PRACTICA 1 PREDICCION

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24 de octubre de 2017

- Se pide el mejor modelo de regresion para estimar la rentabilidad a 1 año:

1. Carga de datos:

En primer lugar, abrimos el csv y visualizamos por encima el mismo intuyendo que problemas podremos tener en cuanto a limpieza del archivo.

```
DS<-read.csv2("Fondos.csv")
getwd()

## [1] "/Users/fede/Desktop/DS/Prediccion"
vY<-DS$rent_1
vX<-cbind(1,DS[,])</pre>
```

Observamos que nuestro data frame de 500 observaciones y 30 variables, hay algunas que no resultan de interes para nuestro estudio y otras que desafortunadamente carecen de datos y no aparecen o aparececen como NA y que habra que eliminar para que no perturbe nuestro modelo.

2. Limpieza del fichero:

```
# Eliminamos las columnas que no son validas para nuestro estudio, y dejamos las que, a priori, nos van DS<-DS[,-3]
DS<-DS[,-3]
DS<-DS[,-11]
DS<-DS[,-11]
DS<-DS[,-13]
DS<-DS[,-18]
DS<-DS[,-18]
DS<-DS[,-18]
DS<-DS[,-17]
DS<-DS[,-17]
```

```
# Tras esto, seguimos teniendo un problema clave que podria alterar nuestro modelo, que son los valores
library(rminer)
library(kknn)
DS=na.omit(DS)
cat("NA values:",sum(is.na(DS)),"\n")
```

NA values: 0

3. Selecion del modelo:

```
regresion01<-lm(rent_1~ Inv_minima_inicial+ X1_Day_Return + X1_Week_Return + rent_1_mes + rent_3_meses
   rent_6_meses + rent_en_el_anio + rent_10_anios +
   Capitaliz_media_bursatil + Sharpe_.3 + Volatilidad_3 + Com_Gestion + Com_deposito, data= DS)
summary(regresion01)
##
## Call:
## lm(formula = rent_1 ~ Inv_minima_inicial + X1_Day_Return + X1_Week_Return +
##
      rent_1_mes + rent_3_meses + rent_6_meses + rent_en_el_anio +
##
      rent_10_anios + Capitaliz_media_bursatil + Sharpe_.3 + Volatilidad_3 +
##
      Com_Gestion + Com_deposito, data = DS)
##
## Residuals:
##
      Min
               1Q Median
                               30
## -2.6529 -0.4908 -0.0068 0.5268 3.1810
## Coefficients:
                             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                           -1.748e+00 3.202e-01 -5.458 2.25e-07 ***
## Inv_minima_inicial
                           -4.523e-07 3.514e-07 -1.287 0.200323
## X1_Day_Return
                            6.234e-02 1.098e-01
                                                   0.568 0.571195
## X1_Week_Return
                           -2.281e-01 7.780e-02 -2.931 0.003968 **
## rent_1_mes
                                                  -0.649 0.517508
                           -6.759e-02 1.042e-01
## rent_3_meses
                            1.647e-01 7.322e-02
                                                  2.249 0.026144 *
## rent_6_meses
                           -2.033e-01 3.283e-02 -6.192 6.79e-09 ***
## rent_en_el_anio
                            9.046e-01 2.345e-02 38.581 < 2e-16 ***
## rent_10_anios
                            1.785e-01 6.211e-02
                                                   2.874 0.004715 **
## Capitaliz_media_bursatil 4.902e-06 4.785e-06
                                                   1.025 0.307411
## Sharpe_.3
                            1.430e+00 3.462e-01
                                                   4.131 6.31e-05 ***
                           -1.064e-01 3.073e-02
                                                 -3.463 0.000718 ***
## Volatilidad_3
## Com Gestion
                            3.025e-01 2.017e-01
                                                   1.500 0.136089
## Com_deposito
                           -7.415e-01 1.036e+00 -0.716 0.475471
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.028 on 134 degrees of freedom
## Multiple R-squared: 0.9671, Adjusted R-squared: 0.9639
## F-statistic: 303.2 on 13 and 134 DF, p-value: < 2.2e-16
```

Nueva Regresion:

```
regresion02<-lm(rent_1~rent_6_meses + rent_en_el_anio + Sharpe_.3 + Volatilidad_3, DS)
summary(regresion02)
##
## Call:
## lm(formula = rent_1 ~ rent_6_meses + rent_en_el_anio + Sharpe_.3 +
       Volatilidad_3, data = DS)
##
## Residuals:
##
      Min
                1Q Median
                                30
                                       Max
## -2.8204 -0.5614 0.0270 0.5119 4.0533
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -1.63982
                              0.24769 -6.620 6.72e-10 ***
## rent_6_meses
                   -0.18316
                               0.03194 -5.734 5.60e-08 ***
## rent_en_el_anio 0.90117
                              0.01960 45.989 < 2e-16 ***
## Sharpe_.3
                   2.15354
                              0.28443
                                       7.571 4.17e-12 ***
## Volatilidad_3
                   -0.09763
                               0.02873 -3.398 0.000879 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.087 on 143 degrees of freedom
## Multiple R-squared: 0.9608, Adjusted R-squared: 0.9597
## F-statistic: 875.3 on 4 and 143 DF, p-value: < 2.2e-16
# Utilizamos el Best Subset para comprobar que hemos elegido bien nuestras variables:
library (leaps)
regfit.full=regsubsets(rent 1~ Inv minima inicial+ X1 Day Return + X1 Week Return + rent 1 mes + rent
    rent_6_meses + rent_en_el_anio + rent_10_anios +
    Capitaliz_media_bursatil + Sharpe_.3 + Volatilidad_3 + Com_Gestion + Com_deposito, data= DS)
reg.summary=summary(regfit.full)
reg.summary
## Subset selection object
## Call: regsubsets.formula(rent_1 ~ Inv_minima_inicial + X1_Day_Return +
##
       X1_Week_Return + rent_1_mes + rent_3_meses + rent_6_meses +
       rent_en_el_anio + rent_10_anios + Capitaliz_media_bursatil +
##
       Sharpe_.3 + Volatilidad_3 + Com_Gestion + Com_deposito, data = DS)
## 13 Variables (and intercept)
                            Forced in Forced out
## Inv_minima_inicial
                                FALSE
                                           FALSE
## X1 Day Return
                                FALSE
                                           FALSE
## X1_Week_Return
                                FALSE
                                           FALSE
## rent_1_mes
                                FALSE
                                           FALSE
## rent_3_meses
                                FALSE
                                           FALSE
## rent_6_meses
                               FALSE
                                           FALSE
## rent_en_el_anio
                                FALSE
                                           FALSE
## rent_10_anios
                                FALSE
                                           FALSE
## Capitaliz_media_bursatil
                                FALSE
                                           FALSE
## Sharpe_.3
                                FALSE
                                           FALSE
## Volatilidad_3
                                FALSE
                                           FALSE
```

```
## Com_Gestion
                              FALSE
                                         FALSE
## Com_deposito
                              FALSE
                                         FALSE
## 1 subsets of each size up to 8
## Selection Algorithm: exhaustive
           Inv_minima_inicial X1_Day_Return X1_Week_Return rent_1_mes
                                           11 11
## 1 (1)""
                              11 11
                                           11 11
## 2 (1)""
## 3 (1)""
                                                          11 11
                              11 11
                                           11 11
## 4 (1)""
                              11 11
## 5 (1)""
                              .. ..
## 6 (1) " "
                                           11 🕌 11
                              11 11
## 7 (1)""
                                           "*"
                              11 11
                                           "*"
                                                          .. ..
## 8 (1)""
##
           rent_3_meses rent_6_meses rent_en_el_anio rent_10_anios
## 1 (1)""
                        11 11
                                    "*"
     (1)""
                        "*"
                                     "*"
## 2
                                                    .. ..
## 3 (1)""
                        "*"
                                     "*"
## 4 (1)""
                        "*"
                                    "*"
## 5 (1)""
                        "*"
                                     "*"
                                     "*"
## 6 (1) " "
                        "*"
                                                    11 * 11
                        "*"
                                     "*"
                                                    "*"
## 7 (1)"*"
                        "*"
                                     "*"
                                                    "*"
## 8 (1) "*"
##
           Capitaliz_media_bursatil Sharpe_.3 Volatilidad_3 Com_Gestion
                                   11 11
                                             11 11
## 1 (1)""
## 2 (1)""
                                             11 11
                                                           11 11
## 3 (1)""
                                   "*"
## 4 (1)""
                                             "*"
                                   "*"
## 5 (1)""
                                   "*"
                                             "*"
## 6 (1) " "
                                   "*"
                                             "*"
## 7 (1)""
                                                           11 11
                                   "*"
                                             "*"
## 8 (1)""
                                   "*"
                                             "*"
                                                           "*"
##
           Com_deposito
## 1 (1)""
## 2 (1)""
## 3 (1)""
## 4 (1)""
## 5 (1)""
## 6 (1)""
## 7
     (1)""
## 8 (1)""
reg.summary$bic
## [1] -351.5088 -401.1186 -447.7473 -454.2439 -455.0070 -458.4547 -458.0226
## [8] -456.2119
summary(regresion02)
##
## lm(formula = rent_1 ~ rent_6_meses + rent_en_el_anio + Sharpe_.3 +
      Volatilidad_3, data = DS)
##
##
## Residuals:
##
      Min
               1Q Median
                              3Q
                                     Max
```

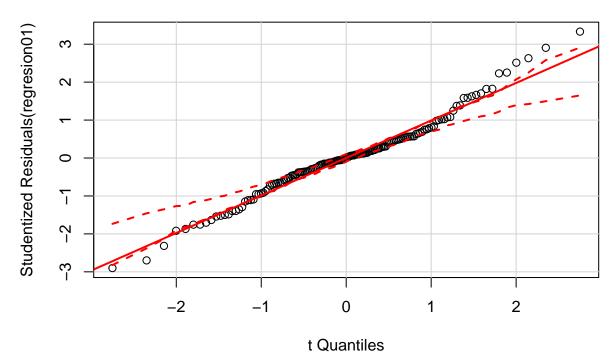
```
## -2.8204 -0.5614 0.0270 0.5119 4.0533
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   -1.63982
                               0.24769
                                       -6.620 6.72e-10 ***
                               0.03194 -5.734 5.60e-08 ***
## rent_6_meses
                   -0.18316
## rent_en_el_anio 0.90117
                               0.01960
                                       45.989 < 2e-16 ***
                                        7.571 4.17e-12 ***
## Sharpe_.3
                    2.15354
                               0.28443
## Volatilidad_3
                   -0.09763
                               0.02873 -3.398 0.000879 ***
## ---
## Signif. codes:
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.087 on 143 degrees of freedom
## Multiple R-squared: 0.9608, Adjusted R-squared: 0.9597
## F-statistic: 875.3 on 4 and 143 DF, p-value: < 2.2e-16
```

Finalmente nos decantamos por el modelo dos basandonos en signnificatividad de las variables, el alto

3. Diagnosis:

Ahora comprobamos normalidad:

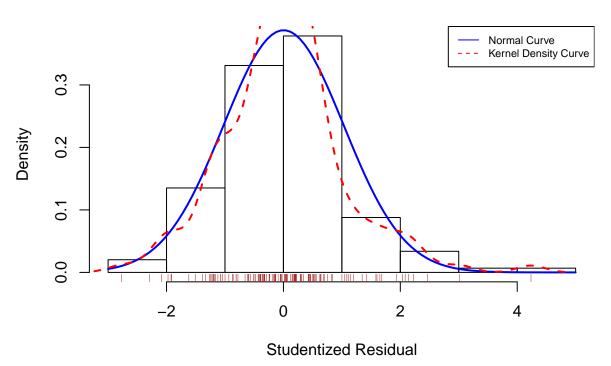
Q-Q Plot



```
residplot <- function(fit, nbreaks=10) {
  z <- rstudent(fit)
  hist(z, breaks=nbreaks, freq=FALSE,</pre>
```

```
xlab="Studentized Residual",
    main="Distribution of Errors")
rug(jitter(z), col="brown")
curve(dnorm(x, mean=mean(z), sd=sd(z)),
    add=TRUE, col="blue", lwd=2)
lines(density(z)$x, density(z)$y,
    col="red", lwd=2, lty=2)
legend("topright",
    legend = c( "Normal Curve", "Kernel Density Curve"),
    lty=1:2, col=c("blue", "red"), cex=.7)
}
residplot(regresion02)
```

Distribution of Errors



podemos observar como los residuos obtenidos de la regresion02 se distribuyen normalmente. Seguidamente realizamos el test de Jarque Bera para corroborarlo.

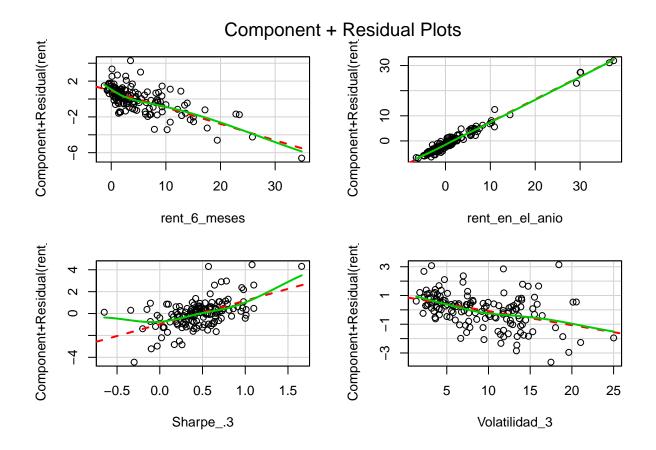
library(fBasics)

```
## Loading required package: timeDate
## Loading required package: timeSeries
##
## Rmetrics Package fBasics
## Analysing Markets and calculating Basic Statistics
## Copyright (C) 2005-2014 Rmetrics Association Zurich
## Educational Software for Financial Engineering and Computational Science
## Rmetrics is free software and comes with ABSOLUTELY NO WARRANTY.
```

```
## https://www.rmetrics.org --- Mail to: info@rmetrics.org
##
## Attaching package: 'fBasics'
## The following object is masked from 'package:car':
##
##
       densityPlot
vResid=resid(regresion02)
library(timeDate)
library(timeSeries)
jbTest(vResid)
## Warning in interpp.old(x, y, z, xo, yo, ncp = 0, extrap = FALSE, duplicate
## = "median", : interpp.old() is deprecated, future versions will only
## provide interpp()
## Warning in interpp.old(x, y, z, xo, yo, ncp = 0, extrap = FALSE, duplicate
## = "median", : interpp.old() is deprecated, future versions will only
## provide interpp()
##
## Title:
## Jarque - Bera Normality Test
## Test Results:
    PARAMETER:
##
##
       Sample Size: 148
    STATISTIC:
##
       LM: 15.1
       ALM: 17.128
##
##
   P VALUE:
       LM p-value: 0.006
##
       ALM p-value: 0.006
##
##
       Asymptotic: 0.001
##
## Description:
## Sat Oct 28 16:08:44 2017 by user:
shapiro.test(vResid)
##
   Shapiro-Wilk normality test
##
## data: vResid
## W = 0.97605, p-value = 0.01085
```

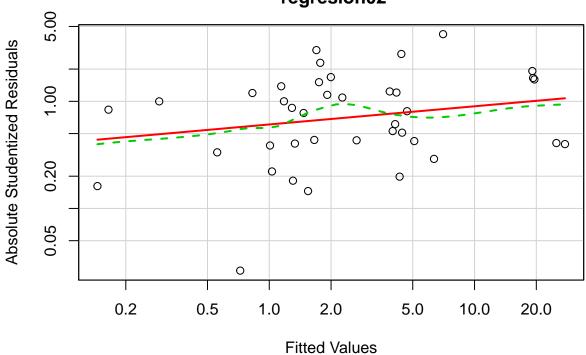
Realizando ambos Test comprobamos que no podemos rechazar la Hipotesis Nula y por tanto los residuos de esta regresion se distribuyen siguiendo una normal.

```
crPlots(regresion02)
```



el proximo paso es comprobar la varianza de las observaciones es o no constante (homocedasticidad o heterocedasticidad). Para ello utilizamos el test de Breusch-Pagan en donde la H0 implica homocedasticidad.

Spread-Level Plot for regresion02



##
Suggested power transformation: 0.8303391

En este primer caso de regresion02 podemos concluir que la varianza de las observaciones es constante, ya que no podemos rechazar la H0.

Seguidamente relizamos el test de validacion global en nuestro modelo:

```
# Regresion3
library(gvlma)
gvmodel <- gvlma(regresion02)</pre>
summary(gvmodel)
##
## Call:
## lm(formula = rent_1 ~ rent_6_meses + rent_en_el_anio + Sharpe_.3 +
##
       Volatilidad_3, data = DS)
##
## Residuals:
       Min
                1Q Median
                                 3Q
                                        Max
## -2.8204 -0.5614 0.0270 0.5119 4.0533
## Coefficients:
```

```
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  -1.63982
                              0.24769 -6.620 6.72e-10 ***
## rent 6 meses
                   -0.18316
                              0.03194 -5.734 5.60e-08 ***
## rent_en_el_anio 0.90117
                              0.01960 45.989 < 2e-16 ***
## Sharpe .3
                   2.15354
                              0.28443
                                        7.571 4.17e-12 ***
## Volatilidad 3
                  -0.09763
                              0.02873 -3.398 0.000879 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.087 on 143 degrees of freedom
## Multiple R-squared: 0.9608, Adjusted R-squared: 0.9597
## F-statistic: 875.3 on 4 and 143 DF, p-value: < 2.2e-16
##
## ASSESSMENT OF THE LINEAR MODEL ASSUMPTIONS
## USING THE GLOBAL TEST ON 4 DEGREES-OF-FREEDOM:
## Level of Significance = 0.05
##
## Call:
##
   gvlma(x = regresion02)
##
##
                        Value p-value
## Global Stat
                     22.28287 0.000176 Assumptions NOT satisfied!
## Skewness
                      4.63147 0.031391 Assumptions NOT satisfied!
## Kurtosis
                     10.46829 0.001214 Assumptions NOT satisfied!
## Link Function
                      0.06065 0.805473
                                          Assumptions acceptable.
## Heteroscedasticity 7.12246 0.007612 Assumptions NOT satisfied!
```

4. Multicolinealidad:

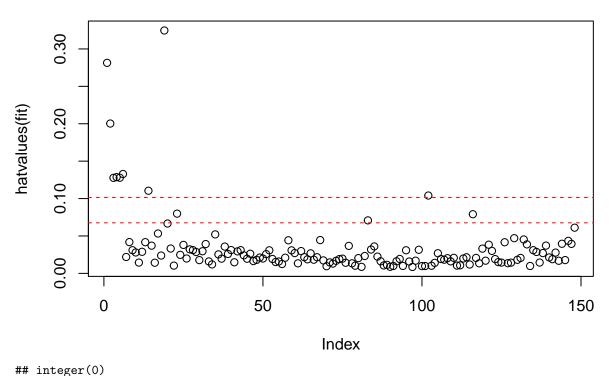
Seguimos comprobando la validez de nuestro modelo, comprobando si existe correlacion entre las variables explicativas (mulicolinealidad) mediante el Test VIF (Factor de inflacion de la varianza).

```
# Regresion3
vif(regresion02)
      rent_6_meses rent_en_el_anio
##
                                           Sharpe_.3
                                                       Volatilidad_3
##
          4.158433
                           2.296332
                                            1.037553
                                                             2.555556
sqrt(vif(regresion02)) > 2
##
      rent_6_meses rent_en_el_anio
                                           Sharpe_.3
                                                       Volatilidad_3
                                               FALSE
##
              TRUE
                              FALSE
                                                               FALSE
```

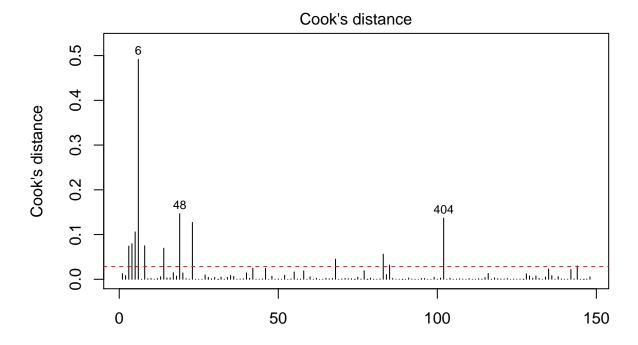
Con el resultado del Test VIF concluimos que, en regresion02, la variable rentabilidad 6 meses presenta multicolinealidad.

5. Identificacion de observaciones anomalas:

Index Plot of Hat Values

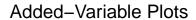


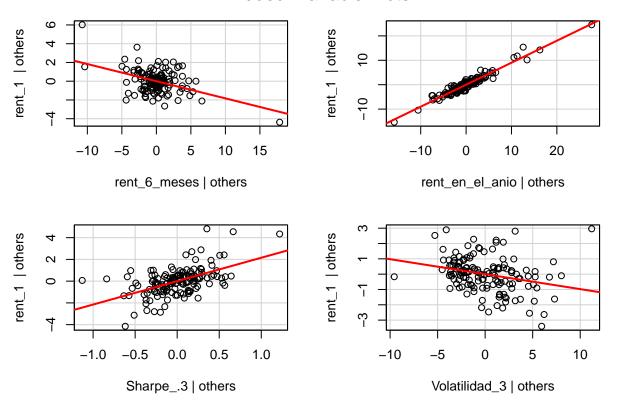
```
### Integer(0)
#Tambien observamos los valores influyentes:
cutoff <- 4/(nrow(DS)-length(regresion02$coefficients)-2)
plot(regresion02, which=4, cook.levels=cutoff)
abline(h=cutoff, lty=2, col="red")</pre>
```



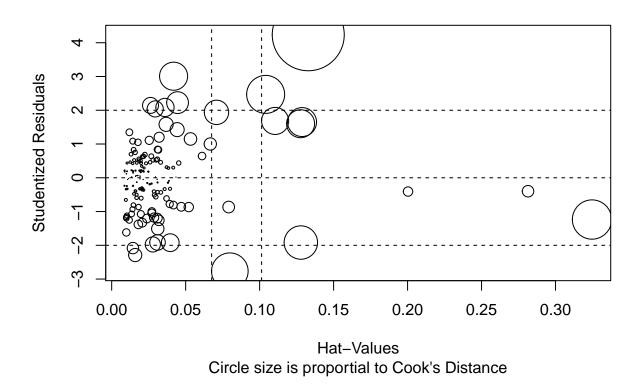
Obs. number Im(rent_1 ~ rent_6_meses + rent_en_el_anio + Sharpe_.3 + Volatilidad_3)

avPlots(regresion02, ask=FALSE, id.method="identify")





Influence Plot



Observamos que tenemos una observacion anomala y la elimnamos del modelo:

```
DS < -DS[-6,]
regresion02<-lm(rent_1~rent_6_meses + rent_en_el_anio + Sharpe_.3 + Volatilidad_3, DS)
summary(regresion02)
##
## Call:
## lm(formula = rent_1 ~ rent_6_meses + rent_en_el_anio + Sharpe_.3 +
       Volatilidad_3, data = DS)
##
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
## -2.5230 -0.5764 -0.0059 0.5263 3.3260
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   -1.46471
                               0.23782 -6.159 7.12e-09 ***
## rent_6_meses
                   -0.13979
                               0.03189
                                        -4.383 2.26e-05 ***
## rent_en_el_anio 0.88205
                               0.01907 46.253 < 2e-16 ***
                    2.04046
                                         7.550 4.82e-12 ***
## Sharpe_.3
                               0.27027
## Volatilidad_3
                   -0.13424
                               0.02851 -4.709 5.86e-06 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.028 on 142 degrees of freedom
## Multiple R-squared: 0.9639, Adjusted R-squared: 0.9629
## F-statistic: 948.8 on 4 and 142 DF, p-value: < 2.2e-16
# Aunque el modelo no mejora demasiado ya que tan solo hemos eliminado una observacion. Comprobamos de
gvmodel <- gvlma(regresion02)</pre>
summary(gvmodel)
##
## Call:
## lm(formula = rent_1 ~ rent_6_meses + rent_en_el_anio + Sharpe_.3 +
       Volatilidad_3, data = DS)
##
## Residuals:
                10 Median
##
      Min
                                3Q
                                       Max
## -2.5230 -0.5764 -0.0059 0.5263 3.3260
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  -1.46471
                              0.23782 -6.159 7.12e-09 ***
                               0.03189 -4.383 2.26e-05 ***
## rent 6 meses
                   -0.13979
## rent_en_el_anio 0.88205
                              0.01907 46.253 < 2e-16 ***
## Sharpe .3
                   2.04046
                               0.27027
                                       7.550 4.82e-12 ***
                               0.02851 -4.709 5.86e-06 ***
## Volatilidad_3
                  -0.13424
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
\#\# Residual standard error: 1.028 on 142 degrees of freedom
## Multiple R-squared: 0.9639, Adjusted R-squared: 0.9629
## F-statistic: 948.8 on 4 and 142 DF, p-value: < 2.2e-16
##
##
## ASSESSMENT OF THE LINEAR MODEL ASSUMPTIONS
## USING THE GLOBAL TEST ON 4 DEGREES-OF-FREEDOM:
## Level of Significance = 0.05
##
## Call:
  gvlma(x = regresion02)
##
##
                     Value p-value
                                                      Decision
## Global Stat
                     9.726 0.04531 Assumptions NOT satisfied!
## Skewness
                     1.354 0.24455
                                       Assumptions acceptable.
## Kurtosis
                     1.605 0.20519
                                       Assumptions acceptable.
## Link Function
                     2.638 0.10431
                                       Assumptions acceptable.
```

Heteroscedasticity 4.128 0.04217 Assumptions NOT satisfied!

De esta manera sin el outlier se cumple los supuestos de asimetria y kurtosis.

Como penultimo paso comparamos los modelos mediante los criterios AIC y de nuevo BIC:

```
## Warning in AIC.default(regresion01, regresion02): models are not all fitted
## to the same number of observations

## df AIC
## regresion01 15 443.3684
## regresion02 6 432.0759

BIC(regresion01,regresion02)

## Warning in BIC.default(regresion01, regresion02): models are not all fitted
## to the same number of observations

## df BIC
## regresion01 15 488.3266
## regresion02 6 450.0185

## Comprobamos la mejora del modelo 02 con respecto al primero bajo ambos criterios de seleccion.
```

6. Cross Validation:

```
library(ISLR)
set.seed(250)
numData=nrow(DS)
train=sample(numData ,numData/2)

regres.train =lm(rent_1-rent_6_meses + rent_en_el_anio + Sharpe_.3 + Volatilidad_3, DS ,subset =train )
attach(DS)
mean((rent_1-predict(regres.train ,Auto))[-train ]^2)

## Warning: 'newdata' had 392 rows but variables found have 147 rows

## [1] 1.401156

set.seed(251)
regres.train2 =lm(rent_1-rent_6_meses + rent_en_el_anio + Sharpe_.3 + Volatilidad_3, DS ,subset =train mean((rent_1-predict(regres.train2 ,Auto))[-train ]^2)

## Warning: 'newdata' had 392 rows but variables found have 147 rows

## [1] 1.401156
```

Leave-one-out Cross Validation:

```
glm.fit1=glm(rent_1~rent_6_meses + rent_en_el_anio + Sharpe_.3 + Volatilidad_3, DS ,family = gaussian()
coef(glm.fit1)
##
       (Intercept)
                      rent_6_meses rent_en_el_anio
                                                          Sharpe_.3
                        -0.1397874
##
        -1.4647074
                                         0.8820467
                                                          2.0404648
##
     Volatilidad_3
        -0.1342384
##
library (boot)
##
## Attaching package: 'boot'
## The following object is masked from 'package:car':
##
       logit
cv.err =cv.glm(DS,glm.fit1)
cv.err$delta
## [1] 1.144061 1.143608
glm.fit2=glm(rent_1~rent_en_el_anio + Sharpe_.3 + Volatilidad_3, DS ,family = gaussian())
cv.err2 =cv.glm(DS,glm.fit2)
cv.err2$delta
## [1] 1.261463 1.261096
```

K-Fold Cross-Validation:

```
library (boot)
cv.err =cv.glm(DS,glm.fit1,K=10)
cv.err$delta

## [1] 1.167098 1.158525

glm.fit2=glm(rent_1~rent_en_el_anio + Sharpe_.3 + Volatilidad_3, DS ,family = gaussian())
cv.err2 =cv.glm(DS,glm.fit2,K=10)
cv.err2$delta

## [1] 1.283470 1.276506
```