

PRDP: Proximal Reward Difference Prediction for Large-Scale Reward Finetuning of Diffusion Models

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A painting of a girl standing on a mountain looking out at an approaching storm over the ocean, with wind blowing and ocean mist, surrounded by lightning.



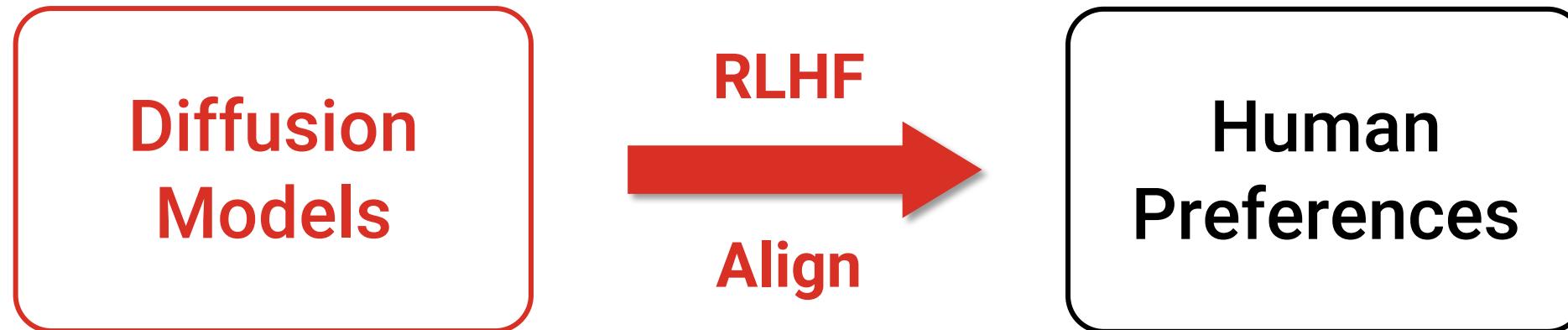
Aligning with Human Preferences

- Numerous products

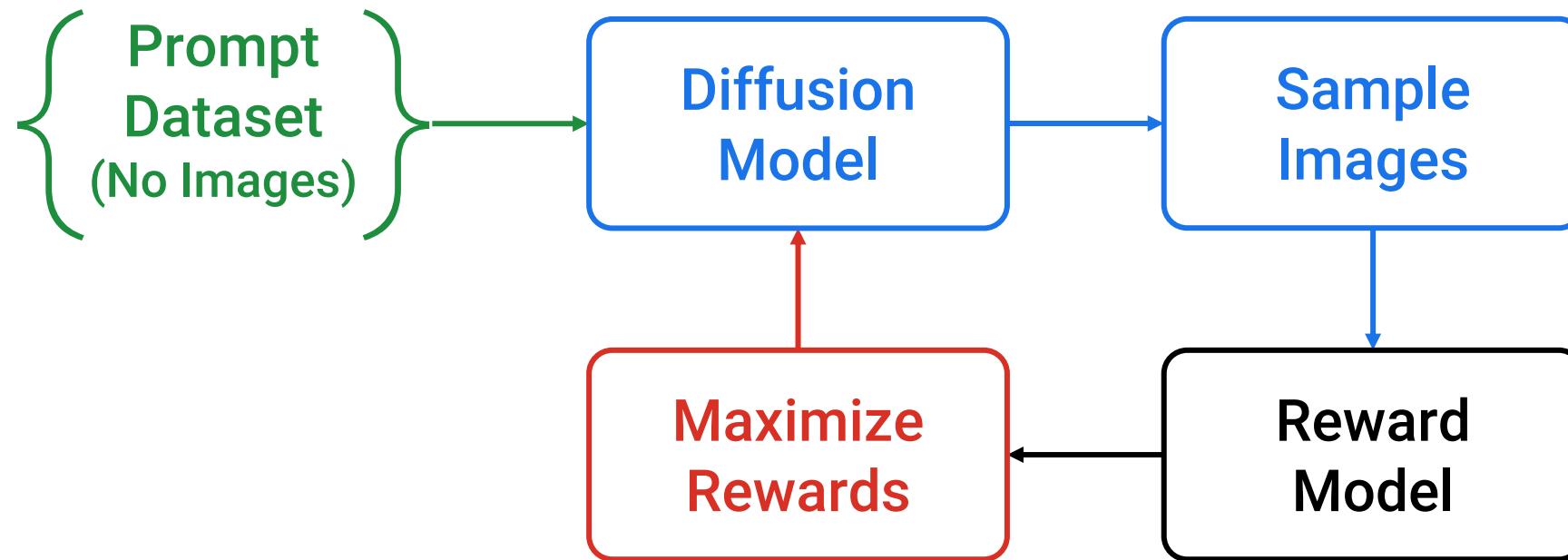


Aligning with Human Preferences

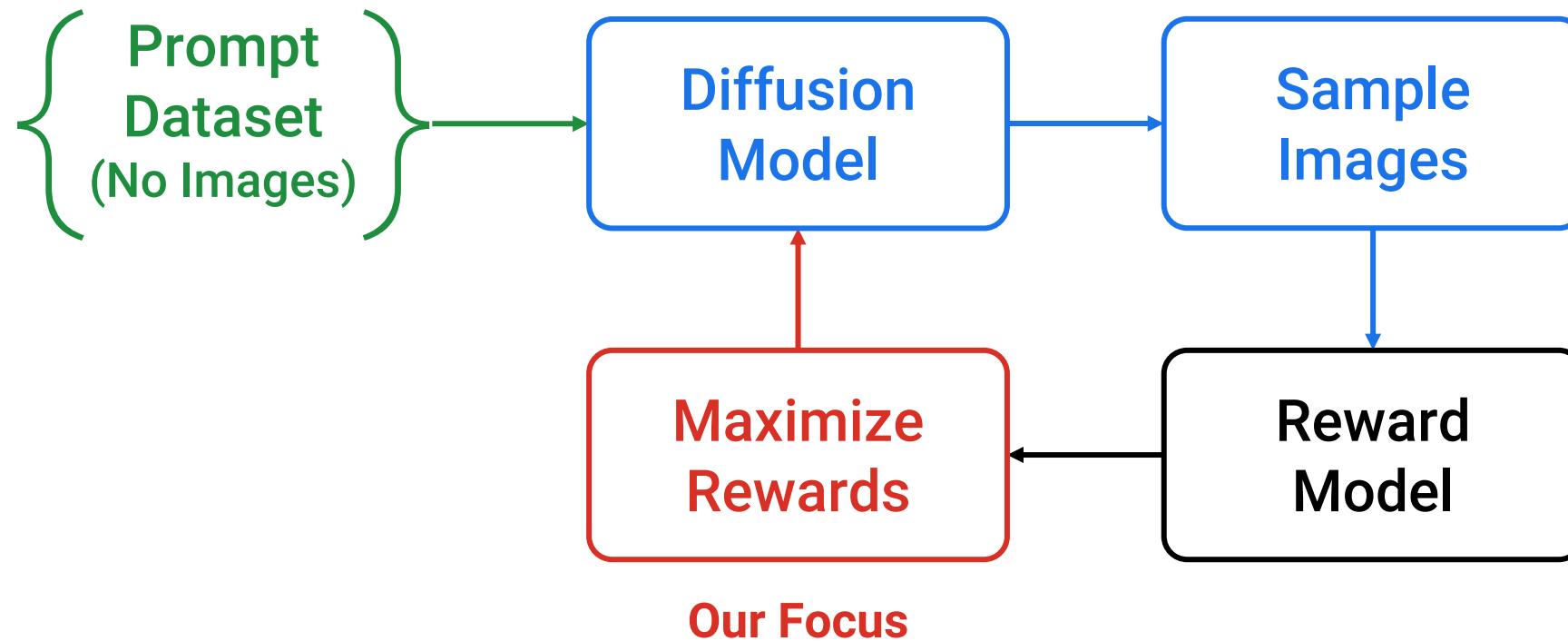
- Our paper



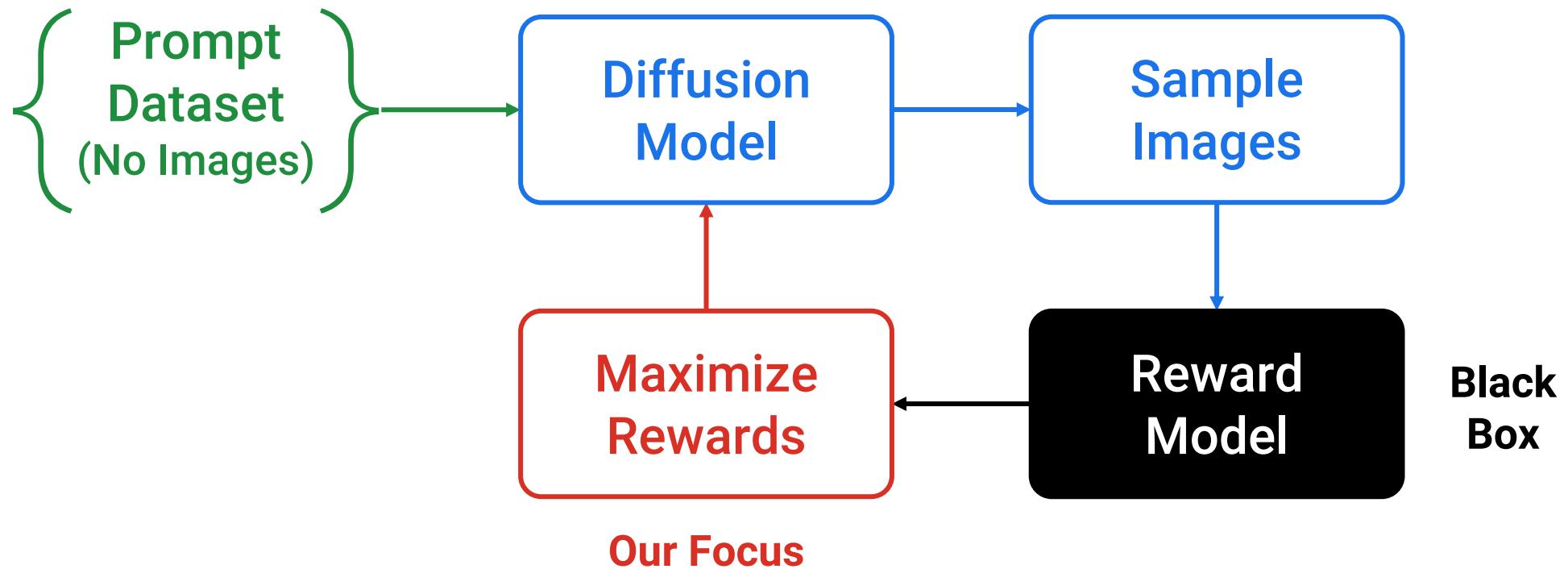
RLHF Pipeline



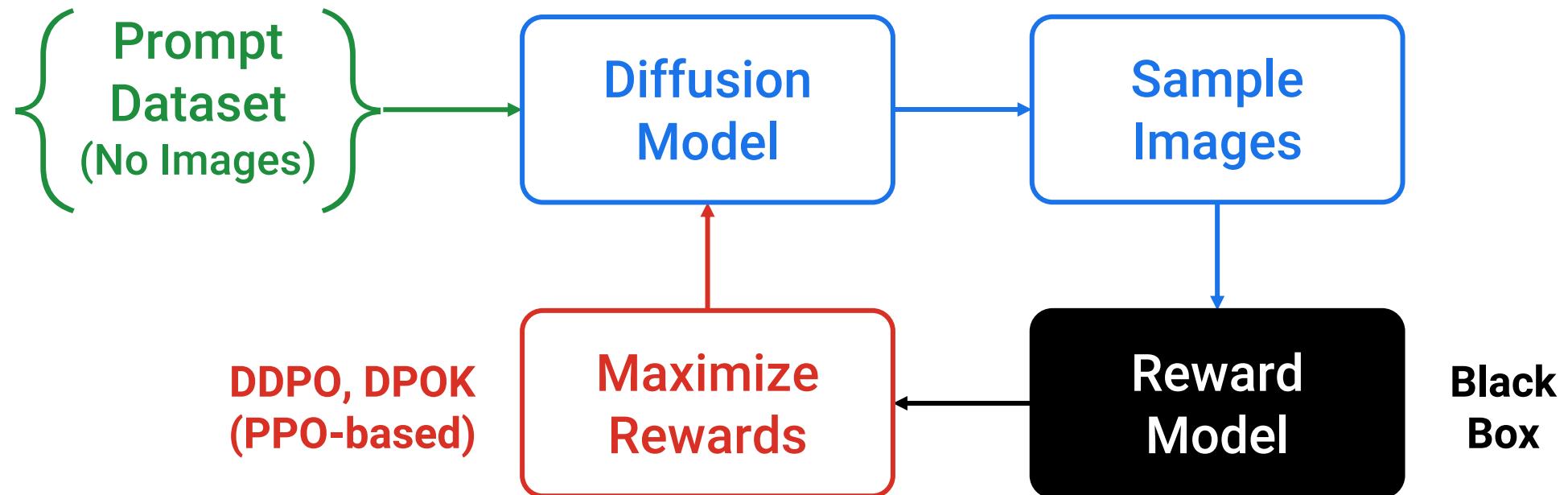
RLHF Pipeline



RLHF Pipeline



RLHF Pipeline

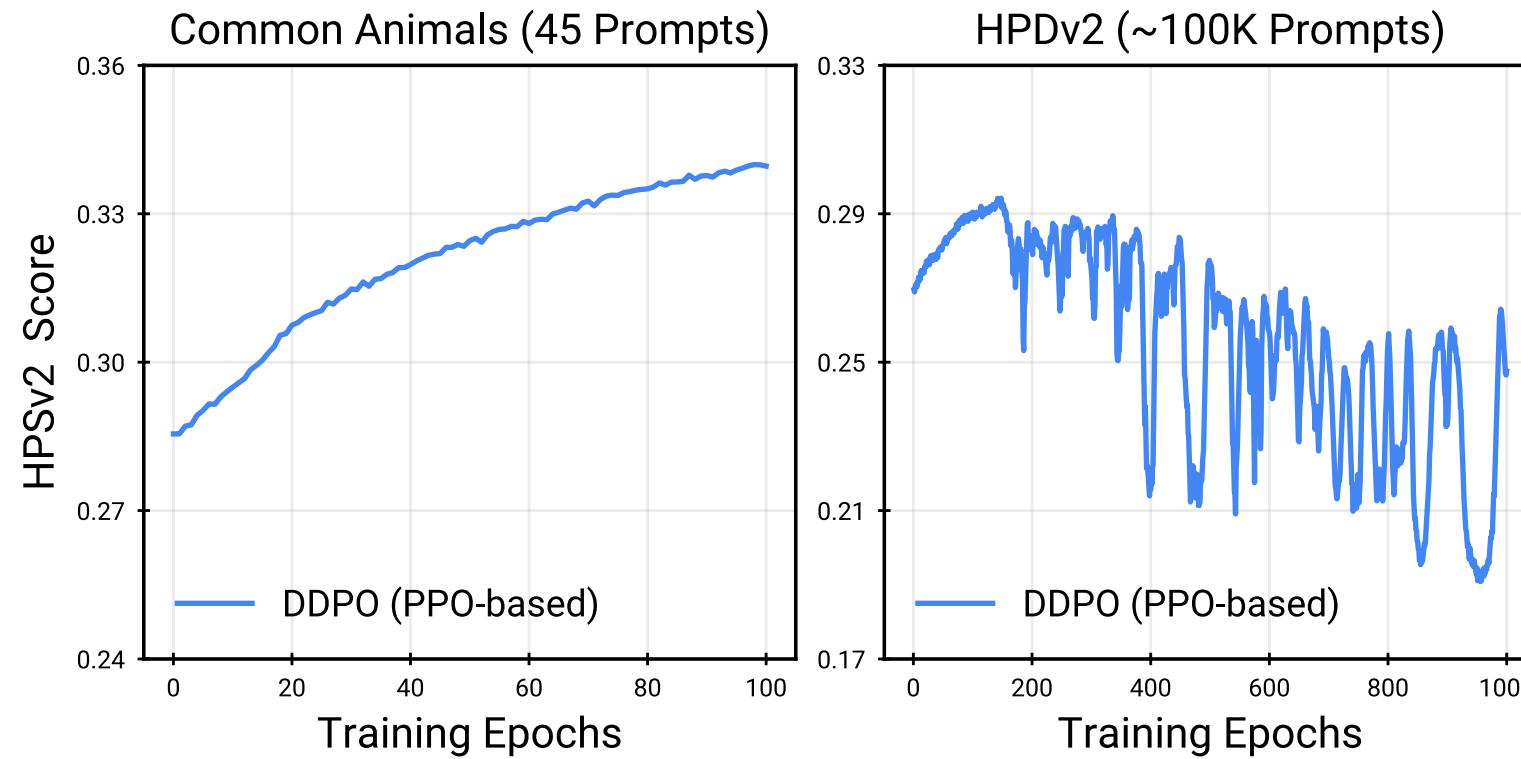


Black et al. Training Diffusion Models with Reinforcement Learning. *ICLR 2024*.

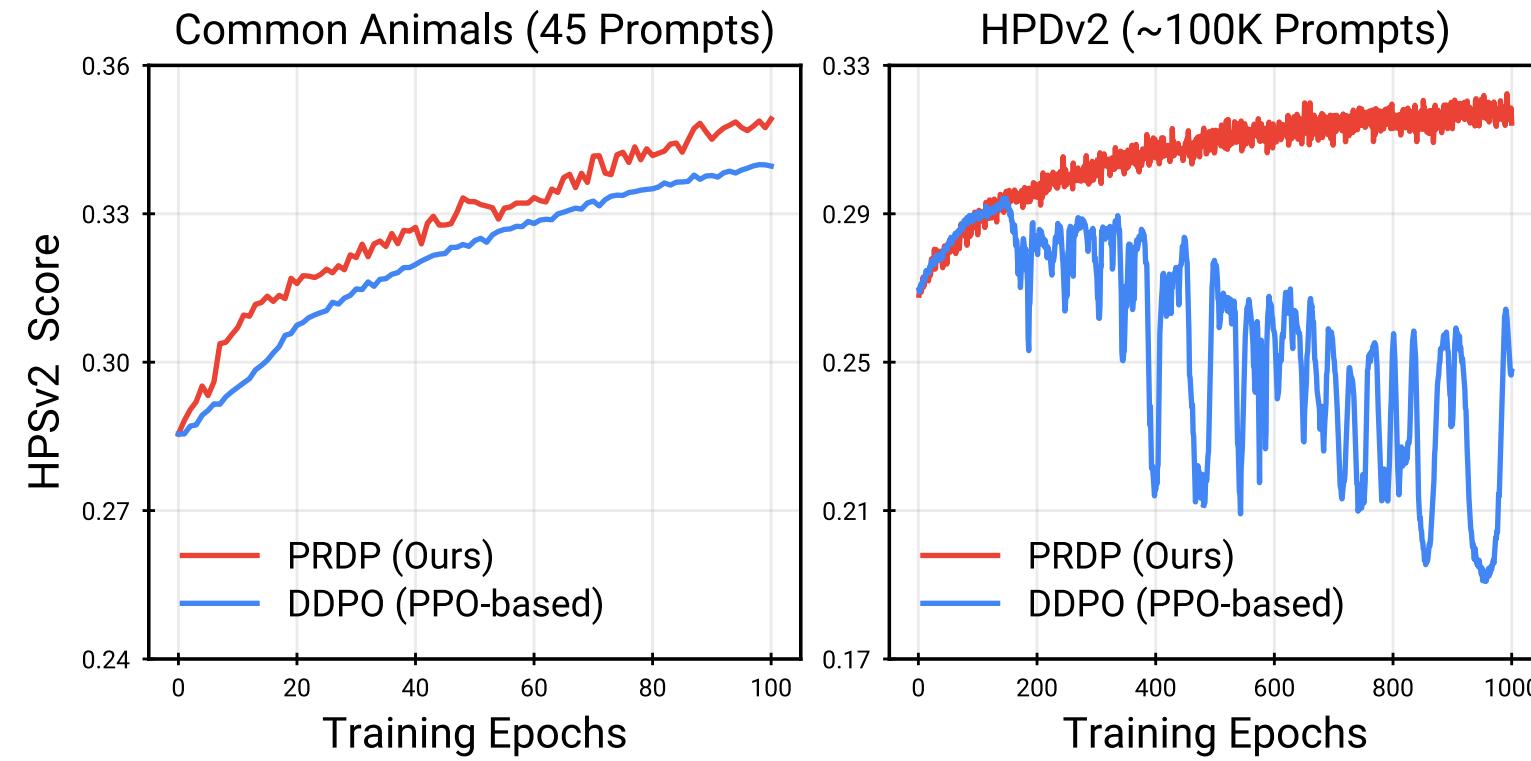
Fan et al. DPOK: Reinforcement Learning for Fine-tuning Text-to-Image Diffusion Models. *NeurIPS 2023*.

Schulman et al. Proximal Policy Optimization Algorithms.

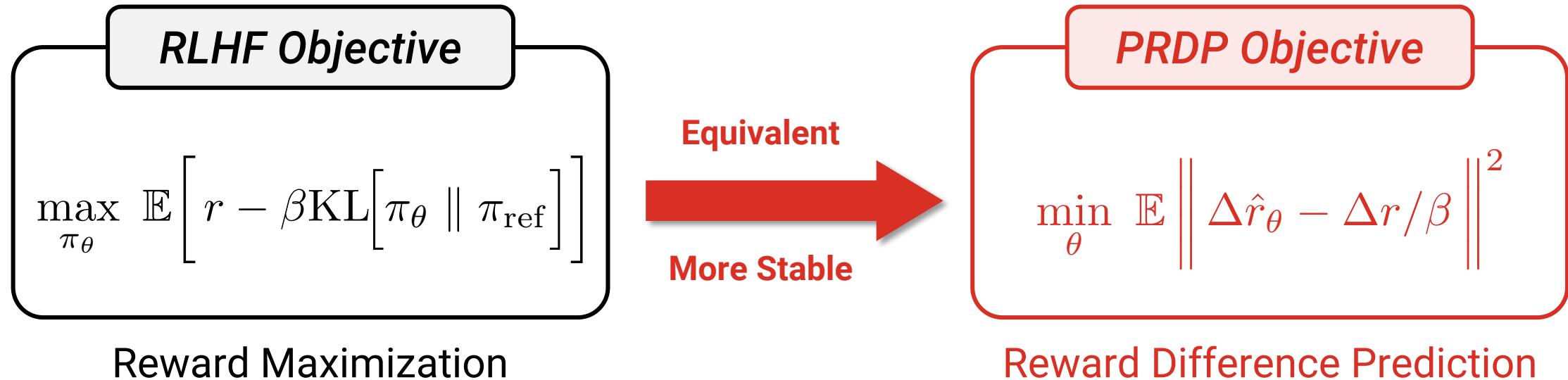
Previous Methods: Unstable at Large Scale



Our Contribution: Stable Large-Scale Training



Method Overview: Novel Training Objective



RLHF Objective

$$\pi_{\theta^*} = \arg \max_{\pi_\theta} \mathbb{E}_{\mathbf{c} \sim p(\mathbf{c})} \left[\mathbb{E}_{\substack{\mathbf{x}_{0:T} \sim \pi_\theta \\ \text{Diffusion Model}}} \left[\frac{\text{Denoising Trajectory}}{r(\mathbf{x}_0, \mathbf{c})} \right] \right]$$

Optimal Solution

$$\pi_{\theta^*}(\mathbf{x}_{0:T} | \mathbf{c}) = \frac{1}{Z(\mathbf{c})} \pi_{\text{ref}}(\mathbf{x}_{0:T} | \mathbf{c}) \exp\left(\frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c})\right)$$

Intractable

Optimal Solution

$$\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c}) = \frac{1}{Z(\mathbf{c})} \pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c}) \exp\left(\frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c})\right)$$

Intractable



Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c})} = \frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c}) - \log Z(\mathbf{c})$$

Optimal Solution

$$\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c}) = \frac{1}{Z(\mathbf{c})} \pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c}) \exp\left(\frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c})\right)$$

Intractable



Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c})} = \frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c}) - \log Z(\mathbf{c})$$

Cancel logZ by considering
two denoising trajectories

Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}|\mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}|\mathbf{c})} = \frac{1}{\beta} r(\mathbf{x}_0, \mathbf{c}) - \log Z(\mathbf{c})$$

Cancel logZ by considering
two denoising trajectories



Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}^a|\mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}^a|\mathbf{c})} - \log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}^b|\mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}^b|\mathbf{c})} = \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\beta}$$

Equivalent Condition

$$\log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}^a | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}^a | \mathbf{c})} - \log \frac{\pi_{\theta^*}(\mathbf{x}_{0:T}^b | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T}^b | \mathbf{c})} = \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\beta}$$



$$\hat{r}_\theta(\mathbf{x}_{0:T}, \mathbf{c}) := \log \frac{\pi_\theta(\mathbf{x}_{0:T} | \mathbf{c})}{\pi_{\text{ref}}(\mathbf{x}_{0:T} | \mathbf{c})}$$

Equivalent Condition

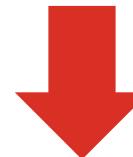
$$\underline{\hat{r}_{\theta^*}(\mathbf{x}_{0:T}^a, \mathbf{c}) - \hat{r}_{\theta^*}(\mathbf{x}_{0:T}^b, \mathbf{c})} = \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\beta}$$

Reward Difference Prediction

Equivalent Condition

$$\hat{r}_{\theta^*}(\mathbf{x}_{0:T}^a, \mathbf{c}) - \hat{r}_{\theta^*}(\mathbf{x}_{0:T}^b, \mathbf{c}) = \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\beta}$$

Reward Difference Prediction

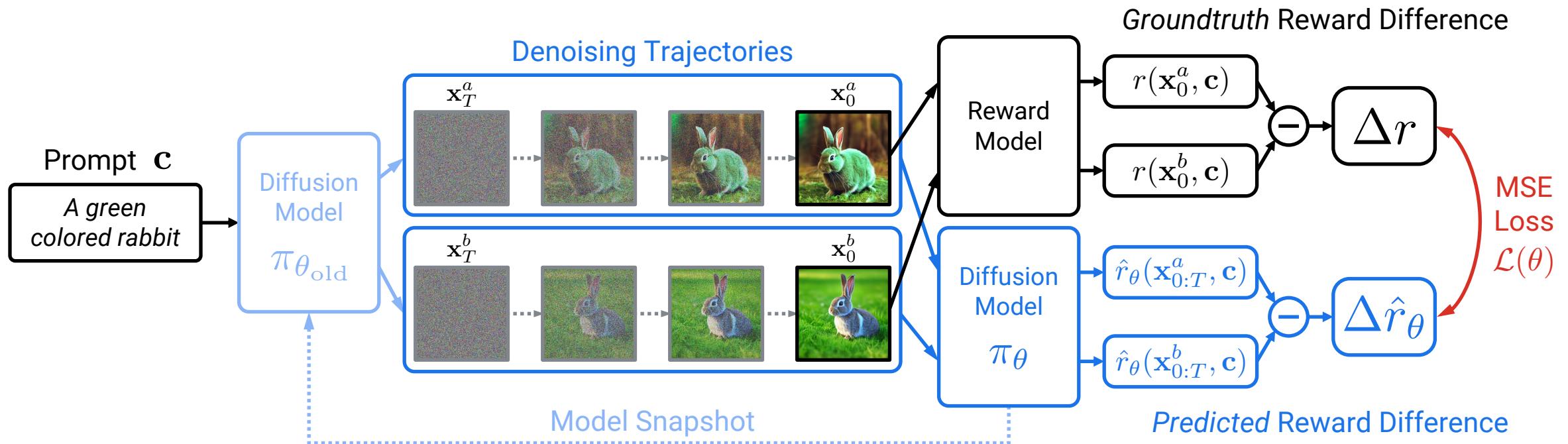


$$\pi_\theta = \pi_{\theta^*} \iff \mathcal{L}(\theta) = 0$$

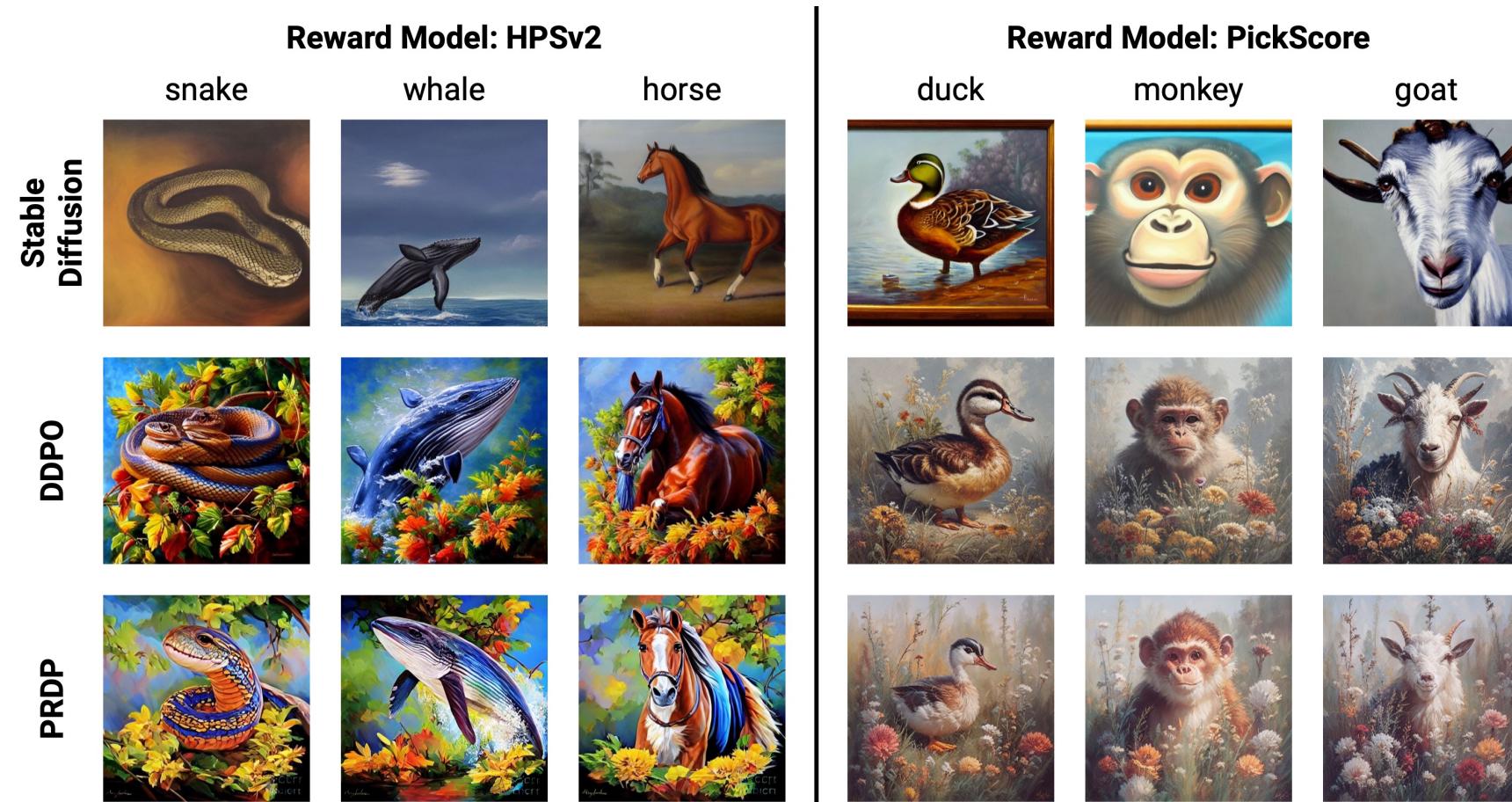
PRDP Objective

$$\mathcal{L}(\theta) = \mathbb{E}_{\mathbf{x}_{0:T}^a, \mathbf{x}_{0:T}^b, \mathbf{c}} \left\| \frac{\hat{r}_\theta(\mathbf{x}_{0:T}^a, \mathbf{c}) - \hat{r}_\theta(\mathbf{x}_{0:T}^b, \mathbf{c})}{\text{Predicted Reward Difference}} \right. \\ \left. - \frac{r(\mathbf{x}_0^a, \mathbf{c}) - r(\mathbf{x}_0^b, \mathbf{c})}{\text{Groundtruth Reward Difference}} / \beta \right\|^2$$

Online Training Pipeline



Small-Scale Training (45 Prompts)



Wu et al. Human Preference Score v2: A Solid Benchmark for Evaluating Human Preferences of Text-to-Image Synthesis.
 Kirstain et al. Pick-a-Pic: An Open Dataset of User Preferences for Text-to-Image Generation. NeurIPS 2023.

Large-Scale Training (~100K Prompts)

Reward Model: HPSv2

cinematic still of highly reflective stainless steel train in the desert, at sunset



The image is a wooden sculpture of a cute robot with cat ears, displayed in a contemporary art gallery.



A chibi frog character surfing at the beach.



Stable Diffusion

Reward Model: PickScore

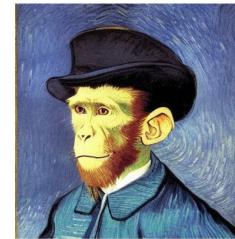
An anthropomorphic frog wizard wearing a cape and holding a wand.



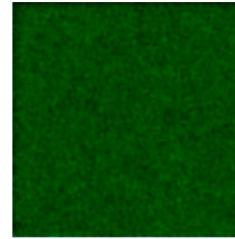
Digital art of a cherry tree overlooking a valley with a waterfall at sunset.



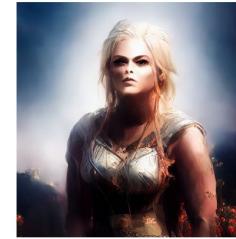
A monkey in a blue top hat painted in oil by Vincent van Gogh in the 1800s.



DDPO



PRDP



Steady Improvement in Large-Scale Training

rural house with a garden and a swimming pool



cinematic still of an adorable walking robot in the desert, at sunset



→

PRDP Training

Summary

- PRDP: Scalable diffusion model alignment
- Superior generation quality
- Generalization to unseen prompts

[Project Page](#)



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