

Lectures on PIV

Last developments and applications

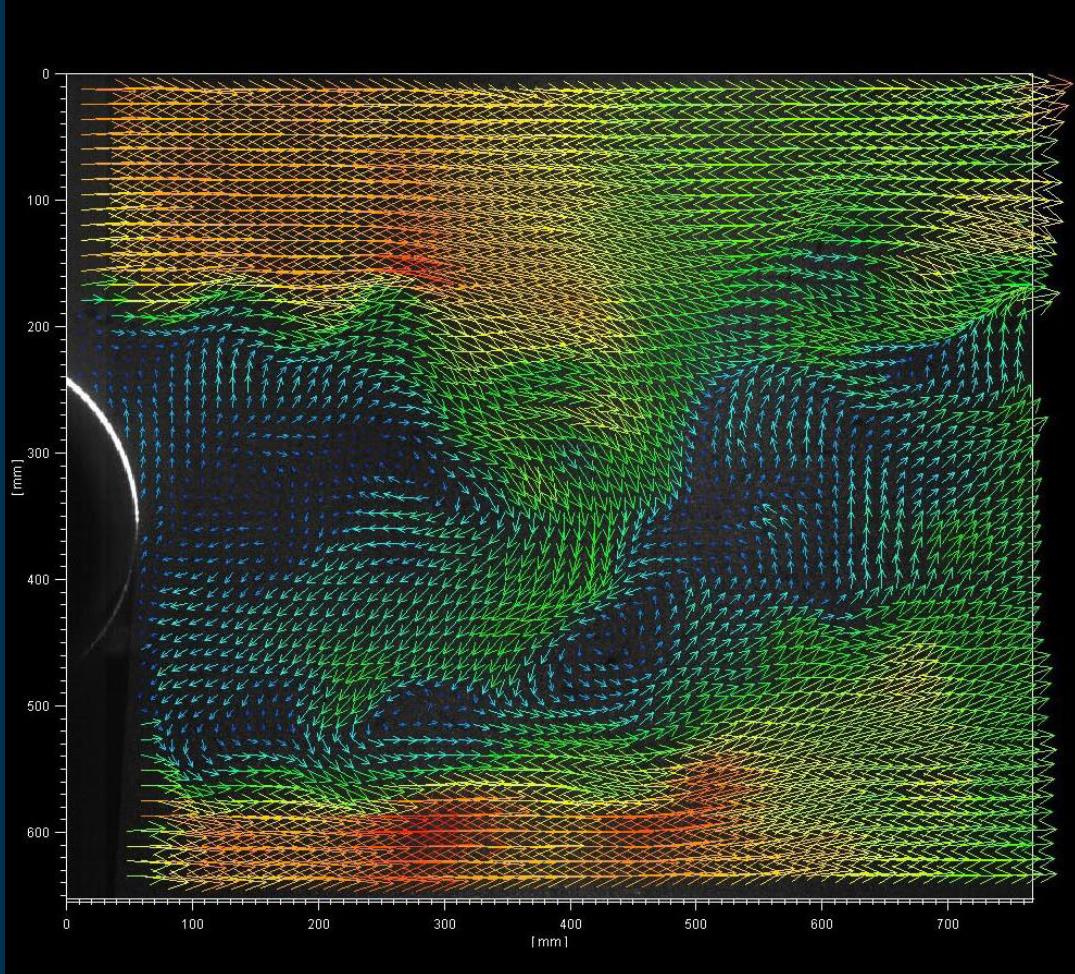
30/11/2022

Federico Cutolo
Giuseppe Familiari
Francesco Miccoli
Giovanni Maria Maneschi

PIV-base pressure and force measurement

Federico Cutolo

Outline



- Pressure extraction from planar velocimetry data
 - Models
 - Boundary conditions
 - Models comparison
 - Dealing with limited resources
- Force extraction from planar velocimetry data
 - Models
 - An example
- Uncertainty sources

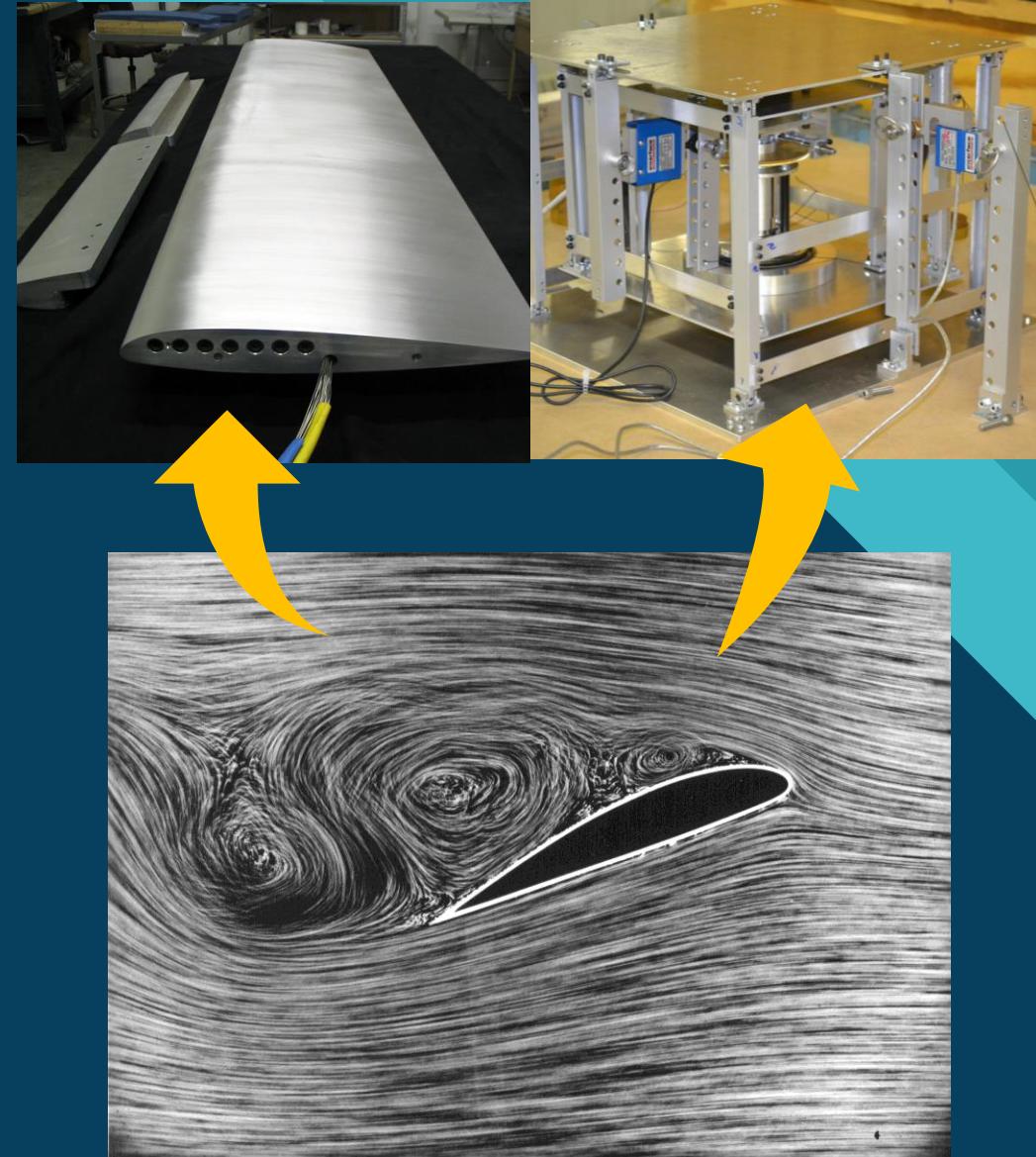
PIV-based measurements: why

- Flow field information and mechanical loads are traditionally obtained by separate techniques:
 - Pressure tappings for surface pressure distribution
 - Force balances for integral loads
 - Probes for point-wise measurements



PIV-based measurements:

- Appealing approach to establish a **direct link** between flow behaviour and loads
- Measuring pressure where direct measurement is **impossible**



Pressure extraction: principles

Two main approaches have been proposed over the years:

- **Integration** of the Navier-Stokes momentum equation
(Gurka et al. 1999)

$$\nabla p = -\rho \left(\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} \right) + \mu \nabla^2 \mathbf{u}$$

- **Solution** of the Poisson equation fro the pressure (Baur & Kongeter 1999)

$$-\nabla^2 p = -\rho \nabla \cdot ((\mathbf{u} \cdot \nabla) \mathbf{u})$$

Hypothesis

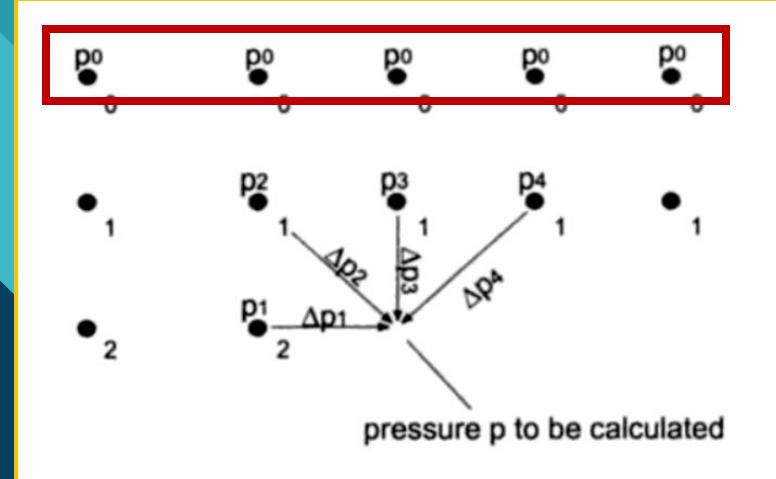
- 2D
- *Incompressible*

$$(\nabla \cdot \mathbf{u} = 0)$$

Pressure extraction: NS momentum

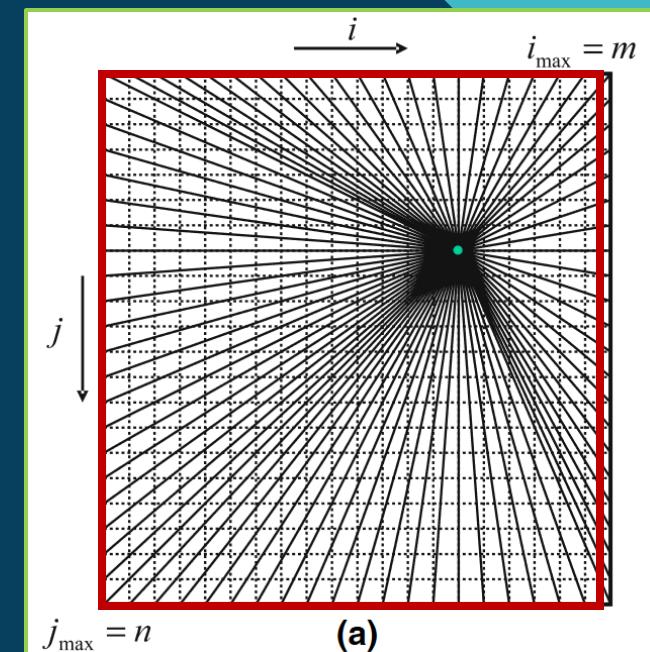
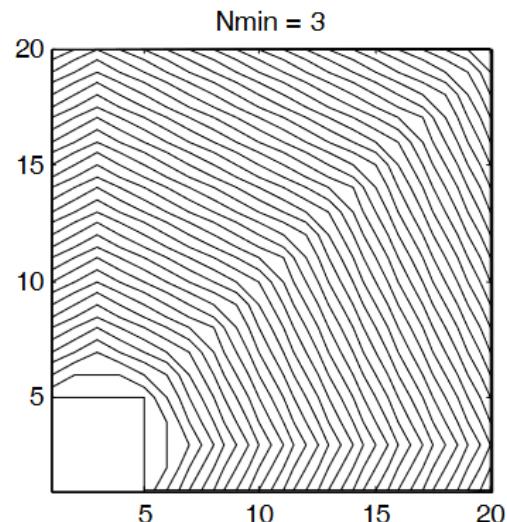
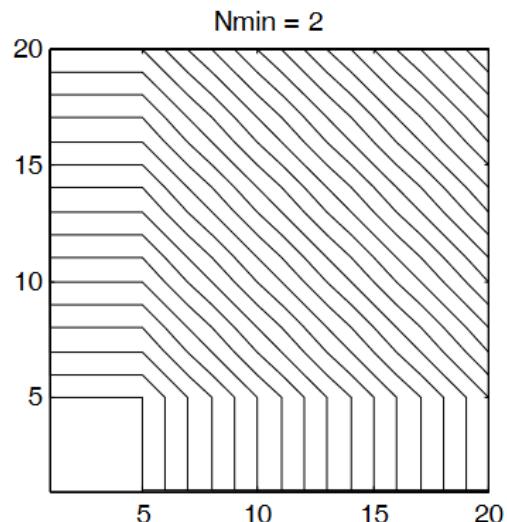
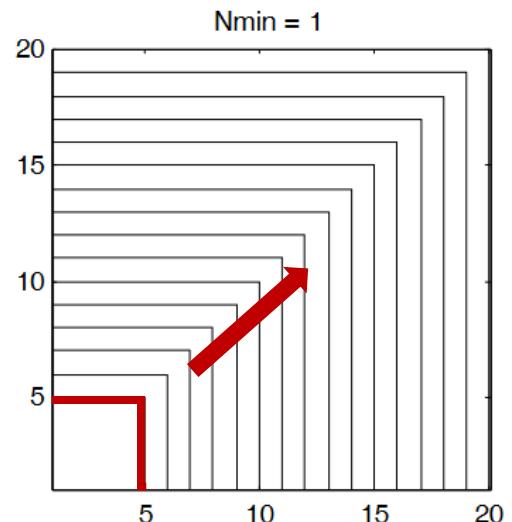
Integration of the NS momentum equation by means of spatial marching scheme

- Systematic marching
- Field erosion



Liu & Katz 2006

Oudheusden & Souverein 2007





Pressure extraction: Poisson

Solution of the Poisson equation for the pressure

- By iterative method
- Despite the incompressibility constraint, the pressure field can still be time-dependent



- Neumann Boundary conditions



- Dirichlet Boundary conditions

Pressure extraction: Boundary Conditions treatment

- Poisson requires BC on the **entire contour** of the integration domain
- NS requires BC on a **limited region** (even a single point!)
- Neumann BC from **momentum** equation (Gurka et al. 1999)
- Dirichlet BC from pressure measurements
 - Bernoulli equation (Hp: irrotational regions)
 - Pressure **tappings**

Poisson more stable with
Dirichlet conditions only!

[Auteri, 2015]

Pressure extraction: summary

Poisson

Need for a simple-connected & simple geometry domain



No masked areas (e.g. corrupted/unavailable data region)

NS momentum

Suffers of error propagation



Sub-division of the integration domain to reduce it

Both have strong dependence on the boundary condition (which and where)

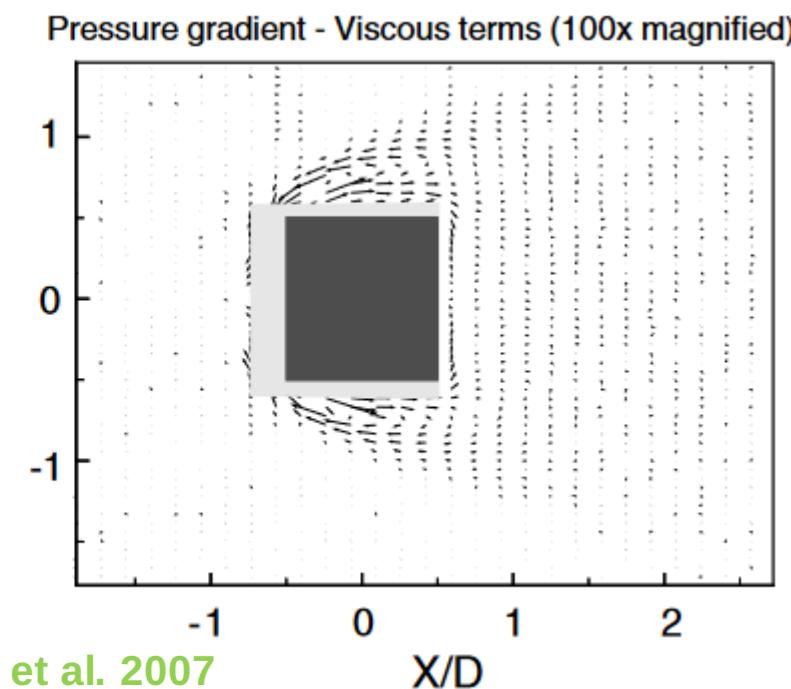
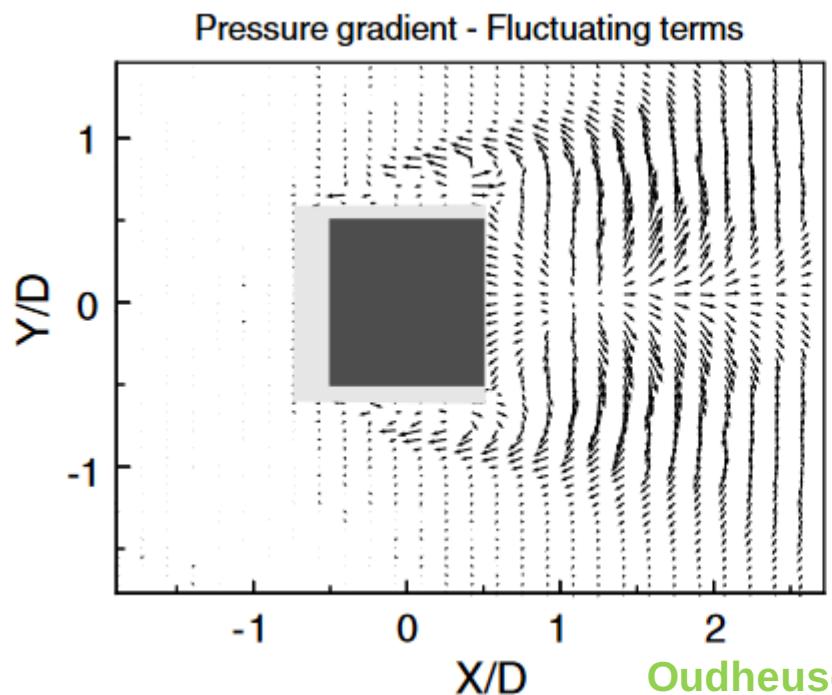
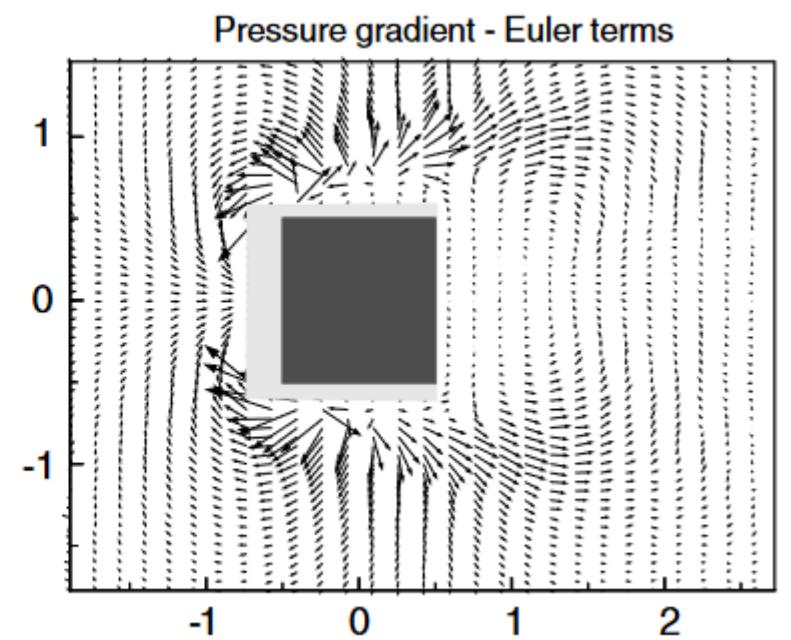
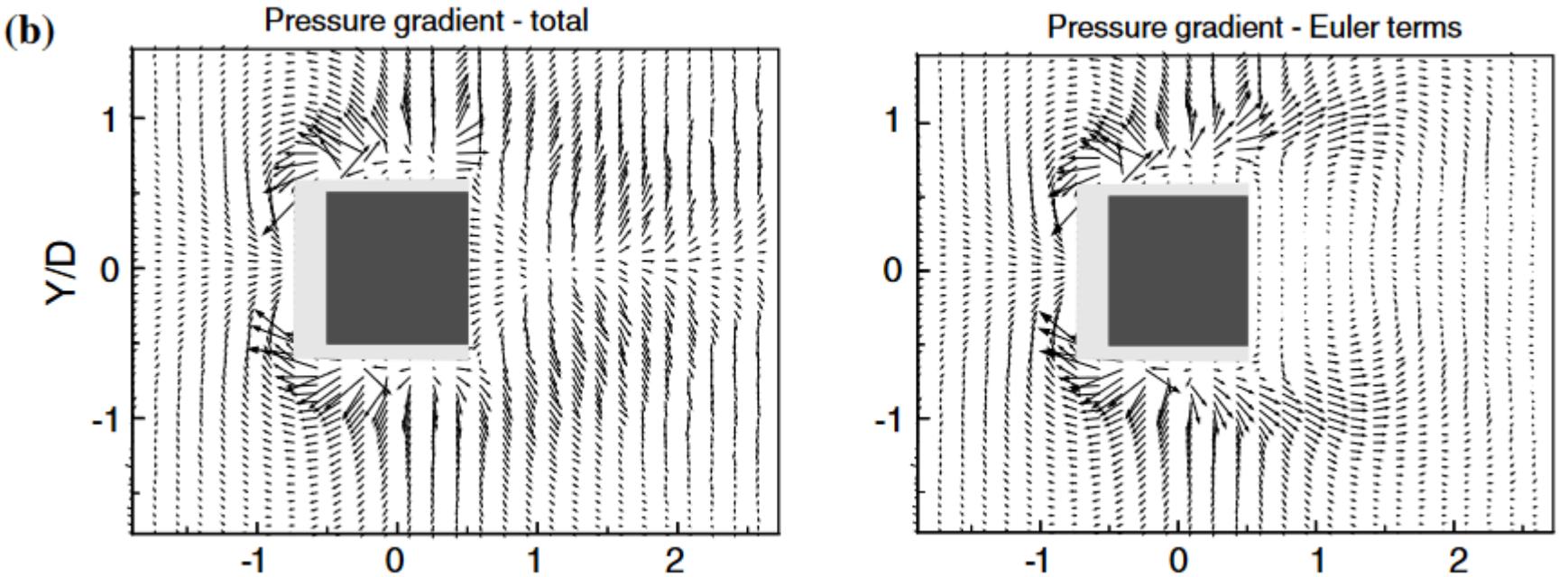
Pressure

- Hp: adequate time (quasi)

- Synthetic

$$\frac{\partial}{\partial t} < \nu$$

No need

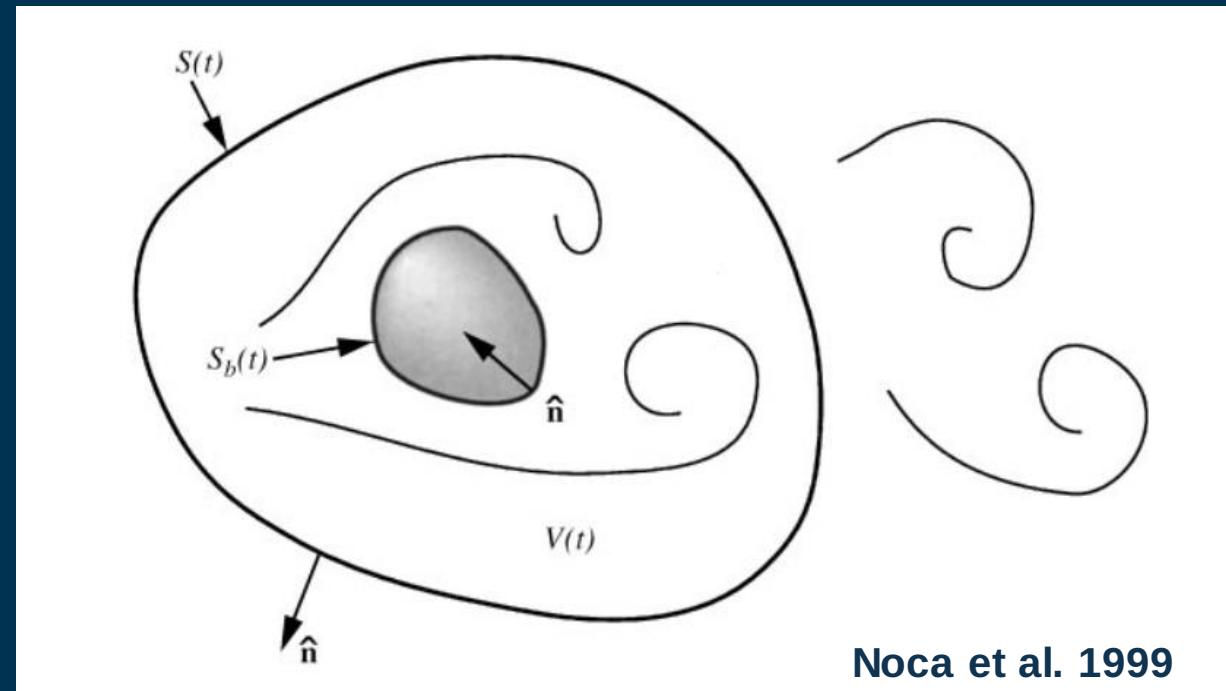


Oudheusden et al. 2007

Loads extraction: principles

Control-volume approach: balance of the NS momentum equation on a domain surrounding the body

- Momentum-based methods (integral form): **pressure is needed**
- Vorticity-based methods: pressure is analytically **eliminated**



Noca et al. 1999

Loads extraction: momentum-based

- NS integral momentum equation:

$$\mathbf{F}(t) = - \left[\int_{V(t)} \frac{\partial \rho \mathbf{u}}{\partial t} dV \right] - \boxed{\int_{S(t)+S_b(t)} \rho \mathbf{u} (\mathbf{u} \cdot \mathbf{n}) dS} + \boxed{\int_{S(t)} (-p \mathbf{n} + \boldsymbol{\tau} \cdot \mathbf{n}) dS}$$

Volume integral acceleration

Momentum flux across the contour

Total force (pressure + viscous stresses)

Pressure is needed on the contour: (differential) momentum integration

Loads extraction: vorticity-based

Fluid-dynamic **impulse** method (Batchelor, 1967):
no pressure needed

- Hp: the control volume has to **include** all the **vorticity** in the domain



Momentum-based impulse method, (Noca, 1997)

- Vorticity is integrated **on surfaces**



Flux equation impulse method, (Noca, 1997)

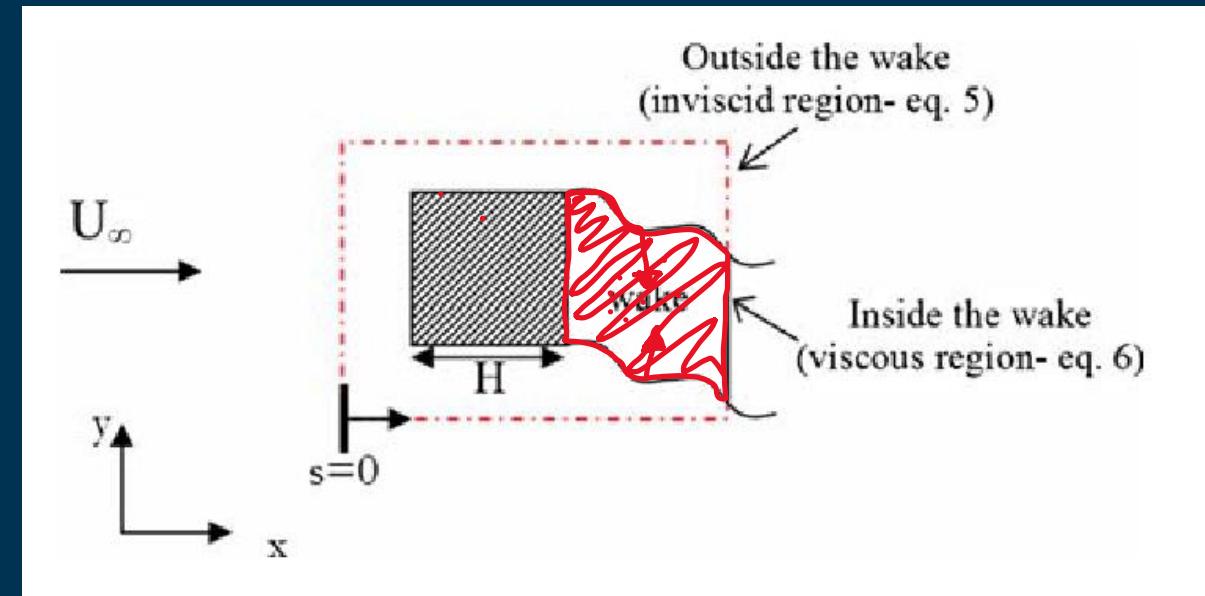
- Only contains surface **integrals** (Hp: $\nabla \cdot \mathbf{u} = 0$)



Example: loads on square prism

The flow around a square cylinder was investigated to study the time-varying loads by means of:

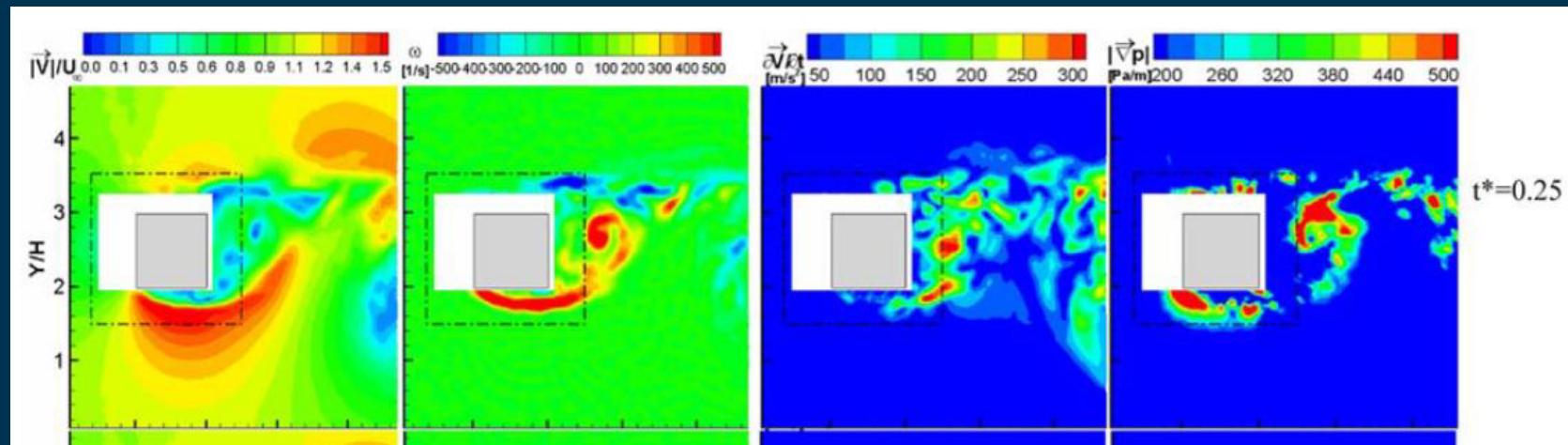
- Control-volume approach
- Spatial integration for pressure gradient
- Time-resolved PIV (high repetition rate laser)

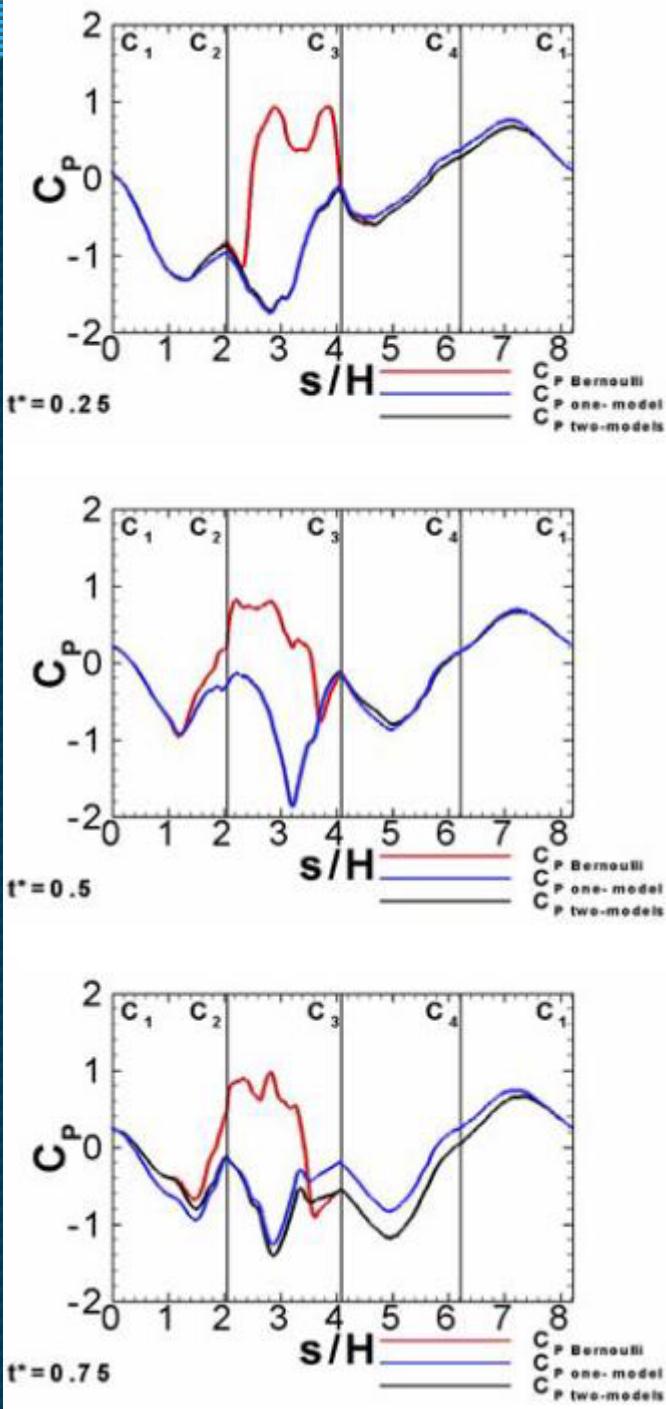


Example: loads on square prism

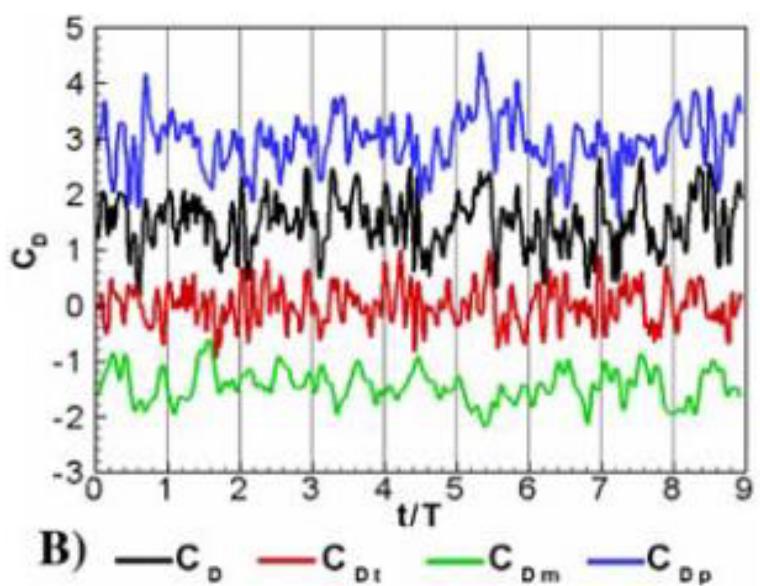
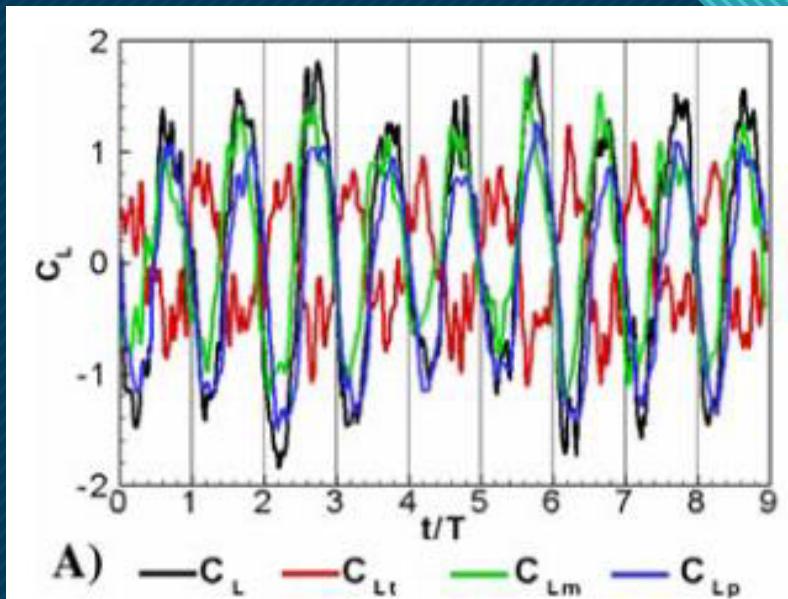
Results:

- Far from the body and outside the wake, the pressure reproduces the velocity pattern
- Alternating value of the pressure in phase opposition on the upper and down sides
- Unsteady lift force fluctuating at half the vortex shedding frequency





$$F(t) = \boxed{- \int_{V(t)} \frac{\partial \rho u}{\partial t} dV} - \int_{S(t) + S_b(t)} \rho u (u \cdot n) dS + \int_{S(t)} (-pn + \tau \cdot n) dS$$



Lift and drag coefficients are obtained:

- Integration of the momentum equation terms along the control surface
- Integration of the unsteady term within the control volume

Error and uncertainty sources

