

# On the spontaneous emergence of discrete and compositional signals

Anonymous ACL submission

## Abstract

We propose a general framework to study language emergence through signaling games with neural agents. Using a continuous latent space, we are able to (i) train using back-propagation, (ii) show that discrete messages nonetheless naturally emerge. We discuss various ways to test classic properties of the emergent language in production and perception.

## 1 Introduction

In a signaling game, artificial agents learn to communicate to achieve a common goal: a sender sees some piece of information and produces a message, which is then sent to a receiver that must take some action (Lewis, 1969; Skyrms, 2010). If the action is coherent with the sender’s initial piece of information, the choice of the message and its interpretation is reinforced. For instance, in a referential game, sender and receiver see a set of objects, and the sender knows which of these the receiver must pick; the sender then sends a message to the receiver, who must interpret it to pick up the right object (Lazaridou et al., 2017, 2018; Havrylov and Titov, 2017; Chaabouni et al., 2019).

This setting has been used to study the factors influencing the emergence of various fundamental properties of natural language, such as *compositionality* (Kirby et al., 2015; Franke, 2016; Steinert-Threlkeld, 2016; Mordatch and Abbeel, 2018; Lazaridou et al., 2018; Choi et al., 2018). In this paper, we add focus on two other so-called ‘design features’ of natural language (Hockett, 1960): *discreteness* (i.e. words form clusters in acoustic space), and *displacement* (i.e. efficient communication can occur about objects and facts beyond the immediate context of the conversation).

From an implementation point of view, we follow the recent literature which has shown that a signaling game is essentially an autoencoder setting,

with the encoder playing the role of the sender, and the decoder the role of the receiver (see Fig. 1). In this literature, however, the discreteness of the communication protocol is assumed, since the networks then traditionally use a (normally sequential and) discrete latent space (Havrylov and Titov, 2017; Chaabouni et al., 2019; Kharitonov et al., 2019).

Our main contribution is a generalization of the current implementation of signaling games as autoencoders. Our implementation covers a broader variety of signaling games, and it crucially incorporates the possibility of displacement and makes no *a priori* assumption of discreteness. Our main result is that under appropriate conditions, discreteness emerges spontaneously: if the latent space is thought about as a continuous acoustic space, then trained messages form coherent clusters, just like regular words do.

In addition to contributing to our understanding of the emergence of communication protocols with features like natural language, these results have a technical significance: by using a fundamentally continuous communication protocol, with discreteness emerging, we can train end-to-end using standard backpropagation techniques, instead of reinforcement learning algorithms like REINFORCE and its refinements (Williams, 1992; Schulman et al., 2015; Mnih et al., 2016), which are difficult to use in practice.

## 2 Related Work

A related line of work attempts to avoid the difficulties of reinforcement learning—which introduces stochastic nodes into a computation graph—by reparameterization and/or non-stochastic estimators (Bengio et al., 2013; Schulman et al., 2015). In the emergent communication case, where the stochastic nodes are discrete (e.g. sampling a message from a sender distribution), the Gumbel-

Softmax estimator has become increasingly popular (Jang et al., 2017; Maddison et al., 2017).

This work enables standard backpropagation to be used for training by optimizing approximations to the true reinforcement learning signal. By contrast, using the auto-encoder analogy more literally, we do not approximate the discrete RL learning signal, but rather ask under what conditions discreteness will emerge.

### 3 Function Games

We here introduce a general communication game setting, which we call Function Games. Our games contain three basic components: (i) a set of contexts  $C$ , (ii) a set of actions  $A$ , (iii) a family of functions  $F$ , from contexts to actions. One play of a Function Game game runs as follows:

1. Nature chooses  $f \in F$  and a context  $c \in C$ .
2. Sender sees the context  $c$  and  $f$ .
3. Sender sends a message  $m$  to Receiver.
4. Receiver sees a possibly different context  $c'$  and the message  $m$  and chooses an action  $a'$ .
5. Both are ‘rewarded’ iff  $a' = f(c')$ .

Abstractly, the function  $f$  represents some piece of knowledge available primarily for Sender, and which determines what action is appropriate in any given context. Two concrete interpretations will help illustrate the variety of communication protocols and goals that this framework encompasses.

**Generalized referential games.** A reference game is one in which Sender tries to get Receiver to pick the correct object out of a given set (Skyrms, 2010; Lazaridou et al., 2017, 2018; Havrylov and Titov, 2017; Chaabouni et al., 2019). Here, contexts are sets of objects (i.e. an  $m \times n$  matrix, with  $m$  objects represented by  $n$  features). Normally (though we will drop this assumption later),  $c' = \text{shuffled}(c)$ : Sender and Receiver see the same objects, but in a different arrangement. Actions are the objects, and the functions  $f \in F$  are *choice functions*:  $f(c) \in c$  for every context  $c$ .

**Belief update games.** Contexts can represent the (possibly different) belief states of the agents. ‘Actions’ can represent updated belief states ( $A = C$ ), the different functions in  $F$  then representing how to update an agent’s beliefs in the light of learning a particular piece of information (passed directly to Sender, and only through the message to Receiver).

## 4 Experiment

Because we are interested in the simultaneous emergence both of discrete and of compositional signals, we use a Function Game called the Extremity Game designed to incentivize and test rich compositionality (Steinert-Threlkeld, 2019). In this game, it is natural to think of the  $n$  dimensions of the objects as gradable properties, e.g., size and darkness, so that a 2D object is determined by a given size and shade of gray. For the functions, we set  $F = \{\arg \min_i, \arg \max_i : 0 \leq i < n\}$ . An emerging language could contain compositional messages like ‘(pick the) MOST + BIG’, ‘LEAST + DARK’, etc.

### 4.1 Model

Our model (Figure 1) resembles an encoder-decoder architecture, with the Sender encoding the context/target pair into a message, and the Receiver decoding the message (together with its context  $c'$ ) into an action. Both the encoder and decoder are multi-layer perceptrons with two hidden layers of size 64 and rectified linear activation (ReLU) (Nair and Hinton, 2010; Glorot et al., 2011). A smaller, intermediate layer without an activation function bridges the encoder and decoder and represents the transformation of the input information to messages.

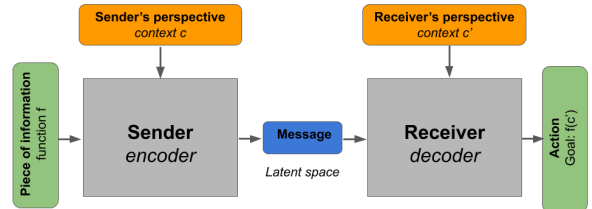


Figure 1: Our model architecture, mixing terminology from the autoencoder and signaling game traditions.

### 4.2 Game Parameters

We manipulated the following parameters:

- **Context identity.** In the *shared* setting, Receiver sees a shuffled version of Sender’s context ( $c' = \text{shuffled}(c)$ ). In the *non-shared* setting, Receiver’s context  $c'$  is entirely distinct from Sender’s. This forces displacement and may incentivize compositional messages, since Sender cannot rely on the raw properties of the target object in communication.
- **Context strictness.** In *strict* contexts, there is a one-to-one (and onto) correspondence be-

tween  $F$  and  $A$  (as in the original Extremity Game from Steinert-Threlkeld, 2019). In *non-strict* contexts, an object may be the arg max or arg min of several dimensions, or of no dimension.

In all experiments, the latent space (message) dimension was always 2,<sup>1</sup> and objects had 5 dimensions. Strict contexts therefore contained 10 objects, while non-strict contexts could contain 5, 10, or 15 objects.

### 4.3 Training Details

We used the Adam optimizer (Kingma and Ba, 2015) with learning rate 0.001,  $\beta_1 = 0.9$ , and  $\beta_2 = 0.999$ . The model was trained for 5,000 epochs by feeding the network with mini-batches of 64 contexts concatenated with one-hot function selectors. The network’s loss is taken as the MSE between the target object  $f(c')$  and the object generated by the Receiver. For each setting of the above parameters, we ran 20 trials with different random seeds.

Code and data will be made available once the paper can be de-anonymized.

## 5 Results

### 5.1 Communicative success

We measure the communicative success of the network by calculating the accuracy of recovering the correct object from  $c'$ . Receiver’s prediction is considered correct if its output is closer to  $f(c')$  than to all other objects in  $c'$ . Accuracy of the different settings is reported in Table 1. While the network handles displacement well (*non-shared contexts*), the model struggles with non-strict contexts. Note that although accuracy is not 100%, it is still well above chance, since e.g. for a context of 10 objects random guessing yields an expected accuracy of 10%. Accordingly, the recovery accuracy for networks before training are at the expected chance level (e.g., for a 10-object, shared, strict setting, accuracy is  $9.92\% \pm 0.01$ , with MSE 8 times larger before than after training).

### 5.2 Discrete signals

Figure 2 depicts message vectors sampled from the latent space layer, before and after training. It is apparent that discrete messages emerge from the

<sup>1</sup>The model also performs well with messages of size 1, not reported here. Using messages of size 2 makes it easier to inspect the latent space using 2-D visualization.

	Shared	Non-shared
<b>Strict</b>		
10 objects	$63.78\% \pm 1.63$	$60.22\% \pm 1.56$
<b>Non-strict</b>		
5 objects	$49.37\% \pm 1.67$	$43.55\% \pm 1.69$
10 objects	$33.06\% \pm 1.47$	$31.89\% \pm 1.63$
15 objects	$27.58\% \pm 1.30$	$27.95\% \pm 1.24$

Table 1: Communicative success, as measured by object recovery accuracy.

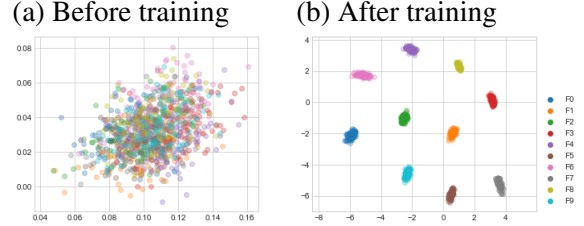


Figure 2: Messages sampled from latent space for objects of size 5 and contexts of 10 objects for (a) an untrained and (b) a trained network. Colors represent the  $f_i \in F$  input part of the Sender.

imposed learning regime. We measured cluster tendency more quantitatively through two measures, one considering Sender’s *production*, and the other Receiver’s *perception*.

First, we sampled 100 contexts, and collected the output of the trained encoder for each of these contexts combined with each possible function  $f$ . We applied an unsupervised clustering algorithm to this set of produced messages (DBSCAN, Ester et al., 1996, with  $\epsilon = 0.5$ ). A label was assigned to each cluster using the ground truth: the label of a cluster is the function  $f$  that was most often at the source of a point in this cluster. This allowed us to compute F1-scores, which are reported in Table 2. The model reached near-optimal clusterization measures for all game parameter settings.

	Shared	Non-shared
<b>Strict</b>		
10 objects	$1.00 \pm 0.00$	$0.90 \pm 0.09$
<b>Non-strict</b>		
5 objects	$0.99 \pm 0.02$	$0.54 \pm 0.15$
10 objects	$1.00 \pm 0.00$	$0.99 \pm 0.01$
15 objects	$1.00 \pm 0.00$	$1.00 \pm 0.00$

Table 2: Discreteness in production, as measured by F1 scores for automatically clusterized messages.

	Shared	Non-shared
<b>Strict</b>		
10 objects	63.39% $\pm$ 1.45	55.37% $\pm$ 3.43
<b>Non-strict</b>		
5 objects	46.94% $\pm$ 1.70	29.40% $\pm$ 5.59
10 objects	32.63% $\pm$ 1.43	31.51% $\pm$ 1.62
15 objects	28.24% $\pm$ 1.11	27.94% $\pm$ 1.20

Table 3: Discreteness in perception, as measured by object recovery accuracy from artificial messages.

The second approach is akin to studying perception. Given the clusterization of the message space, we are able to sample new messages from each cluster, and test Receiver’s perception of these ‘artificial’ messages, which have never been produced by Sender. As a sampling procedure for artificial messages, we take the average of 10 messages from a (now labelled) cluster. These artificial messages are fed to Receiver for 100 different contexts. The output object accuracy for these artificial messages is given in Table 3. The model achieves recovery accuracy similar to when interpreting actual messages.

In sum, we can identify discrete, abstract regions of the latent space corresponding to different functions in the input, just like words form clusters in acoustic space.

### 5.3 Compositionality

Our agents are capable of communicating in abstract situations, namely some in which their contexts are different in the first place. This generalizability suggests that the messages may be ‘compositional’. We here probe for a candidate compositional structure to the latent space, by asking how the messages relate to the structure of the family of functions  $F$ .

First, in the pioneering Mikolov et al., 2013, compositionality is looked for at the level of word embeddings (WE) through addition, most classically asking whether  $WE(\text{queen}) = WE(\text{king}) - WE(\text{man}) + WE(\text{woman})$ .

In the current Game, we can ask whether the messages are related as follows, for any dimensions  $i$  and  $j$ :  $M(c, \arg \max_i) = M(c, \arg \max_j) - M(c, \arg \min_j) + M(c, \arg \min_i)$ . For each such pair of object dimensions we calculate the right-hand side of the equation above for 100 contexts, feed it to Receiver expecting the output for  $\arg \max_i$ , and average the communicative success across all

parameters. This leads to important degradation of communicative success (a drop of at least 24 percentage points across parameter combinations, to around chance level).

Second, we note as others that the composition-as-addition assumption is disputable, both in general and in the original application case (Linzen, 2016; Chen et al., 2017). To abstract away from this issue, we train a ‘composition network’ (an MLP with 2 hidden layers of 64 ReLU units) on the task of predicting  $M(c, \arg \max_i)$  from  $M(c, \arg \max_j)$ ,  $M(c, \arg \min_j)$  and  $M(c, \arg \min_i)$ , therefore letting it discover any function for mixing values, and not involving addition *a priori*. We leave out one dimension  $i_0$  from training, and feed Receiver with the message predicted by the ‘composition network’ from  $M(c, \arg \max_j)$ ,  $M(c, \arg \min_j)$  and  $M(c, \arg \min_{i_0})$ . If the language was compositional, this predicted message should behave like  $M(c, \arg \max_{i_0})$ , but we found that, as in the case of addition, the average communication accuracy for all taken-out parameters dropped dramatically (again, at least 24 percentage points drop).

Complete results for the compositionality tests may be found in the Appendix.

## 6 Conclusion

We proposed a general signaling game framework in which fewer *a priori* assumptions are imposed on the conversational situations. We find in particular that under appropriate conditions, which are met by most studies involving neural signaling games, messages become discrete without the analyst having to force this property into the language (and having to deal with non-differentiability issues). We probed for compositional structure using vector analogies and a generalization thereof, but did not find any evidence of such structure in the emergent language.

Our analysis of discreteness in production and perception can lead to more psycholinguistic-like queries about these emergent languages. For instance, one may ask whether classical ‘Categorical Perception’ effects obtain, whereby messages shifting continuously in the latent space may be interpreted as if they crossed a sharp boundary for interpretation purposes (see Damper and Harnad, 2000 for early discussions in the context of neural architectures). Future work will similarly explore other measures and alternative game settings for the emergence of compositionality.



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