

ASTR 792 HW 11

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14.2a

The transition probability in general can be written as

$$P(3p \rightarrow 1s) = A_{3p \rightarrow 1s} \delta t$$

The two possible transitions from the $3p$ state are

$$\begin{aligned} 3p \rightarrow 2s & \quad A_{3p \rightarrow 2s} = 2.245 \cdot 10^7 \text{ s}^{-1} \\ 3p \rightarrow 1s & \quad A_{3p \rightarrow 1s} = 1.672 \cdot 10^8 \text{ s}^{-1} \end{aligned}$$

with wavelengths

$$\begin{aligned} H\alpha : 3p \rightarrow 2s & \quad \lambda_{3p \rightarrow 2s} = 656.46 \text{ nm} \\ Ly\beta : 3p \rightarrow 1s & \quad \lambda_{3p \rightarrow 1s} = 102.57 \text{ nm} \end{aligned}$$

The transition probability can be calculated by taking the branching ratios

$$\begin{aligned} \frac{A_{3p \rightarrow 2s}}{A_{3p \rightarrow 1s}} &= \frac{2.245 \cdot 10^7 \text{ s}^{-1}}{1.672 \cdot 10^8 \text{ s}^{-1}} \\ &= .135 \end{aligned}$$

Thus, the probability for emitting $Ly\beta = 1 - .134 = .866$