

# POLITECNICO DI TORINO

Corso di Laurea Magistrale  
in Ingegneria Matematica

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## Some recent results on the norm of localization operators



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