

$$a) \log(S_i^2) + \frac{2p_i}{n} \quad L=0,1$$

$$\log(S_0^2) + \frac{2p_0}{n} < \log(S_1^2) + \frac{2p_1}{n}$$

$$\log(S_0^2) - \log(S_1^2) < \frac{2}{n}(p_1 - p_0) \quad \left. \begin{array}{l} \log(a) - \log(b) = \log\left(\frac{a}{b}\right) \\ \text{exponent both sides} \end{array} \right\}$$

$$\log\left(\frac{S_0^2}{S_1^2}\right) < \frac{2(p_1 - p_0)}{n}$$

$$\left(\frac{S_0^2}{S_1^2}\right) < e^{\frac{2}{n}(p_1 - p_0)}$$

$$b) e^x \approx 1+x \quad e^{\frac{2}{n}(p_1 - p_0)} \approx 1 + \frac{2}{n}(p_1 - p_0)$$

$$\frac{S_0^2}{S_1^2} < 1 + \frac{2}{n}(p_1 - p_0)$$

$$\frac{S_0^2}{S_1^2} - 1 < \frac{2}{n}(p_1 - p_0)$$

$$\frac{S_0^2 - S_1^2}{S_1^2} < \frac{2}{n}(p_1 - p_0) \quad (*)$$

$$c) s^2 = e'e / (n-k) \quad S_0^2 = e_R'e_R / (n-p_0) \quad S_1^2 = e_U'e_U / (n-p_1) \quad \begin{array}{l} n \text{ large} \\ n-p_0 \approx n \\ n-p_1 \approx n \end{array}$$

$$(*) \text{ LHS } \frac{S_0^2 - S_1^2}{S_1^2} = \frac{e_R'e_R / (n-p_0) - e_U'e_U / (n-p_1)}{e_U'e_U / (n-p_1)}$$

$$(*) \text{ becomes } \frac{e_R'e_R - e_U'e_U}{e_U'e_U} < \frac{2}{n}(p_1 - p_0)$$

$$d) \quad F = \frac{(e_R' e_R - e_u' e_u) / (p_1 - p_0)}{e_u' e_u / (n - p_1)}$$

$$\text{from (1)} \quad \frac{e_R' e_R - e_u' e_u}{e_u' e_u} < \frac{2}{n} (p_1 - p_0) \quad (**)$$

F nearly equal to LHS of (\*\*)

$$\frac{(e_R' e_R - e_u' e_u) / (p_1 - p_0)}{e_u' e_u / (n - p_1)} < 2 \frac{n - p_1}{n}$$

$\times \frac{n - p_1}{p_1 - p_0}$   
 $\searrow$   
 $\hookrightarrow$  n large  $\frac{2(n - p_1)}{n} \approx 2$