

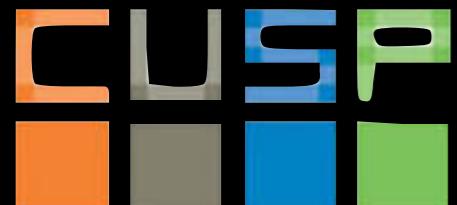
Urban Informatics

Fall 2018

dr. federica bianco fbianco@nyu.edu

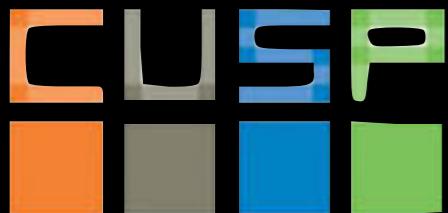


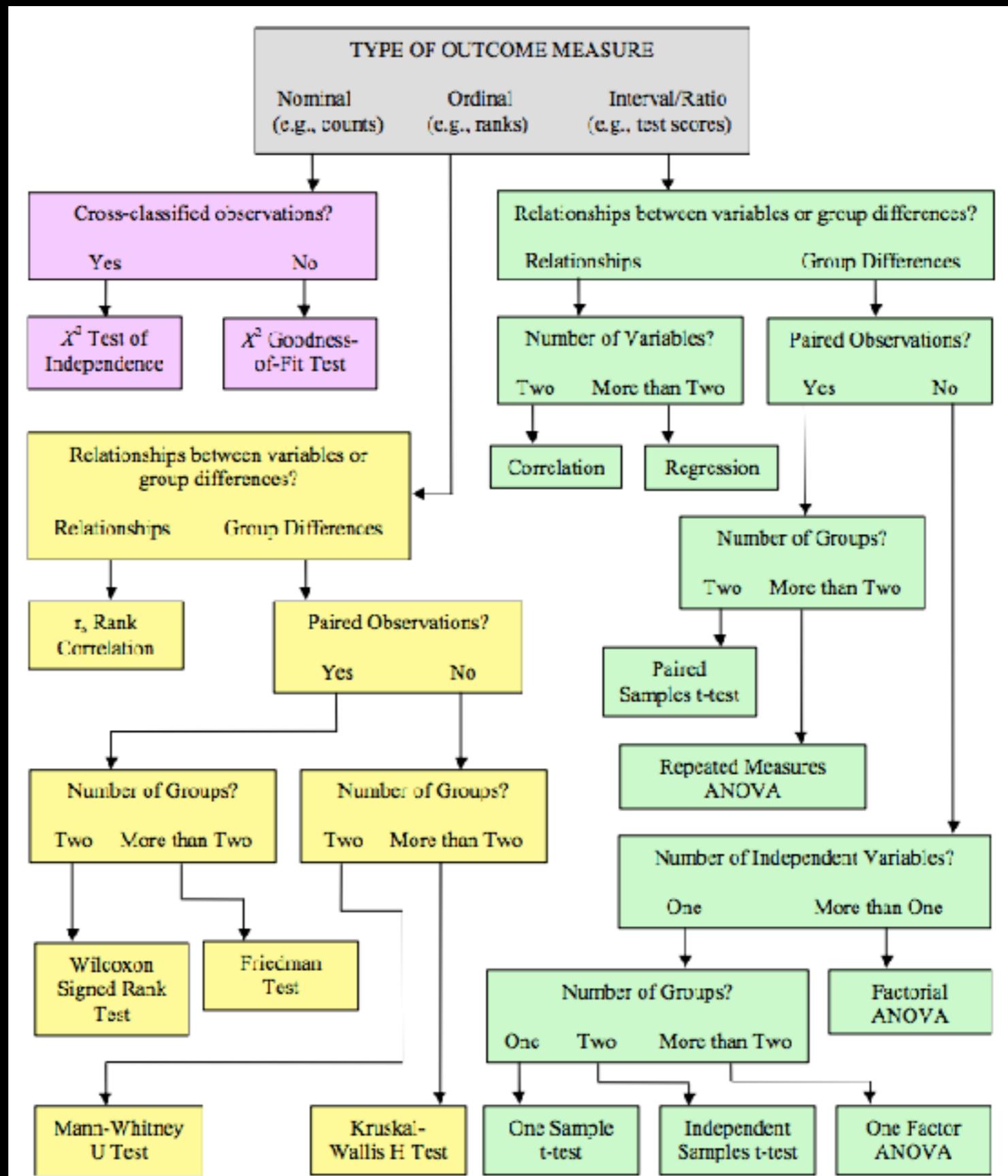
@fedhere



Recap:

- Good practices with data: falsifiability, reproducibility
- Basic data retrieving and munging: APIs, Data formats
- Basic statistics: distributions and their moments
- Hypothesis testing: p -value, statistical significance



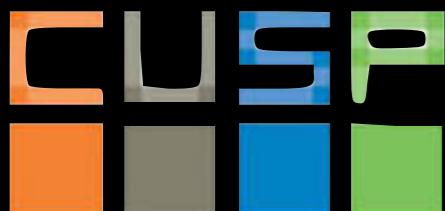


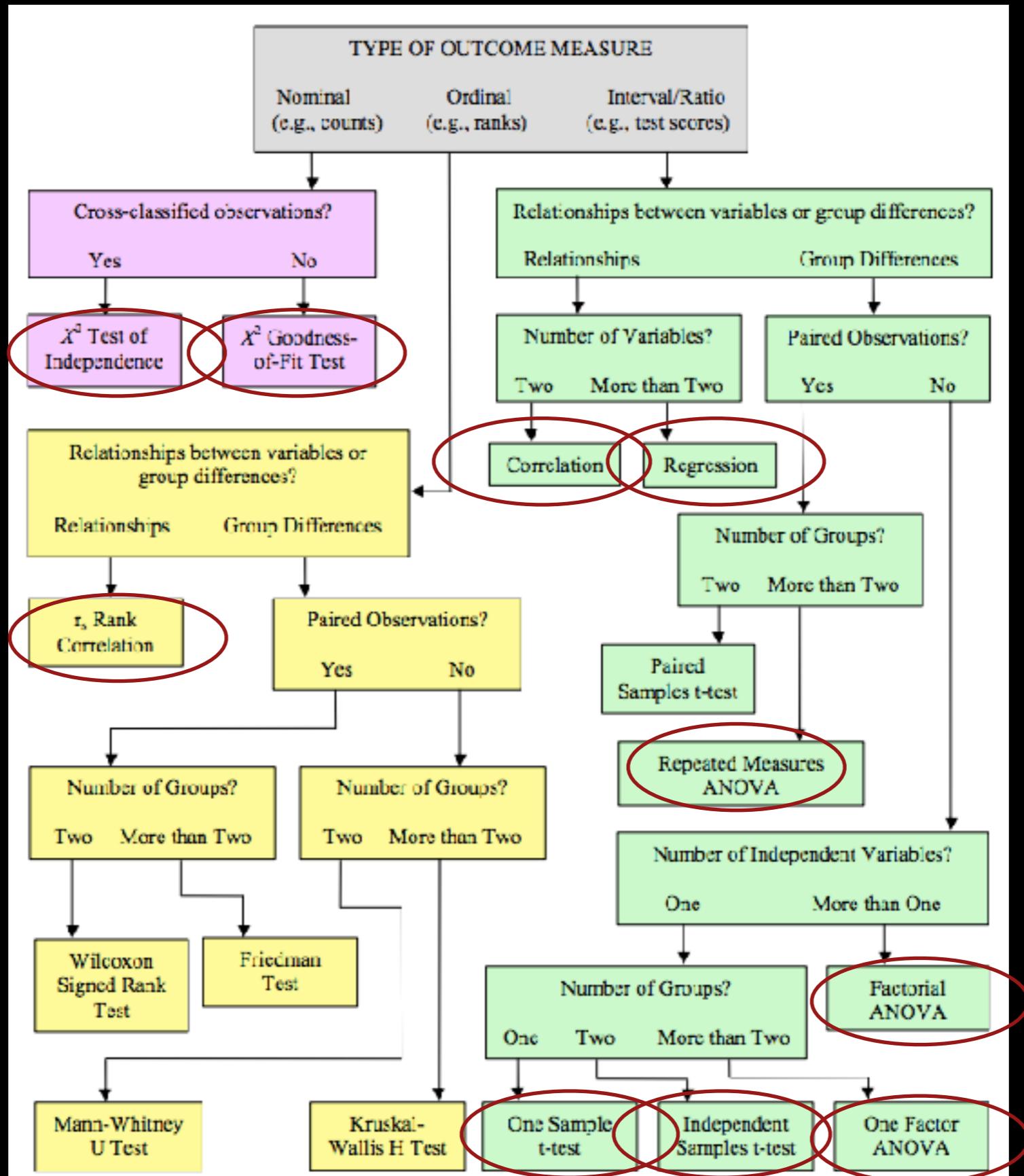
Recap:

- Good practices with data: falsifiability, reproducibility
- Basic data retrieving and munging: APIs, Data formats
- Basic statistics: distributions and their moments
- Hypothesis testing: p -value, statistical significance

Today:

- Statistical and Systematic errors
- Goodness of fit tests



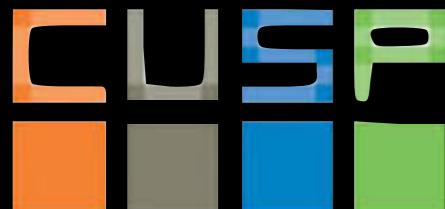


hypothesis testing

did we detect a phenomenon?

null hypothesis: no relationship between two measured phenomena,
or no difference among groups
if you have a test control sample: test sample and
control sample are the same - no effect

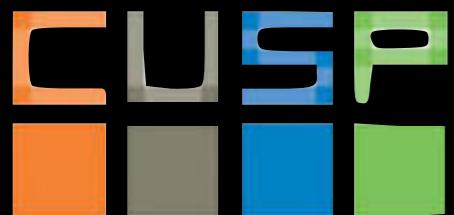
falsify the null hypothesis: do you see an effect?
do you see a difference b/w samples?



A simple (too simple?) answer

did we detect a phenomenon?

p-value a measure of the probability that the result you observed could have been observed by chance under the *Null hypothesis*

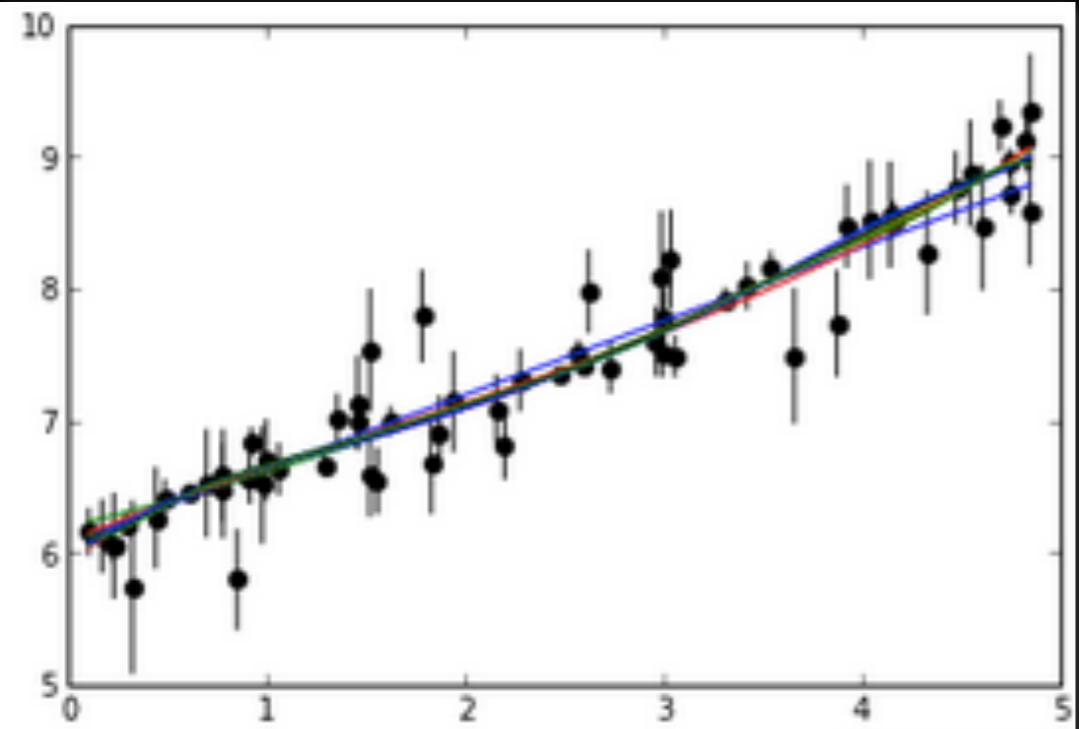


Effect size in place of test statistics

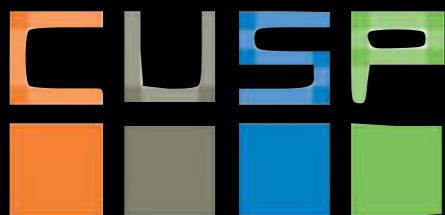
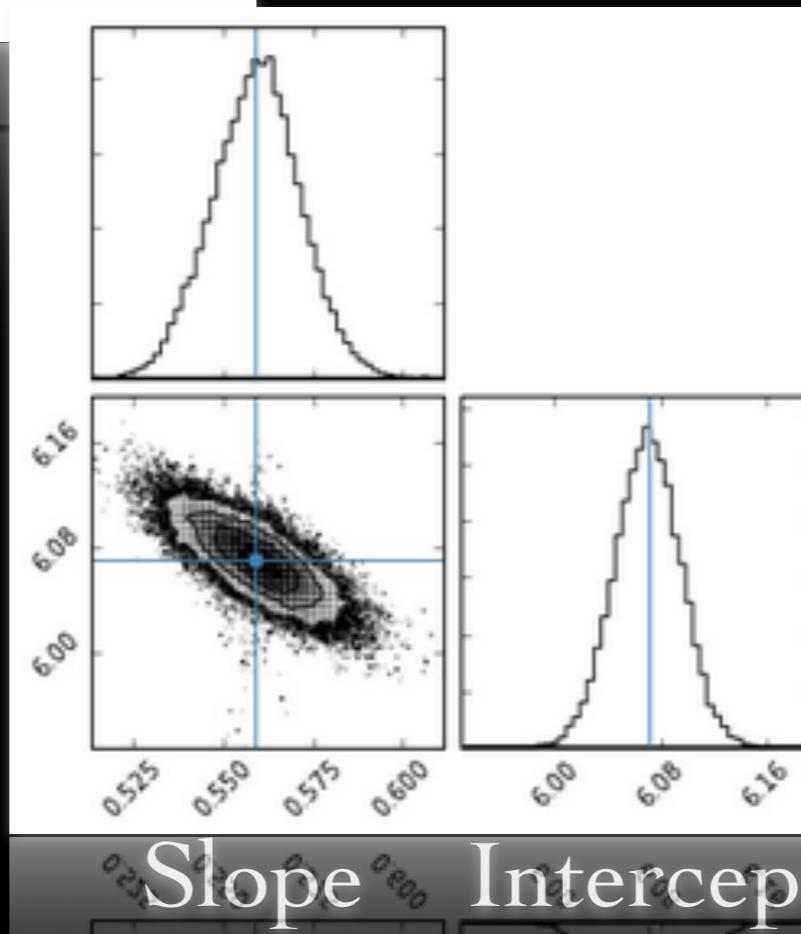
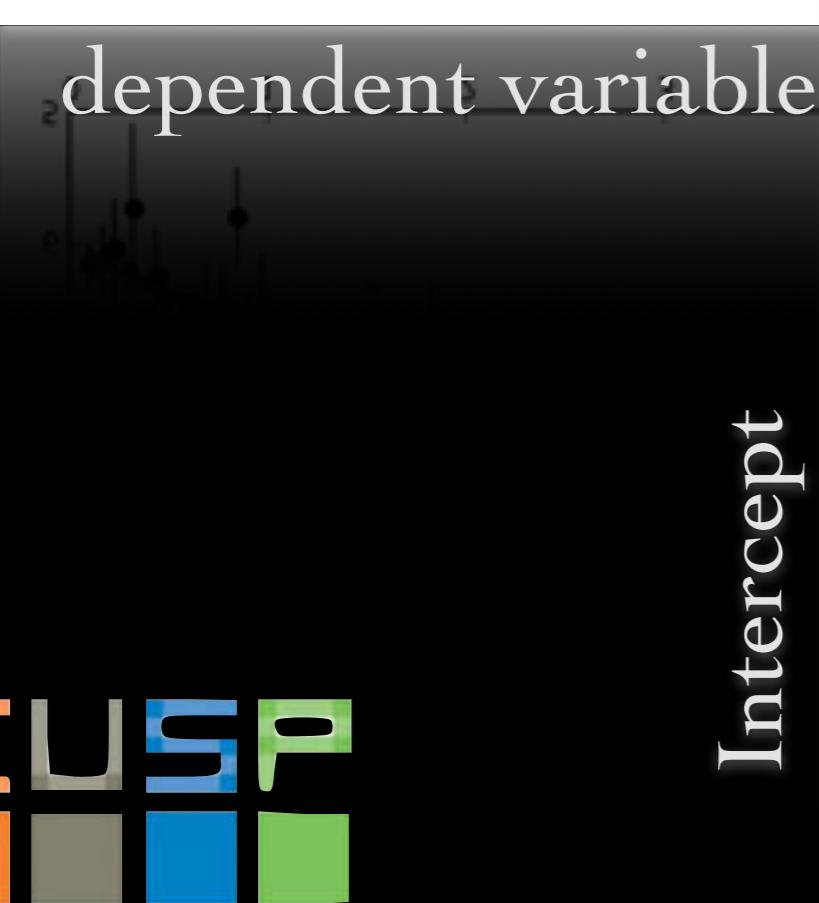
Estimate the strength of, for example, an apparent relationship, rather than assigning a significance level. The effect size does not directly determine the significance level, or vice versa.

A more complex and complete answer...

independent variable

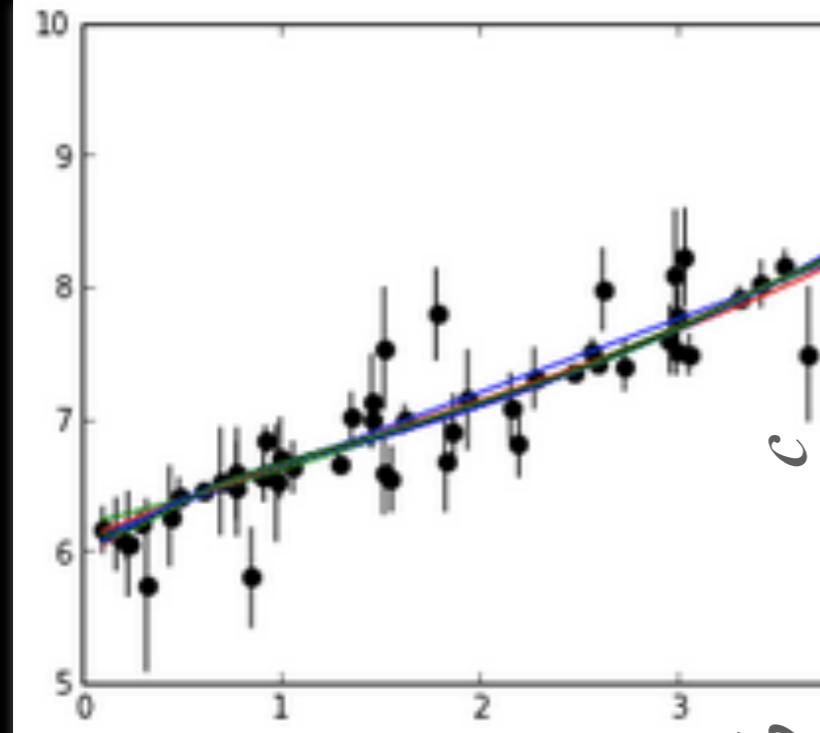


$$y = m + ax$$

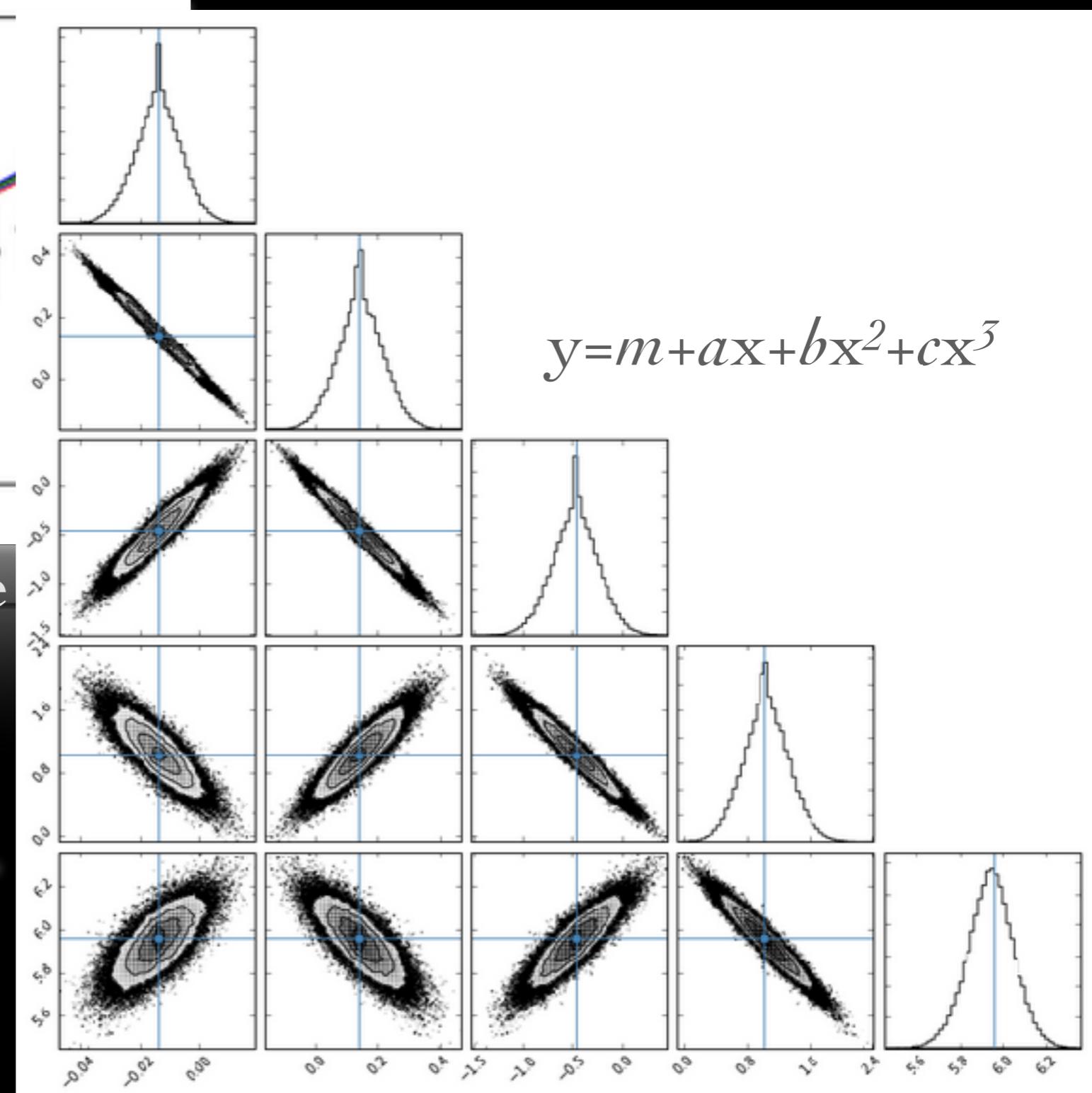


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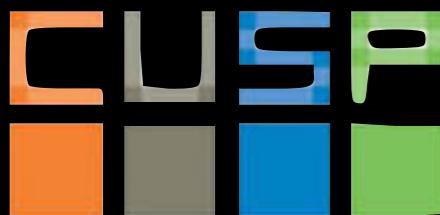
independent variable



dependent variable
 b

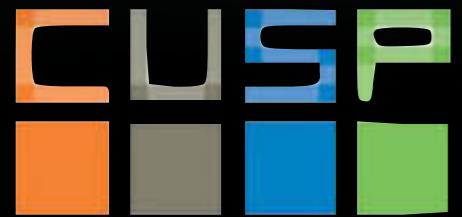


$$y = m + ax + bx^2 + cx^3$$





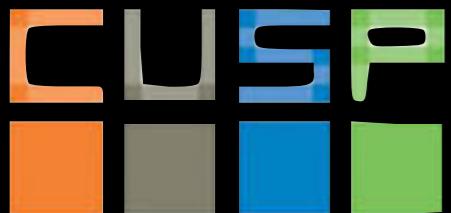
Errors and uncertainties.



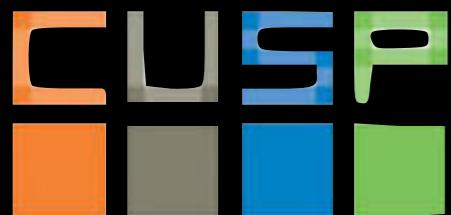
IV: Statistical analysis

Errors and uncertainties.

- Systematic error
- Statistical error (Stochastic & Random)



systematic errors



Errors and uncertainties.

- Systematic error

tendency to systematically underestimate/overestimate the average
difference between the *population* and the subset you test or *sample* because the sample is intrinsically different or the measurements are consistently off



HEALTHY ENVIRONMENT

EMERGENCY PREPAREDNESS

DATA & STATISTICS

Surveys

Tools

Your Neighborhood

Health Data Publications

HEALTH CARE PROVIDERS

INFORMATION FOR:

Licenses and Permits

Press

Public Testimony

Vendors and Contractors

Hurricane Sandy Health

9/11 Health

HEALTH DEPARTMENT:

About Us

Take Care New York

Board of Health/Health Code

Public Meetings Archive

Official Notices

Publications

Career Opportunities

Citizen Observatory

Seaport District

Healthcare Quality

Bureau of Health Statistics

Office of Health Information

Healthcare

Physical Activity and Transit Survey

Physical Activity and Transit Survey: Methodology

[Target Population](#) | [Health Topics](#) | [Sampling](#) | [Limitations](#) | [Sample Size, Response and Cooperation Rates](#) | [Data Analysis](#)

The Physical Activity and Transit (PAT) survey was conducted in 2010 and 2011 by the New York City Department of Health and Mental Hygiene. Data were collected to measure the level and context of physical activity in New York City and to improve understanding of what motivates individuals to be physically active including opportunities for activity, perceptions of safety and security, and other neighborhood factors. For more information on the PAT, please visit:

- [PAT Overview](#)
- [PAT Device Methodology](#)
- [PAT Public Use Datasets](#)

TARGET POPULATION

The target population of the PAT was adults aged 18 and older who were able to walk more than 10 feet and who lived in one of the five boroughs of New York City. Of the 3908 adults who completed the initial telephone screener, 3811 were mobile and completed the full survey.

HEALTH TOPICS

The PAT asked approximately 125 questions, covering the following: a modified version of the Global Health and Physical Activity Questionnaire (GPAQ) designed by the World Health Organization on physical activity in the work, recreation and transportation domains. Also included were questions on chronic disease, diet, alcohol and tobacco, neighborhood conditions, and mental health. The survey also asked a multiple demographic variables to facilitate weighting and comparisons among different groups of New Yorkers.

SAMPLING

The PAT was conducted using a fully overlapping dual frame design, using randomly generated landline and cellular telephone samples. (Roughly 25% were completed on a cell phone.) To provide equal statistical power for borough-level comparisons, a similar number of participants were interviewed in each borough of New York (Bronx, Brooklyn, Manhattan, Queens and Staten Island). All data were then weighted to adjust for the probability of selection and differential nonresponse and sum to Census estimates of the number of people living in each borough.

Interviewing was done by Abt-SRBI, a survey research company based in New York City. Interviews were conducted in English, Spanish, Russian and Chinese (Cantonese and Mandarin). Data collection for wave 1 occurred in September – November of 2010; wave 2 was conducted in March – November of 2011. The average length of the survey was 35 minutes.

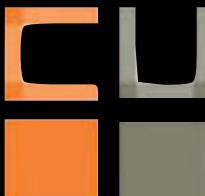
[back to top](#)

LIMITATIONS

The sampling methodology did not capture adults who could not be reached by either landline or cellular telephone. The PAT also excluded adults living in institutional group housing, such as incarcerated persons or those living in college dormitories.

[back to top](#)

<http://www.nyc.gov/html/doh/html/data/pat-methods.shtml#4>



Errors and uncertainties.



Errors and uncertainties.



Errors and uncertainties.



projection induces a *systematic underestimation*

Bias in measurements: know your data

- Systematic error: SURVEY BIAS

UNBIASED survey:
average from *all* samples
equals *population* average

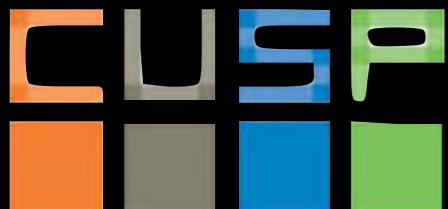
different surveys/experiments give different results
because they have different systematic errors or bias

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Undercoverage bias



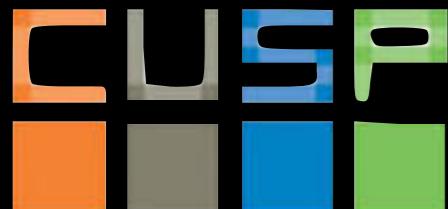
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Undercoverage bias

the surveyed segment of the population is lower in a sample than it is in the population. This can happen because the frame used to obtain the sample is incomplete or not representative of the population.

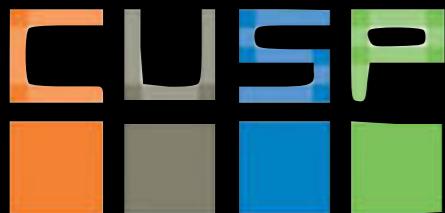


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Self selection bias



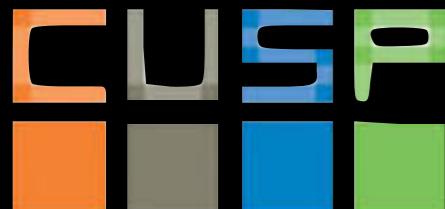
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Self selection bias

higher test scores observed among students who participate in a test preparation courses, but due to self-selection, people who choose to take the course may be more motivated, have more support...



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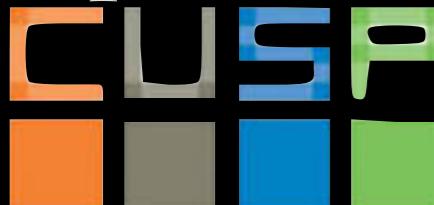
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people willing to answer a survey about climate are likely more concerned and responsible citizens



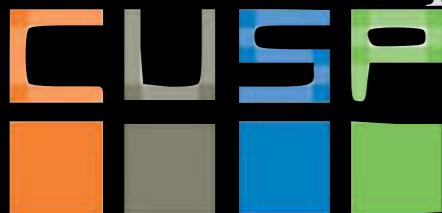
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Social desirability bias

tendency of survey respondents to answer questions in a manner that will be viewed favorably: over-reporting "good behavior" or under-reporting undesirable behavior (e.g. drug+alcohol use).



Bias in measurements: know your data

Random and Systematic Error Effects of Insomnia on Survey Behavior

**Larissa K. Barber¹, Christopher M. Barnes²,
and Kevin D. Carlson²**

Organizational Research Methods
00(0) 1-34
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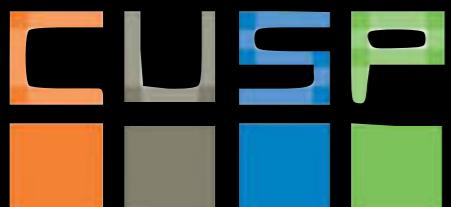


Abstract

Insomnia is a prevalent experience among employees and survey respondents. Drawing from research on sleep and self-regulation, we examine both random (survey errors) and systematic (social desirability) effects of research participant insomnia on survey responses. With respect to random effects, we find that insomnia leads to increased survey errors, and that this effect is mediated by a lack of self-control and a lack of effort. However, insomnia also has a positive systematic effect, leading to lower levels of social desirability. This effect is also mediated by self-control depletion and a lack of

http://www.researchgate.net/publication/244478619_Random_and_Systematic_Error_Effects_of_Insomnia_on_Survey_Behavior

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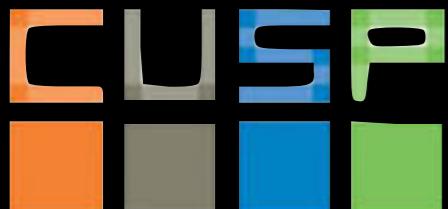
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UNBIASED survey:
average from *all* samples
equals *population* average

Undercoverage bias
Self selection bias
Social desirability bias

Other systematic errors
Publication Bias
Data Dredging



Bias in measurements: know your data

- Systematic error: PUBLICATION BIAS

The screenshot shows a news article from the journal 'nature'. The header features the word 'nature' in large white letters on a dark red background, with the subtitle 'International weekly journal of science' below it. A navigation bar includes links for Home, News & Comment, Research, Careers & Jobs, Current Issue, Archive, Audio & Video, and a search icon. Below the navigation is a breadcrumb trail: News & Comment > News > 2015 > August > Article. The main content area has a light gray background. On the left, 'NATURE | NEWS' is written in a small font. On the right, there are sharing icons for social media. The main headline reads 'Social sciences suffer from severe publication bias'. Below the headline is a sub-headline: 'Survey finds that 'null results' rarely see the light of the day.' The author's name, 'Mark Peplow', is listed, along with the date '28 August 2014'. The title of the article is 'Publication Bias'. At the bottom of the page, there is a logo for 'CUSP' with four colored squares (orange, blue, gray, green) and some smaller text.

nature International weekly journal of science

Home | News & Comment | Research | Careers & Jobs | Current Issue | Archive | Audio & Video | F

News & Comment > News > 2015 > August > Article

NATURE | NEWS

Social sciences suffer from severe publication bias

Survey finds that 'null results' rarely see the light of the day.

Mark Peplow

28 August 2014

Publication Bias

CUSP

IV: Statistical analysis

Bias in measurements: know your data

- Systematic error: PUBLICATION BIAS

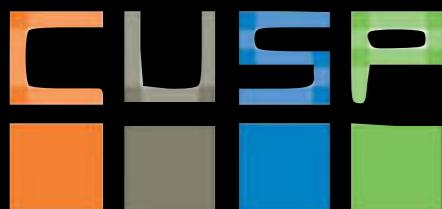
His team investigated the fate of 221 sociological studies conducted between 2002 and 2012, which were recorded by Time-sharing Experiments for the Social Sciences (TESS), a US project that helps social scientists to carry out large-scale surveys of people's views.

Only 48% of the completed studies had been published. So the team contacted the remaining authors to find out whether they had written up their results, or submitted them to a journal or conference. They also asked whether the results supported the researchers' original hypothesis.

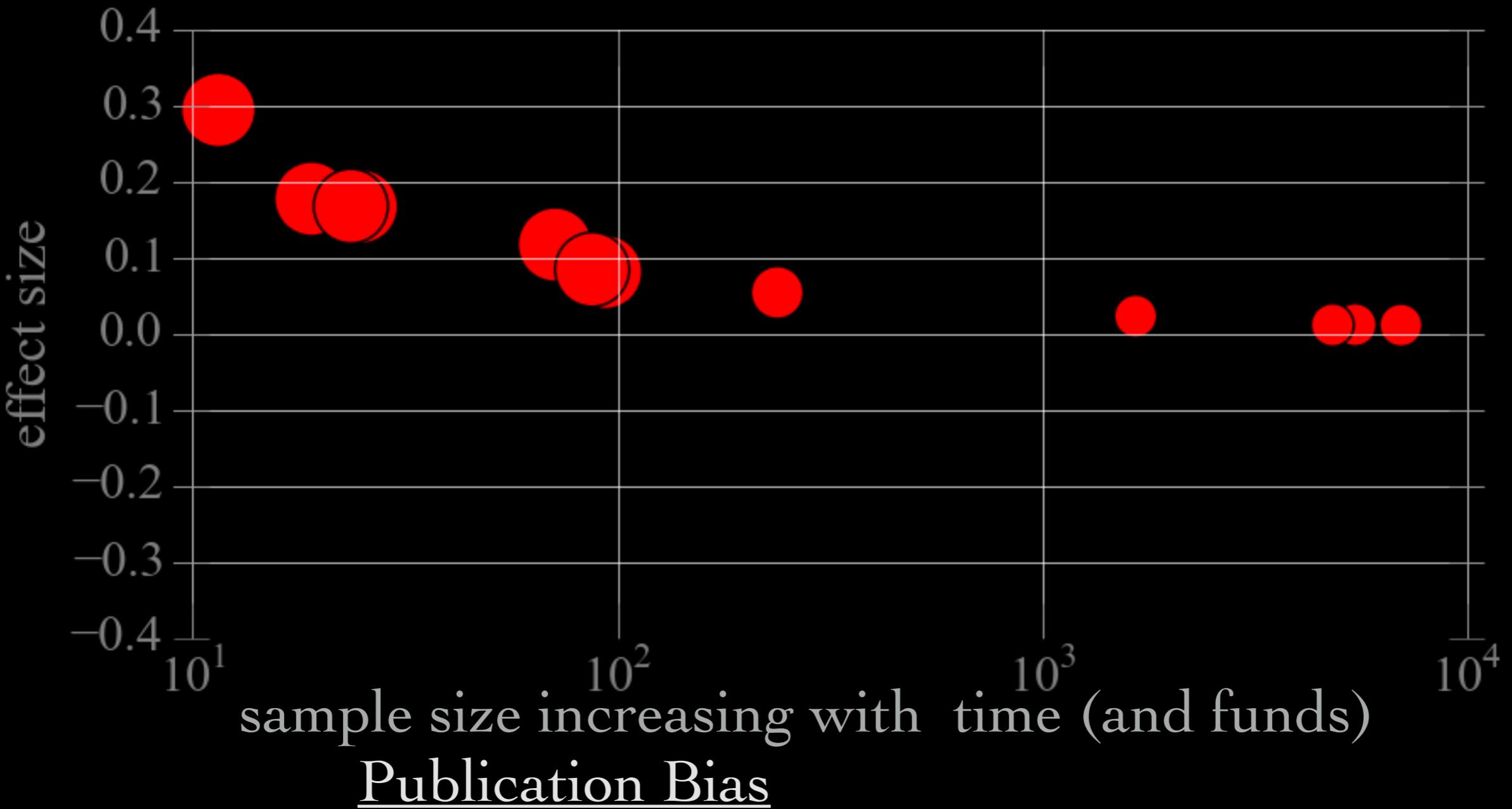
Of all the null studies, just 20% had appeared in a journal, and 65% had not even been written up.

By contrast, roughly 60% of studies with strong results had been published. Many of the researchers contacted by Malhotra's team said that they had not written up their null results because they thought that journals would not publish them, or that the findings were neither interesting nor important enough to warrant any further effort.

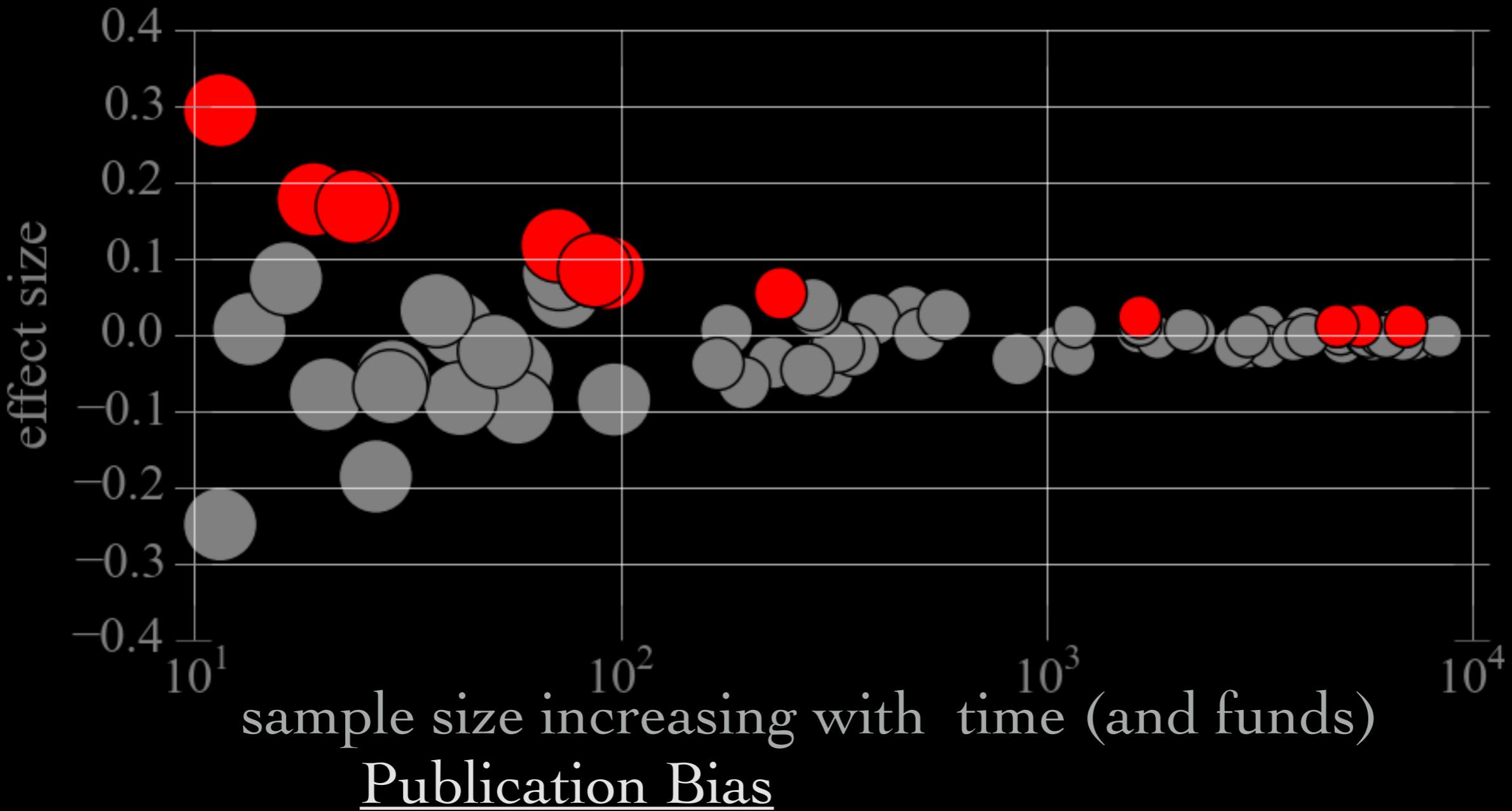
Publication Bias



Bias in measurements: know your data



Bias in measurements: know your data



Bias in measurements: know your data

- Systematic error: PUBLICATION BIAS



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Publication Bias in Measuring Climate Sensitivity

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Dominika Rečková and Zuzana Iršová (zuzana.irsova@ies-prague.org)

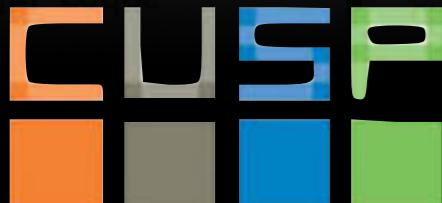
No 2015/14, [Working Papers IES](#) from [Charles University Prague, Faculty of Social Sciences, Institute of Economic Studies](#)

Abstract: We present a meta-regression analysis of the relation between the concentration of carbon dioxide in the atmosphere and changes in global temperature. The relation is captured by "climate sensitivity", which measures the response to a doubling of carbon dioxide concentrations compared to pre-industrial levels. Estimates of climate sensitivity play a crucial role in evaluating the impacts of climate change and constitute one of the most important inputs into the computation of the social cost of carbon, which reflects the socially optimal value of a carbon tax. Climate sensitivity has been estimated by many researchers, but their results vary significantly. We collect 48 estimates from 16 studies and analyze the literature quantitatively. We find evidence for publication selection bias: researchers tend to report preferentially large estimates of climate sensitivity. Corrected for publication bias, the bulk of the literature is consistent with climate sensitivity lying between 1.4 and 2.3C.

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Publication Bias

<http://ies.fsv.cuni.cz/default/file/download/id/28421>



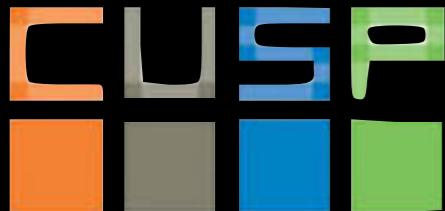
Bias in measurements: know your data

- Systematic error:

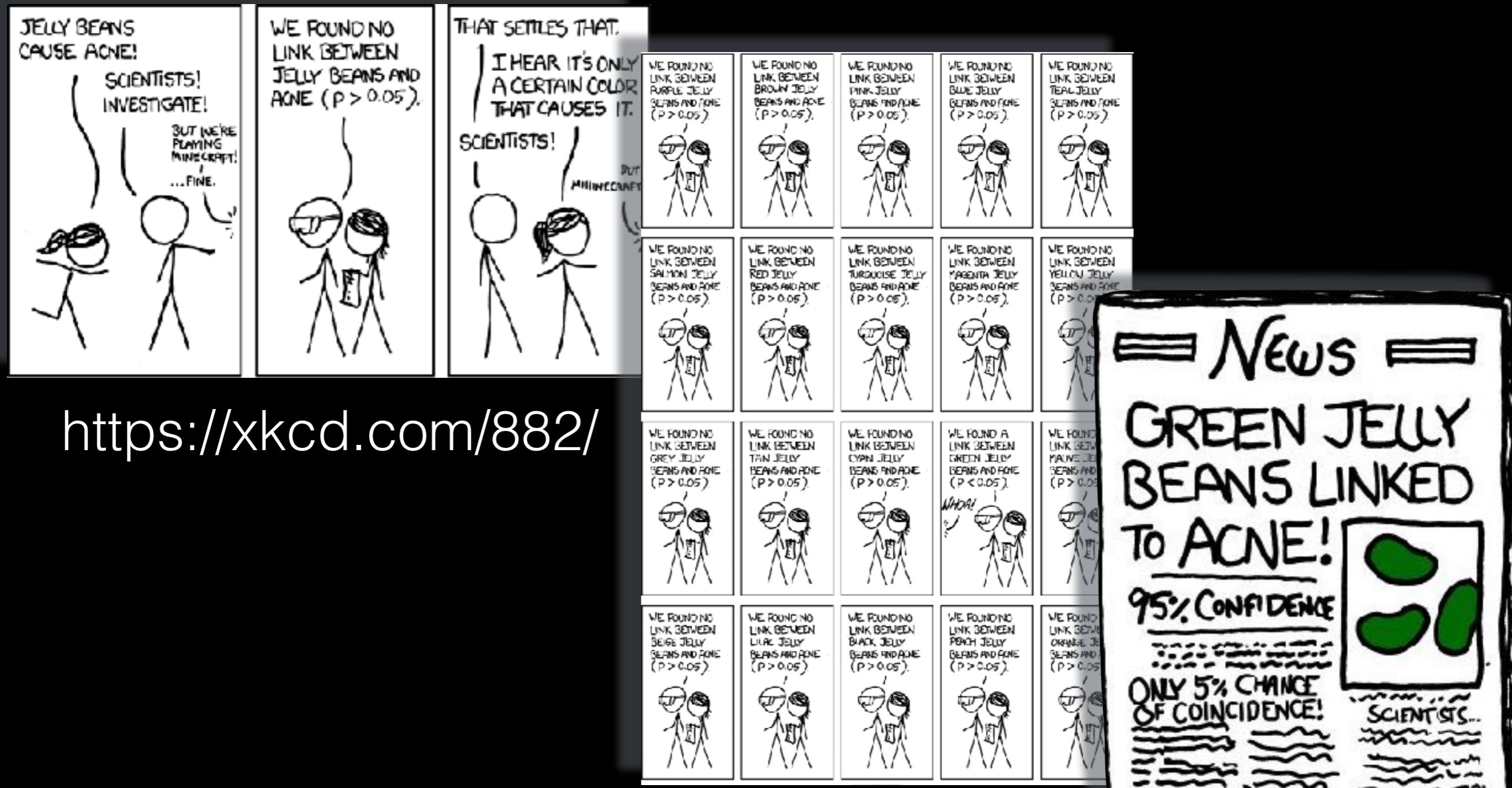
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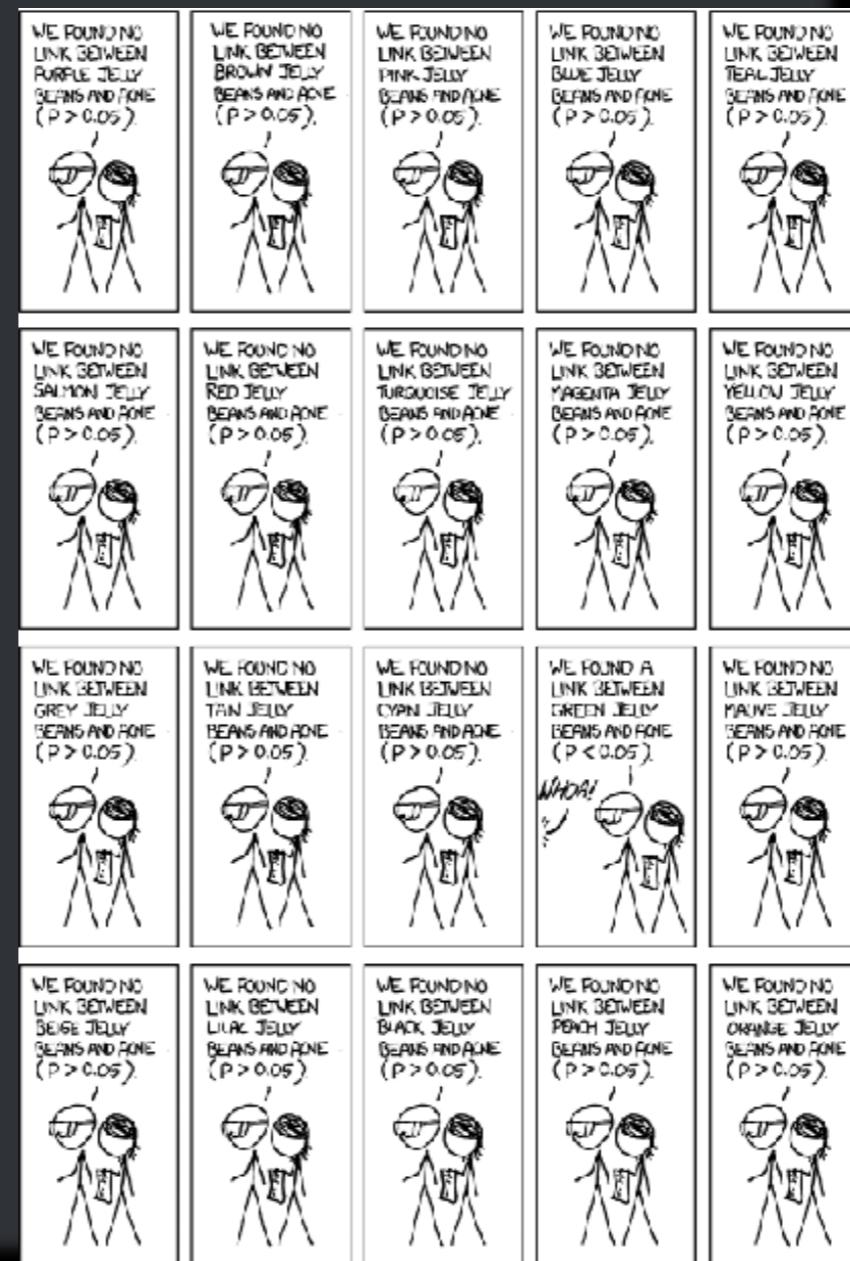
Bias in measurements: know your data



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each test has a probability $p \leq 0.05$ of Type I error significance 95%

20 tests are preformed



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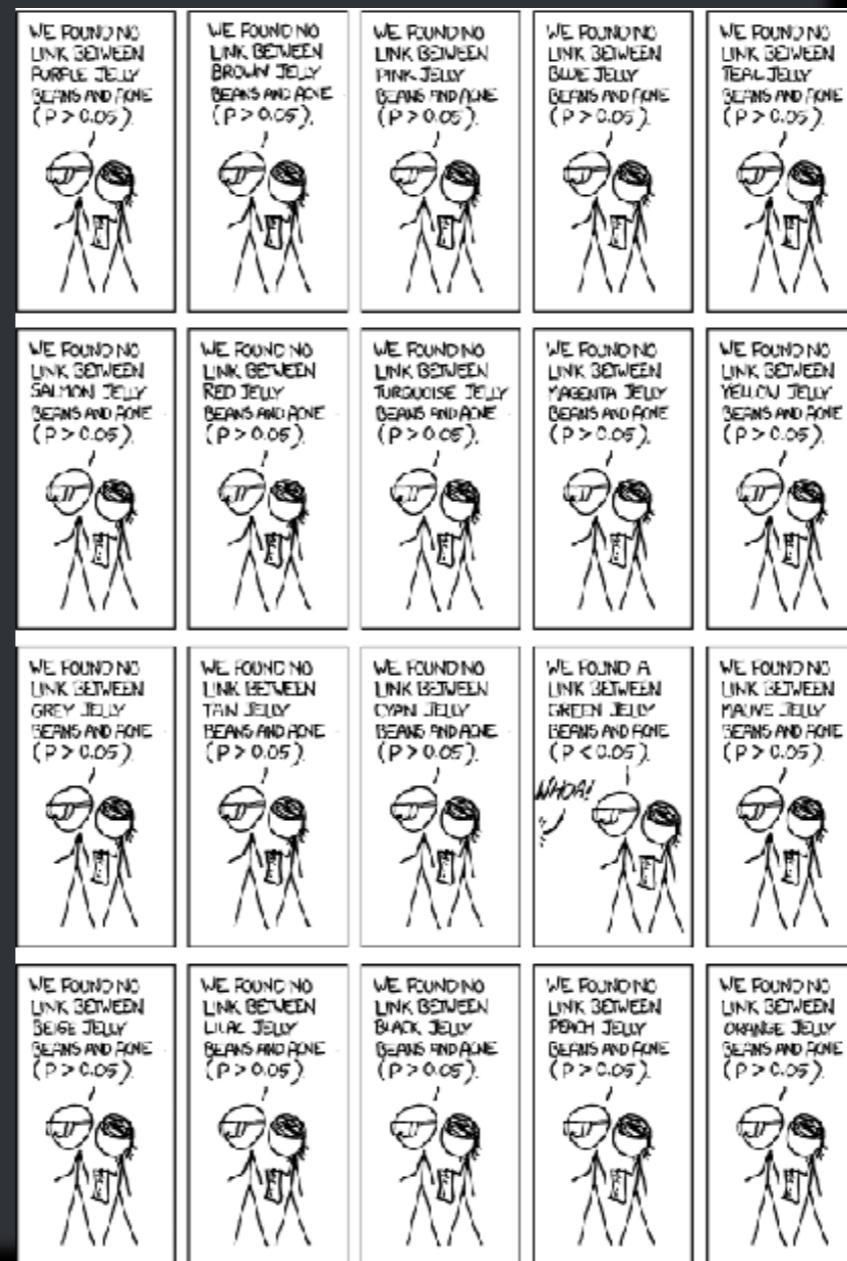
20 tests are preformed

assume independence:
if $\rho_i = 0.05$ for each $i=1..20$

total significance=

$$1 - (1 - 0.05)^{20}$$

$$\rho_{\text{tot}} = (1 - 0.05)^{20}$$



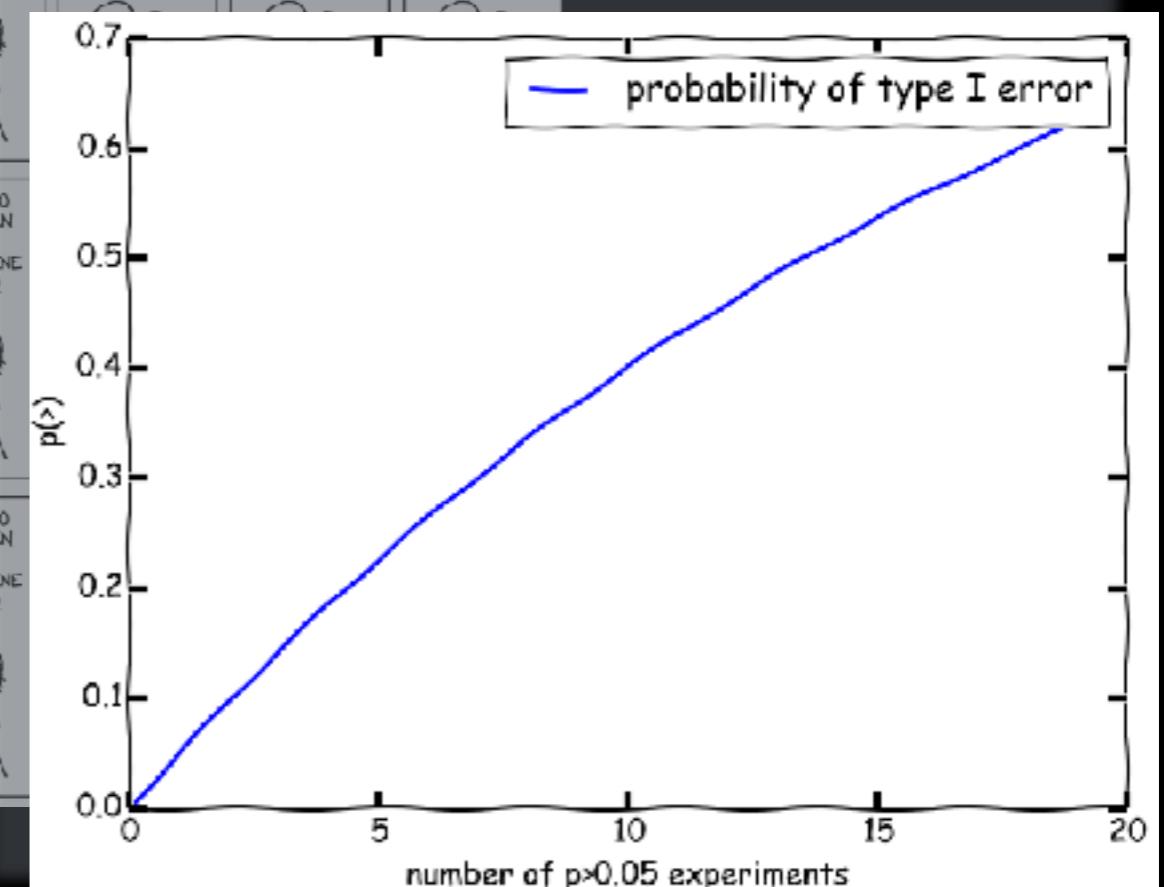
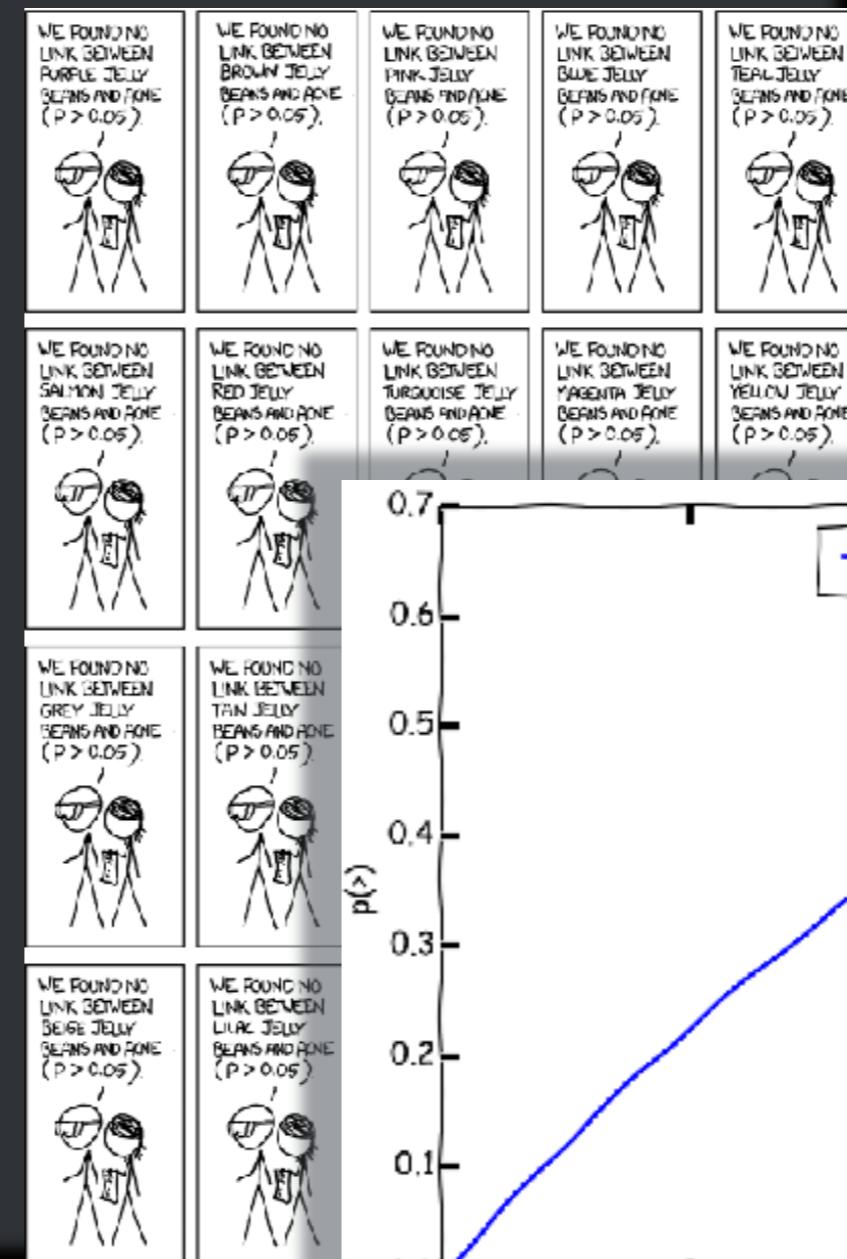
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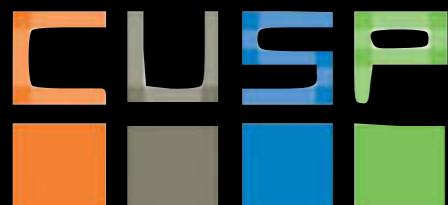
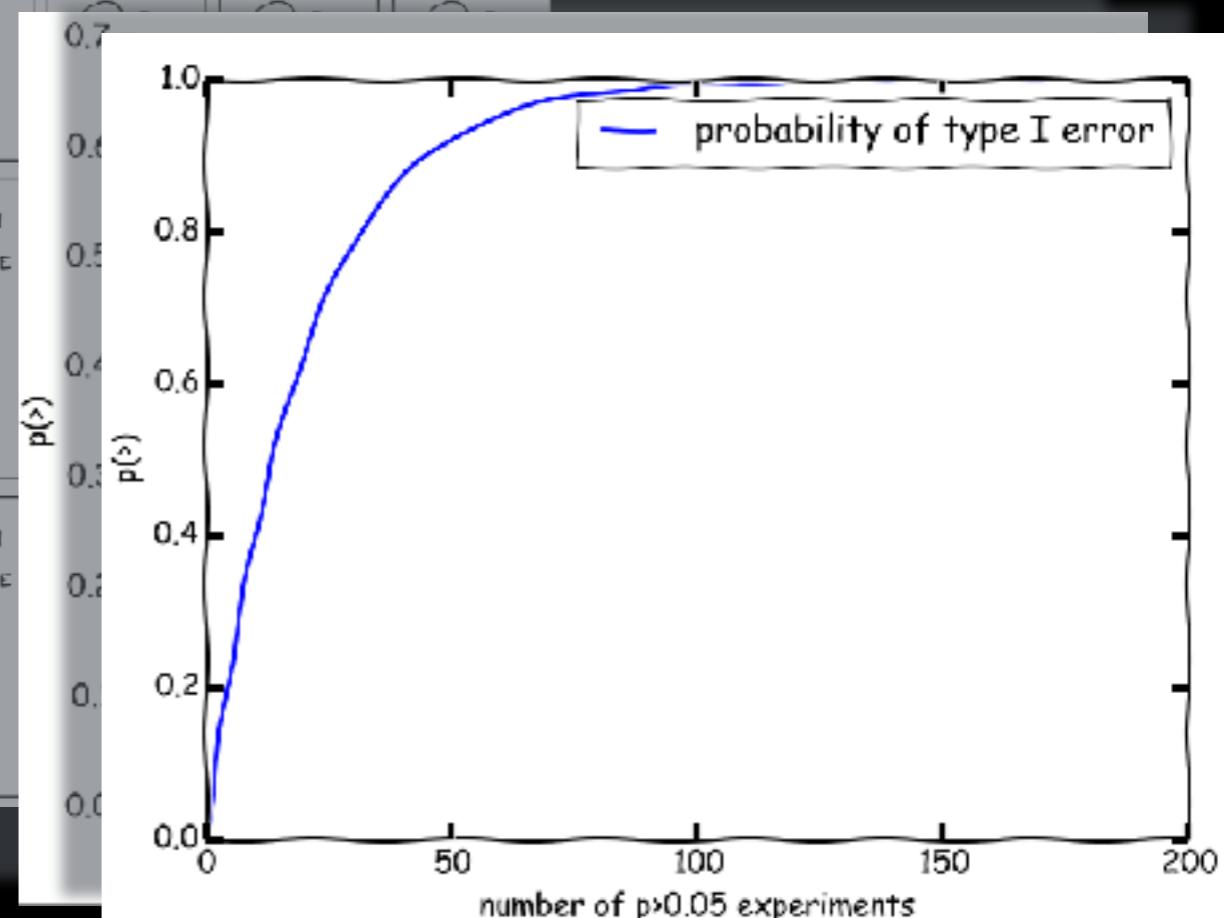
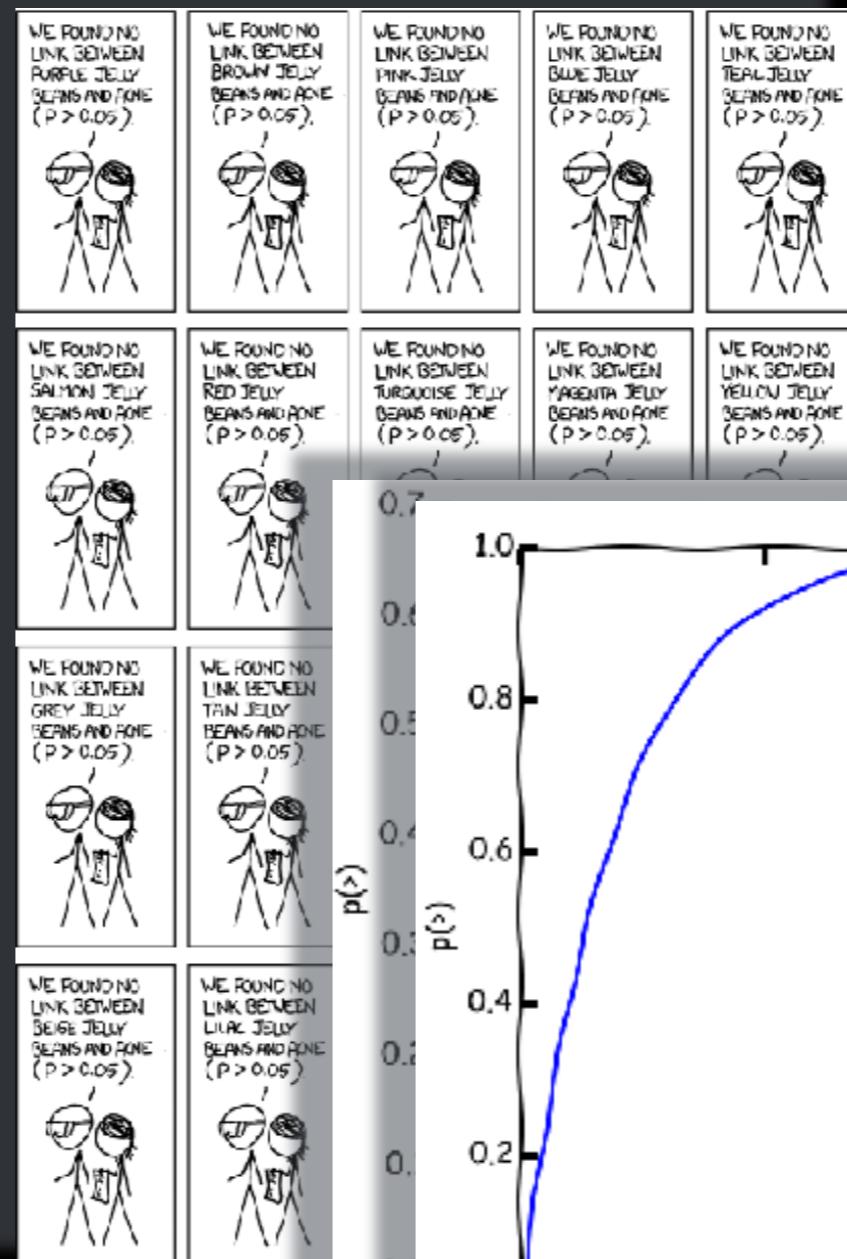
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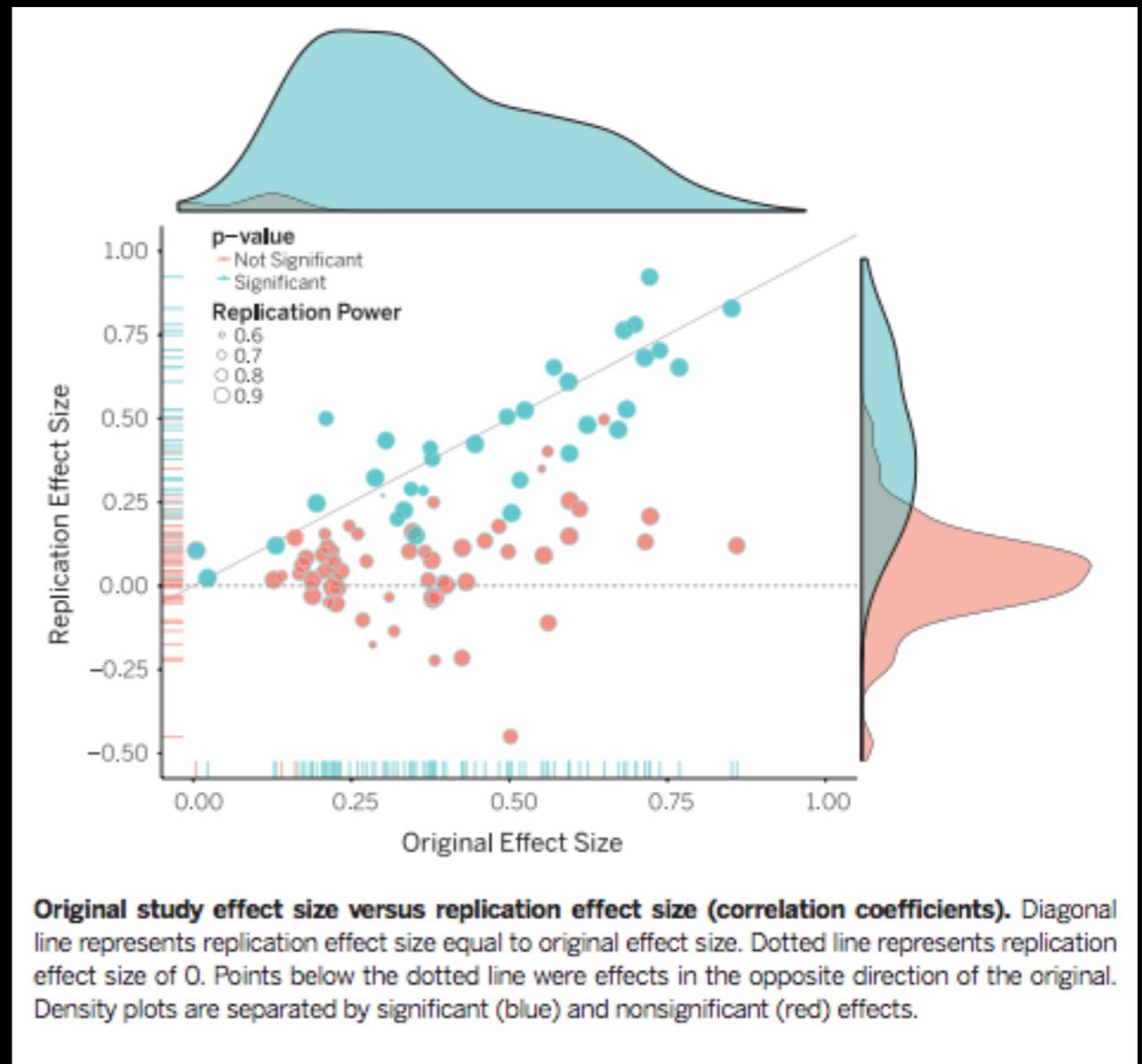


Data Dredging

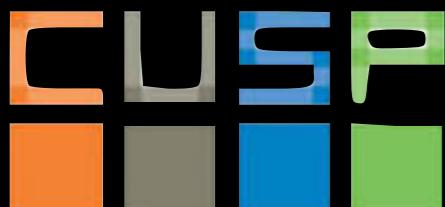
Systematic errors, biases, and reproducibility



Science,
August 28, 2015



<http://www.sciencemag.org/content/349/6251/aac4716.full.pdf>



IV: Statistical analysis

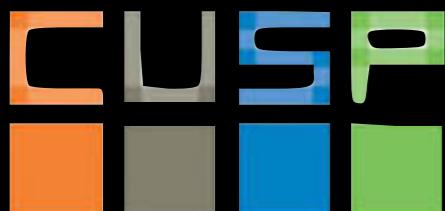
Errors and uncertainties.

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 - tendency to systematically underestimate/overestimate the average
difference between the *population* and the subset you test or *sample* because the sample is intrinsically different or the measurements are consistently off

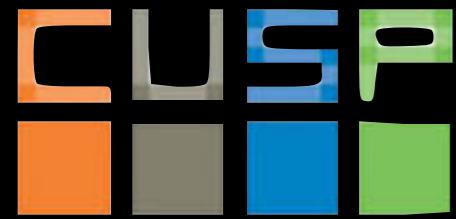
Solution: Good experimental design

Calibration (to assess systematics induced by your measurements)

Simulations (to assess the systematics induced by your analysis)



statistical errors



Errors and uncertainties.

- Systematic error
- Stochastic & Random error
 - unpredictable uncertainty in a measurement due to lack of sensitivity in the measurement or to stochasticity in a process

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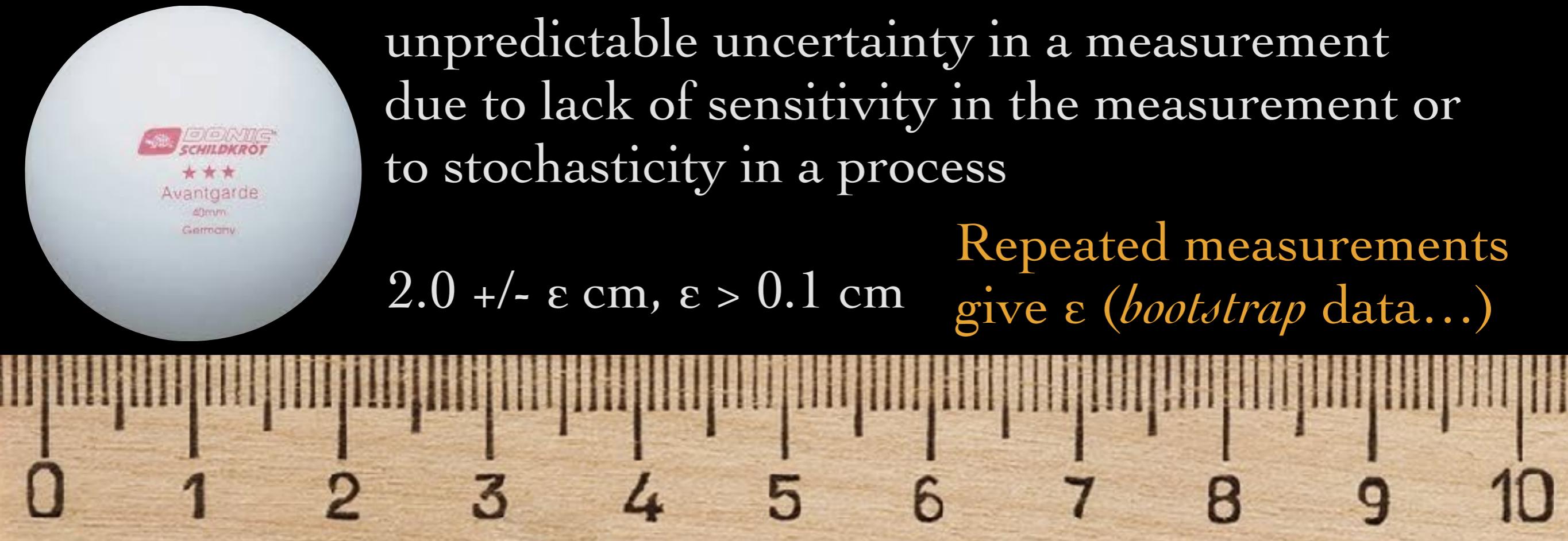
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unpredictable uncertainty in a measurement
due to lack of sensitivity in the measurement or
to stochasticity in a process

$$2.0 \pm \varepsilon \text{ cm}, \varepsilon > 0.1 \text{ cm}$$

Repeated measurements
give ε (*bootstrap* data...)



Errors and uncertainties.

- Systematic error
- Stochastic & Random error

Deterministic systems have no randomness in their evolution. *Chaos* is deterministic....

Stochastic processes can be *completely random*: the probability of any event is disjoint from that of the previous one
These are Poisson processes:

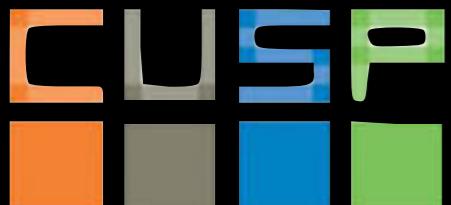
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These are **Poisson processes**: they are described by a Poisson distribution.

A discrete distribution that expresses the probability of a number of events occurring in a fixed period of time if these events occur with a known average rate and independently of the time since the last event.

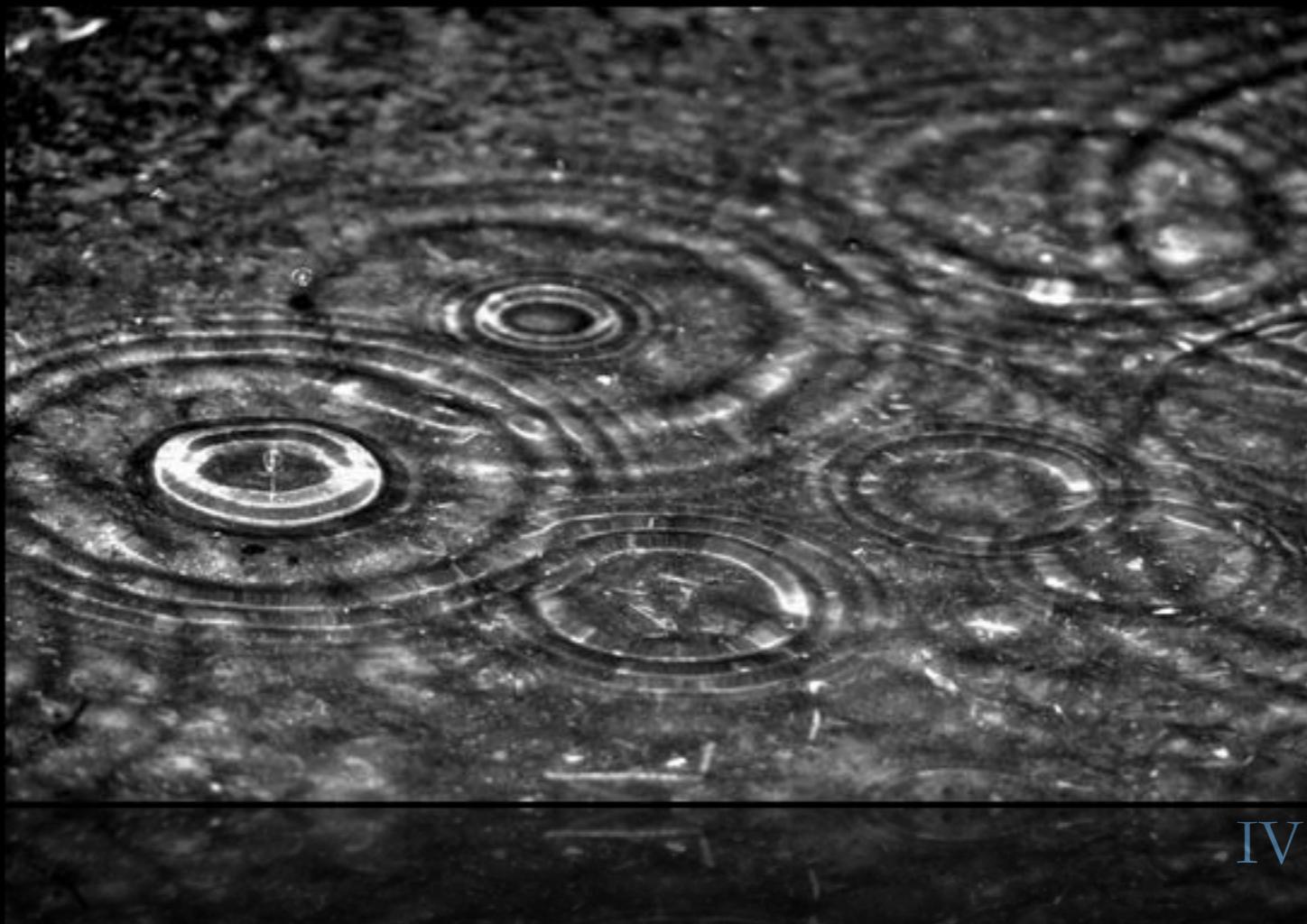


Errors and uncertainties.

- Systematic error
- Stochastic & Random error

Poisson processes :

<https://github.com/fedhere/UInotebooks/blob/master/poisson%20vs%20gaussian.ipynb>



Errors and uncertainties.

- Systematic error
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for large enough λ
a Poisson distribution $P(\lambda)$
parametrized by λ
tends to a
Gaussian distribution $N(\mu, \sigma)$
of mean $\mu = \lambda$ and standard deviation $\sigma = \sqrt{\lambda}$

$$P(\lambda) \xrightarrow{\lambda \rightarrow \infty} N(\lambda, \sqrt{\lambda})$$

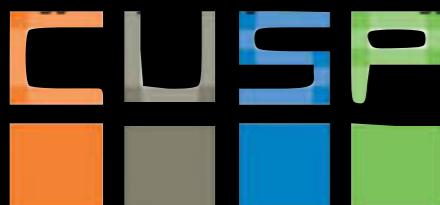
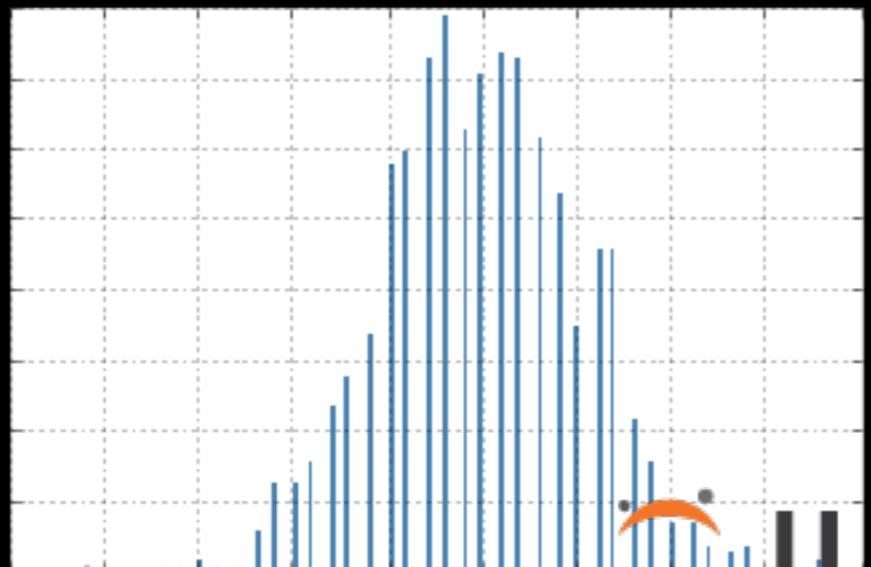
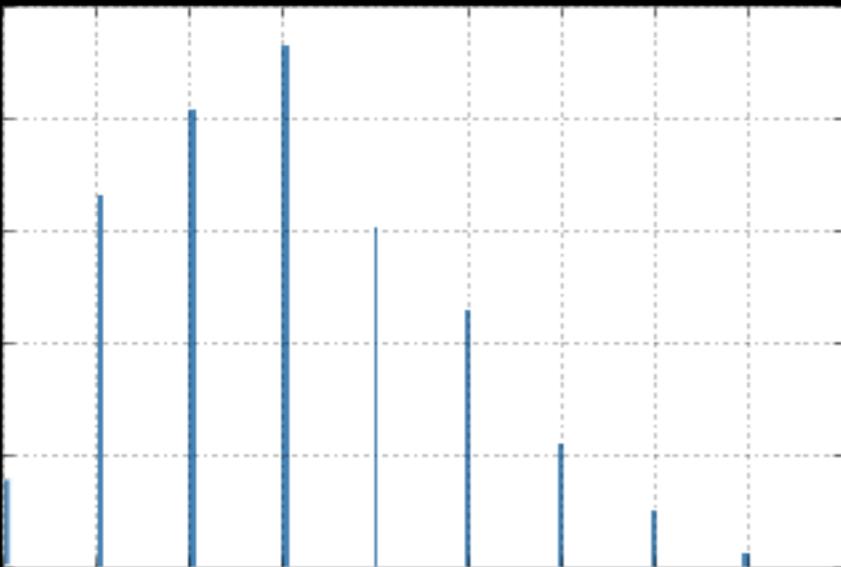
Binomial

discrete bivariate

2 parameters: n,p

support: [0 , ∞]

moments: np, \sqrt{npq} , >0



https://github.com/fedhere/UInotebooks/blob/master/binomial_gaussian_poisson.ipynb

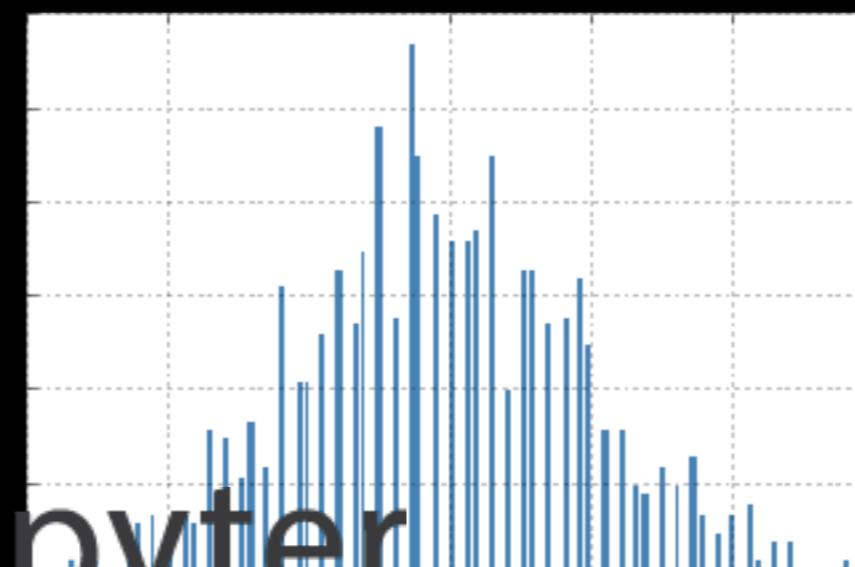
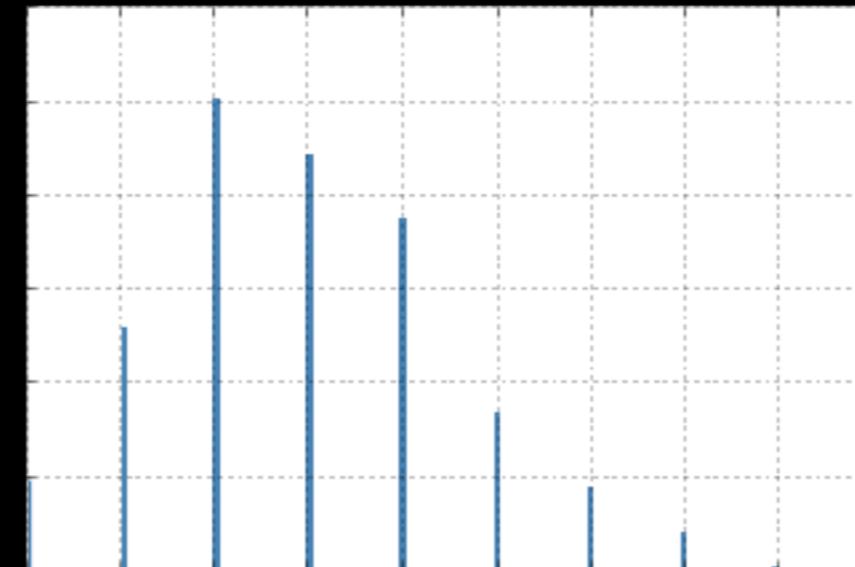
Poisson

discrete univariate

1 parameters: λ

support: [0 , ∞]

moments: $\lambda, \sqrt{\lambda}$, >0



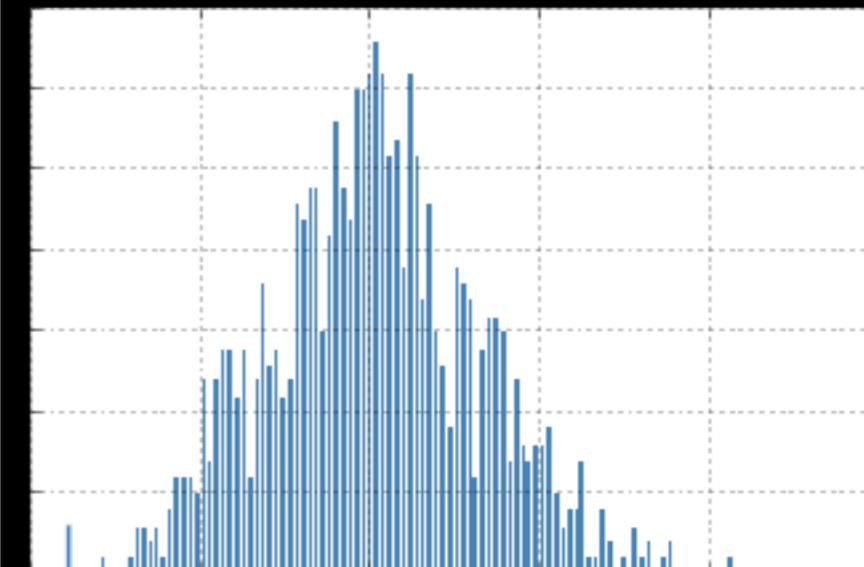
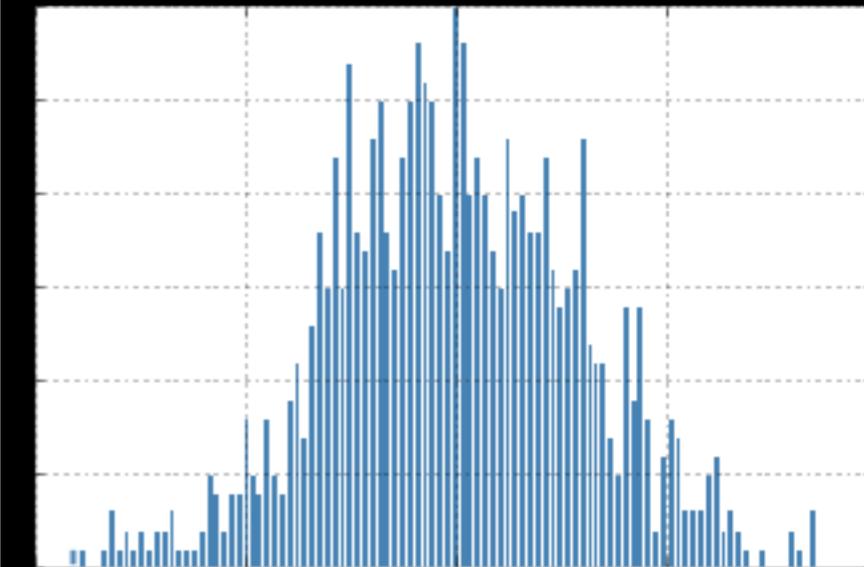
Gaussian

continuous bivariate

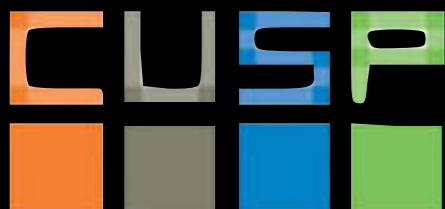
2 parameters: μ, σ

support:[- ∞ , ∞]

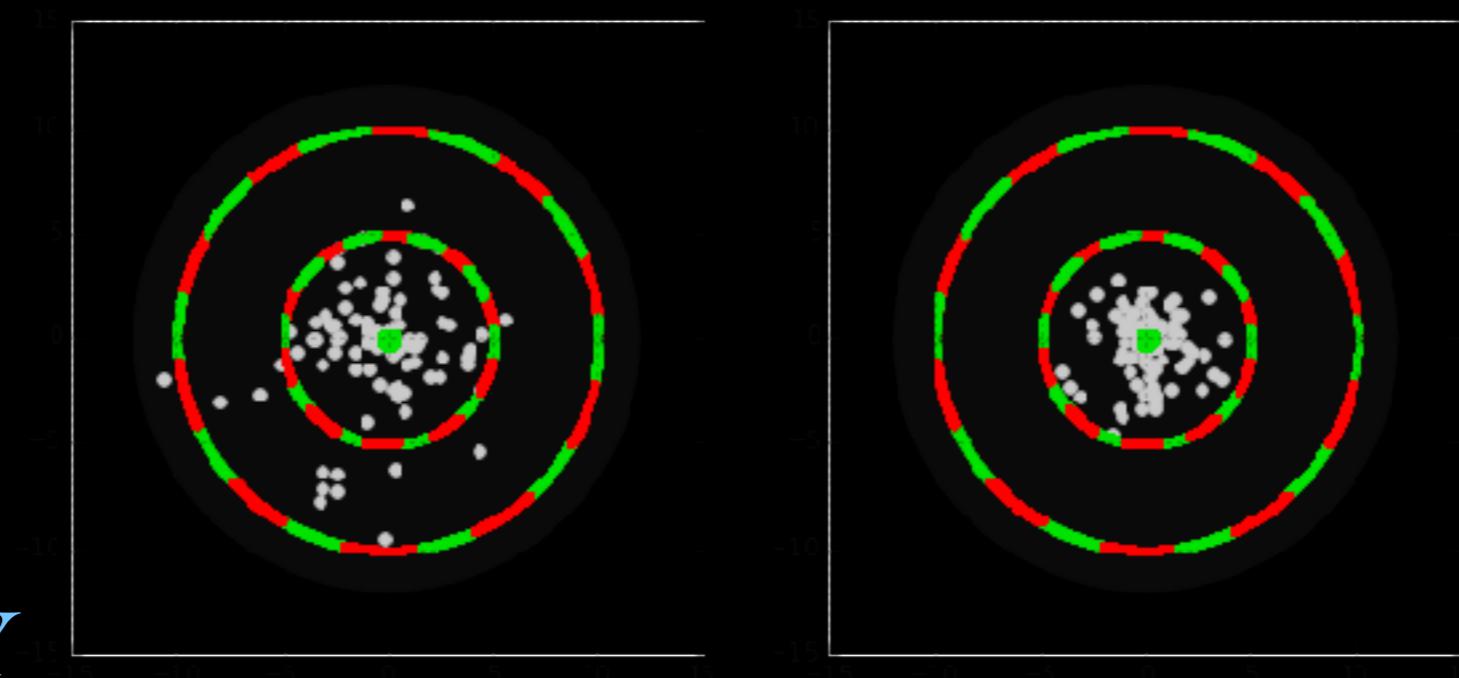
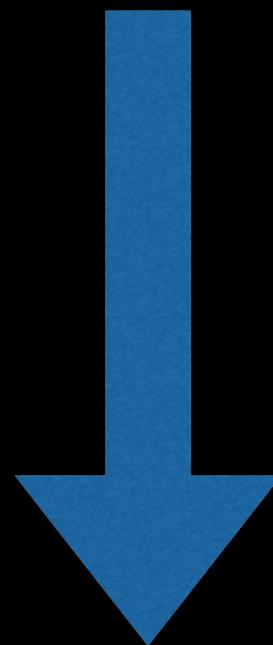
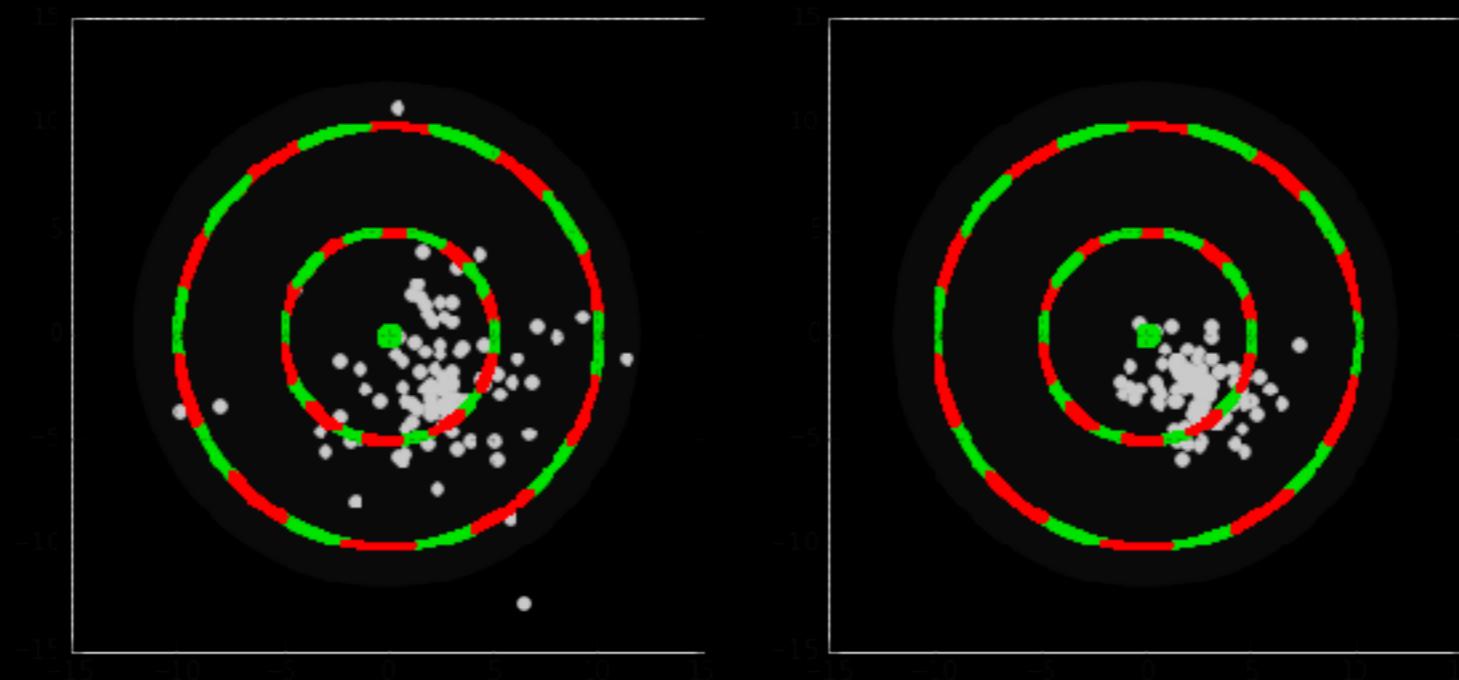
moments: $\mu, \sigma, 0$



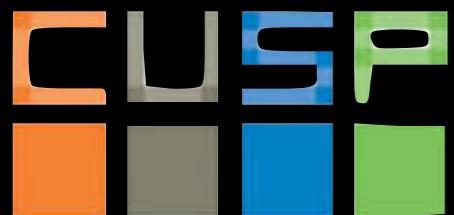
Systematic	Statistical
Biases the measurement in one direction	No preferred direction
Affects the sample regardless of the size	Shrinks with the sample size (typically as \sqrt{N})
Any distribution (usually we use Gaussian though)	Gaussian or Poisson



PRECISION



ACCURACY



IV: Statistical analysis

Error propagation

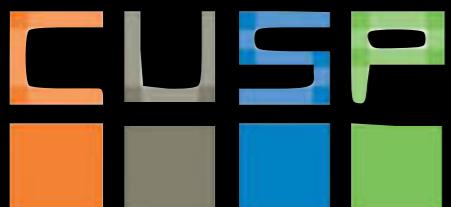
IID: Independent identically distributed:
add in quadrature for linear data operations

$$x_1 \pm \mathcal{E}(x_1)$$

$$x_2 \pm \mathcal{E}(x_2)$$

$$\bar{x} = \frac{x_1 + x_2}{2}$$

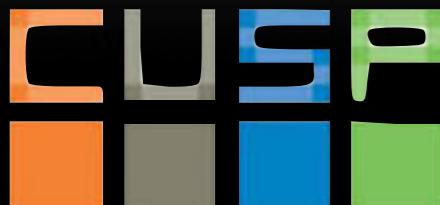
$$\mathcal{E}(\bar{x}) = \sqrt{\mathcal{E}(x_1)^2 + \mathcal{E}(x_2)^2}$$



Function	Variance	Standard Deviation
$f = aA$	$\sigma_f^2 = a^2 \sigma_A^2$	$\sigma_f = a\sigma_A$
$f = aA + bB$	$\sigma_f^2 = a^2 \sigma_A^2 + b^2 \sigma_B^2 + 2ab \sigma_{AB}$	$\sigma_f = \sqrt{a^2 \sigma_A^2 + b^2 \sigma_B^2 + 2ab \sigma_{AB}}$
$f = aA - bB$	$\sigma_f^2 = a^2 \sigma_A^2 + b^2 \sigma_B^2 - 2ab \sigma_{AB}$	$\sigma_f = \sqrt{a^2 \sigma_A^2 + b^2 \sigma_B^2 - 2ab \sigma_{AB}}$
$f = AB$	$\sigma_f^2 \approx f^2 \left[\left(\frac{\sigma_A}{A} \right)^2 + \left(\frac{\sigma_B}{B} \right)^2 + 2 \frac{\sigma_{AB}}{AB} \right]$	$\sigma_f \approx f \sqrt{\left(\frac{\sigma_A}{A} \right)^2 + \left(\frac{\sigma_B}{B} \right)^2 + 2 \frac{\sigma_{AB}}{AB}}$
$f = \frac{A}{B}$	$\sigma_f^2 \approx f^2 \left[\left(\frac{\sigma_A}{A} \right)^2 + \left(\frac{\sigma_B}{B} \right)^2 - 2 \frac{\sigma_{AB}}{AB} \right]$ [11]	$\sigma_f \approx f \sqrt{\left(\frac{\sigma_A}{A} \right)^2 + \left(\frac{\sigma_B}{B} \right)^2 - 2 \frac{\sigma_{AB}}{AB}}$
$f = aA^b$	$\sigma_f^2 \approx (abA^{b-1}\sigma_A)^2 = \left(\frac{fb\sigma_A}{A} \right)^2$	$\sigma_f \approx abA^{b-1}\sigma_A = \left \frac{fb\sigma_A}{A} \right $
$f = a \ln(bA)$	$\sigma_f^2 \approx \left(a \frac{\sigma_A}{A} \right)^2$ [12]	$\sigma_f \approx \left a \frac{\sigma_A}{A} \right $
$f = a \log_{10}(A)$	$\sigma_f^2 \approx \left(a \frac{\sigma_A}{A \ln(10)} \right)^2$ [12]	$\sigma_f \approx \left a \frac{\sigma_A}{A \ln(10)} \right $
$f = ae^{bA}$	$\sigma_f^2 \approx f^2 (b\sigma_A)^2$ [13]	$\sigma_f \approx f(b\sigma_A) $
$f = a^{bA}$	$\sigma_f^2 \approx f^2 (b \ln(a)\sigma_A)^2$	$\sigma_f \approx f(b \ln(a)\sigma_A) $
$f = A^B$	$\sigma_f^2 \approx f^2 \left[\left(\frac{B}{A} \sigma_A \right)^2 + (\ln(A)\sigma_B)^2 + 2 \frac{B \ln(A)}{A} \sigma_{AB} \right]$	$\sigma_f \approx f \sqrt{\left(\frac{B}{A} \sigma_A \right)^2 + (\ln(A)\sigma_B)^2 + 2 \frac{B \ln(A)}{A} \sigma_{AB}}$

$\chi = \frac{A}{B}$ $\sigma_\chi^2 \approx \chi^2 \left[\left(\frac{\sigma_A}{A} \right)^2 + (\ln(\chi) \sigma_B)^2 + \frac{A}{B^2} \sigma_{AB}^2 \right]$ $\sigma_\chi \approx |\chi| \sqrt{\left(\frac{\sigma_A}{A} \right)^2 + (\ln(\chi) \sigma_B)^2 + \frac{A}{B^2} \sigma_{AB}^2}$
https://en.wikipedia.org/wiki/Propagation_of_uncertainty#Linear_combinations

$\chi = \alpha_p \gamma$ $\sigma_\chi^2 \approx \chi^2 (\rho \mu(\alpha) \sigma_\gamma^2)$ $\sigma_\chi \approx |\chi| (\rho \mu(\alpha) \sigma_\gamma)$



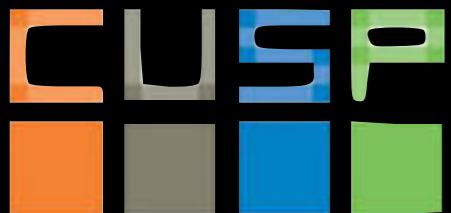
Covariance matrix

$$\xrightarrow{\hspace{1cm}} \mathbf{x} = \{\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3, \dots, \mathbf{x}_n\}$$

$$f_k = \sum_i^n A_{ki} x_i$$

$$\Sigma = \begin{pmatrix} \sigma_1^2 & \sigma_{12} & \dots & \sigma_{1n} \\ \sigma_{21} & \sigma_2^2 & \dots & \sigma_{2n} \\ \dots & \dots & \dots & \dots \\ \sigma_{m1} & \sigma_{m2} & \dots & \sigma_m^2 \end{pmatrix}$$

$$\Sigma(f) = A \Sigma^x A^\top$$



Covariance matrix



$$\textbf{x} = \{\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3, \dots, \mathbf{x}_n\}$$

$$f_k = \sum_i^n A_{ki} x_i$$

IF
Independent
variables

$$\Sigma = \begin{pmatrix} \sigma_1^2 & \sigma_{12} & \dots & \sigma_{1n} \\ \sigma_{21} & \sigma_2^2 & \dots & \sigma_{2n} \\ \dots & \dots & \dots & \dots \\ \sigma_{m1} & \sigma_{m2} & \dots & \sigma_m^2 \end{pmatrix}$$

$$\Sigma = \begin{pmatrix} \sigma_1^2 & 0 & \dots & 0 \\ 0 & \sigma_2^2 & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & \sigma_m^2 \end{pmatrix}$$

$$\Sigma(f) = A \Sigma^x A^\top \quad \Sigma(f)_{ij} = \sum_k^n A_{ik} \Sigma_k A_{jk}$$

Reporting Your Results

It is essential that the systematic error be reported separately from the imprecision part of the reported value

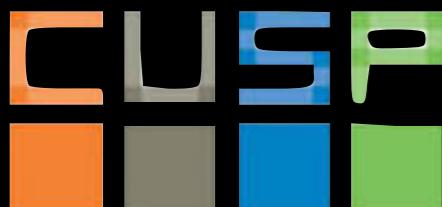
Statistical Concepts and Procedures
by United States. National Bureau of Standards 1969

Keep statistical, systematic errors separate. Report results as something like:

$$x = [965 \pm 30(\text{stat}) \pm 12(\text{sys})] \text{ number of car accidents}$$

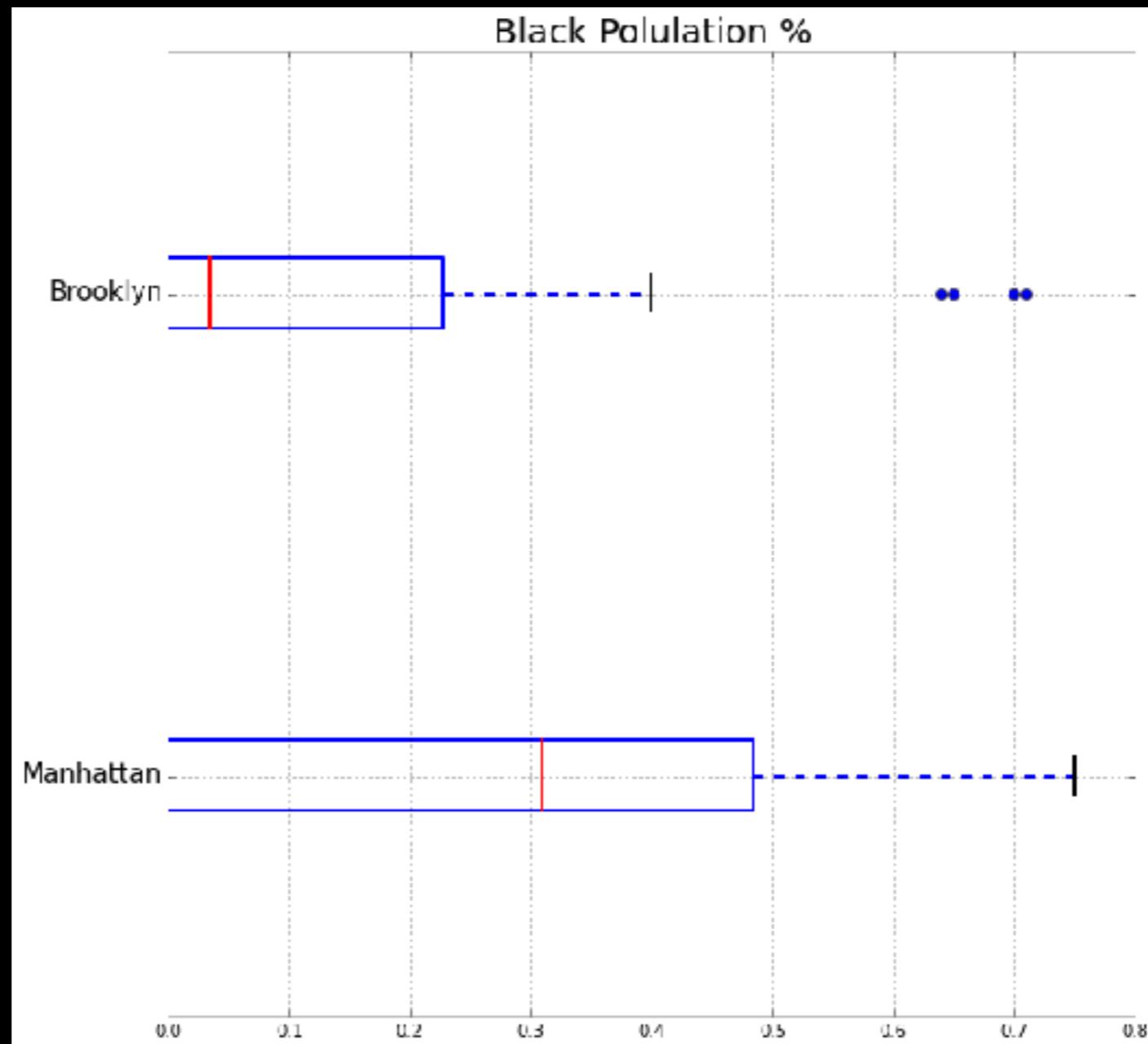
Add in quadrature (note that this assumes Gaussian distribution)
compare with known values $32 = \sqrt{30^2 + 12^2}$:

$$x = [965 \pm 32(\text{total})] \text{ number of car accidents}$$

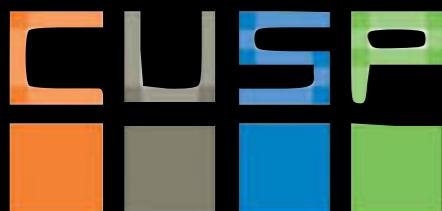


Reporting Your Results

Percentage of Black population by Borrow
(Manhattan vs Brooklyn)



jupyter
[http://localhost:
8889/
notebooks/
black_percenta
ge.ipynb#](http://localhost:8889/notebooks/black_percentange.ipynb#)

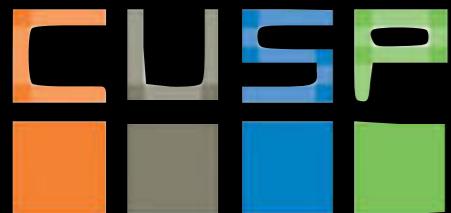


Reporting Your Results

x_{test} = [965 ± 32(total)] number of car accidents

$x_{\text{population}}$ = [932 ± 29(total)] number of car accidents

Test statistic = (Statistic - Parameter) / (statistics Standard error)



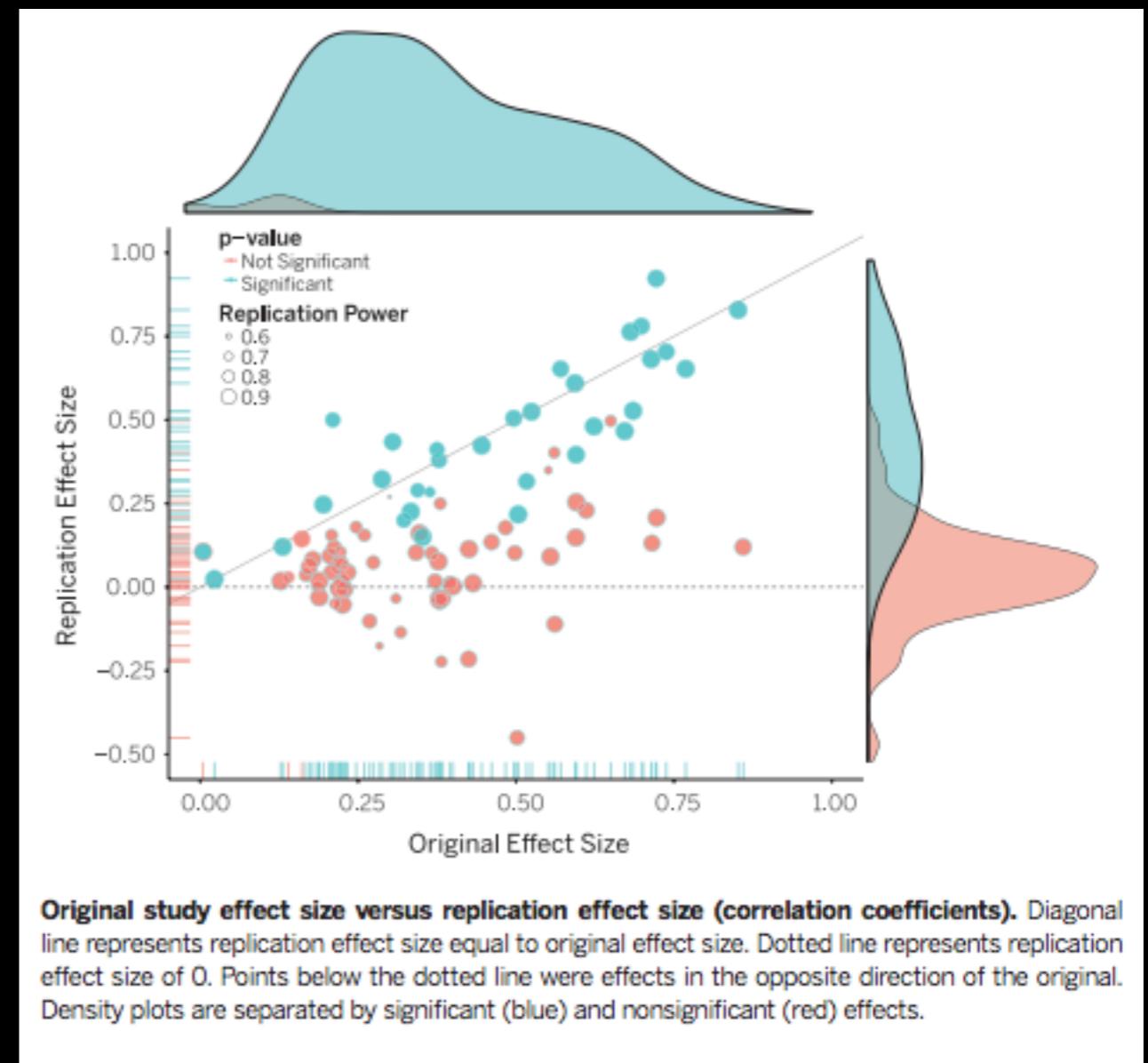
Homework: READING

RESEARCH ARTICLE SUMMARY

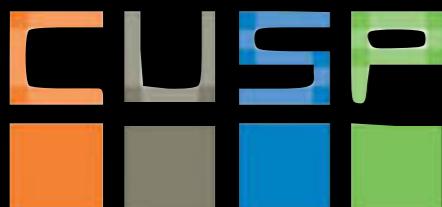
PSYCHOLOGY

Estimating the reproducibility of psychological science

Open Science Collaboration*



<http://www.sciencemag.org/content/349/6251/aac4716.full.pdf>



IV: Statistical analysis

Homework: 1. Compare Tests for Correlation

The following are 3 tests that assess correlation between 2 samples of citibike data:

- **Pearson's test** (answer: are the 2 samples correlated?)
- **Spearman's test** (answer: are the 2 samples correlated?)
- **K-S test** (answer: are the samples likely to come from the same parent distribution?)

Use: age of bikers for 2 genders, age of bikers in day vs night and assess the correlation/independence of the 2 samples in each case. State your result in words.

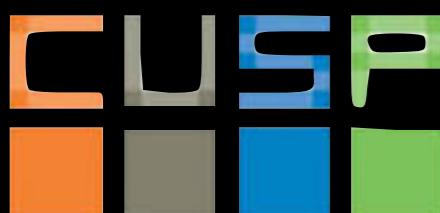
Homework: 2. Compare Tests for Goodness of fit (synthetic data)

The following are 5 tests that can be used to assess the goodness of fit of a model

- **K-S**
- **Pearson's Chi squared**
- **Anderson-Darling**
- **K-L Divergence**
- **(Likelihood ratio, you do not need to do this yet!)**

Use KS, K-L divergence, and one more test (AD or Chisq) to quantify the difference between a binomial & Gaussian distribution and a Poisson & Gaussian distribution as a function of the parameters of the first distribution (np for binomial, λ for poisson)

For each test plot the relevant parameter (the K-L parameter, Anderson-Darling statistics, p-value for KS, Chi-sq parameter), against the distribution parameter (np, λ)

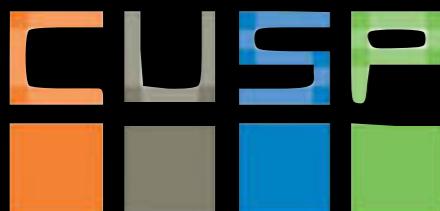


Homework: 3. Compare Tests for Goodness of fit (real data)

Test whether a gaussian model for the age distribution of citibike drivers is a sensible model, or if you can find a better fit with another distribution. Use 2 tests (from the previous exercise) to do this. Test at least 2 distributions.

Divide your riders sample by seasons: SpringSummer vs FallWinter and see if you notice any changes.

Optional (extra credit): Divide your sample geographically: by Borrow + split Manhattan in an Uptown and a Downtown sample (use your discretion to do so) and see if you notice any differences in how the age distribution can be modeled.



MUST KNOWS:

- Statistical errors
- Systematic errors
- Undercoverage, SelfSelection, Social desirability
publication bias, data dredging
- Precision vs accuracy

Resources:

Sarah Boslaugh, Dr. Paul Andrew Watters, 2008

Statistics in a Nutshell (Chapters 3,4,5)

https://books.google.com/books/about/Statistics_in_a_Nutshell.html?id=ZnhgO65Pyl4C

David M. Lane et al.

Introduction to Statistics (XVIII)

http://onlinestatbook.com/Online_Statistics_Education.epub

<http://onlinestatbook.com/2/index.html>

Reckova & Irsova

Publication Bias in Measuring Climate Sensitivity

IES Working Paper: 14/2015

http://salserver.org.aalto.fi/vanhat_sivut/Opinnot/Mat-2.4108/pdf-files/emet03.pdf

