

$$d \leq \beta d \leq \beta^2 d \leq \beta^3 d$$

