QUESTIM : Decision rule -2

· How to select kt that minimize the prob

P(Z) = P(HINA)+ P(HONA)

where E: ever event.

ito: decide its

Hi decide Hi

let Xo: # number of heads of Ho.

X1: number of heads of HI.

P(H1 1/h)= P(h) H1)P(H1)

= P (X1 > K) . P (H1)

P(Honfi)= P(fi/Ho)P(Ho) = P(Xo=K)P(Ho)

> (see implementation) USIZ cdf of Binimial RV.

Ouestim 2:
$$E(x) = \frac{3}{2}z_1$$
; $P(x_1) = (-2)x \frac{1}{3} + (-1)x \frac{1}{3}$

$$= -\frac{1}{3}.$$

$$E(x^2) = \frac{3}{2}xi^2P(x_1) = (-2)^2 \cdot \frac{1}{3} + (-1)^2x \frac{1}{3}$$

$$= 2$$

$$V_{4Y}(x) = E(x^2) - (E(x))^2 = 2 - \frac{17}{9}.$$

$$E(2x+5) = 2E(x) + 5 = 2x(-\frac{1}{3}) + 5 = -\frac{13}{5}$$

$$E(3x^2+6) = 3E(x^2) + 6 = 3x + 2 + 6 = (2)$$

Question 2. (RV.)

X: the number of cars being repaired.

Yange of
$$\times$$
. [0, 57

$$P(X=2) = P(X=1) = P(X=1) = P(X=1) = P(X=2) = P(X=0) = P(X=1) = P(X$$

 $=\frac{1}{2}(P(X=2)+P(X=0)-P(X=3)X=0)$

$$2P_{1} = \frac{1}{2} \cdot 2P_{0} = 2P_{1} = P_{0}$$

$$P_1 = \frac{1}{6}$$
. $P_0 = \frac{1}{3}$.

$$P(X=1) = P(X=2) = 6$$

$$P(X=3) = P(X=0) = \frac{1}{3}.$$

Question 3

Y						
6	-5	-4	-3	-2	-1	ာ
5	<u>-</u> 4	-3	-2	4	J	[
4	_3	-2_	4	O	l	2
}	-2	1-1	Ð	(2	3
2	\1	0	\	2	3	4
	0	1	2	. 3	4	5
	X	(2 ع	, _/	`\	6
	/\					

$$P(\overline{z} = -1) = \frac{5}{36} = P(\overline{z} = 1)$$

$$P(\overline{z} = -2) = \frac{4}{36} = P(\overline{z} = 2)$$

$$P(\overline{z} = -3) = \frac{3}{36} = P(\overline{z} = 3)$$

$$P(\overline{z} = -4) = \frac{2}{36} = P(\overline{z} = 4)$$

$$P(\overline{z} = -4) = \frac{1}{36} = P(\overline{z} = -4)$$

$$P(\overline{z} = -4) = \frac{1}{36} = P(\overline{z} = -4)$$

$$P(\overline{z} = -4) = \frac{1}{36} = P(\overline{z} = -4)$$

implementation smitted.

$$P(X4) = \int_{-5}^{1} -\frac{1}{10} dx$$

$$= \frac{1}{10}$$

$$= \frac{1}{1$$

$$= \sum_{i=1}^{n} Var(X_i) + \sum_{i=1}^{m} Var(Y_i) \cdot (-1)^2$$

= $n.6^{2} + m6^{2}$

(2): E(X-Y)= M1-M2; Var(X-Y)= Var(X) + Var(Y) = /2 · n6/2+ /m2 m6? $P(X=k) = \frac{\lambda^{k}e^{-\lambda}}{k!}$ Question. CLT:

λ: expetted number of events in a given inferval.

 $\lambda = 10$ for day) $E(X) = \lambda = 14$

 $Y = X_1 + \cdots + X_{365}$; s the

total number of actidene.

Y~ N(365×E(x); 365× Var(x)) N (3650: 3650)

(1) P(X) 3850)= Q(3850-3650)

= 2.2004

Question 2.

Xi ~ bemoulli(0.1)
$$E(X_i)=0.09$$

 $Y = X_1 + \cdots + X_{1000}$ is the total
number of errors. $Var(Y) = n \ var(X_i) = 0.09 \times 1000$
 $= 90$
P(decoding failure) = P(Y>[25)

$$= Q\left(\frac{|2s-|00|}{\sqrt{q_0}}\right) = 0.0042.$$
in Pythod simulation. obtain similar results.

Overtion 3:

Coin Xin Bernoulli(a.5)

$$Y = \frac{\chi_1 + \dots + \chi_n}{\chi_n} : \mathbb{E}(Y) = 0.5.$$

$$\forall \alpha r(Y) = \frac{v \cdot r(X)}{n}$$

$$= |-2\sqrt{2}\left(\frac{0.55-0.5}{\sqrt{0.25/n}}\right) > 0.95$$

$$(1, Q(\frac{0.05\sqrt{n}}{0.5}) < 0.025$$

using inverse of 2.

$$=) n > Q^{-1}(0.025) \times 0.5$$

$$M = E(X_i) = 0.9$$

 $Var(X_i) = 0.9 \times 0.1 = 0.09$

$$S_{100} = \sum_{i=1}^{600} X_i \sim N(0.9 \times 100, 0.9 \times 100)$$

= $N(90, 9)$

$$P(S_{100} \leq 80) = P(\frac{S_{100} - 90}{3} \leq \frac{80 - 90}{3})$$

$$= P(z = -\frac{0}{3})$$

: Standard normal RV.

$$P(S_{100} \in 80) < Q = 0.01$$

So. rejet the company's statement.

programming. 1,
Program miy. 1. $Pr(P Z) = P(Z P) P(P)$ $P(Z)$
P(2)