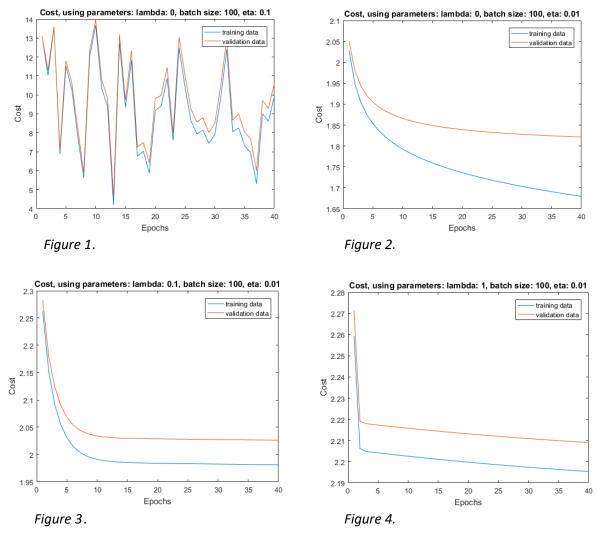
## Report Lab 1

Search Engines DD2424

In this assignment, mini-batch gradient descent was used to classify images from CIFAR-10 into 10 classes. The network only had one layer and L2 regularization was used.

The main result of the report is that the network achieved an accuracy of 37 % in classifying images. This accuracy was achieved when using step size  $\eta$  at 0.01 and no regularization.

The following graphs show the cost functions for different values of  $\lambda$  and  $\eta$ .



If you compare figure 1 to figures 2-4, you can draw the conclusion that if the step size  $\eta$  is too large, the method cannot find a local minimum. When comparing figure 2, 3 and 4 you can see different results depending on how much regularization is used. If regularization is very large as in figure 4, the cost function seems to be pressed down very early. The fact that the network seems to perform worse with regularization, even for the validation data, could suggest that the method becomes underfitted with the regularization.

**Table 1.** Accuracy for different parameters

λ	η	Accuracy
0	0.1	0.1881
0	0.01	0.3678
0.1	0.01	0.3338
1	0.01	0.2192

This table indicates similar results as *figures 1-4*. When the step size is very small, the accuracy 19 % is only somewhat better than with random guessing (10 %). When decreasing the step size to 0.1 the results improve. In this setup, the accuracy is the highest when there is no regularization, and step size 0.01. The accuracy is almost as good when  $\lambda$  is 0.1, but when  $\lambda$  is 1 the accuracy is almost as bad as with the small step size of 0.1.



Figure 5. Weight matrix,  $\lambda$  is set to 0 and  $\eta$  to 0.1 Figure 6. Weight matrix,  $\lambda$  is set to 0 and  $\eta$  to 0.01

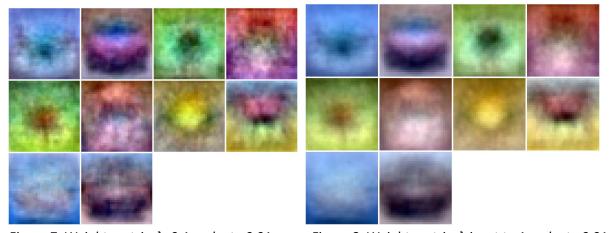


Figure 7. Weight matrix,  $\lambda$ : 0.1 and  $\eta$  to 0.01

Figure 8. Weight matrix,  $\lambda$  is set to 1 and  $\eta$  to 0.01

Figures 5-8 show the weight matrix for different network parameters. If you compare figure 6 to figure 7 and 8 you can see that with increasing regularization the images do seem to generalize the images in a good way. In the second image, you can see the contour of a car, and in the 8<sup>th</sup> image, the contour of a cow. You can see that with regularization, lots of the noise is flattened out, creating a smooth model.

## Code

```
[X,Y,y] = LoadBatch('data batch 1.mat');
K = 10;
d = size(X, 1);
N = size(X, 2);
W = randn(K,d)*0.01;
b = randn(K, 1) *0.01;
lambda = 1;
n epochs = 40;
n^-batch = 100;
eta = 0.01;
[Wstar, bstar] = MiniBatchGD(X, Y, n batch, eta, n epochs, W, b, lambda);
for i=1:10
    im = reshape(Wstar(i, :), 32, 32, 3);
    s im{i} = (im - min(im(:))) / (max(im(:)) - min(im(:)));
    s_{im}\{i\} = permute(s_{im}\{i\}, [2, 1, 3]);
end
montage(s_im);
[Xtest, Ytest, ytest] = LoadBatch('test batch.mat');
acc = ComputeAccuracy(Xtest, ytest, Wstar, bstar);
disp(['Accuracy: ', num2str(acc)]);
function acc = ComputeAccuracy(X, y, W, b)
%Calculate the accuracy scalar
   that is the percentage of correctly classified
    samples
    P = EvaluateClassifier(X, W, b);
    sumCorrect = 0;
    for sample=1:size(P,2)
        [\sim, class] = max(P(:, sample));
        if class == y(sample)
            sumCorrect = sumCorrect + 1;
        end
    end
    acc = sumCorrect / sample;
end
```

```
function J = ComputeCost(X, Y, W, b, lambda)
%Computes the cost
  J is a scalar with the sum of the loss of the network's
       predictions for the images in X relative
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        to the labels and regularization term on W
    s = 0;
    P = EvaluateClassifier(X, W, b);
    N = size(X, 2);
    for i=1:N
        cross = -log(dot(Y(:,i)',P(:,i)));
        s = s + cross;
    end
    s = s / N;
    J = s + lambda*sum(diag(W'*W));
end
function [grad W, grad b] = ComputeGradients(X, Y, P, W, lambda)
\$ \bullet each column of X corresponds to an image and it has size d \times n .
\$ \bullet each column of Y (K×n) is the one-hot ground truth label for the
corresponding
% column of X.
\$\, \bullet \, each column of P contains the probability for each label for the image
\mbox{\%} in the corresponding column of X. P has size K×n.
% • grad W is the gradient matrix of the cost J relative to W and has size
% K×d.
% • grad b is the gradient vector of the cost J relative to b and has size
  K \times 1.
    n = size(X, 2);
    sumW = 0;
    sumb = 0;
    for i=1:n
        y = Y(:,i);
        p = P(:,i);
        x = X(:,i);
        g = - (y'/(y'*p))*(diag(p)-p*p');
        dldW = g'*x'; %size c x d (10*3072)
        sumW = sumW + dldW;
        dldb = g;
        sumb = sumb + dldb;
    end
    grad W = sumW/n + 2*lambda*W;
    grad b = sumb'/n;
end
```

```
function P = EvaluateClassifier(X, W, b)
%Evaluates the classifier by calculating the score
   and softmax
   each column of P contains the probability of each label
    for the image. P has size K*N
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    K = size(W, 1);
    N = size(X, 2);
    P = zeros(K,N);
    for i=1:N
        s = W*X(:,i) + b;
        P(:,i) = \exp(s)/\det(\operatorname{ones}(K,1), \exp(s));
    end
end
function [X, Y, y] = LoadBatch(filename)
%Function that reads the data from the file
   X is a matrix containing image pixel data.
       it has size d*N, N is number of
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        images = 10000, and d is dimensionality = 32*32*2=3072,
응
       each column represents one image
응
   Y contains on each column the one-hot represention of the label
       for each image
       and is the size N*K where K is \#labels = 10
  y is a row vector containing the label for each image, between 1 and 10
    batch = load(filename);
    X = double(batch.data')/255;
    y = batch.labels' + 1;
    N = size(X, 2);
    K = 10;
    Y = zeros(K, N);
    for i=1:N
        Y(y(i),i) = 1;
    end
end
```

```
function [Wstar, bstar] = MiniBatchGD(X, Y, n batch, eta, n epochs, W, b,
%Mini-batch learning function of W and b, with gradient descent
  X training images
   Y labels for training images
  W and b initial values
   lambda regularization factor in the cost function
   GDparams contains n_batch, eta and n_epochs
N = size(X, 2);
costTrain = zeros(1, n epochs);
costVal = zeros(1, n epochs);
[Xval, Yval, ~] = LoadBatch('data batch 2.mat');
for i=1:n epochs
    for j=1:N/n batch
        j start = (j-1)*n batch + 1;
        j end = j*n batch;
        Xbatch = X(:, j start:j end);
        Ybatch = Y(:, j start:j end);
        P = EvaluateClassifier(Xbatch, W, b);
        [grad W, grad b] = ComputeGradients(Xbatch, Ybatch, P, W, lambda);
        W = W - \text{eta*grad } W;
        b = b - eta*grad b;
    end
    costTrain(i) = ComputeCost(X, Y, W, b, lambda);
    costVal(i) = ComputeCost(Xval, Yval, W, b, lambda);
    disp(['epoch: ', num2str(i), '/', num2str(n epochs), '
num2str(costTrain(i))]);
end
Wstar = W;
bstar = b;
plot(1:n epochs, costTrain, 1:n epochs, costVal);
title(['Cost, using parameters: lambda: ', num2str(lambda), ', batch size:
', num2str(n batch), ', eta: ', num2str(eta)]);
xlabel('Epochs')
ylabel('Cost')
legend('training data', 'validation data')
figure
end
```