

**U.B.A. FACULTAD DE INGENIERÍA**

**Departamento de Electrónica**

**LABORATORIO 66-02**  
**Informática**

**TRABAJO PRÁCTICO N°0**

*Análisis de circuitos*

**Curso 2021 – 1er Cuatrimestre**

**GRUPO N° 6**

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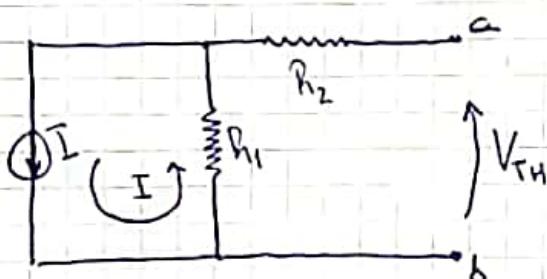
**Observaciones:**

1) Obtenga los valores indicados en cada circuito sobre  $R_h$ , aplicando los teoremas de Thévenin y de Norton.

a)



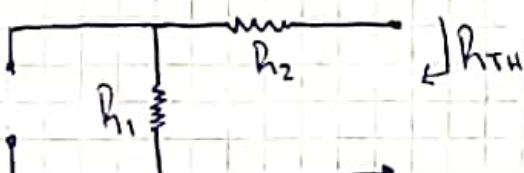
Buscamos la tensión de Thévenin:



Sobre  $R_2$  no circula corriente entonces  $V_{TH} = V_{R_1} = I \cdot R_1$

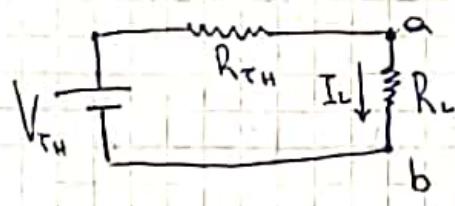
$$V_{TH} = 100 \mu\text{A} \cdot 50 \text{ }\Omega = 5 \text{ V}$$

Para encontrar  $R_{TH}$  debemos quitar la fuente de corriente:



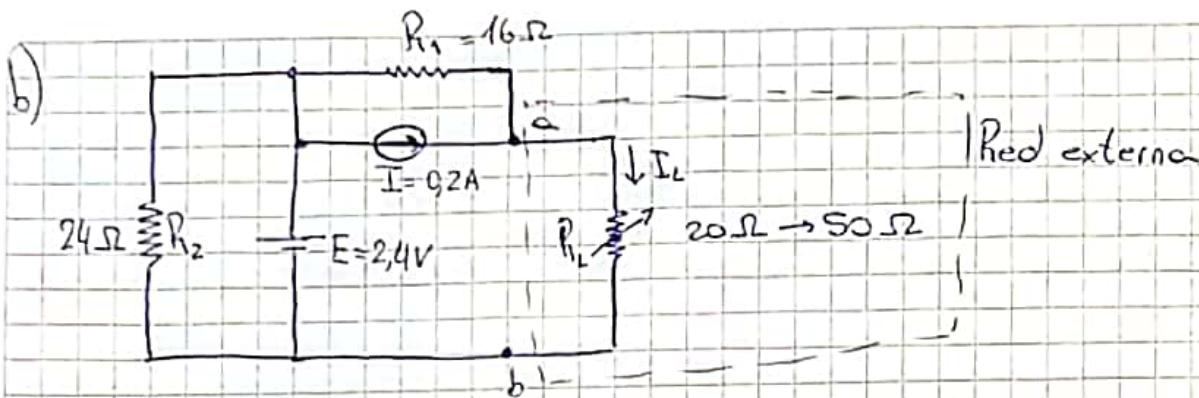
$$R_{TH} = R_h + R_2 = 70 \text{ }\Omega$$

Luego, el siguiente circuito es el que se obtiene por el T. de Thévenin:



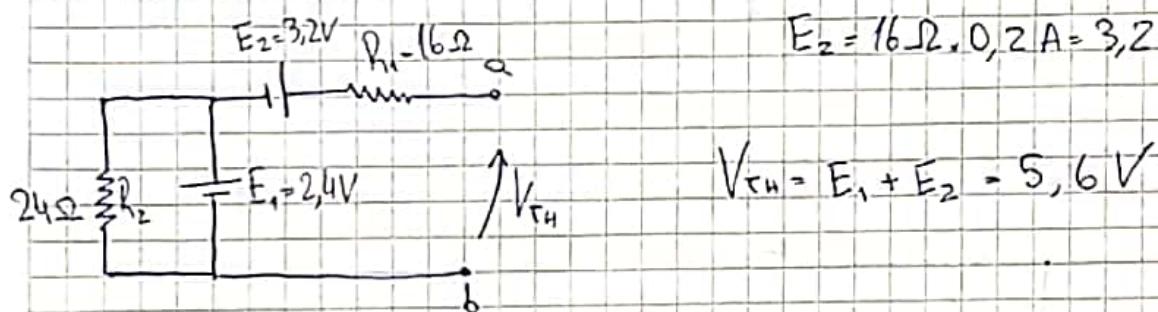
$$I_L = \frac{V_{TH}}{R_L + R_{TH}} = \frac{5 \text{ V}}{180 \text{ }\Omega + 70 \text{ }\Omega} = 20 \mu\text{A}$$

$$\boxed{I_L = 20 \mu\text{A}}$$

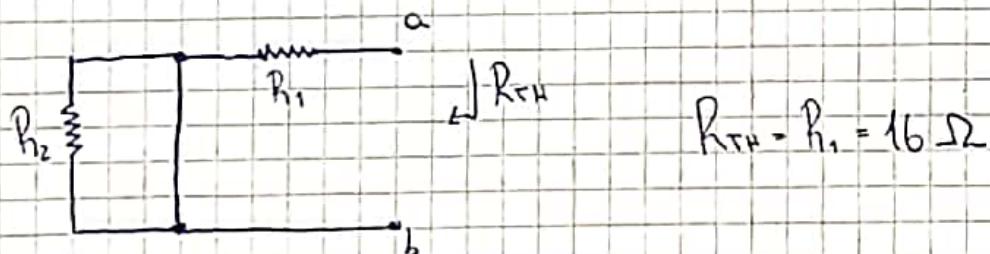


Reemplazamos la fuente de corriente y la resistencia que están en paralelo por su equivalente de Thévenin.

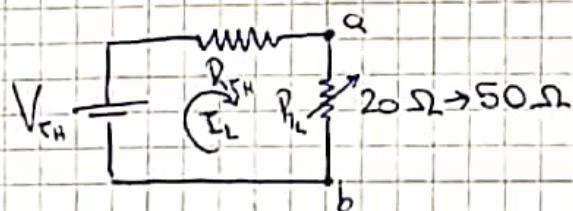
Buscamos  $V_{TH}$ :



Buscamos  $R_{TH}$ :



Entonces, por el teorema de Thévenin se obtiene el siguiente circuito:



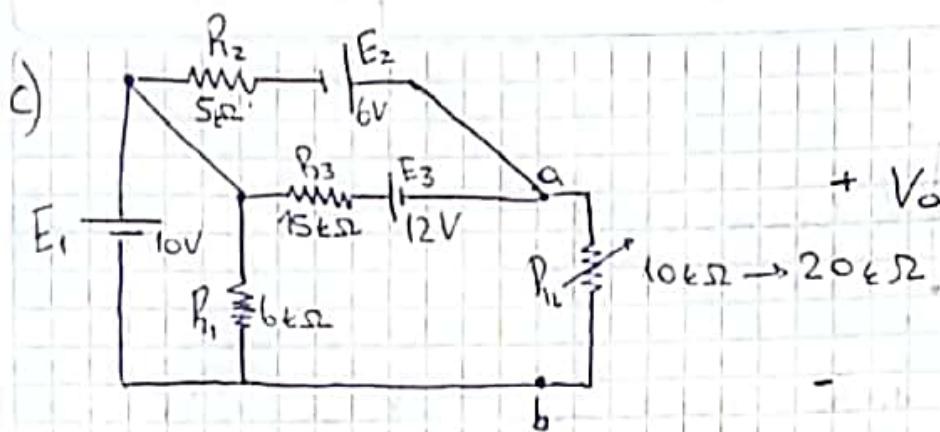
$$I_L = \frac{V_{TH}}{R_{TH} + R_L}$$

entonces, para  $R_L = 20 \Omega$ :  $I_L = \frac{5.6 V}{(16 + 20) \Omega} = 0.156 A$

y  $|V_{ab} = 3.12 V|$

para  $R_L = 50 \Omega$ :  $I_L = \frac{5.6 V}{(16 + 50) \Omega} = 0.0848 A$

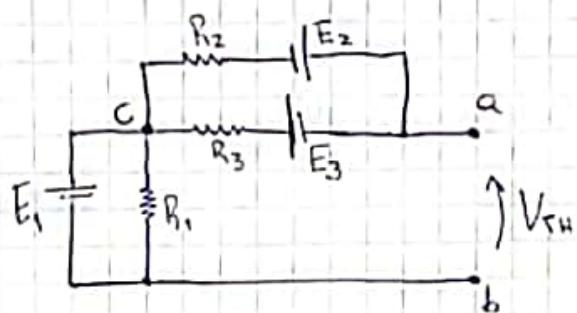
y  $|V_{ab} = 1.70 V|$



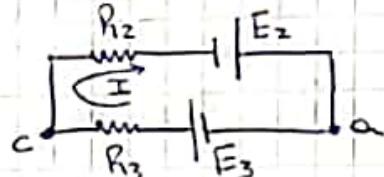
$$+ V_{ab}$$

$$10k\Omega \rightarrow 20k\Omega$$

Buscamos  $V_{TH}$ :



$$V_{TH} = E_1 + V_{ac}$$



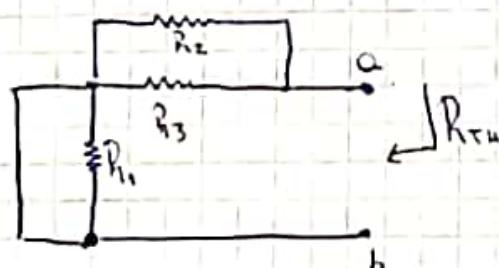
$$E_3 + E_2 - I(R_2 + R_3) = 0$$

$$\Rightarrow I = \frac{E_2 + E_3}{R_2 + R_3} = \frac{18V}{20k\Omega} = 9 \times 10^{-4}A = 0,9mA$$

Entonces  $V_{ac} = -0,9mA \cdot R_2 + E_2 = 1,5V$

$$V_{TH} = E_1 + V_{ac} = 10V + 1,5V = 11,5V$$

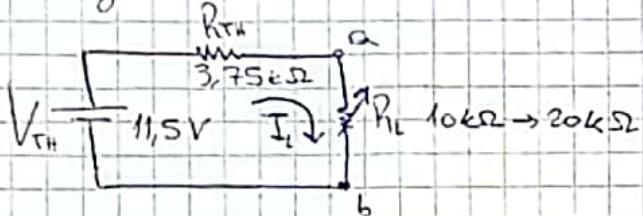
Buscamos  $R_{TH}$ :



$$R_{TH} = R_2 \parallel R_3 = \left( \frac{1}{R_2} + \frac{1}{R_3} \right)^{-1}$$

$$R_{TH} = \frac{R_2 R_3}{R_2 + R_3} = 3,75k\Omega$$

Luego, el circuito que se obtiene por el teorema de Thévenin es el siguiente:



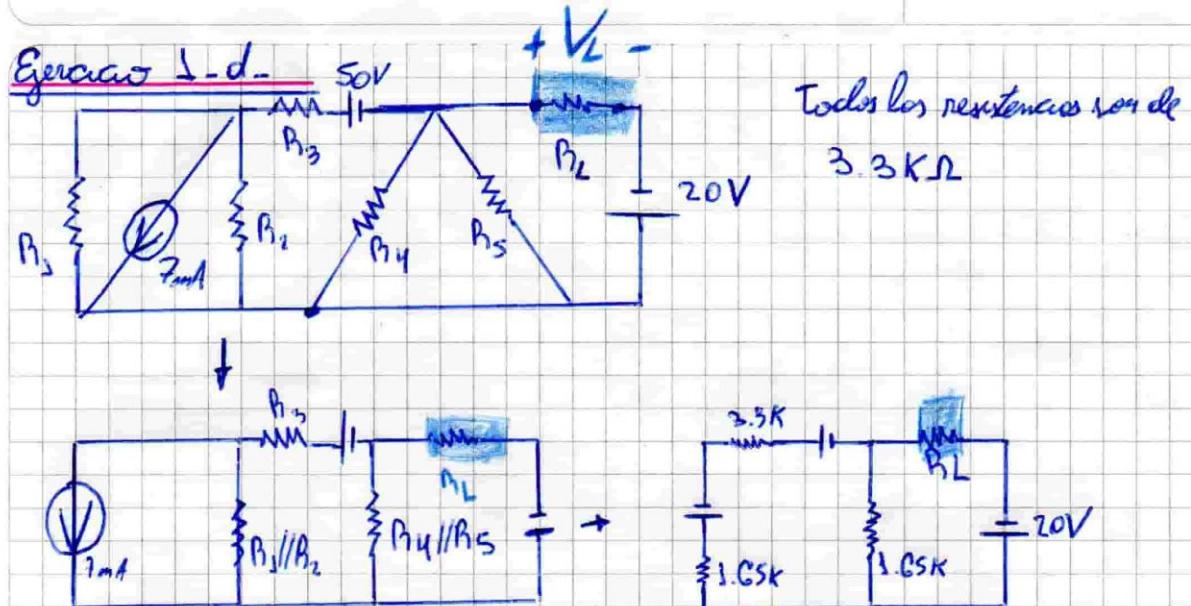
$$I_L = \frac{V_{TH}}{R_{TH} + R_L}$$

si  $R_L = 10 \text{ k}\Omega$ :  $I_L = \frac{11,5 \text{ V}}{(3,75 + 10) \text{ k}\Omega} = 0,836 \text{ mA}$

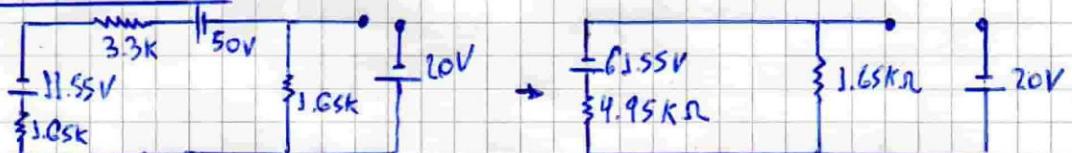
$$V_{ab} = I_L \times R_L = 8,36 \text{ V}$$

si  $R_L = 20 \text{ k}\Omega$ :  $I_L = \frac{11,5 \text{ V}}{(3,75 + 20) \text{ k}\Omega} = 0,484 \text{ mA}$

$$V_{ab} = I_L \times R_L = 9,68 \text{ V}$$



Mi Red lineal actua:



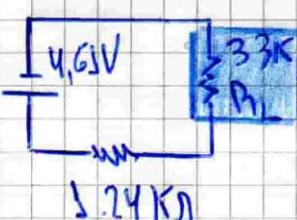
Busco  $R_{TH}$ : como fuente

$$\frac{1}{4.95\text{ k}\Omega} \parallel \frac{1}{1.65\text{ k}\Omega} \quad R_{TH} = 4.95\text{ k}\Omega // 1.65\text{ k}\Omega = 1.24\text{ k}\Omega$$

Busco  $V_{TH}$

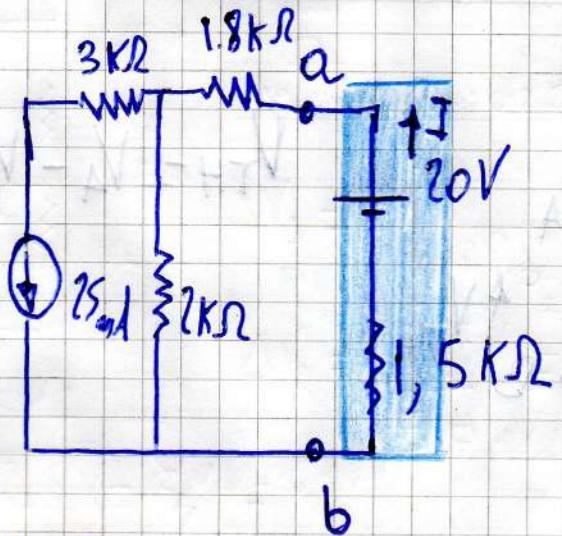
$$V_{TH} = -20V + 6.155V \cdot \frac{1.65\text{ k}\Omega}{4.95\text{ k}\Omega + 1.65\text{ k}\Omega} = -4.61V$$

Circuito equivalente:



$$V_L = -4.61V \cdot \frac{3.3\text{ k}\Omega}{3.3\text{ k}\Omega + 1.24\text{ k}\Omega} = -3.35V$$

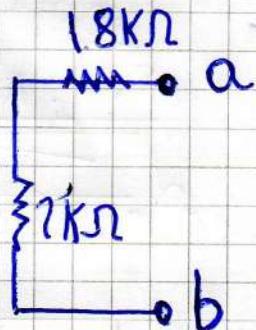
Ejercicio 1-e



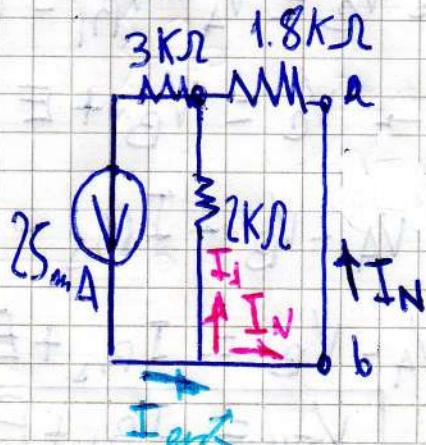
Voy a usar el T de Norton

Halla la  $R_N$

$$R_N = 3.8 \text{ k}\Omega$$



Halla la  $I_N$

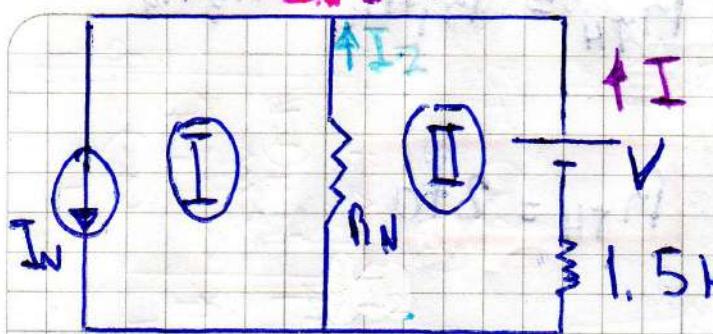


Usa DIVISORES DE CORRIENTE

$$I_N = I_{\text{ent}} \cdot \frac{2 \text{ k}\Omega}{1.8 \text{ k}\Omega + 2 \text{ k}\Omega}$$

$$I_N = 25 \text{ mA} \cdot \frac{10}{19} = 13.16 \text{ mA}$$

$$I_N = 13.16 \text{ mA}$$



Planteo Sección de Kirchhoff

$$I_2 = I_N - I$$

2) (I)  $-1,5k\Omega I + V + I_2 R_N = 0$

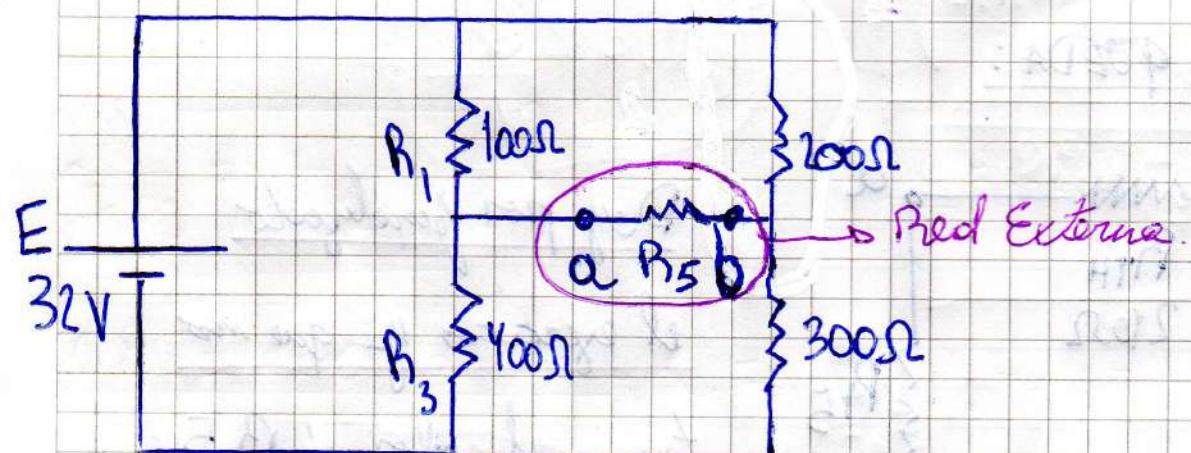
$$-1,5k\Omega I + V + (I_N - I) R_N = 0$$

$$-1,5k\Omega I + 20V + (13,16mA - I) 3,8k\Omega = 0$$

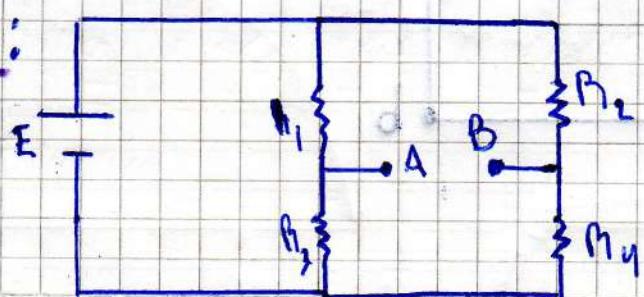
$$+20V + 50V - 5,3k\Omega I = 0$$

$$\boxed{I = 13,20mA}$$

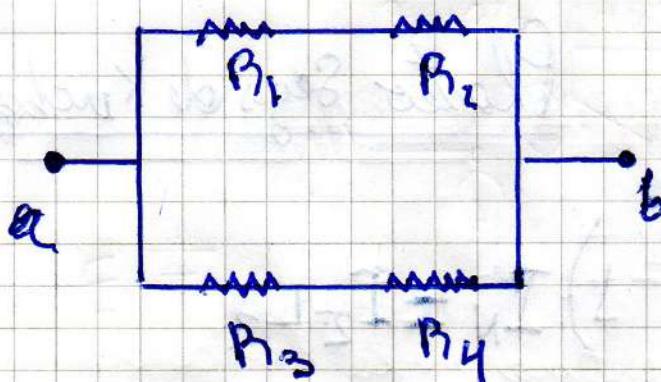
### Ejercicio 1-6.



Red lineal activa:



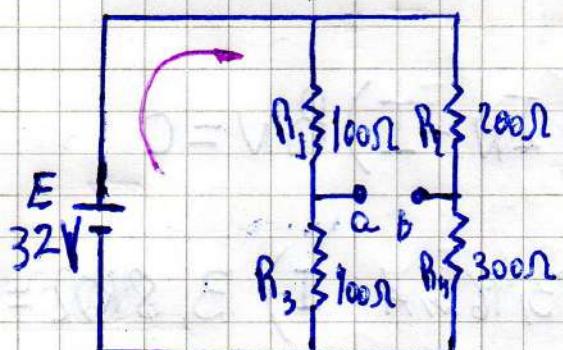
## BUSCO la $R_{TH}$



$$\frac{1}{R_{TH}} = \frac{1}{R_1+R_2} + \frac{1}{R_3+R_4}$$

$$R_{TH} = 210$$

## BUSCO la $V_{TH}$



Doy un orden de tamaños

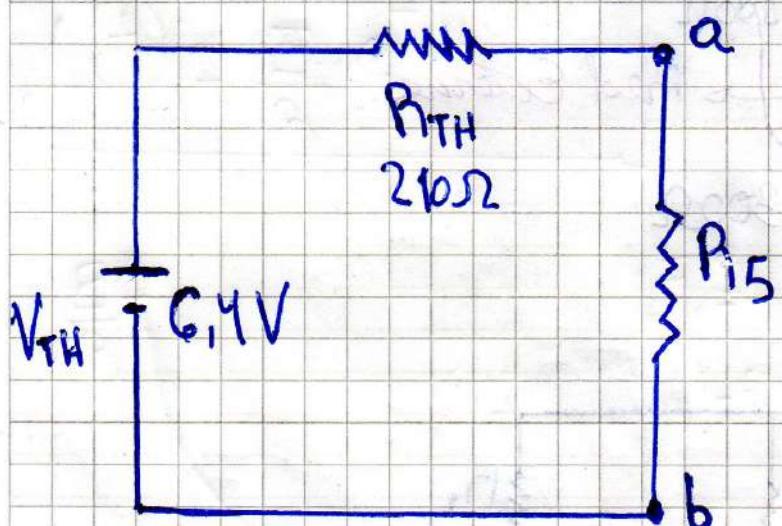
$$\Delta V_1 = \frac{R_1}{R_1+R_3} E = \frac{32}{5} V = 6,4V$$

$$\Delta V_2 = \frac{R_2}{R_2+R_4} E = \frac{64}{5} V = 12,8V$$

$$V_{TH} = V_a - V_b = 12,8V - 6,4V = 6,4V$$

$$V_{TH} = 6,4V$$

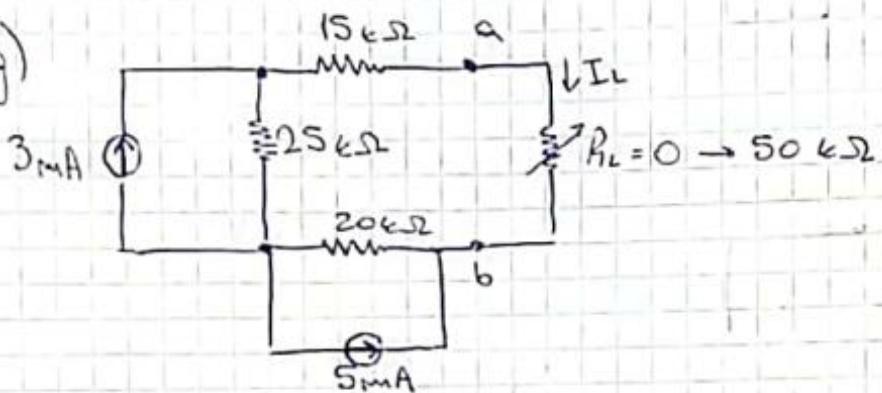
MICROCUITO QUEDA:



Doy por fundamental

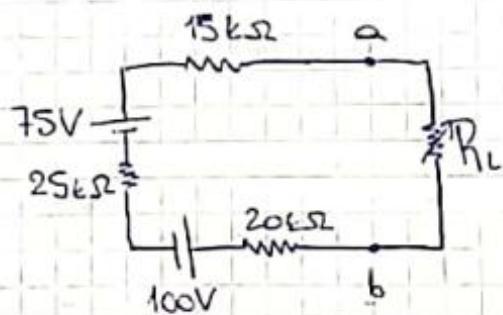
el ejercicio ya que no tengo el valor de R15.

1)g)



Podemos reemplazar aquellas fuentes de corriente que tienen una resistencia en paralelo por su equivalente de Thévenin:

Thévenin:

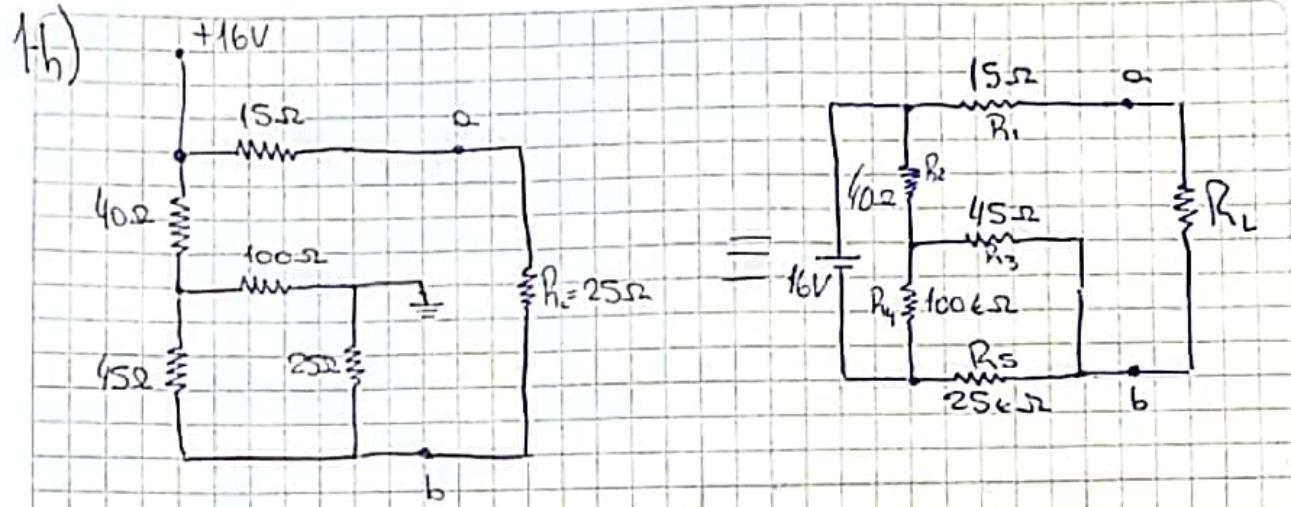


Podemos simplificar el circuito sumando las fuentes y las resistencias

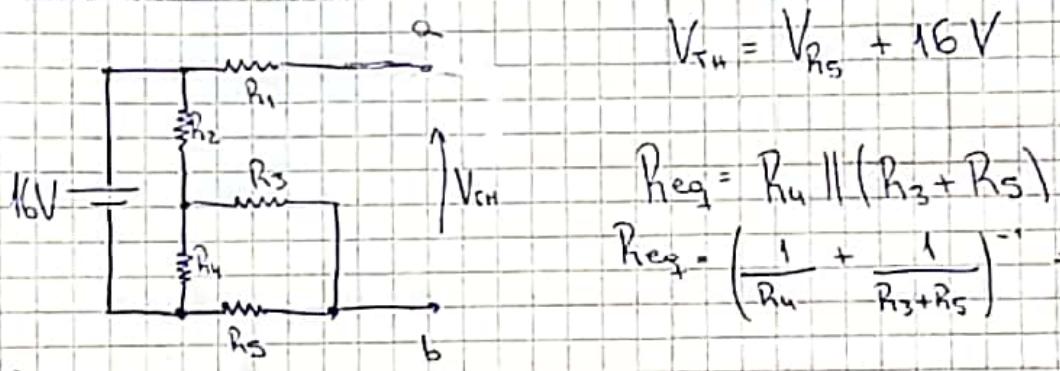
$$I_L = \frac{-25\text{V}}{60\text{k}\Omega + R_L}$$

$$\text{Si } R_L = 0 \rightarrow I_L = -0,4167\text{ mA}$$

$$\text{Si } R_L = 50\text{k}\Omega \rightarrow I_L = -0,2273\text{ mA}$$



Buscamos  $V_{TH}$ :



$$R_{eq} = R_h \parallel (R_3 + R_5)$$

$$R_{eq} = \left( \frac{1}{R_h} + \frac{1}{R_3 + R_5} \right)^{-1} = 41,2\Omega$$

Entonces, tenemos:

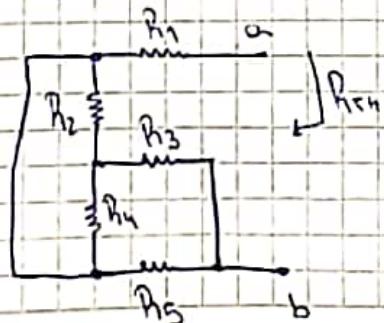
$$V_{R_2} = 16V \cdot \frac{R_2}{R_2 + R_{eq}} = 7,88V$$

$$V_{R_h} + V_{R_2} = 16V \Rightarrow V_{R_h} = 8,12V$$

$$V_{R_5} = -V_{R_h} \cdot \frac{R_5}{R_3 + R_4} = -2,9V$$

$$\Rightarrow V_{TH} = -2,9V + 16V = 13,1V$$

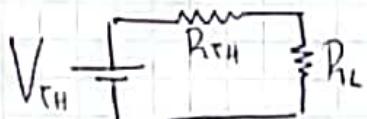
Buscamos  $R_{TH}$ :



$$\begin{aligned} R_{TH} &= R_h + [(R_2 \parallel R_4) + R_3] \parallel R_5 = \\ &= 15\Omega + [28,57\Omega + 45\Omega] \parallel 25\Omega = \\ &= 15\Omega + 73,57\Omega \parallel 25\Omega = 33,7\Omega \end{aligned}$$

$$R_{TH} = 33,7\Omega$$

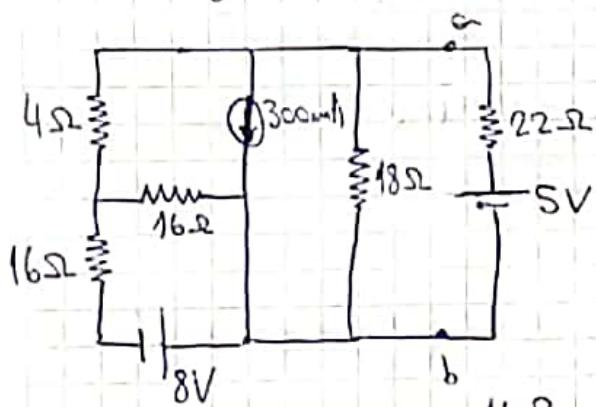
A partir del teorema de Thévenin se obtiene el siguiente circuito:



$$I_{R_L} = \frac{V_{TH}}{R_{TH} + R_L} = \frac{13,1 \text{ V}}{33,75\Omega + 25\Omega} = 0,22 \text{ A}$$

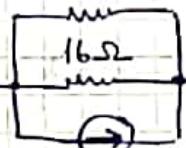
$$V_{R_L} = V_{TH} \cdot \frac{R_L}{R_{TH} + R_L} = 5,58 \text{ V}$$

- C) i) El siguiente circuito es equivalente al del enunciado



Vemos que puede ser simplificado

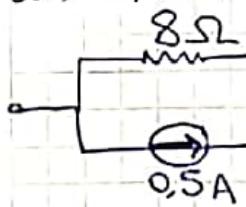
16Ω



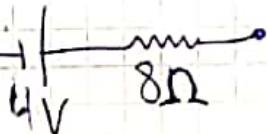
0.5A

Buscamos el equivalente de Norton:

Las resistencias están en paralelo:

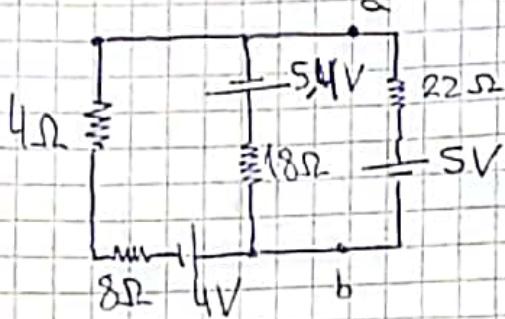


esto es equivalente a:



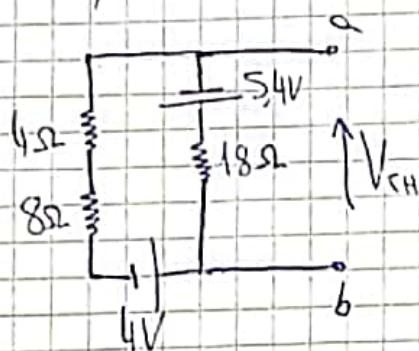
Además, en el circuito inicial hay una fuente de corriente con una resistencia en paralelo que pueden ser reemplazadas por su equivalente de Thévenin.

Entonces, nos quedó el siguiente circuito:



Ahora aplicamos el teorema de Thevenin

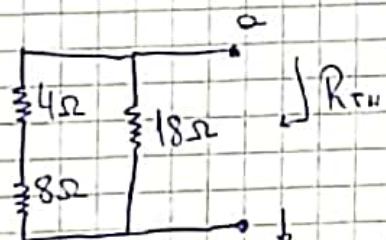
$V_{TH}$ )



$$V_{TH} = -5.4V + \frac{(5.4V - 4V) \cdot 18\Omega}{18\Omega + 8\Omega + 4\Omega}$$

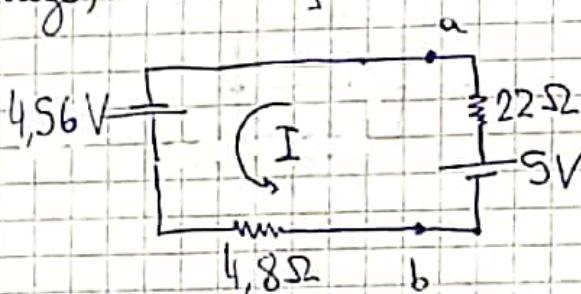
$$V_{TH} = -4.56V$$

$R_{TH}$ )



$$R_{TH} = 18\Omega \parallel (4\Omega + 8\Omega) = 4.8\Omega$$

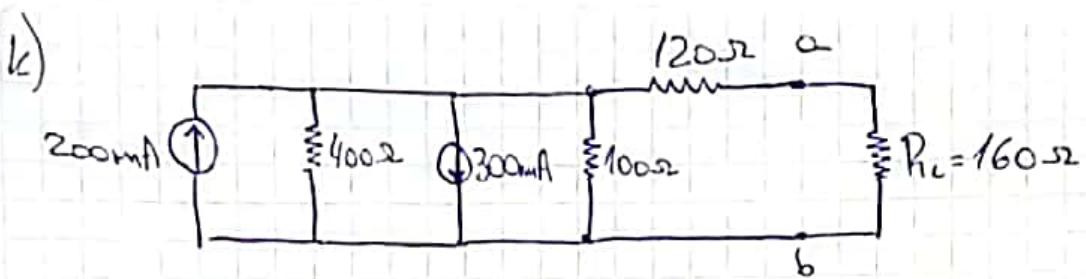
Luego, tenemos que:



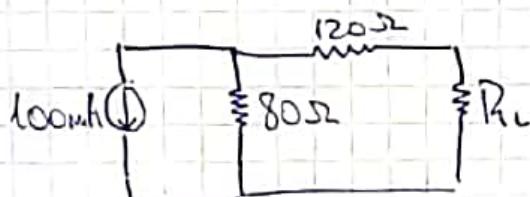
$$I = \frac{5V + 4.56V}{22\Omega + 4.8\Omega} = 0.357A$$

$$V_{ab} = 5V - 0.357A \cdot 22\Omega$$

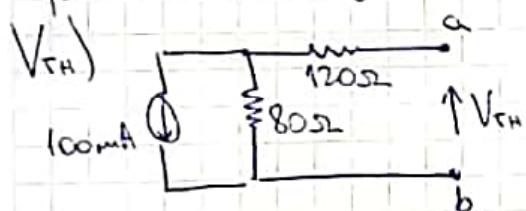
$$\boxed{V_{ab} = -2.85V}$$



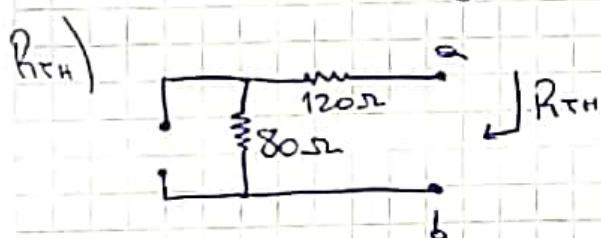
Las fuentes de corriente en paralelo pueden reducirse a una sola fuente. Y las resistencias  $400\Omega$  y  $100\Omega$  están en paralelo, entonces:



Aplicamos el teorema de Thévenin:

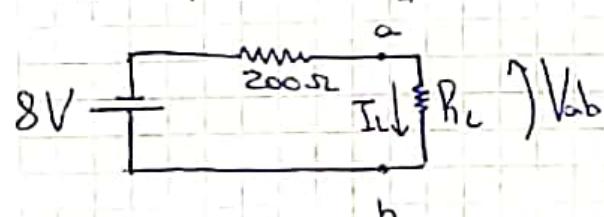


$$V_{TH} = 100 \text{ mA} \cdot 80 \Omega = -8 \text{ V}$$



$$R_{TH} = 80 \Omega + 120 \Omega = 200 \Omega$$

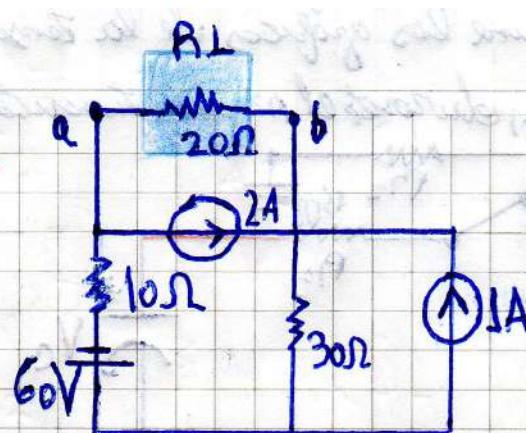
Entonces, tenemos que:



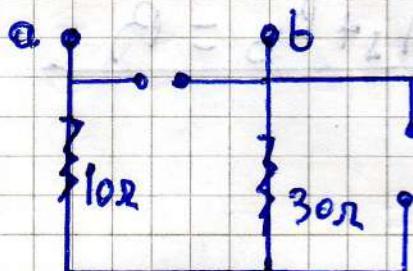
$$I_L = \frac{-8 \text{ V}}{200 \Omega + 160 \Omega} = 22,2 \text{ mA}$$

$$V_{RL} - V_{ab} = 8 \text{ V} \cdot \frac{160 \Omega}{200 \Omega + 160 \Omega} = 3,56 \text{ V}$$

## Ejercicio 1-3



Busco  $R_{TH}$  → Pongo fuentes.



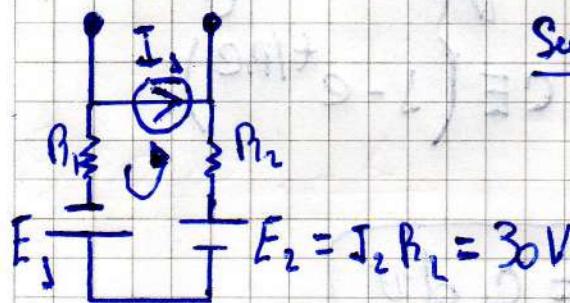
$$R_{TH} = 10\Omega + 30\Omega = 40\Omega$$

Busco  $V_{TH}$

Estoyezco el 0 del potenciómetro A y uso el equivalente de Norton →

$$\frac{V}{I} = \frac{1}{R_E} = \frac{1}{E - iR_1}$$

Sig de mallas de Kirchhoff:

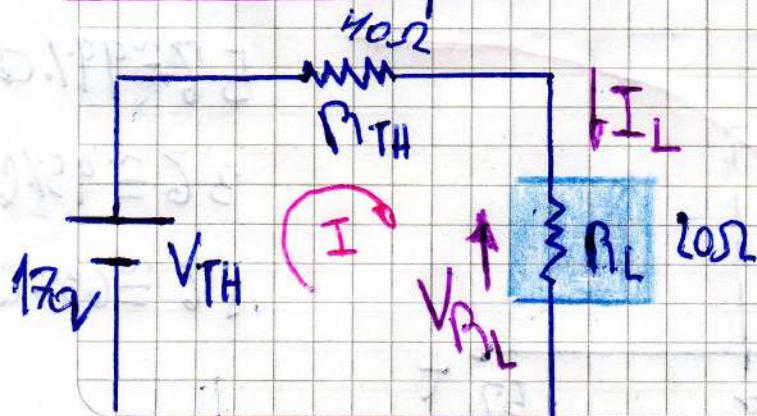


$$V_{AB} = V_{R1} + V_{R2} + E_1 + E_2$$

$$V_{R1} = I_1 R_1 = 24 \cdot 10\Omega = 240V \quad V_{R2} = 24 \cdot 20\Omega = 480V$$

$$V_{TH} = V_{AB} = 20V + 60V + 60V + 30V \Rightarrow V_{TH} = 170V$$

MICRUCTO QUEDA:



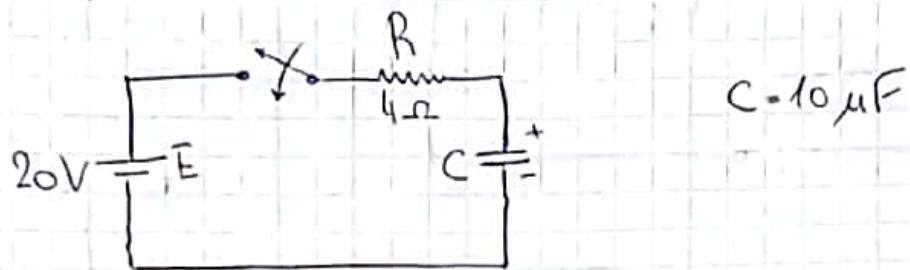
USO LEY DE OHM PARA SACAR  $I_L$

$$170V = I \cdot (40\Omega + 20\Omega)$$

$$I_L = 2,83A$$

$$V_{RL} = 20\Omega \cdot 2,83A = 56,66V$$

3)a)



Si la llave está abierta, el capacitor se mantiene descargado. Tomamos a  $t=0$  como el momento en el cual se cierra la llave.

Una vez cerrada la llave tenemos que:

$$E = V_R(t) + V_C(t); \quad V_R(t) = I(t) \cdot R = \frac{dV_C(t)}{dt} \cdot C \cdot R$$

$$\text{Entonces } E = \frac{dV_C(t)}{dt} C \cdot R + V_C(t)$$

$$\frac{E}{RC} = \frac{dV_C(t)}{dt} + \frac{V_C(t)}{RC}$$

$$\text{Sea } Z = RC \rightarrow \frac{E}{Z} = \frac{dV_C(t)}{dt} + \frac{V_C(t)}{Z}$$

$$\text{Propongo la solución } V_C(t) = A \cdot e^{-t/Z} + B$$

$$\text{Para } t \rightarrow \infty \quad V_C(t) = E \Rightarrow B = E$$

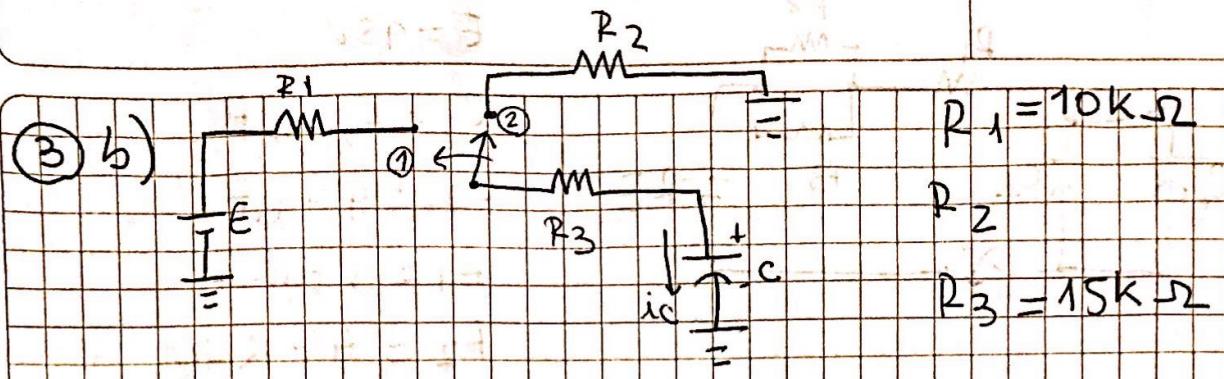
$$\text{Para } t \rightarrow 0 \quad V_C(t) = 0 \Rightarrow A + B = 0 \Rightarrow A = -E$$

$$\Rightarrow V_C(t) = -E e^{-t/Z} + E = E(1 - e^{-t/Z}) ; \quad Z = C \cdot R = 10\mu F \cdot 4\Omega = 40\mu s$$

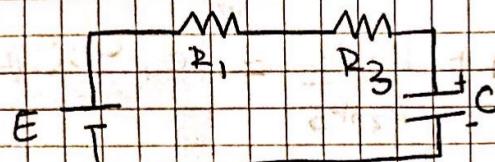
$$\boxed{V_C(t) = 20V (1 - e^{-t/40\mu s})}$$

$$\text{Luego, como } I(t) = \frac{dV_C(t)}{dt} \cdot C = \frac{20V}{40\mu s} e^{-t/40\mu s} \cdot 10\mu F$$

$$\boxed{I(t) = 5A e^{-t/40\mu s}}$$



• cuando la llave está en ①:



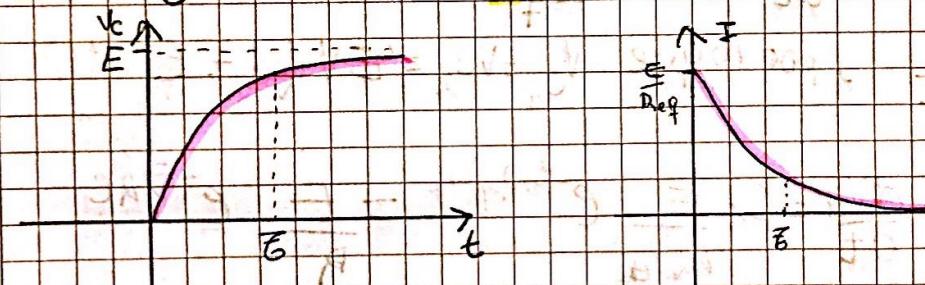
$$R_{eq} = R_1 + R_3$$

$$E = \frac{dQ}{dt} R_{eq} + \frac{Q}{C} \quad (Q(0)=0)$$

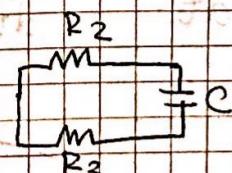
initialmente descargado

$$\Rightarrow Q = CE [1 - e^{-t/R_{eq}C}]$$

$$[V_C = \frac{Q}{C} = E [1 - e^{-t/R_{eq}C}]] \quad , \quad [I = \frac{dQ}{dt} = \frac{E}{R_{eq}} \cdot e^{-t/R_{eq}C}]$$



se carga  $C$   
hasta cargarse  
por completo,  
cuando  $V_C = E$

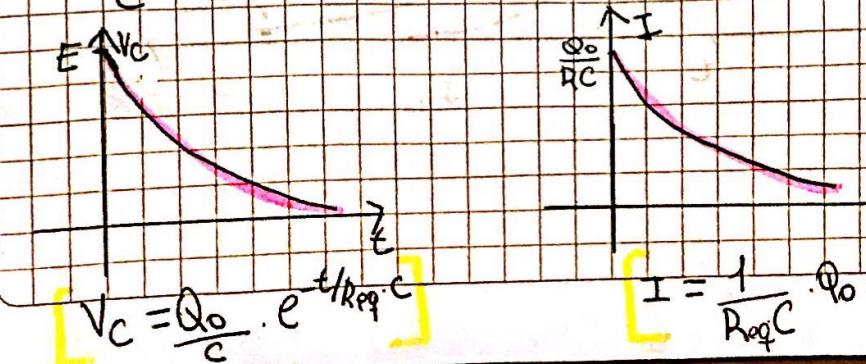


$$R_{eq} = R_2 + R_3$$

• Luego la llave pasa a ②:

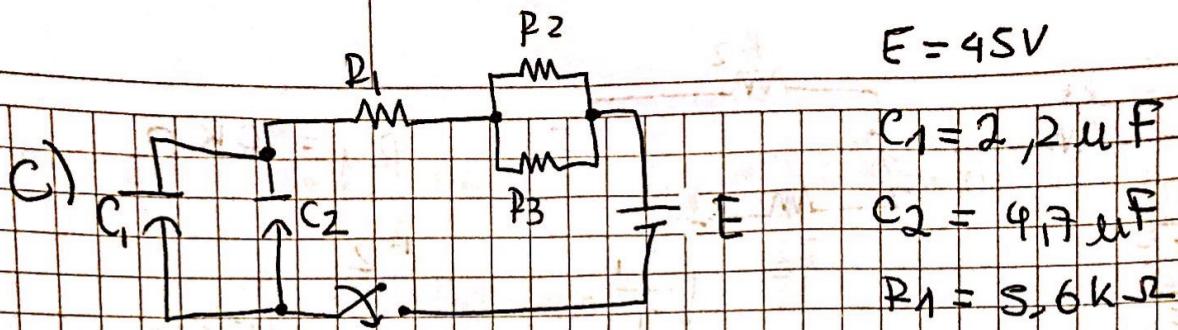
$Q(0) = E$  (capacitor inicialmente cargado)

$$\frac{Q}{C} = IR \quad , \quad I = \frac{dQ}{dt} \Rightarrow Q = Q_0 \cdot e^{-t/R_{eq}C}$$



$$[V_C = \frac{Q_0}{C} \cdot e^{-t/R_{eq}C}] \quad [I = \frac{1}{R_{eq}C} \cdot Q_0 \cdot e^{-t/R_{eq}C}]$$

Asamblea



$$E = 45V$$

$$C_1 = 2,2 \mu F$$

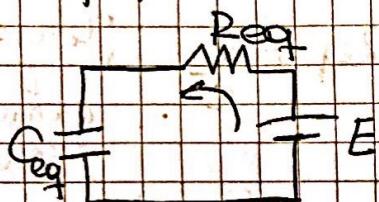
$$C_2 = 4,7 \mu F$$

$$R_1 = 5,6 k\Omega$$

$$R_2 = 47 k\Omega$$

$$R_3 = 39 k\Omega$$

Simplificando el circuito:



$$R_{eq} = R_1 + \frac{R_2 R_3}{R_2 + R_3} = 26,9 k\Omega$$

$$C_{eq} = C_1 + C_2 = 6,9 \mu F$$

$$E = 45V$$

$$\text{Entonces: } E = \frac{dQ}{dt} \cdot R_{eq} + \frac{Q}{C_{eq}} \Rightarrow Q = C E [1 - e^{-t/R_{eq} C_{eq}}]$$

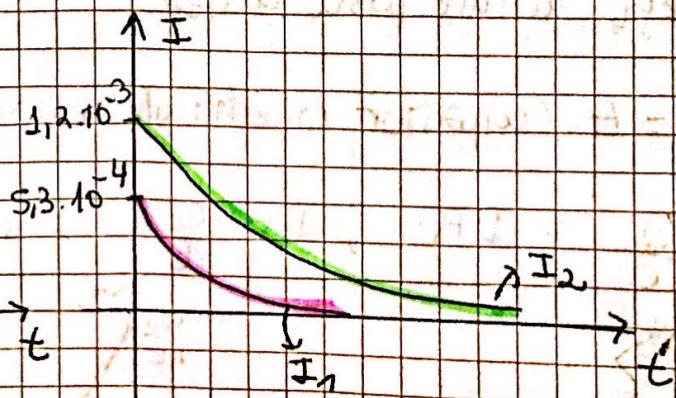
A demás

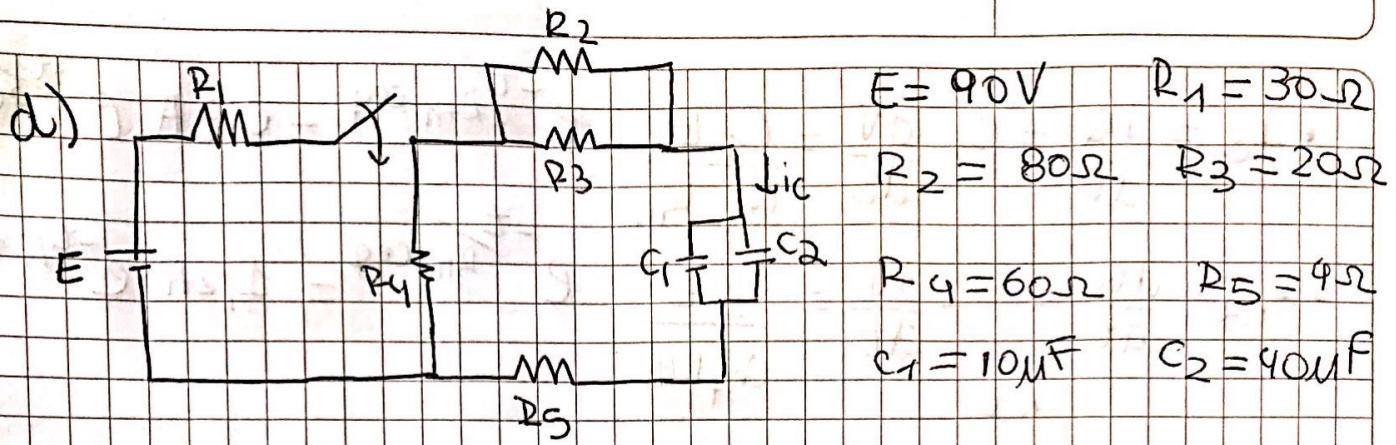
$$V_{C_{eq}} = V_{C_1} = V_{C_2} = \frac{Q}{C}, \text{ por lo que } V_{C_1} = V_{C_2} = 45V (1 - e^{-t/26,9 k\Omega \cdot 6,9 \mu F})$$

$$I_{C_1} = \frac{dQ_1}{dt} = C_1 \cdot \frac{dV_1}{dt} = C_1 \cdot \frac{E}{R_{eq} C_{eq}} \cdot e^{-t/R_{eq} C_{eq}}$$

$$I_{C_2} = \frac{dQ_2}{dt} = C_2 \frac{dV_2}{dt} = C_2 \cdot \frac{E}{R_{eq} C_{eq}} \cdot e^{-t/R_{eq} C_{eq}}$$

$$V_C \uparrow$$





Primero simplifico el circuito:



$$R_{eq} = \frac{R_2 R_3}{R_2 + R_3} + R_5 = 20\Omega$$

$$C_{eq} = C_1 + C_2 = 50\mu F$$

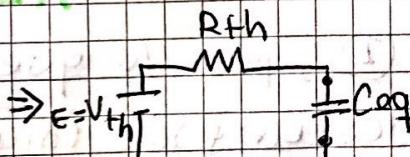
Ahora puedo aplicar thévenin:



$$R_{th} = \frac{R_1 R_4}{R_1 + R_4} + R_{eq} = 40\Omega$$

$$V_{th} = 60\Omega \cdot \frac{90V}{3\Omega + 60\Omega} = 60V$$

R.L.A



Donde

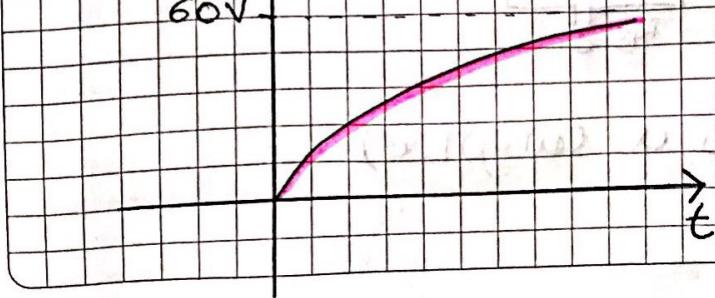
$$E = IR + \frac{Q}{C} = \frac{dQ}{dt} R_{th} + \frac{Q}{C_{eq}}$$

$$\Rightarrow Q = E \cdot C_{eq} \left( 1 - e^{-\frac{t}{R_{th} \cdot C_{eq}}} \right)$$

Entonces:

$$V_{C_{eq}} = V_{C_1} = V_{C_2} = \frac{Q}{C_{eq}} = E \left( 1 - e^{-\frac{t}{R_{th} \cdot C_{eq}}} \right) = 60V \left( 1 - e^{-\frac{t}{40\Omega \cdot 50\mu F}} \right)$$

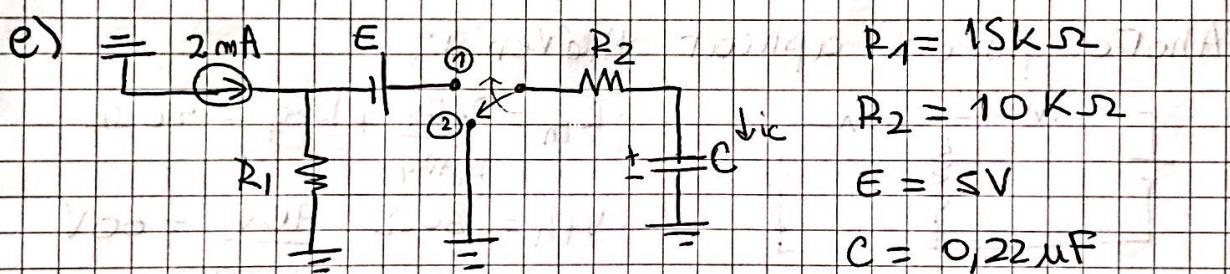
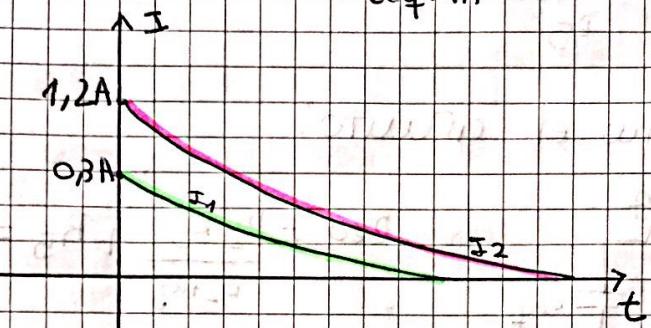
$V_C$   
60V



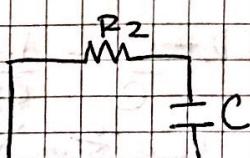
Asamblea

$$\bullet I_{C_1} = \frac{dQ}{dt} = C_1 \cdot \frac{dV}{dt} = \frac{C_1 E}{C_{eq} R_{th}} \cdot e^{-t/R_{th} \cdot C_{eq}} = 0,3 A \cdot e^{-t/2 \text{ ms}}$$

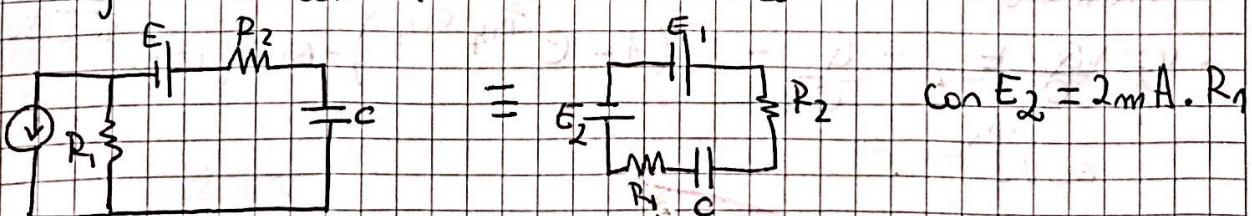
$$\bullet I_{C_2} = \frac{dQ}{dt} = C_2 \frac{dV}{dt} = \frac{C_2 E}{C_{eq} R_{th}} \cdot e^{-t/R_{th} \cdot C_{eq}} = 1,2 A \cdot e^{-t/2 \text{ ms}}$$



Primeramente la llave está en ②, por lo que el capacitor está descargado inicialmente



Luego se coloca la llave en ①:



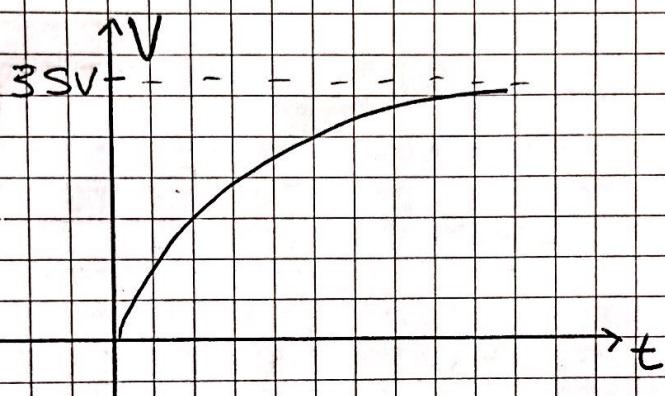
(El capacitor comienza a cargarse)

$$\text{Donde } E = \frac{Q}{C} + \frac{dQ}{dt} R$$

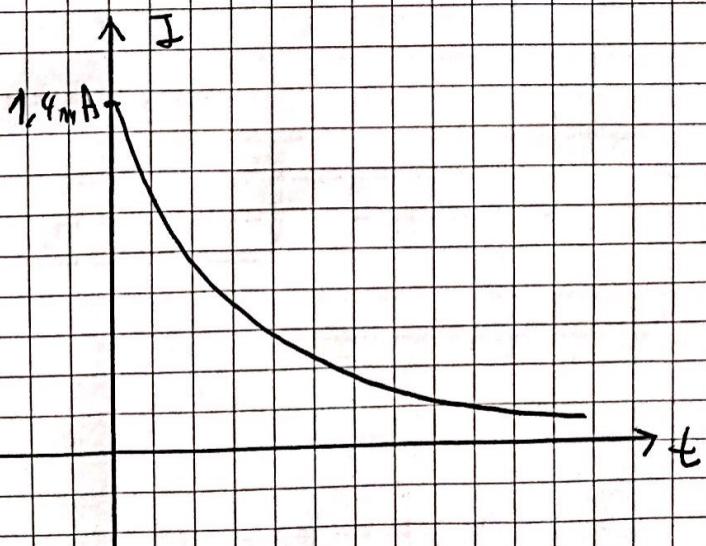
$$\Rightarrow Q = CE \cdot (1 - e^{-t/RC})$$

Entonces

$$\bullet V_c = \frac{Q}{C} = E(1 - e^{-t/RC}) = (5V + 30V) \cdot (1 - e^{-\frac{t}{25k\Omega \cdot 0,22\mu F}})$$

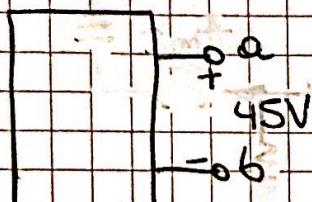


$$\bullet I_c = \frac{dQ}{dt} = \frac{E}{R} \cdot e^{-t/RC} = \frac{35V}{25k\Omega} \cdot e^{-\frac{t}{25k\Omega \cdot 0,22\mu F}}$$



④ Una caja negra contiene resistores y fuentes.

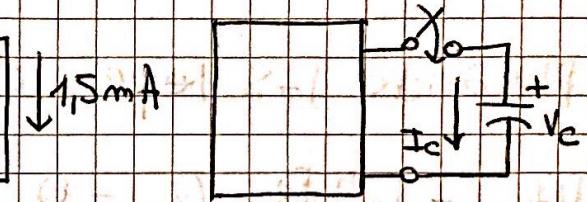
Sela mide externamente y se obtienen los valores indicados. Luego se le conecta un capacitor de  $500\text{nF}$  mediante una llave. Determinar el valor de la corriente en el capacitor 25 s después de conectar la llave.



(a)

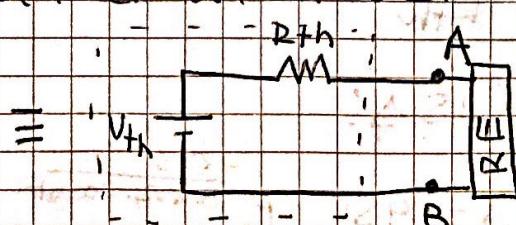
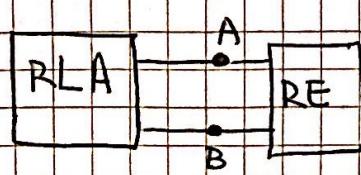


(b)

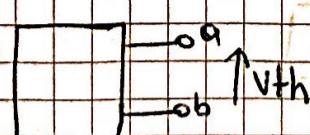


(c)

Usando el teorema de Thévenin, podemos pensar la caja como la red lineal activa

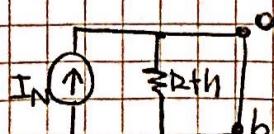


Entonces por (a)  $V_{th} = 45V$ .



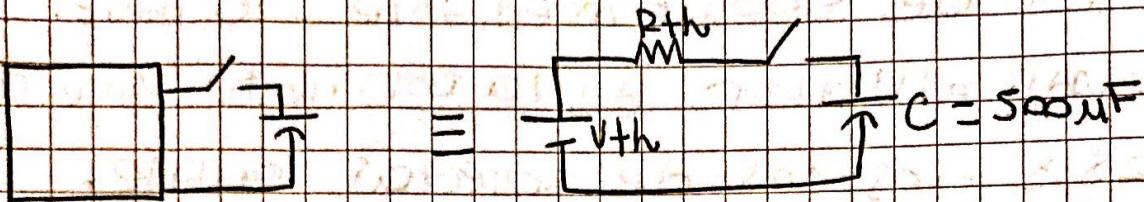
Análogamente, usando el teorema de Norton, por (b)

$$I_N = 1.5 \text{ mA}$$



$$\text{Además } R_{th} = \frac{V_{th}}{I_N} = \frac{45V}{15mA} = 30k\Omega$$

Entonces (c) es equivalente a:



Aplicando las leyes de Kirchoff:

$$V_{th} - IR_{th} - \frac{Q}{C} = 0, \quad I = \frac{dQ}{dt}$$

$$\Rightarrow Q = C V_{th} [1 - e^{(-t)/R_{th} \cdot C}]$$

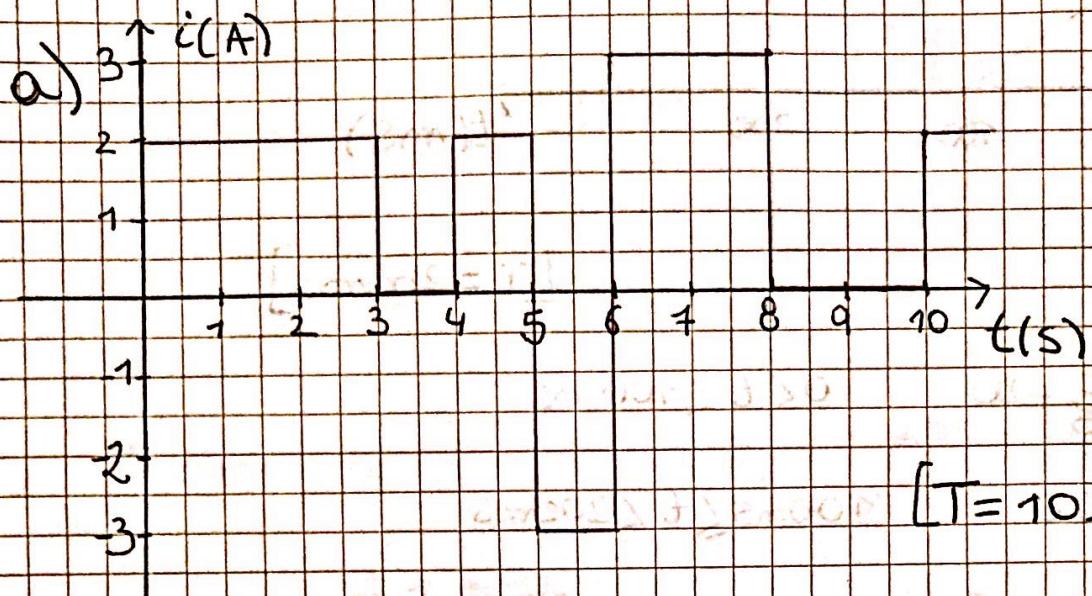
$$\Rightarrow I = \frac{V_{th}}{R_{th}} e^{-t/R_{th} \cdot C}$$

para  $t = 25s$ :

$$I(25s) = \frac{45V}{30k\Omega} \cdot e^{-\frac{25s}{30k\Omega \cdot 500\mu F}}$$

$$[I(25s) = 0,203mA]$$

5) Determine los valores medio y eficaz de cada una de las formas de onda



Sabiendo que  $I_{\text{Medio}} = \frac{1}{T} \cdot \int_0^T I dt$  y teniendo la función partida  $I(t)$ :

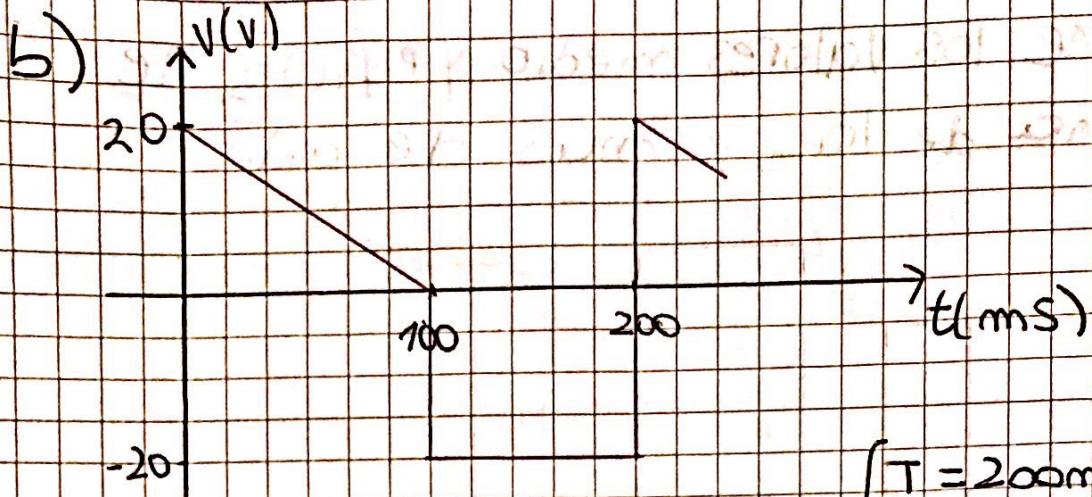
$$I_{\text{Medio}} = \frac{1}{10} \cdot \left[ \int_0^3 2 dt + \int_3^4 0 \cdot dt + \int_4^5 2 dt + \int_5^6 (-3) dt + \int_6^8 3 dt + \int_8^{10} 0 \cdot dt \right]$$

$$\Rightarrow I_{\text{Medio}} = \frac{1}{10} \cdot 11A = 1,1A$$

Por otro lado  $I_{\text{ef}} = \sqrt{\frac{1}{T} \cdot \int_0^T I^2 dt}$ , entonces:

$$I_{\text{ef}} = \sqrt{\frac{1}{10} \cdot \int_0^{10} I^2 dt} = \sqrt{\frac{1}{10} \cdot \left( \int_0^3 2^2 dt + \int_3^4 2^2 dt + \int_4^5 2^2 dt + \int_5^6 (-3)^2 dt + \int_6^8 3^2 dt \right)}$$

$$\Rightarrow I_{\text{ef}} = \sqrt{\frac{43}{10}} \approx 2,074A$$



$$V(t) = \begin{cases} -\frac{t}{5} + 20 & 0 < t < 100 \text{ ms} \\ -20 & 100 \text{ ms} \leq t < 200 \text{ ms} \end{cases}$$

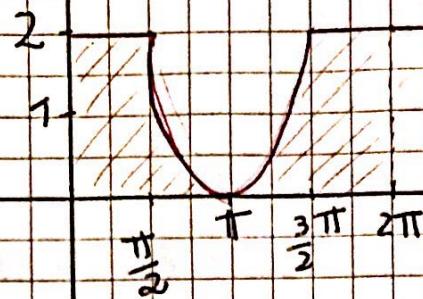
$$\cdot V_{\text{medio}} = \frac{1}{T} \int_0^T V(t) dt = \frac{1}{200} \left[ \int_0^{100} \left( -\frac{t}{5} + 20 \right) dt + \int_{100}^{200} (-20) dt \right]$$

$$[V_{\text{medio}} = \frac{1}{200} \cdot (-1000) = -5 \text{ V}]$$

$$\cdot V_{\text{ef}} = \sqrt{\frac{1}{T} \int_0^T V^2 dt} = \sqrt{\frac{1}{200} \left( \int_0^{100} \left( -\frac{t}{5} + 20 \right)^2 dt + \int_{100}^{200} (-20)^2 dt \right)}$$

$$[V_{\text{ef}} = \sqrt{\frac{1}{200} \cdot \frac{160000}{3}} \approx 16,33 \text{ V}]$$

c)  $\uparrow i(A)$



$$[T = 2\pi]$$

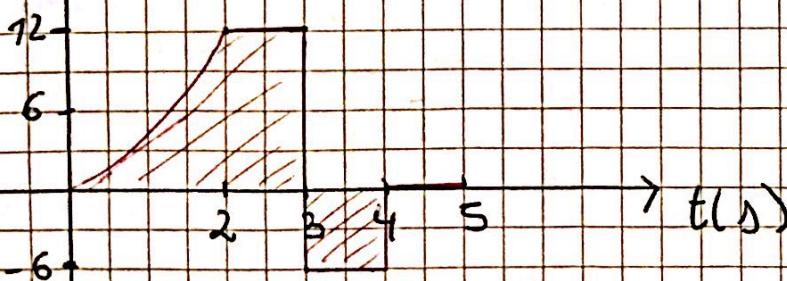
$$\cdot I_{\text{Medio}} = \frac{1}{T} \int_0^T i dt = \frac{1}{2\pi} \cdot \left[ \int_0^{\frac{\pi}{2}} 2 dt + \int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} (2 \cos(t) + 2) dt + \int_{\frac{3\pi}{2}}^{2\pi} 2 dt \right]$$

$$[I_{\text{Medio}} \approx 1,36 A]$$

$$\cdot I_{\text{ef}} = \sqrt{\frac{1}{T} \int_0^T i^2 dt} = \sqrt{\frac{1}{2\pi} \left( \int_0^{\frac{\pi}{2}} 2^2 dt + \int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} (2 \cos(t) + 2)^2 dt \right)}$$

$$[I_{\text{ef}} \approx 1,57 A]$$

d)  $\uparrow v(V)$



$$[T = 4 s]$$

$$v(t) = \begin{cases} 3t^2 & 0 < t < 2 \\ 12 & 2 \leq t < 4 \\ -6 & 4 \leq t < 6 \end{cases}$$

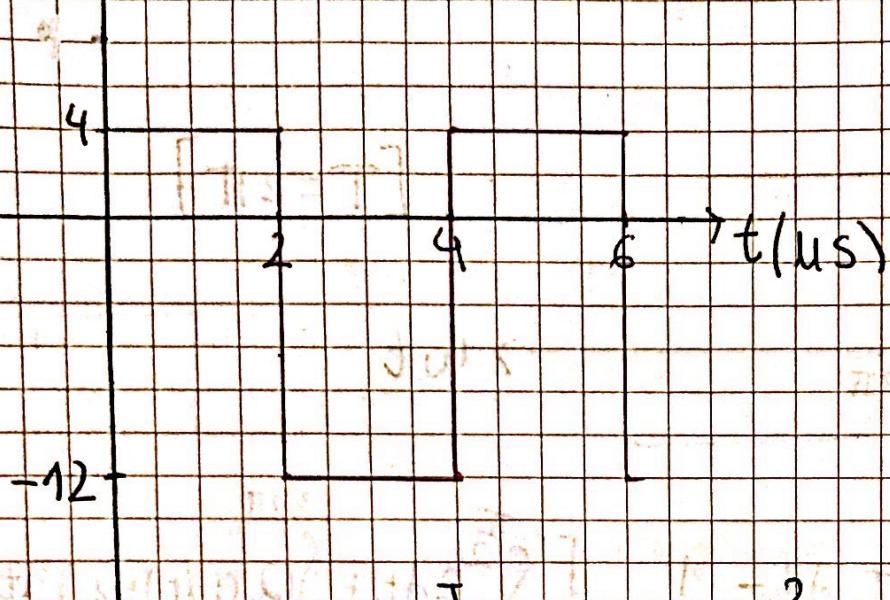
$$\cdot V_{\text{Medio}} = \frac{1}{T} \int_0^T v dt = \frac{1}{4} \left( \int_0^2 3t^2 dt + \int_2^4 (-6) dt + \int_4^6 12 dt \right)$$

$$[V_{\text{Medio}} = 3,5 V]$$

$$\cdot V_{\text{ef}} = \sqrt{\frac{1}{T} \left( \int_0^T v^2 dt \right)} = \sqrt{\frac{1}{4} \left( \int_0^2 (3t^2)^2 dt + \int_2^4 (-6)^2 dt + \int_4^6 12^2 dt \right)}$$

$$[V_{\text{ef}} \approx 7,7 V]$$

e)  $\uparrow i(t)$



$$\cdot I_{\text{Medio}} = \frac{1}{T} \int_0^T i dt = \frac{1}{6} \left( \int_0^2 4 dt + \int_2^4 (-12) dt + \int_4^6 4 dt \right)$$

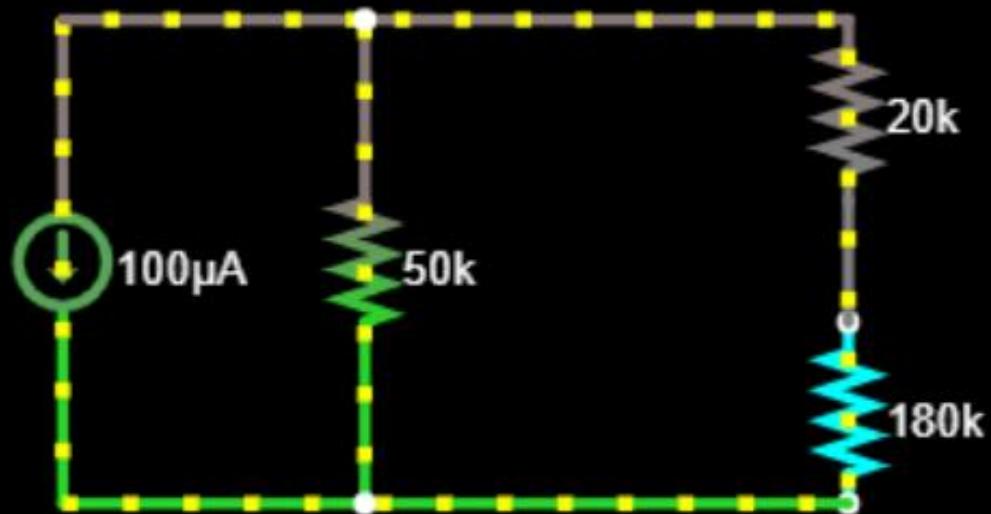
$$[I_{\text{Medio}} \approx -1,33 \text{ A}]$$

$$\cdot I_{\text{ef}} = \sqrt{\frac{1}{T} \cdot \int_0^T i^2 dt} = \sqrt{\frac{1}{6} \left( \int_0^2 4^2 dt + \int_2^4 (-12)^2 dt + \int_4^6 4^2 dt \right)}$$

$$[I_{\text{ef}} \approx 7,66 \text{ A}]$$

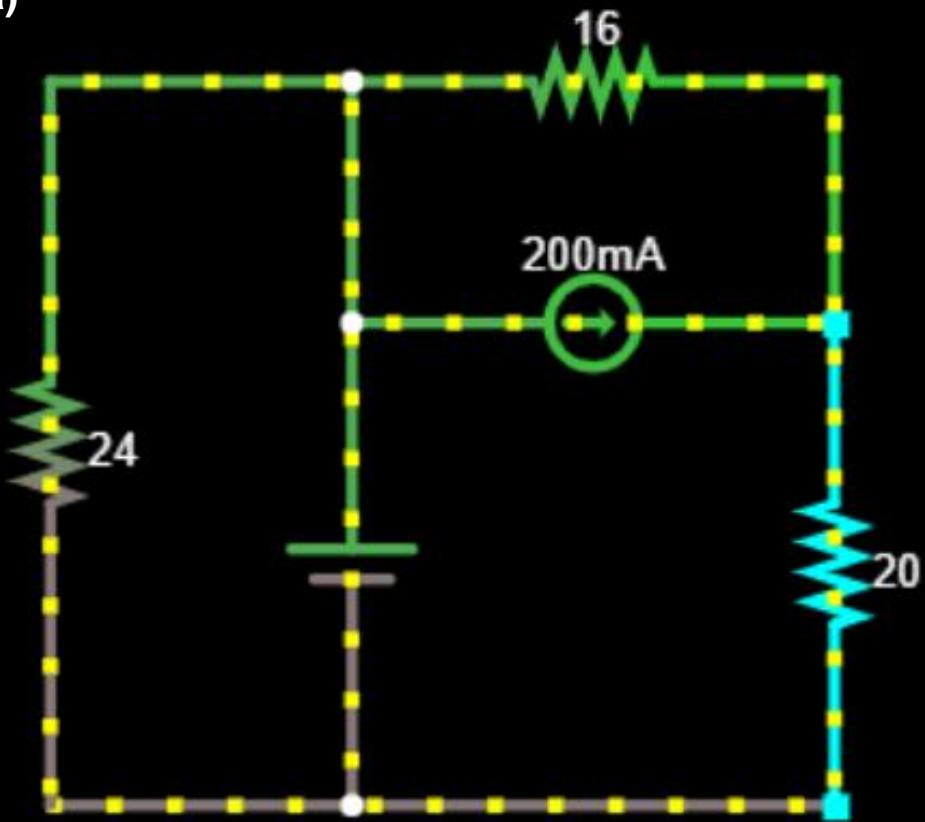
# Anexo: **SIMULACIONES**

## Ejercicio 1A



resistor  
 $I = 20 \mu A$   
 $V_d = 3.6 V$   
 $R = 180 k\Omega$   
 $P = 72 \mu W$

Ejercicio 1B a)



resistor

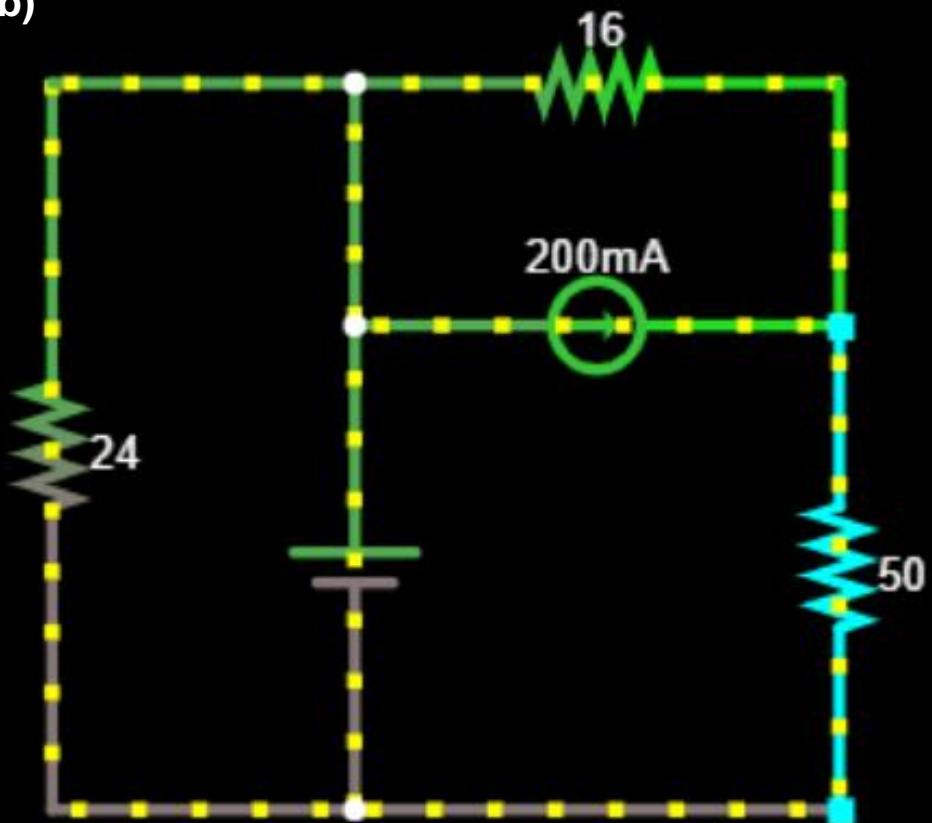
$$I = 155.556 \text{ mA}$$

$$V_d = 3.111 \text{ V}$$

$$R = 20 \Omega$$

$$P = 483.951 \text{ mW}$$

Ejercicio 1B b)



resistor

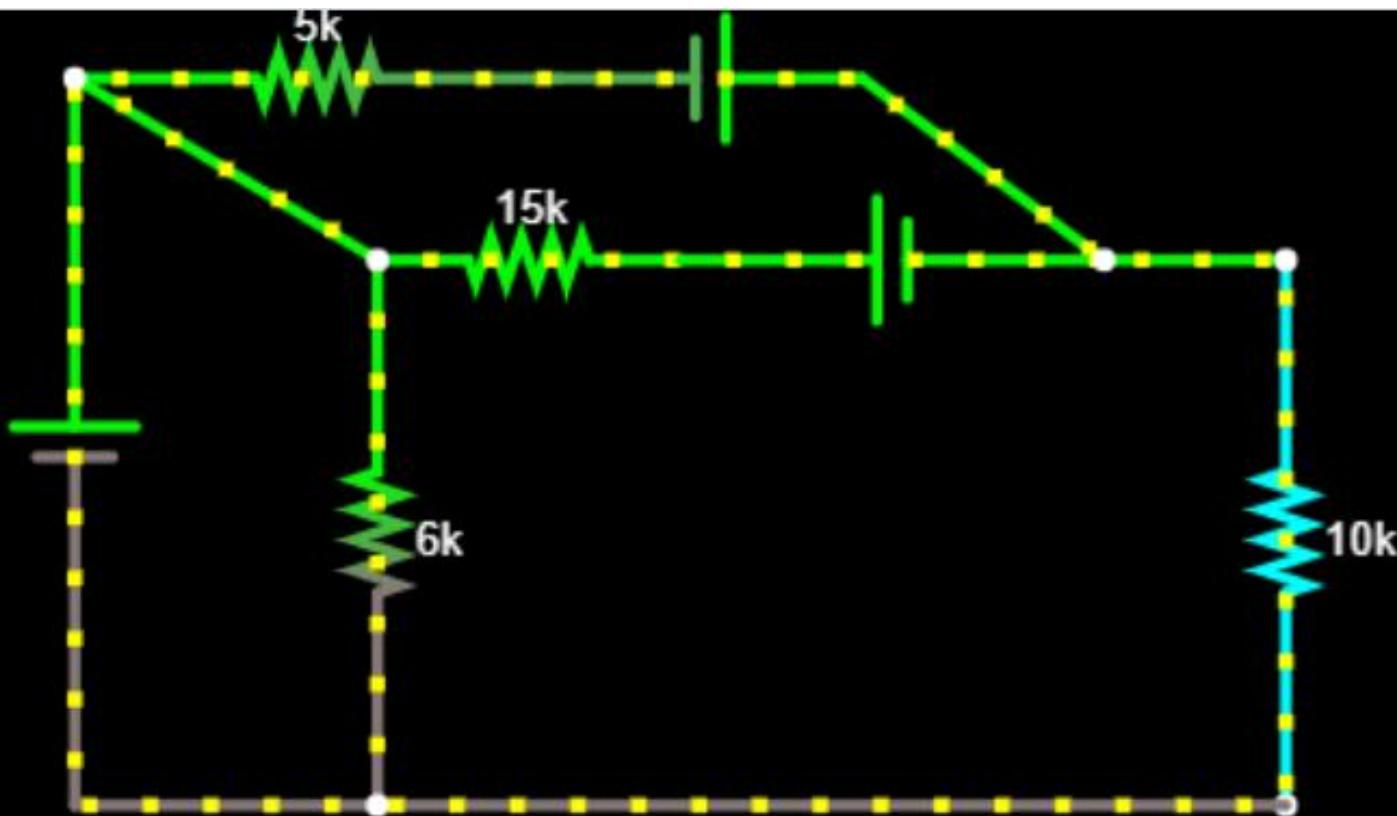
$$I = 84.848 \text{ mA}$$

$$V_d = 4.242 \text{ V}$$

$$R = 50 \Omega$$

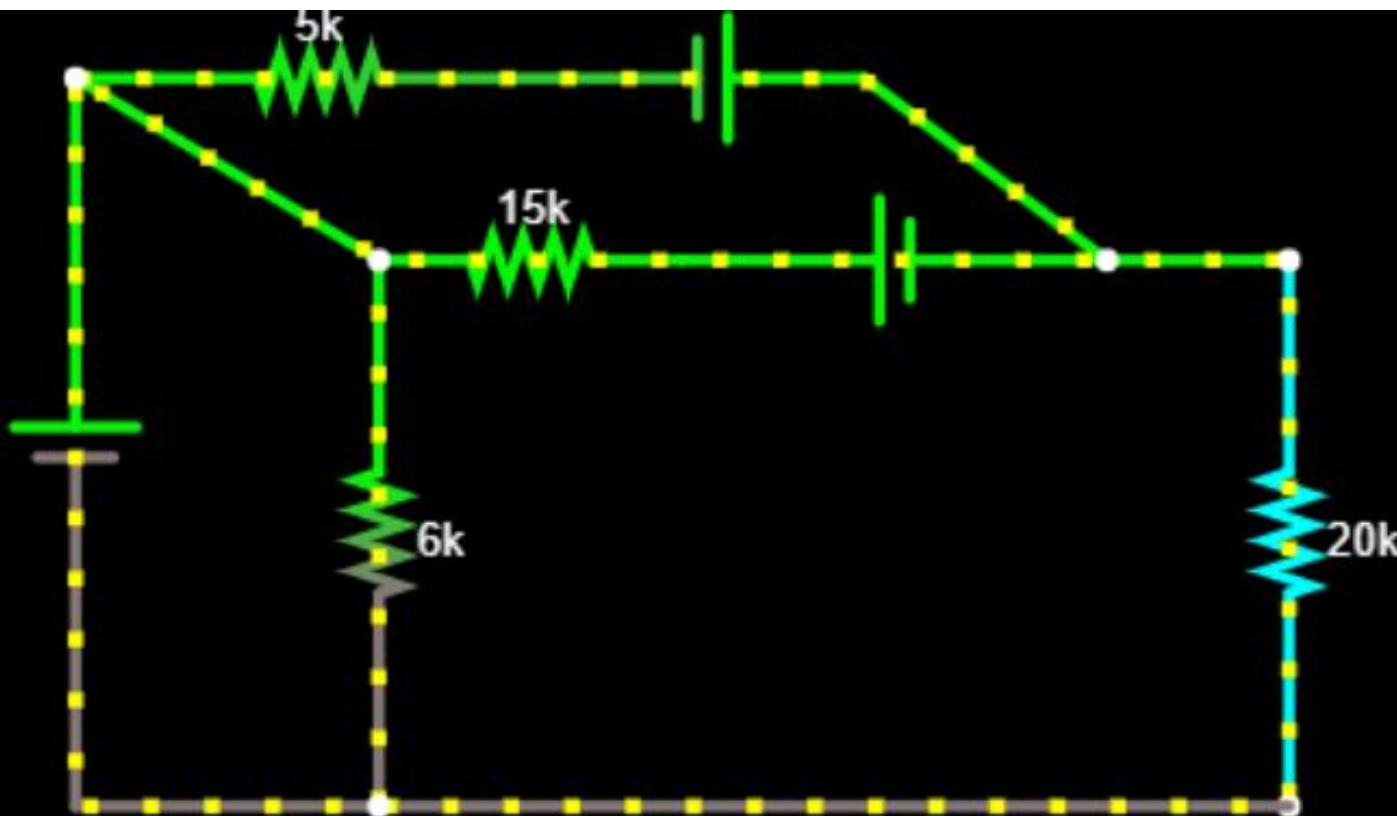
$$P = 359.963 \text{ mW}$$

Ejercicio 1C a)



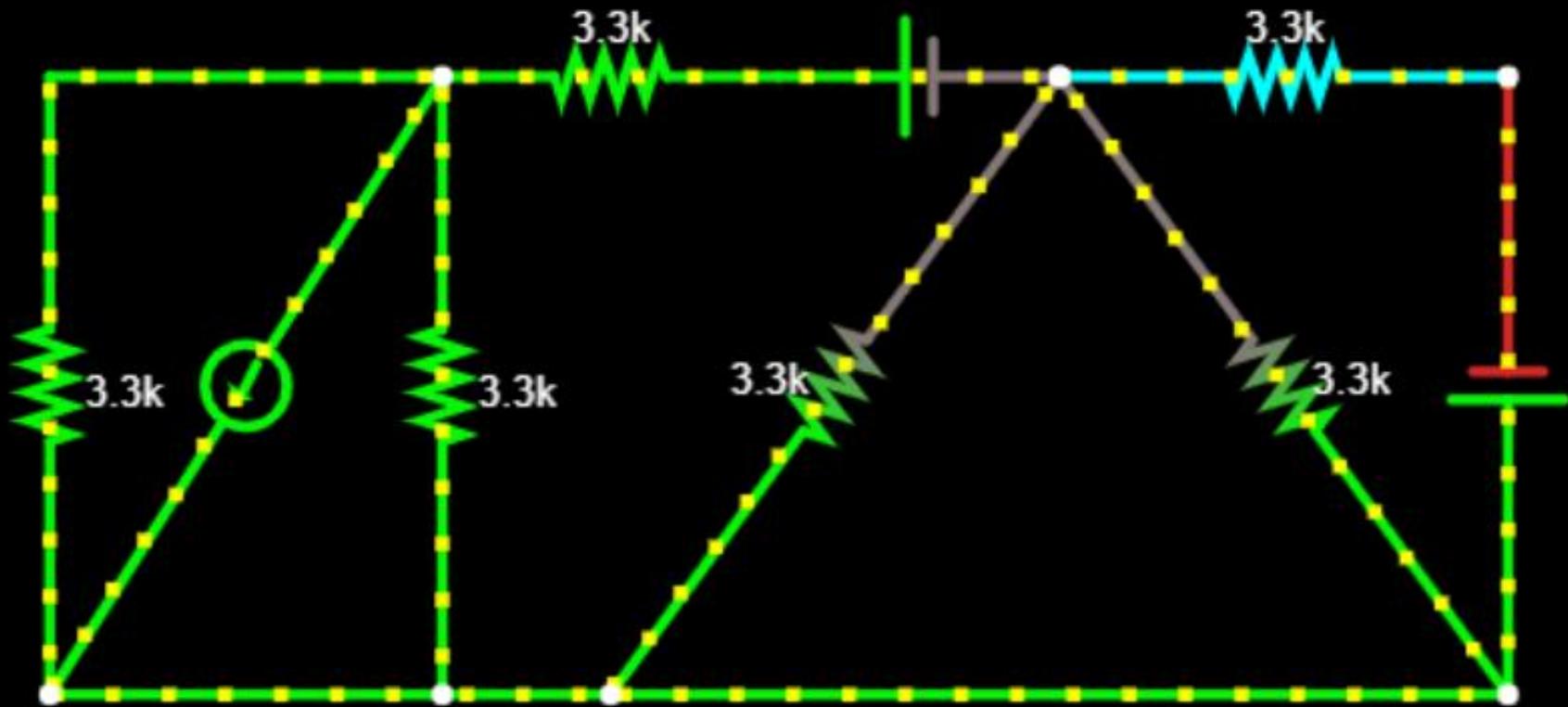
resistor  
 $I = 836.364 \mu\text{A}$   
 $V_d = 8.364 \text{ V}$   
 $R = 10 \text{ k}\Omega$   
 $P = 6.995 \text{ mW}$

Ejercicio 1C b)



resistor  
 $I = 484.211 \mu\text{A}$   
 $V_d = 9.684 \text{ V}$   
 $R = 20 \text{ k}\Omega$   
 $P = 4.689 \text{ mW}$

## Ejercicio 1D



resistor

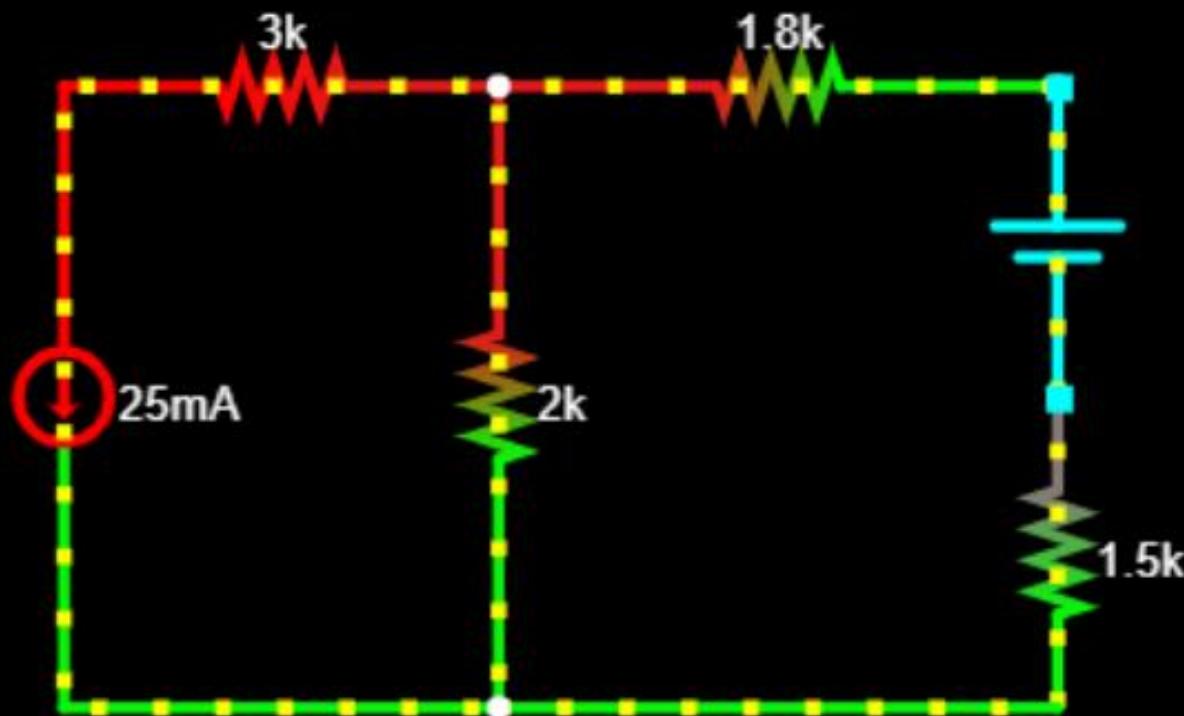
$$I = 1.017 \text{ mA}$$

$$V_d = 3.355 \text{ V}$$

$$R = 3.3 \text{ k}\Omega$$

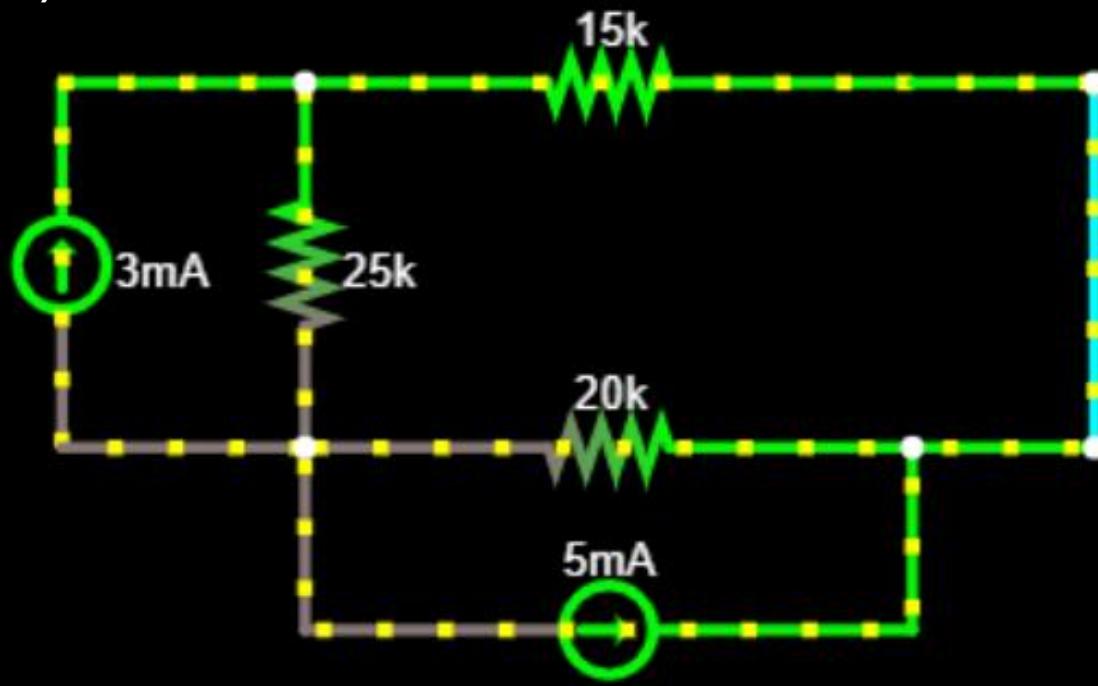
$$P = 3.41 \text{ mW}$$

## Ejercicio 1E



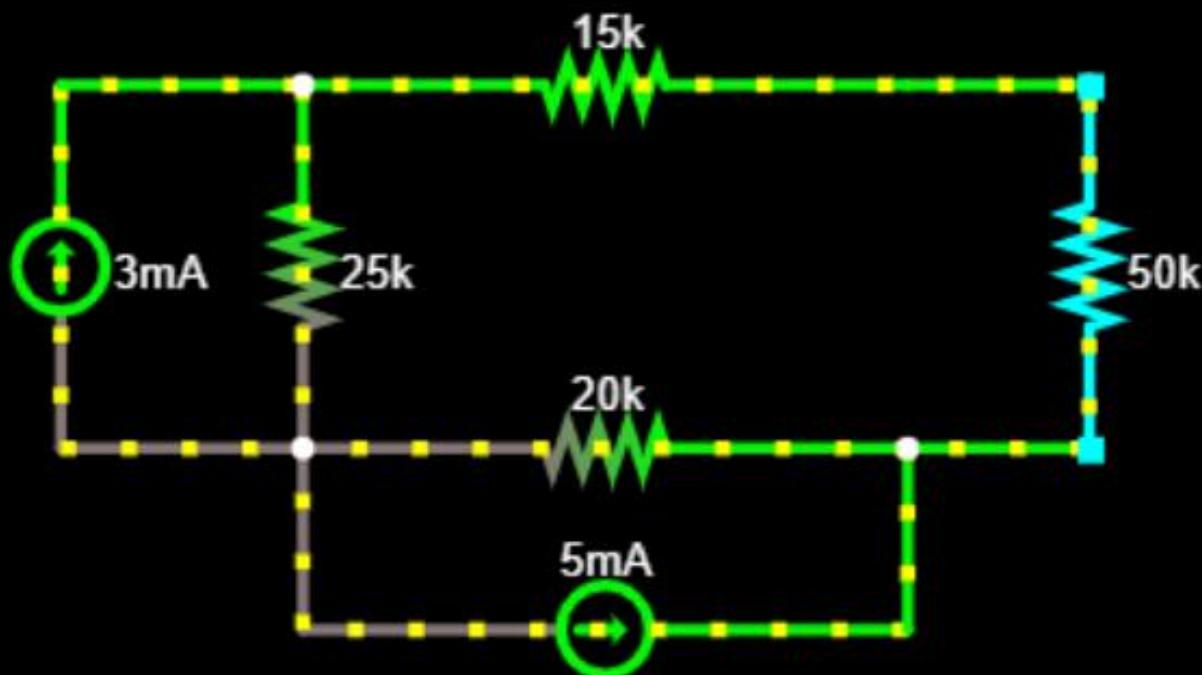
voltage source  
 $I = 13.208 \text{ mA}$   
 $V_d = 20 \text{ V}$   
 $(R = 1.514 \text{ k}\Omega)$   
 $P = -264.151 \text{ mW}$

Ejercicio 1G a)



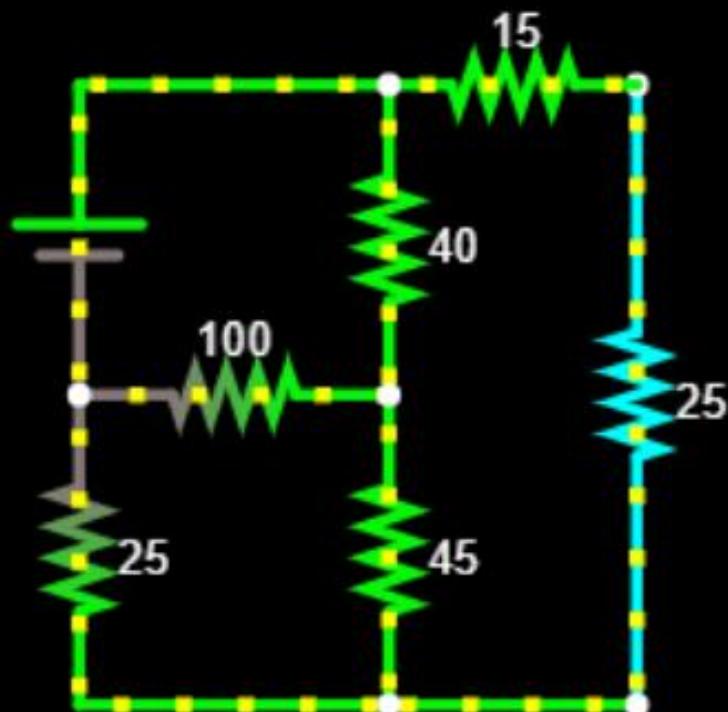
wire  
 $I = 416.667 \mu\text{A}$   
 $V = 91.667 \text{ V}$

Ejercicio 1G b)



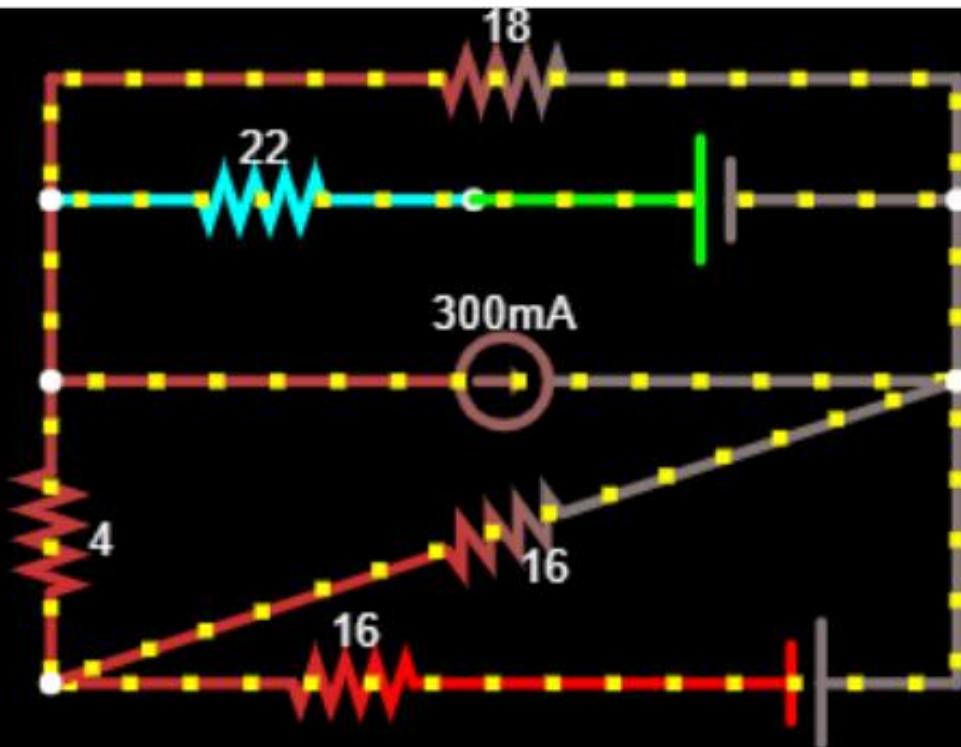
resistor  
 $I = 227.273 \mu\text{A}$   
 $V_d = 11.364 \text{ V}$   
 $R = 50 \text{ k}\Omega$   
 $P = 2.583 \text{ mW}$

## Ejercicio 1H



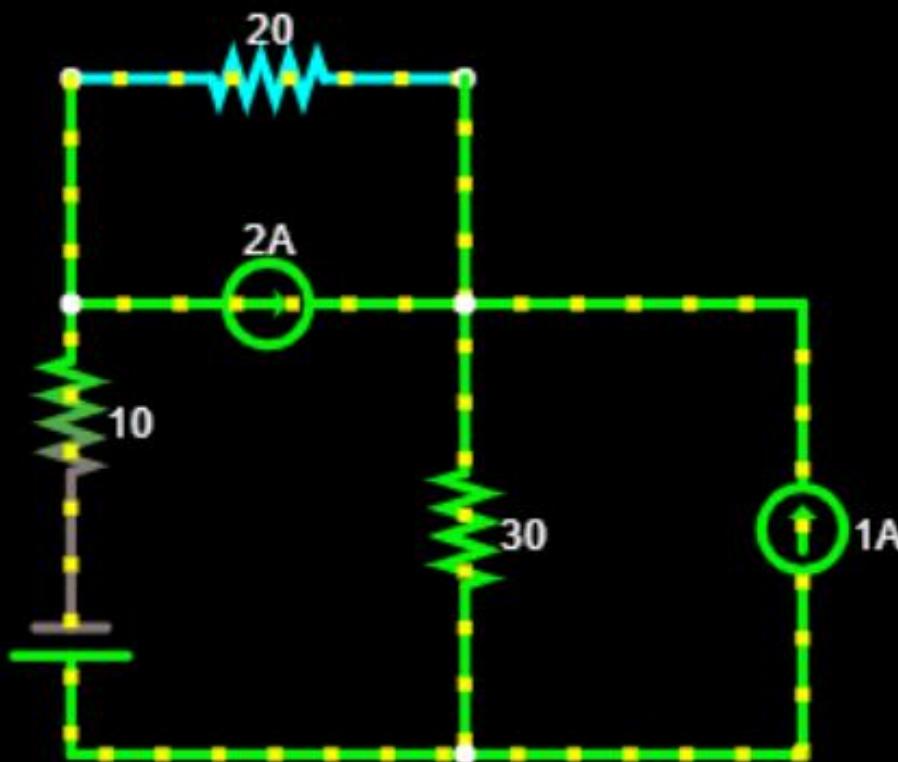
resistor  
 $I = 223.348 \text{ mA}$   
 $V_d = 5.584 \text{ V}$   
 $R = 25 \Omega$   
 $P = 1.247 \text{ W}$

### Ejercicio 1i



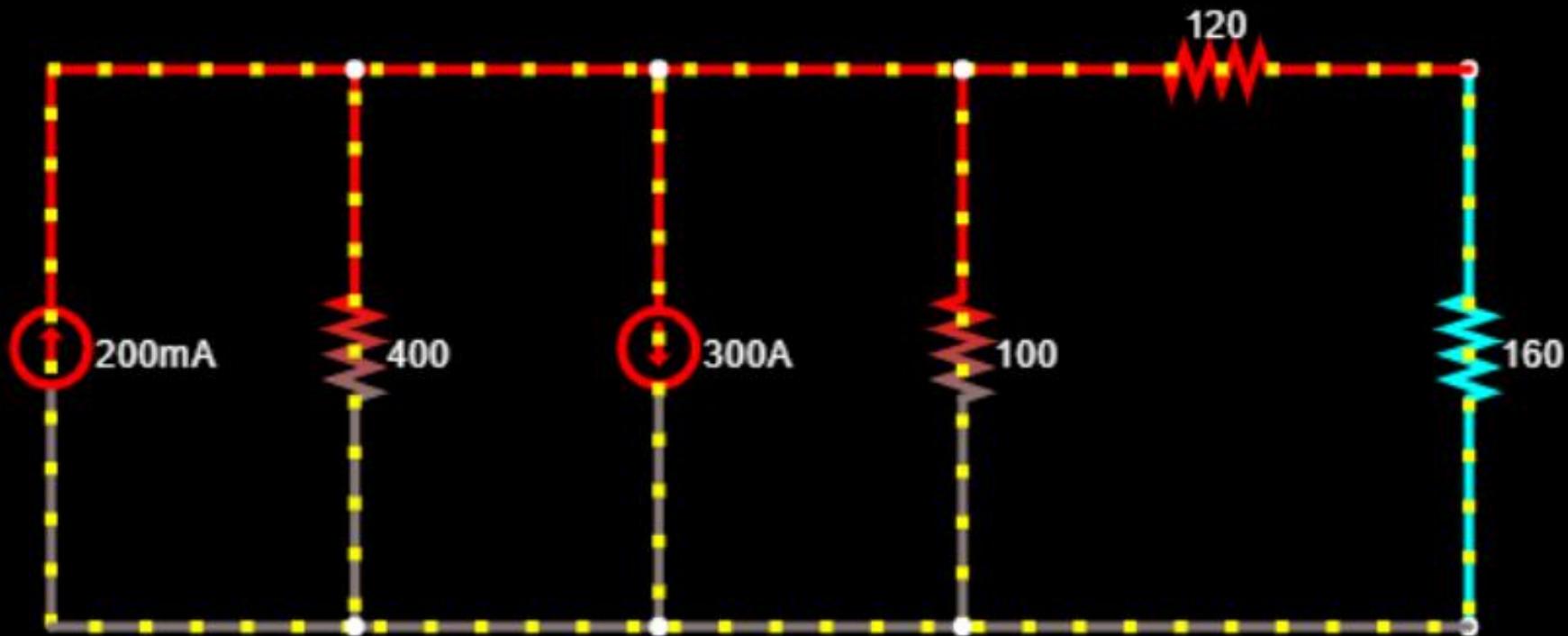
resistor  
 $I = 327.397 \text{ mA}$   
 $V_d = 7.203 \text{ V}$   
 $R = 22 \Omega$   
 $P = 2.358 \text{ W}$

## Ejercicio 1J



resistor  
 $I = 2.833\text{ A}$   
 $V_d = 56.667\text{ V}$   
 $R = 20\ \Omega$   
 $P = 160.556\text{ W}$

## Ejercicio 1K



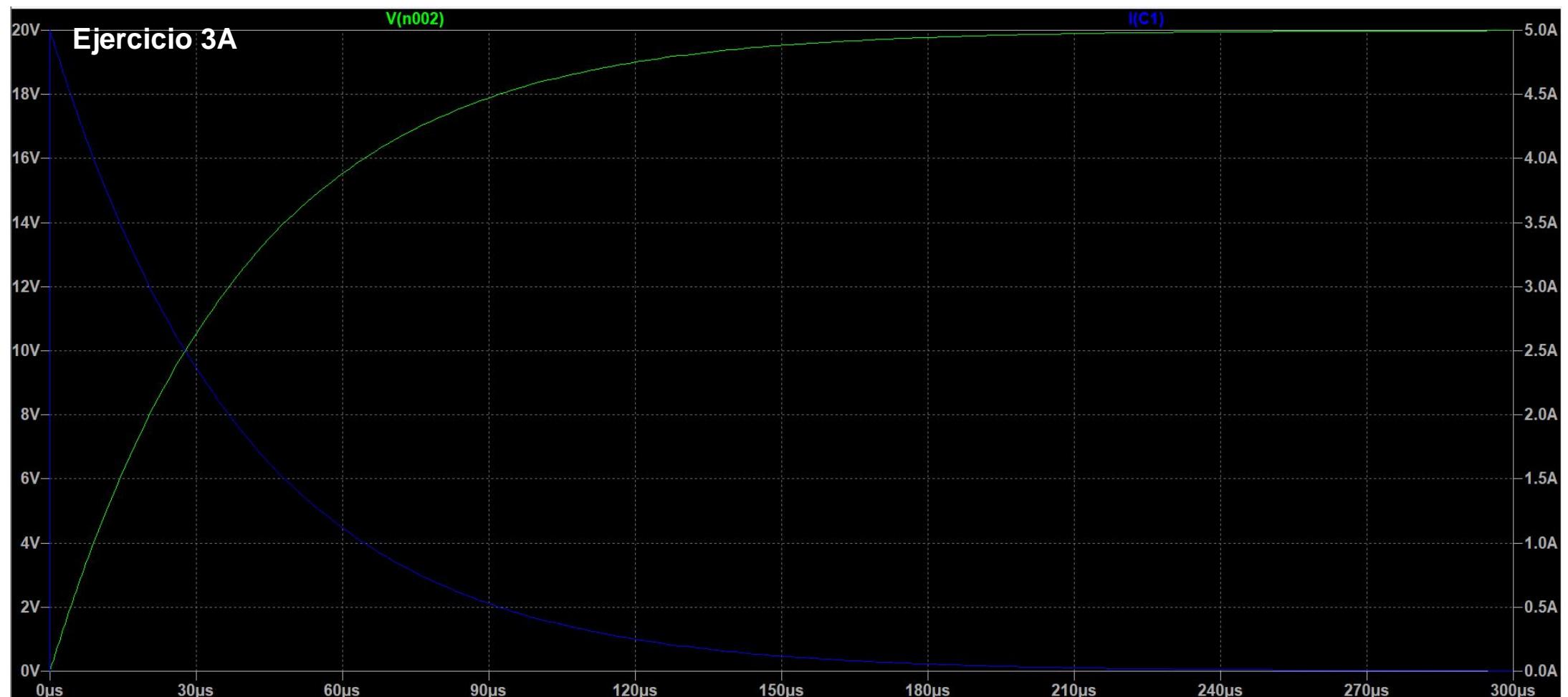
resistor

$$I = 66.622 \text{ A}$$

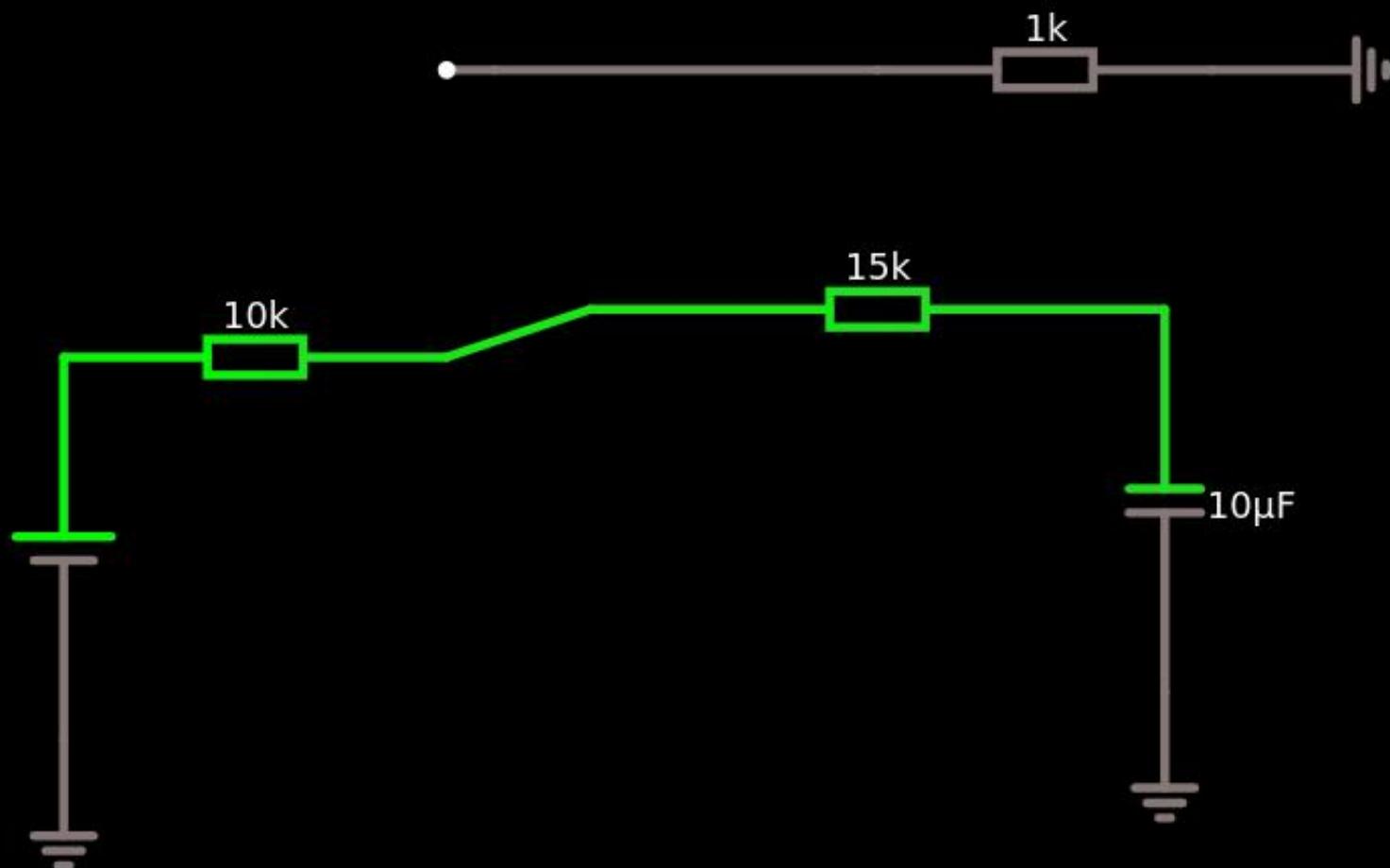
$$V_d = 10.66 \text{ kV}$$

$$R = 160 \Omega$$

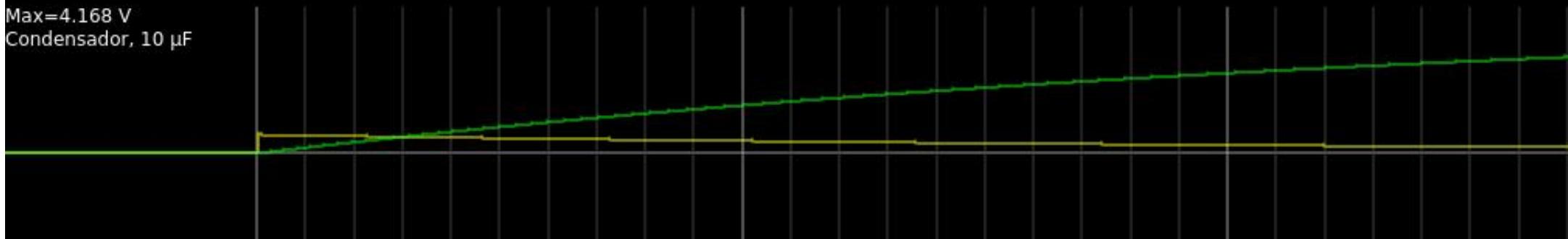
$$P = 710.163 \text{ kW}$$



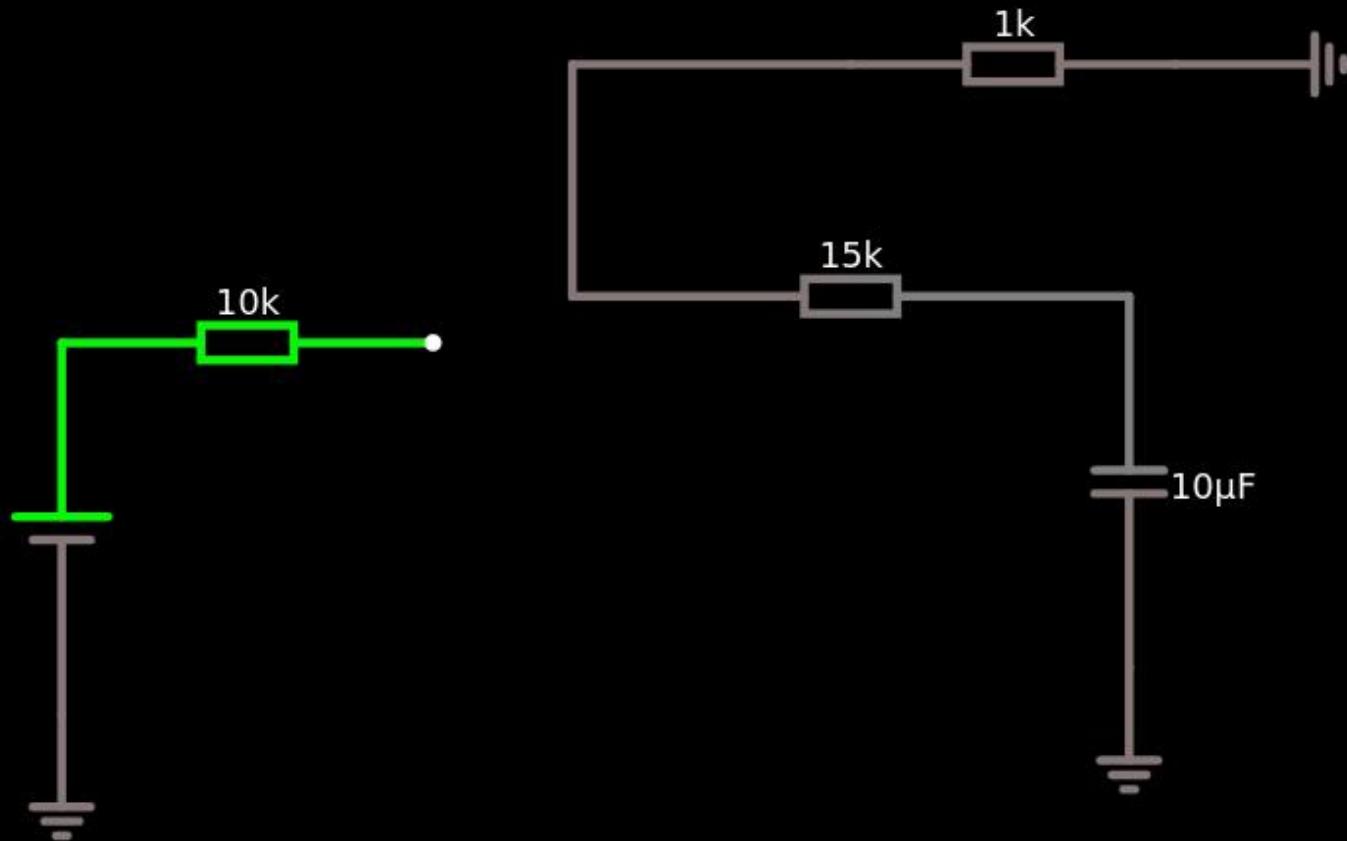
### Ejercicio 3B a)



Max=4.168 V  
Condensador,  $10 \mu\text{F}$

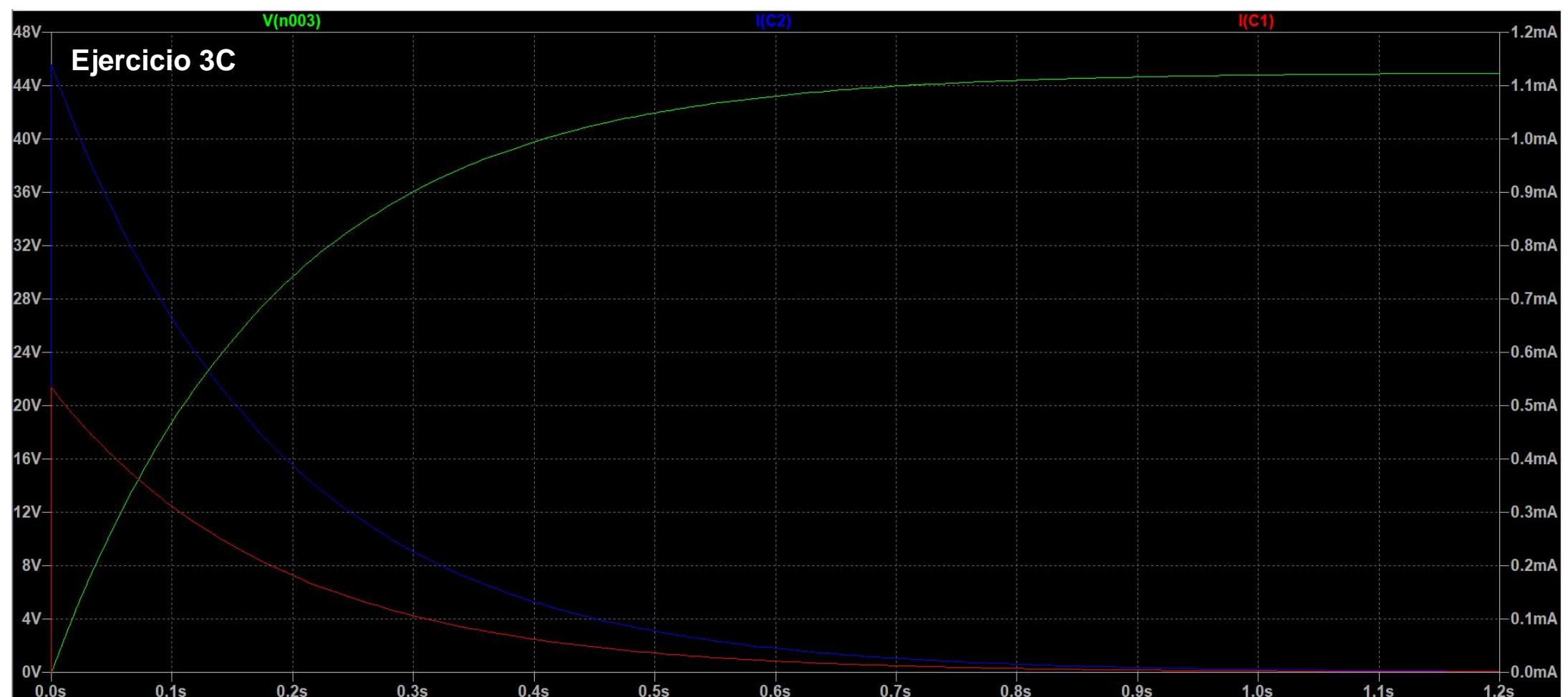


### Ejercicio 3B b)

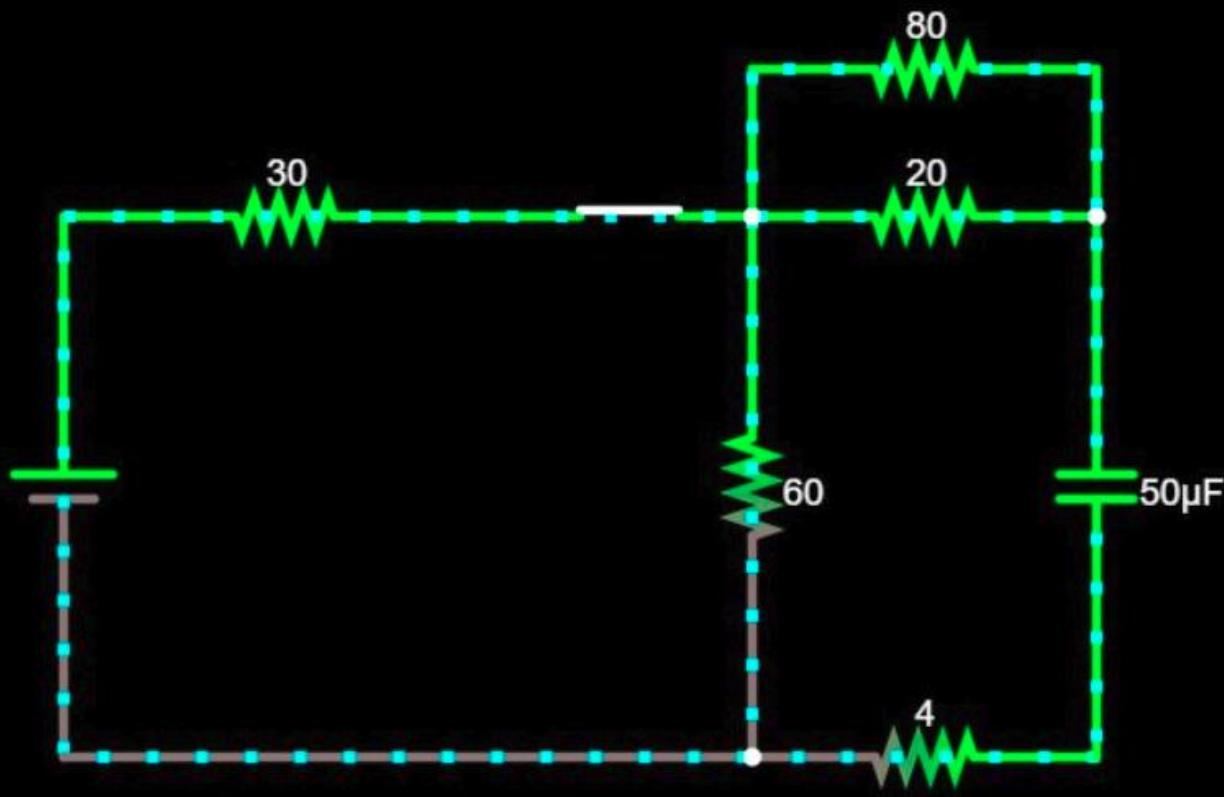


$I_{max} = 2.584 \text{ V}$   
condensador, 10  $\mu\text{F}$





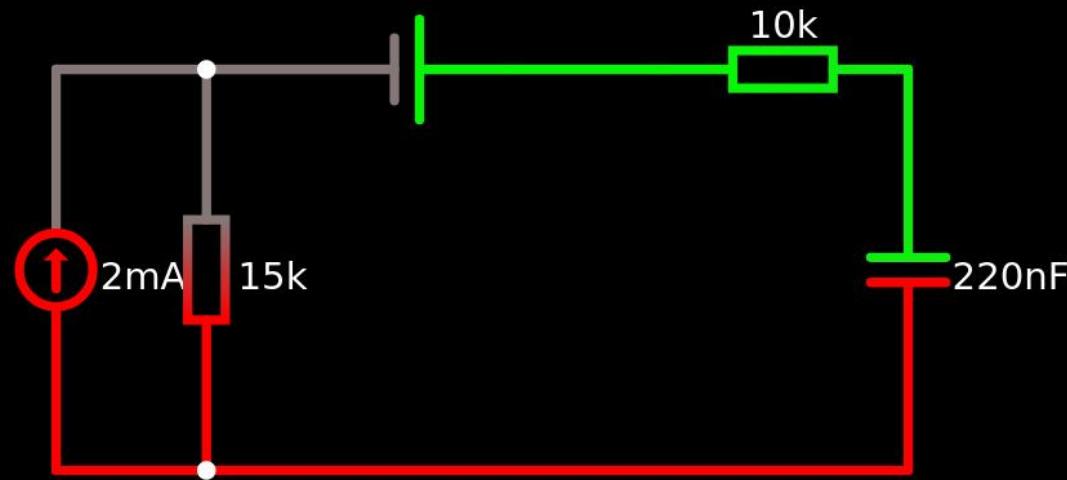
### Ejercicio 3D



60 V  
capacitor, 50  $\mu\text{F}$



### Ejercicio 3E



Max=35 V  
Condensador, 220 nF

t = 167.315 ms  
intervalo tiempo = 5  $\mu$ s

