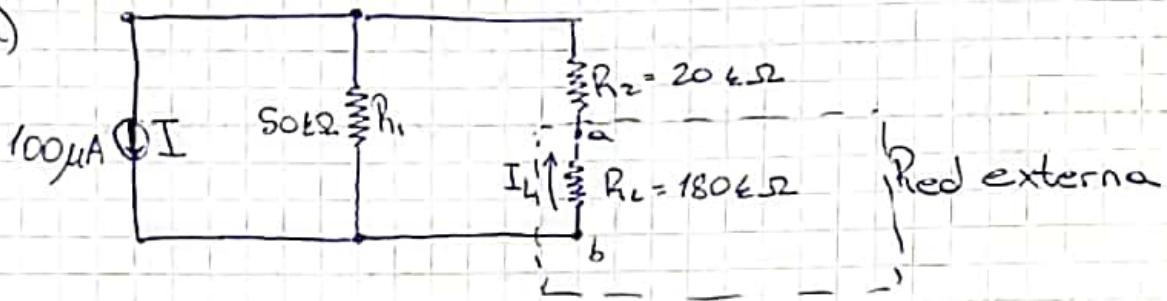
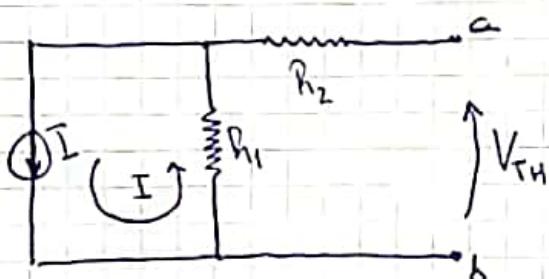


1) Obtenga los valores indicados en cada circuito sobre R_h , aplicando los teoremas de Thévenin y de Norton.

a)



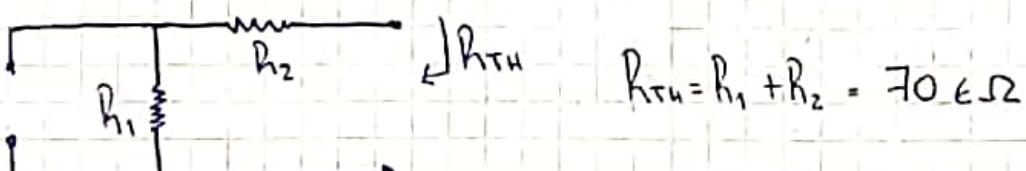
Buscamos la tensión de Thévenin:



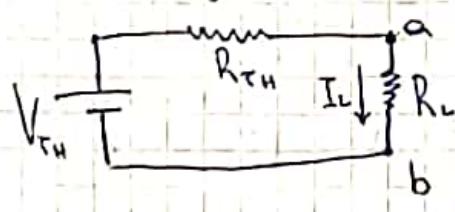
Sobre R_2 no circula corriente entonces $V_{TH} = V_{R_h} = I \cdot R_h$,

$$V_{TH} = 100 \mu\text{A} \cdot 50 \text{ }\Omega = 5 \text{ V}$$

Para encontrar R_{TH} debemos retirar la fuente de corriente:

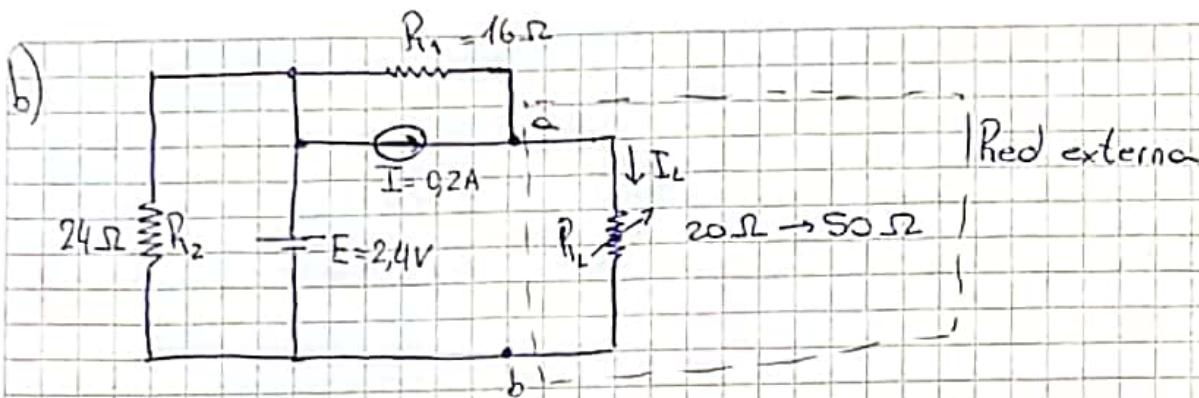


Luego, el siguiente circuito es el que se obtiene por el T. de Thévenin:



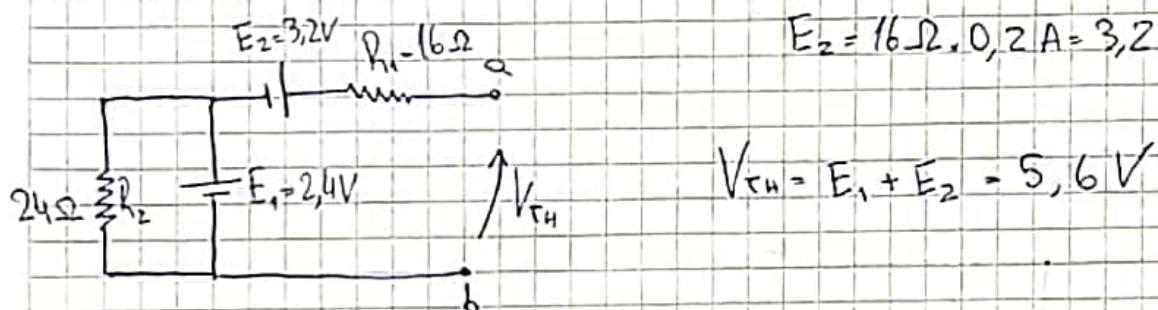
$$I_L = \frac{V_{TH}}{R_L + R_{TH}} = \frac{5 \text{ V}}{180 \text{ }\Omega + 70 \text{ }\Omega} = 20 \mu\text{A}$$

$$\boxed{I_L = 20 \mu\text{A}}$$

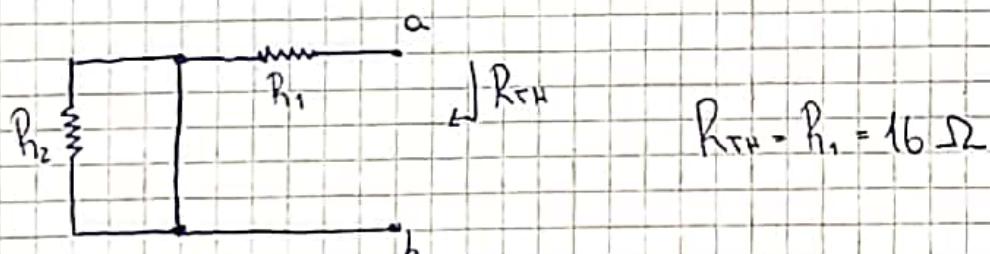


Reemplazamos la fuente de corriente y la resistencia que están en paralelo por su equivalente de Thévenin.

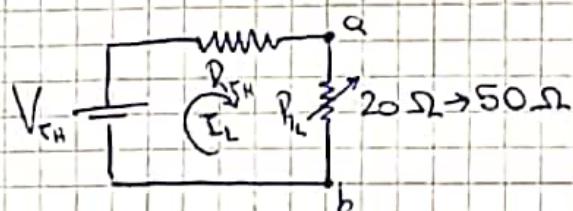
Buscamos V_{TH} :



Buscamos R_{TH} :



Entonces, por el teorema de Thévenin se obtiene el siguiente circuito:



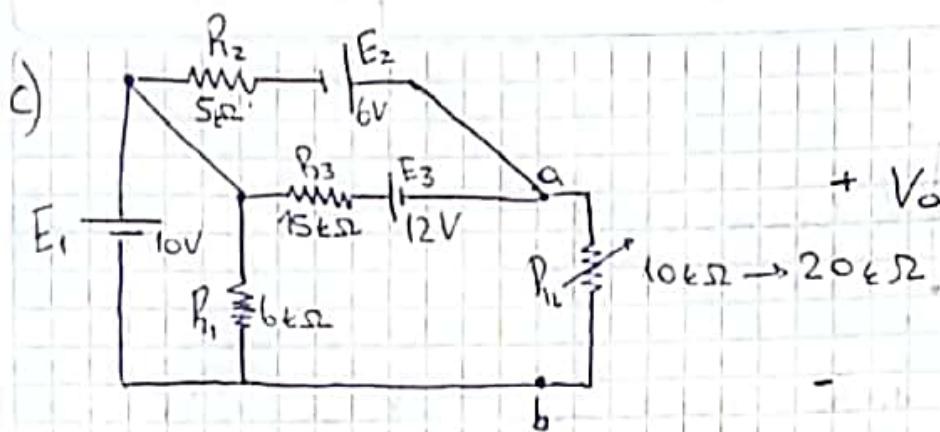
$$I_L = \frac{V_{TH}}{R_{TH} + R_L}$$

entonces, para $R_L = 20\Omega$: $I_L = \frac{5.6V}{(16+20)\Omega} = 0.156A$

y $|V_{ab} = 3.12V|$

para $R_L = 50\Omega$: $I_L = \frac{5.6V}{(16+50)\Omega} = 0.0848A$

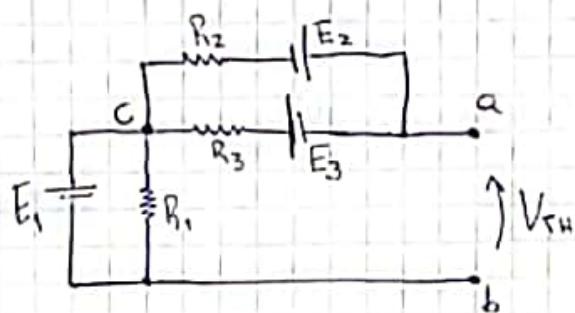
y $|V_{ab} = 1.70V|$



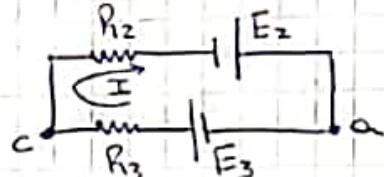
$$+ V_{ab}$$

$$10k\Omega \rightarrow 20k\Omega$$

Buscamos V_{TH} :



$$V_{TH} = E_1 + V_{ac}$$



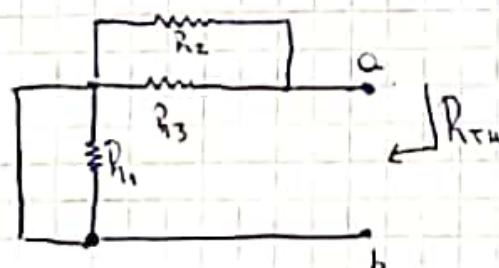
$$E_3 + E_2 - I(R_2 + R_3) = 0$$

$$\Rightarrow I = \frac{E_2 + E_3}{R_2 + R_3} = \frac{18V}{20k\Omega} = 9 \times 10^{-4}A = 0,9mA$$

Entonces $V_{ac} = -0,9mA \cdot R_2 + E_2 = 1,5V$

$$V_{TH} = E_1 + V_{ac} = 10V + 1,5V = 11,5V$$

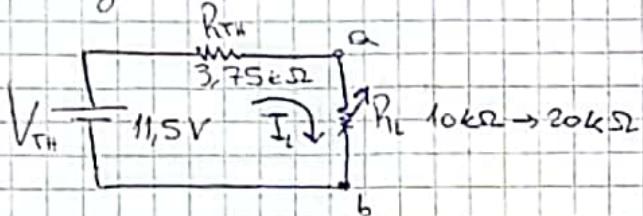
Buscamos R_{TH} :



$$R_{TH} = R_2 \parallel R_3 = \left(\frac{1}{R_2} + \frac{1}{R_3} \right)^{-1}$$

$$R_{TH} = \frac{R_2 R_3}{R_2 + R_3} = 3,75k\Omega$$

Luego, el circuito que se obtiene por el teorema de Thévenin es el siguiente:

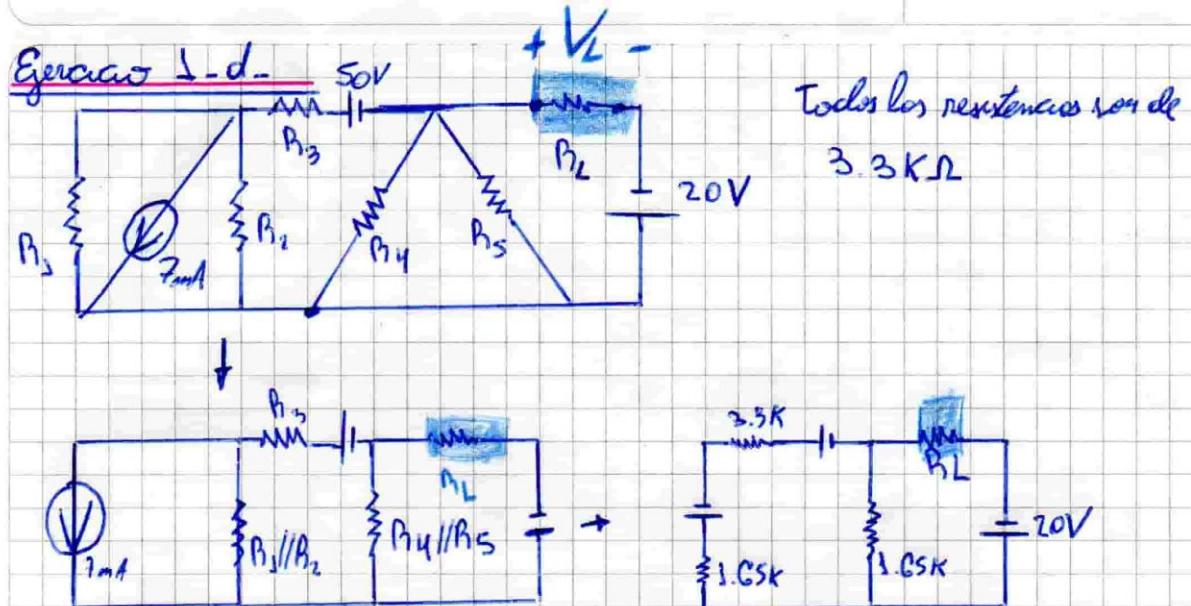


$$I_L = \frac{V_{TH}}{R_{TH} + R_L} \quad \text{si } R_L = 10 \text{ k}\Omega : I_L = \frac{11,5 \text{ V}}{(3,75 + 10) \text{ k}\Omega} = 0,836 \text{ mA}$$

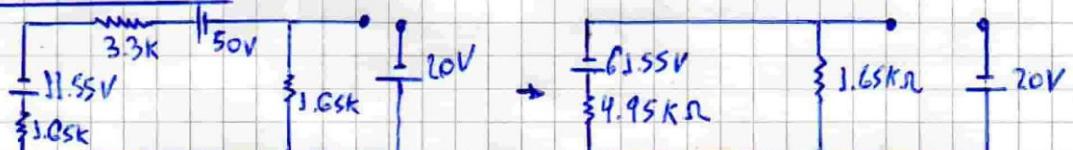
$$V_{ab} = I_L \times R_L = 8,36 \text{ V}$$

$$\text{si } R_L = 20 \text{ k}\Omega : I_L = \frac{11,5 \text{ V}}{(3,75 + 20) \text{ k}\Omega} = 0,484 \text{ mA}$$

$$V_{ab} = I_L \times R_L = 9,68 \text{ V}$$



Mi Red lineal actua:



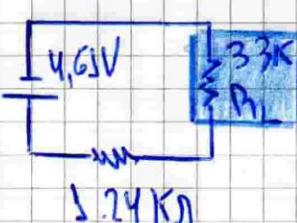
Busco R_{TH} : como fuente

$$\frac{1}{4.95\text{ k}\Omega} \parallel \frac{1}{1.65\text{ k}\Omega} \quad R_{TH} = 4.95\text{ k}\Omega // 1.65\text{ k}\Omega = 1.24\text{ k}\Omega$$

Busco V_{TH}

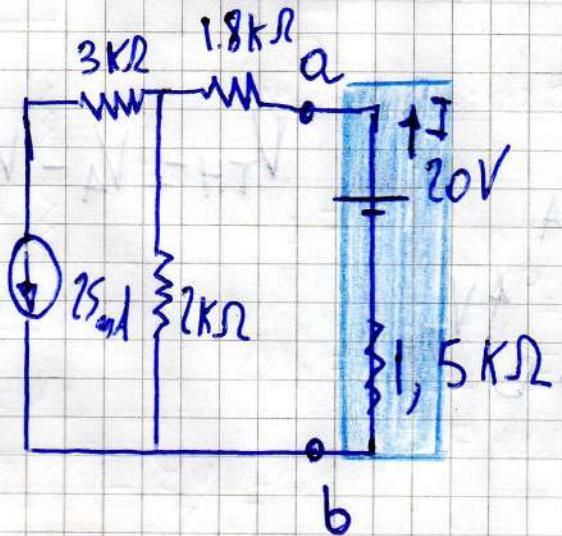
$$V_{TH} = -20V + 6.155V \cdot \frac{1.65\text{ k}\Omega}{4.95\text{ k}\Omega + 1.65\text{ k}\Omega} = -4.61V$$

Circuito equivalente:



$$V_L = -4.61V \cdot \frac{3.3\text{ k}\Omega}{3.3\text{ k}\Omega + 1.24\text{ k}\Omega} = -3.35V$$

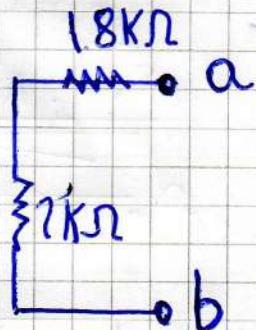
Ejercicio 1-e



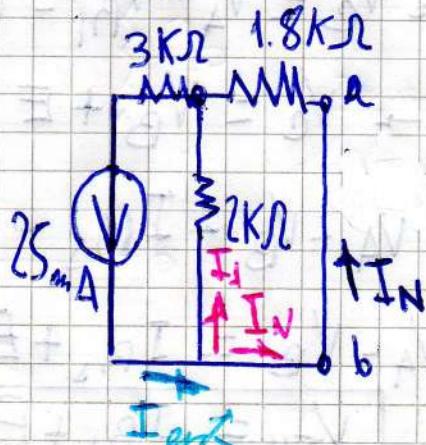
Voy a usar el T de Norton

Halla la R_N

$$R_N = 3.8 \text{ k}\Omega$$



Halla la I_N

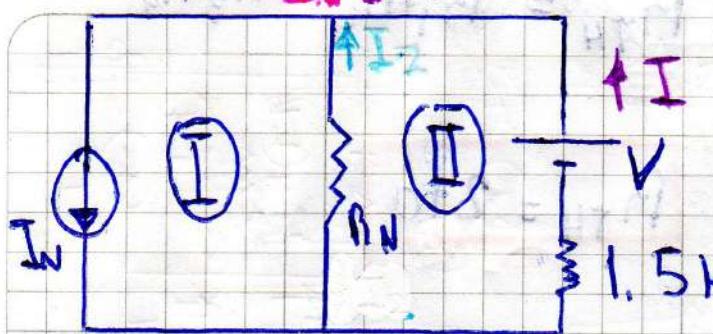


Usa DIVISORES DE CORRIENTE

$$I_N = I_{\text{ent}} \cdot \frac{2 \text{ k}\Omega}{1.8 \text{ k}\Omega + 2 \text{ k}\Omega}$$

$$I_N = 25 \text{ mA} \cdot \frac{10}{19} = 13.16 \text{ mA}$$

$$I_N = 13.16 \text{ mA}$$



Planteo Sección de Kirchhoff

$$I_2 = I_N - I$$

2) $\textcircled{I} \textcircled{\times}$ $-1,5k\Omega I + V + I_2 R_N = 0$

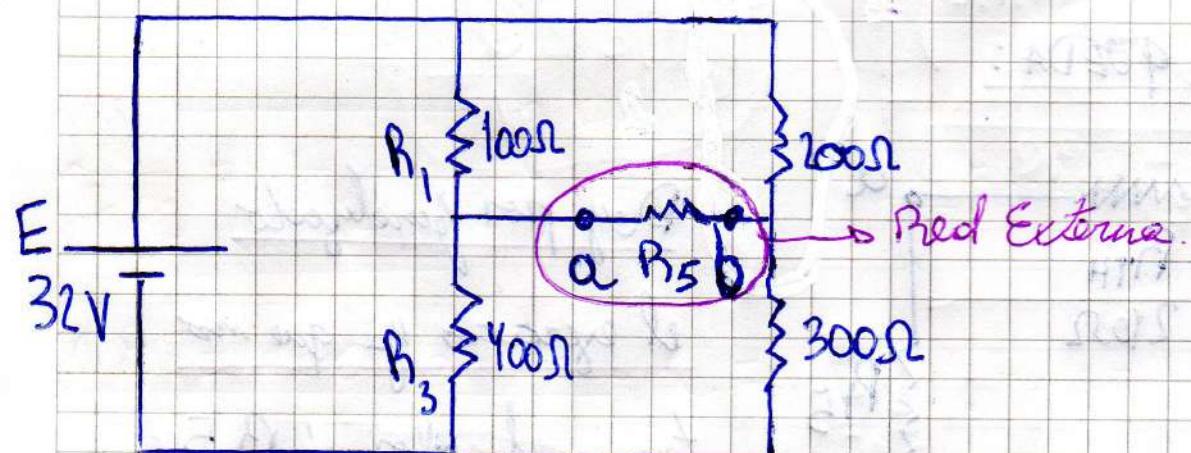
$$-1,5k\Omega I + V + (I_N - I) R_N = 0$$

$$-1,5k\Omega I + 20V + (13,16mA - I) 3,8k\Omega = 0$$

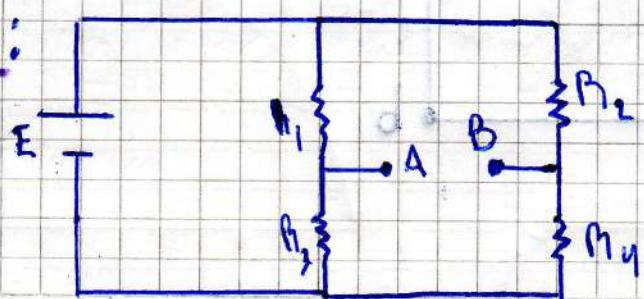
$$+20V + 50V - 5,3k\Omega I = 0$$

$$\boxed{I = 13,20mA}$$

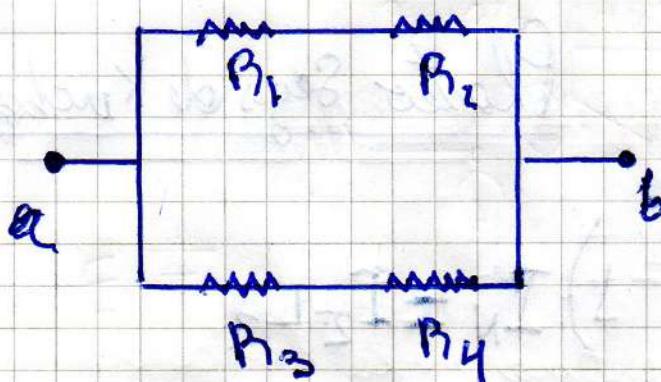
Ejercicio 1-6.



Red lineal activa:



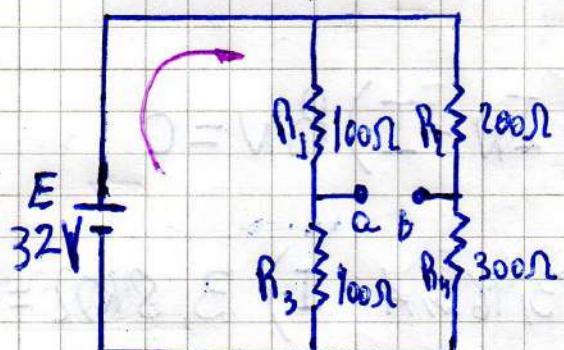
BUSCO la R_{TH}



$$\frac{1}{R_{TH}} = \frac{1}{R_1+R_2} + \frac{1}{R_3+R_4}$$

$$R_{TH} = 210$$

BUSCO la V_{TH}



Doy un orden de tamaños

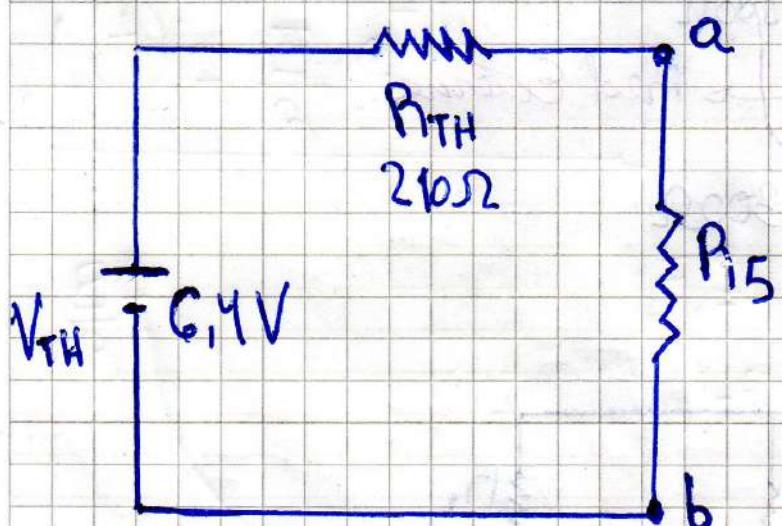
$$\Delta V_1 = \frac{R_1}{R_1+R_3} E = \frac{3^2}{5} V = 6,4V$$

$$\Delta V_2 = \frac{R_2}{R_2+R_4} E = \frac{6^4}{5} V = 12,8V$$

$$V_{TH} = V_a - V_b = 12,8V - 6,4V = 6,4V$$

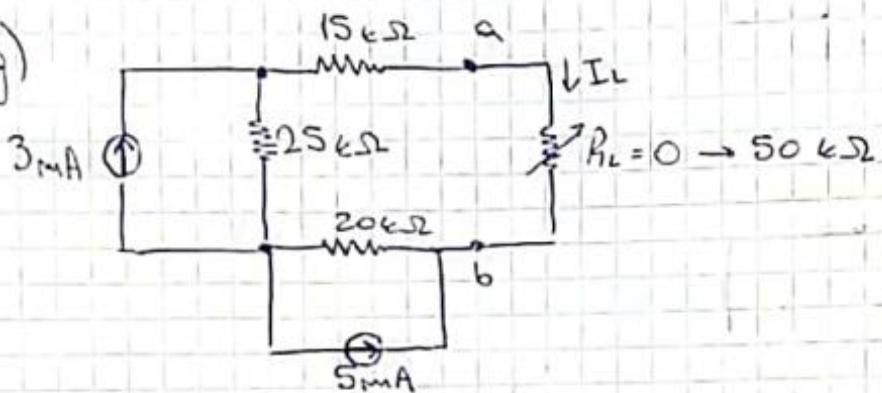
$$V_{TH} = 6,4V$$

MICROCUITO QUEDA:



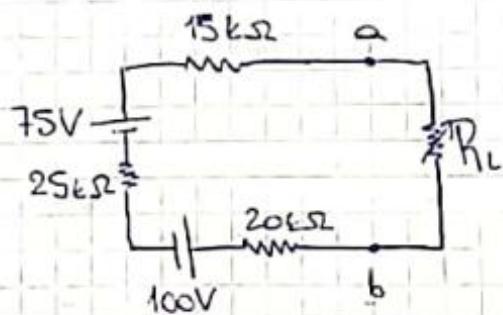
Doy por fundamental
el ejercicio ya que no
tengo el valor de R15.

1)g)



Podemos reemplazar aquellas fuentes de corriente que tienen una resistencia en paralelo por su equivalente de Thévenin:

Thévenin:



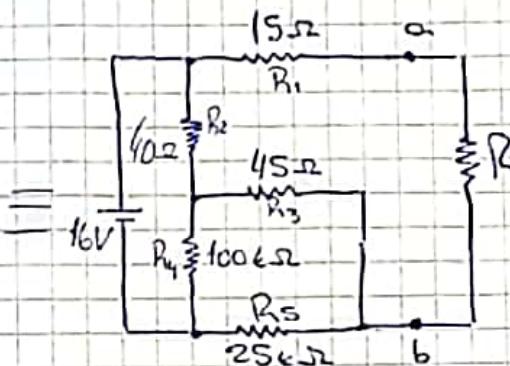
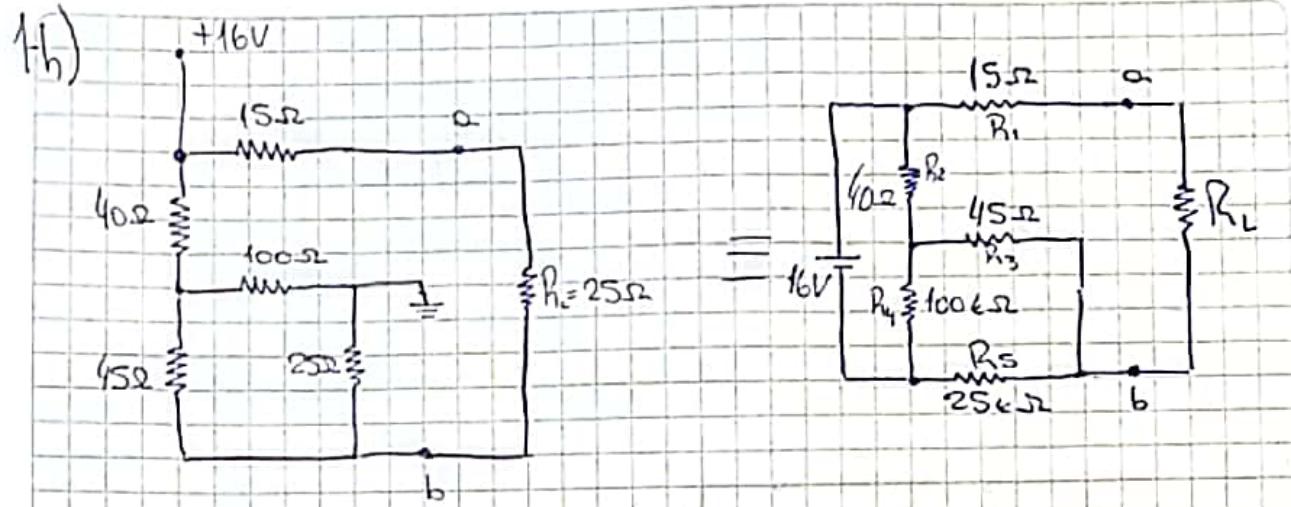
Podemos simplificar el circuito sumando las fuentes y las resistencias

Simplified Thévenin circuit:

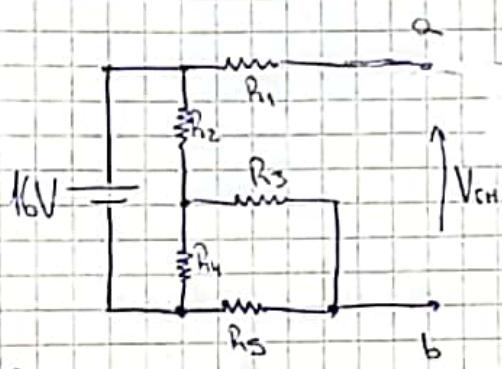
$$95\text{V} \xrightarrow{\text{---}} \frac{60\text{k}\Omega}{60\text{k}\Omega + R_L} \downarrow R_L \quad I_L = \frac{-25\text{V}}{60\text{k}\Omega + R_L}$$

$$\text{Si } R_L = 0 \rightarrow I_L = -0,4167\text{ mA}$$

$$\text{Si } R_L = 50\text{k}\Omega \rightarrow I_L = -0,2273\text{ mA}$$



Buscamos V_{TH} :

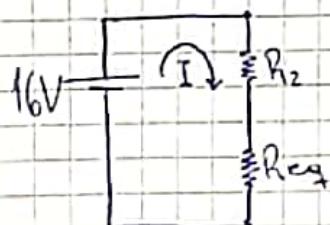


$$V_{TH} = V_{R_5} + 16V$$

$$R_{eq} = R_4 \parallel (R_3 + R_5)$$

$$R_{eq} = \left(\frac{1}{R_4} + \frac{1}{R_3 + R_5} \right)^{-1} = 41,2\Omega$$

Entonces, tenemos:



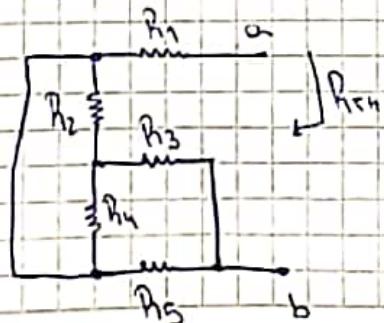
$$V_{R_2} = 16V \cdot \frac{R_2}{R_2 + R_{eq}} = 7,88V$$

$$V_{R_4} + V_{R_2} = 16V \Rightarrow V_{R_4} = 8,12V$$

$$V_{R_5} = -V_{R_4} \cdot \frac{R_5}{R_3 + R_4} = -2,9V$$

$$\Rightarrow V_{TH} = -2,9V + 16V = 13,1V$$

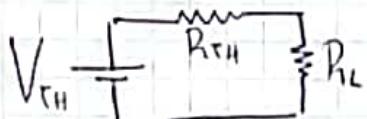
Buscamos R_{TH} :



$$\begin{aligned} R_{TH} &= R_1 + [(R_2 \parallel R_4) + R_3] \parallel R_5 = \\ &= 15\Omega + [28,57\Omega + 45\Omega] \parallel 25\Omega = \\ &= 15\Omega + 73,57\Omega \parallel 25\Omega = 33,7\Omega \end{aligned}$$

$$R_{TH} = 33,7\Omega$$

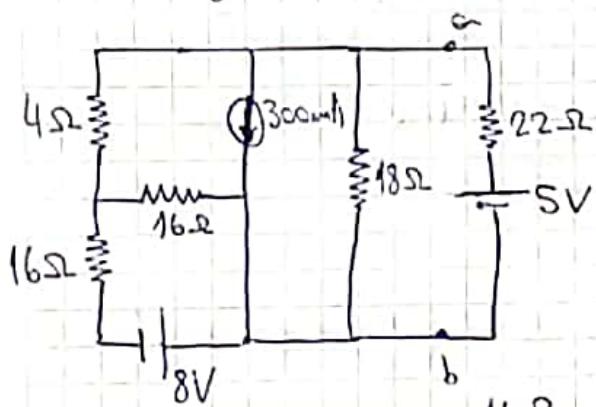
A partir del teorema de Thévenin se obtiene el siguiente circuito:



$$I_{R_L} = \frac{V_{TH}}{R_{TH} + R_L} = \frac{13,1 \text{ V}}{33,75\Omega + 25\Omega} = 0,22 \text{ A}$$

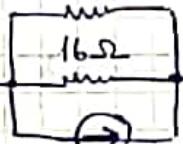
$$V_{R_L} = V_{TH} \cdot \frac{R_L}{R_{TH} + R_L} = 5,58 \text{ V}$$

- C) i) El siguiente circuito es equivalente al del enunciado



Vemos que puede ser simplificado

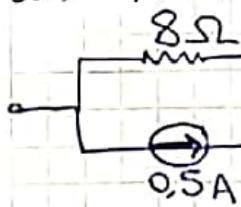
16Ω



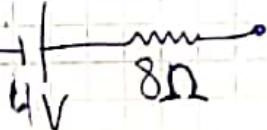
0.5A

Buscamos el equivalente de Norton:

Las resistencias están en paralelo:

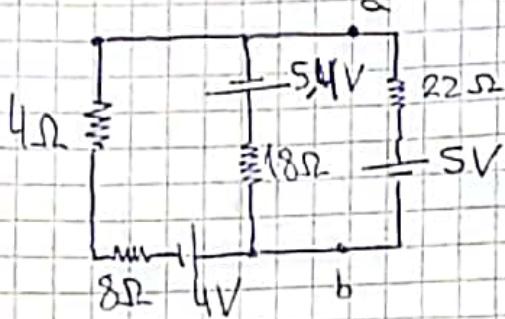


esto es equivalente a:



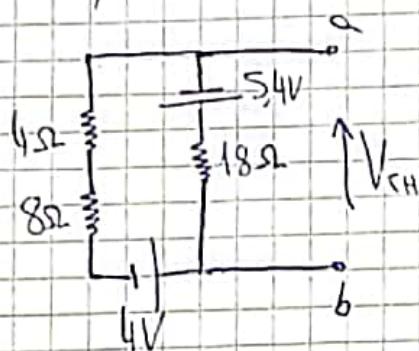
Además, en el circuito inicial hay una fuente de corriente con una resistencia en paralelo que pueden ser reemplazadas por su equivalente de Thévenin.

Entonces, nos quedó el siguiente circuito:



Ahora aplicamos el teorema de Thevenin

V_{TH})



$$V_{TH} = -5.4V + \frac{(5.4V - 4V) \cdot 18\Omega}{18\Omega + 8\Omega + 4\Omega}$$

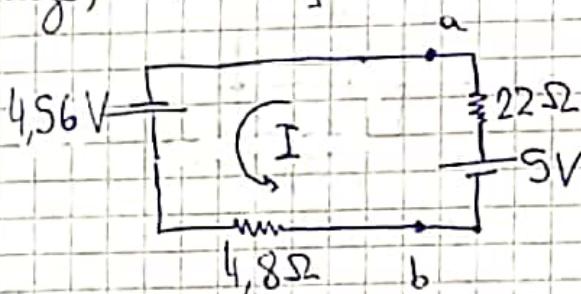
$$V_{TH} = -4.56V$$

R_{TH})



$$R_{TH} = 18\Omega \parallel (4\Omega + 8\Omega) = 4.8\Omega$$

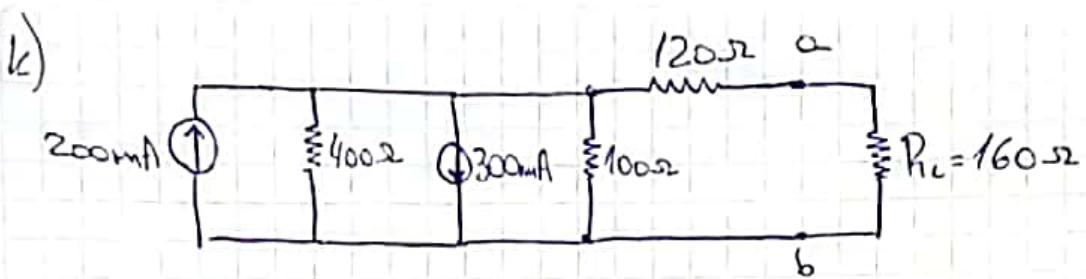
Luego, tenemos que:



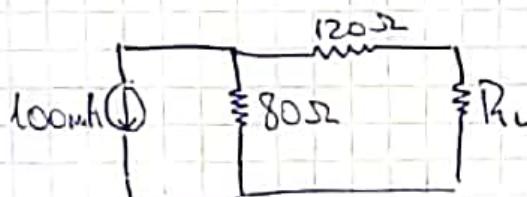
$$I = \frac{5V + 4.56V}{22\Omega + 4.8\Omega} = 0.357A$$

$$V_{ab} = 5V - 0.357A \cdot 22\Omega$$

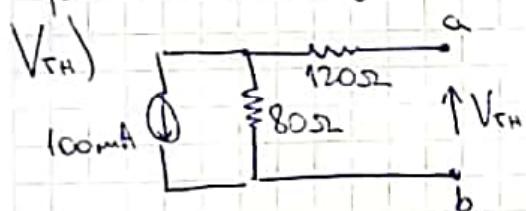
$$\boxed{V_{ab} = -2.85V}$$



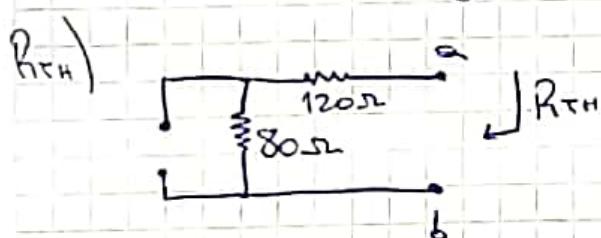
Las fuentes de corriente en paralelo pueden reducirse a una sola fuente. Y las resistencias 400Ω y 100Ω están en paralelo, entonces:



Aplicamos el teorema de Thévenin:

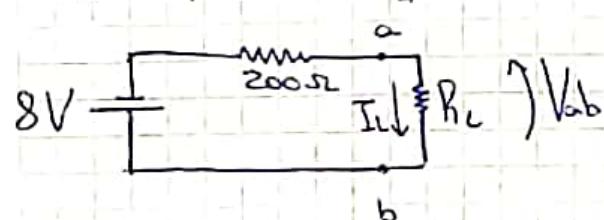


$$V_{TH} = 100 \text{ mA} \cdot 80\Omega = -8 \text{ V}$$



$$R_{TH} = 80\Omega + 120\Omega = 200\Omega$$

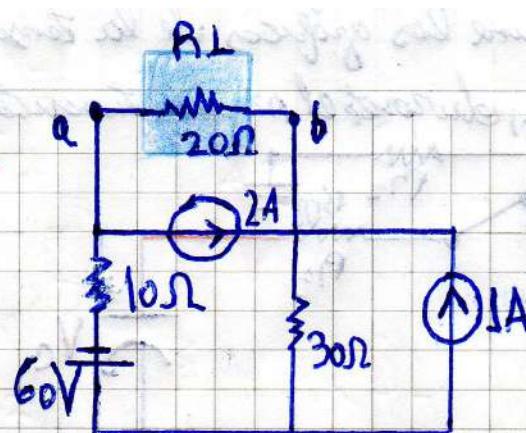
Entonces, tenemos que:



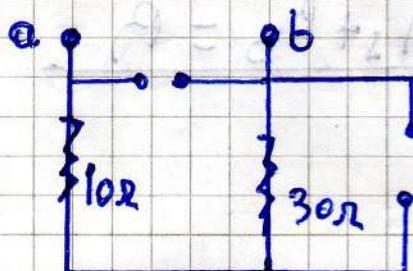
$$I_L = \frac{-8 \text{ V}}{200\Omega + 160\Omega} = 22,2 \text{ mA}$$

$$V_{R_L} - V_{ab} = 8 \text{ V} \cdot \frac{160\Omega}{200\Omega + 160\Omega} = 3,56 \text{ V}$$

Ejercicio 1-3



Busco R_{TH} → Pongo fuentes.



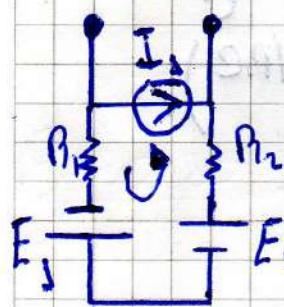
$$R_{TH} = 10\Omega + 30\Omega = 40\Omega$$

Busco V_{TH}

Estoyezco el 0 del potenciómetro A y uso el equivalente de Norton →

$$\frac{V}{I} = \frac{1}{R_E} = \frac{1}{E - iR_1}$$

Sig de mallas de Kirchhoff:



$$V_{AB} = V_{P11} + V_{P21} + E_1 + E_2$$

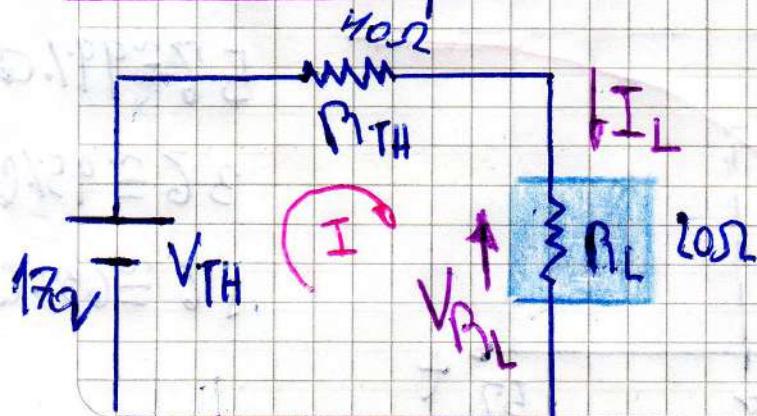
$$E_1 = I_2 R_2 = 30V$$

$$V_{P11} = I_1 R_1 = 24 \cdot 10\Omega = 240V$$

$$V_{P21} = 2A \cdot 20\Omega = 40V$$

$$V_{TH} = V_{AB} = 20V + 60V + 60V + 30V \Rightarrow V_{TH} = 170V$$

MICRÓCIRCUITO QUEDA:



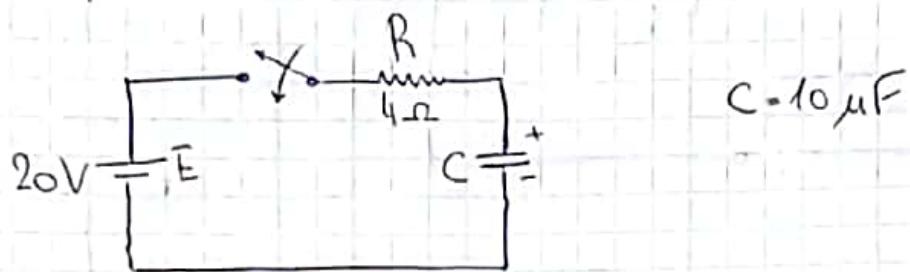
USO LEY DE OHM PARA SACAR I_L

$$170V = I_L \cdot (40\Omega + 20\Omega)$$

$$I_L = 2,83A$$

$$V_{RL} = 20\Omega \cdot 2,83A = 56,66V$$

3)a)



Si la llave está abierta, el capacitor se mantiene descargado. Tomamos a $t=0$ como el momento en el cual se cierra la llave.

Una vez cerrada la llave tenemos que:

$$E = V_R(t) + V_C(t); \quad V_R(t) = I(t) \cdot R = \frac{dV_C(t)}{dt} \cdot C \cdot R$$

$$\text{Entonces } E = \frac{dV_C(t)}{dt} C \cdot R + V_C(t)$$

$$\frac{E}{RC} = \frac{dV_C(t)}{dt} + \frac{V_C(t)}{RC}$$

$$\text{Sea } Z = RC \rightarrow \frac{E}{Z} = \frac{dV_C(t)}{dt} + \frac{V_C(t)}{Z}$$

$$\text{Propongo la solución } V_C(t) = A \cdot e^{-t/Z} + B$$

$$\text{Para } t \rightarrow \infty \quad V_C(t) = E \Rightarrow B = E$$

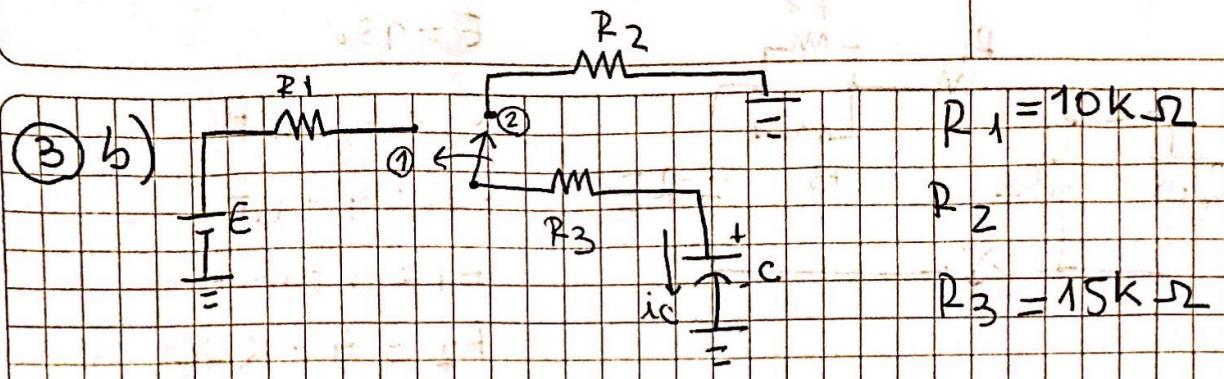
$$\text{Para } t \rightarrow 0 \quad V_C(t) = 0 \Rightarrow A + B = 0 \Rightarrow A = -E$$

$$\Rightarrow V_C(t) = -E e^{-t/Z} + E = E(1 - e^{-t/Z}) ; \quad Z = C \cdot R = 10\mu F \cdot 4\Omega = 40\mu s$$

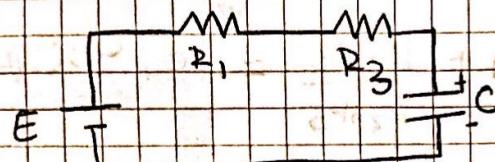
$$\boxed{V_C(t) = 20V (1 - e^{-t/40\mu s})}$$

$$\text{Luego, como } I(t) = \frac{dV_C(t)}{dt} \cdot C = \frac{20V}{40\mu s} e^{-t/40\mu s} \cdot 10\mu F$$

$$\boxed{I(t) = 5A e^{-t/40\mu s}}$$



• cuando la llave está en ①:

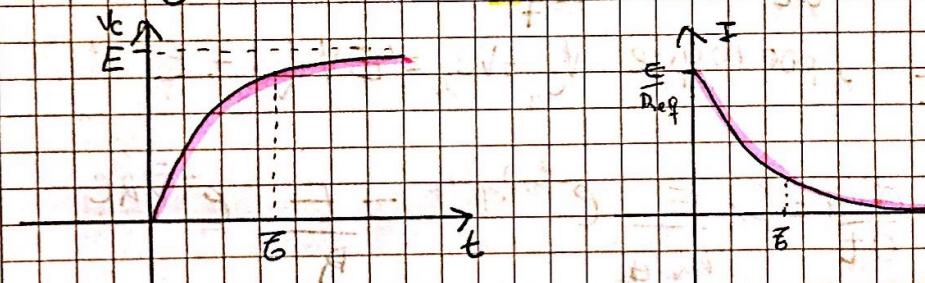


$$E = \frac{dQ}{dt} R_{eq} + \frac{Q}{C} \quad (Q(0)=0)$$

$$R_{eq} = R_1 + R_3$$

$$\Rightarrow Q = CE [1 - e^{-t/R_{eq}C}]$$

$$[V_C = \frac{Q}{C} = E [1 - e^{-t/R_{eq}C}]] \quad , \quad [I = \frac{dQ}{dt} = \frac{E}{R_{eq}} \cdot e^{-t/R_{eq}C}]$$

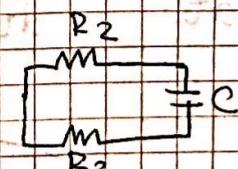


se carga C
hasta cargarse
por completo,
cuando $V_c = E$
circuito

$$\bar{E} = R_{eq} \cdot C = 25 \text{ k}\Omega \cdot C$$

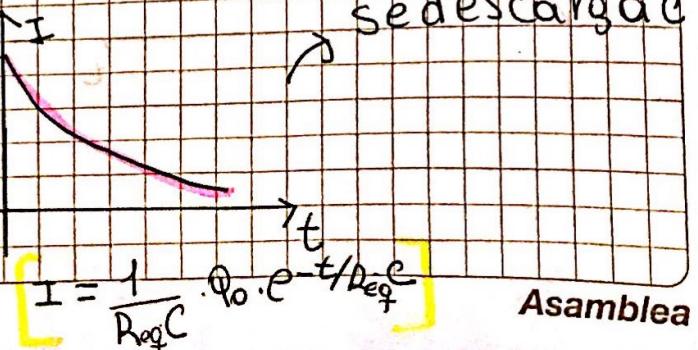
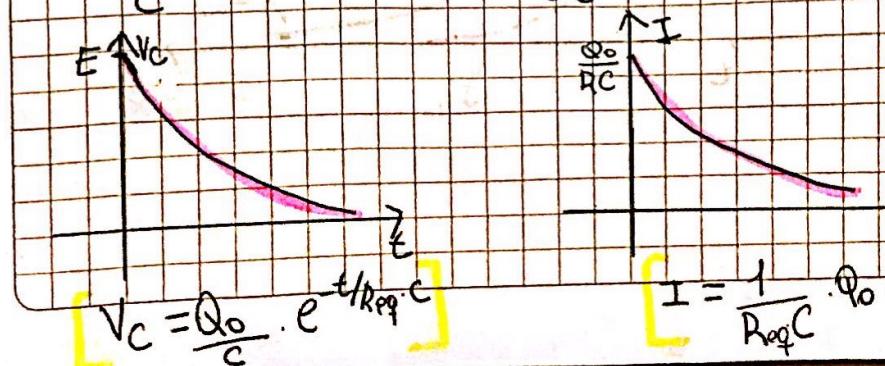
• Luego la llave pasa a ②:

$$Q(0) = E \quad (\text{capacitor inicialmente cargado})$$

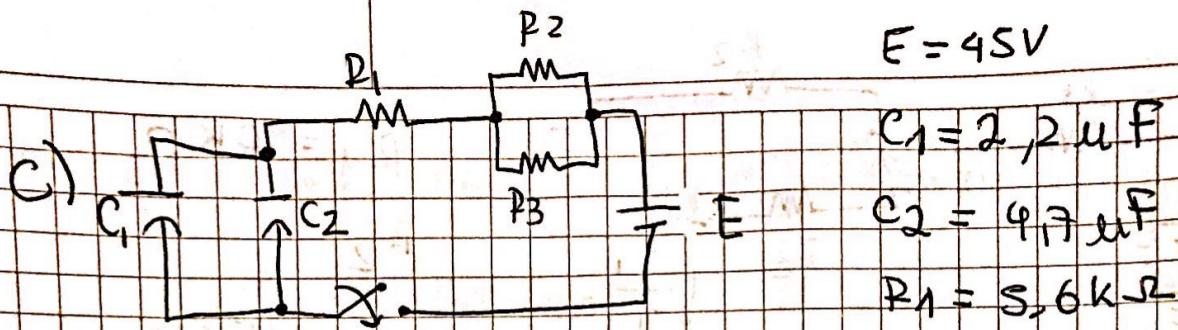


$$R_{eq} = R_2 + R_3$$

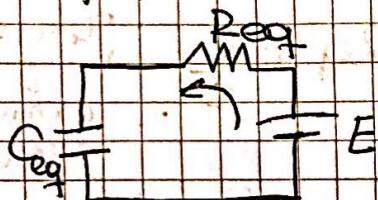
$$\frac{Q}{C} = IR \quad , \quad I = \frac{dQ}{dt} \Rightarrow Q = Q_0 \cdot e^{-t/R_{eq}C}$$



Asamblea



Simplificando el circuito:



$$R_{eq} = R_1 + \frac{R_2 R_3}{R_2 + R_3} = 26,9 k\Omega$$

$$C_{eq} = C_1 + C_2 = 6,9 \mu F$$

$$E = 45V$$

$$\text{Entonces: } E = \frac{dQ}{dt} \cdot R_{eq} + \frac{Q}{C_{eq}} \Rightarrow Q = C E [1 - e^{(-t/R_{eq} C_{eq})}]$$

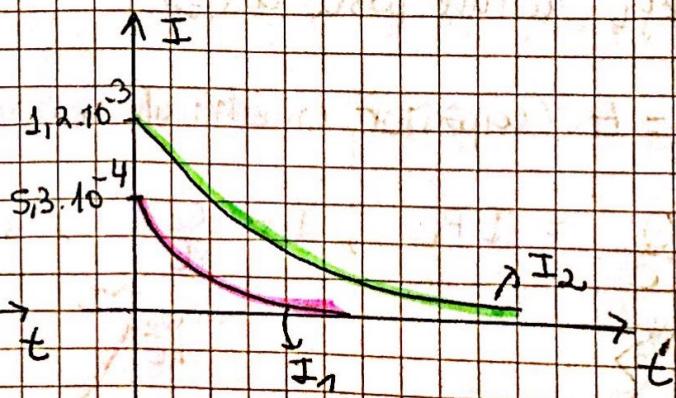
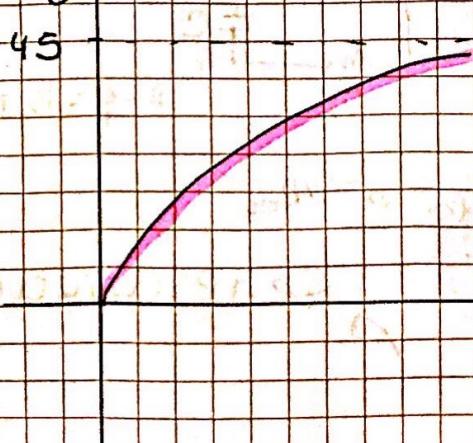
A demás

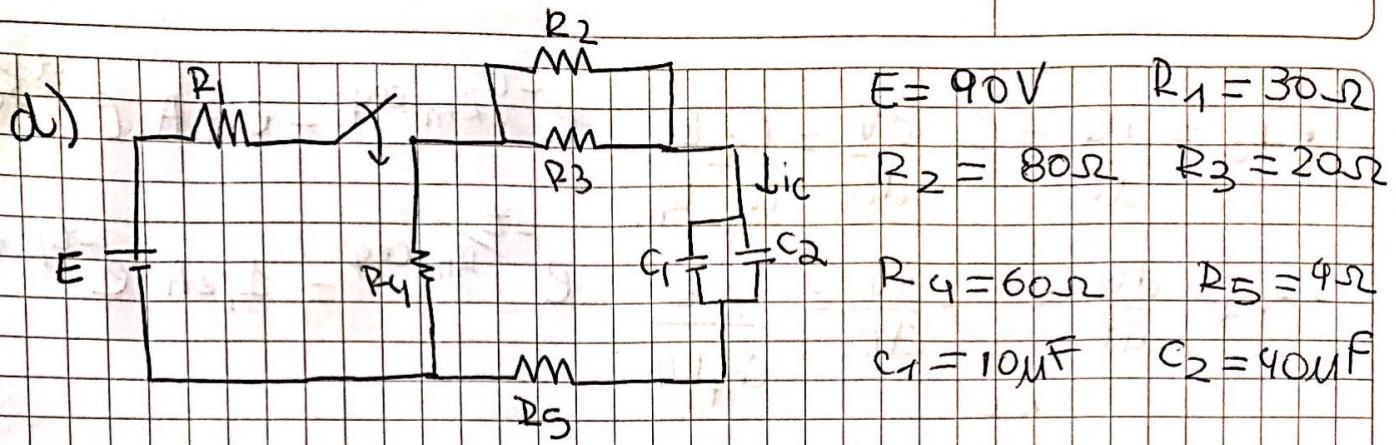
$$V_{C_{eq}} = V_{C_1} = V_{C_2} = \frac{Q}{C_{eq}}, \text{ por lo que } V_{C_1} = V_{C_2} = 45V (1 - e^{-t/26,9 k\Omega \cdot 6,9 \mu F})$$

$$I_{C_1} = \frac{dQ_1}{dt} = C_1 \cdot \frac{dV_{C_1}}{dt} = C_1 \cdot \frac{E}{R_{eq} C_{eq}} \cdot e^{-t/R_{eq} C_{eq}}$$

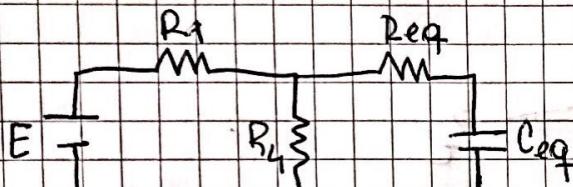
$$I_{C_2} = \frac{dQ_2}{dt} = C_2 \frac{dV_{C_2}}{dt} = C_2 \cdot \frac{E}{R_{eq} C_{eq}} \cdot e^{-t/R_{eq} C_{eq}}$$

$V_C \uparrow$





Primero simplifico el circuito:



$$R_{eq} = \frac{R_2 R_3}{R_2 + R_3} + R_5 = 20\Omega$$

$$C_{eq} = C_1 + C_2 = 50\mu F$$

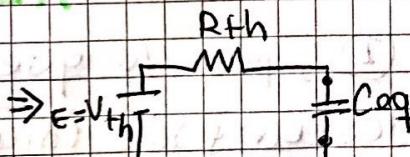
Ahora puedo aplicar thévenin:



$$R_{th} = \frac{R_1 R_4}{R_1 + R_4} + R_{eq} = 40\Omega$$

$$V_{th} = 60\Omega \cdot \frac{90V}{3\Omega + 60\Omega} = 60V$$

R.L.A



Donde

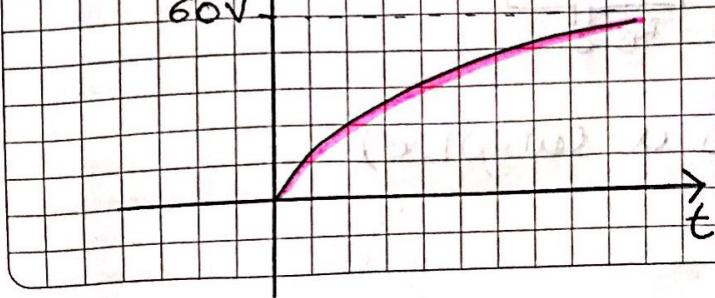
$$E = IR + \frac{Q}{C} = \frac{dQ}{dt} R_{th} + \frac{Q}{C_{eq}}$$

$$\Rightarrow Q = E \cdot C_{eq} \left(1 - e^{-\frac{t}{R_{th} \cdot C_{eq}}} \right)$$

Entonces:

$$V_{c_{eq}} = V_{C_1} = V_{C_2} = \frac{Q}{C_{eq}} = E \left(1 - e^{-\frac{t}{R_{th} \cdot C_{eq}}} \right) = 60V \left(1 - e^{-\frac{t}{40\Omega \cdot 50\mu F}} \right)$$

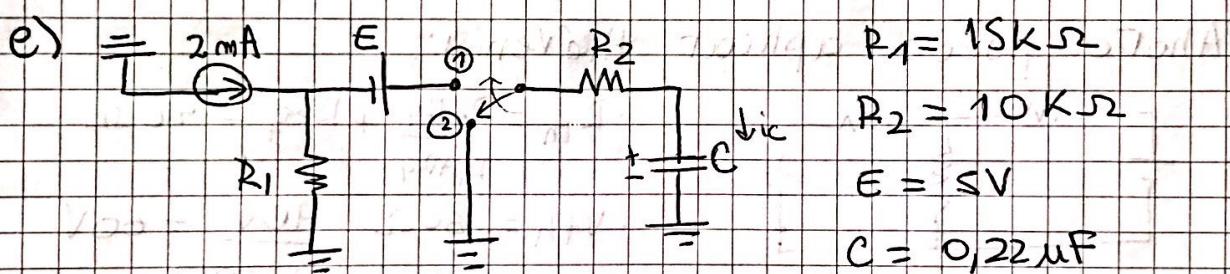
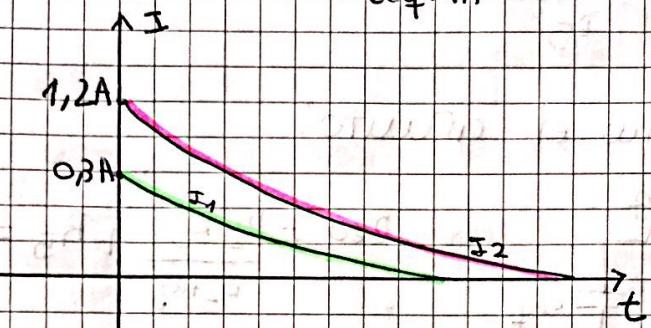
V_c
60V



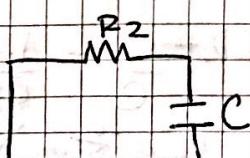
Asamblea

$$\bullet I_{C_1} = \frac{dQ}{dt} = C_1 \cdot \frac{dV}{dt} = \frac{C_1 E}{C_{eq} R_{th}} \cdot e^{-t/R_{th} \cdot C_{eq}} = 0,3 A \cdot e^{-t/2 \text{ ms}}$$

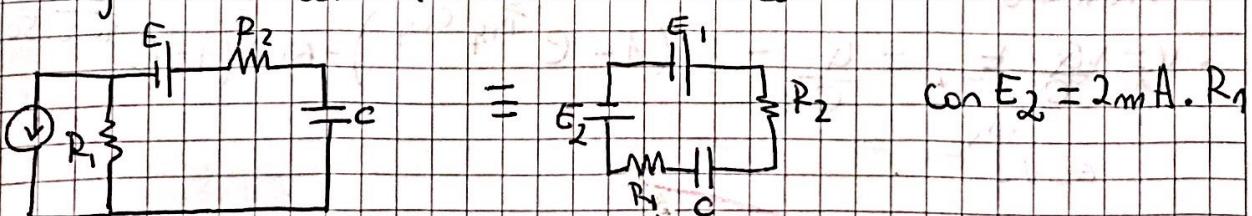
$$\bullet I_{C_2} = \frac{dQ}{dt} = C_2 \frac{dV}{dt} = \frac{C_2 E}{C_{eq} R_{th}} \cdot e^{-t/R_{th} \cdot C_{eq}} = 1,2 A \cdot e^{-t/2 \text{ ms}}$$



Primeramente la llave está en ②, por lo que el capacitor está descargado inicialmente



Luego se coloca la llave en ①:



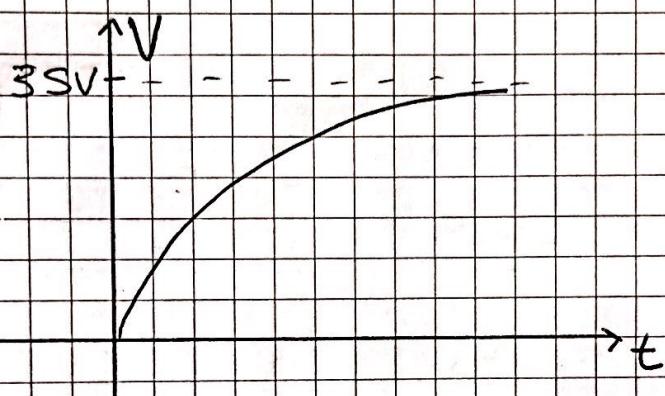
(El capacitor comienza a cargarse)

$$\text{Donde } E = \frac{Q}{C} + \frac{dQ}{dt} R$$

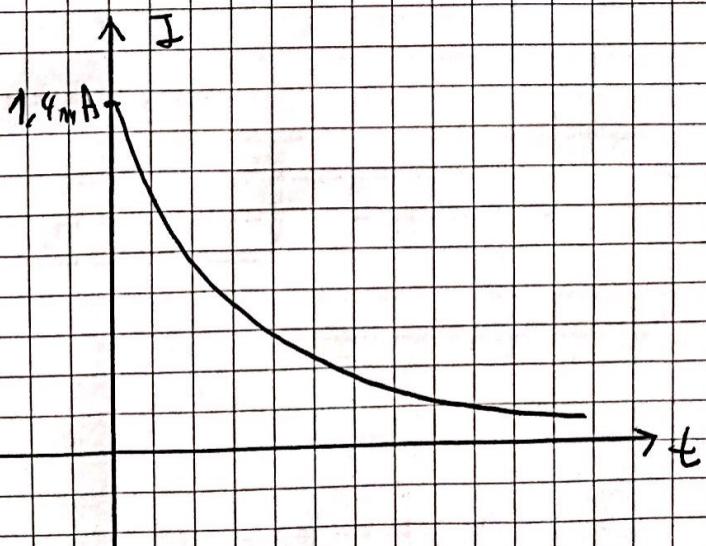
$$\Rightarrow Q = CE \cdot (1 - e^{-t/RC})$$

Entonces

$$\bullet V_c = \frac{Q}{C} = E(1 - e^{-t/RC}) = (5V + 30V) \cdot (1 - e^{-\frac{t}{25k\Omega \cdot 0,22\mu F}})$$

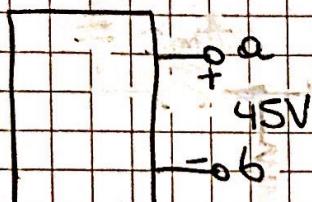


$$\bullet I_c = \frac{dQ}{dt} = \frac{E}{R} \cdot e^{-t/RC} = \frac{35V}{25k\Omega} \cdot e^{-\frac{t}{25k\Omega \cdot 0,22\mu F}}$$



④ Una caja negra contiene resistores y fuentes.

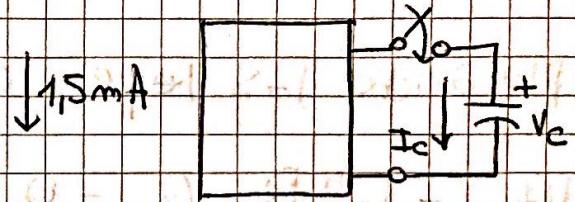
Sela mide externamente y se obtienen los valores indicados. Luego se le conecta un capacitor de 500nF mediante una llave. Determinar el valor de la corriente en el capacitor 25 s después de conectar la llave.



(a)

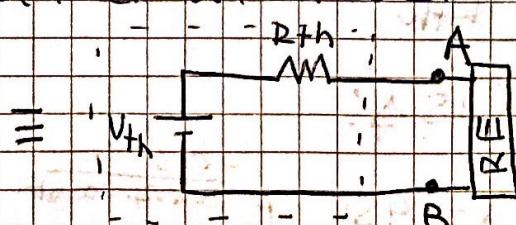
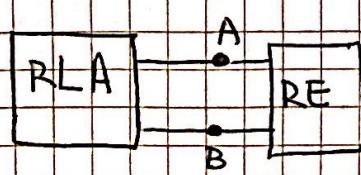


(b)

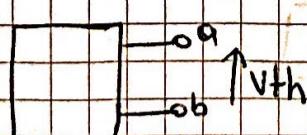


(c)

Usando el teorema de Thévenin, podemos pensar la caja como la red lineal activa

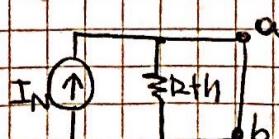


Entonces por (a) $V_{th} = 45V$.



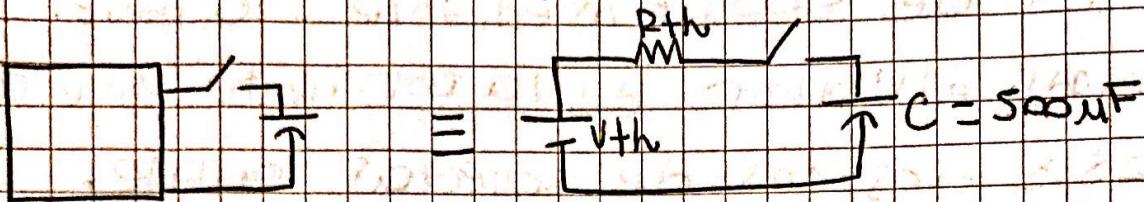
Análogamente, usando el teorema de Norton, por (b)

$$I_N = 1.5 \text{ mA}$$



$$\text{Además } R_{th} = \frac{V_{th}}{I_N} = \frac{45V}{15mA} = 30k\Omega$$

Entonces (c) es equivalente a:



Aplicando las leyes de Kirchoff:

$$V_{th} - IR_{th} - \frac{Q}{C} = 0, \quad I = \frac{dQ}{dt}$$

$$\Rightarrow Q = C V_{th} [1 - e^{(-t)/R_{th} \cdot C}]$$

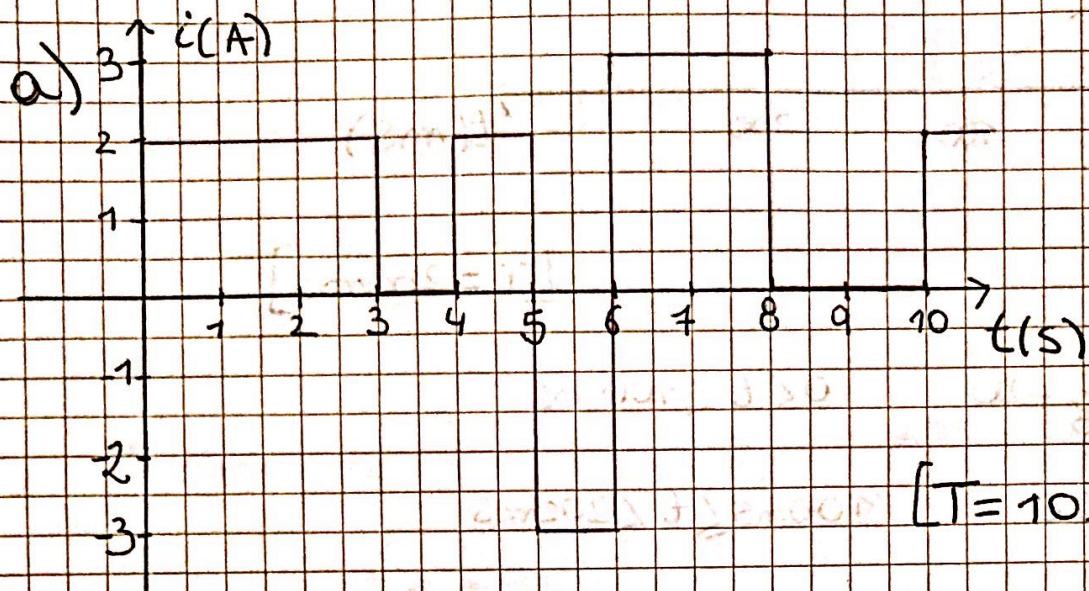
$$\Rightarrow I = \frac{V_{th}}{R_{th}} e^{-t/R_{th} \cdot C}$$

para $t = 25s$:

$$I(25s) = \frac{45V}{30k\Omega} \cdot e^{-\frac{25s}{30k\Omega \cdot 500\mu F}}$$

$$[I(25s) = 0,203mA]$$

5) Determine los valores medio y eficaz de cada una de las formas de onda



Sabiendo que $I_{\text{Medio}} = \frac{1}{T} \cdot \int_0^T I dt$ y teniendo la función partida $I(t)$:

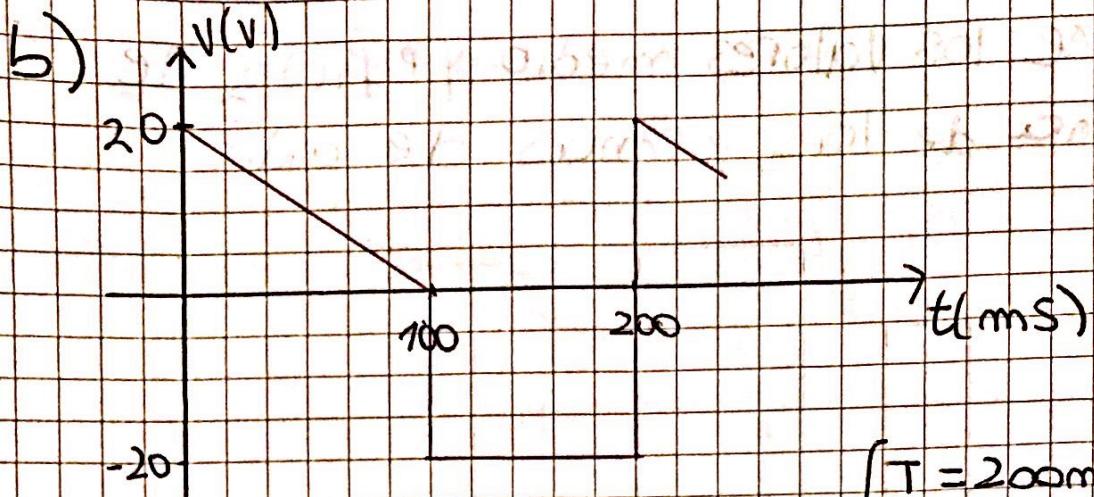
$$I_{\text{Medio}} = \frac{1}{10} \cdot \left[\int_0^3 2 dt + \int_3^4 0 dt + \int_4^5 2 dt + \int_5^6 (-3) dt + \int_6^8 3 dt + \int_8^{10} 0 dt \right]$$

$$\Rightarrow I_{\text{Medio}} = \frac{1}{10} \cdot 11A = 1,1A$$

Por otro lado $I_{\text{ef}} = \sqrt{\frac{1}{T} \cdot \int_0^T I^2 dt}$, entonces:

$$I_{\text{ef}} = \sqrt{\frac{1}{10} \cdot \int_0^{10} I^2 dt} = \sqrt{\frac{1}{10} \cdot \left(\int_0^3 2^2 dt + \int_3^5 2^2 dt + \int_5^6 (-3)^2 dt + \int_6^8 3^2 dt \right)}$$

$$\Rightarrow I_{\text{ef}} = \sqrt{\frac{43}{10}} \approx 2,074 A$$



$$V(t) = \begin{cases} -\frac{t}{5} + 20 & 0 < t < 100 \text{ ms} \\ -20 & 100 \text{ ms} \leq t < 200 \text{ ms} \end{cases}$$

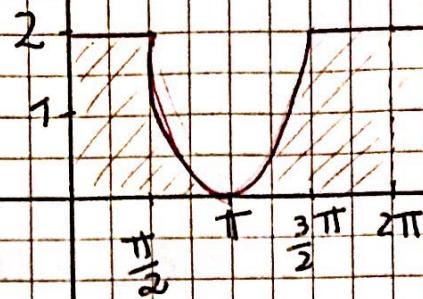
$$\cdot V_{\text{medio}} = \frac{1}{T} \int_0^T V(t) dt = \frac{1}{200} \left[\int_0^{100} \left(-\frac{t}{5} + 20 \right) dt + \int_{100}^{200} (-20) dt \right]$$

$$[V_{\text{medio}} = \frac{1}{200} \cdot (-1000) = -5 \text{ V}]$$

$$\cdot V_{\text{ef}} = \sqrt{\frac{1}{T} \int_0^T V^2 dt} = \sqrt{\frac{1}{200} \left(\int_0^{100} \left(-\frac{t}{5} + 20 \right)^2 dt + \int_{100}^{200} (-20)^2 dt \right)}$$

$$[V_{\text{ef}} = \sqrt{\frac{1}{200} \cdot \frac{160000}{3}} \approx 16,33 \text{ V}]$$

c) $\uparrow i(A)$



$$[T = 2\pi]$$

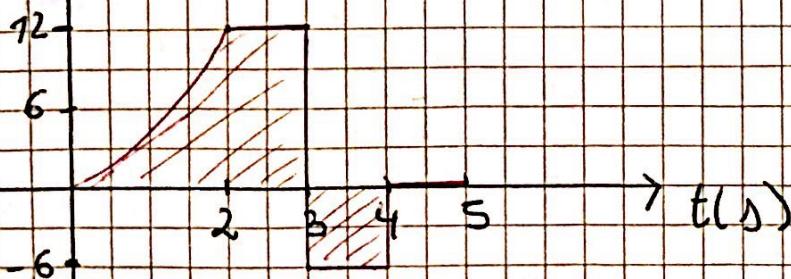
$$\cdot I_{\text{Medio}} = \frac{1}{T} \int_0^T i dt = \frac{1}{2\pi} \cdot \left[\int_0^{\frac{\pi}{2}} 2 dt + \int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} (2 \cos(t) + 2) dt + \int_{\frac{3\pi}{2}}^{2\pi} 2 dt \right]$$

$$[I_{\text{Medio}} \approx 1,36 A]$$

$$\cdot I_{\text{ef}} = \sqrt{\frac{1}{T} \int_0^T i^2 dt} = \sqrt{\frac{1}{2\pi} \left(\int_0^{\frac{\pi}{2}} 2^2 dt + \int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} (2 \cos(t) + 2)^2 dt \right)}$$

$$[I_{\text{ef}} \approx 1,57 A]$$

d) $\uparrow v(V)$



$$[T = 4 s]$$

$$v(t) = \begin{cases} 3t^2 & 0 < t < 2 \\ 12 & 2 \leq t < 4 \\ -6 & 4 \leq t < 6 \end{cases}$$

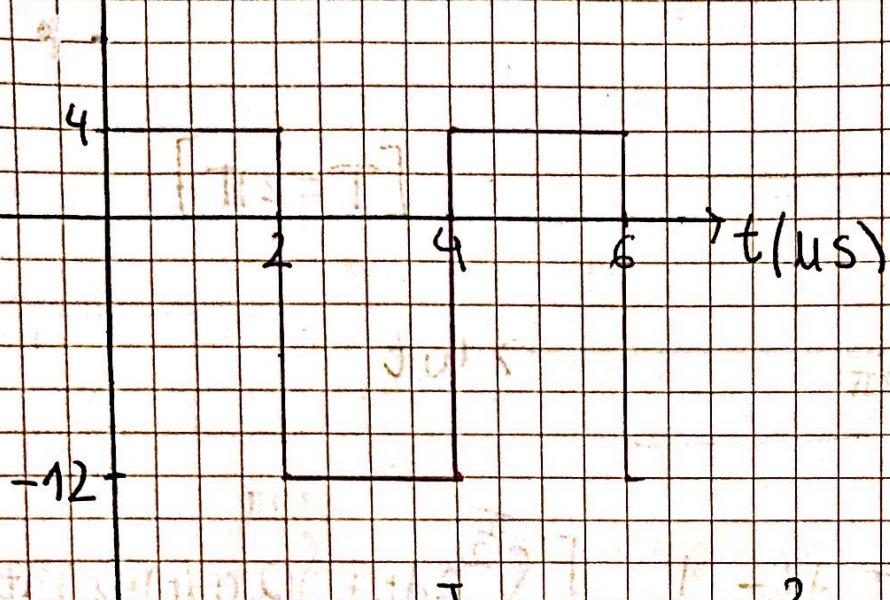
$$\cdot V_{\text{Medio}} = \frac{1}{T} \int_0^T v dt = \frac{1}{4} \left(\int_0^2 3t^2 dt + \int_2^4 (-6) dt + \int_4^6 12 dt \right)$$

$$[V_{\text{Medio}} = 3,5 V]$$

$$\cdot V_{\text{ef}} = \sqrt{\frac{1}{T} \cdot \left(\int_0^T v^2 dt \right)} = \sqrt{\frac{1}{4} \left(\int_0^2 (3t^2)^2 dt + \int_2^4 (-6)^2 dt + \int_4^6 12^2 dt \right)}$$

$$[V_{\text{ef}} \approx 7,7 V]$$

e) $\uparrow i(t)$



$$\cdot I_{\text{Medio}} = \frac{1}{T} \int_0^T i dt = \frac{1}{6} \left(\int_0^2 4 dt + \int_2^4 (-12) dt + \int_4^6 4 dt \right)$$

$$[I_{\text{Medio}} \approx -1,33 \text{ A}]$$

$$\cdot I_{\text{ef}} = \sqrt{\frac{1}{T} \cdot \int_0^T i^2 dt} = \sqrt{\frac{1}{6} \left(\int_0^2 4^2 dt + \int_2^4 (-12)^2 dt + \int_4^6 4^2 dt \right)}$$

$$[I_{\text{ef}} \approx 7,66 \text{ A}]$$