

d_1, d_2, d_3 positive integer. $\Omega \subset \mathbb{R}^{d_1}$, $m(\Omega) < \infty$ y $f : \Omega \times \mathbb{R}^{d_2} \rightarrow \mathbb{R}^{d_3}$.

For Orlicz Spaces we will use the Orlicz norm.

Nemitski operator

$$\mathbf{f}u(x) = f(x, u(x))$$

maps \mathbb{R}^{d_2} -valued functions defined on $\Omega \subset \mathbb{R}^{d_1}$ into \mathbb{R}^{d_3} -valued functions defined on $\Omega \subset \mathbb{R}^{d_1}$. Measurability seems follows the same lines that [?, p. 349].???

Let $\Phi_1 : \mathbb{R}^{d_2} \rightarrow \mathbb{R}$ and $\Phi_2 : \mathbb{R}^{d_3} \rightarrow \mathbb{R}$ be anisotropic N -functions.

Theorem 0.1. *Deber #1 Theorem similar to [?, Lemma 17.2]*

Proof. Let $u \in \Pi(E^\Phi(\cdot, \mathbb{R}^{d_2}), r)$ be. Adapting the [?, Prop. 3, p. 92-93] to \mathbb{R}^d -valued functions (see also [] By [?, Th. 5.5] for Luxemburg norm and N -functions defined on infinite dimensional Banach space) (???) we obtain $\|u_0\|_{L^\Phi(\Omega, \mathbb{R}^{d_2})} < r$ where $u_0 = u - \chi_A u$ for certain set $A \subset \Omega$ where $\|u\|_{L^\infty(A, \mathbb{R}^{d_2})} < \infty$, in particular $\chi_A u \in E^\Phi(\Omega, \mathbb{R}^{d_2})$. From [?, Th. 5.4] we obtain that $\chi_A u$ has an absolutely continuous norm. Therefore we can find u_1, \dots, u_n with $u_i u_j \equiv 0$, for $i \neq j$, $\|u_i\|_{L^\Phi(\Omega, \mathbb{R}^{d_2})} < r$, $i = 1, \dots, n$ and $\chi_A u = u_1 + \dots + u_n$. The result follows from the identity (see [?, p. 353])

$$\mathbf{f}(u_0 + \dots + u_n) = \mathbf{f}u_0 + \dots \mathbf{f}u_n - (n-1)\mathbf{f}0.$$

Deber #2 completar otros enunciados

□

Deber #3 Acotacion y continuidad

Deber #4 Nemitsky asociado a $f = \Phi'$.

Lemma 0.2 (Lemma 9.1 KR). *Suppose that $d \geq 1$ and $\|u\|_{L^\Phi(\Omega, \mathbb{R}^d)} \leq 1$. Then $v(x) = \nabla \Phi(u(x))$ belong to $\tilde{L}^\Psi(\Omega, \mathbb{R}^d)$ and $\rho_\Psi(v) \leq 1$.*

Proof. Sale igual, s \tilde{A}^3 lo hay que evitar escribirm \tilde{A}^3 dulos

□

El Lemma 9.2 KR sale sin cambios.