

$$_2y_{\overline{dx^2+p(x)\frac{dy}{dx}+q(x)y=r(x),ec_{2_g}en\,donde}}son\,funciones\,de\,finidas\,en\,un\,intervalo\,de\,con\,valores\,en.\,Si\equiv$$

$$_0y_{\overline{dx^2+p(x)\frac{dy}{dx}+q(x)y=0,ec_{2_g}en_h\,om}}$$

$$p,q,r$$

$$I$$

$$x_0\in$$

$$I$$

$$y_0,y_1\in$$

$$\begin{cases} \frac{d^2y}{dx^2}+p(x)\frac{dy}{dx}+q(x)y=r(x),x\in I\\ y(x_0)=y_0\\ y'(x_0)=y_0^1 \end{cases}$$

$$z'=$$

$$y'(x)$$

$$\begin{cases} y'(x)=z(x)\\ z'(x)=-p(x)z(x)-q(x)y+r(x),\\ y(x_0)=y_0\\ z(x_0)=y_0^1 \end{cases}$$

$$w'(x)=$$

$$f(x,w(x))$$

$$w(x)=$$

$$(y(x),z(x))$$

$$f(x,w)=$$

$$(z,-p(x)z-$$

$$q(x)y+$$

$$r(x)$$

$$f$$

$$I\times^2$$

$$(x,w_0),(x,w_1)\in$$

$$I\times^2$$

$$w_0=$$

$$(z_0,y_0)$$

$$w_1=$$

$$(z_1,w_1)$$

$$\|f(x,w_1)-f(x,w_2)\|\leq \sqrt{(z_1-z_0)^2+(p(x)(z_1-z_0)+q(x)(y_1-y_0))^2}\leq C\|w_1-w_0\|,$$

$$C$$

$$|p(x)|,|q(x)|$$

$$x\in$$

$$I$$

$$f$$

$$_2$$

$$I$$

$$y_1$$

$$y_2$$

$$_{2_g}en_h\,om\,y_1,c_2\in$$

$$c_1y_1+$$

$$c_2y_2$$

$$y\equiv$$

$$0$$

$$triv-$$

$$ial$$

$$L[y]:=y''+py'+qy$$

$$L[c_1y_1+$$

$$c_2y_2]=$$

$$c_1L[y_1]+$$

$$c_2L[y_2]=$$

$$0.$$

$$y_p$$

$$_{2_g}en\,y\,que_g=$$

$$y_g(x,c_1,c_2)$$

$$_{2_g}en_h\,om.\,Entonces_p+$$

$$y_g$$

$$_{2_g}en.$$

$$L[y]:=y''+py'+qy$$

$$L[y_g+$$

$$y_p]=$$

$$L[y_g]+$$

$$L[y_p]=$$

$$0+$$

$$f=$$

$$f_y$$

$$L[y]=$$

$$r$$

$$L[y-$$

$$y_p]=$$

$$L[y]-$$

$$L[y_p]=$$

$$r-$$

$$f=$$

$$0.$$

$$c_1$$

$$c_2$$

$$y(x)-$$

$$y_p(x)=$$