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Hash Tables

Performance Analysis

COMP2521 19T0

Week 8, Tuesday: Hash Tables

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hashing performance

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Hash Tables

Hashing
Collision Resolution
Performance

Performanc Analysis

Hash Tables

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Hash Tables

Searching Hashing

Collision Resolution Performance

Performance Analysis Searching
The State Of Play

So far we've seen... linked list: insert O(1), search O(n)

ordered linked list: insert O(n), search O(n)

array: insert O(1), search O(n)

ordered array: insert O(n), search $O(\log n)$

search tree: insert $O(\log n)$, search $O(\log n)$

... but these are still all pretty slow, and perform less-than-ideally on modern architectures (due to cache locality effects) Hash Tables Searching In an ideal world, we can index on arbitrary keys, and get constant-time O(1) access. Key-indexed arrays get some of the way there, but have downsides: ... requires dense range of index values ... uses fixed-size array; sizing it is hard ... can't use arbitrary keys! COMP2521 Hashing 19T0 lec14 cs2521@ jashankj@ Hashing lets us approximate this: arbitrary keys! (so long as we can hash them) Hashing map keys into a compact range of index values! store items in array, accessed by index value! O(1)!We need three things: an array of Items, of size Na hash function, $ext{HASH}:: \mathsf{Key} o \mathsf{size} o [0 \cdots N)$, a collision resolution method, for when $k_1 \neq k_2 \land \text{HASH}(k_1, N) = h(k_2, N)$; collisions are inevitable when $DOM(k) \gg N$ COMP2521 **Hash Functions** 19T0 lec14 cs2521@ jashankj@ Hashing Properties we want h to have: • for a table of size N, output range is 0 to N-1; • pure, deterministic: h(k, N) gives the same result;

> spreads key values uniformly over index range (assuming keys are unformly distributed)

cheap (enough) to compute ... otherwise, what's the point?

Searching

Even Faster?

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COMP2521 **Hash Functions** 19T0 lec14 Aside: Cryptographic Hash Functions cs2521@ jashankj@ Hashing Ideally all of the above, and pre-image resistant: for h = HASH(m), given h, hard to pick m; second pre-image resistant: for $HASH(m_1) = HASH(m_2)$, given m_1 , hard to find $m_2 \neq m_1$; collision resistant: for $HASH(m_1) = HASH(m_2)$, hard to find m_1 and m_2 . For our purposes, we don't need cryptographic hash functions. (COMP6[48]41, MATH3411 go into detail.) COMP2521 **Hash Functions** 19T0 lec14 Example (I) cs2521@ jashankj@ Hashing A simple hash function for single characters, if N=128: size_t hash (char key, size_t N) { return key; // N redundant } Not really useful: key range is usually much larger than N. COMP2521 **Hash Functions** 19T0 lec14 Example (II) cs2521@ jashankj@ Hashing Another simple hash function, for integers: size_t hash (int key, size_t N) {

How big is N? small $N \Rightarrow$ too many collisions!

return key % N;

}

```
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Hash Functions

Example (III)
```

```
Hash Tables
Searching
Hashing
```

Performance

```
A simple hash function, for strings:
```

```
size_t hash (char *key, size_t N)
{
    return strlen (key) % N;
}
```

(You should never actually do this.)

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Hash Functions

Example (IV)

A better string hash function:

```
size_t hash (char *key, size_t N)
{
    size_t h = 0;
    for (size_t i = 0; key[i] != '\0'; i++)
        h += key[i];
    return h % N;
}
```

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Hash Functions

Example (V)

A more sophisticated hash function:

```
size_t hash (char *key, size_t N)
{
    size_t h = 0;
    unsigned a = 127; // prime
    for (size_t i = 0; key[i] != '\0'; i++)
        h = ((a * h) + key[i]) % N;
    return h;
}
```

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Hash Functions

Example (VI)

Using universal hashing, which introduces randomness while using the entire key:

```
size_t hash (char *key, size_t N)
{
    size_t h = 0;
    unsigned a = 31415, b = 21783;
    for (size_t i = 0; key[i] != '\0'; i++) {
        a = (a * b) % (N - 1);
        h = ((a * h) + key[i]) % N;
    }
    return h;
}
```

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Hash Tables
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Collision Resolution

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Performance

Collisions

What happens if two keys hash the same? We go to the same array index ... then what?

... allow multiple Items in a single location, via e.g., array of item arrays array of linked lists

... systematically compute new indices by various *probing* strategies

... resize the array by adjusting the hash function, and moving everything (!)

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Hashing Collision Resolution

Performance

Collisions

Separate Chaining

Given N slots and M items: best case, all lists have length M/N worst case, one list with length M, all others 0

with a good hash and $M \leq N$, cost O(1); with a good hash and M > N, cost O(M/N)

(The M/N ratio is called *load*.)

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Hash Table

Collision Resolution

Performance

Performance Analysis Collisions
Linear Probing

If the table is not close to being full, there are still many empty slots; we could just use the next available slot along; open-address hashing.

to reach the first item is O(1); search for subsequent items depends on load; successful search cost: $\frac{1}{2}\left(1+1/\left(1-\alpha\right)\right)$ unsuccessful search cost: $\frac{1}{2}\left(1+1/\left(1-\alpha\right)^2\right)$ (assuming reasonably uniform data, good hash function)

... but tends towards O(N) when α is high.

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Searching Hashing Collision Resolution

Performance

Collisions

Double-Hash Probing

We switch from HASH to HASH2 (which should not return 0!), and use it as the step to the 'next' item. HASH and HASH2 should be relatively prime to each other, and to N. (Easy, if we pick a prime N.)

Significantly faster than linear probing for high α

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Searching
Hashing
Collision Resolution
Performance

Performance Analysis Hash Table Performance

Choosing a good N for M is critical. Choosing a good N for M is critical. Choosing a good resolution approach is critical.

linear probing: fastest, given big N! double hashing: fastest for higher α , more efficient chaining: possible for $\alpha \geq 1$, but degenerates

Performance

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Hach Tables

Performance Analysis

Why do we care, anyway?

good performance \Rightarrow less hardware, happy users. bad performance \Rightarrow more hardware, unhappy users.

generally, performance is proportional to execution time; we may be interested in other things (memory, i/o, ...)

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Performance Analysis

Premature optimisation

is the root of all evil.

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Performance Analysis

Developing Efficient Programs

- Design the program well¹
- Implement the program well²
- Test the program well
- Only after you're sure it's working, measure performance
- If (and only if) performance is inadequate, find the 'hot spots'
- 6 Tune the code to fix these
- Repeat measure-analyse-tune cycle until performance ok

¹See, e.g., Algorithms by Sedgewick, Algorithms by Cormen/Leierson/Rivest/Stein.

²See, e.g., Programming Pearls, the Practice of Programming.

COMP2521 Performance Estimates 19T0 lec14 cs2521@ jashankj@ Complexity analysis give info on most appropriate algorithm. Performance We can also consider an experimental approach to performance: Analysis determine the critical operations in the program determine classes of input data and likelihood of each estimate the cost (#crit.ops) for each class of data produce a weighted sum estimate for overall cost Often, however... assumptions made in estimating performance are invalid we overlook some frequent and/or expensive operation COMP2521 Performance Measurements 19T0 lec14 cs2521@ jashankj@ Basis of performance evaluation: Performance Analysis measure program execution. empirical study suggests the '80/20' rule: most programs spend most of their execution time in a small part of their code. most code has little impact on overall performance small parts account for most execution time To improve performance: focus on bottlenecks first. COMP2521 Performance Measurement 19T0 lec14 **Profiling Execution** cs2521@ jashankj@ We need a way to measure how much Performance each block of code costs: Analysis a profiler. gprof(1) displays execution profiles for programs compiled with -pg; profiling info is left behind in gmon.out, which *qprof(1)* can read. gprof(1) gives a table (a flat profile) containing:

number of times each function was called, % of total execution time spent in the function, average execution time per call to that function, execution time for this function and its children

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Performance Analysis	Once you have a profile, you can identify hot points. To improve the performance:
	 change the algorithm and/or data-structures may give orders-of-magnitude better performance but it is extremely costly to rebuild the system
	 use simple efficiency tricks to reduce costs
	 may improve performance by one order-of-magnitude use the compiler's optimization switches (e.g., -0, -02, -03)
	 may improve performance by one order-of-magnitude
COMP2521 19T0 lec14	Conclusions
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Performance Analysis	Time and profile your code
	Time and profile your code only when you are done.
	, ,
	only when you are done. Don't optimise code unless you have to.

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