



B E H A V E

# Agent-based modelling towards the future of social network research

**Workshop on “Agent-based models of social networks”**

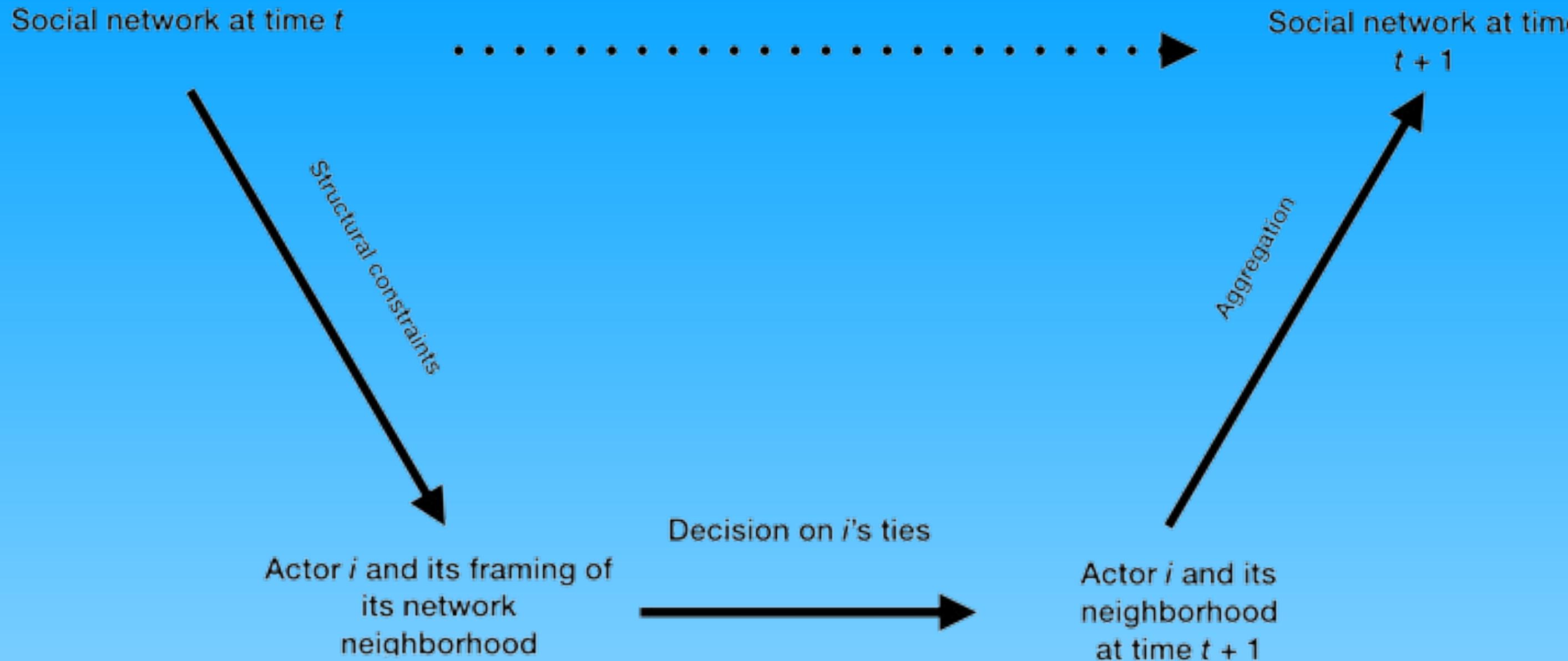
**Behave Lab and Computational Models and Designs Hub,  
Department of Social and Political Sciences, University of Milan**

**22-23 April 2024**

**Federico Bianchi**

**Behave Lab, Department of Social and Political Sciences, University of Milan**

# Causal mechanisms of social network evolution



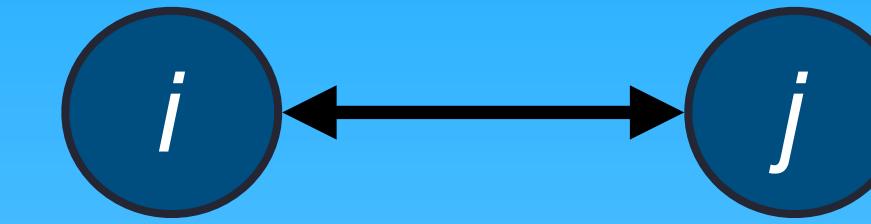
- Identifying the **causal mechanisms** of social network evolution
- Patterns of **social actors' inter(actions)** bringing about regular network structures or compositions (Hedström & Bearman, 2009)
  - **Motives** behind decisions (desires and preferences)
  - **Context framing** (cognition and culture)
  - **Types of ties** (events or states; Borgatti et al., 2009)

## Underdetermination of statistical models



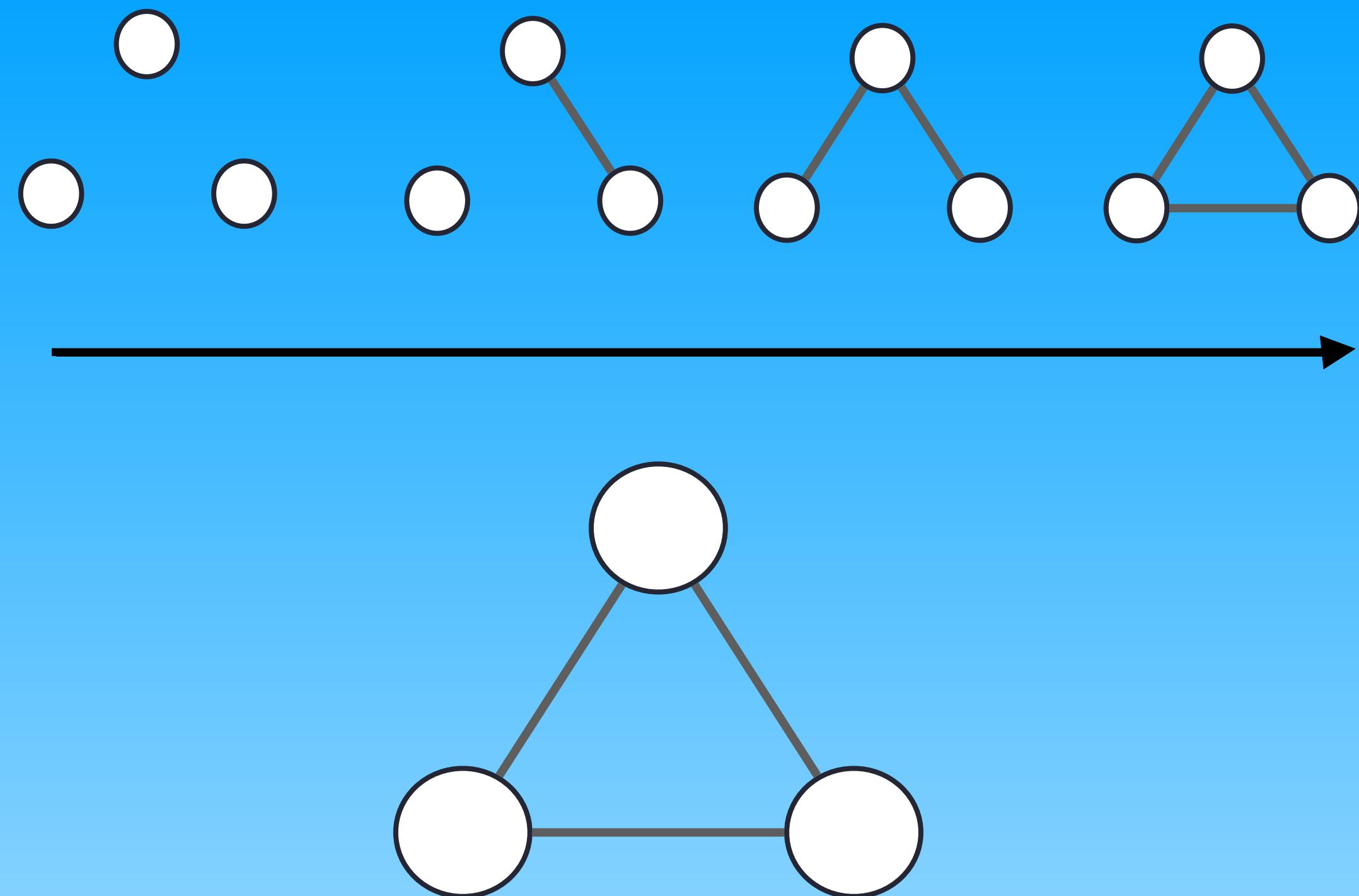
$t = 0$

1. Complying to a solidarity norm (Lindenberg, 2015)
2. Strategically investing in a long-term relationship (Coleman, 1991)
3. Controlling one's reputation (Buskens & Raub, 2005)



$t = 1$

- Statistical models of social networks usually provide **underdetermined evidence of causal mechanisms**
- “Network patterns” (Robins, 2015) or “network mechanisms” (Stadtfeld & Amati, 2021) underlie different possible causal mechanisms



**Why?**

## Methodological models

- Prevalence or incidence of the “**archeological traces**” of unobserved, past relational processes (White, 1970, 2008; Lusher et al., 2013)
- **Mathematical tractability:** sufficient statistics of local configurations + parameters estimated via robust algorithms (maximum likelihood or method of moments)
- “**Methodological models**” (Skvoretz, 1991; Sørensen, 1998): finding internal associations within aggregate-level data

```

11: if  $i$  is low-skilled ( $L$ ) then
12:   Evaluate utility from removing ties to current advisors ( $f_i^{L,rem}$ )
13:   Evaluate utility from sending requests to potential advisors ( $f_i^{L,add}$ )
14:   Select  $f_i^{L,*} = \max\{f_i^{L,rem}, f_i^{L,add}\}$ 
15:   Compute  $f_i^{L,N}$ , the utility from doing nothing
16:   if  $f_i^{L,*} > f_i^{L,N}$  and  $f_i^{L,*} = f_i^{L,add}$  then:
17:     if New advisor is a  $H$  with In-Degree ( $H$ )  $> \tau$  then
18:       Remove and redirect between 1 and  $\tau$  low-skilled  $L$  asking to  $H$ 
19:       for Every redirecting  $L$  do

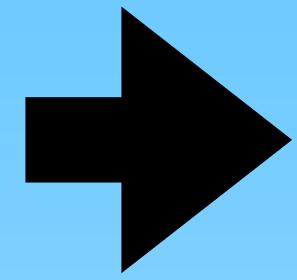
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## Theoretical models

- **Computational, dynamic models** that formalize a population of **interdependent social actors** (i.e., **agents**) with specific **properties**, interacting according to a set of **behavioural rules** within certain **environmental constraints** (Gilbert & Troitzsch, 2005; Squazzoni, 2012; Hedström & Manzo, 2015)
- ABMs are “**theoretical models**” (Skvoretz, 1991; Hedström & Manzo, 2015): models of **logical or numerical propositions** of a theory assumed to explain a phenomenon

## Real mechanism

- Actors
- Actors' properties
- Actors' (inter)actions
- Actors' relationships



## Agent-based model

- Agents
- Agents' attributes
- Agents' rules of behaviour
- Agents' structural constraints

**ABM:**

**flexibility and  
granularity**

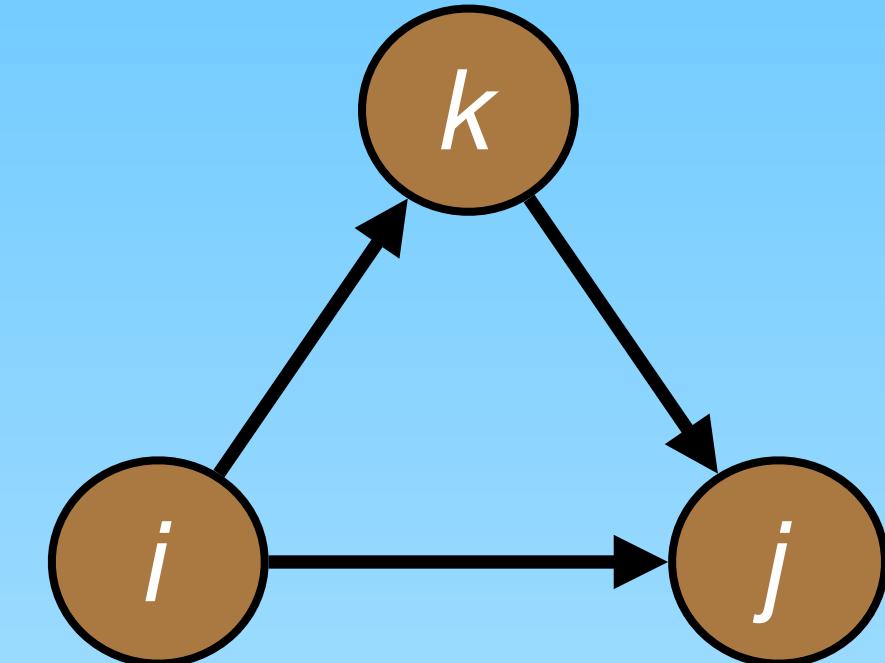
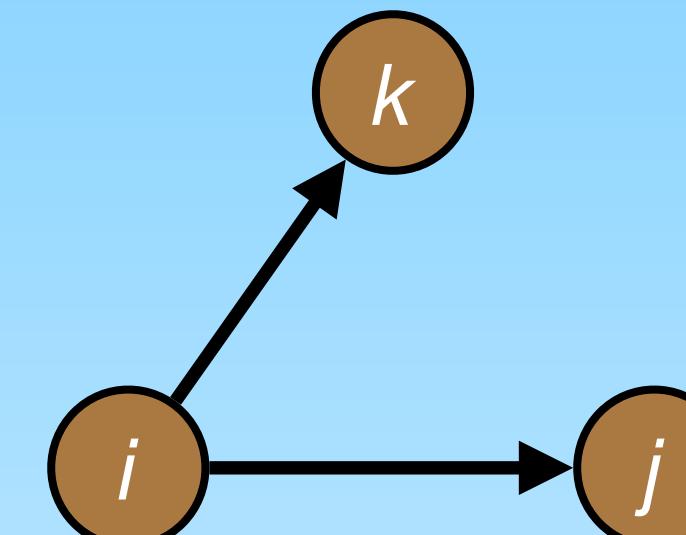
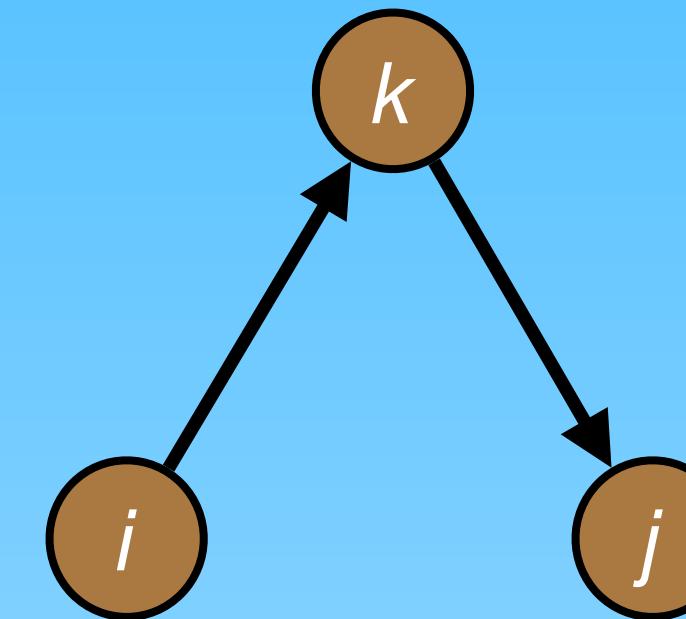
- “**Structural homology**” with causal mechanisms (Manzo, 2014):
  - **Cognitive** or **cultural** constituents of actors’ decisions
  - Social **interactions**
  - **Institutional, relational, or spatial** constraints
- High **flexibility** –> wide **granularity** range of agent modelling (Wooldridge & Jennings, 1995)
  - **Social** characteristics: autonomy, interdependence, embeddedness, heterogeneity
  - **Cognitive** characteristics: reactivity, proactivity, heuristic-based rationality, adaptiveness

$$Pr(x \rightarrow x^{\pm ij}; \theta) = \frac{1}{n(n-1)} \cdot \frac{\exp \sum_k \theta_k \Delta z_k(x, x^{\pm ij})}{1 + \exp \sum_k \theta_k \Delta z_k(x, x^{\pm ij})}$$

**ABMs can complement  
for statistical models'  
limits concerning:**

- actors' behaviour
- tie types
- context

- Tie-based models (ERGM-family; Lusher et al., 2013):**
- occurrence of a tie is assessed independently on agents' multinomial choice, typical of many decision-making contexts
  - are **indifferent to the specific tie sequences** through which particular configurations emerge (Block et al., 2019)



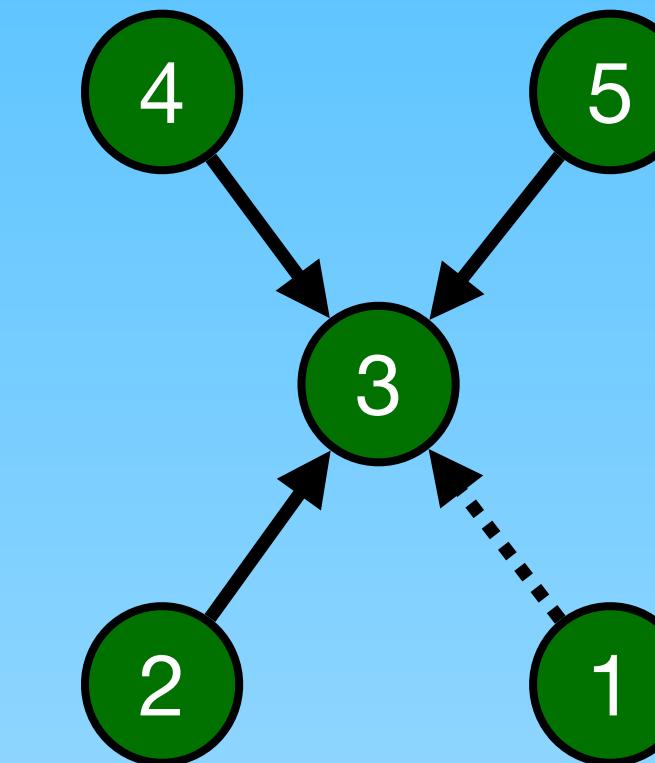
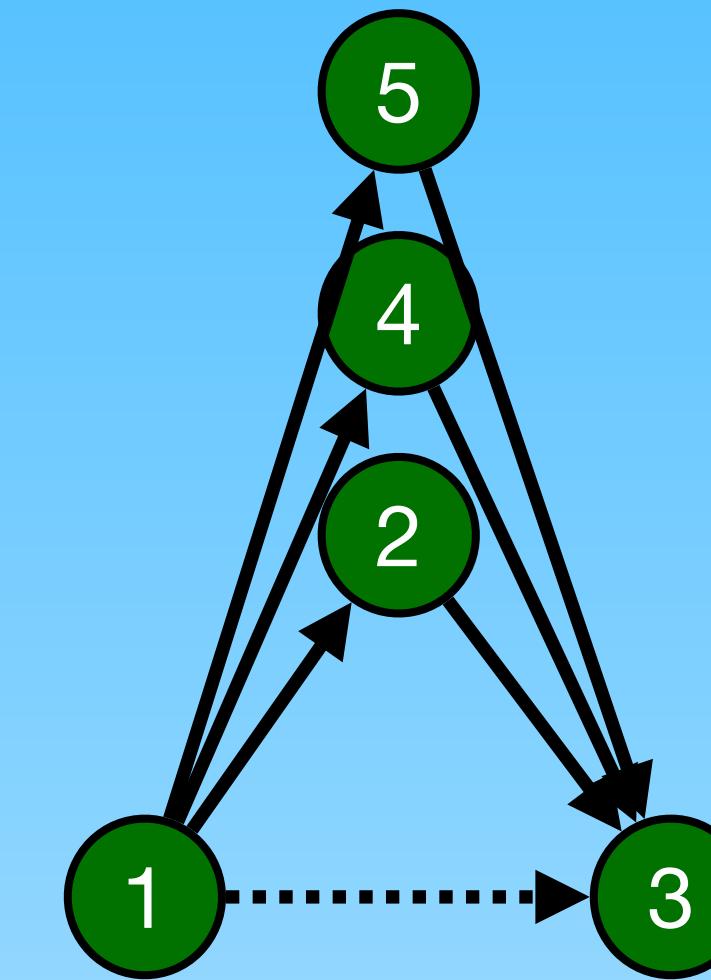


## ABMs can complement for statistical models' limits concerning:

- actors' behaviour
- tie types
- context

To be **mathematically tractable**, (most) **SAOMs** (Snijders, 2017) assume agents':

- access to **information about the whole network** (e.g., geometrically weighted configurations): **unplausible for large networks or competitive contexts** where information is strategically concealed (e.g., Renzini et al., 2023) —> **idiosyncratic models**
- **changing one tie at each simulation step: prevents modelling coordination** and collective action (Leifeld & Cranmer, 2019) and **cascade dynamics** driven by **threshold-based preferences** (Renzini et al., 2023)





$$P(x \rightarrow x^{\pm ij}) = \frac{\exp(f_i(\beta; x^{\pm ij}))}{\sum_{h=1}^n \exp(\beta; f_i(x^{(ih\pm)}))}$$

**ABMs can complement  
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- tie selection as a **multinomial choice** based on **preference optimization: unplausible for cognitive relations** not requiring psychological investment (liking vs. disliking, status attribution)
- **myopia: prevents modelling** a) **backward-looking rationality** and learning processes; b) **forward-looking rationality** (strategic behaviour in competitive contexts)

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- To be mathematically tractable, (most) SAOMs need assuming agents':
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Contents lists available at [ScienceDirect](#)

## Social Networks

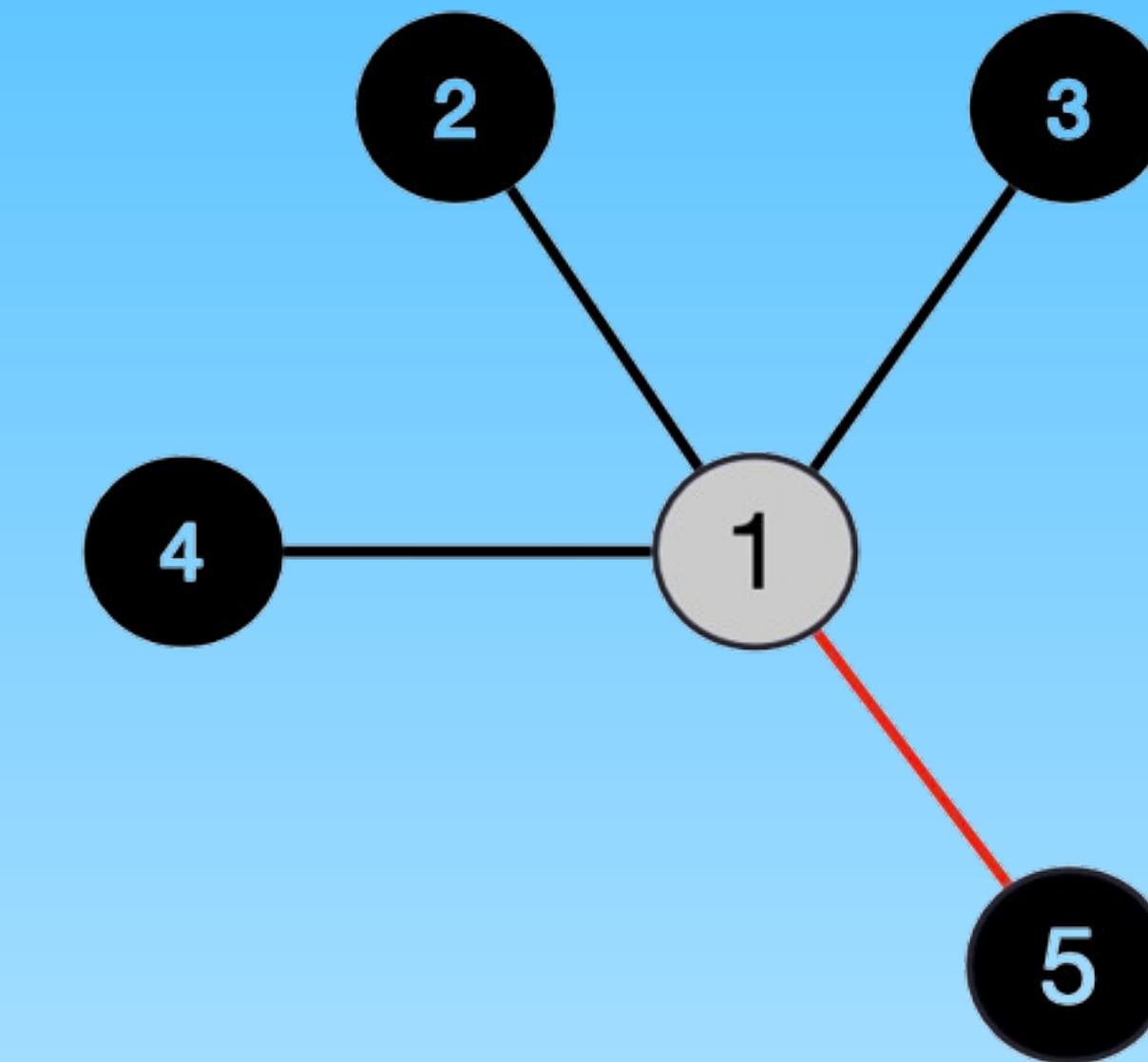
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### Status, cognitive overload, and incomplete information in advice-seeking networks: An agent-based model

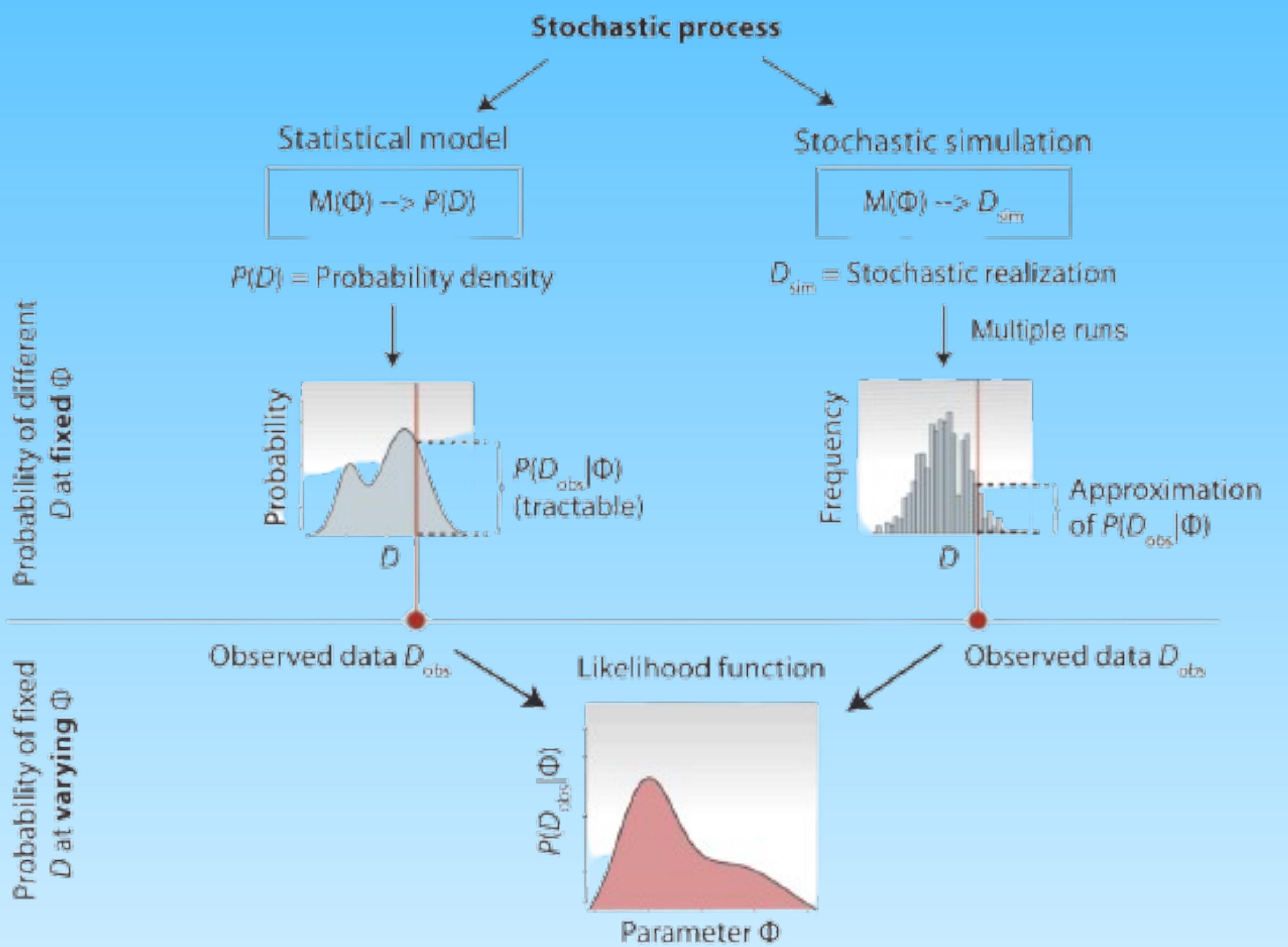
Francesco Renzini <sup>\*</sup>, Federico Bianchi, Flaminio Squazzoni

Department of Social and Political Sciences, University of Milan, Via Conservatorio 7, 20125 Milan, Italy



- **Renzini, Bianchi, & Squazzoni (2023):**
  - Explaining advice-seeking network formation as the outcome of request overload (threshold-based)
  - Limited information, local heuristics, plausible and parsimonious model
  - Fitted to classic Lazega's (2001) network
- **Bellotti, Bianchi, & Renzini (*wip*):**
  - Explaining low adoption rates of malaria preventive practices in tribal villages in Meghalaya (India)
  - Complex contagion via information ties (threshold-based) \* negative influence

## Examples of ABMs of social networks



- **Generativist method (Epstein, 2006): sequential complexification of the modelled mechanism along with computer simulations until the generated outcome fits the empirical observations (summary statistics)**
- **Testing for unobserved (unobservable?) mechanism components (e.g., thresholds, motives, etc.)**
- Simulation-based **point estimates** of parameters and **uncertainty measures** for **untractable likelihood functions** (Hartig et al., 2011; Carrella, 2021)
- **No need to rely on unplausible assumptions** to obtain a tractable likelihood function

## Theoretical, yet empirical

# Agent-based models of social networks

## A hybrid workshop

**April 22-23, 2024**

Department of Social and Political Sciences, University of Milan  
Via Conservatorio, 7 - Milan

### Discussion

- **Explicitly modelling causal mechanisms**
- **Empirically testing** their explanatory power
- More realistic and parsimonious models (middle-range)
- Modelling the **unobserved** —> not giving up on **actors' cognition/culture** (experiments), **tie diversity**, and **social context**
- To what extent and how?

# References

- Block, P., Stadtfeld, C., & Snijders, T.A.B. (2019). Forms of dependence: comparing SAOMs and ERGMs from basic principles, in *Sociological Methods & Research*, 48(1), 202-239. doi: 10.1177/0049124116672680
- Carrella, E. (2021). No free lunch when estimating simulation parameters. *Journal of Artificial Societies and Social Simulation*, 24(2), 7. doi: 10.18564/jasss.4572
- Epstein, J.M. (2006). *Generative Social Science: Studies in Agent-Based Computational Modeling*. Princeton: Princeton University Press
- Gilbert, N. & Troitzsch, K. (2005). *Simulation for the Social Scientist* (2nd ed.). Maidenhead: Open University Press.
- Hartig, F., Calabrese, J.M., Reineking, B., Wiegand, T., & Huth, A. (2011). Statistical inference for stochastic simulation models - theory and application. *Ecology Letters*, 14(8), 816-827. doi: 10.1111/j.1461-0248.2011.01640.x
- Hedström, P., & Bearman, P. (2009). What is analytical sociology all about? An introductory essay. In P. Hedström & P. Bearman (Eds.), *The Oxford Handbook of Analytical Sociology* (pp. 3-24), Oxford: Oxford University Press
- Hedström, P., & Manzo, G. (2015). Recent trends in agent-based computational research: a brief introduction. *Sociological Methods & Research*, 44(2), 179-185. doi: 10.1177/0049124115581211

# References/2

- Leifeld, P., & Cramer (2019). A theoretical and empirical comparison of the temporal exponential random graph model and the stochastic actor-oriented model. *Network Science*, 7(1), 20-51. doi: 10.1017/nws.2018.26
- Lusher, D., Koskinen, J., & Robins, G. (Eds.) (2013), *Exponential Random Graph Models. Theory, Methods, and Applications*, New York, NY: Cambridge University Press
- Manzo, G. (2014). Data, generative models, and mechanisms: more on the principles of analytical sociology. In G. Manzo (Ed.), *Analytical Sociology: Actions and Networks* (pp. 4-52). Chichester: Wiley
- Renzini, F., Bianchi, F., & Squazzoni, F. (2023). Status, cognitive overload and incomplete information in advice-seeking networks: an agent-based model. *Social Networks*, 76, 150–159. doi: 10.1016/j.socnet.2023.09.001
- Skvoretz, J. (1991). Theoretical and methodological models of networks and relations. *Social Networks*, 13(3), 275-300.
- Snijders, T.A.B. (2017). Stochastic actor-oriented models for network dynamics. *Annual Review of Statistics and its Application*, 4, 343-363. doi: 10.1146/annurev-statistics-060116-054035
- Squazzoni, F. (2012). *Agent-Based Computational Sociology*. Chichester: Wiley
- Wooldridge, M., & Jennings, N.R. (1995). Intelligent agents: theory and practice. *The Knowledge Engineering Review*, 10(2), 115-152. doi: 10.1017/S0269888900008122