

Unit : 4

4. Analysis of Trusses

* Truss:-

Truss is the structure which is formed by connecting various two force members to each other by using pin joint.

* Plane truss:

When all members of truss lies in one plane, then truss is known as plane truss.

* Rigid truss: A truss which do not collapse when external load is applied on it.

* Simple truss: The structure formed by basic triangle made by connecting various members are called simple truss.

* Classification of Truss

Perfect truss

(Stable)

$(n = 2j - R)$

Imperfect truss
(unstable)

$(n \neq 2j - R)$

Overset

(Redundant) Truss

$(n > 2j - R)$

Deficient

Truss

$(n < 2j - R)$

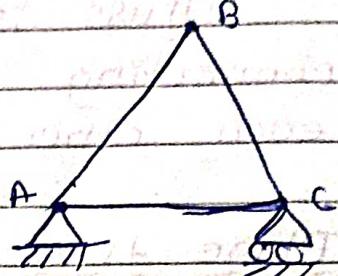
> Perfect truss : A truss which ~~not~~ does not collapse under the action of load is called...

Condition : $n = 2j - R$

n = no. of members

j = no. of joints

R = no. of Reaction



In truss ABC, $n = 3$ & $2j - R = 3$, $n = 3$

\therefore Perfect truss

$$j = 3$$

$$R = 3$$

* Imperfect Truss: A truss which collapses under the action of load is called imperfect truss

Condition : $n = 2j - R$ Here, $n \neq 2j - R$

n = no. of members

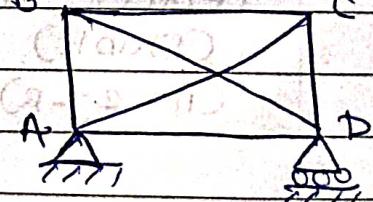
j = no. of joints

R = no. of Reaction

* Overstable (Redundant) Truss

A truss in which $n > 2j - R$,

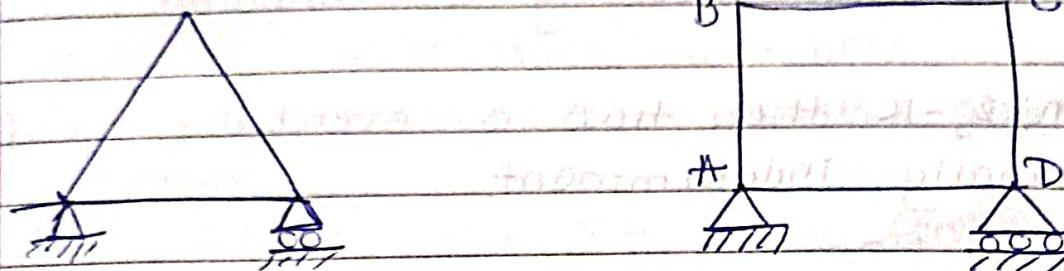
then it is overstable truss



↓ A redundant truss is composed of no. of members more than req. to keep the truss stable

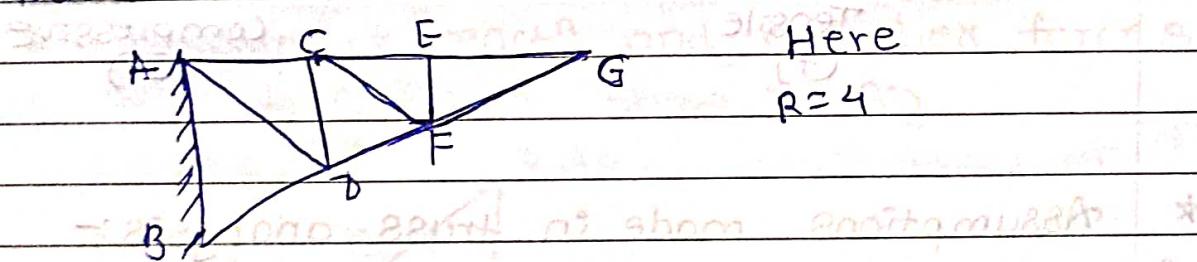
* Deficient Truss:

It is composed of no. of members less than that req. to keep the truss stable.



* Cantilever Truss:

A truss which is fixed on one side & force at other end is called as cantilever truss.



* Determinacy of truss:-

i) Ext Support

Support reactⁿ of truss can be found out using three condition of equilibrium
Conditions:- $\sum F_x = 0$; $\sum F_y = 0$; $\sum M = 0$

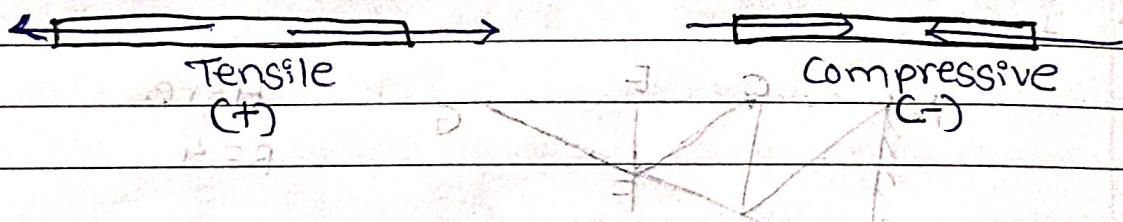
ii) Int force members

If all the axial forces in the truss member can be found out using eqn of equilibrium, $\sum F_x = 0$; $\sum F_y = 0$

- If $n = 2j - R$ then truss structure is perfect, stable and internally determinant.
- If $n < 2j - R$, then truss structure is imperfect unstable but internally determinant.
- If $n > 2j - R$ then truss is overstable and internally indeterminant.

* Two force members

Members of truss must be two force members and forces must be axial acting at ends can be compressive or tensile



* Assumptions made in truss analysis:-

- Truss is a perfect truss
- Truss can be internally determinant and stable
- All members of truss are connected by pin joints only
- All members of truss are two force members
- Self weight of members are neglected
- All ext ~~ext~~ loads are acting at joints only.

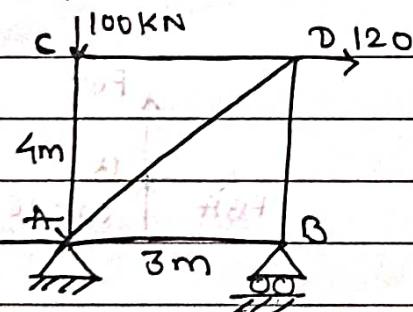
* Determination of axial force in the member of truss

i) Joint method:

- Use equilibrium equations i.e $\sum F_x = \sum F_y = \sum M = 0$ to find support reactions.
- Identify zero force members
- Draw FBD of a joint where, unknown is minimum
- Use $\sum F_x = 0$ and $\sum F_y = 0$ to find unknown force
- Proceed to next joint, where unknown is minimum
- At last joint verify $\sum F_x = 0$ & $\sum F_y = 0$

② Numericals:

(i) Find support reactⁿ and member forces of the truss as show in fig.



Ques To find support Reaction

$$\sum F_x = 0$$

$$H_A + 120 = 0$$

$$H_A = -120 \text{ kN}$$

$$\sum F_y = 0$$

$$V_A + V_B = 100 \quad \dots \textcircled{1}$$

$$\sum M_A = 0$$

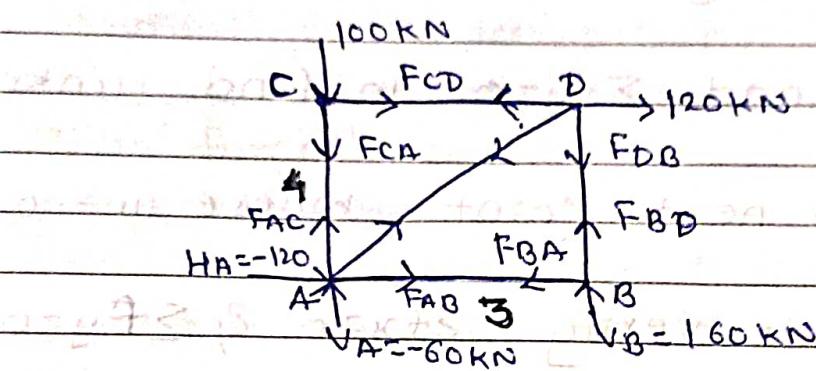
$$-(V_B \times 3) + (120 \times 4) = 0$$

$$V_B = 160 \text{ kN}$$

from ①

$$V_A = -60 \text{ kN}$$

To find member forces: —

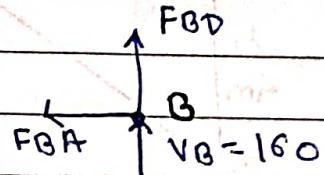


(Start from pt B less unknown forces) (B is at base)

i) At point B

$$\sum f_x = 0$$

$$F_{AB} = 0$$



$$\sum f_y = 0$$

$$F_{BD} = -160 \text{ kN}$$

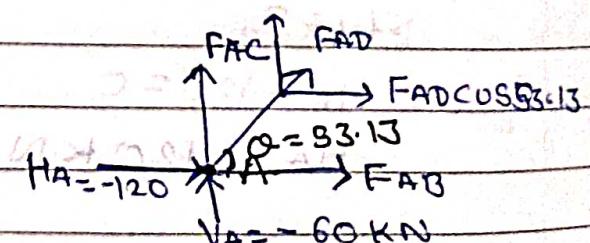
$$FAD \sin 53.13$$

ii) At joint A

$$\sum f_x = 0$$

$$-120 + F_{AD} + FAD \cos 53.13 = 0$$

$$[FAD = 200]$$



$$\theta \Rightarrow \tan \theta = \frac{4}{3} \quad \theta = \tan^{-1} \left(\frac{4}{3} \right)$$

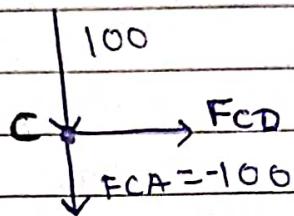
$$\theta = 53.13$$

$$\sum F_y = 0$$

$$-60 + F_{AC} + 200 \sin 53^\circ 13^\circ = 0$$

$$[F_{AC} = -100]$$

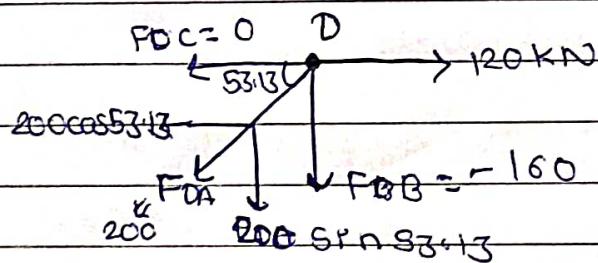
iii) At joint C



$$\sum F_x = 0$$

$$F_{CD} = 0$$

iv) At joint D



$$\sum F_x = 0$$

$$-0 + 120 - 200 \cos 53^\circ 13^\circ = 0$$

$$0 = 0$$

$$\sum F_y = 0$$

$$+160 - 200 \sin 53^\circ 13^\circ = 0$$

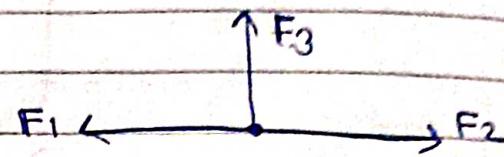
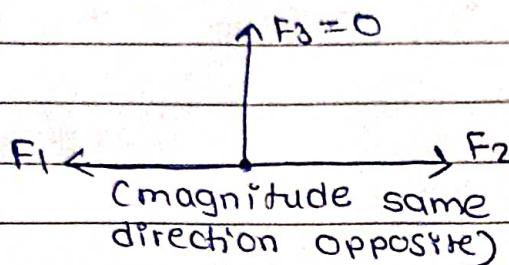
$$0 = 0$$

* Table :-

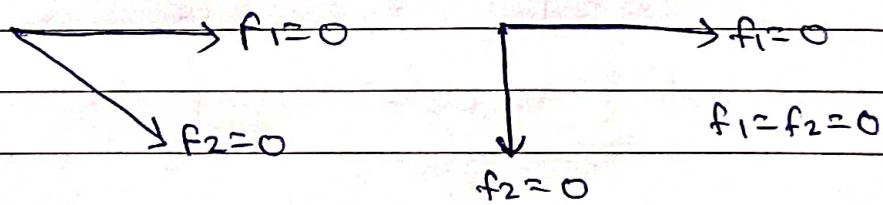
Member	Force	Nature
AB	0	-
AC	100	C
AD	200	T
BD	160	C
CD	0	-

* Zero Force Members:-

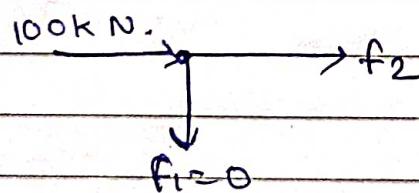
- i) If there are three members at a joint out of which two are collinear and no external force acts on that joint third member is zero force member.



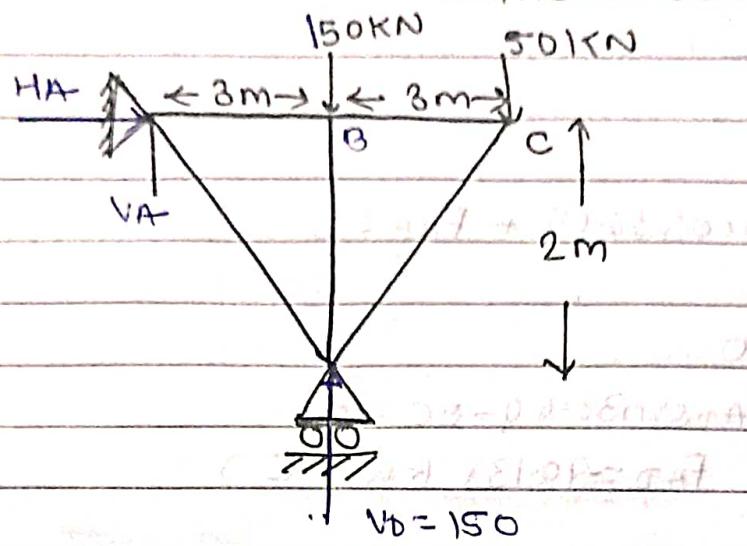
- ii) If there are only two members at a joint and there is no external force at that joint, than both member are zero force members.



- iii) If there are only two members at a joint and external force is acting along one member than other is zero force member.



Q) Determine each member of truss as shown in fig and tabulate the result.

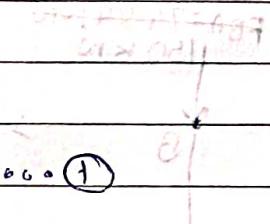


$$\text{Eqn } \sum F_x = 0$$

$$H_A = 0$$

$$2) \sum F_y = 0$$

$$V_A + V_B = 200 \text{ kN}$$



$$3) M_A = 0$$

$$-(V_D \times 3) + (150 \times 3) + (430 \times 6) = 0$$

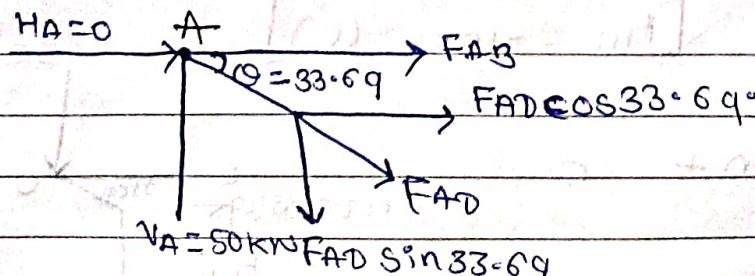
$$V_D = 280$$

$$280 - 50 = 230$$

from eqn ①

$$V_A = -50 \text{ kN}$$

At joint A



At joint (3)

$$\theta = 33.69^\circ$$

$$\sum F_{x30}$$

$$0 + F_{AD} \cos 33.69^\circ + F_{AB} = 0$$

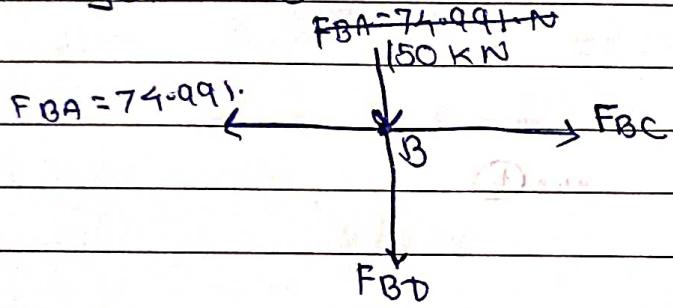
$$\sum f_y = 0$$

$$-F_{AD} \sin 33.69^\circ - 80 = 0$$

$$F_{AD} = -90.138 \text{ kN (C)}$$

$$F_{AB} = 74.99 \text{ kN}$$

ii) At joint B



$$\sum f_x = 0 \rightarrow (x \times 74.99) + (x \times 150) + (x \times 74.99) = 0$$

$$F_{BC} - F_{BA} = 0$$

$$F_{BC} = F_{BA}$$

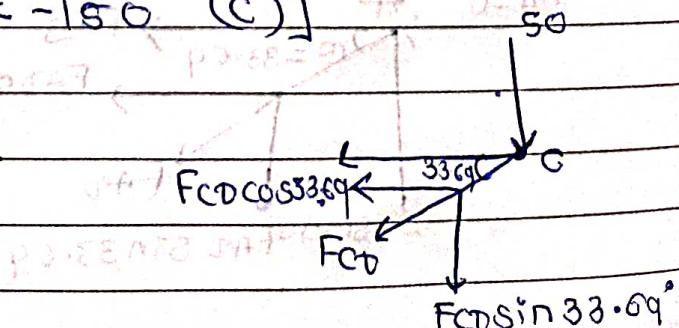
$$F_{BC} = 74.99$$

$$\sum f_y = 0$$

$$-F_{BD} - 150 = 0$$

$$[F_{BD} = -150 \text{ (C)}]$$

At joint + C

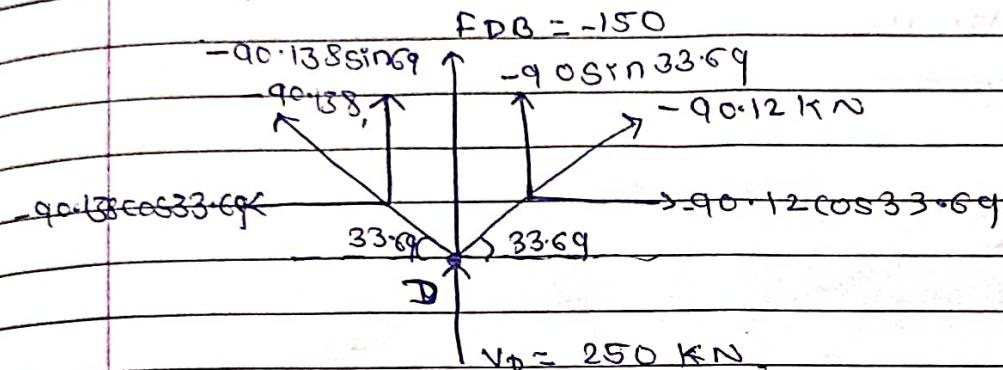


$$\sum F_x = 0$$

$$-74.99 - F_{CD} \cos 33.69^\circ = 0$$

$$F_{CD} = -90.12 \text{ kN} \quad (\text{C})$$

At joint D (last).



$$\sum F_x = 0$$

$$-90.12 \cos 33.69^\circ + 90.138 \cos 33.69^\circ = 0$$

$$0 = 0$$

$$\sum F_y = 0$$

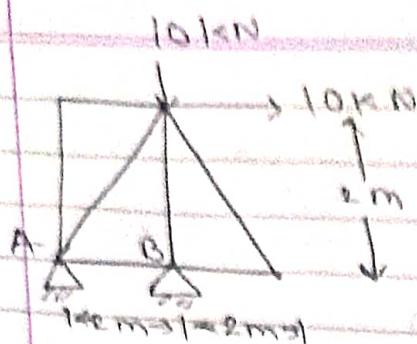
$$-90.138 \cos 33.69^\circ - 90.12 \sin 33.69^\circ - 150 - 250 = 0$$

$$0 = 0$$

② Table:-

Member	Force	Nature
F_{AB}	90.138	C
F_{AB}	74.99	T
F_{BC}	74.99	T
F_{CD}	90.12	C
F_{DB}	150	C

Q) Identify Zero force members and determine forces?



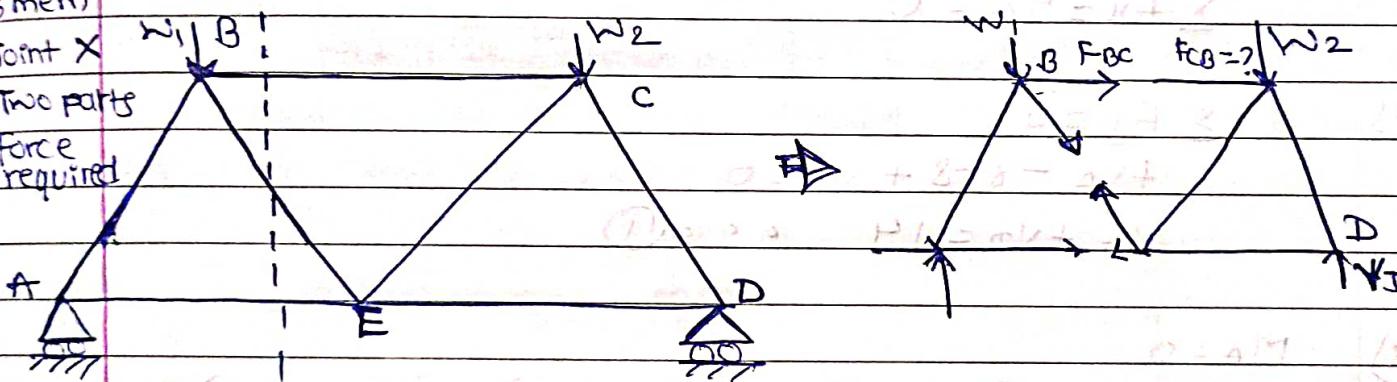
Here two members
are present with no
external load.

$$F_{DF} = 0$$

$$F_{DA} = 0$$

* Section Method:

- 1) Find the support reactions using three equations of equilibrium.
 - 2) Draw forces in the required members.
 - 3) Cut this members by an imaginary sections i.e. laying or curve such that truss structure divides into two separate parts.
- Note:-
- a) Line or curve do not cut more than three members
 - b) Line and curve should be passed through members only not through joint.



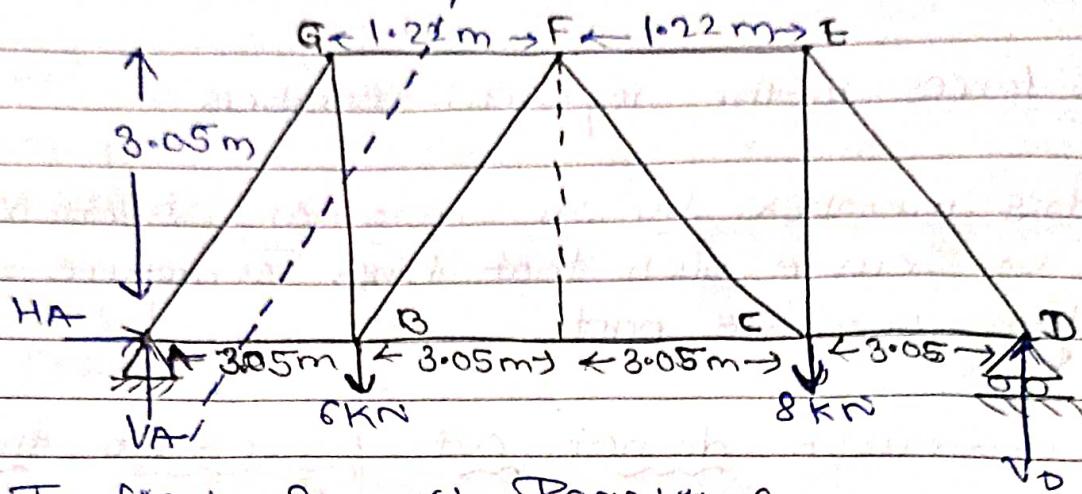
- 4) Consider only one part for analysis i.e. called as configuration diagram.
- 5) Again apply static equilibrium equation i.e. $\sum F_x = 0$, $\sum F_y = 0$ & moment about any point = 0 in configuration diagram.

Note:-

In $\sum F_x = 0$, $\sum F = 0$ & $M_O = 0$ only those forces must be considered which are involved in the configuration diagram.

Q)

Determine force develop in members GB and GF of the truss and state if this members are in tension or compression.



Q) To find Support Reactions

$$\sum F_x = 0$$

$$\sum F_x = H_A = 0$$

$$\sum F_y = 0$$

$$+V_A - 6 - 8 + V_D = 0$$

$$V_A + V_D = 14$$

①

$$M_A = 0$$

$$M_A = + (6 \times 3.05) + (8 \times 9.15) - (V_D \times 12.2) = 0$$

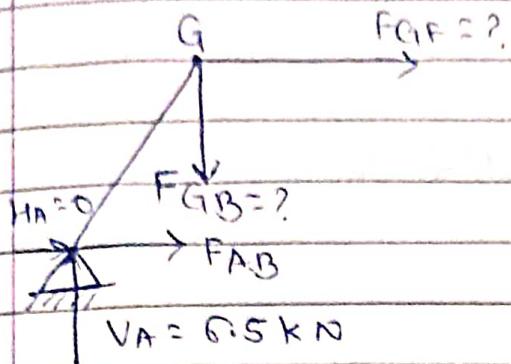
$$V_D = + (6 \times 3.05) + (8 \times 9.15) = 7.5 \text{ kN}$$

12.12

$$V_D = 7.5 \text{ kN}$$

from ①

$$V_A = 6.5 \text{ kN}$$



$$\sum F_y = 0$$

$$-F_{GB} + 6.5 \text{ kN} = 0$$

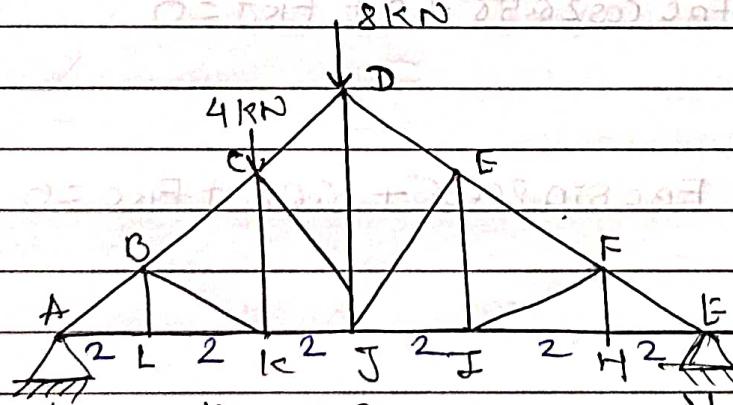
$$F_{GB} = 6.65 \text{ kN} \quad (\text{T})$$

$$3) M_A = 0$$

$$+ (F_{GF} \times 3.05) + (6.5 \times 3.05) = 0$$

$$F_{GF} = -6.5 \text{ kN} \quad (\text{C})$$

(Q) Determine the force in members BC, EI and KJ and state if these members are in tension or compression



$$\rightarrow \sum F_x = 0$$

$$H_A = 0$$

$$3) \sum F_y = 0$$

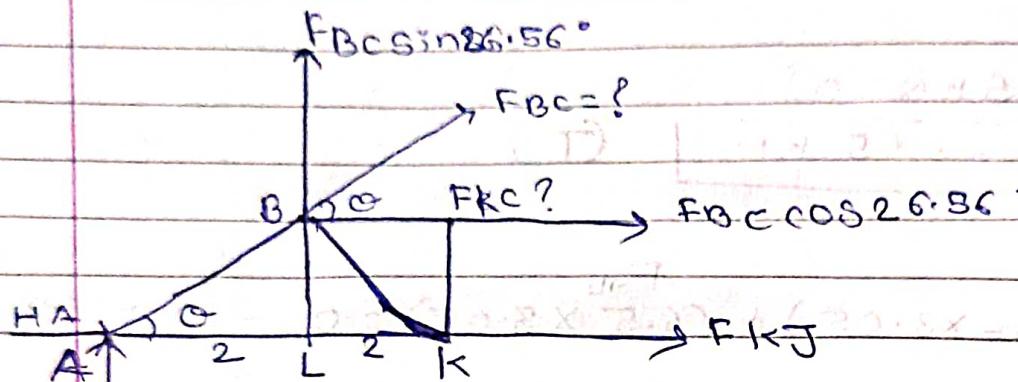
$$V_F + V_G = 12 \quad \text{Ans} \quad (1)$$

$$3) \sum M_A = 0$$

$$4(4 \times 4) + (8 \times 6) - (V_A \times 12) = 0$$

$$V_A = 5.33 \text{ kN}$$

$$V_A = 6.67 \text{ kN}$$



$$\tan \theta = \frac{3}{6} \quad [\theta = 26.56^\circ]$$

$$1) \sum F_x = 0$$

$$F_{Bc} \cos 26.56^\circ + 0 + F_{IJ} = 0$$

$$2) \sum F_y = 0$$

$$F_{Bc} \sin 26.56^\circ + 6.67 + F_{Kc} = 0$$

$$3) \sum M_A = 0$$

$$-(F_{Bc} \sin 26.56^\circ \times 2) + (F_{Bc} \times \cos 26.56^\circ \times 1) - (F_{Kc} \times 4) = 0$$

$$-0.89 F_{Bc} + 0.89 F_{Bc} - F_{Kc} \times 4 = 0$$

$$\boxed{F_{Kc} = 0}$$

$$F_{BC} \sin 26.56^\circ = -6.67$$

$$F_{BC} = \frac{-6.67}{0.447} = -14.92 \text{ kN (C)}$$

$$[F_{BC} = -14.92 \text{ kN}] \text{ (C)}$$

$$F_{KJ} = 14.92 \cos 26.56$$

$$[F_{KJ} = 13.34]$$

* Cables:-

- Cables are used in engineering structures to support different types of loads. They are commonly used in cranes, transmission lines, suspension bridges etc. Normally cables are subjected to point load.

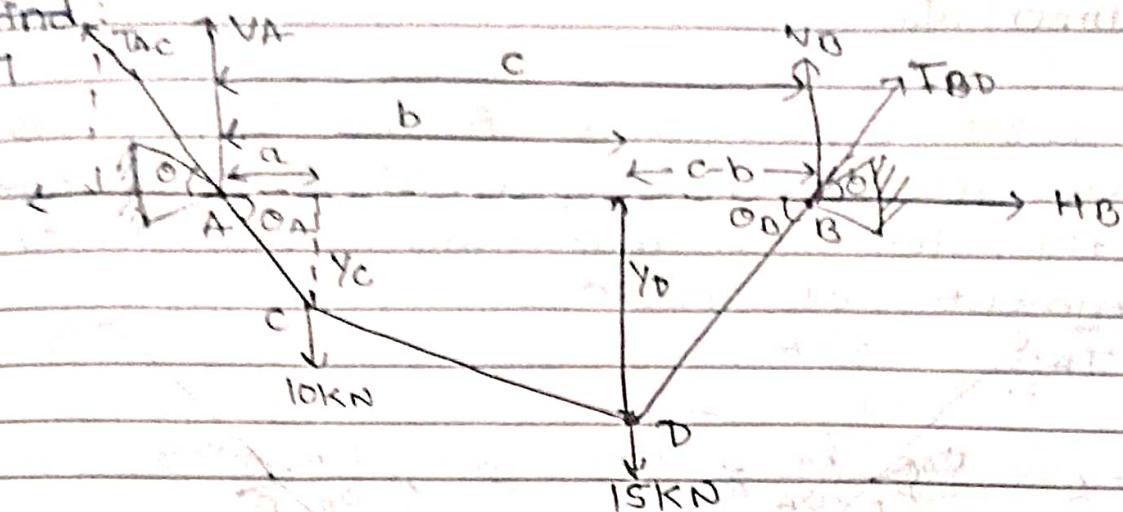
* Assumption in cables :-

- 1) The material of cable is flexible but inextensible in nature.
- 2) Self weight of cables is neglected.
- 3) Cables are.
- 4) All loads acting are vertical.
- 5) Vertical as-well-as horizontal distance of one the external load is known from one support.
- 6) Cable carries only tension.

* Steps for analysis of cable;

- 1) Draw FBD of complete cable and find support reactions.
- 2) Support Reactions can be found out by using 3 equilibrium equations.
 $\sum F_x = 0$; $\sum F_y = 0$ & $\sum M_O = 0$
- For
- 3) A fourth unknown consider - section betw any two points & take moment about that point is equal to zero (Take Moment either from left or right part).
- 4) Find Reactions at ends and it will equal to tension at that point.

g) Find:



y

$$\sum F_x = 0$$

$$\sum F_y = 0$$

$$\sum M_A = 0$$

$$\sum M_D = 0 \quad \text{OR}$$

By Pythagoras theorem,

$$T_{BD} = R_B = \sqrt{H_A^2 + V_B^2}$$

$$T_{AC} = R_A = \sqrt{H_A^2 + V_A^2}$$

$$\tan \theta_B = \frac{V_B}{H_B}$$

$$\tan \theta_A = \frac{V_A}{H_A}$$

$$\tan \theta_B = \frac{Y_D}{c-b}$$

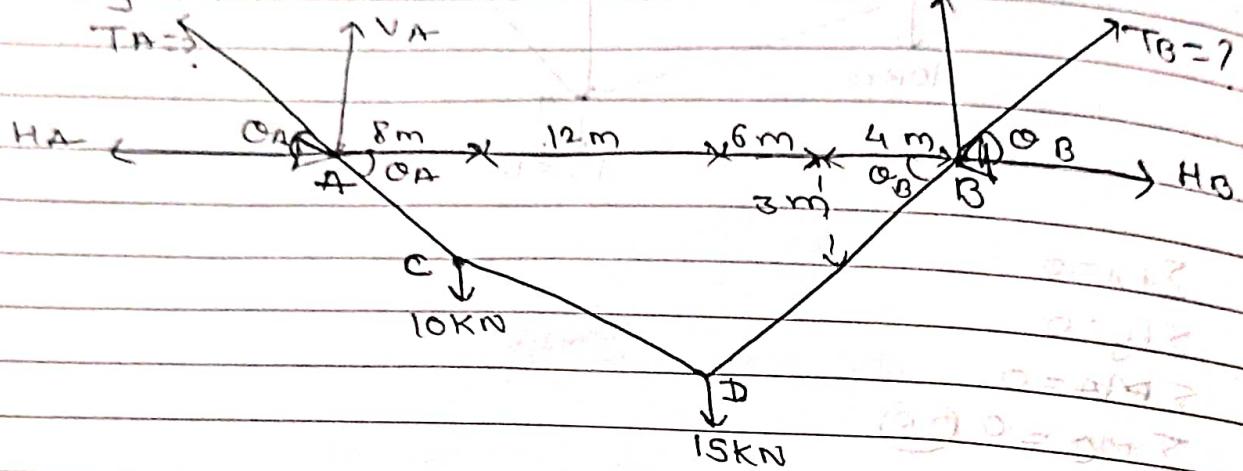
$$\tan \theta_A = \frac{Y_C}{a}$$

$$\therefore \tan \theta_B = \frac{Y_D}{c-b} = \frac{V_B}{H_B}$$

$$\therefore \tan \theta_A = \frac{V_A}{H_A} = \frac{Y_C}{a}$$

Numericals:

- Q) A cable supported at A and B at the same level over a span of 30m, as shown in fig. determine maximum tension in the segment of cable.



Using equilibrium equations,

$$\sum f_{rx} = 0$$

$$H_A = H_B$$

1)

$$\sum f_y = 0$$

$$V_A + V_B = 25 \text{ kN}$$

$$V_A + V_B = 25 = 25$$

2)

$$\sum M_A = 0$$

$$-(V_B \times 30) + (10 \times 8) + (15 \times 20) = 0$$

$$V_B = 12.67 \text{ kN}$$

eqn (1)

$$V_A = 12.33 \text{ kN}$$

$$4) \sum M_A = 0 R$$

$$\tan \theta_B = \frac{V_B}{H_B} = \frac{12.67}{H_B}$$

$$\tan \theta_B = \frac{3}{4}$$

$$\frac{12.67}{H_B} = \frac{3}{4} \quad H_B = 16.89 \text{ kN}$$

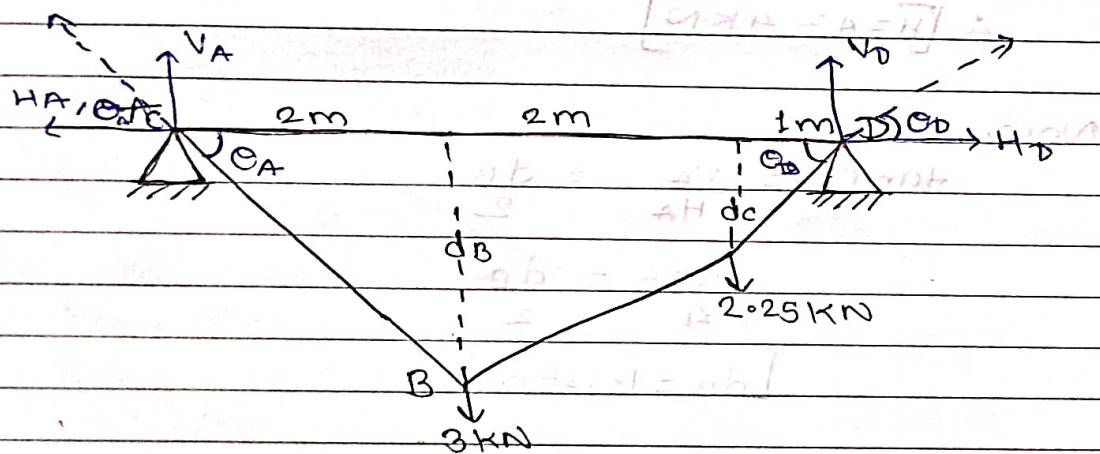
$$H_A = 16.89 \text{ kN}$$

$$T_B = R_B = \sqrt{(H_B)^2 + V_B^2}$$

$$[T_B = 21.11 \text{ kN}]$$

$$T_A = R_A = \sqrt{(H_A)^2 + V_A^2}$$

$$[T_A = 20.91 \text{ kN}]$$



$$\sum f_{xx} = 0 \quad \text{and} \quad P_{xx}^2 = F_{xx}^2 + F_{yy}^2 = AT$$

$$H_D = H_A$$

$$2) \sum F_y = 0$$

$$V_n + V_d = 5.25 \text{ kN}$$

$$3) \sum M_A = 0$$

$$-(V_d \times 5) + (2.25 \times 4) + (3 \times 2) = 0$$

$$\boxed{V_d = 3 \text{ kN}}$$

from eqn ①

$$\boxed{V_A = 2.25 \text{ kN}}$$

$$\tan \theta_D = \frac{V_d}{H_d} = 0.75$$

$$\boxed{H_d = 4 \text{ kN}}$$

$$\therefore \boxed{H = A = 4 \text{ kN}}$$

Now,

$$\tan \theta_A = \frac{V_A}{H_A} = \frac{d_B}{2}$$

$$\frac{2.25}{4} = \frac{d_B}{2}$$

$$\boxed{d_B = 1.125 \text{ m}}$$

Also,

$$T_d = \sqrt{H_d^2 + V_d^2} = 5 \text{ kN}$$

and

$$T_A = \sqrt{H_A^2 + V_A^2} = 4.589 \text{ kN}$$

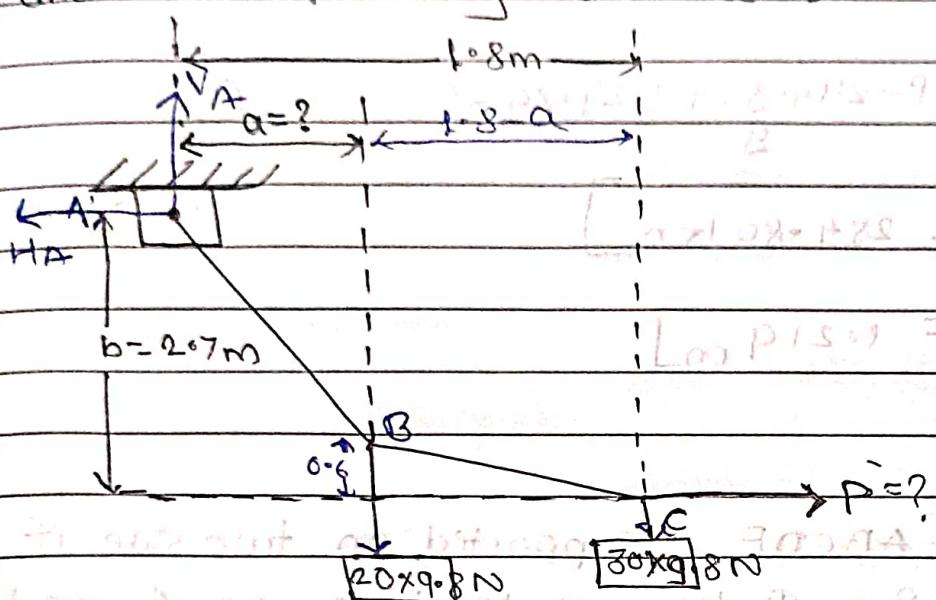
Hence Tension is max at cable CD.

* Horizontal force \rightarrow vertical distance

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Cables - Type 2

- Q1 Cable ABC supports two boxes as shown in fig knowing that $V = v = 2.7 \text{ m}$, determine the required magnitude of the horizontal force P and corresponding distance a.



Point

$$\Rightarrow \sum f_x = 0$$

$$H_A = P$$

$$\Rightarrow \sum f_y = 0$$

$$V_A = (20 \times 9.81) + (30 \times 9.81)$$

$$V_A = 490.51 \text{ N}$$

$$\Rightarrow \sum M_A = 0$$

$$-(P \times 2.7) + (20 \times 9.81 \times a) + (30 \times 9.81 \times 1.8) = 0$$

$$-2.7P + 196.2a + 529.74 = 0 \quad \text{--- (1)}$$

$$\sum M_B = 0$$

$$+ [30 \times 9.81 \times (1.8 - a)] - P \times 0.6 = 0$$

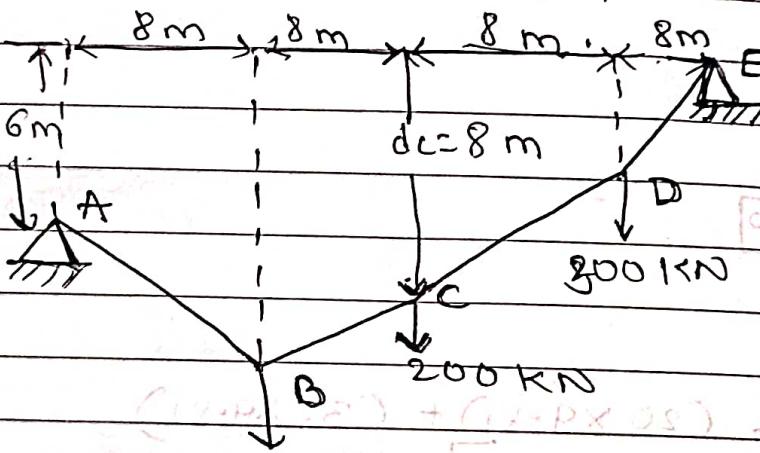
$$529.74 - 294.3a - 0.6P = 0$$

$$- 0.6P - 294.3a + 529.74 = 0 \quad \text{--- Eqn ②}$$

$$[P = 284.80 \text{ kN}]$$

$$[a = 1.219 \text{ m}]$$

Q2) Given ABCDE supported on two side if DC is equal to 8m. Determine reaction at A and



$$OF(8(81.25x - c)) + (ax^2 + bx + c) + (500x^2) = 0$$

$$(8a^2 + 8b + 8c) + 8ax^2 + 8bx + 8c + 500x^2 = 0$$

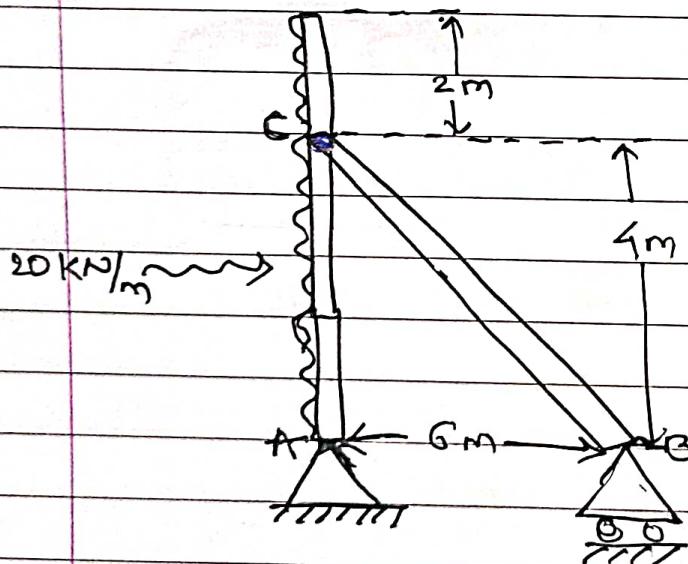
* FRAMES:-

Frames are structures consisting of several members connected to each other out of which at least one member is multi-force member that means member having non-co-axial force.

- > A member which is subjected to two equal opposite and collinear forces are called as two force members
- > Analysis of frame is done by using equation of equilibrium.

* Numerical

- Q) Determine components of Reactions pin joint at point C for the frame as shown in figure.

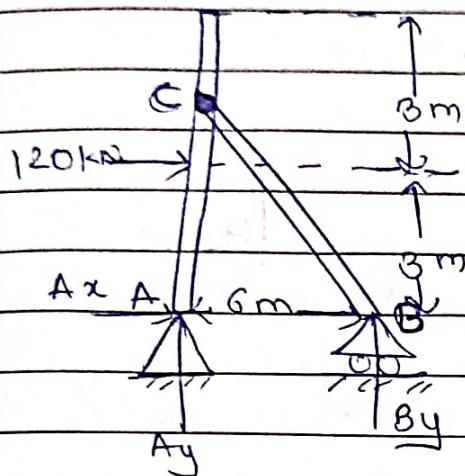


(Q1) UDL to point load

$$= \text{Load} \times \text{length}$$

$$= 20 \text{ kN} \times 6 \text{ m}$$

$= 120 \text{ kN}$ (It will act at center of length)



$$1) \sum f_x = 0$$

$$Ax + 120 = 0$$

$$Ax = -120 \text{ kN}$$

$$2) \sum f_y = 0$$

$$Ay + By = 0 \quad \dots \textcircled{1}$$

$$3) \sum M_A = 0$$

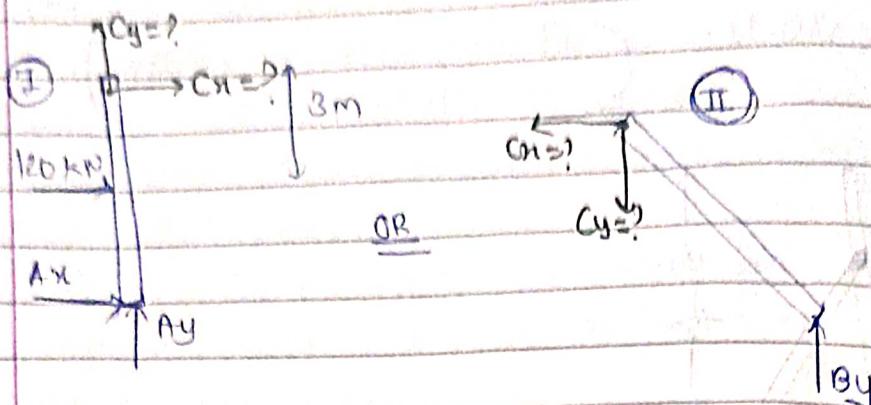
$$(-By \times 6) + (120 \times 3) = 0$$

$$\boxed{By = 60 \text{ kN}}$$

from $\textcircled{1}$

$$\therefore \boxed{Ay = -60 \text{ kN}}$$

* Deplating both bars



From part(I)

$$\sum F_x = 0$$

$$120 + Ax + Cx = 0$$

$$120 - 120 + Cx = 0$$

$$Cx = 0$$

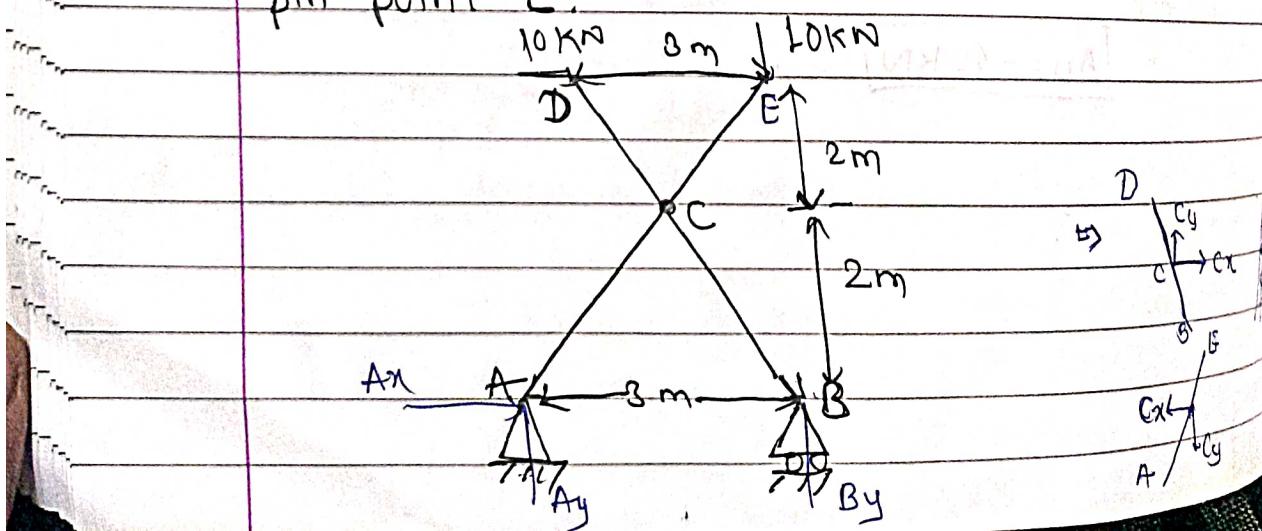
$$\sum F_y = 0 - 60$$

$$Cy + Ay = 0$$

$$Cy - 60 = 0$$

$$Cy = 60 \text{ kN}$$

Q) Find reactions at A and B and Forces at pin point C.



Ques 1

$$\text{1) } \sum f_x = 0$$

$$A_x + 10 = 0$$

$$A_x = -10 \text{ kN}$$

$$\text{2) } \sum F_y = 0$$

$$A_y + B_y - 10 \text{ kN} = 0$$

$$A_y + B_y = 10 \text{ kN} \quad \dots \quad \textcircled{1}$$

$$\text{3) } \sum M_A = 0$$

$$-(B_y \times 3) + (10 \times 4) - (10 \times 3) = 0$$

$$-B_y \times 3 + 10 - 30 = 0$$

$$-B_y \times 3 + 10 = 0$$

$$B_y = \frac{10}{3}$$

$$B_y = 3.33 \text{ kN}$$

From \textcircled{1}

$$A_y = 10 - 3.33$$

$$A_y = 6.67 \text{ kN}$$



Unit

3.

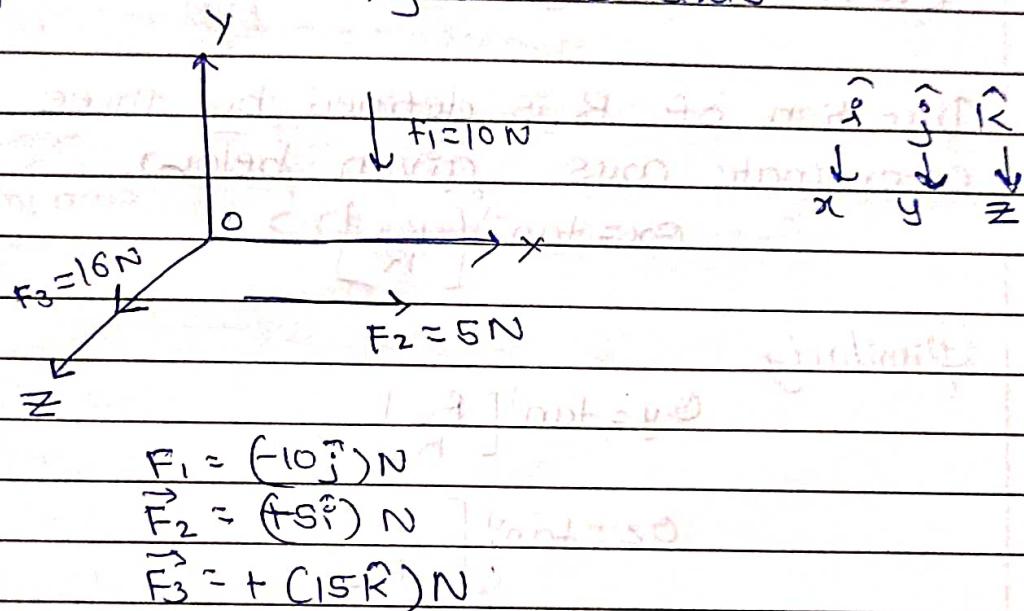
* Space:-

forces as vector

* Forces as vector in 3D

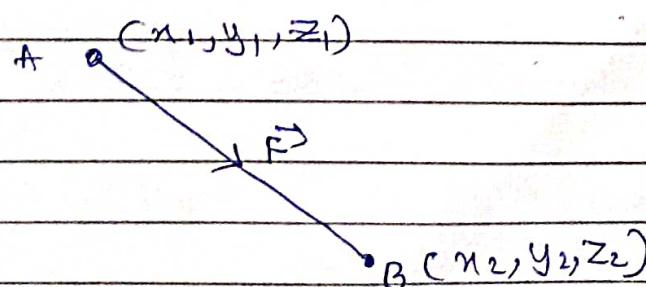
for expressing force in terms of Unit vectors $\hat{i}, \hat{j}, \hat{k}$ along x, y , and z axis are given below.

i) Forces parallel to x, y and z axis



ii) Two points on the line of action when known
Consider a force F

Consider a force F is directed from A to B then unit vector from A to B is



$$\vec{F} = F_{\text{mag}} \times \hat{e}_{AB}$$

mag direction = $\vec{F} \times$

$$[(x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}]$$

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

* Concurrent Force System:-

> Resultant of Concurrent force system can be found out by using $R_x = \sum f_x$

$$R_y = \sum f_y$$

$$R_z = \sum f_z$$

$$R = \sqrt{R_x^2 + R_y^2 + R_z^2}$$

> Direction of R is defined by three angles with co-ordinate axis given below.

$$\theta_x = \tan^{-1} \left[\frac{R_y}{R} \right]$$

Similarly

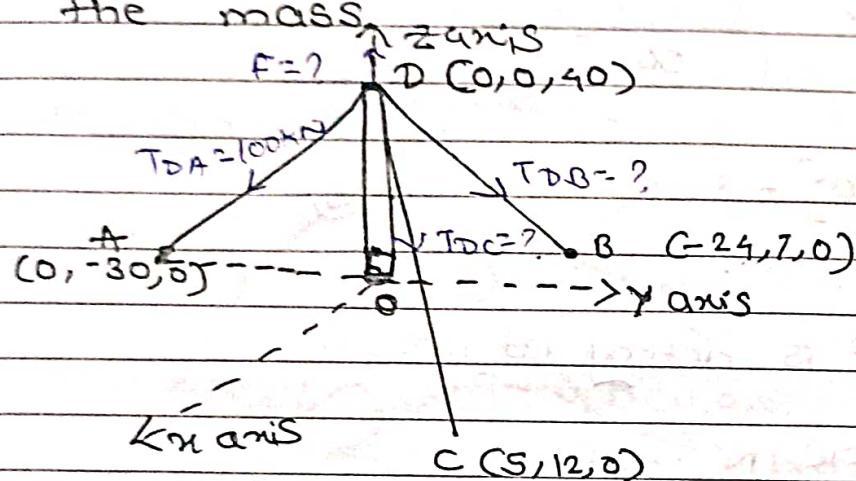
$$\theta_y = \tan^{-1} \left[\frac{R_z}{R} \right]$$

$$\theta_z = \tan^{-1} \left[\frac{R_x}{R} \right]$$

> Equation of equilibrium for concurrent force system $\sum F_x = 0, \sum F_y = 0, \sum F_z = 0$.

* Type-I Numerical; To find forces in Concurrent force system:-

Q) A vertical mass OI is having base O. Three cables DA, DB & DC Kept the mass in equilibrium, tension in cable DA is 100kN. Find tension in cable DC and DB and Force in the mass.



Ans

~~Given~~

$$T_{DA} = 100 \text{ kN}$$

$$F = ?$$

$$T_{DB} = ?, T_{DC} = ?$$

$$\text{Step (I)}: \vec{T}_{DB} = T_{DB} \times \hat{e}_{DB}$$

$$\vec{T}_{DB} = T_{DB} \times \left[\frac{(x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}}{\sqrt{(-24-0)^2 + (7-0)^2 + (0-40)^2}} \right]$$

$$\vec{T}_{DB} = \frac{T_{DB}(-24\hat{i} + 7\hat{j} - 40\hat{k})}{47.17} \quad \text{--- (1)}$$

$$\vec{T}_{DC} = T_{DC} \times \hat{e}_{DC}$$

$$\vec{T}_{DC} = T_{DC} \times \left[\frac{(x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}}{\sqrt{(5-0)^2 + (12-0)^2 + (6-40)^2}} \right]$$

$$T_{DA} = T_{DC} \times 5\hat{i} + 12\hat{j} - 10\hat{k} \quad \text{--- (2)}$$

42.05

$$\vec{T}_{DA} = T_{DA} \times \left[(0-0)\hat{i} + (30-0)\hat{j} + (0-10)\hat{k} \right]$$

$\sqrt{(6-0)^2 + (30-0)^2 + (0-10)^2}$

$$\vec{T}_{DA} = T_{DA} \times \left[0\hat{i} - 30\hat{j} - 10\hat{k} \right]$$

50

$$T_{DA} = -60\hat{j} - 80\hat{k} \text{ KN} \quad \text{--- (3)}$$

Let force 'F' is acting at mass 'k'.

$$\vec{F} = (F12) \text{ N} \quad \text{--- (4)}$$

$$\text{Step II :- } \textcircled{1} \quad \sum f_k^j = 0$$

$$-24T_{DB} + 5T_{DC} = 0 \quad \text{--- (5)}$$

47.17 42.06

$$\textcircled{2} \quad \sum f_k^i = 0$$

$$-60 + 7T_{DB} + 12T_{DC} = 0 \quad \text{--- (6)}$$

47.17 42.06

$$\textcircled{3} \quad \sum f_k^K = 0$$

$$-80 - 40T_{DB} - 40T_{DC} + F = 0 \quad \text{--- (7)}$$

47.17 42.06

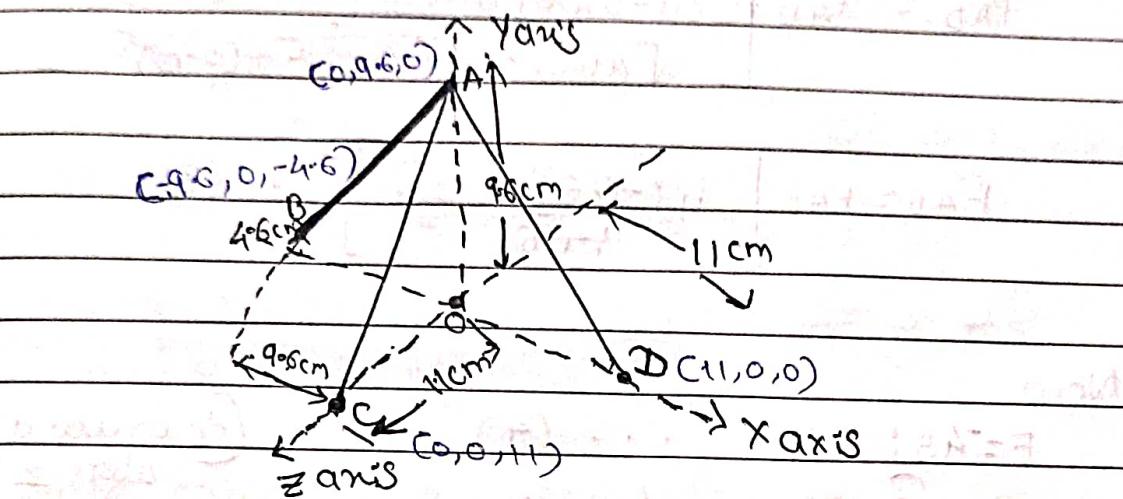
By calculator

$$TDB = 18.81$$

$$TDC = 187.512$$

Femar

- Q) Support Assembly shown in fig is bolted at point B, C and D. Supporting downward force of 45 N at A. Determine forces in member AB, AC and AD.



Soln

$$A(0, 9.6, 0)$$

$$B(-9.6, 0, -4.6)$$

$$C(0, 0, 11)$$

$$D(11, 0, 0)$$

Step I :-

$$\vec{F}_{AB} = F_{AB} \left[\frac{(9.6-0)\hat{i} + (0-9.6)\hat{j} + (-4.6-0)\hat{k}}{\sqrt{(9.6-0)^2 + (0-9.6)^2 + (-4.6-0)^2}} \right]$$

$$= F_{AB} \left(\frac{-9.6\hat{i} - 9.6\hat{j} - 4.6\hat{k}}{14.33} \right) \quad \text{Ans. (1)}$$

$$= \frac{-9.6}{14.33} F_{AB} - \frac{9.6}{14.33} F_{AB} - \frac{4.6}{14.33} \hat{k} F_{AB}$$

$$F_{AB} = F_{AC} \left[\frac{(0-0)^2 + (0-3.6)^2 + (11-0)^2}{\sqrt{0^2 + (0-3.6)^2 + (11-0)^2}} \right]$$

$$= F_{AC} \left[\frac{0^2 + 9.6^2 + 11^2}{14.6} \right] \quad \dots \textcircled{①}$$

$$F_{AD} = F_{AO} \left[\frac{(11-0)^2 + (0-0)^2 + (0-0)^2}{\sqrt{(11-0)^2 + (0-0)^2 + (0-0)^2}} \right]$$

$$F_{AD} = F_{AO} \left[\frac{11^2 + 0^2 + 0^2}{14.6} \right] \quad \dots \textcircled{③}$$

Now

$$F = -45 \hat{j} \quad \text{NOX} \dots \textcircled{④}$$

(downward along z)

Step (II) :-

$$1) \sum f_x = 0$$

$$\frac{-9.6}{14.33} F_{AB} + \frac{11}{14.6} F_{AD} = 0$$

- ⑤

$$2) \sum f_y = 0$$

$$\frac{-9.6}{14.33} F_{AB} - \frac{9.6}{14.6} F_{AC} - \frac{9.6}{14.6} F_{AD} - 45 = 0$$

- ⑥

$$3) \sum f_z = 0$$

$$\frac{-4.6}{14.33} F_{AB} + \frac{11}{14.6} F_{AC} = 0$$

- ⑦

F_{AB}

By Solving equation ⑤, ⑥ & ⑦

$$F_{AB} = -29.03 \text{ N}$$

$$F_{AD} = +25.81 \text{ N}$$

$$F_{AC} = +12.37 \text{ N}$$

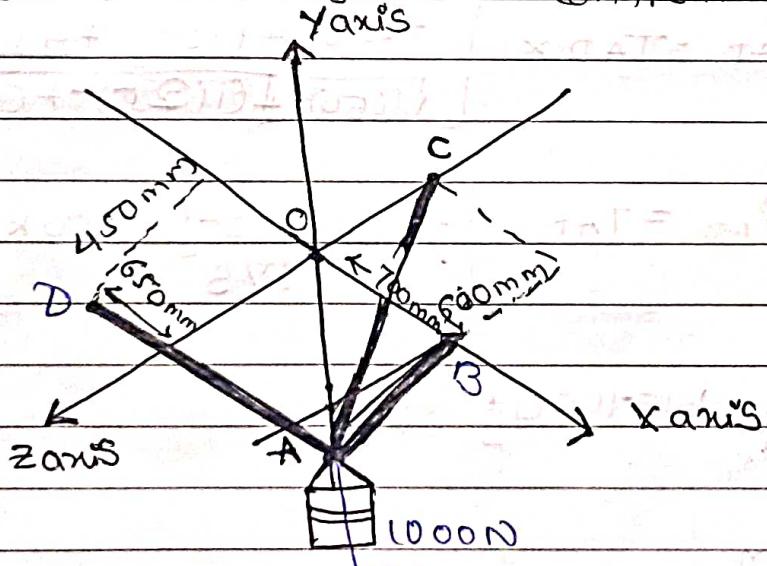
Since ans are coming in ⁺ve assumed direction can be reversed

$$F_{BA} = 29.3 \text{ N}$$

$$F_{DA} = 26.07 \text{ N}$$

$$F_{AC} = 12.49 \text{ N}$$

Three cables are used to support a container as shown in fig determine tension force in each cable if weight of container is 1000N



Q81)

Ans Given,

$$l(OA) = 1125 \text{ mm}$$

$$l(Oc) = 600 \text{ mm}$$

- $\vec{A} (0, -1125, 0)$
 $\vec{B} (700, 0, 0)$
 $\vec{C} (0, 0, -600)$
 $\vec{D} (-650, 0, 450)$
 $W = 1000 \text{ j}$

Step I :-

$$\vec{T}_{AB} = T_{AB} \times \left[\frac{(700-0)\hat{i} + (0+1125)\hat{j} + (0-0)\hat{k}}{\sqrt{(700-0)^2 + (0+1125)^2 + (0-0)^2}} \right]$$

$$T_{AB} \times \left[700\hat{i} + 1125\hat{j} + 0\hat{k} \right] / 1325$$

$$\vec{T}_{AC} = T_{AC} \times \left[\frac{(0-0)\hat{i} + (0+1125)\hat{j} + (-600-0)\hat{k}}{\sqrt{0^2 + (1125)^2 + (-600-0)^2}} \right]$$

$$\vec{T}_{AC} = T_{AC} \times \left[-650\hat{i} + 1125\hat{j} - 600\hat{k} \right] / 1275$$

$$\vec{T}_{AD} = T_{AD} \times \left[\frac{-650\hat{i} + 1125\hat{j} + 450\hat{k}}{\sqrt{(650)^2 + (1125)^2 + (450)^2}} \right]$$

$$\vec{T}_{AD} = T_{AD} \times \left[-650\hat{i} + 1125\hat{j} + 450\hat{k} \right] / 1375$$

$$W = 1000 \text{ j}$$

1)

$$\sum F_x = 0$$

$$700T_{AB} - 650T_{AD} = 0$$

$$\sum F_y = 0$$

2) $\sum M_A = 0$

$$1125 T_{AD} + 1125 T_{AC} + 1125 T_{AD} - 1000 = 0$$

$$1325 \quad 1275 \quad 1375$$

3) $\sum F_Z = 0$

$$-600 T_{AD} + 500 T_{AC} = 0$$

$$1275 \quad 1375$$

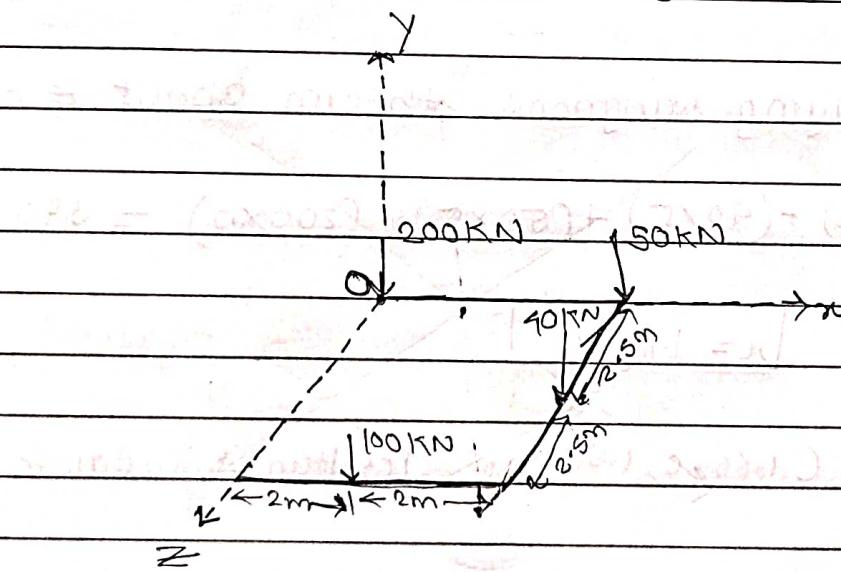
$$T_{AD} = 108.29$$

$$T_{AC} = 456.29$$

$$T_{AB} = 317.33$$

* Type-2 Parallel Force System:

- (Q1) Square mat foundation supports four column columns as shown in fig. Determine magnitude and position of resultant force w.r.t origin.



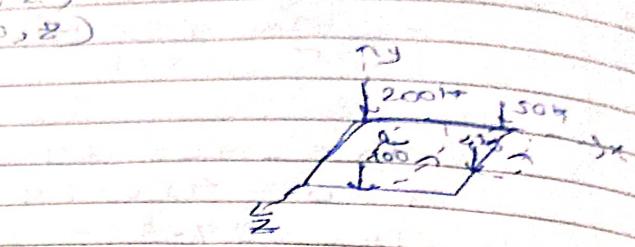
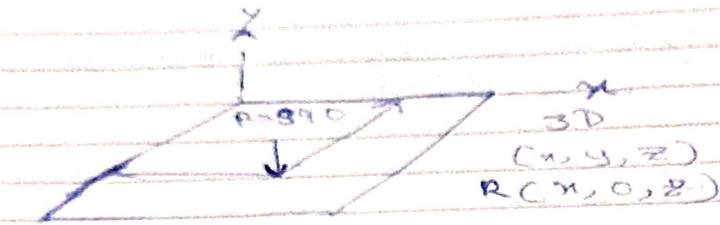
Ry =

$$R_y = \sum F_y = -200 - 50 - 10 - 100 = -390 \text{ kN}$$

$$\therefore (R_x = R_z = 0)$$

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(R) acts along z-axis



Now applying Varignon's theorem about z axis

$$ACLK - (40 \times 2.5) - (100 \times 5) + (200 \times 0) + (80 \times 0) = -390 \times z$$

$$-600 = -390 \times z$$

$$z = 1.53$$

Now applying Varignon's theorem about z axis

$$(100 \times 2) + (40 \times 5) + (50 \times 5) + (200 \times 0) = 390 \times x$$

$$bx = 1.667 m$$

$$R(1.66, 0, 1.53)$$

resultant co-ordinates

* Note :-

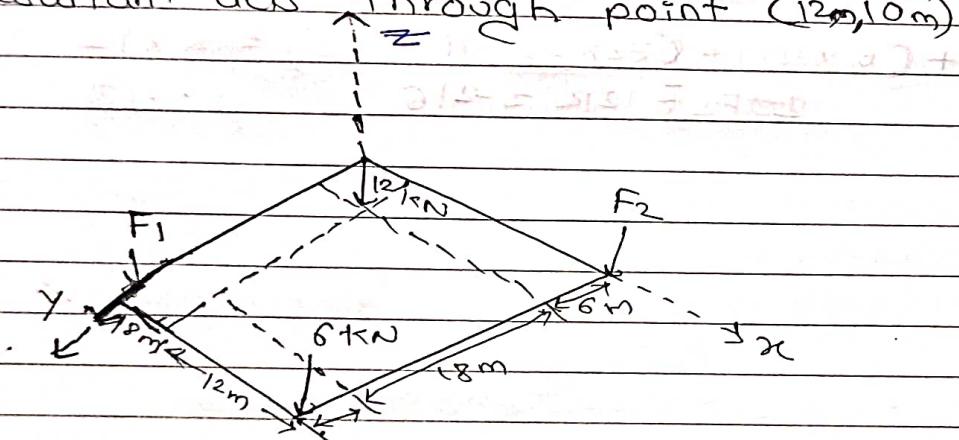
1. Axis in which all forces are given then resultant will act in that axis only.
2. Resultant need three coordinates to locate if it acts on y axis then y coordinate will be zero.

If it acts in z axis then z co-ordinate will be zero. & for x-axis x co-ordinate will be zero.

3. Moment about z axis gives x co-ordinate.
Moment about x axis gives z co-ordinate in x-z plane.

Similarly in x-y plane with moment about y-axis will give x-coordinates & vice versa.

- Q) Building slab is subjected to four parallel column as shown in fig determine force F_1 & F_2 if resultant acts through point (12m, 10m)



Soln Given,

$$R(12m, 10m)$$

$$R = ?$$

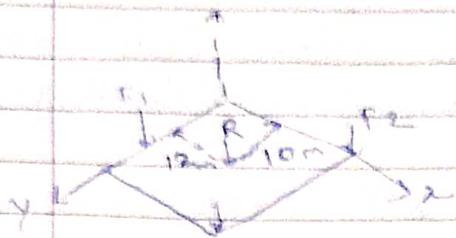
$$F_1, F_2 = ?$$

$$R_z = \sum F_z = -F_1 - F_2 - 6 - 12 \quad \text{--- (1)}$$

$$R + F_1 + F_2 = 28$$

$$\therefore (R_x = R_y = 0)$$

Plane is $x = y$



Applying V.T about x -axis.

$$-(12 \times 6) - (F_1 \times 24) - (6 \times 28) = -R \times 10$$

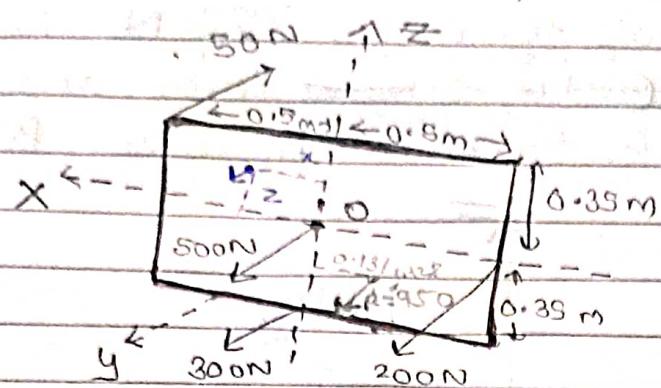
$$\Rightarrow -24F_1 + 10R = 240 \quad \dots \textcircled{2}$$

Applying V.T about y -axis.

$$+(6 \times 20) + (F_2 \times 20) + (12 \times 8) = R \times 12$$

$$20F_2 + 12R = 216 \quad \dots \textcircled{3}$$

Q) Determine resultant of parallel force system which acts on the plate as shown in figure.



Ques

$$\text{Ans} \quad R_y = \sum f_y = 500 + 300 + 200 - 50 = \\ R = 950 \text{ N}$$

Now

$$R(x, 0, z)$$

Varignon's Theorem about x-axis :-

$$+ (50 \times 0.35) + (300 \times 0.35) = - Rx \\ 122.5 / 950 = -x$$

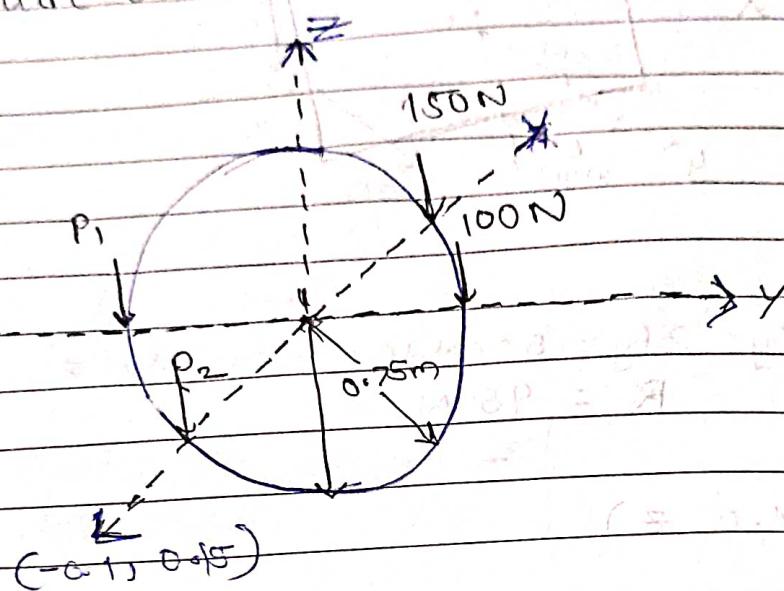
$$x = -0.128 \text{ m}$$

Varignon's Theorem about z axis.

$$+ (50 \times 0.5) + (200 \times 0.35) = - Rx \\ 125 / 950 = -x$$

$$x = -0.131 \text{ m}$$

Q) Four parallel rolling forces act on the rim of circular corner plate as shown in figure. If resultant force is 750 N is passing through $(0.15, 0.15 \text{ m})$ from origin O determine magnitude of force of P_1 , P_2 , $P_1 + P_2$.



Given

$$R = 750 \text{ N}$$

$$R(0.15, 0.15, 0)$$

$$R_z = \sum f_z = -150 - 100 - P_1 - P_2 \quad \Sigma$$

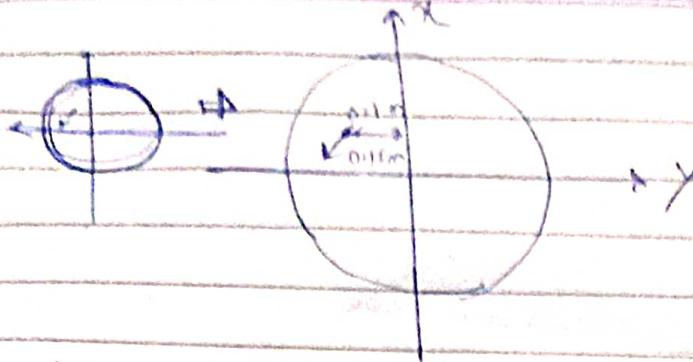
$$P_1 + P_2 - 250 = -750$$

$$P_1 + P_2 = 500 \quad \text{.....} \quad \text{Eqn ①}$$

Vernier's theorem about $Z-Z$ plane -

~~$$-(P_1 \times 0.75) + (100 \times 0.75) + (150 \times 0) - (P_2 \times 0)$$~~

$$P_1 = -250$$



Varignon's Theorem about x-y-axis.

$$-(R \times 0.75) + (100 \times 0.75) = -R \times 0.1$$

$$\begin{aligned} P_1 &= 200 \text{ N} \\ \therefore P_2 &= 300 \text{ N} \end{aligned}$$