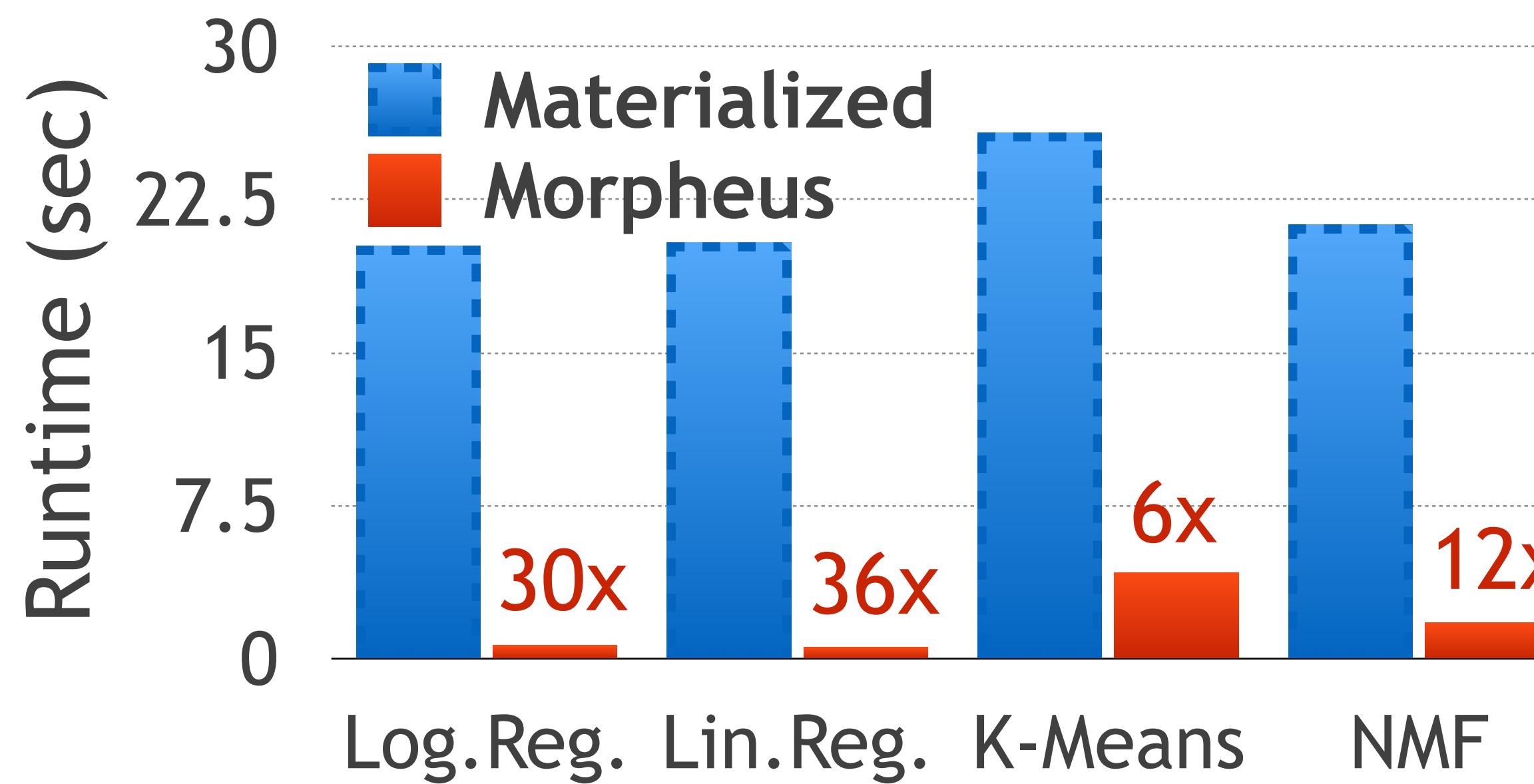
Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine



S: Ratings  
R<sub>1</sub>: Users  
R<sub>2</sub>: Businesses



S: Listings  
R<sub>1</sub>: Hotels  
R<sub>2</sub>: Search details

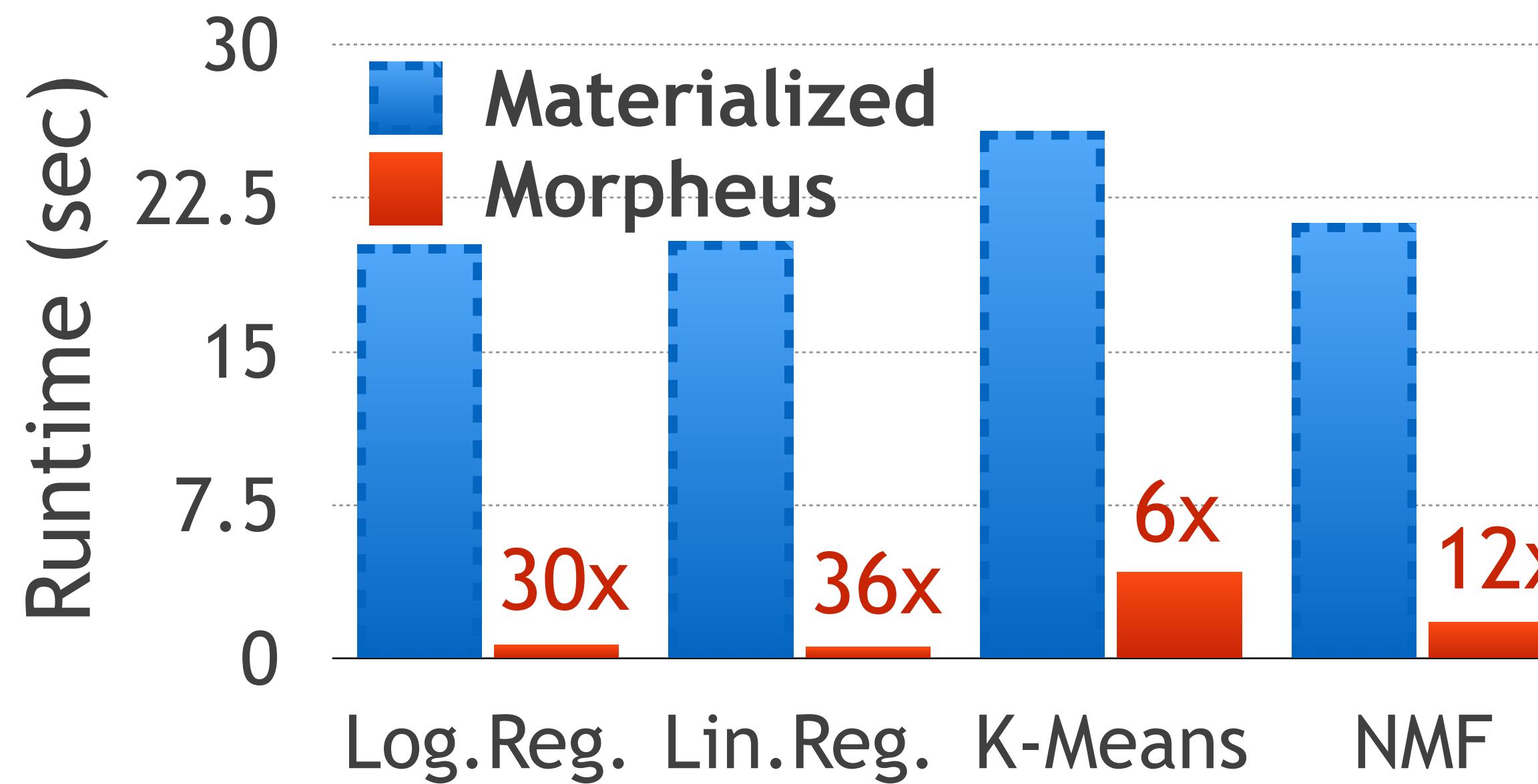


# Snapshot of Empirical Results

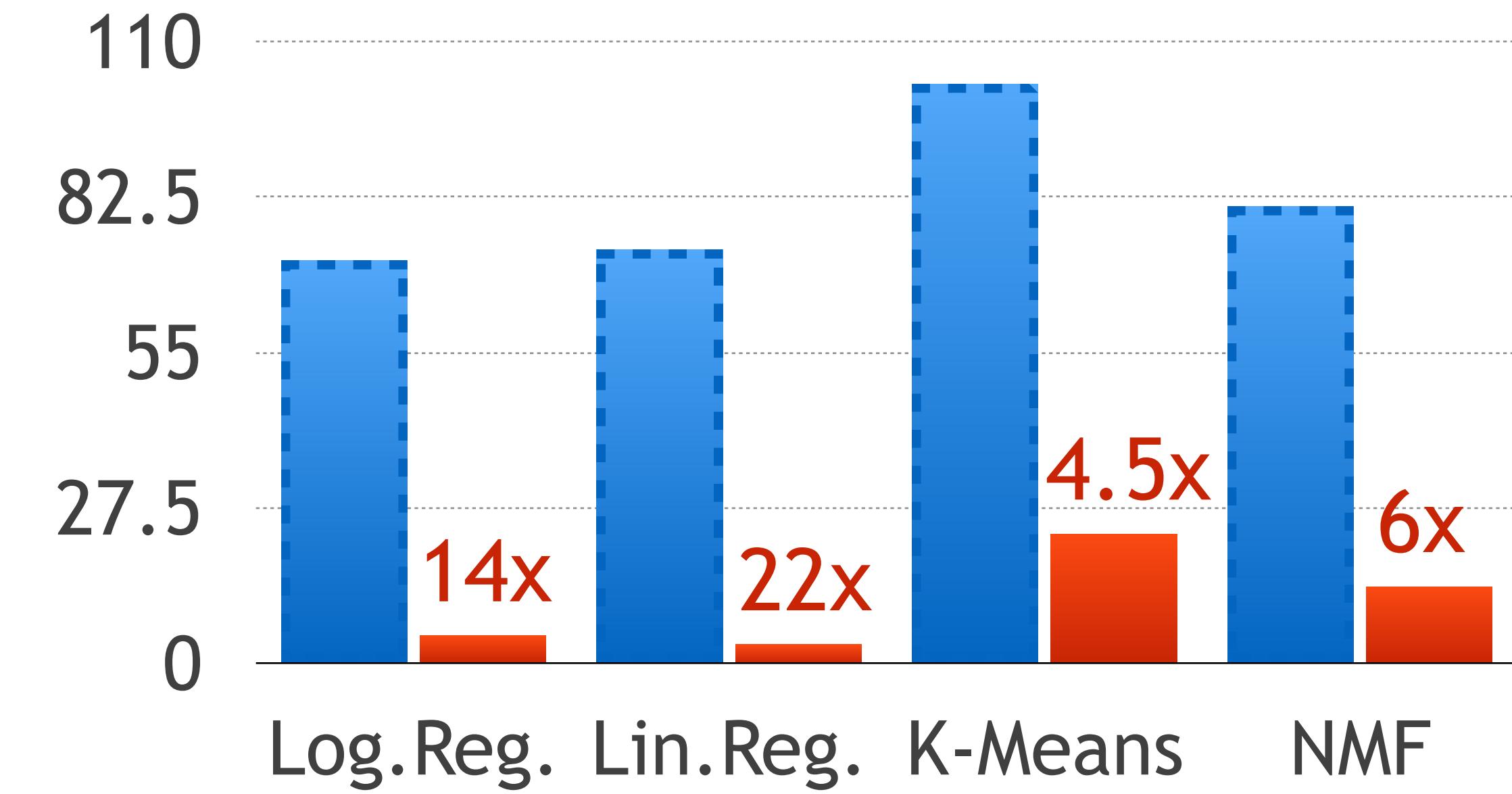
Prototype in R (and Python) for listed LA ops; ~800 LOC; commodity machine



S: Ratings  
R<sub>1</sub>: Users  
R<sub>2</sub>: Businesses



S: Listings  
R<sub>1</sub>: Hotels  
R<sub>2</sub>: Search details



# When is MORPHEUS not likely to be beneficial?

# When is MORPHEUS not likely to be beneficial?

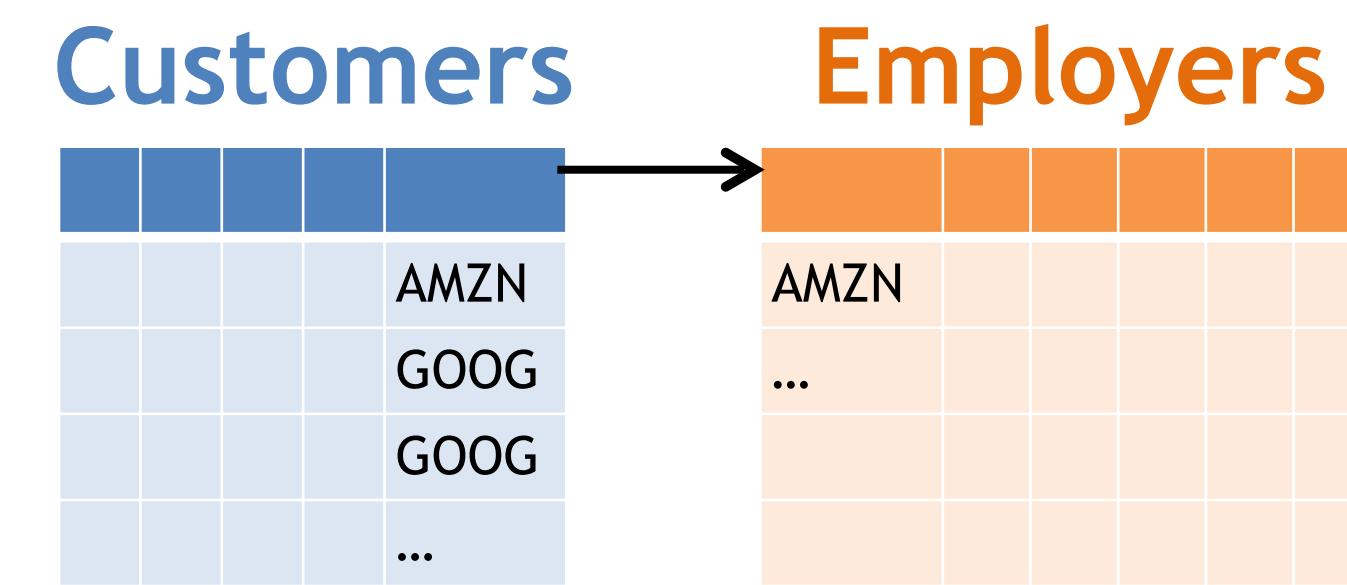
**Short Answer:** When the join(s) do *not* introduce much redundancy

# When is MORPHEUS not likely to be beneficial?

**Short Answer:** When the join(s) do *not* introduce much redundancy

**Case 1:**

Fact table is *not much taller* than dimension table(s)

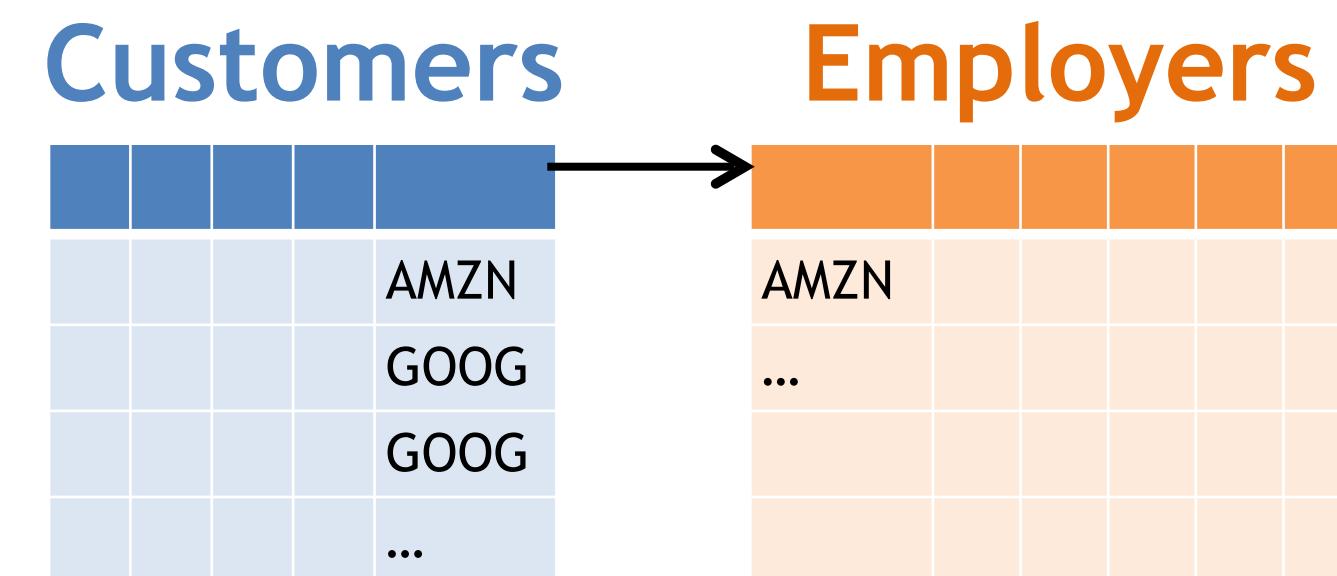


# When is MORPHEUS not likely to be beneficial?

**Short Answer:** When the join(s) do *not* introduce much redundancy

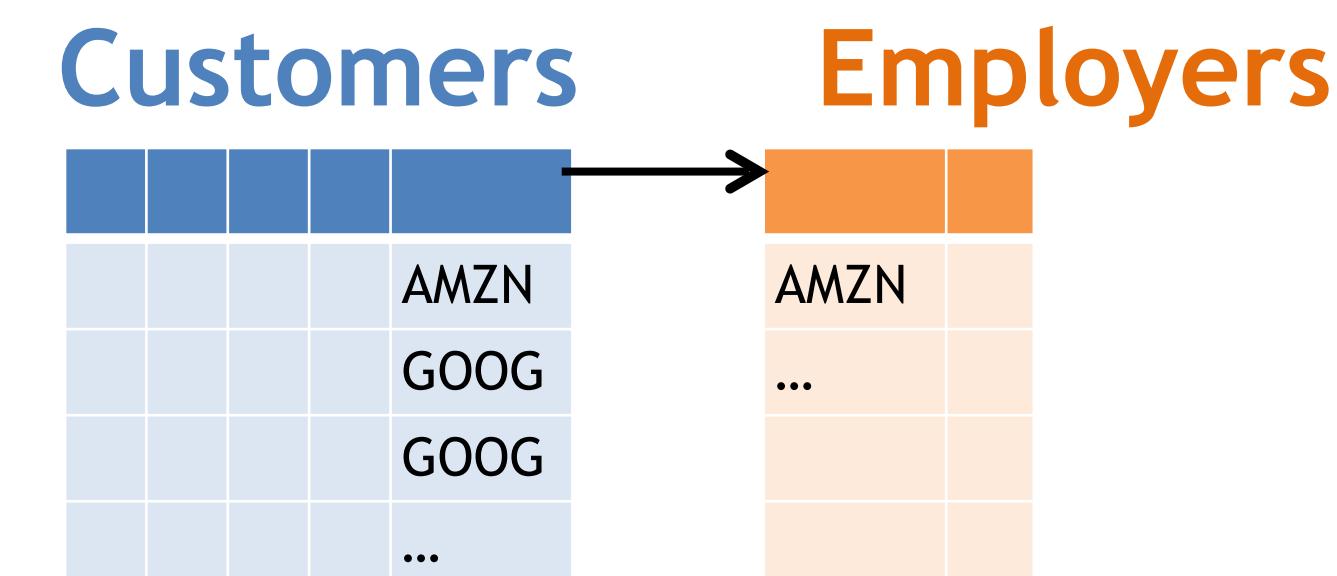
**Case 1:**

Fact table is *not much taller* than dimension table(s)



**Case 2:**

Dimension table has *much fewer* features than fact table

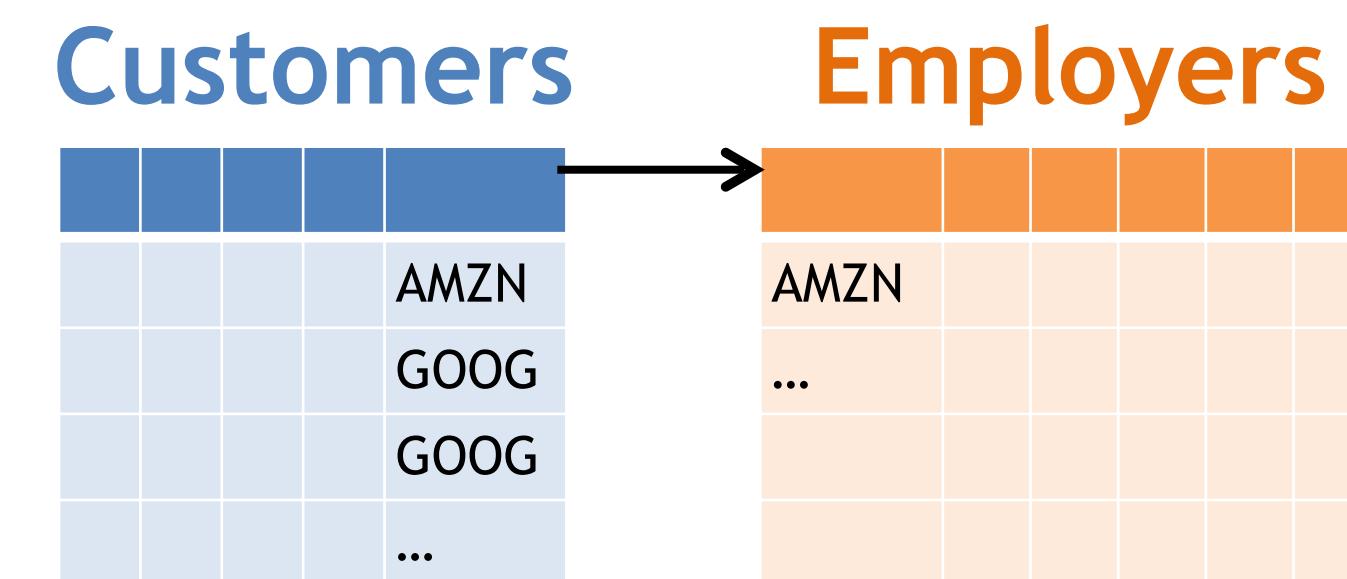


# When is MORPHEUS not likely to be beneficial?

**Short Answer:** When the join(s) do *not* introduce much redundancy

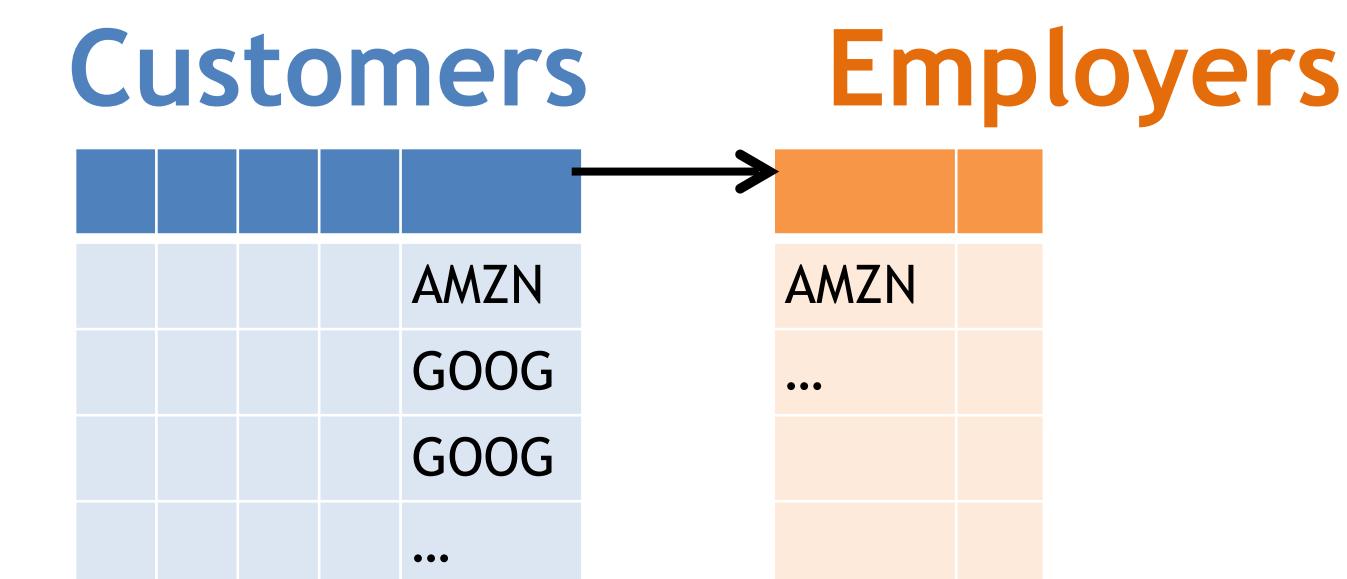
## Case 1:

Fact table is *not much taller* than dimension table(s)



## Case 2:

Dimension table has *much fewer* features than fact table



**Case 3:** MLPs do *not* have much computational redundancy (anyway)

# MORPHEUS: Implementations and Extensions

*Towards Linear Algebra over Normalized Data.* [VLDB 2017](#)  
*Enabling and Optimizing Non-linear Feature Interactions in Factorized Linear Algebra.* [SIGMOD 2019](#)  
 *Tuple-oriented Compression for Large-scale Mini-batch Stochastic Gradient Descent.* [SIGMOD 2019](#)

# MORPHEUS: Implementations and Extensions

Library released for both R and Python NumPy

*Towards Linear Algebra over Normalized Data.* [VLDB 2017](#)  
*Enabling and Optimizing Non-linear Feature Interactions in Factorized Linear Algebra.* [SIGMOD 2019](#)  
 *Tuple-oriented Compression for Large-scale Mini-batch Stochastic Gradient Descent.* [SIGMOD 2019](#)

# MORPHEUS: Implementations and Extensions

Library released for both R and Python NumPy

Supports star schemas for many LA ops; snowflakes can be reduced to star

*Towards Linear Algebra over Normalized Data.* [VLDB 2017](#)

*Enabling and Optimizing Non-linear Feature Interactions in Factorized Linear Algebra.* [SIGMOD 2019](#)

*Tuple-oriented Compression for Large-scale Mini-batch Stochastic Gradient Descent.* [SIGMOD 2019](#)

# MORPHEUS: Implementations and Extensions

Library released for both R and Python NumPy

Supports star schemas for many LA ops; snowflakes can be reduced to star

Some data cleaning/prep ops also factorized

*Towards Linear Algebra over Normalized Data.* [VLDB 2017](#)

*Enabling and Optimizing Non-linear Feature Interactions in Factorized Linear Algebra.* [SIGMOD 2019](#)

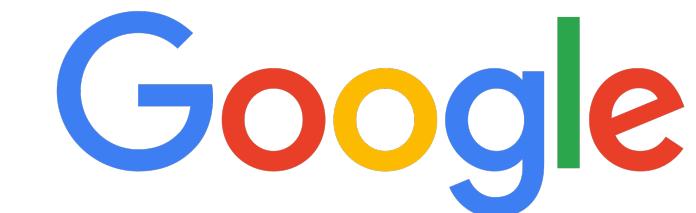
*Tuple-oriented Compression for Large-scale Mini-batch Stochastic Gradient Descent.* [SIGMOD 2019](#)

# MORPHEUS: Implementations and Extensions

Library released for both R and Python NumPy

Supports star schemas for many LA ops; snowflakes can be reduced to star

Some data cleaning/prep ops also factorized



*Towards Linear Algebra over Normalized Data.* [VLDB 2017](#)

*Enabling and Optimizing Non-linear Feature Interactions in Factorized Linear Algebra.* [SIGMOD 2019](#)

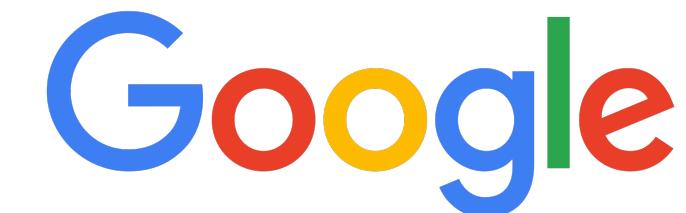
*Tuple-oriented Compression for Large-scale Mini-batch Stochastic Gradient Descent.* [SIGMOD 2019](#)

# MORPHEUS: Implementations and Extensions

Library released for both R and Python NumPy

Supports star schemas for many LA ops; snowflakes can be reduced to star

Some data cleaning/prep ops also factorized



**MORPHEUSFI:** Second-order feature interactions in Morpheus

*Towards Linear Algebra over Normalized Data.* [VLDB 2017](#)

*Enabling and Optimizing Non-linear Feature Interactions in Factorized Linear Algebra.* [SIGMOD 2019](#)

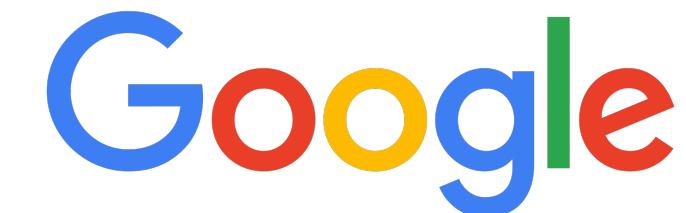
*Tuple-oriented Compression for Large-scale Mini-batch Stochastic Gradient Descent.* [SIGMOD 2019](#)

# MORPHEUS: Implementations and Extensions

Library released for both R and Python NumPy

Supports star schemas for many LA ops; snowflakes can be reduced to star

Some data cleaning/prep ops also factorized



**MORPHEUSFI:** Second-order feature interactions in Morpheus

**MORPHEUSFLOW:** “Lazy join” for SGD in TensorFlow

*Towards Linear Algebra over Normalized Data.* [VLDB 2017](#)

*Enabling and Optimizing Non-linear Feature Interactions in Factorized Linear Algebra.* [SIGMOD 2019](#)

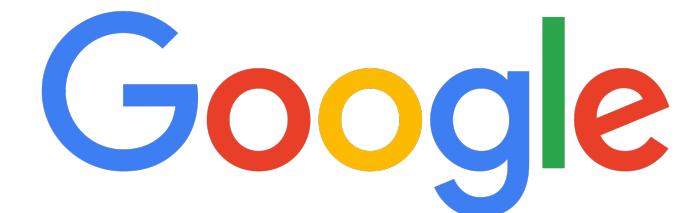
*Tuple-oriented Compression for Large-scale Mini-batch Stochastic Gradient Descent.* [SIGMOD 2019](#)

# MORPHEUS: Implementations and Extensions

Library released for both R and Python NumPy

Supports star schemas for many LA ops; snowflakes can be reduced to star

Some data cleaning/prep ops also factorized



**MORPHEUSFI:** Second-order feature interactions in Morpheus

**MORPHEUSFLOW:** “Lazy join” for SGD in TensorFlow

**TOC:** Generalized data compression for SGD

*Towards Linear Algebra over Normalized Data.* [VLDB 2017](#)

*Enabling and Optimizing Non-linear Feature Interactions in Factorized Linear Algebra.* [SIGMOD 2019](#)

*Tuple-oriented Compression for Large-scale Mini-batch Stochastic Gradient Descent.* [SIGMOD 2019](#)

# TRINITY: MORPHEUS Meets Oracle GraalVM

# TRINITY: MORPHEUS Meets Oracle GraalVM

**Goal:** *Automate Morpheus itself to many PLs in a unified way*

# TRINITY: MORPHEUS Meets Oracle GraalVM

**Goal:** *Automate Morpheus itself to many PLs in a unified way*

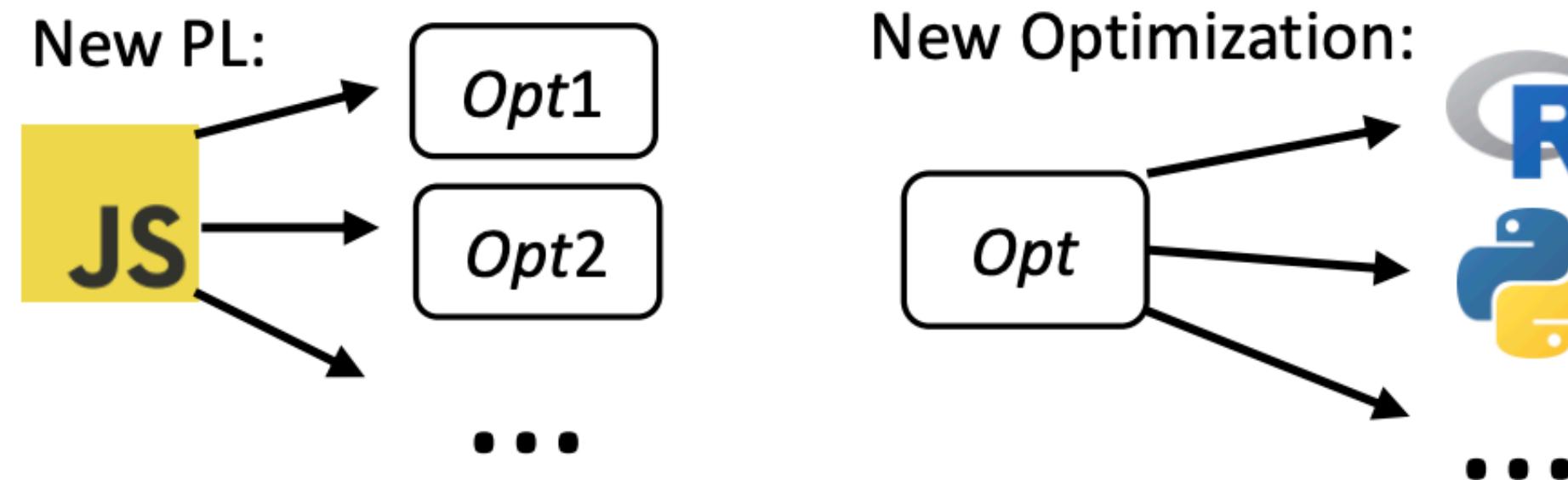
**Idea:** Exploit GraalVM, an industrial-strength *Polyglot* compiler + runtime for data science workloads (R, Py, Javascript, etc.)

# TRINITY: MORPHEUS Meets Oracle GraalVM

**Goal:** Automate Morpheus itself to many PLs in a unified way

**Idea:** Exploit GraalVM, an industrial-strength *Polyglot* compiler + runtime for data science workloads (R, Py, Javascript, etc.)

## World without Trinity

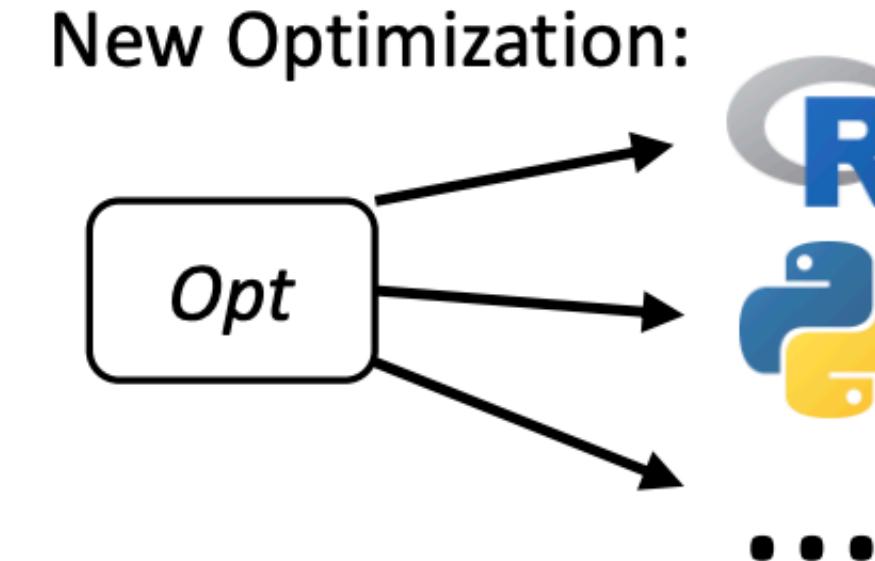
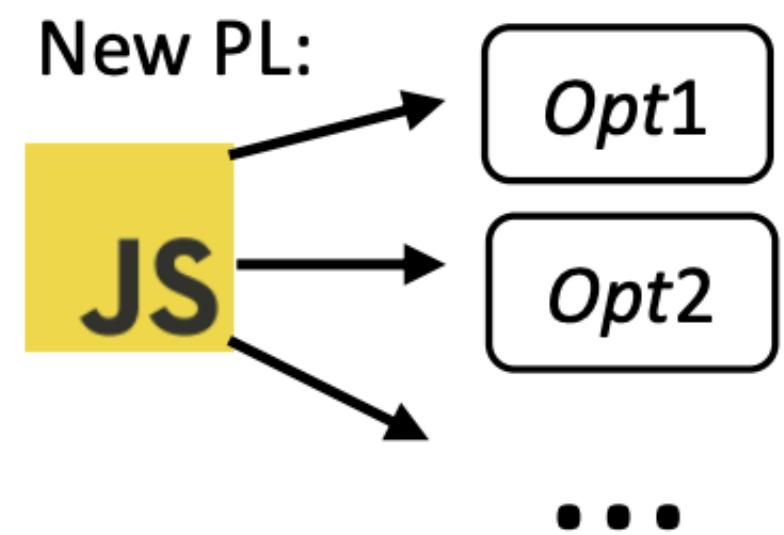


# TRINITY: MORPHEUS Meets Oracle GraalVM

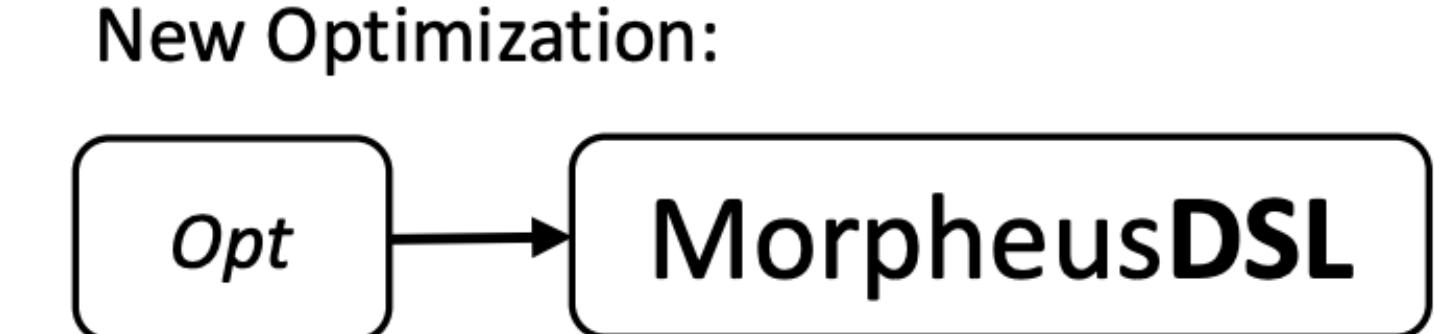
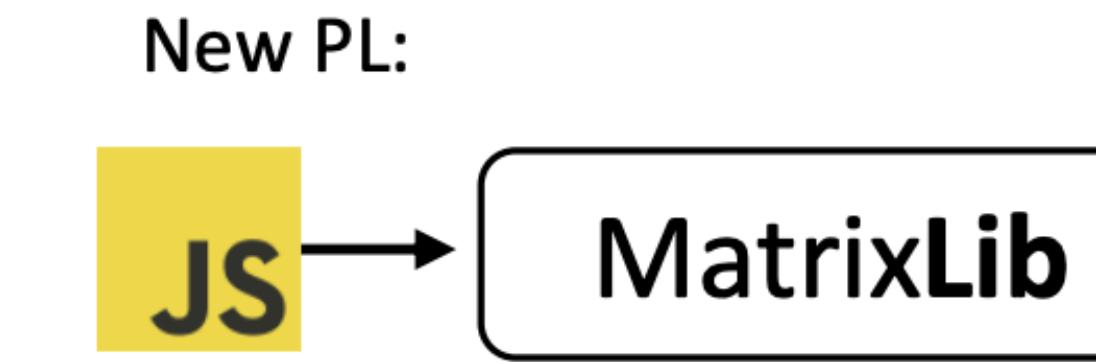
**Goal:** Automate Morpheus itself to many PLs in a unified way

**Idea:** Exploit GraalVM, an industrial-strength *Polyglot* compiler + runtime for data science workloads (R, Py, Javascript, etc.)

## World without Trinity



## World with Trinity

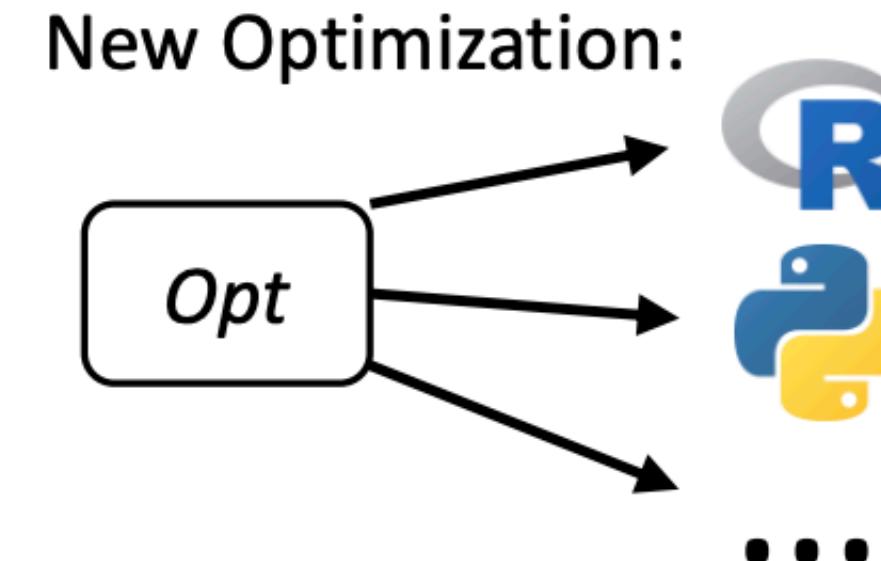
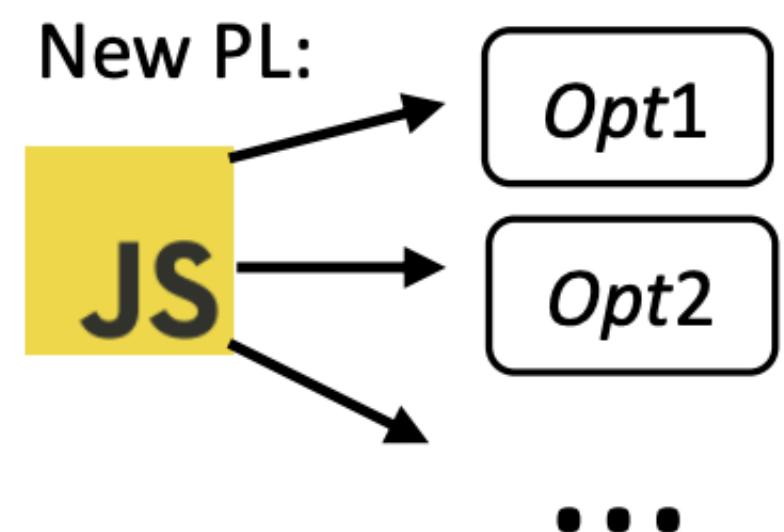


# TRINITY: MORPHEUS Meets Oracle GraalVM

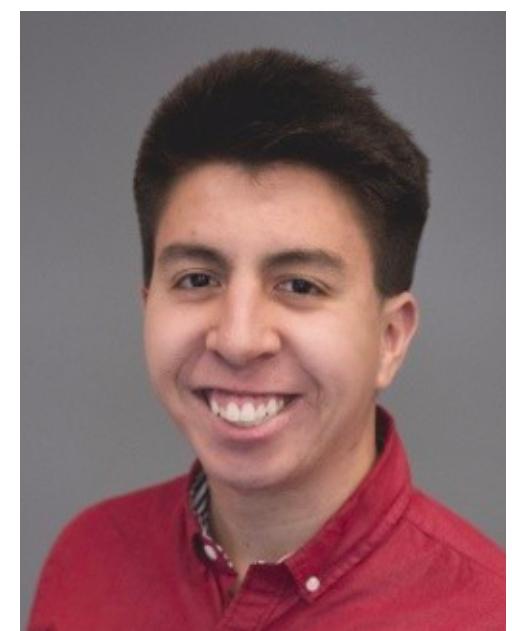
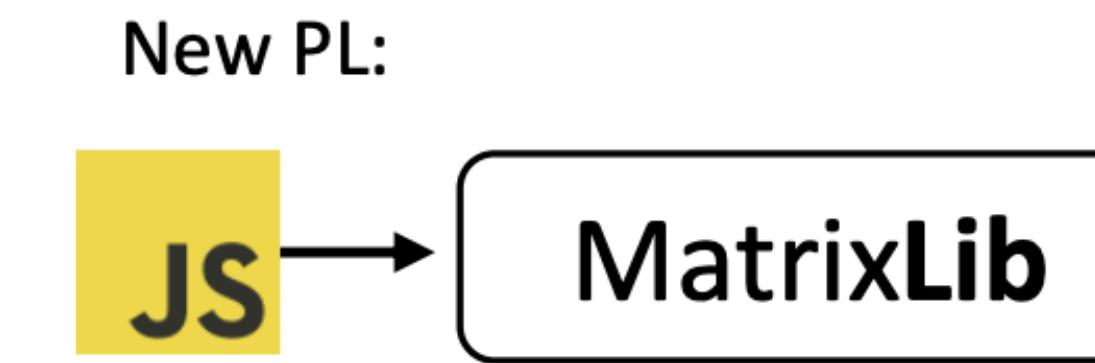
**Goal:** Automate Morpheus itself to many PLs in a unified way

**Idea:** Exploit GraalVM, an industrial-strength *Polyglot* compiler + runtime for data science workloads (R, Py, Javascript, etc.)

## World without Trinity



## World with Trinity



*Learn more about Trinity from David Justo at 3:30pm today!*

# Outline

4m

Introducing ML over Joins

4m

Orion: Factorized ML

10m

Morpheus and Extensions

4m

Roadblocks and Musings

# Roadblocks for Factorized ML

# Roadblocks for Factorized ML

**Observation:** Factorized ML yet to have big practical impact on any path. :-/

# Roadblocks for Factorized ML

**Observation:** Factorized ML yet to have big practical impact on any path. :-/

**Reason 1:** Applicability to *business-critical* ML algorithms limited

Tree ensembles rule tabular data; factorized ML gains marginal there

GLMs, clustering, etc. often not big bottleneck in real-world pipelines

# Roadblocks for Factorized ML

**Observation:** Factorized ML yet to have big practical impact on any path. :-/

**Reason 1:** Applicability to *business-critical* ML algorithms limited

Tree ensembles rule tabular data; factorized ML gains marginal there

GLMs, clustering, etc. often not big bottleneck in real-world pipelines

# Roadblocks for Factorized ML

**Observation:** Factorized ML yet to have big practical impact on any path. :-/

**Reason 1:** Applicability to *business-critical* ML algorithms limited

Tree ensembles rule tabular data; factorized ML gains marginal there

GLMs, clustering, etc. often not big bottleneck in real-world pipelines

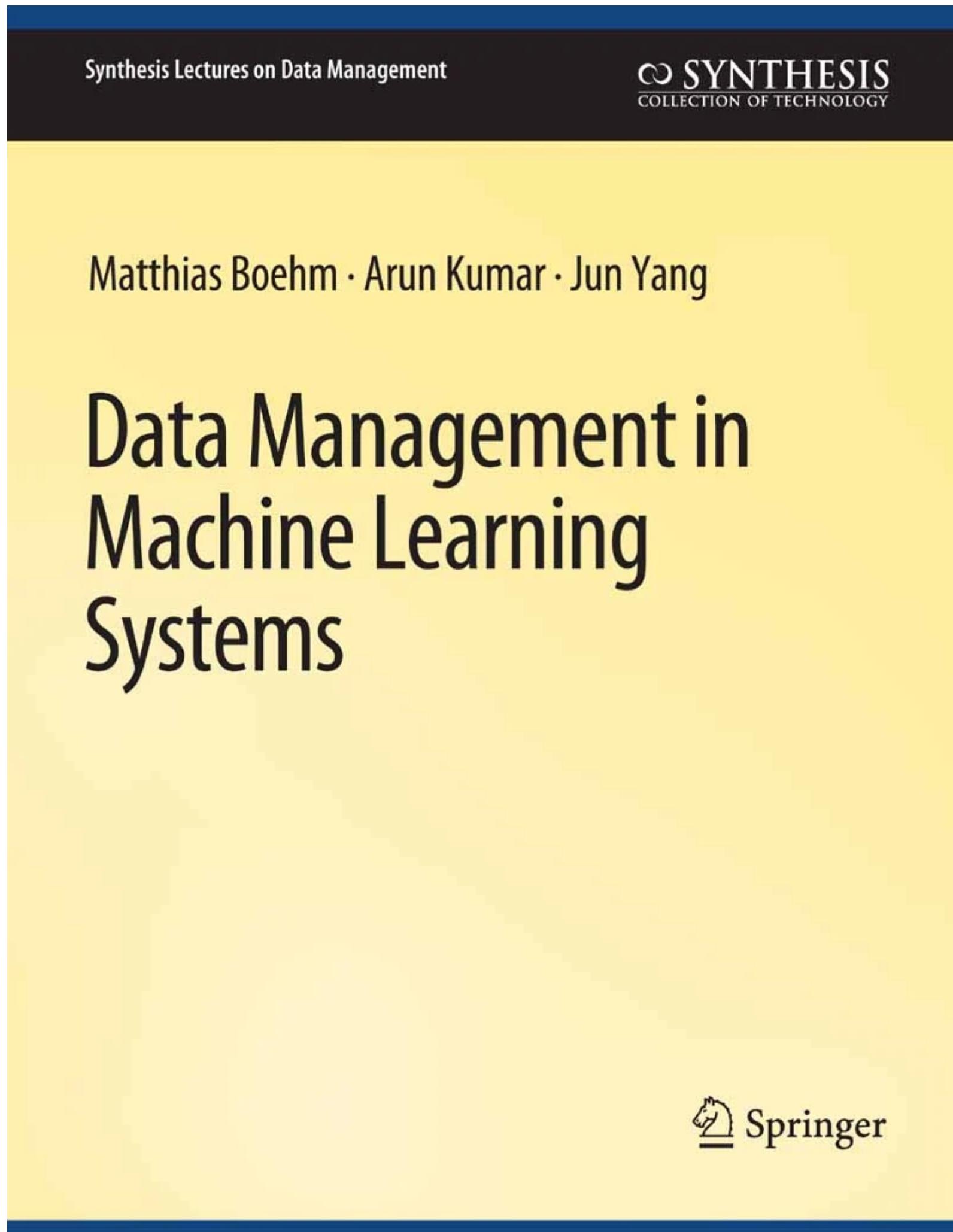
**Reason 2:** *Implementation* effort to make it practical still non-trivial

Orion-style: UDFs too complex to implement/maintain on RDBMS/Spark

Morpheus-style: ML not always written as LA scripts; hidden C++ callouts

Trinity-style: Likely promising; over the wall at Oracle now! :)

# Plug: First Textbook on ML Systems



## Table of Contents

- Introduction
- ML Through Database Queries and UDFs
- Multi-Table ML and Deep Systems Integration
- Rewrites and Optimization
- Execution Strategies
- Data Access Methods
- Resource Heterogeneity and Elasticity
- Systems for ML Lifecycle Tasks
- Conclusions
- Bibliography
- Authors' Biographies

<https://tinyurl.com/MLSystemsBook>

<https://adalabucsd.github.io>

arunkk@eng.ucsd.edu



[github.com/ADALabUCSD](https://github.com/ADALabUCSD)



@TweetAtAKK

ACKS:

