

# 1. Electromagnetism

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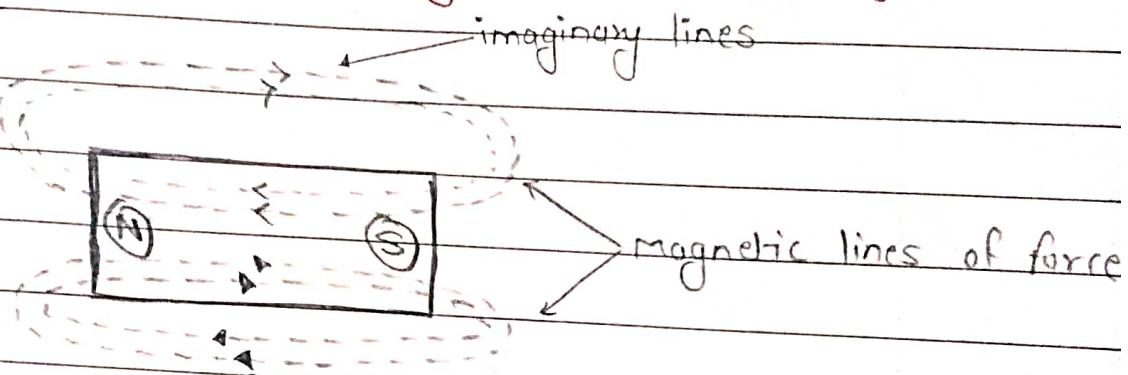
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## • Important Terms

### 1) Magnetic field (Magnetic Lines of force) :-

The region around magnet in which effect of magnetism can be experienced is called as **MAGNETIC FIELD**

To represent a magnetic field imaginary lines are considered around the magnet called **Magnetic lines of force**.



- Magnetic field lines are closed curves
- lines do not intersect with each other.

### 2) Magnetic Flux :-

The total number of lines of force in a magnetic field is called **magnetic flux ( $\Phi$ )**  
S.I. unit (Weber)  $1 \text{ Wb} = 10^8 \text{ lines of force}$

### 3) Magnetic Field Intensity (Magnetising Force) :-

strength of force experienced by a unit north pole, placed at any point in magnetic field is called as ...

(H)  $(\text{N/Wb})$   $(\text{A/m})$   $(\text{AT/m})$

Newton  
Webers

Amperc  
metre

Amper turns  
meter

$$H = \frac{NI}{l} \dots \text{AT/m}$$

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4) Magnetic Flux Density :- The flux per unit area measured in a plane, perpendicular to the flux, is

$$(B) \text{ Weber} \quad \frac{\text{Wb}}{\text{meter}^2} \quad B = \frac{\text{Total Flux}}{\text{Unit area}} = \frac{\phi}{a} \quad \text{Tesla}$$

5) Pole Strength :- Amount of magnetic flux coming out from a given magnetic pole.

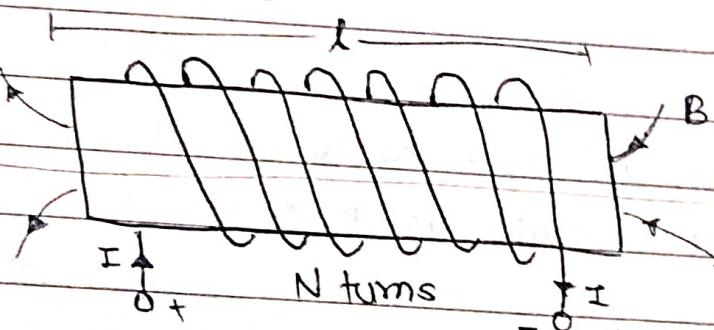
\* Electromagnet :- An conductor wounded by wire and wire is carrying current in it. (Behave like magnet)

\* Dot Convention :-  $\odot$  Current flowing towards observer

Cross Convention:  $\times$  Current flowing away from observer

\* Right Hand Thumb Rule :- "If a conductor is held in right hand such that thumb indicates direction of current flowing through conductor then remaining four fingers around the conductor indicates the direction of magnetic field lines".  
Thumb  $\Rightarrow$  Towards current  
Cuddled fingers  $\Rightarrow$  Direction of Magnetic field

\* Magnetic field due to Solenoid :-



$$B = \mu H = \frac{\mu NI}{l} = \mu k$$

$B$  = Magnetic flux density (Tesla)

$\mu$  = Permeability of medium ( $H/m$ )

$N$  = Number of turns

$I$  = Current

$l$  = length  $k$  = sheet current density ( $A/m$ )

\* Permeability :- Ability of a material to carry the magnetic flux lines in a given medium.

\* Absolute permeability :- (1) The ratio of magnetic flux density ( $B$ ) to magnetic field strength ( $H$ )

$$\text{Absolute permeability} = \frac{\text{Magnetic flux density } (B)}{\text{Magnetic field strength } (H)}$$

$$\mu = \frac{B}{H} \text{ H/m Henrie meter}$$

\* Permeability of Vacuum or Free Space ( $\mu_0$ ):-

When a magnet is placed in a vacuum or free space, ratio of  $B/H$   $\mu_0 = 4\pi \times 10^{-7}$  H/m

\* Relative Permeability :- Ratio of flux density to magnetic flux density in free space

$$\mu_r = \frac{B}{B_0} \text{ unit less} \quad [\mu_r \text{ air} = 1]$$

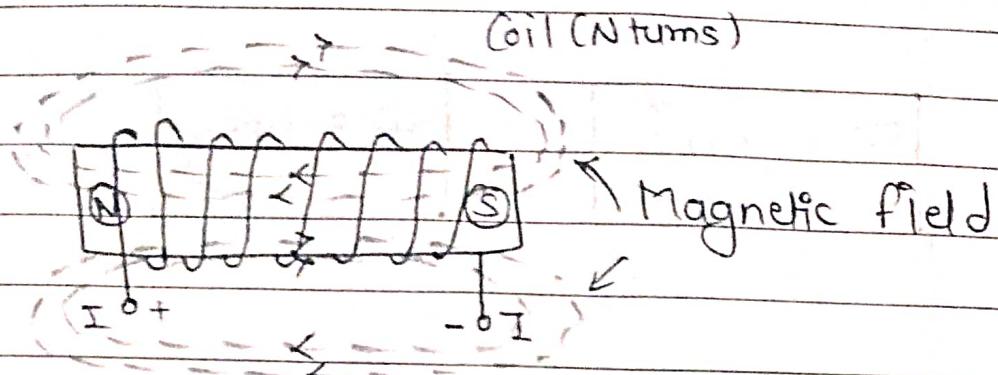
$$B = \mu_0 I$$

$\mu = \text{magnetic permeability}$

$B_0 = \text{permeability of free space}$

$I = \text{current permeability}$

\* (MMF) Magnetomotive Force :-



The force required for generation / flow of magnetic flux, in a magnetic circuit.  $N \Rightarrow$  turn

$$\boxed{MMF = NI}$$

Amperes Turns  
AT

$I \Rightarrow$  Current

\* Reluctance :- Opposition to flow of magnetic flux by material called... (S)

$$\boxed{S = \frac{l}{\mu a}}$$

$l \Rightarrow$  Length  
 $a \Rightarrow$  Cross-sectional area  $m^2$   
 $\mu \Rightarrow$  permeability

$$\boxed{S = \frac{l}{\mu_0 a r_a}}$$

Amperes Turns      AT  
Weber                Wb

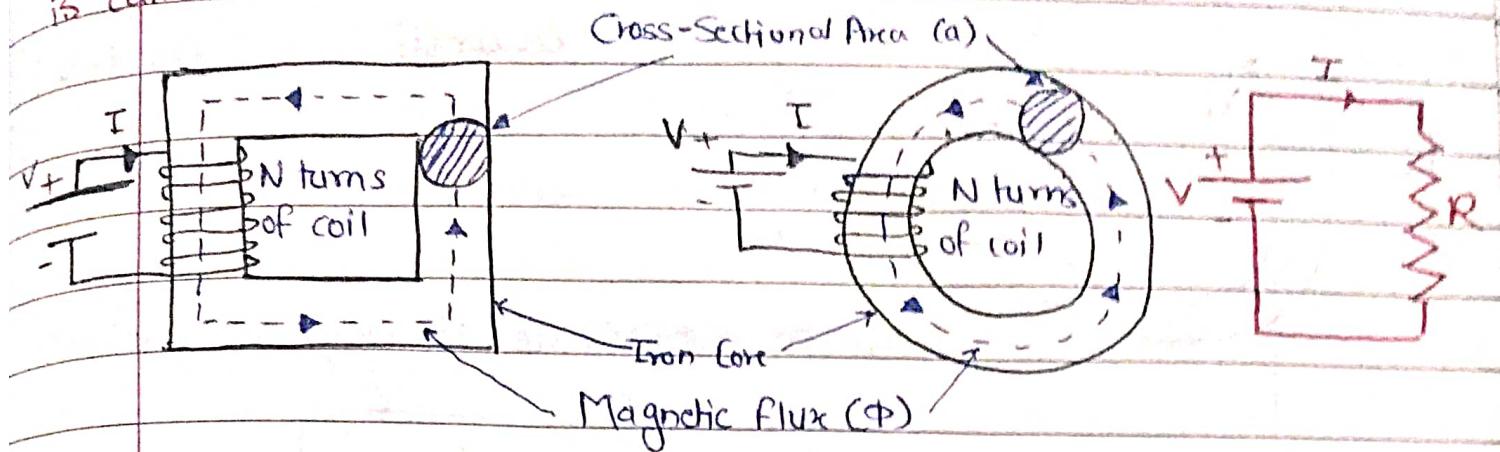
$$\boxed{S = \frac{mmf}{\Phi}}$$

$$\boxed{S = \frac{NI}{\Phi}}$$

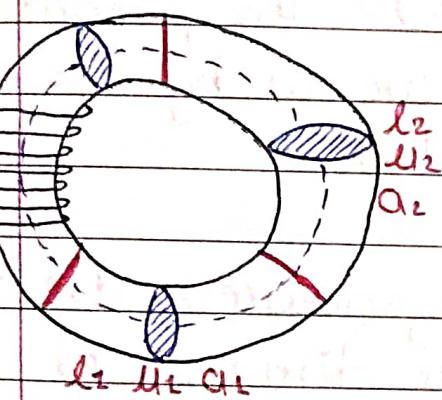
\* Permeance :- Reciprocal of reluctance

$$\boxed{\text{Permeance} = \frac{1}{\text{Reluctance}}} \quad \text{Wb/AT}$$

\* Magnetic Circuit :- A closed path followed by magnetic lines of force that means magnetic flux, is called as 'MAGNETIC CIRCUIT'.



\* Series Magnetic Circuit :- same flux



$$\Phi = MMF \quad \text{--- (1)}$$

$$ST = \frac{l_1}{\mu_1 A_1} + \frac{l_2}{\mu_2 A_2} + \frac{l_3}{\mu_3 A_3} \quad \text{--- (2)}$$

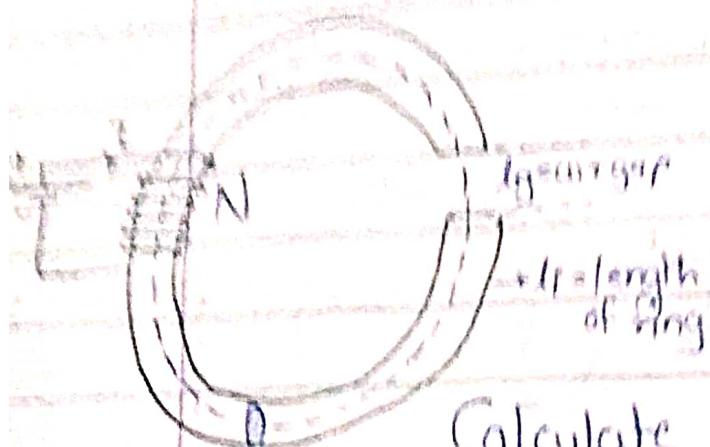
from (1) and (2)

$$\begin{aligned} MMF_T &= [MMF]_1 + [MMF]_2 + [MMF]_3 \\ &= \Phi [S_1 + S_2 + S_3] \\ &= \Phi \left[ \frac{l_1}{\mu_1 A_1} + \frac{l_2}{\mu_2 A_2} + \frac{l_3}{\mu_3 A_3} \right] \end{aligned}$$

$$H = NI$$

$$\therefore MMF_T = H_1 l_1 + H_2 l_2 + H_3 l_3$$

## Magnetic Circuit with air gap:



$$\text{St} = \frac{l}{l_g}$$

$$H_{\text{air}} = \frac{B}{\mu_0}$$

$$S_{\text{gap}} = \frac{l_g}{H_{\text{air}}}$$

$$H_{\text{air}} = 1 \text{ ... air}$$

Calculate separate if gap is present

$$\Phi = \frac{\text{MMF}}{S_t}$$

$$S_t = l_i + l_g$$

$$H_{\text{air}}; H_{\text{air}}$$

- Electromagnetic Induction (EMF): - The phenomenon in which magnetic flux lines are cut by the conductor, to induce emf, is called as.....

\* Lenz's Law: When an emf is generated due to change in magnetic flux, the direction of induced emf is such that it produces a current that opposes the cause responsible for inducing emf.

$$e = -N \frac{d\Phi}{dt}$$

\* Faraday's Law of Electromagnetic Induction :-

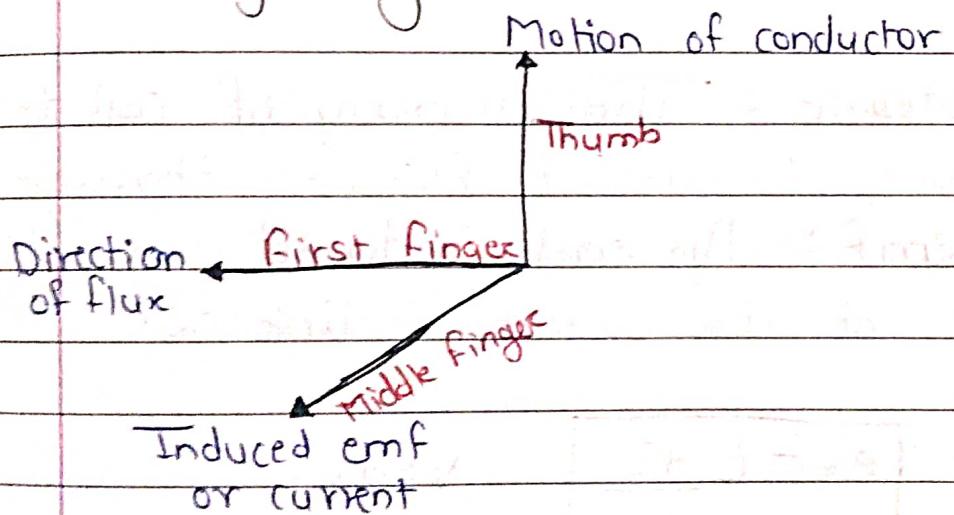
1st :- When ever the flux lines linking with a coil or conductor change ; an emf is induced in the coil or conductor.

2nd :- The magnitude of induced emf directly proportional to rate of change of flux linkage

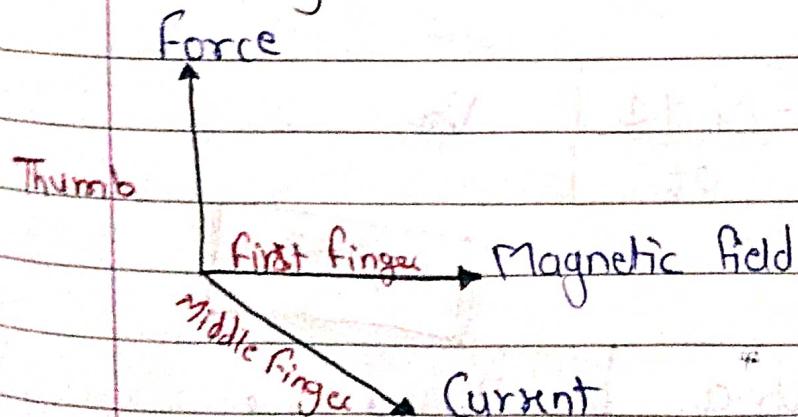
$$e = N \frac{d\phi}{dt} \quad \text{--- Number of turns of coil}$$

\* laws to decide Direction of induced emf

① Fleming's Right Hand Rule :- Conductor Generator



② Fleming's Left Hand Rule :- Generator Motor



\* 1) Dynamically Induced EMF :- If an induced emf is due to physical movement of coil or magnet, then it is called.....

$$e = B l V \sin \theta$$

\* 2) Statically Induced emf :- If an emf is induced without physical movement of coil or magnet, but due to changing current in a coil

$$d\phi$$

$$dt$$

\* 3) Self Inductance :- The property of coil to oppose the change in current flowing through it.  
 Self Induced emf :- An emf induced in coil due to change of its own flux linkage.

$$e = -L \frac{di}{dt}$$

Volts

$$e = -N \frac{d\phi}{dt}$$

Volt

$$L = \frac{N^2}{S}$$

$$L = N^2 \mu_0 A r a$$

$$L = \frac{N\phi}{I}$$

Henry

+ Force on a current carrying conductor placed in a magnetic circuit :-

$$F = IBL \sin\theta$$

Fleming's  
Right / Left  
Hand Rule

4) Mutual Inductance ( $M$ ) :-

$$e_2 = -M \frac{dI_1}{dt}$$

Volts

$$M = N_2 \Phi_2$$

$$M = \frac{N_2 k_1 \Phi_1}{I_1}$$

$$M = \frac{K_1 N_1 N_2}{S}$$

$$M = \frac{N_1 N_2 U_0 H_{ra}}{l}$$

$K_1$  fraction of flux

$$\Phi = N_1 I_1$$

$$M = \frac{N_1 N_2}{S}$$

$$M = 1$$

$$\Phi = e^{xL}$$

## ~~Faraday's Law of Electromagnetic Induction~~

\* IMP

### Derivation of Coefficient of Coupling ( $k$ ):

- If coil A carries current  $I_1$  and part of  $\Phi_1$  gets linked in coil B then mutual inductance is

$$M = \frac{N_2 I_1 \Phi_1}{I_1} \quad \dots \dots \textcircled{1}$$

- Coil B carries current  $I_2$  produces main flux  $\Phi_2$  and  $\Phi_2$  gets linked with coil A then mutual inductance is

$$M = \frac{N_1 K_2 \Phi_2}{I_2} \quad \dots \dots \textcircled{2}$$

Multiply  $\textcircled{1}$  and  $\textcircled{2}$

$$M^2 = \frac{N_2 K_1 \Phi_1}{I_1} \cdot \frac{N_1 K_2 \Phi_2}{I_2}$$

$$M^2 = K_1 K_2 \left[ \frac{N_1 \Phi_1}{I_1} \right] \left[ \frac{N_2 \Phi_2}{I_2} \right]$$

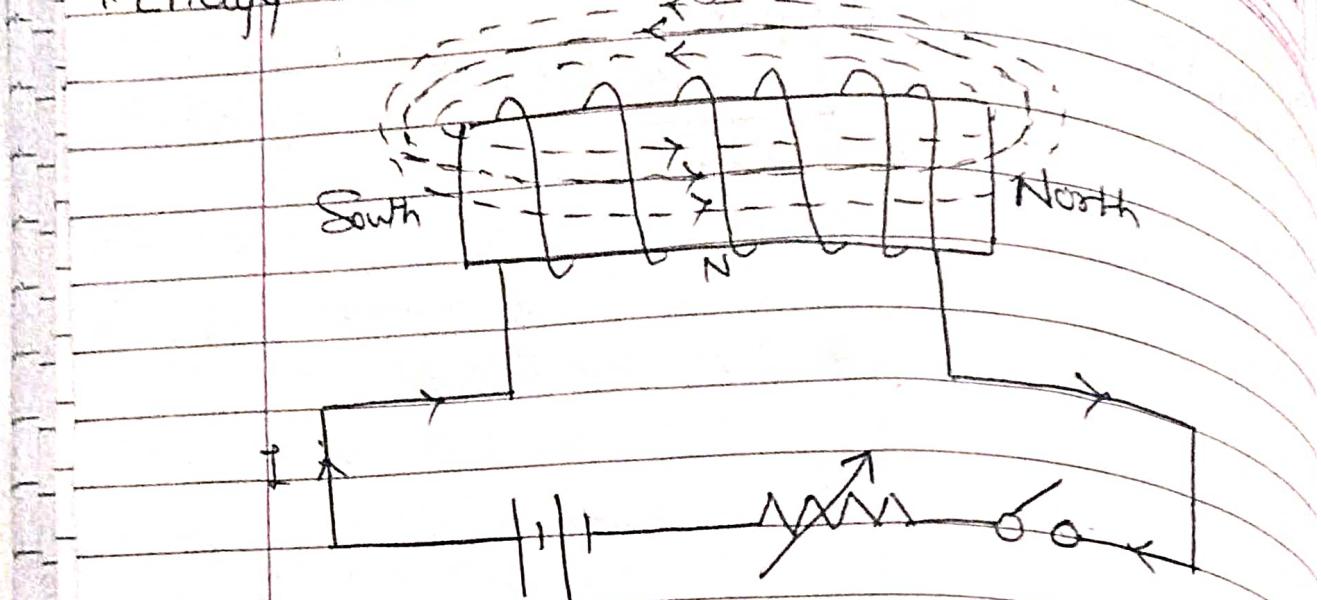
$$\therefore L = \frac{N \Phi}{I}$$

$$M^2 = K_1 K_2 L_1 L_2$$

$$M = \sqrt{K_1 K_2 \cdot L_1 L_2}$$

## (Solenoid)

\* Energy Stored in Magnetic Field :-



$$C = -L \frac{dI}{dt}$$

$$E = L \frac{dI}{dt} \times I \times dt$$

$$V = -e$$

$$E = L dI \cdot I$$

integrating

$$V = - \left[ -L \frac{dI}{dt} \right]$$

$$\text{Energy stored} = \int_0^I L dI \times I$$

$$V = L \frac{dI}{dt}$$

$$= L \int_0^I dI \times I$$

$$\text{Power} = V \times I$$

$$= \left[ \frac{I^2}{2} \right]_0^I$$

$$= L \frac{dI \times I}{dt}$$

$$E = \frac{1}{2} L I^2 \dots \text{Joules}$$

Energy stored in the  
magnetic field  $\frac{dt}{dt}$

$$\therefore E = \frac{1}{2} LI^2$$

$$= \frac{1}{2} \frac{N\Phi}{I} \times I^2$$

$$E = \frac{1}{2} NI \times B \times a \quad \dots \quad B = \frac{\Phi}{a} \quad \therefore B \propto \Phi$$

$$E = \frac{1}{2} H \times l \times B \times a \quad \dots \quad \therefore H = Nz$$

$$E = \frac{1}{2} H \times B \times (l \times a) \quad \dots \quad [\text{volume} = l \times a]$$

Energy stored per unit volume  $= \frac{1}{2} HB$

$$= \frac{1}{2} \mu H^2 \quad \dots \quad B = \mu H$$

Joules/m<sup>3</sup>

$$= \frac{1}{2} \frac{B^2}{\mu} \quad \text{Joules/m}^3$$

$$\text{Area} = \frac{\pi d^2}{4} = \pi r^2$$

- Q An aircored solenoid 1m in length and 10 cm in diameter has 5000 turns calculate ① Self induction ② Energy stored in magnetic field when current of 2A flows in the solenoid.

Given:-

$$\text{length} = 1\text{m}$$

$$N = 5000 \text{ turns}$$

$$\text{diameter} = 10\text{cm} = 10 \times 10^{-2}\text{m}$$

$$\text{Current (I)} = 2\text{A}$$

To find:- ① Self inductance ② Energy stored

Soln :- ① Self inductance ( $L$ )

$$L = N^2 \mu_0 A r$$

$$\mu_r = 1$$

$$= \frac{5000 \times 5000 \times 4\pi \times 10^{-7}}{2} \times 1 \times \pi \times (10 \times 10^{-2})^2$$

$$= 98698.844 \times 0.2467$$

$$\text{② Energy stored} = \frac{1}{2} L I^2$$

$$= \frac{1}{2} \times (0.2467) \times (2)^2$$

$$= 0.4934$$

II If a current of 5A flowing in coil with 1000 turns wound on a ring of ferro magnetic material produces flux of 0.5mWb in the ring calculate (1) self induction of coil (2) EMF induced in coil when current is switched off and reaches zero value in 2ms. (3) Mutual induction in coils if 2nd coil with 750 turns is wound uniformly over the 1st one

Given:-  $I = 5\text{A}$        $t = 2\text{ms} = 2 \times 10^{-3} \text{ s}$   
 $N_1 = 1000$        $N_2 = 750$   
 $\Phi = 0.5\text{mWb} = 0.5 \times 10^{-3} \text{ Wb}$

To find :- (1) L (2) EMF when  $I=0$  (3) M

Soln:- (1)  $L = \frac{N\Phi}{I} = \frac{1000 \times 0.5 \times 10^{-3}}{5} = 0.1 \text{ Henry}$

(2)  $e = -L \frac{dI}{dt} = 0.1 \left[ 0 - 5 \right] \frac{1}{2 \times 10^{-3}} = \frac{0.5}{2 \times 10^{-3}} = 250 \text{ Volts}$

(3)  $M = \frac{N_2 \Phi_2}{I_1} = \frac{N_2 \Phi_1 K_1}{I_1} \quad \therefore \text{uniformly then } K_1 = 1$   
 $= \frac{750 \times 0.5 \times 10^{-3}}{5} = 0.075 \text{ H}$