

Problem Set 04

Assignement 1.1

Slowest

- $\log_4 n$
- $40 \log_2 n$
- $k \log_2 n$
- $n \log_2 n$
- $5 n^2$
- $12 n^6$
- 4^n

Fastest

Assignement 1.2

- a) $O(n^2)$
- b) $O(n)$
- c) $O(n \cdot \log(n))$
- d) $O(n^2)$
- e) $O(2^n)$
- f) $O(n^2)$
- g) $O(n \cdot \log(n))$

Assignement 1.3

1)

```
def printCalendar(self):
    print(f'{self.monthName()} {self.year()}\nSu\tMo\tTu\tWe\tTh\tFr\tSa')

    dateArray = []
    spaces = [1, 2, 3, 4, 5, 6, 0]

    startingDate = Date(self.month(), 1, self.year())

    for i in range(spaces[startingDate.dayOfWeek()]):
        dateArray.append(' ')

    while self.month() == startingDate.month():
        dateArray.append(startingDate.day())
        startingDate.advanceBy(1)

    for index, e in enumerate(dateArray):
        print(f'{e}\t', end='')
        if index % 7 == 6:
            print()
```

Lines : 7

First for : n

First while : $2n$

Second for : $2n * 3 = 6n$

$T(n) = 9n + 12$

Complexity order: $O(n)$

2)

```
# Check if a given set is a proper subset of another set
def is_proper_subset(self, setB):
    if self.isSubsetOf(setB):
        if not self.__eq__(setB):
            return True

    return False
```

$$T(n) = n * n + 2$$

Complexity order: $O(n^2)$

3)

```
# Removes an element from the set.
def remove(self, element):
    assert element in self, "The element must be in the set."
    self._theElements.remove(element)
```

In the worst case scenario we have to go through all n elements, and compare every element, then remove it if it's the case. So n to iterate, n to compare and 1 extra to delete the element.

$$T(n) = n + n + 1$$

Complexity order: $O(n)$

```
# Adds a new unique element to the set.
def add(self, element):
    if element not in self:
        self._theElements.append(element)
```

In the worst case scenario we need to add an element at the start of list, making n iterations to shift every other element. So 1 to add it and n to iterate the shifts.

$$T(n) = n + 1$$

Complexity order: $O(n)$

Assignement 1.4

	Best	Worst
a)	$O(n)$	$O(n)$
b)	$O(n)$	$O(\log_2 n)$
c)	$O(n)$	$O(n^2)$

Assignment 1.5

```
def my_slice(input_list, first, last):  
    new_list = []  
    for element in range(first, last):  
        new_list.append(input_list[element])  
    return new_list
```

In the best case the algorithm needs n for the for loop plus 2 extra lines. In the worst case it's the same.

Complexity for both worst and best: $O(n)$