COMP2521 19T0 lec07

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Granh Ren

# COMP2521 19T0 Week 4, Thursday: Graphic Content (III)!

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computability directed graphs



Computabili

# **Graph Representation**

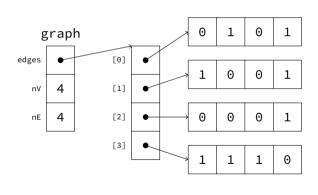
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```
struct graph {
    size_t nV, nE;
    bool **matrix;
};
```

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## Recap: Ways of Representing Graphs

**Adjacency Matrices** 

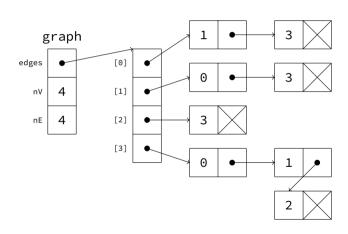


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```
typedef
    struct adjnode
    adjnode;
struct graph {
    size_t nV, nE;
    adjnode **edges;
};
struct adjnode {
    vertex w;
    adjnode *next;
};
```

### Recap: Ways of Representing Graphs

Adjacency Lists



```
struct graph {
    size_t nV, nE;
    edge *edges;
};
```

```
\begin{array}{c|cccc}
v & w \\
\hline
0 & 1 \\
0 & 3 \\
\hline
1 & 3 \\
2 & 3
\end{array}
```

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Graph Rep.

```
typedef struct vertex {
    Item it;
    size_t degree;
    vertex *neighbours;
} vertex;

struct graph {
    size_t nV, nE;
    vertex *root;
};
```

## Recap: Ways of Representing Graphs

Comparison

	matrix	adj.list	edge list	node links
space	$V^2$	V + E	E	V + E
initialise	$V^2$	V	1	V
destroy	V	E	E	V + E
insert edge	1	V	1	E
find/remove edge	1	V	E	E
is isolated?	V	1	E	1
degree	V	E	E	E
is adjacent?	1	V	E	E

#### **Hamilton Path:**

a simple path connecting two vertices that visits each vertex in the graph exactly once

#### Hamilton Tour:

a cycle that visits each vertex in the graph exactly once

\* \* \*

Given a list of vertices or edges, easy to check. Given a graph ... how do we know if one exists? Do we have to find one? If so, how do we find one? Computability

### Hamilton Paths and Tours

Brute Force Is Best Force

IDEA brute force! enumerate every possible path, and check each one.

hack a BFS or DFS to do it: keep a counter of vertices visited in the current path; only accept a path only if count is equal to the number of vertices.

problem how many paths? given a simple path: no path from t to w implies no path from v to w via t... so there's no point visiting a vertex twice on a simple search ... but that's not true for a Hamilton path!

Computability

we must inspect every possible path in the graph. in a complete graph, we have V! different paths ( $\approx (V/e)^V$ )

there are well-known, well-defined subsets of this problem which are easy to solve (Dirac, Ore) ... but in general this is a non-deterministic polynomial, or NP problem

#### **Euler Path:**

a simple path connecting two vertices that visits each edge in the graph exactly once ... exists iff the graph is connected and has exactly two vertices of odd degree

#### **Euler Tour:**

a cycle that visits each edge in the graph exactly once ... exists iff the graph is connected and all vertices are of even degree

... these can be found in linear time.

Computability

### **Graph Problems**

Tractable and Intractable

- tractable: can we find a simple path connecting two vertices in a graph?
   tractable: what's the shortest such path?
   intractable: what's the longest such path?
- tractable: is there a clique in a given graph? intractable: what's the largest clique?
- tractable: given two colours, can we colour every vertex in a graph such that no two adjacent vertices are the same colour? intractable: what about three colours?

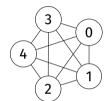
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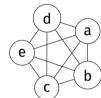
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Graph Rep

## **Graph Problems**

**Bonus Round!** 





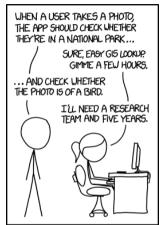
### Graph isomorphism:

Can we make two given graphs identical by renaming vertices?

No general solution exists. We don't know if one can exist. COMP2521 19T0 lec07

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Graph Rep. Computability



IN CS, IT CAN BE HARD TO EXPLAIN THE DIFFERENCE BETWEEN THE EASY AND THE VIRTUALLY IMPOSSIBLE.

xkcd 1425 "Tasks" // cc BY-NC 2.5