# Shared Memory machines and OpenMP programming

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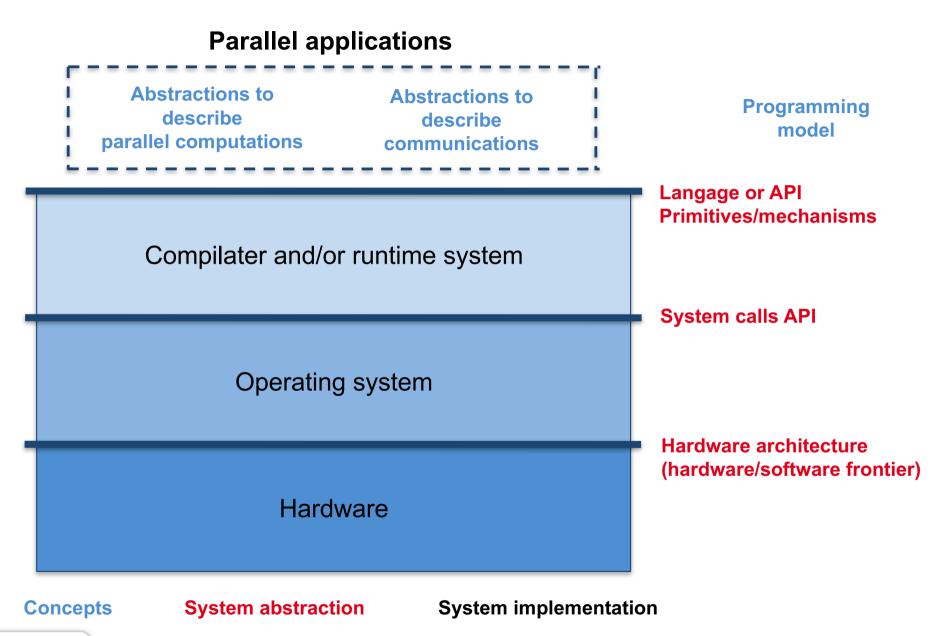


#### Some references

- OpenMP web site
  - http://www.openmp.org
  - http://www.openmp.org/specifications/
- OpenMP lecture, François Broquedis (Corse), CERMACS School 2016
  - http://smai.emath.fr/cemracs/cemracs16/programme.php
- OpenMP lecture, Françoise Roch (Grenoble)
- IDRIS lecture and lab work
  - http://www.idris.fr/formations/openmp/
- Using OpenMP, Portable Shared Memory Model, Barbara Chapman
- Parallel Programming in C with MPI and OpenMP, M.J. Quinn
- Programming Models for Parallel Computing, P. Balaji
- Parallel Programming For Multicore and Cluster System, T. Rauber, G.
   Rünger



#### Introduction





#### Introduction

Programming model: how to write (and describe) a parallel program

#### We will learn MPI (Message Passing Interface)

 The programmer manages everything (data distribution, computation distribution, processors synchronization, data exchanges)

#### Avantages

- Greater control from the programmer
- Performances (if the code is well written!)

#### Drawbacks

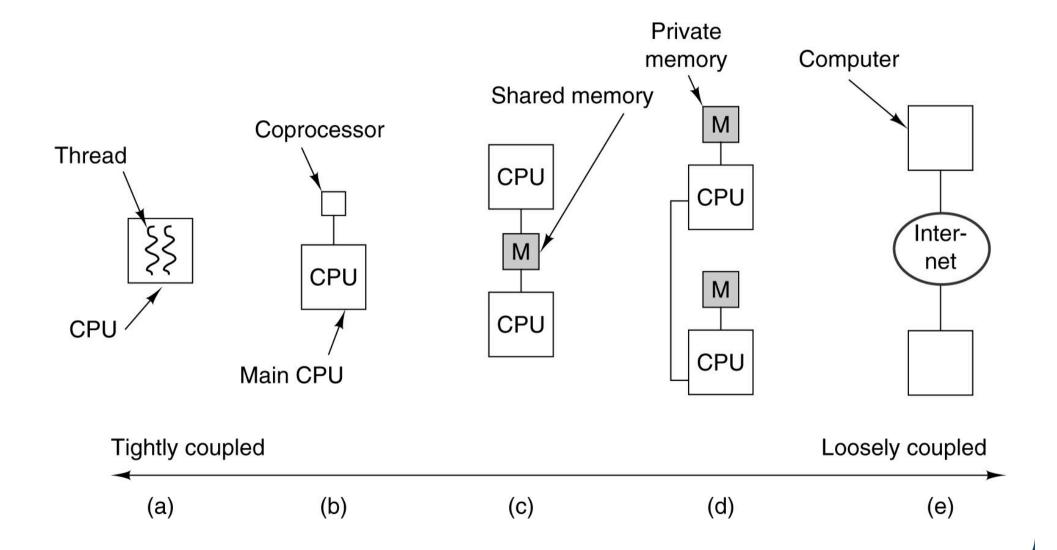
- Parallelisme assembly code
- Performance portability
- Less transparency

#### Other solution

- Give more work to the compiler and the runtime system!



#### **Parallel architectures**





# MIMD: Multiple Instructions stream, multiple data stream

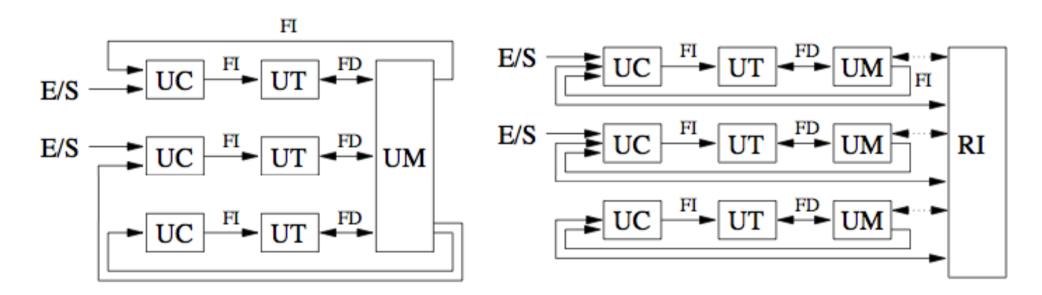
**Multi-Processor Machines** 

Each processor runs its own code asynchronously and independently

#### Two sub-classes

**Shared memory** 

#### **Distributed memory**



A mix between SIMD and MIMD: SPMD (Single Program, Multiple Data)



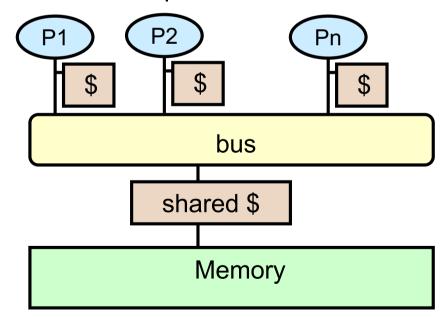
# **Shared memory machine model**

Processors are connected to a large shared memory

- Also known as *Symmetric Multiprocessors* (SMPs)
- SGI, Sun, HP, Intel, SMPs IBM
- Multicore processors (except that caches are shared)

Scalability issues for large numbers of processors

- Usually <= 32 processors
- Uniform memory access (*Uniform Memory Access*, UMA)
- Lower cost for caches compared to the main memory

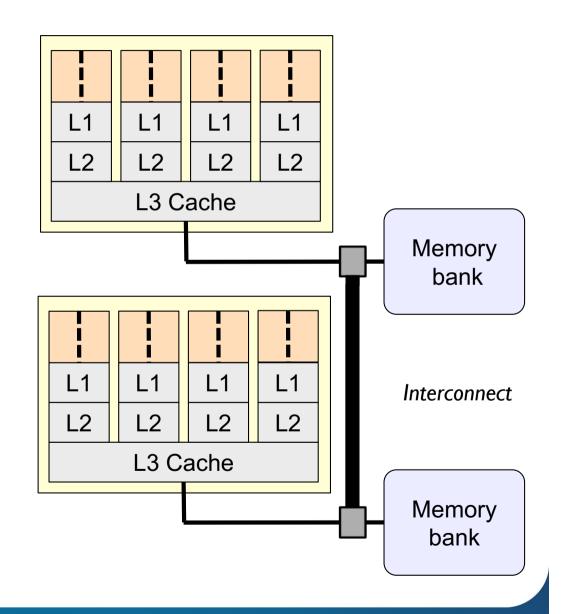


Note: \$ = cache



# HPC architecture are getting more and more hierarchical

- Parallelism is everywhere!
  - > At the architecture level
    - SMP
    - NUMA
  - At the processor level
    - Multicore chips
- Current (solid) trend: back to the cc-NUMA era
  - AMD Hypertransport or Intel
     QuickPath to connect
     multicore chips together in a
     NUMA fashion





## How to program these parallel machines?

- The « good old » thread library
  - A way to achieve the best performance for a particular instance of a problem (architecture, application, data set)
  - Not portable, most of the time...

#### The « user-friendly » (...) parallel programming environments

- MPI
  - Standard for distributed programming
- OpenMP
  - De-facto standard for shared-memory programming
- and all these great programming languages I won't talk about today
  - Cilk+, TBB, Charm++, UPC, X10, Chapel, OpenCL, CUDA, OpenACC, ...







# Multi-task programming model on shared memory architecture

- Several tasks are executed in parallel
- Memory is shared (physically or virtually)
- Communication between tasks is done by reads and writes in the shared memory.
- Eg. The general-purpose multi-core processors share a common memory
  - Tasks can be assigned to distinct cores

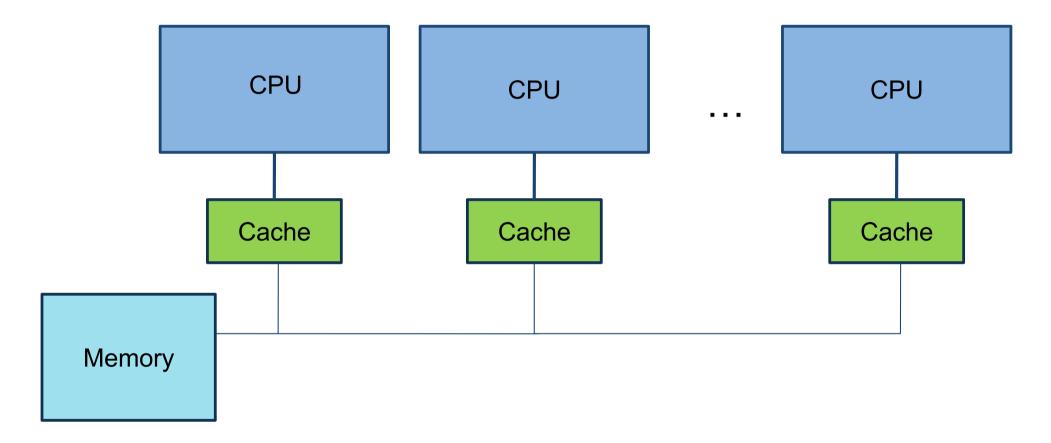


# Multi-task programming model on shared memory architecture

- The Pthreads library: POSIX thread library, adopted by most operating systems
  - The writing of a code requires a considerable number of lines specifically dedicated to threads
  - Example: parallelizing a loop involves
    - Declare thread structures,
    - create threads,
    - compute loop boundaries,
    - assign them to threads, ...
- OpenMP: a simpler alternative for the programmer



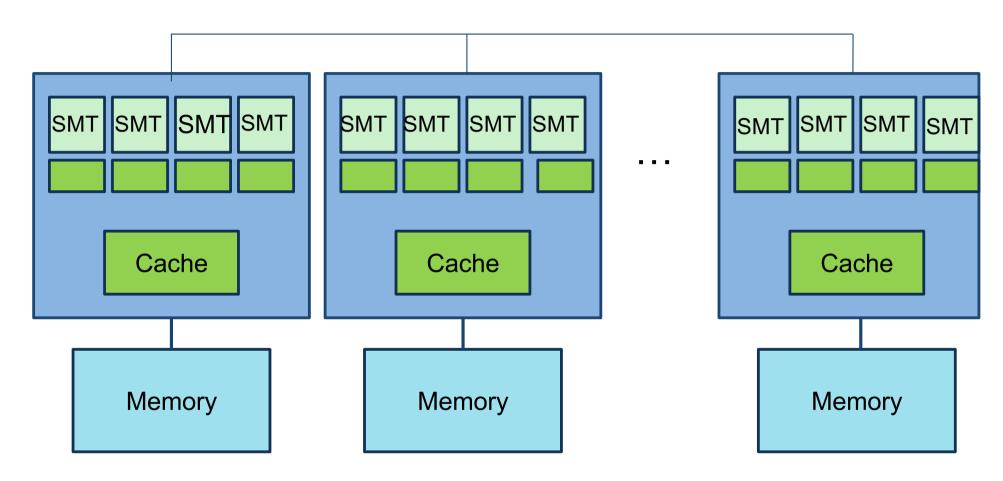
# Multi-task programming on UMA architectures



- Memory is shared
  - Uniform Memory Access Architectures (UMA)
  - An inherent problem: memory contentions



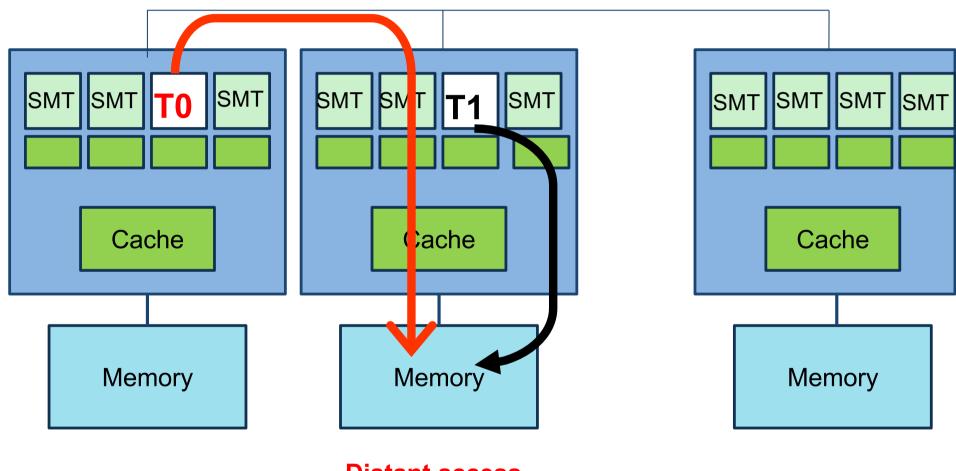
# Multi-task programming on UMA multicore architectures



- Memory is directly attached to multicore chips
  - Non-Uniform Memory Access architectures (NUMA)



# Multi-task programming on UMA multicore architectures



**Distant access** 

Local access



# **OpenMP**

- A de-facto standard API to write shared memory parallel applications in C, C++ and Fortran
- Consists of compiler directives, runtime routines and environment variables
- Specification maintained by the OpenMP Architecture Review Board (http://www.openmp.org)
- Current version of the specification: 4.5 (November 2015)



## **Advantages of OpenMP**

- A mature standard
  - Speeding-up your applications since 1998
- Portable
  - Supported by many compilers, ported on many architectures
- Allows incremental parallelization
- Imposes low to no overhead on the sequential execution of the program
  - Just tell your compiler to ignore the OpenMP pragmas and you get back to your sequential program
- Supported by a wide and active community
  - The specifications have been moving fast since revision 3.0 (2008) to support:
    - new kinds of parallelism (tasking)
    - new kinds of architectures (accelerators)



## **OpenMP model characteristics**

#### **Avantages**

- Transparent and portable thread management
- Easy programming

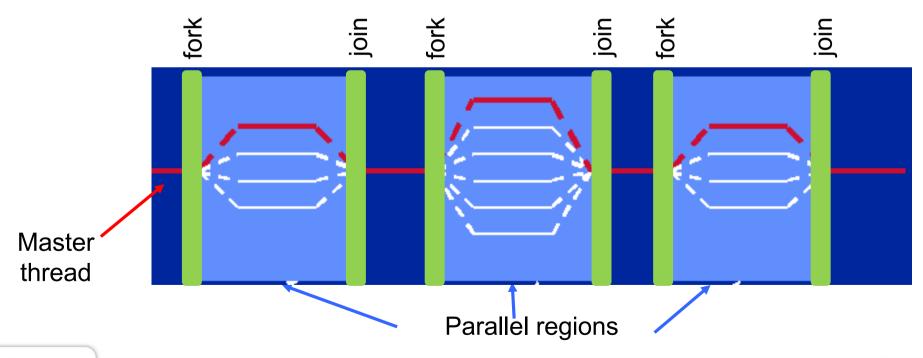
#### **Drawbacks**

- Data locality problem
- Shared but non-hierarchical memory
- Efficiency not guaranteed (impact of the material organization of the machine)
- Limited scalability, moderate parallelism



#### Introduction: execution model

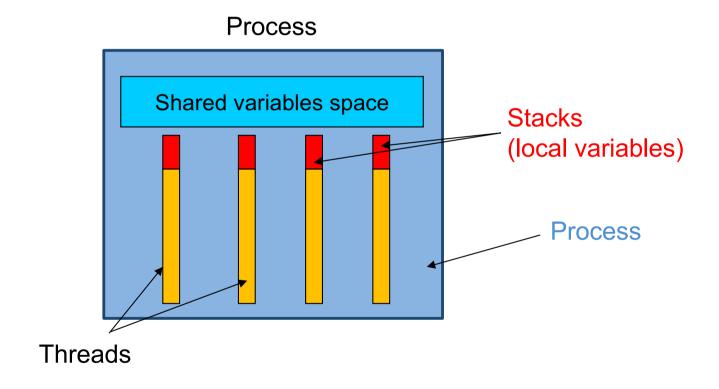
- An OpenMP program is executed by a unique process (on one or many cores)
- Fork-Join Parallelism
  - Master thread spawns a team of threads as needed
  - Parallelism is added incrementally: that is, the sequential program evolves into a parallel program
    - Entering a parallel region will create some threads (fork)
    - Leaving a parallel region will **terminate** them (*join*)
    - Any statement executed outside parallel regions are executed sequentially





#### Introduction: threads

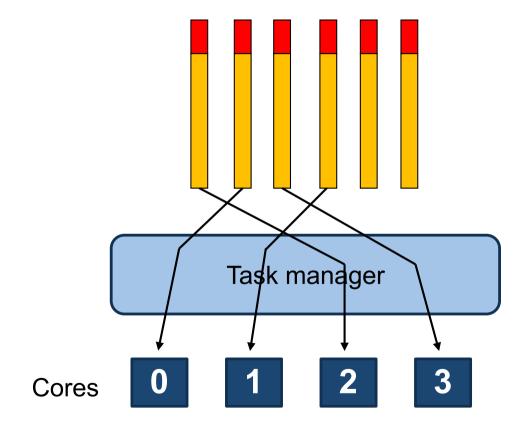
- Threads access the same resources as the main process
- They have a stack (stack, stack pointer and clean instructions pointer)





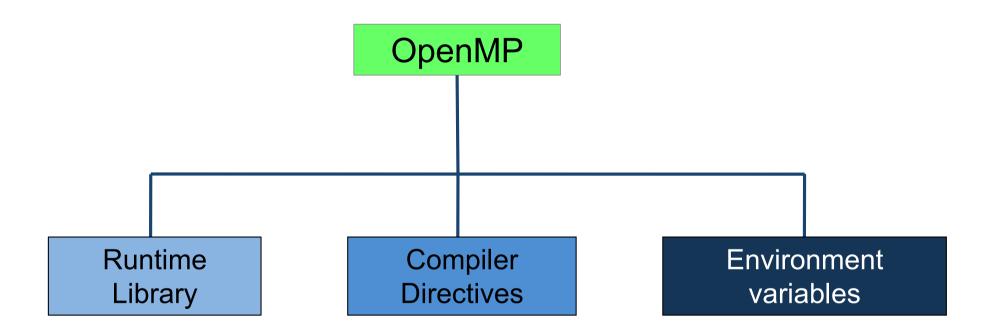
# Introduction: execution of an OpenMP program on a multicore

The task management system of the operating system assigns the tasks on the cores





# **OpenMP structure: software architecture**





#### **OpenMP structure: directives/pragmas formats**

directive [clause[clause]..]

```
!$OMP PARALLEL PRIVATE(a,b) & !$OMP FIRSTPRIVATE(c,d,e) ... !$OMP END PARALLEL
```

```
#pragma omp parallel private(a,b)
firstprivate(c,d,e)

{ ...
}
```

- The line is interpreted if openmp option to the compiler call otherwise comment
  - → portability



# **OpenMP structure: prototyping**

#### We have

- A Fortran 95 module OMP\_LIB
- An C/C++ input file omp.h

that define the prototypes of all the functions of the OpenMP library

#### **Fortran**

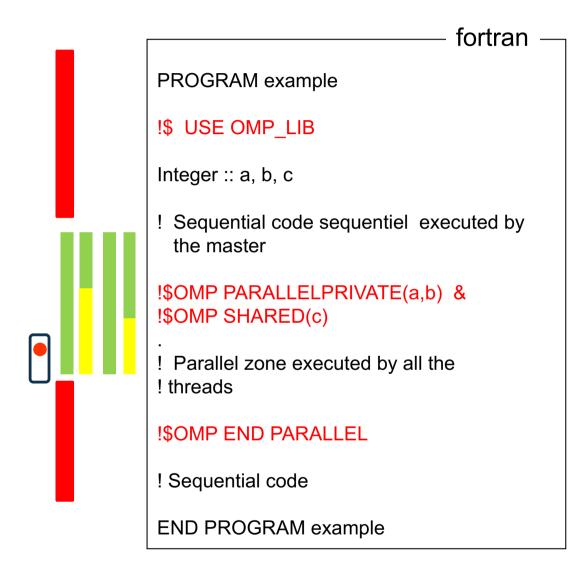
Program example
!\$ USE OMP\_LIB
!\$OMP PARALLEL PRIVATE(a,b) &

tmp= OMP\_GET\_THREAD\_NUM()
!\$OMP END PARALLEL

```
#include <omp.h>
```



# OpenMP structure: construction of a parallel region



```
C/C++
#include <omp.h>
main () {
Int a,b,c:
/* Sequential code sequential executed by
 the master
#pragma omp parallel private(a,b) \
                       shared(c)
    /* Parallel zone executed by all the
      threads
                                           */
/* Sequential code
```



#### Hello world!

```
void main()
{
    int ID = 0;
    printf(" hello(%d) ", ID);
    printf(" world(%d) \n", ID);
}
```



# OpenMP's Hello world!

```
OpenMP include file
#include "omp.h"
                                         Parallel region with
void main()
                                         default number of threads
#pragma omp parallel
                                                       Runtime library
                                                       function to return a
        int ID = omp_get_thread_num();
                                                       thread ID.
         printf(" hello(%d) ", ID);
         printf(" world(%d) \n", ID);
                                                      Sample Output
                                                      hello(1) hello(0) world(1)
                  End of the Parallel region
                                                      world(0)
                                                      hello (3) hello(2) world(3)
                                                      world(2)
```



#### **Example: Hello world Solution Calling the OpenMP compiler**

```
Linux and OS X
#include "omp.h"
                                 PGI Linux
void main()
                                 Intel windows
                                 Intel Linux and OS X
#pragma omp parallel
        int ID = omp_get_thread_num();
        printf(" hello(%d) ", ID);
        printf(" world(%d) \n", ID);
```



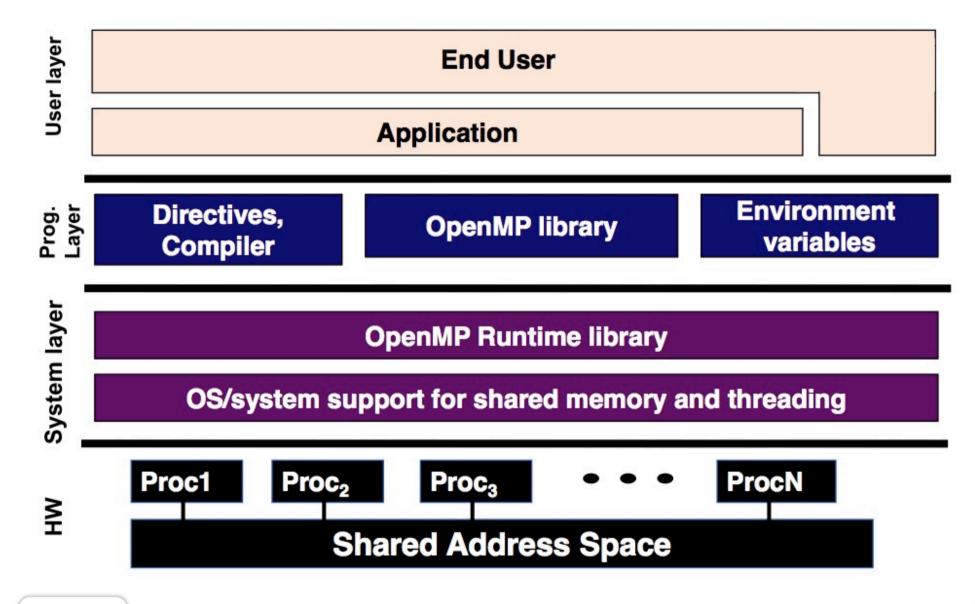
gcc -fopenmp

icl/Qopenmp

icpc -openmp

pgcc -mp

#### **OpenMP Basic Defs: Solution Stack**





#### IF clause of the PARALLEL directive

Conditional creation of a parallel region IF(logical\_expression) clause

fortran -

! Sequential code

!\$OMP PARALLEL IF(expr)

! Parallel or sequential code depending of the expr value

**!\$OMP END PARALLEL** 

! Sequential code

The logical expression will be evaluated before entering the parallel region

#### How do threads interact?

- OpenMP is a multi-threading, shared address model
  - Threads communicate by sharing variables
- Unintended sharing of data causes race conditions:
  - race condition: when the program's outcome changes as the threads are scheduled differently
- To control race conditions
  - Use synchronization to protect data conflicts
- Synchronization is expensive so
  - Change how data is accessed to minimize the need for synchronization



## **OpenMP threads**

#### Number of threads definition

- Through an environment variable: OMP NUM THREADS
- Through the routine: OMP\_SET\_NUM\_THREADS()
- Through the clause NUM\_THREADS() of the PARALLEL directive

#### Threads are numbered

- The number of threads is not necessary equal to the number of physical cores
- thread #0 is the master task
- OMP\_GET\_NUM\_THREADS(): number of threads
- OMP\_GET\_THREAD\_NUM(): thread number
- -OMP\_GET\_MAX\_THREADS(): maximum number of threads



# OpenMP structure: compilation and execution

```
ifort (ou icc) –openmp prog.f (INTEL)

f90 (ou cc ou CC) –openmp prog.f (SUN Studio)

gcc/gfortran –fopenmp –std=f95 prog.f (GNU)

export OMP_NUM_THREADS=2

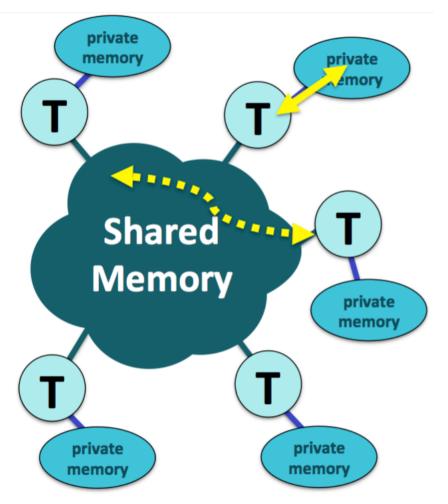
/a.out

# ps –eLF

USER PID PPID LWP C NLWP SZ RSS PSR ...
```



# The OpenMP memory model



- All the threads have access to the same globally shared memory
- Each thread has access to its own
   private memory area that can not be
   accessed by other threads
- Data transfer is performed through shared memory and is 100% transparent to the application
- The application programmer is responsible for providing the corresponding data-sharing attributes

## **Data sharing attributes**

- Need to set the visibility of each variable that appears inside an OpenMP parallel region using the following data-sharing attributes
  - shared: the data can be read and written by any thread of the team. All changes are visible to all threads
  - private: each thread is working on its own version of the data that cannot be accessed by other threads of the team
  - **firstprivate**: each thread is working on its own version of the variable. The data is initialized using the value it had before entering the parallel region
  - **lastprivate**: each thread is working on its own version of the variable. The value of the last thread leaving the region is copied back to the variable.



#### Variable status

The status of a variable in a parallel zone

- SHARED, it's located in the global memory
- PRIVATE, it's located in the thread of each thread. It's value is undefined at the entrance of the zone
- Declaring the variable status
  - # pragma omp parallel private (list)
  - # pragma omp parallel firstprivate (list)
  - # pragma omp parallel shared (list)
- Declaring a default status
  - DEFAULT(PRIVATE|SHARED|NONE) clause

```
program private var.f
!$USE OMP LIB
integer:: tmp =999
Call OMP_SET_NUM_THREADS(4)
!$OMP PARALLEL PRIVATE(tmp)
  print *, tmp
  tmp = OMP_GET_THREAD_NUM()
  print *, OMP_GET_THREAD_NUM(), tmp
!$OMP END PARALLEL
print *, tmp
end
```

### **Putting Threads to Work: the Worksharing Constructs**

```
void simple_loop(int N,
                    float *a,
2
                    float *b)
3
4 {
       int i;
5
       // i, N, a and b are shared by
       default
      #pragma omp parallel firstprivate(N)
           // i is private by default
           #pragma omp for
10
           for (i = 1; i <= N; i++) {
11
               b[i] = (a[i] + a[i-1]) / 2.0;
12
           }
13
       }
14
15 }
```

- omp for : distribute the iterations of a loop over the threads of the parallel region.
- Here, assigns N/P
   iterations to each
   thread, P being the
   number of threads of
   the parallel region.
- omp for comes with an implicit barrier
   synchronization at the end of the loop one can remove with the nowait keyword.



## **Work sharing**

- Distributing a loop between threads (// loop)
- Distribution of several sections of code between threads, one section of code per thread (// sections)
- Running a portion of code on a single thread
- Execution of several occurrences of the same function by different threads
- Execution by different threads of different work units, tasks



## Work sharing: parallel loop

#### **DO** Directive in Fortran, for in C

Parallelism by distribution of iterations of a loop

- The way in which the iterations can be distributed can be specified in the SCHEDULE clause (coded in the program or by an environment variable)
- A global synchronization is performed at the end of construction END DO (unless NOWAIT)
- Possibility to have several DO constructions in a parallel region
- The loop indices are integers and private
- Infinite loops and do while are not parallelizable



# DO and PARALLEL DO Directives

```
Program loop
implicit none
integer, parameter :: n=1024
integer :: i, j
real, dimension(n, n) :: tab
!SOMP PARALLEL
              ! Replicated code
 !$OMP DO
   do j=1, n ! Shared loop
    do i=1, n ! Replicated loop
        tab(i, j) = i*j
    end do
   end do
 !$OMP END DO
!$OMP END PARALLEL
end program loop
```

```
Program parallelloop
implicit none
integer, parameter :: n=1024
integer :: i, j
real, dimension(n, n) :: tab
!$OMP PARALLEL DO
  do j=1 n ! Shared loop
   do i=1, n ! Replicated loop
     tab(i, j) = i*j
    end do
  end do
!SOMP END PARALLEL DO
end program parallelloop
```

PARALLEL DO is a fusion of 2 directives

Beware: END PARALLEL DO includes a synchronization barrier!



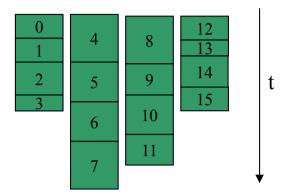
# **Work sharing: SCHEDULE**

#### !\$OMP DO SCHEDULE(STATIC, packet-size)

By default packet-size = #\_iterations/#\_threads

Ex: 16 iterations (0 to 15), 4 threads: packet size by default

is 4



#### !\$OMP DO SCHEDULE(DYNAMIC, packet-size)

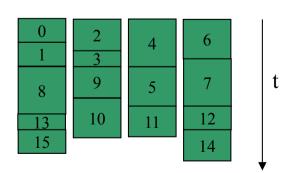
Packets are distributed to free threads in a dynamic way
All the packets have the same size (except maybe the last
one), by default the packet size is one

0	1	2	3	
5	6	7	4	
8	9	11	10	t
	12	11	12	
14	12	15	15	

#### !\$OMP DO SCHEDULE(GUIDED, packet-size)

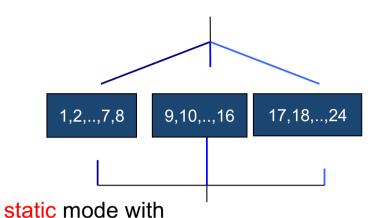
Packet-size: minimal packet size (1 by default) except the last one

Maximal packet size at the begining of the loop (here 2) then decrease to balance the load

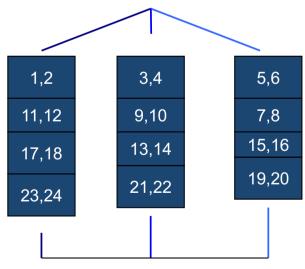


# Work sharing: SCHEDULE

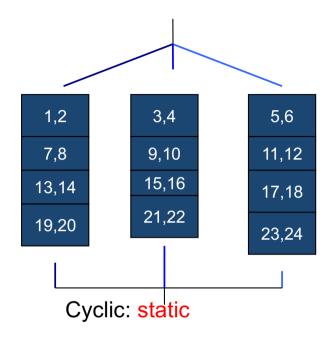
Ex: 24 iterations, 3 threads

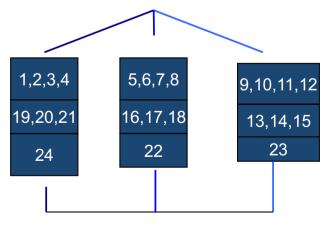


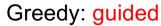
Packet size = # iterations/# threads



Greedy: dynamic









# Work sharing: SCHEDULE

The choice of the repartition mode can be delayed at the execution time using SCHEDULE(RUNTIME)

Taking into account the environment variable OMP\_SCHEDULE

-Ex

export OMP\_SCHEDULE="DYNAMIC,400"



Parallelize this simple code using OpenMP

```
f = 1.0

for (i = 0; i < N; i++)
  z[i] = x[i] + y[i];

for (i = 0; i < M; i++)
  a[i] = b[i] + c[i];

...

scale = sum (a, 0, m) + sum (z, 0, n) + f;
...</pre>
```

First create the parallel region and define the data-sharing attributes

```
#pragma omp parallel default (none) shared (z, x, y, a, b, c, n, m)
private (f, i, scale)
  f = 1.0
                                                                        parallel region
  for (i = 0; i < n; i++)
    z[i] = x[i] + y[i];
  for (i = 0; i < m; i++)
    a[i] = b[i] + c[i];
  scale = sum (a, 0, m) + sum (z, 0, n) + f;
} /* End of OpenMP parallel region */
```



```
#pragma omp parallel default (none) shared (z, x, y, a, b, c, n, m)
private (f, i, scale)
                                                                           parallel region
  for (i = 0; i < n; i++)
    z[i] = x[i] + y[i];
                                                         Statements
                                                       executed by all
                                                        the threads of
  for (i = 0; i < m; i++)
                                                         the parallel
    a[i] = b[i] + c[i];
                                                           region!
  scale = sum (a, 0, m) + sum (z, 0, n) + f; \leftarrow
} /* End of OpenMP parallel region */
```

At this point, all the threads execute the whole program (you won't get any speed-up from this!)



Now distribute the loop iterations over the threads using omp for

```
#pragma omp parallel default (none) shared (z, x, y, a, b, c, n, m)
private (f, i, scale)
                                                        Statements executed
  f = 1.0
                                                         by all the threads of
                                                          the parallel region
#pragma omp for
                                     parallel loop
  for (i = 0; i < n; i++)
     z[i] = x[i] + y[i];
                                  (work is distributed)
#pragma omp for
                                     parallel loop
  for (i = 0; i < m; i++)
                                  (work is distributed)
     a[i] = b[i] + c[i];
                                                        Statements executed
  scale = sum (a, 0, m) + sum (z, 0, n) + f;
                                                         by all the threads of
                                                         the parallel region
} /* End of OpenMP parallel region */
```

## **Optimization #1: Remove Unnecessary Synchronizations**

There are no dependencies between the two parallel loops, we remove the implicit barrier between the two

```
#pragma omp parallel default (none) shared (z, x, y, a, b, c, n, m)
private (f, i, scale)
  f = 1.0
                                                                        parallel region
#pragma omp for nowait
  for (i = 0; i < n; i++)
    z[i] = x[i] + y[i];
#pragma omp for nowait
  for (i = 0; i < m; i++)
    a[i] = b[i] + c[i];
#pragma omp barrier
  scale = sum (a, 0, m) + sum (z, 0, n) + f;
} /* End of OpenMP parallel region */
```



## Optimization #2: Don't Go Parallel if the Workload is Small

We don't want to pay the price of thread management if the workload is too small to be computed in parallel

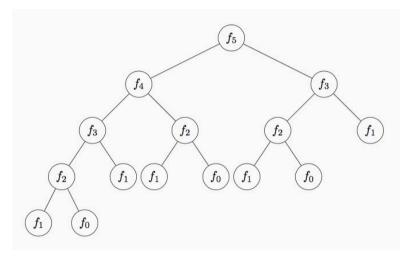
```
#pragma omp parallel default (none) shared (z, x, y, a, b, c, n, m)
private (f, i, scale) if (n > some threshold && m > some threshold)
  f = 1.0
#pragma omp for nowait
  for (i = 0; i < n; i++)
    z[i] = x[i] + y[i];
#pragma omp for nowait
  for (i = 0; i < m; i++)
    a[i] = b[i] + c[i];
  . . .
#pragma omp barrier
  scale = sum (a, 0, m) + sum (z, 0, n) + f;
} /* End of OpenMP parallel region */
```



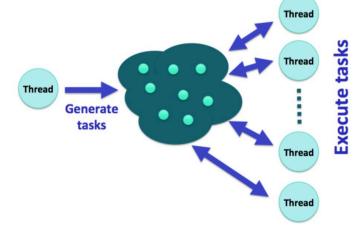
### **Extending the Scope of OpenMP with Task Parallelism**

 omp for has made OpenMP popular and remains for most users its central feature. But what if my application was not written in a loop-based fashion?

```
int fib(int n) {
   int i, j;
   if (n < 2) {
      return n;
   } else {
      i = fib(n - 1)
   ;
      j = fib(n - 2)
   ;
   return i + j;
}</pre>
```



 The OpenMP tasking concept: tasks generated by one OpenMP thread can be executed by any of the threads of the parallel region





# Tasking in OpenMP: Basic Concept (cont'd)

- The application programmer specifies regions of code to be executed in a task with the #pragma omp task construct
- All tasks can be executed independently
- When any thread encounters a task construct, a task is generated
- Tasks are executed asynchronously by any thread of the parallel region
- Completion of the tasks can be guaranteed using the taskwait synchronization construct

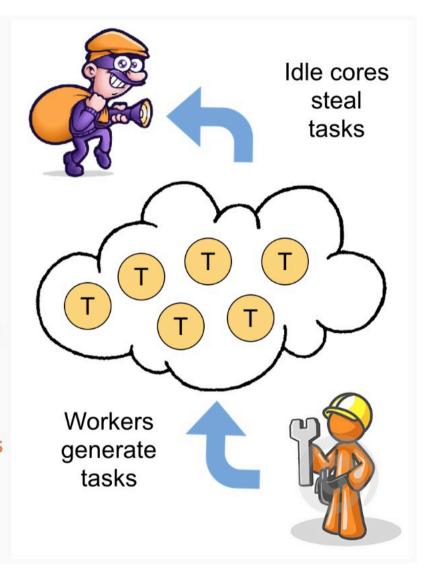
```
int main(void) {
       #pragma omp parallel
           #pragma omp single
           res = fib(50):
8
9 }
10
  int fib(int n) {
       int i, j;
12
       if (n < 2) {
13
           return n;
14
       } else {
15
           #pragma omp task
16
           i = fib(n - 1):
17
           #pragma omp task
18
           j = fib(n - 2);
19
           #pragma omp task
20
       wait
           return i + j;
21
22
23 }
```

## Tasking in OpenMP: Execution Model

# The Work-Stealing execution model

- Each thread has its own task queue
- Entering an omp task construct pushes a task to the thread's local queue
- When a thread's local queue is empty, it steals tasks from other queues

Tasks are well suited to applications with irregular workload.





## First OpenMP Tasking Experience

```
int main(void)

{
   printf("A ");
   printf("race ");
   printf("car ");

printf("\n");
   return 0;
}
```

- We want to use OpenMP to make this program print either A race car or A car race using tasks.
- Here is a battle plan :
  - Create the threads that will execute the tasks
  - 2. Create the tasks and make one of the thread generate them

#### Program output:

```
$ OMP_NUM_THREADS=2 ./task-1
$ A race car
```



```
int main(void)
{
    #pragma omp parallel
    {
        printf("A ");
        printf("race ");
        printf("car ");
}

printf("\n");
return 0;
}
```

- We want to use OpenMP to make this program print either A race car or A car race using tasks.
- Here is a battle plan :
  - Create the threads that will execute the tasks
  - 2. Create the tasks and make one of the thread generate them

Program output:

```
$ OMP_NUM_THREADS=2 ./task-2
```

\$ A race A race car car



```
1 int main(void)
2 {
       #pragma omp parallel
3
           #pragma omp single
                printf("A ");
                #pragma omp
       task
                printf("race ")
                #pragma omp
10
       task
                printf("car ");
11
           }
12
       7
13
14
       printf("\n");
15
       return 0;
16
17 }
```

- We want to use OpenMP to make this program print either A race car or A car race using tasks.
- Here is a battle plan :
  - Create the threads that will execute the tasks
  - 2. Create the tasks and make one of the thread generate them

```
Program output:
```

```
$ OMP_NUM_THREADS=2 ./task-3
$ A race car
$ OMP_NUM_THREADS=2 ./task-3
$ A car race
```



```
1 int main(void)
2 {
       #pragma omp parallel
3
           #pragma omp single
                printf("A ");
                #pragma omp task
                printf("race ");
                #pragma omp task
10
                printf("car ");
11
12
                printf("is fun ");
13
                printf("to watch "
14
       );
           }
15
       }
16
17
       printf("\n");
18
       return 0;
19
20 }
```

- Now that everything is working as intended, we would like to print is fun to watch at the end of the output string.
- This example illustrates the asynchronous execution of tasks.

```
Program output:
```

```
$ OMP_NUM_THREADS=2 ./task-4
$ A is fun to watch race car
$ OMP_NUM_THREADS=2 ./task-4
$ A is fun to watch car race
```



```
1 int main(void)
2 {
       #pragma omp parallel
           #pragma omp single
                printf("A ");
                #pragma omp task
                printf("race ");
                #pragma omp task
10
                printf("car ");
11
                #pragma omp task
12
       wait
                printf("is fun ");
13
                printf("to watch "
14
       );
           }
15
       }
16
17
       printf("\n");
18
       return 0;
19
20 }
```

- Now that everything is working as intended, we would like to print is fun to watch at the end of the output string.
- This example illustrates the asynchronous execution of tasks.
- To fix this, you need to explicitly wait for the completion of the tasks with taskwait before printing "is fun to watch"

#### Program output:

```
$ OMP_NUM_THREADS=2 ./task-5
$ A race car is fun to watch
$ OMP_NUM_THREADS=2 ./task-5
$ A car race is fun to watch
```



## What About Tasks with Dependencies on Other Tasks?

- Here, task A is writing some data that will be processed by task C. The same goes for task B and task D.
- The taskwait construct here makes sure task C won't execute before task A and task D before task B.
- As a side effect, task C won't execute until the execution of task B is over, creating some kind of fake dependency between task B and C.

```
void data_flow_example (void)
      type x, y;
      #pragma omp parallel
      #pragma omp single
           #pragma omp task
           write_data(&x); // Task A
           #pragma omp task
10
           write_data(&y); // Task B
11
12
           #pragma omp taskwait
13
14
           #pragma omp task
15
           print_results(x); // Task
16
           #pragma omp task
17
           print_results(y); // Task
18
19
20
```

# **OpenMP Tasks Dependencies: Rationale**

- The depend clause allows you to provide information on the way a task will access data.
- It is followed by an access mode that can be in, out or inout.
- Here are some examples of use for the depend clause:
  - depend(in: x, y, z): the task will read variables x, y and z
  - depend(out: res): the task will write variable res, any previous value of res will be ignored and overwritten
  - depend(inout: k, buffer[0:n]): the task will both read and write
     variable k and the content of n elements of buffer starting from index 0
- The OpenMP runtime system dynamically decides whether a task is ready for execution or not considering its dependencies (there is no need for further user intervention here)



### **OpenMP Tasks Dependencies: Some Trivial Example**

```
void data_flow_example (void)
2 {
      type x, y;
3
      #pragma omp parallel
5
      #pragma omp single
7
           #pragma omp task depend(out:
       x)
           write data(&x): // Task A
9
           #pragma omp task depend(out:
10
       y)
           write_data(&y); // Task B
11
12
           #pragma omp task depend(in: x
13
           print_results(x); // Task C
14
           #pragma omp task depend(in: y
15
          print_results(y); // Task D
16
      }
17
18 }
```

- Here is the previous example program written with tasks dependencies
- The taskwait construct is gone
  - The runtime system will rely on data dependencies to choose a ready task to execute
- In this version, task C could be executed before task B, as long as the execution of task A is over
- Expressing dependencies sometimes helps unlocking more parallelism



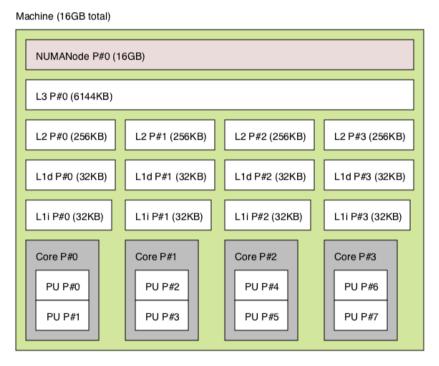
# **Speeding up OpenMP applications**

- Preambule: Have a closer look at your favorite/target platform
- Improving the execution of a parallel application requires a good understanding of the target platform architecture
- In particular, knowing about the following items is always useful:
  - The multicore processor: how many cores are available?
    - Which of them are physical/logical cores (HyperThreading and friends)?
  - The memory hierarchy: what kind of memory is available?
    - How is it organized?
  - The architecture topology: how (multicore) processors are connected together and how do they access memory?



## Getting to Know Your Platform with hwloc

The hwloc library gathers valuable information about your platform and synthesize it into a generic representation.



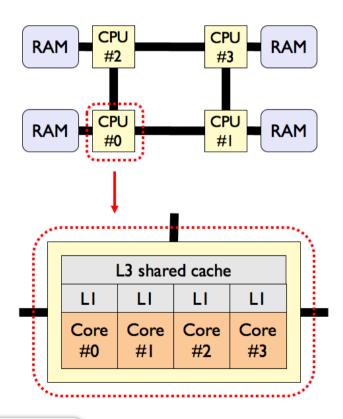
- Provides information about
  - the processing units (logical/physical cores)
  - the cache hierarchy
  - the memory hierarchy (NUMA nodes)
  - However, hwloc does not provide
     the entire architecture topology (the
     way processors are connected
     together).

https://www.open-mpi.org/projects/hwloc/



# **Understanding the Architecture Topology**

 The operating system knows about the way processors are connected together to some extent. It can provide a distance table that roughly represent how many crossbars you need to cross to access a specific NUMA node (see the hwloc-distances program)

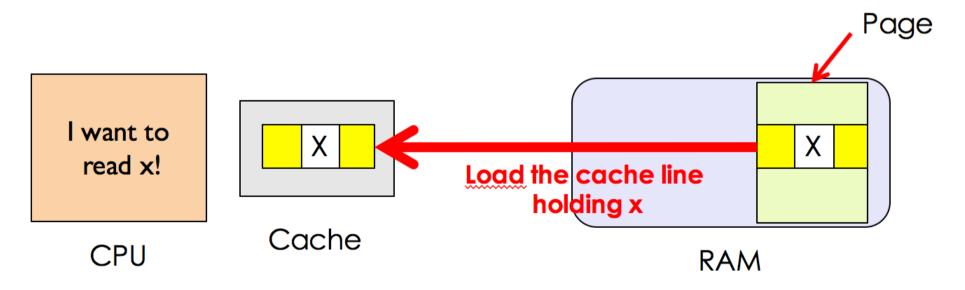


	$N_0$	$N_1$	$N_2$	$N_3$
$N_0$	0	10	10	20
$N_1$	10	0	20	10
$N_2$	10	20	0	10
$N_3$	20	10	10	0

A 4-nodes NUMA machine with the corresponding NUMA distance table

# **Cache Memory: Basic Concept**

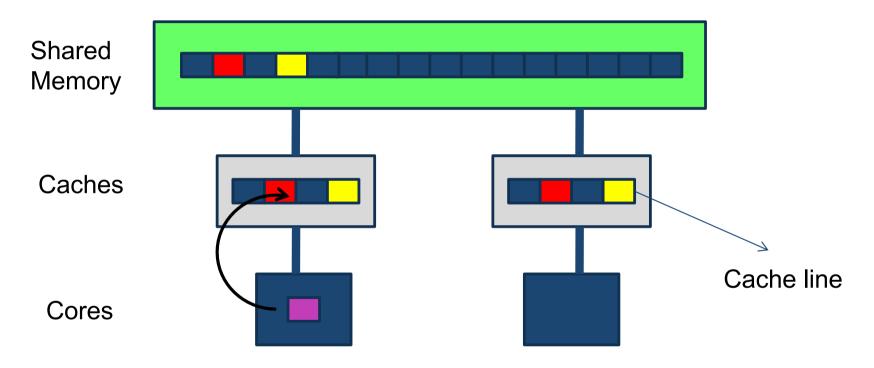
- A cache can be seen as a table of cache lines holding a predefined amount of memory (64B on most processors)
- Accessing a variable results in a cache hit if the corresponding cache line has already been cached (fast memory access)
- It can also result in a cache miss if the corresponding cache line is not cached yet. The hardware has to load the cache line to the cache before the processor can access it (longer memory access).





# Performance: False Sharing effect

Cache coherency and the negative effect of false sharing can have a big impact on performance



Charging a line of a shared cache invalids the other copies of this line

# Performance: False Sharing effect, contd.

# Using data structures in memory may lead to a decrease of performance and a lack of scalability

- To get performance, use the cache
- If several cores manipulate different data items close in memory, the update of individual elements leads a load of a line of cache (to keep coherency with the main memory)

# False sharing leads to bad performance when the following conditions are met

- Shared data a modified on # cores
- Several threads on # cores update data which are located on the same cache line
- These update appeards simultaneously and frequently



# Performance: False Sharing effect, contd.

When data are only read, we don't get false sharing

#### It can be avoided (or reduced) by

- Privatizing variables
- Increasing the array size or by using "padding"
- -By increasing the packet size (modifying the way loop iterations are shared between threads)



## Performance: False Sharing effect, contd.

Nthreads: # threads executing the loop

If we suppose that every thread possess a copy of a in his local cache

Packet size of 1 leads to a false sharing phenomenon for each update

If a cache line can contain **C** elements of vector **a**, we can sole the problem by extending artificially the array dimensions (array padding)
We declare an array **a(C,n)** and remplace **a(i)** by **a(1,i)** 



#### **Naive Square Matrix Multiplication Algorithm**

We consider a simple matrix multiplication algorithm involving square matrices of double precision floats.

$$\begin{bmatrix} C_0 & C_1 & C_2 & C_3 \\ C_4 & C_5 & C_6 & C_7 \\ C_8 & C_9 & C_{10} & C_{11} \\ C_{12} & C_{13} & C_{14} & C_{15} \end{bmatrix} = \begin{bmatrix} A_0 & A_1 & A_2 & A_3 \\ A_4 & A_5 & A_6 & A_7 \\ A_8 & A_9 & A_{10} & A_{11} \\ A_{12} & A_{13} & A_{14} & A_{15} \end{bmatrix} \times \begin{bmatrix} B_0 & B_1 & B_2 & B_3 \\ B_4 & B_5 & B_6 & B_7 \\ B_8 & B_9 & B_{10} & B_{11} \\ B_{12} & B_{13} & B_{14} & B_{15} \end{bmatrix}$$

where 
$$C_0 = A_0B_0 + A_1B_4 + A_2B_8 + A_3B_{12}$$

Let's implement this using what we've learned about OpenMP!

## Speeding-Up OpenMP: Benefit from Cache Memory (2)

```
void gemm_omp(double *A, double *B, double *C, int n) {
       #pragma omp parallel
           int i, j, k;
           #pragma omp for
           for (i=0; i<n; i++) {
               for (j=0; j< n; j++) {
                    for (k=0; k< n; k++) {
                        C[i*n+j] += A[i*n+k]*B[k*n+j];
                    }
10
               }
11
           }
12
13
14 }
                             On the Intel192 machine
```

Serial time: 40.3018250s Parallel time: 0.270773s Achieved speed-up: 148



$$\begin{bmatrix} C_0 & C_1 & C_2 & C_3 \\ C_4 & C_5 & C_6 & C_7 \\ C_8 & C_9 & C_{10} & C_{11} \\ C_{12} & C_{13} & C_{14} & C_{15} \end{bmatrix} = \begin{bmatrix} A_0 & A_1 & A_2 & A_3 \\ A_4 & A_5 & A_6 & A_7 \\ A_8 & A_9 & A_{10} & A_{11} \\ A_{12} & A_{13} & A_{14} & A_{15} \end{bmatrix} \times \begin{bmatrix} B_0 & B_1 & B_2 & B_3 \\ B_4 & B_5 & B_6 & B_7 \\ B_8 & B_9 & B_{10} & B_{11} \\ B_{12} & B_{13} & B_{14} & B_{15} \end{bmatrix}$$

$$C_0 = A_0B_0$$

- $+A_1B_4$
- $+ A_{2}B_{8}$
- $+ A_3 B_{12}$



$$\begin{bmatrix} C_0 & C_1 & C_2 & C_3 \\ C_4 & C_5 & C_6 & C_7 \\ C_8 & C_9 & C_{10} & C_{11} \\ C_{12} & C_{13} & C_{14} & C_{15} \end{bmatrix} = \begin{bmatrix} A_0 & A_1 & A_2 & A_3 \\ A_4 & A_5 & A_6 & A_7 \\ A_8 & A_9 & A_{10} & A_{11} \\ A_{12} & A_{13} & A_{14} & A_{15} \end{bmatrix} \times \begin{bmatrix} B_0 & B_1 & B_2 & B_3 \\ B_4 & B_5 & B_6 & B_7 \\ B_8 & B_9 & B_{10} & B_{11} \\ B_{12} & B_{13} & B_{14} & B_{15} \end{bmatrix}$$

$$C_0 = A_0B_0$$

- $+A_1B_4$
- $+A_2B_8$
- $+ A_3 B_{12}$



$$\begin{bmatrix} C_0 & C_1 & C_2 & C_3 \\ C_4 & C_5 & C_6 & C_7 \\ C_8 & C_9 & C_{10} & C_{11} \\ C_{12} & C_{13} & C_{14} & C_{15} \end{bmatrix} = \begin{bmatrix} A_0 & A_1 & A_2 & A_3 \\ A_4 & A_5 & A_6 & A_7 \\ A_8 & A_9 & A_{10} & A_{11} \\ A_{12} & A_{13} & A_{14} & A_{15} \end{bmatrix} \times \begin{bmatrix} B_0 & B_1 & B_2 & B_3 \\ B_4 & B_5 & B_6 & B_7 \\ B_8 & B_9 & B_{10} & B_{11} \\ B_{12} & B_{13} & B_{14} & B_{15} \end{bmatrix}$$

$$C_0 = A_0B_0$$
  
+  $A_1B_4$   
+  $A_2B_8$   
+  $A_3B_{12}$ 



$$\begin{bmatrix} C_0 & C_1 & C_2 & C_3 \\ C_4 & C_5 & C_6 & C_7 \\ C_8 & C_9 & C_{10} & C_{11} \\ C_{12} & C_{13} & C_{14} & C_{15} \end{bmatrix} = \begin{bmatrix} A_0 & A_1 & A_2 & A_3 \\ A_4 & A_5 & A_6 & A_7 \\ A_8 & A_9 & A_{10} & A_{11} \\ A_{12} & A_{13} & A_{14} & A_{15} \end{bmatrix} \times \begin{bmatrix} B_0 & B_1 & B_2 & B_3 \\ B_4 & B_5 & B_6 & B_7 \\ B_8 & B_9 & B_{10} & B_{11} \\ B_{12} & B_{13} & B_{14} & B_{15} \end{bmatrix}$$

$$C_0 = A_0B_0$$

$$+A_1B_4$$

$$+ A_{2}B_{8}$$

$$+ A_3 B_{12}$$

Assuming we work with 32 bytes-long cache lines and each element of the matrix is 8 bytes long, how many cache lines do I need to compute one element of C?

$$\begin{bmatrix} C_0 & C_1 & C_2 & C_3 \\ C_4 & C_5 & C_6 & C_7 \\ C_8 & C_9 & C_{10} & C_{11} \\ C_{12} & C_{13} & C_{14} & C_{15} \end{bmatrix} = \begin{bmatrix} A_0 & A_1 & A_2 & A_3 \\ A_4 & A_5 & A_6 & A_7 \\ A_8 & A_9 & A_{10} & A_{11} \\ A_{12} & A_{13} & A_{14} & A_{15} \end{bmatrix} \times \begin{bmatrix} B_0 & B_1 & B_2 & B_3 \\ B_4 & B_5 & B_6 & B_7 \\ B_8 & B_9 & B_{10} & B_{11} \\ B_{12} & B_{13} & B_{14} & B_{15} \end{bmatrix}$$

$$C_0 = A_0B_0$$
  
+  $A_1B_4$   
+  $A_2B_8$   
+  $A_3B_{12}$ 

#### Conclusion:

- Every access to A<sub>i</sub> use the same cache line => cache friendly
- Every access to B<sub>j</sub> use a different cache line => poor cache utilization

# Deal with the B<sub>j</sub> Situation

To improve cache utilization, we can transpose matrix B to make sure  $B_0$ ,  $B_4$ ,  $B_8$  and  $B_{12}$  are stored on the same cache line

$$\begin{bmatrix} C_0 & C_1 & C_2 & C_3 \\ C_4 & C_5 & C_6 & C_7 \\ C_8 & C_9 & C_{10} & C_{11} \\ C_{12} & C_{13} & C_{14} & C_{15} \end{bmatrix} = \begin{bmatrix} A_0 & A_1 & A_2 & A_3 \\ A_4 & A_5 & A_6 & A_7 \\ A_8 & A_9 & A_{10} & A_{11} \\ A_{12} & A_{13} & A_{14} & A_{15} \end{bmatrix} \times \begin{bmatrix} B_0 & B_4 & B_8 & B_{12} \\ B_1 & B_5 & B_9 & B_{13} \\ B_2 & B_6 & B_{10} & B_{14} \\ B_3 & B_7 & B_{11} & B_{15} \end{bmatrix}$$

$$C_0 = A_0B_0$$

$$+A_1B_4$$

$$+ A_2B_8$$

$$+ A_3 B_{12}$$

#### Performance evaluation on Intel192:

Serial time: 5.188652s (prev: 40.3018250s)

Parallel time: 0.067657s (prev: 0.270773s)

Achieved speed-up: 77 (rel to prev: 595(!))