k-Nearest Neighbors algorithm: comparison between sequential, OpenMP and CUDA implementations

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Outline

- 1 Introduction
- 2 Implementation

Sequential Parallel OpenMp CUDA

- 3 Results
- 4 Conclusion

k-Nearest Neighbors problem

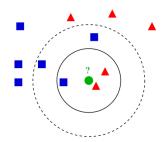
Given a dataset \mathcal{D} of N points $x_i \in \mathbb{R}^n$, a test point $q \in \mathbb{R}^n$ and a distance measure d, the k-Nearest Neighbors problem (k-NN) is to find the k points closest to q in \mathcal{D} , i.e. find an ordered subset \mathcal{S} of \mathcal{D} such that:

• $S = \{x_{i_1}, x_{i_2}, ..., x_{i_k}\}$

Introduction

- $j < h \implies d(q, x_{i_i}) \leq d(q, x_{i_h})$
- $d(q, x_{i_i}) \leq d(q, x_m), \forall x_{i_i} \in \mathcal{S}, \forall x_m \in \mathcal{D} \setminus \mathcal{S}$

Example of k-NN problem



• : query

▲ ■ : dataset points

In this example, the neighbors have information (shape/color) that can be used for other tasks, such as classification/regression

Objective

Introduction 0000

Compare a sequential and two parallel versions of k-NN measuring:

- compute time
- speedup

while varying:

- number of threads
- dataset size

Dataset

We use the k-NN algorithm on a SIFT dataset

Introduction 000

Why k-NN it's important on SIFT data

- SIFT is a feature detection algorithm used in computer vision to detect and describe local features in images
- SIFT descriptors are 128-dimensional floating point vectors, used for image classification and object detection
- k-NN is used to find training SIFTs "near/similar" to the SIFTs in the test image

Sequential Implementation

Algorithm 1: k-Nearest Neighbors - Sequential version

```
Input: dataset, query, k
  Output: nearestNeighbors
1 // init
indexes = new int[dataset.size]
3 distances = new float[dataset.size]
4 // calculate distances
5 for p from 0 to dataset.size-1 do
      indexes[p] = p
      distances[p] = euclideanDistance(query, dataset[p])
8 end
9 // sort by increasing distance
10 sortByKey(indexes, keys=distances)
11 // slice
_{12} nearestNeighbors = indexes[:k]
```

Open MP Implementation (1)

Algorithm 2: k-Nearest Neighbors - OpenMP version

```
Input : dataset, query, k, numThreads
Output: nearestNeighbors
1  // init
2  indexes = new int[dataset.size]
3  distances = new float[dataset.size]
4  // calculate distances
6  for p from 0 to dataset.size-1 do
7   indexes[p] = p
8   distances[p] = euclideanDistance(query, dataset[p])
9  end
```

Algorithm 3: k-Nearest Neighbors - OpenMP version

```
Input : dataset, query, k, numThreads
Output: nearestNeighbors
1  // init
2  indexes = new int[dataset.size]
3  distances = new float[dataset.size]
4  // calculate distances
5  # pragma omp parallel for
6  for p from 0 to dataset.size-1 do
7  indexes[p] = p
8  distances[p] = euclideanDistance(query, dataset[p])
9  end
```

```
chunkSize = dataset.size / numThreads

11 // sort chunks by increasing distance

12 # pragma omp parallel for

13 for j from 0 to numThreads-1 do

14 | s = j * chunkSize

15 | e = s + chunkSize

16 | sortByKey(indexes[s:e], keys=distances[s:e])

17 end
```

Open MP Implementation (2)

```
10 chunkSize = dataset.size / numThreads
11 // sort chunks by increasing distance
12 # pragma omp parallel for
13 for j from 0 to numThreads-1 do
  s = i * chunkSize
14
    e = s + chunkSize
     sortByKey(indexes[s:e], keys=distances[s:e])
17 end
18 // merge sorted chunks
19 for j from 1 to numThreads-1 do
      i, d = indexes[:k], distances[:k]
20
    s = i * chunkSize
21
    e = s + k
22
      indexes[:k], distances[:k] = merge(i,d,indexes[s:e],distances[s:e])
23
24 end
25 // slice
  nearestNeighbors = indexes[:k]
```

OpenMP creates the threads and distributes the iterations between them depending on the **scheduling**, which can be:

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****	****
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```
***
                ****
    ***
```

• dynamic: equal-sized chunks, available thread

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static: equal-sized chunks, circular order

```
***
    ****
                 ****
```

• dynamic: equal-sized chunks, available thread

guided: decreasing-size chunks, available thread

```
*****
                      **
```

• static: equal-sized chunks, circular order

*** ***

CUDA Implementation

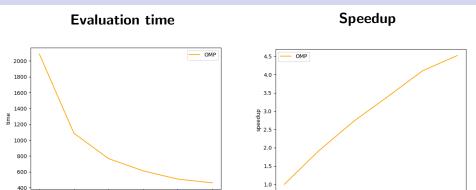
Algorithm 4: k-Nearest Neighbors - CUDA version

```
Input: dataset, query as q, k, bSize
  Output: nearestNeighbors
1 // init
indexes = new int[dataset.size]
3 distances = new float[dataset.size]
4 // move query to GPU memory
g = toGPU(q)
6 // determine number of blocks
7 blocks = (datasetSize + bSize - 1) / bSize
8 // calculate the distances
9 idxs, dists = cudaDistances<<<blooks,bSize>>>(dataset,q)
10 // sort by increasing distance on GPU
11 sortByKeyOnGPU(idxs, keys=dists)
12 // slice and move results to CPU memory
nearestNeighbors = toCPU(idxs[:k])
```

- CPU: Intel Core i7-8750H, 6 cores / 12 threads
- GPU: NVIDIA GeForce GTX 1050 Ti (Notebook), 768 CUDA cores, 4 GiB video RAM, 6 SM
- RAM: 16 GiB
- CUDA: 10.0
- OpenMP: 4.5

OpenMP

5



Plots in function of the number of threads

3

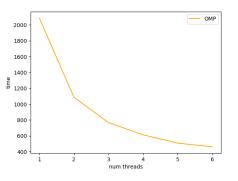
num threads

5

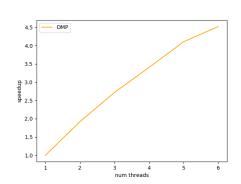
num threads

OpenMP





Speedup

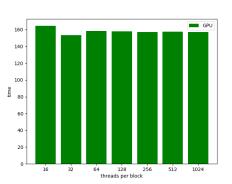


Plots in function of the number of threads

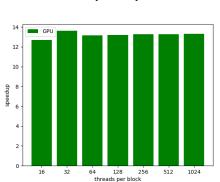
The obtained SpeedUp is sub-linear

CUDA





Speedup



Plots in function of the number of threads per block

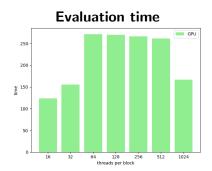
The block size in k-NN is not much relevant for the evaluation time.

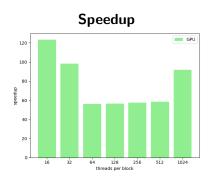
- GPU used in our tests has 6 Streaming Multiprocessors only
- Even with a big block size, it's easy to occupy every SM
- Distances calculation time > data transfer + sync time *

^{*:} verified using Valgrind tools: https://valgrind.org

Other experiment on CUDA

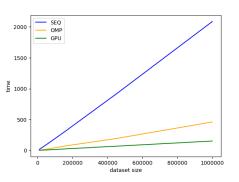
To check if with a more powerful GPU the block size becomes important, we run the experiments on a NVidia GTX 980~GPU (which has 16~SM)



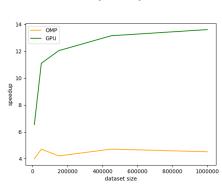


Comparison





Speedup



Plots in function of the dataset size

OpenMP

- Implementation difficulty: low
- Speedup: sub-linear
- Makes parallel computing very accessible

OpenMP

- Implementation difficulty: low
- Speedup: sub-linear
- Makes parallel computing very accessible

CUDA

- Implementation difficulty: high
- *Speedup*: huge (\sim 10-100)
- Highest level of single-machine parallelism

End

Thanks for attention