	Discrete: pmf $p(\cdot)$	Continuous: pdf $f(\cdot)$
Support Set	Countable set of values	Uncountable set of values
Probabilities	p(x) = P(X = x)	$f(x) \neq P(X = x) = 0$ for all $x$ $P(a \le X \le b) = \int_a^b f(x)dx = F(b) - F(a)$
Joint	$p_{XY}(x,y) = \mathbb{P}(X=x,Y=y)$	$\mathbb{P}(X \in [a,b], Y \in [c,d]) = \int_a^b \int_c^d f_{XY}(x,y)  dx  dy$
Marginal	$p_X(x) = \sum_y p_{XY}(x, y)$	$f_X(x) = \int_{-\infty}^{\infty} f_{XY}(x, y)  dy$
Conditional	$p_{X Y}(x y) = p_{XY}(x,y)/p_Y(y)$	$f_{X Y}(x y) = f_{XY}(x,y)/f_Y(y)$
Independence	$p_{XY}(x,y) = p_X(x)p_Y(y)$	$f_{XY}(x,y) = f_X(x)f_Y(y)$
Expected Value	$\mu_X = \mathbb{E}[X] = \sum_x x p(x)$	$\mu_X = \mathbb{E}[X] = \int_{-\infty}^{\infty} x f(x) \ dx$
	$\mathbb{E}[g(X)] = \sum_{x} g(x)p(x)$	$\mathbb{E}[g(X)] = \int_{-\infty}^{\infty} g(x)f(x) \ dx$
	$\mathbb{E}[g(X,Y)] = \sum_{x} \sum_{y} g(x,y)p(x,y)$	$\mathbb{E}[g(X,Y)] = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} g(x,y) f_{XY}(x,y) \ dx \ dy$

Table 1: Differences between Discrete and Continous Random Variables

Probability Mass Function $p(x)$	Probability Density Function $f(x)$
Discrete Random Variables	Continuous Random Variables
p(x) = P(X = x)	$f(x) \neq P(X = x) = 0$
$p(x) \ge 0$	$f(x) \neq P(X = x) = 0$ $f(x) \ge 0$
$p(x) \le 1$	f(x) can be greater than one!
$\sum_{x} p(x) = 1$	$\int_{-\infty}^{\infty} f(x) \ dx = 1$
$F(x_0) = \sum_{x \le x_0} p(x)$	$F(x) = \int_{-\infty}^{x} f(t) dt$

Table 2: Probability mass function (pmf) versus probability density function.

Definition of R.V.	$X \colon S \to \mathbb{R}$ (RV is a fixed function from sample space to reals)
Support Set	Collection of all possible realizations of an RV take
CDF	$F(x_0) = P(X \le x_0)$
Standard Deviation	$\sigma_X = \sqrt{\sigma_X^2}$
Cov. and Independence	$X, Y$ independent $\Rightarrow \operatorname{Cov}(X, Y) = 0$ but $\operatorname{Cov}(X, Y) = 0 \Rightarrow X, Y$ independent
Functions and Independence	$X, Y$ independent $\Rightarrow g(X), h(Y)$ independent
Definition of Correlation	$ ho_{XY} = \operatorname{Corr}(X, Y) = \sigma_{XY}/(\sigma_X \sigma_Y)$
Expectation of a Function	In general, $\mathbb{E}[g(X)] \neq g(\mathbb{E}[X])$
Linearity of Expectation	$\mathbb{E}[a+X] = a + \mathbb{E}[X]$
	$\mathbb{E}[bX] = b\mathbb{E}[X]$
	$\mathbb{E}[X_1+\ldots+X_k]=\mathbb{E}[X_1]+\ldots\mathbb{E}[X_k]$
Variance	$\sigma_X^2 \equiv \operatorname{Var}(X) \equiv \mathbb{E}\left[ (X - \mathbb{E}[X])^2 \right] = \mathbb{E}[X^2] - (\mathbb{E}[X])^2 = \mathbb{E}\left[ X(X - \mu_X) \right]$
Var. of Linear Combination	$\operatorname{Var}(a+X) = \operatorname{Var}(X)$
	$\operatorname{Var}(bX) = b^2 \operatorname{Var}(X)$
	$Var(aX + bY + c) = a^{2}Var(X) + b^{2}Var(Y) + 2abCov(X, Y)$
	$X_1, \ldots, X_k$ are uncorrelated $\Rightarrow \operatorname{Var}(X_1 + \ldots + X_k) = \operatorname{Var}(X_1) + \ldots \operatorname{Var}(X_k)$
Covariance	$\sigma_{XY} \equiv \text{Cov}(X,Y) \equiv \mathbb{E}\left[ (X - \mathbb{E}[X])  (Y - \mathbb{E}[Y]) \right] = \mathbb{E}[XY] - \mathbb{E}[X]\mathbb{E}[Y] = \mathbb{E}\left[ X(Y - \mu_Y) \right] = \mathbb{E}\left[ (X - \mu_X) Y \right]$
Bilinearity of Covariance	Cov(a + X, Y) = Cov(X, a + Y) = Cov(X, Y)
	Cov(bX, Y) = Cov(X, bY) = bCov(X, Y)
	Cov(X, Y + Z) = Cov(X, Y) + Cov(X, Z) and $Cov(X + Z, Y) = Cov(X, Y) + Cov(Z, Y)$

Table 3: Essential facts that hold for all random variables, continuous or discrete: X, Y, Z and  $X_1, \ldots, X_k$  are random variables; a, b, c, d are constants;  $\mu, \sigma, \rho$  are parameters; and  $g(\cdot), h(\cdot)$  are functions.

	Sample Statistic	Population Parameter	Population Parameter
Setup	oopulation	Population viewed as list of objects Population viewed as a RV	Population viewed as a RV
Mean	$ar{x} = rac{1}{n} \sum_{i=1}^{n} x_i$	$\mu_X = \frac{1}{N} \sum_{i=1}^{N} x_i$	Discrete $\mu_X = \sum xp(x)$
		i=1	Continuous $\mu_X = \int_{-\infty}^{\infty} x f(x) dx$
Variance	$s_X^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$	$\sigma_X^2 = \frac{1}{N} \sum_{i=1}^N (x_i - \mu_X)^2$	$\sigma_X^2 = E\left[ (X - E[X])^2 \right]$
Std. Dev.	$s_X = \sqrt{s_X^2}$	$\sigma_X = \sqrt{\sigma_x^2}$	$\sigma_X = \sqrt{\sigma_x^2}$
Covariance	$s_{XY} = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - x_i)^{-1}$	$(\bar{x})(y_i - \bar{y}) \left  \sigma_{XY} = \frac{1}{N} \sum_{i=1}^{N} (x_i - \mu_X)(y_i - \mu_Y) \right $	$\sigma_{XY} = E\left[ (X - \mu_X) \left( Y - \mu_Y \right) \right]$
Correlation	Correlation $r_{XY} = s_{XY}/(s_X s_Y)$	$\rho_{XY} = \sigma_{XY}/(\sigma_X \sigma_Y)$	$\rho_{XY} = \sigma_{XY} / (\sigma_X \sigma_Y)$