

Exam 2

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1) (25 pts.) The argument to prove that the complement of a regular language is also a regular language is:

“Since L is regular, there is Deterministic Finite State Automaton D that recognizes L . But then, the Deterministic Finite State Automaton \bar{D} obtained interchanging accept and non-accept states of D , recognizes \bar{L} , the complement of L .”

Is the argument valid when Deterministic FSA is replaced with Non-deterministic FSA and no transformation from Non-deterministic to Deterministic FSA is invoked?

2) (25 pts). Let $L = \{ \langle a, b, c, p \rangle : a, b, c \text{ and } p \text{ are integers } a^p \equiv c \pmod{p} \}$. Demonstrate that L is in P .

3) (25 pts) Consider the problem $L = \{ \langle T, w \rangle : T \text{ is a Turing Machine and } w \text{ a fixed string such that } T \text{ enters each of its states on input } w \}$

4) (25 pts) Consider the problem $L = \{ \langle G, w \rangle : G \text{ is a context free grammar and } w \text{ a string, such that } w \in L(G) \}$. Is L decidable? Provide a formal answer.