$d_1,d_2,d_3$  positive integer.  $\Omega \subset \mathbb{R}^{d_1}, m(\Omega) < \infty$  y  $f: \Omega \times \mathbb{R}^{d_2} \to \mathbb{R}^{d_3}$ . For Orlicz Spaces we will use the Orlicz norm. Nemitski operator

$$fu(x) = f(x, u(x))$$

maps  $\mathbb{R}^{d_2}$ -valued functions defined on  $\Omega \subset \mathbb{R}^{d_1}$  into  $\mathbb{R}^{d_3}$ -valued functions defined on  $\Omega \subset \mathbb{R}^{d_1}$ . Measurability seems follows the same lines that [2, p. 349].??? Let  $\Phi_1 : \mathbb{R}^{d_2} \to \mathbb{R}$  and  $\Phi_2 : \mathbb{R}^{d_3} \to \mathbb{R}$  be anisotropic N-functions.

## **Theorem 0.1.** Deber #1 Theorem similar to [1, Lemma 17.2]

*Proof.* Let  $u \in \Pi(E^{\Phi}(\mathbb{R}^{d_2}), r)$  be. Adapting the [3, Prop. 3, p. 92-93] to  $\mathbb{R}^d$ -valued functions (see also [] By [4, Th. 5.5] for Luxemburg norm and N-functions defined on infinite dimensional Banach space) (???) we obtain  $\|u_0\|_{L^{\Phi}(\Omega,\mathbb{R}^{d_2})} < r$  where  $u_0 = u - \chi_A u$  for certain set  $A \subset \Omega$  where  $\|u\|_{L^{\infty}(A,\mathbb{R}^{d_2})} < \infty$ , in particular  $\chi_A u \in E^{\Phi}(\Omega,\mathbb{R}^{d_2})$ . From [4, Th. 5.4] we obtain that  $\chi_A u$  has an absolutely continuous norm. Therefore we can finf  $u_1,\ldots,u_n$  with  $u_iu_j\equiv 0$ , for  $i\neq j, \|u_i\|_{L^{\Phi}(\Omega,\mathbb{R}^{d_2})} < r, i=1,\ldots,n$  and  $\chi_A u = u_1 + \cdots + u_n$ . The result follows from the identity (see [2, p. 353])

$$f(u_0 + \cdots + u_n) = fu_0 + \cdots fu_n - (n-1)f0.$$

Deber #2 completar otros enunciados

## References

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