數位影像處理 Digital Image Processing

Chapter 3 Spatial Filtering

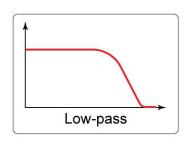
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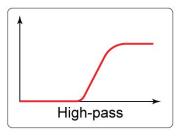
3 空間濾波 Spatial Filtering

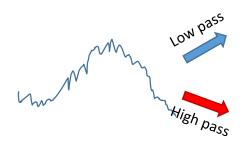
- 1. 簡介
- 2. 空間濾波技術
- 3. 空間相關性與迴旋積
- 4. 平滑空間濾波器

1. 簡介

- · 濾波器(filter)一詞是從頻域(frequency domain)發展而來。
- 濾波:指接受(通過)或拒絕某些頻率成分
 - -高通濾波器(highpass filter)只讓高頻成分通過
 - -低通濾波器(lowpass filter)只讓低頻成分通過







 空間濾波器(spatial filter):亦稱遮罩(mask)、核 心(kernel)、模板(template)、視窗(window)...

2. 空間濾波技術

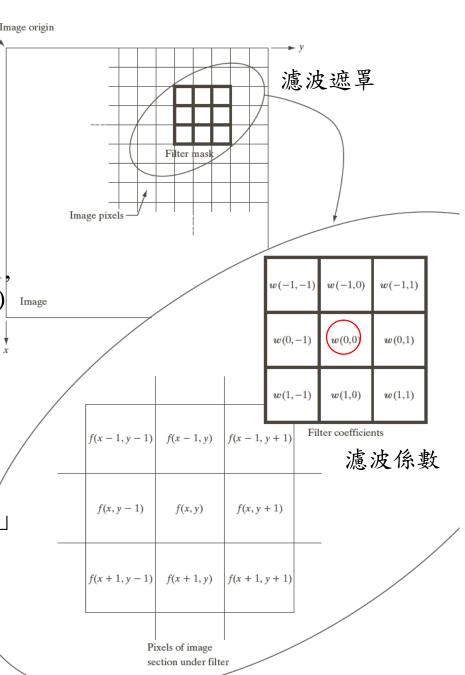
• 濾波處理:影像中的一點(x, y),其 濾波響應(response) g(x, y)是濾波係 數與濾波器所圍繞之影像像素乘績 的總和:

$$g(x, y) = w(-1,-1) f(x-1, y-1) + w(-1,0) f(x-1, y) + ... + w(0,0) f(x, y) + w(1, 1) f(x+1, y+1)$$

濾波器的中央係數w(0,0)與像素(x, y)對齊。

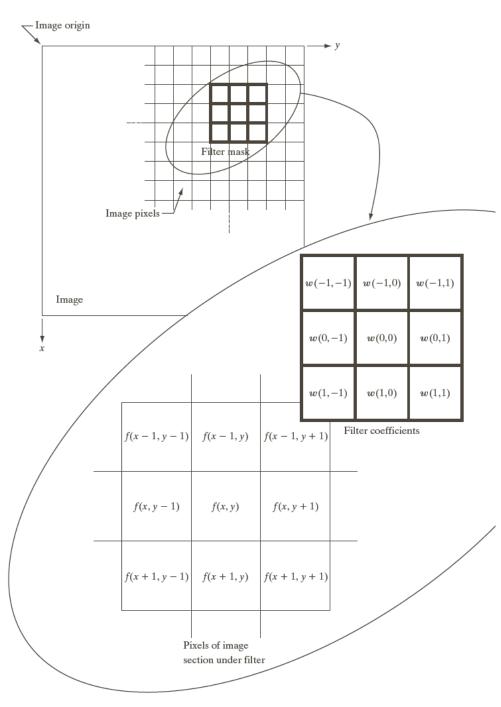
注意

- 濾波計算過程需有一張「新的影像」儲存結果。
- 很少把濾波後的像素取代原影像中 對應位置上的值,因為當濾波還在 執行時,這會改變影像的內容。



3. 空間相關性與迴旋積

- 相關性(correlation):如上頁 之運算,把濾波遮罩在影像 上移動,並在每個位置上計 算乘積的和。
- g(x, y) = w(-1,-1) f(x-1, y-1)+ w(-1,0) f(x-1, y)+... + w(0,0) f(x, y)+ w(1, 1) f(x+1, y+1)
- 迴旋積(convolution):計算 方式相同,但濾波器要先旋 轉180度。



Correlation

Convolution

一維範例 f: function w: filter

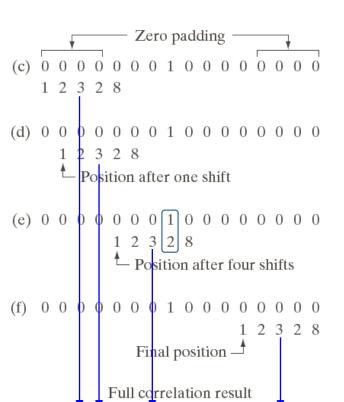


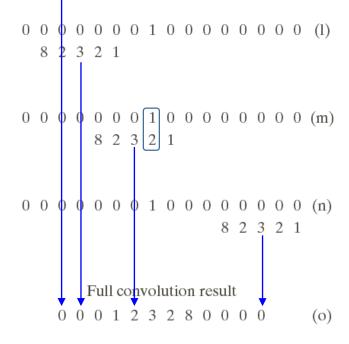




0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 (k)

8 2 3 2 1





Cropped correlation result

0 0 0 8 2 3 2 1 0 0 0 0

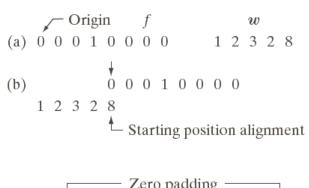
Cropped convolution result
0 1 2 3 2 8 0 0

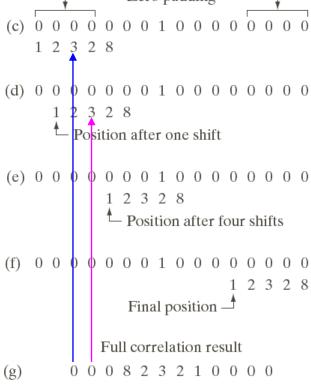
(g)

Correlation

3. 空間相關性與迴旋積

- 相關性是濾波器位移(displacement)的函數
 - -相關性第一個值對應濾波器的零位移
 - 第二個值對應到一個單位的位移
- 一個濾波器w與一個有單一個1,其它為0的 函數(稱「離散單位脈衝」discrete unit impulse)進行相關性運算後,得到一旋轉180 度的w。
- 若將濾波器先作旋轉,則能在脈衝處產生與 原函數一樣的訊號→迴旋積

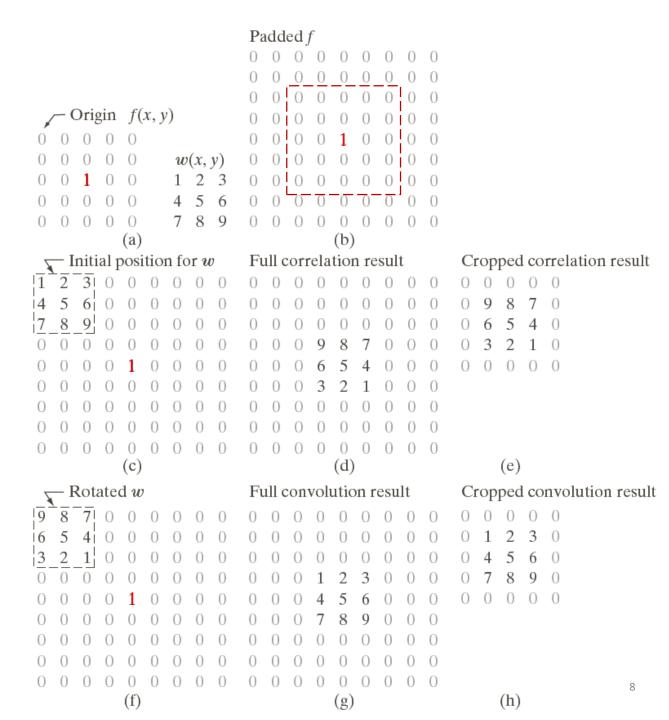




Cropped correlation result

(h) 0 8 2 3 2 1 0 0

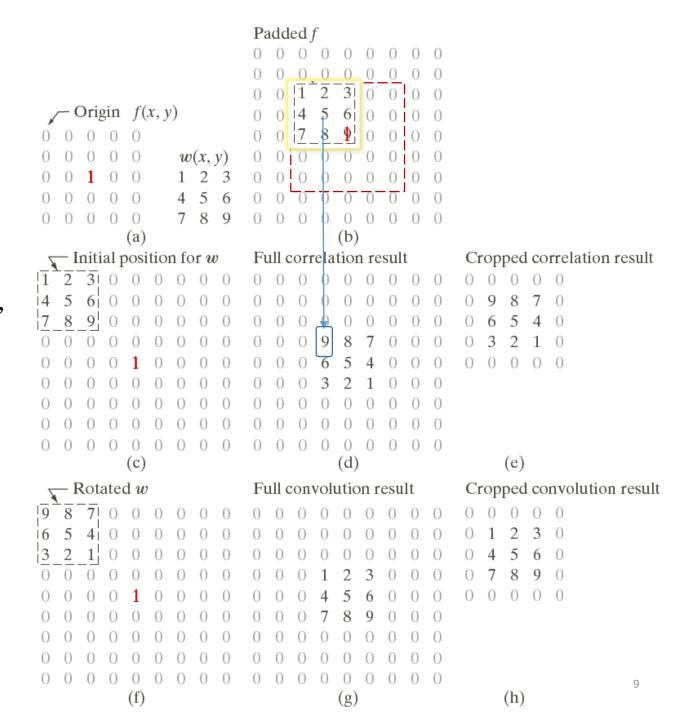
二維範例 f: function w: filter



二維範例

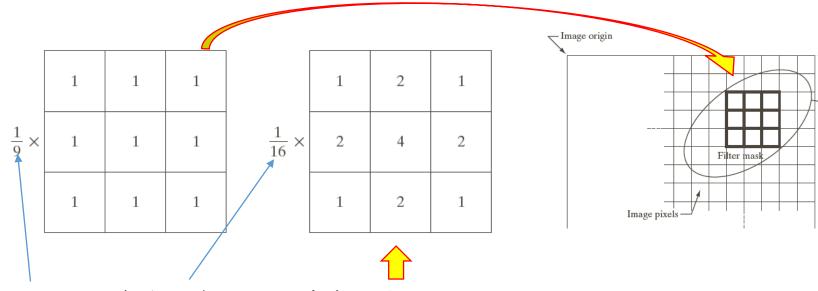
f: function *w*: filter

- 若濾波遮罩是對稱的, 則相關性與迴旋積會 有相同結果。
- •在一些文獻中可能會 提到「將影像與遮罩 作迴旋積」,但可能 指的是前述「滑動 指積和」的過程。



4. 平滑空間濾波器

- · 平滑(smoothing)濾波器用於模糊化與減少雜訊
- 平均濾波器(averaging filter)→線性濾波器

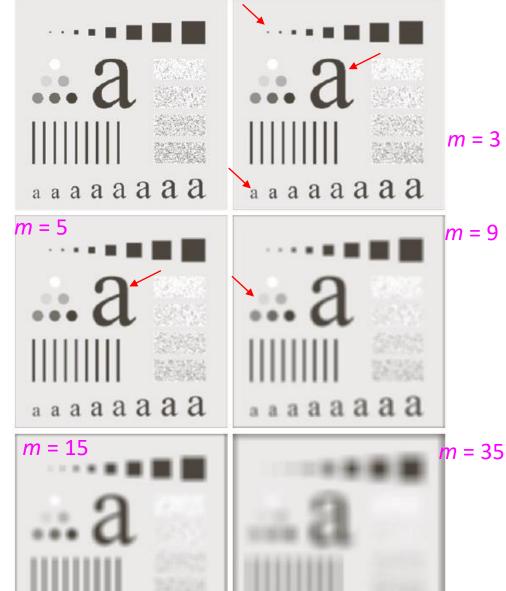


正規化,讓總和為1。

權重平均(weighted average), 給某些像素更高的重要性 (權重)

4. 平滑空間濾波器

- 原影像:500x500
- 正方形平均濾波器
- 遮罩邊長 m = 3, 5, 9, 15, 35
- 圖上端黑正方形大小: 3,5,9,25,35,45,55。間隔25像素。
- m=3,輕微模糊,與遮罩同樣大小的細節影像較大。字元鋸齒邊緣被平滑化。
- *m*=5,類似,模糊略增。
- m=9,黑圈已不易與背景區分。
- m=15 and 35, 小方塊、圓圈、 雜訊矩形已混合到背景中。



OpenCV: Image Blur - Average

- Smooth an image by replacing each pixel by the average pixel value computed over a rectangular neighborhood.
- void **blur**(InputArray **src**, OutputArray **dst**, **Size ksize**, Point **anchor**=Point(-1,-1), int **borderType**=BORDER_DEFAULT)
 - src input image
 - dst output image of the same size and type as src.
 - ksize blurring kernel size.
 - anchor anchor point; default value Point(-1,-1) means that the anchor is at the kernel center.
 - borderType border mode used to extrapolate pixels outside of the image.
 - \rightarrow cv::blur(image, result, cv::Size(3,3)); $\frac{1/9}{1/9}$ $\frac{1/9}{1/9}$ $\frac{1}{1/9}$ $\frac{1}{1/9}$ $\frac{1}{1/9}$

Such a matrix is sometimes called a kernel or a mask.

OpenCV: Image Blur - Average

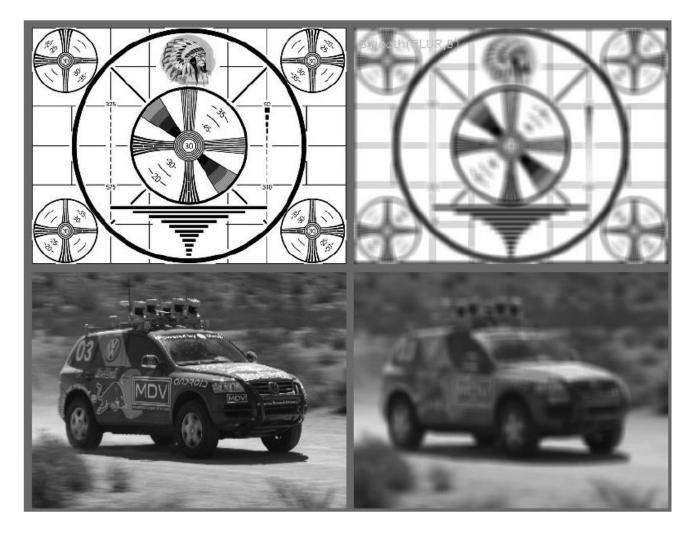


Image smoothing by block averaging

Average Blur













3*3

7*7

11*11

4. 平滑空間濾波器

 空間平均的一個重要應用:為了獲得感興趣物體的整體表示而 將一影像模糊,使較小的物體融入背景,較大物體則呈「斑點 狀」,而較易偵測到。

門檻化 (Thresholding)

• f(x, y): 像素值, g(x, y): thresholding後的結果

•
$$T$$
: 門檻值
$$g(x,y) = \begin{cases} 255, if \ f(x,y) > T \\ 0, if \ f(x,y) \le T \end{cases} \text{ or } g(x,y) = \begin{cases} 1, if \ f(x,y) > T \\ 0, if \ f(x,y) \le T \end{cases}$$



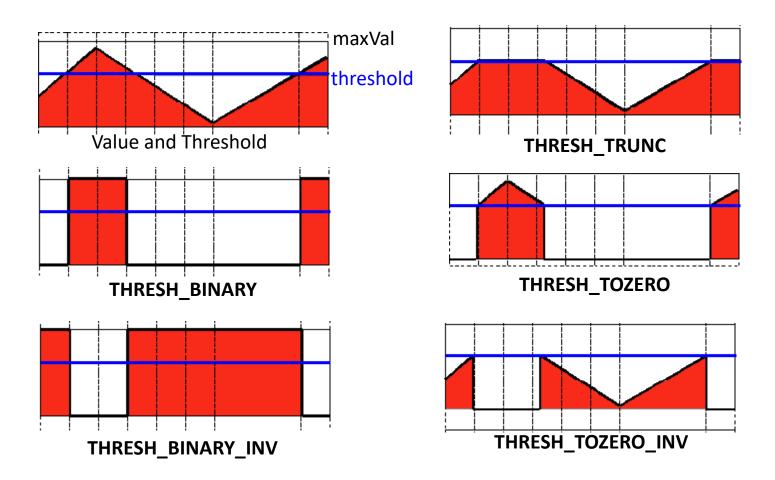




- (a)哈伯望遠鏡之太空影像, 528x485
- (b)用15x15的平均遮罩作 濾波
- (c) 對(b)做門檻化

OpenCV Threshold Types

threshold (src, dst, threshold, max_value, threshold_type);



- cvtColor (src, dst, CV_BGR2GRAY);
- threshold (src, dst, threshold, max_value, threshold_type);

cvtColor (frame, gray, CV_BGR2GRAY);



frame (3 channels)



gray (1 channel)

- cvtColor (src, dst, CV_BGR2GRAY);
- threshold (src, dst, threshold, max_value, threshold_type);

threshold (gray, white, 200, 255, THRESH_BINARY);



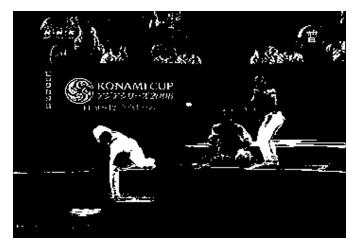
HINTER TO STATE OF THE STATE OF

gray

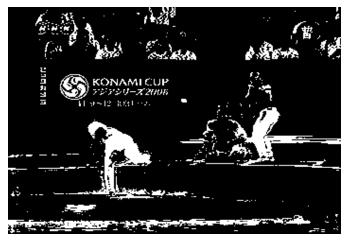
White (threshold = 200)

• Different thresholds





(threshold = 200)



(threshold = 180)







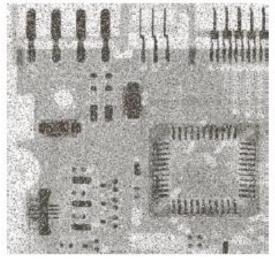


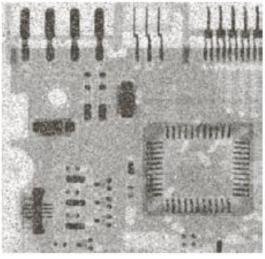


4. 平滑空間濾波器

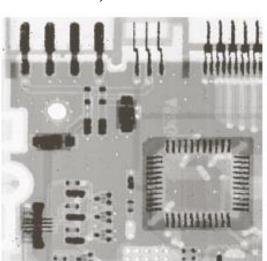
非線性濾波器

- 以中值濾波器(median filter)最常用
- 在一遮罩內,取中間值當作結果。
- 有效去除脈衝雜訊(impose noise), 因為在影像上脈衝雜訊看起來有黑點 與白點,又稱椒鹽雜訊(salt-and-pepper noise)









23, 23, 24, 25, 25, 27, 27, 30, 235

Median = 25

Avg = 48.8

3x3 median filter

Image Blur - Median

- The median filter replaces each pixel by the median or "middle" pixel (as opposed to the mean pixel) value in a square neighborhood around the center pixel.
- void **medianBlur**(InputArray **src**, OutputArray **dst**, int **ksize**)
 - src input image.
 - − **dst** − output image of the same size and type as src.
 - **ksize** aperture linear size; it must be odd and greater than 1, for example:

3, 5, 7 ...

It is int \rightarrow square kernal

→ cv::medianBlur(image, result, 5);

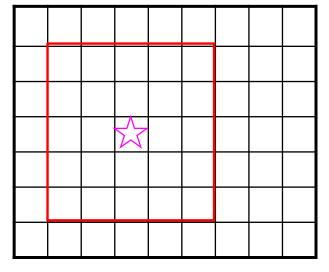
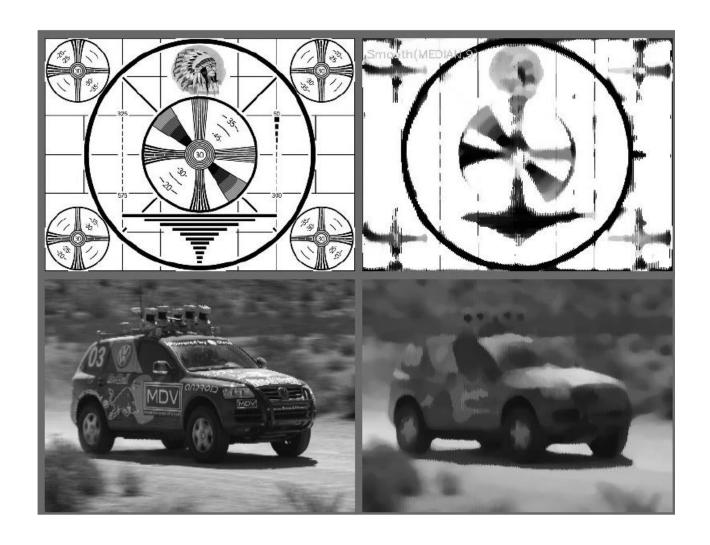


Image Blur - Median



Median Blur





1	1	1	1	1	1
1	2	3	1	1	3
1	1	1	1	1	1

挑出眾數=1



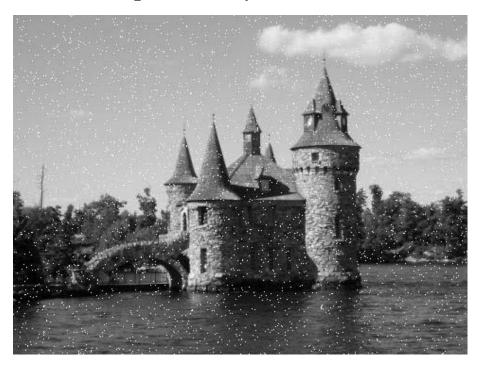




25

Image Blur - Median

- Simple blurring by averaging can be sensitive to image noise, especially large isolated outlier points.
- Median filtering is able to ignore the outliers by selecting the middle points.
 - particularly useful to combat salt-and-pepper noise



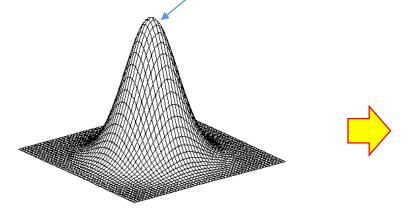


OpenCV Functions

Image Blur – Gaussian filter

- Gaussian filtering is probably the most useful.
 - convolve each point in the input array with a Gaussian kernel and then summing to produce the output array.

The pixels closer to the center are weighted more.



$$h_{\sigma}(u,v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$

1	4	7	4	1
4	16	26	16	4
7	26	41	26	7
4	16	26	16	4
1	4	7	4	1

5x5 kernel,
$$\sigma_x = \sigma_v = 1$$

Recall → 4. 平滑空間濾波器

- · 平滑(smoothing)濾波器用於模糊化與減少雜訊
- 平均濾波器(averaging filter)→線性濾波器

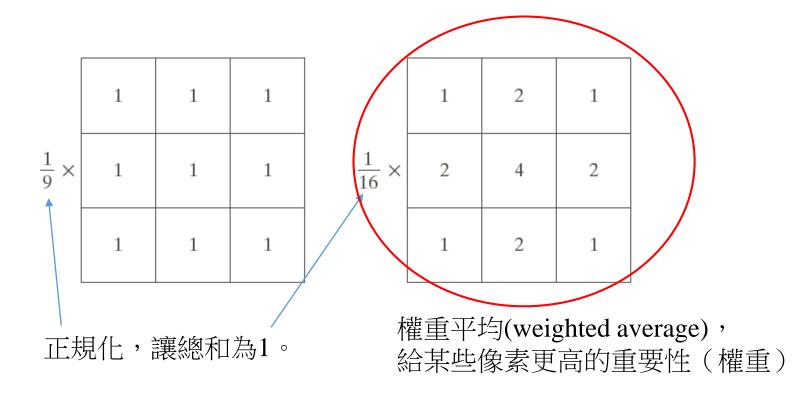


Image Blur – Gaussian filter

- void GaussianBlur(InputArray src, OutputArray dst, Size ksize, double sigmaX, double sigmaY=0, int borderType=BORDER_DEFAULT)
 - ksize Gaussian kernel size.
 - ksize.width and ksize.height can differ but they both must be positive and odd.
 - Or, they can be zero's and then they are computed from sigma*.
 - **sigmaX** Gaussian kernel standard deviation in X direction.
 - sigmaY Gaussian kernel standard deviation in Y direction.
 - if sigmaY is zero, it is set to be equal to sigmaX
 - if both sigmas are zeros, they are computed from ksize.width and ksize.height, respectively.

$$h_{\sigma}(u,v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$

Image Blur – Gaussian filter





- Bilateral filtering → edge-preserving smoothing.
- A typical motivation for Gaussian smoothing:
 - pixels in a real image should vary slowly over space and thus be correlated to their neighbors
 - random noise can be expected to vary greatly from one pixel to the next (i.e., noise is spatially uncorrelated).
- It is in this sense that Gaussian smoothing reduces noise while preserving signal.
- Unfortunately, this method breaks down near edges, where you do expect pixels to be uncorrelated with their neighbors.
 - →Gaussian smoothing smoothes away the edges.



- Like Gaussian smoothing, bilateral filtering constructs a weighted average of each pixel and its neighboring components.
- The weighting has two components:
 - the first is the same weighting used by Gaussian smoothing, based on the spatial distance from the center pixel
 - The second is also a Gaussian weighting but is based on the difference in intensity from the center pixel.
- You can think of bilateral filtering as Gaussian smoothing that weights more similar pixels more highly than less similar ones.
- The effect of this filter is typically to turn an image into what appears to be a watercolor painting of the same scene.
- This can be useful as an aid to segmenting the image.

Comparison – Gaussian filter













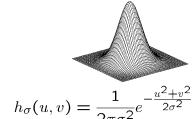








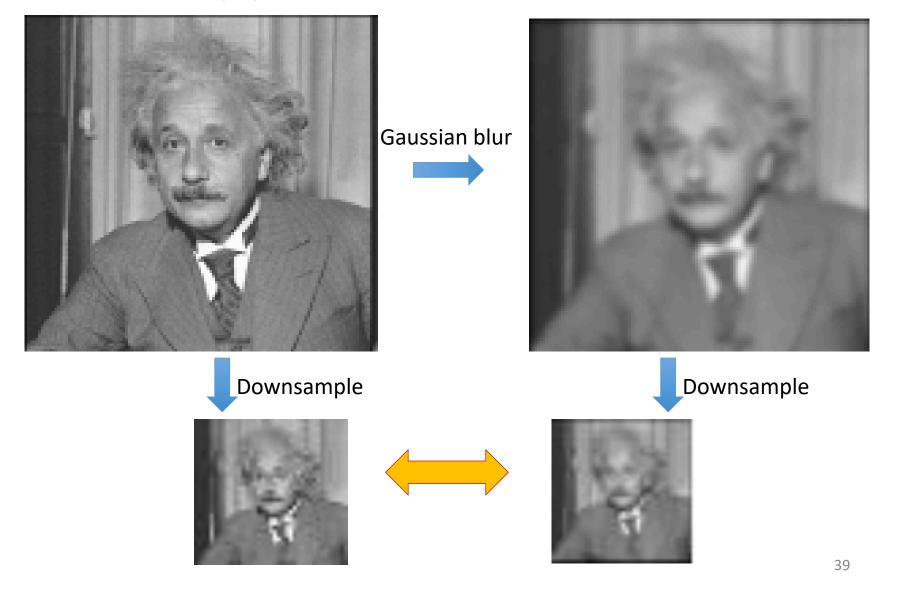




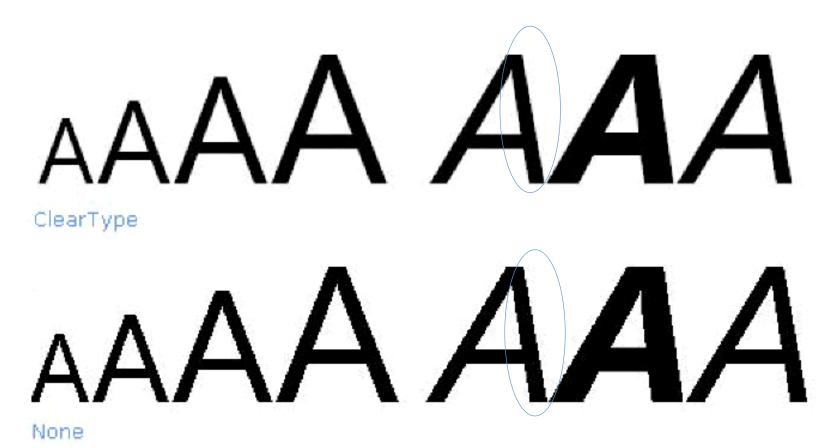
- void bilateralFilter(InputArray src, OutputArray dst, int d, double sigmaColor, double sigmaSpace, int borderType=BORDER_DEFAULT)
 - **d** Diameter of each pixel neighborhood that is used during filtering.
 - → Large filters (d > 5) are very slow. Recommend: use d=5 for real-time applications.
 - sigmaColor Filter sigma in the color space. A larger value of the parameter means that farther colors within the pixel neighborhood will be mixed together, resulting in larger areas of semi-equal color.
 - **sigmaSpace** Filter sigma in the coordinate space. A larger value of the parameter means that farther pixels will influence each other as long as their colors are close enough.
 - → For simplicity, you can set the 2 sigma values to be the same.

If they are small (< 10), the filter will not have much effect, whereas if they are large (> 150), they will have a very strong effect, making the image look "cartoonish".

Some applications



Clear Type Font



Clear Type Font

Two Fairy Tales

1

Two Fairy Tales

 \neg

The Emperor's New Clothes

The Emperor's New Clothes

Many years ago, there was an Emperor who was so excessively fond of new clothes that he spent all his money on dress. He did not trouble himself in the least about his soldiers; nor did

Many years ago, there was an Emperor who was so excessively fond of new clothes that he spent all his money on dress. He did not trouble himself in the least about his soldiers; nor did

without ClearType*

with ClearType*

Appendix: Integral Image

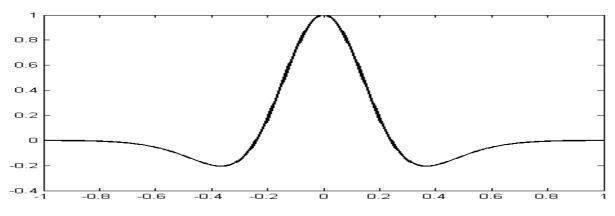
- 單純套用Filter計算次數太多
- Ex: 512*512的圖,套用7*7 Filter,需要:
 - 對512*512的每個pixel執行
 - 49次乘法, 49次加法
 - 對於即時運算需求(例如即時影片中的物件追蹤)是件大問題

• Hint:能不能預先計算好一部分的資料?



Integral Image

- 對於某些用途的Filter,我們簡化計算方式
 - Ex: DoG (Difference of Gaussian)



$$[0 \ -0.01 \ -0.02 \ -0.2 \ 0 \ 1 \ 0 \ -0.2 \ -0.02 \ -0.01 \ 0]$$



Integral Image

• 如此一來,原本的矩陣乘法問題就變成區塊加法問題

1	2	2	1	1	2
2	2	2	4	1	2
2	2 3 4 4 0 0				
2	2	4	4	0	0
2	4	5	4	1	1
1	2	2	2	2	2

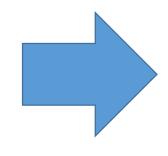


Next:怎麼減少加法的計算次數?

Integral Image

• 將圖片預先累加好

1	2	2	4	1	2
2	2	2	4	1	2
2	3	4	4	0	0
2	2	4	4	0	0
2	4	5	4	1	1
1	2	2	2	2	2



1	3	5	9	10	12
3	7	11	19	21	25
5	12	20	32	34	38
7	16	28	44	46	50
9	22	39	59	62	67
10	25	44	66	71	78

• Q&A