

Lecture notes for 2.1-2.4

LOTS of definitions today

Def: Cryptography

- The art [science] of secret writing
- Codemaking

Def: Cryptanalysis

- The art [science] of breaking codes
- Codebreaking

Def: Cryptology

- Cryptography UNION cryptanalysis

Def: Encryption [enciphering]

- Conversion of plaintext [cleartext] to ciphertext
- $C = E(P)$

Def: Decryption [deciphering]

- Conversion of ciphertext to plaintext
- $P = D(C)$

Def: (Reversible) Cryptographic scheme [cipher]

- Encryption algorithm UNION decryption algorithm
- Constraint: $D(E(P)) = P$

Cryptographic schemes have 0, 1, or 2 keys

Def: Cryptographic hash function

- $H = E(P)$
- Preimage resistant
 - Given H , “hard” to find P
- Second preimage resistant
 - Hard to find P and P' satisfying $E(P) = E(P')$
- Properties:
 - Non-reversible (preimage resistant)
 - 0 keys: anyone can compute a hash of a plaintext
 - 1 key: only people possessing key can compute a hash
 - Principle: non-linear bit transformations (substitutions, transpositions)
- Common algorithms:
 - MD5, SHA1, SHA256

Def: Symmetric [secret] key cryptography

- $P = D(E(P, K), K)$
- Properties:
 - Reversible
 - Same encryption & decryption key
 - Key must be a shared secret, called “secret key”
 - Principle: non-linear bit transformations (substitutions, transpositions)
- Common algorithms:
 - DES, 3DES, AES

Def: Assymmetric [public] key cryptography

- $P = D(E(P, e), d)$
- Properties:
 - Reversible
 - Different encryption & decryption keys
 - One of the keys can be published, called “public key”
 - One key not disclosed, called “private key”
 - Principle: math, NP-hard problems
- Common algorithms:
 - RSA

Foundation of confidentiality & integrity

- Confidentiality: Encrypt private data
- Integrity: Use a cryptographic hash to detect alterations of data
 - “Summary” of the input data, attacker cannot recompute summary if changing data
 - This is the principle used to verify passwords at system login

Comparisons

- Symmetric key crypto
 - Fast
 - Must manage many keys
 - Must protect many keys
- Assymmetric key crypto
 - Slow
 - Must manage no keys
 - Must protect only own private key

Principles:

- Attackers know algorithms (Why?)
- Entire security comes from secrecy of the key

Key distribution problem

- Symmetric key crypto
 - How do both parties share the key ahead of time? Need confidential channel, but doesn't exist until keys already established. Chicken-and-egg.
 - Generally done via out-of-band channel (phone call, keyboard)
 - Diffie-Hellman key exchange
- Assymmetric key crypto
 - How do I trust your public key? Attacker may be spoofing identity
 - Certificates (you've gotten cert warnings in your web browser)
 - Assertion by someone you trust that an unknown identity is legit
 - Root trust set via out-of-band channel (OS update mechanism)

Cryptanalysis techniques

- Brute force (try all possible keys)
- Discover mathematical properties of ciphertext
- For cryptograms: use properties of natural language (covered in textbook)
- Guess at what plaintext might have been (headers...)

Def: Ciphertext-only attack

- Cryptanalyst recovers plaintext (& possibly key) from ciphertext

Def: Known plaintext attack

- Cryptanalyst recovers key from plaintext / ciphertext pair

Def: Chosen plaintext attack

- As before, but attacker gets to choose plaintext
- Some plaintexts may trigger weaknesses in the system & reveal info
- Occurs when the cipher is operating as an encryption oracle

Def: Perfect secrecy

- The property that every plaintext (of the appropriate length) is mathematically equally likely for a given ciphertext
- Requirement: bits of key \geq bits of plaintext
- Example: one-time pad

Modes of operation apply to many enciphering & deciphering algorithms

Def: Stream mode

- A cryptosystem that encrypts and decrypts data symbol-by-symbol
- Useful for handling low latency data (cannot wait for entire block)

Def: Block mode

- A cryptosystem that encrypts and decrypts data block-by-block
- Useful for bulk encryption/decryption

Rebuttal to text: Shannon principle 4

- "Errors should not propagate"
- Lack of propagation may be weakness in system
- Want data to continually mix, affect data further away
- Stream & block ciphers mix current data with previous data

Basic math

- Modular arithmetic
- Exponentiation

Diffie-Hellman key exchange

- Protocol to allow two parties to establish secret key over insecure medium
- Invented (in secret) by GCHQ in early 1970s
- 1. Alice choose a, g, p (p prime, $g < p$)
- 2. Alice compute $A = g^a \bmod p$
- 3. Alice sends g, p, A to Bob
- 4. Bob choose b
- 5. Bob compute $B = g^b \bmod p$
- 6. Bob send B to Alice
- 7. Alice compute $K = B^a \bmod p$
- 8. Bob compute $K = A^b \bmod p$
- K is the shared secret key
- Works because $g^{ab} \bmod p = g^{ba} \bmod p$ && K , a , b are never sent in the clear && g is a generator of \mathbb{Z}_p since $\gcd(g, p) = 1$

Trivial cryptosystems

- Alphabetic shift
 - Caesar cipher
- Vigenere