

Anatomy of the inert two-Higgs-doublet model in the light of the LHC and non-LHC dark matter searches

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The inert two-Higgs-doublet model (i2HDM) is a theoretically well-motivated example of a minimal consistent dark matter (DM) model which provides monojet, mono-Z, mono-Higgs, and vector-boson-fusion + E_T^{miss} signatures at the LHC, complemented by signals in direct and indirect DM search experiments. In this paper we have performed a detailed analysis of the constraints in the full five-dimensional parameter space of the i2HDM, coming from perturbativity, unitarity, electroweak precision data, Higgs data from the LHC, DM relic density, direct/indirect DM detection, and LHC monojet analysis, as well as implications of experimental LHC studies on disappearing charged tracks relevant to a high DM mass region. We demonstrate the complementarity of the above constraints and present projections for future LHC data and direct DM detection experiments to probe further i2HDM parameter space. The model is implemented into the CALCHEP and MICROMEGAs packages, which are publicly available at the HEPMDB database, and it is ready for a further exploration in the context of the LHC, relic density, and DM direct detection.

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I. INTRODUCTION

The evidence for dark matter (DM) is well established from several independent cosmological observations, including galactic rotation curves, cosmic microwave background fits of the WMAP and PLANCK data, gravitational lensing, large scale structure of the Universe, as well as interacting galaxy clusters such as the Bullet Cluster. Despite these large-scale evidences, the microscopic nature of the DM particles remains unknown, since no experiment so far has been able to claim their detection in the laboratory and probe their properties. Potentially, DM can be produced at the LHC and probed in the DM direct detection (DD) underground experiments. The fundamental importance and vast experimental opportunities make the search for and investigation of DM one of the key goals in astroparticle physics and high energy physics (HEP), worthy of the intense efforts undertaken by the physics community.

At the other end of the length scale, the Standard Model (SM) of particle physics recently demonstrated its vitality once again. The scalar boson with mass $m_H \approx 125$ GeV found at the LHC [1,2] closely resembles, in all its manifestations, the SM Higgs boson. Since the SM cannot be the ultimate theory, many constructions beyond the SM (BSM) have been put forth, at different levels of sophistication. Yet, without direct experimental confirmation, none of them can be named the true theory beyond the SM.

One way the particle theory community can respond to this situation is to propose simple, fully calculable, renormalizable BSM models with viable DM candidates. We do not know yet which of these models (if any) corresponds to reality, but all models of this kind offer an excellent opportunity to gain insight into the intricate interplay among various astrophysical and collider constraints. We call here these models minimal consistent dark matter (MCDM) models. MCDM models which can be viewed as toy models, are self-consistent and can easily be incorporated into a bigger BSM model. Because of these attractive features, MCDM models can be considered as the next step beyond DM effective field theory (EFT) (see e.g. [3–15]) and simplified DM models (see e.g. [16–23]).

In this paper, we explore, in the light of the recent collider, astroparticle, and DD DM experimental data, the inert two-Higgs-doublet model (i2HDM), also known as

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the inert doublet model. This model is easily doable with analytic calculations, its parameter space is relatively small, and it can be strongly constrained by the present and future data. The model leads to a variety of collider signatures, and, in spite of many years of investigation, not all of them have yet been fully and properly explored. It is the goal of the present paper to investigate in fine detail the present constraints and the impact of the future LHC and DD DM data on the parameter space of this model.

The i2HDM [24–27] is a minimalistic extension of the SM with a second scalar doublet ϕ_2 possessing the same quantum numbers as the SM Higgs doublet ϕ_1 but with no direct coupling to fermions (the inert doublet). This construction is protected by the discrete Z_2 symmetry under which ϕ_2 is odd and all the other fields are even. The scalar Lagrangian is

$$\mathcal{L} = |D_\mu \phi_1|^2 + |D_\mu \phi_2|^2 - V(\phi_1, \phi_2) \quad (1)$$

with the potential V containing all scalar interactions compatible with the Z_2 symmetry,

$$\begin{aligned} V = & -m_1^2(\phi_1^\dagger \phi_1) - m_2^2(\phi_2^\dagger \phi_2) + \lambda_1(\phi_1^\dagger \phi_1)^2 + \lambda_2(\phi_2^\dagger \phi_2)^2 \\ & + \lambda_3(\phi_1^\dagger \phi_1)(\phi_2^\dagger \phi_2) + \lambda_4(\phi_2^\dagger \phi_1)(\phi_1^\dagger \phi_2) \\ & + \frac{\lambda_5}{2}[(\phi_1^\dagger \phi_2)^2 + (\phi_2^\dagger \phi_1)^2]. \end{aligned} \quad (2)$$

All free parameters here are real,¹ which precludes the CP violation in the scalar sector. There is a large part of the parameter space in which only the first, SM-like doublet acquires the vacuum expectation value (VEV). In the notation $\langle \phi_i^0 \rangle = v_i/\sqrt{2}$, this inert minimum corresponds to $v_1 = v$, $v_2 = 0$. In the unitary gauge, the doublets are expanded near the minimum as

$$\phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H \end{pmatrix}, \quad \phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}h^+ \\ h_1 + ih_2 \end{pmatrix}. \quad (3)$$

The Z_2 symmetry is still conserved by the vacuum state, which forbids direct coupling of any single inert field to the SM fields, and it stabilizes the lightest inert boson against decay. Pairwise interactions of the inert scalars with the gauge bosons and with the SM-like Higgs H are still possible, which gives rise to various i2HDM signatures at colliders and in the DM detection experiments.

The idea that the symmetry-protected second Higgs doublet naturally produces a scalar dark matter candidate was first mentioned more than 30 years ago [24]. However, the real interest in phenomenological consequences of the i2HDM woke up in mid-2000 and intensified in the past

few years. Its simplicity, predictive power, rich yet manageable parameter space, makes it an ideal playground for checking its compatibility with the DM relic density, with the results of the direct and indirect DM searches, and with collider searches of various BSM signals.

Assuming that the lightest inert scalar is the only DM candidate, one typically finds that the low-mass region, below about 50 GeV, is excluded by the relic density constraints coupled with the LHC constraints on the invisible Higgs decay [28–30]. The funnel region, with the DM mass close to $M_H/2$, the intermediate, 100–500 GeV, and the high mass regions are still compatible with data and lead to interesting predictions at colliders. Additional theoretical constraints on the parameter space and DM candidate properties can be deduced from assumptions of full stability of the i2HDM up to the PLANCK scale [31,32] or of multidoublet Higgs inflation [33]. The i2HDM can also produce signals for direct [34] and indirect DM search experiments via heavy inert scalar annihilation, which can be detectable via γ rays [35–37] or via its neutrino [38,39] and cosmic-ray signals [40].

The i2HDM can also have interesting cosmological consequences. Being an example of 2HDM, it possesses a rich vacuum structure, which evolves at high temperatures [41–43]. This opens up the possibility within i2HDM that the early Universe, while cooling down, went through a sequence of phase transitions including strong first-order phase transitions [44–50]. Such analyses are capable of restricting the parameter space; for example, the recent study [50] showed that combining the strong first-order phase transition with other astroparticle and collider constraints gives preference to the funnel region.

There has also been a number of studies on collider signatures of the i2HDM. They focus on specific processes such as SM-like Higgs decays to $\gamma\gamma$ and γZ [28,51–53], multilepton production plus missing transverse momentum (E_T^{miss}) [54–56] with as many as five leptons [57], dijet + E_T^{miss} [58], and dileptons accompanied with dijets [56]. Other works present combined analyses of astroparticle and collider constraints [29,57,59–62]. Comparing the i2HDM predictions with the electroweak precision data, the measured SM-like Higgs properties, the nonobservation of long-lived charged particles and other exotic signals, and finally the astroparticle observations, allows one to significantly restrict the i2HDM parameter space. The recent analysis [29] gave a detailed account of these constraints. For specific benchmark points or benchmark planes in the surviving parameter space, it predicted the cross section of pair production of inert scalars followed by various modes of their decay. As for the specific signatures of the i2HDM at the LHC, dileptons and mono-Z signals were mentioned. An earlier analysis [60] investigated multilepton, multijet, mono-Z, and several channels for the monojet with large E_T^{miss} . Reference [59] took into account one-loop corrections to the masses and, for a part of the numerical scans,

¹Even if we started with a complex λ_5 , we could redefine the second doublet via a global phase rotation, which would render λ_5 real without affecting any other part of the Lagrangian.

included the additional theoretical constraint that the perturbativity and stability be satisfied up to a large scale Λ . The version of i2HDM equipped with Peccei-Quinn $U(1)$ symmetry spontaneously broken to Z_2 was investigated in [62]. Here, dark matter acquires a second component, the axion, which changes the DM phenomenology. It is also possible to hunt for i2HDM at the future colliders, via searching for new scalars and reconstructing the potential [63] or by accurately measuring the SM-like Higgs couplings and deducing patterns of the deviations from the SM [64].

In the present work, to these many studies on the i2HDM, we add the following:

- (i) detailed combined analysis of the i2HDM model in its full five-dimensional (5D) parameter space, taking into account perturbativity and unitarity, LEP and electroweak precision data, Higgs data from the LHC, DM relic density, direct/indirect DM detection complemented by realistic (beyond-the-parton-level) LHC monojet analysis at the LHC;
- (ii) quantitative exploration of the surviving regions of parameters, including very fine details and a qualitatively new region not seen in previous studies, which is enabled by our extensive numerical scans;
- (iii) a combination of different processes giving the LHC monojet signatures: those with direct DM pair production and those with associate production of DM with another scalar with a close mass from the inert multiplet;
- (iv) implication of experimental LHC studies on disappearing charged tracks relevant to a high (≈ 500 GeV) DM mass region;
- (v) separate, equally detailed analyses for the assumptions of the DM relic density being fitted to the PLANCK results or underabundant, allowing thus for additional allowed regions of the parameter space.

All these points above are in close focus of the present paper where we have performed a comprehensive scan and study of the full parameter space of the i2HDM model. In addition, we have performed an independent implementation and validation of the model in two gauges including Higgs-gluon-gluon and Higgs-photon-photon effective couplings, and we made it public together with the LanHEP model source.

The paper is organized as follows. In Sec. II we discuss the i2HDM model parameter space, implementation, theoretical constraints, as well as constraints from LEP and electroweak precision data. In Sec. III we discuss results of a comprehensive scan of the i2HDM parameter space and combined constraints considering both the cases when the relic density is “just right” and agrees with the PLANCK results and when it is underabundant. In this section we also present the reach of LHC studies in the high DM mass region using results on disappearing charged tracks. In Sec. IV we present results on future projections of the LHC

and DM DD experiments in combination with all previous constraints. Finally, in Sec. V we draw our conclusions.

II. i2HDM: PARAMETER SPACE, MODEL IMPLEMENTATION, THEORETICAL AND EXPERIMENTAL CONSTRAINTS

A. Constraints from the Higgs potential

In order to represent a viable model, the potential (2) must be bounded from below and must have a neutral, not charge-breaking, vacuum. The former requirement leads to the well-known restrictions on the free parameters of the model,

$$\begin{aligned} \lambda_1 > 0, \quad \lambda_2 > 0, \quad 2\sqrt{\lambda_1\lambda_2} + \lambda_3 > 0, \\ 2\sqrt{\lambda_1\lambda_2} + \lambda_3 + \lambda_4 - |\lambda_5| > 0. \end{aligned} \quad (4)$$

The absence of the charge-breaking vacuum is guaranteed if one assumes

$$\lambda_4 - |\lambda_5| < 0. \quad (5)$$

This is a sufficient but not necessary condition for the vacuum to be neutral. A neutral vacuum can also be achieved for positive $\lambda_4 - |\lambda_5|$ with appropriate m_1^2 and m_2^2 . However, in this case the lightest DM candidate will be the charged scalar. Condition (5) avoids this situation as well.

Once these restrictions are applied, the vacuum is neutral, and one can calculate the masses of the physical Higgs bosons. In addition to the SM-like scalar H , one gets charged h^\pm and neutral h_1, h_2 scalars. It is well known that the two neutral scalars of the i2HDM have opposite CP parities, but it is impossible to unambiguously assign which of them is CP even and which is CP odd. In the absence of any suitable vertex, the model has two CP symmetries, $h_1 \rightarrow h_1, h_2 \rightarrow -h_2$ and $h_1 \rightarrow -h_1, h_2 \rightarrow h_2$, which get interchanged upon basis change $\phi_2 \rightarrow i\phi_2$. Either can be used as the CP symmetry of the model, making the specification of the CP properties of h_1 and h_2 a basis dependent statement. Therefore, we denote the two neutral inert scalar masses as $M_{h_1} < M_{h_2}$, without specifying which is scalar and pseudoscalar. The masses of the physical scalars are

$$\begin{aligned} M_H^2 &= 2\lambda_1 v^2 = 2m_1^2, & M_{h^+}^2 &= \frac{1}{2}\lambda_3 v^2 - m_2^2, \\ M_{h_1}^2 &= \frac{1}{2}(\lambda_3 + \lambda_4 - |\lambda_5|)v^2 - m_2^2, \\ M_{h_2}^2 &= \frac{1}{2}(\lambda_3 + \lambda_4 + |\lambda_5|)v^2 - m_2^2 > M_{h_1}^2. \end{aligned} \quad (6)$$

The mass differences, written as

$$M_{h_2}^2 - M_{h_1}^2 = |\lambda_5|v^2, \quad M_{h^+}^2 - M_{h_1}^2 = -(\lambda_4 - |\lambda_5|)v^2/2, \quad (7)$$

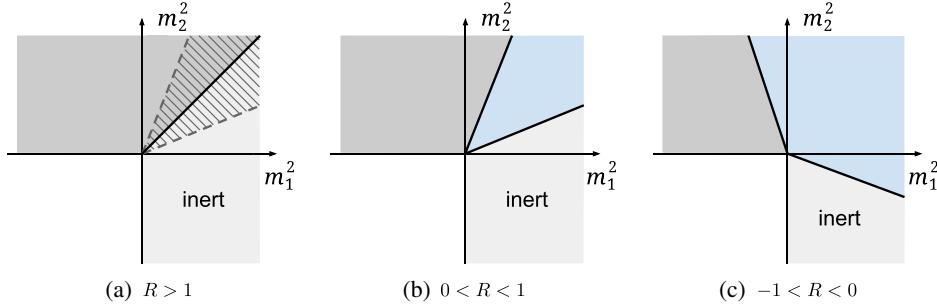


FIG. 1. Restrictions on the (m_1^2, m_2^2) plane coming from the requirement that the inert vacuum is the deepest minimum of the potential. The three cases correspond to (a) $R > 1$, (b) $0 < R < 1$, (c) $-1 < R < 0$. Light and dark grey correspond to models with an inert $v_1 = v$, $v_2 = 0$ and a pseudoinert $v_1 = 0$, $v_2 = v$ vacuum, respectively, while the blue region in between corresponds to the mixed vacuum, when both v_1 and v_2 are nonzero. The dashed region in the left plot indicates coexistence of the inert and pseudoinert minima at different depths.

highlight the role of the parameters λ_4 and λ_5 and are consistent with (5). It should also be stressed that the parameters λ_1 and m_1^2 correspond to the Higgs potential in the SM, and can thus be fixed by the values of the VEV and Higgs mass.

One also notices that the sign of λ_5 is phenomenologically irrelevant: flipping the sign of λ_5 would only lead to swapping the CP parities of the inert neutral scalars, which are unobservable anyway. In order to eliminate double counting, we make the standard choice of $\lambda_5 < 0$ and introduce the shorthand notation $\lambda_{345} = \lambda_3 + \lambda_4 + \lambda_5$. The latter parameter plays an important phenomenological role, as it governs the Higgs-DM interaction vertex $H h_1 h_1$. For future convenience, we also introduce the shorthand notation

$$\tilde{\lambda}_{345} \equiv \lambda_3 + \lambda_4 - \lambda_5 = \lambda_{345} + 2|\lambda_5| = \lambda_{345} + \frac{2(M_{h_2}^2 - M_{h_1}^2)}{v^2}, \quad (8)$$

which is not a new free parameter and is the combination which governs, in particular, the $H h_2 h_2$ coupling as well as the quartic coupling of h_1 to the longitudinal Z bosons $h_1 h_1 Z_L Z_L$.

With all these conventions, we describe the five-dimensional parameter space of i2HDM with the following phenomenologically relevant variables:

$$\begin{aligned} M_{h_1}, \quad M_{h_2} &> M_{h_1}, \quad M_{h^+} > M_{h_1}, \\ \lambda_2 > 0, \quad \lambda_{345} &> -2\sqrt{\lambda_1 \lambda_2}. \end{aligned} \quad (9)$$

Another set of theoretical constraints comes from the symmetry breaking patterns in i2HDM [24] and from the fact that the potential can have two minima at different depths. Following [44], we introduce $R = \lambda_{345}/2\sqrt{\lambda_1 \lambda_2}$, which satisfies $R > -1$. Requiring that the inert vacuum corresponds to the global minimum leads to the following

conditions on the parameters of the potential, apart from $m_1^2 > 0$:

$$\begin{aligned} m_2^2 < \frac{\lambda_{345}}{2\lambda_1} m_1^2 &= R \sqrt{\frac{\lambda_2}{\lambda_1} m_1^2}, \quad \text{if } |R| < 1, \\ m_2^2 < \sqrt{\frac{\lambda_2}{\lambda_1} m_1^2}, &\quad \text{if } R > 1. \end{aligned} \quad (10)$$

In Fig. 1 we visualize these restrictions on the (m_1^2, m_2^2) plane for the three choices of R . The inert, $v_1 = v$, $v_2 = 0$, and pseudoinert, $v_1 = 0$, $v_2 = v$, vacua can coexist only when $R > 1$, which is shown by the dashed region in Fig. 1(a). For $R > 1$, the second line in Eq. (10) is a stronger condition than the first line, and it guarantees that the inert minimum is the deepest one. This condition is shown in Fig. 1(a) by the solid black line.

Rewriting conditions (10) for the physical parameters we get the constraint on the Higgs potential in the following compact final form:

$$\text{the trivial one, } M_{h_1}^2 > 0 \quad \text{for } |R| < 1, \quad (11)$$

and

$$\begin{aligned} M_{h_1}^2 > (\lambda_{345}/2\sqrt{\lambda_1 \lambda_2} - 1)\sqrt{\lambda_1 \lambda_2} v^2 \\ = (R - 1)\sqrt{\lambda_1 \lambda_2} v^2 \quad \text{for } R > 1, \end{aligned} \quad (12)$$

where $\lambda_1 \approx 0.129$ is fixed as in the Standard Model by the Higgs mass (6). The latter condition places an upper bound on λ_{345} for a given DM mass M_{h_1} .

B. Model implementation

We have implemented the i2HDM into the CALCHEP package [65] with the help of the LANHEP program [66,67] for automatic Feynman rules derivation. The effective Hgg and $H\gamma\gamma$ vertices were included, and the model was

cross-checked in two different gauges to ensure a correct, gauge invariant implementation. It is publicly available at the High Energy Physics Model Data-Base (HEPMDB) [68] at <http://hepmdb.soton.ac.uk/hepmdb:0715.0187> together with the LANHEP source of the model. The model is implemented in terms of the five independent parameters defined in Eq. (9), consisting of three physical masses and two couplings. We found this choice the most convenient for exploration of i2HDM phenomenology and constraints of its parameter space. We should stress that the M_{h_1} and M_{h_2} parameters conveniently define the mass order of the two neutral inert states *independently* of their CP properties. This choice is especially convenient and relevant for collider phenomenology since, as we discussed above, one cannot assign (or determine) the CP parity of each neutral inert scalar.

To explore the phenomenology of the i2HDM we need to consider other constraints on its parameter space in addition to those coming from vacuum stability which we discussed above.

C. Constraints from perturbativity and unitarity

The first requirement we impose on the quartic couplings in (2) is that their values are such that perturbative calculations can be trusted in the model. The most effective way is to impose perturbative unitarity on all the scattering processes involving the scalars. Following [51], we impose this condition on the full scattering matrix, which leads to the following bounds on combinations of couplings e_i :

$$|e_i| \leq 8\pi, \quad (13)$$

where $e_{1,2} = \lambda_3 \pm \lambda_4$, $e_{3,4} = \lambda_3 \pm \lambda_5$, $e_{5,6} = \lambda_3 + 2\lambda_4 \pm 3\lambda_5$, $e_{7,8} = -\lambda_1 - \lambda_2 \pm \sqrt{(\lambda_1 - \lambda_2)^2 + \lambda_4^2}$, $e_{9,10} = -3\lambda_1 - 3\lambda_2 \pm \sqrt{9(\lambda_1 - \lambda_2)^2 + (2\lambda_3 + \lambda_4)^2}$, $e_{11,12} = -\lambda_1 - \lambda_2 \pm \sqrt{(\lambda_1 - \lambda_2)^2 + \lambda_5^2}$. The parameter λ_1 is fixed by SM-Higgs mass and the vacuum expectation value. One can verify that the constraints given by Eq. (13) imply that all quartic couplings in (2) are bound to be smaller than 8π , thus within the perturbative regime. The perturbativity constraints can also be used to find upper bounds on the two input couplings we defined in the previous section, i.e. λ_2 and λ_{345} . From e_{10} one finds

$$\lambda_2 < \lambda_2^{\max} < 4\pi/3, \quad (14)$$

where λ_2^{\max} is a function of model parameters, while from $e_5 = 3\lambda_{345} - (2\lambda_3 + \lambda_4)$, combined with e_{10} in the limit $\lambda_2 = 0$, we obtain an upper bound for λ_{345} ,

$$\begin{aligned} -1.47 &\approx -2\sqrt{\lambda_1(4\pi/3)} < -2\sqrt{\lambda_1\lambda_2^{\max}} < \lambda_{345} \\ &\lesssim \frac{2}{3} \times 8\pi - \lambda_1, \end{aligned} \quad (15)$$

where we expanded at leading order in the small coupling λ_1 , and the lower bound comes from the stability of the potential. This limit, derived from the constraints on e_5 and e_{10} is not actually the most stringent one: in the limit of $\lambda_2 \rightarrow 0$ we have found that the biggest value for λ_{345} is realized in the $|\lambda_{4,5}| \rightarrow 0$ limit when $\lambda_3 = 4\pi$ and, respectively, $\lambda_{345} \simeq 4\pi$. After expansion in the small coupling λ_1 , the upper limit on λ_{345} in the small λ_2 limit reads as

$$\lambda_{345} \lesssim 4\pi - \frac{3}{2}\lambda_1, \quad (16)$$

while for finite λ_2 the limit can be found numerically. We would like to note that the limit from perturbative unitarity and perturbativity given by Eqs. (13)–(16) we are using in our study is consistent with that implemented in the 2HDMC code [69].

One should also stress that the vacuum stability condition given by Eq. (12) sets an important constraint on the maximum value of λ_{345} in the small M_{h_1} region (which is the region of our special interest because of the collider phenomenology constraints as we discuss below). This can be seen from Eq. (12) which can be written as

$$\lambda_{345} < 2 \left(\frac{M_{h_1}^2}{v^2} + \sqrt{\lambda_1 \lambda_2^{\max}} \right). \quad (17)$$

In Fig. 2, we present viable parameter space in the $(\lambda_{345}, \lambda_2)$ plane after constraints from Eq. (13) as well as constraints from the scalar potential given by Eqs. (11), (12), (17). To produce this plot we have performed the wide random scan to cover the full five-dimensional parameter space of the model, with the following chosen range for the model parameters:

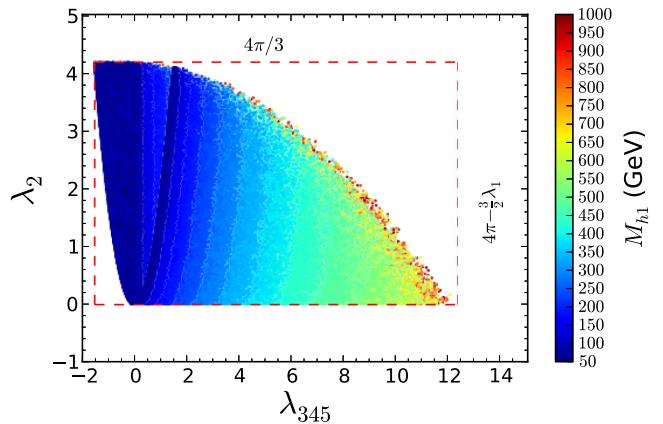


FIG. 2. The part of the $(\lambda_{345}, \lambda_2)$ parameter space allowed by the unitarity, perturbativity, and scalar potential constraints.

$$\begin{aligned} 10 \text{ GeV} &< M_{h_1, h_2, h^+} < 1000 \text{ GeV} \\ 0 &< \lambda_2 < \frac{4\pi}{3} \\ -1.47 &< \lambda_{345} < 4\pi. \end{aligned} \quad (18)$$

The color map in Fig. 2 presents the values for the third essential parameter, the DM candidate mass M_{h_1} , with points of smaller values of M_{h_1} on the top of points with larger M_{h_1} values. From Fig. 2 one can observe a nontrivial shape of the allowed parameter space in the $(\lambda_{345}, \lambda_2)$ plane defined by the constraints mentioned above. In particular, for small M_{h_1} values, the upper limit on λ_{345} comes from Eq. (17) which restricts $H h_1 h_1$ coupling λ_{345} to be not very large. The value of λ_2^{\max} entering there can be found in general only numerically.

D. Constraints from LEP and electroweak precision data

Very strong constraints on the i2HDM arise from precision data and searches from LEP experiments. First of all, the model should respect the precise measurements of the W and Z widths which lead to the following lower limit on the odd scalar masses:

$$\begin{aligned} M_{h_1} + M_{h^+} &> M_{W^+}, \quad M_{h_2} + M_{h^+} > M_{W^+}, \\ M_{h_1} + M_{h_2} &> M_Z, \quad 2M_{h^+} > M_Z, \end{aligned} \quad (19)$$

to make sure that $\Gamma(W^+ \rightarrow h_1 h^+, h_2 h^+)$ and $\Gamma(Z \rightarrow h_1 h_2, h^+ h^-)$ decay channels are kinematically forbidden.

While studying the phenomenology of the i2HDM, we should also make sure that Electroweak Precision Test (EWPT) data are respected. As we know, EWPT can be expressed in terms of three measurable quantities, called S , T , and U , that parametrize contributions from beyond standard model physics to electroweak radiative corrections [70]. The contribution to the S and T parameters [26] can be written as

$$\begin{aligned} S = \frac{1}{72\pi} \frac{1}{(x_2^2 - x_1^2)^3} &[x_2^6 f_a(x_2) - x_1^6 f_a(x_1) \\ &+ 9x_2^2 x_1^2 (x_2^2 f_b(x_2) - x_1^2 f_b(x_1))], \end{aligned} \quad (20)$$

where $x_1 = M_{h_1}/M_{h^+}$, $x_2 = M_{h_2}/M_{h^+}$, $f_a(x) = -5 + 12 \log(x)$, $f_b(x) = 3 - 4 \log(x)$, and

$$\begin{aligned} T = \frac{1}{32\pi^2 \alpha v^2} &[f_c(M_{h^+}^2, M_{h_2}^2) + f_c(M_{h^+}^2, M_{h_1}^2) \\ &- f_c(M_{h_2}^2, M_{h_1}^2)], \end{aligned} \quad (21)$$

where the function $f_c(x, y)$ is defined by

$$f_c(x, y) = \begin{cases} \frac{x+y}{2} - \frac{xy}{x-y} \log\left(\frac{x}{y}\right), & x \neq y \\ 0, & x = y \end{cases}.$$

We have written the contributions to S and T in a form which demonstrates explicitly their symmetry with respect to swapping $h_1 \leftrightarrow h_2$, pointing again to the fact that one cannot distinguish their CP properties. With U fixed to be zero, the central values of S and T , assuming a SM Higgs boson mass of $m_h = 125$ GeV, are given by [71]

$$S = 0.06 \pm 0.09, \quad T = 0.1 \pm 0.07 \quad (22)$$

with correlation coefficient +0.91. The effect of the constraints on S and T is presented in Fig. 3, where panels 3(a) and 3(b) present the color map of the S and T parameters, respectively, in the (M_{h^+}, M_{h_2}) plane. One can see that the T variable is more sensitive than S to this mass split; thus only modest splits are allowed by EWPT data. Finally, Fig. 3(c) presents the color map of the $M_{h^+} - M_{h_2}$ split in the (S, T) plane together with the 65% and 95% exclusion contours, based on a χ^2 with 2 degrees of freedom. One can see that EWPT data prefer a modest positive $M_{h^+} - M_{h_2}$ mass split below about 100 GeV, which is mainly defined by the T parameter, while the role and the respective range of variation of S is milder. One should stress that it is crucial to take into account the correlation between S and T and combine limits from these two parameters. This combination gives a much stronger limit on the parameter space, in particular on the $M_{h^+} - M_{h_2}$ mass split, while a much larger splitting would naively be allowed by looking at the S and T values separately. This can be seen from Figs. 3(a) and 3(b), respectively.

We also excluded the region defined by the intersection of the conditions below:

$$\begin{aligned} M_{h_1} &< 80 \text{ GeV}, \quad M_{h_2} < 100 \text{ GeV}, \\ M_{h_2} - M_{h_1} &> 8 \text{ GeV}. \end{aligned} \quad (23)$$

This region is excluded by the LEP data since it would lead to a visible dijet or dilepton signal as demonstrated in [72] where a reinterpretation in the i2HDM of a LEP-II limit of the second neutralino production in the Minimal Supersymmetric Standard Model (MSSM) was presented. A more detailed analysis of this specific region of the parameter space—low M_{h_1} and M_{h_2} with large enough mass gap—was studied recently [73]. One should also mention that $e^+ e^- \rightarrow h^+ h^-$ production at LEP2 sets

$$M_{h^+} > 70 \text{ GeV} \quad (24)$$

as found in [74] as a result of the reinterpretation of LEP-II limits on charginos.

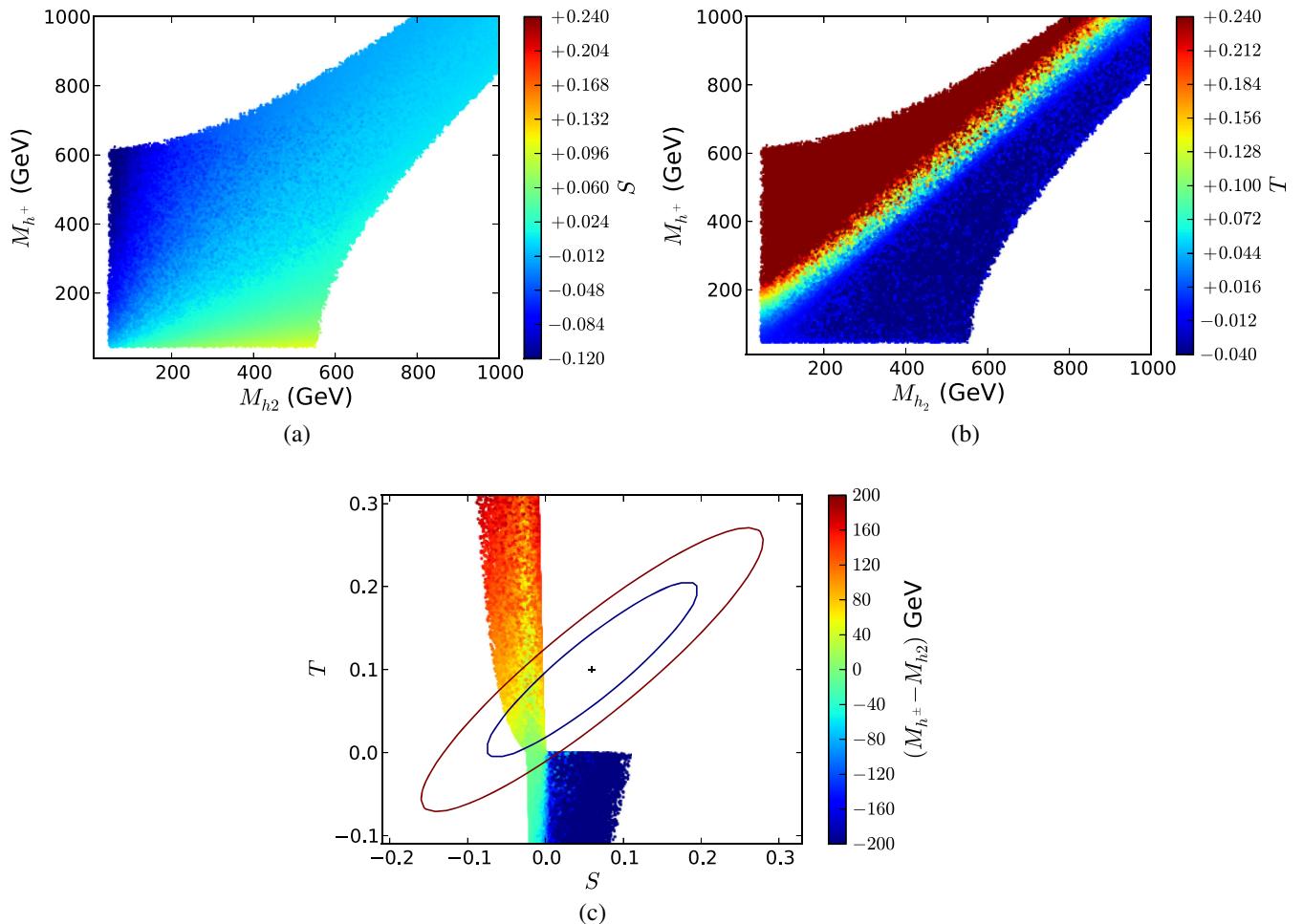


FIG. 3. Effect of the S and T constraints on the $M_{h^+} - M_{h_2}$ mass difference: (a) and (b) show the color map of the S and T parameters, respectively, in the (M_{h^+}, M_{h_2}) plane; (c) shows the color map of the $M_{h^+} - M_{h_2}$ split in the (S, T) plane together with the 65% and 95% exclusion contours based on the χ^2 (S, T) characterization for 2 degrees of freedom.

E. Constraints from LHC Higgs data

The LHC Higgs data further restrict the i2HDM parameters space in the form of constraints on the couplings of the SM-like Higgs boson. A collection of combined fits from the Run I data, for both ATLAS and CMS, can be found in [75]. In the i2HDM, the leading effect is encoded in two observables: the decays of the Higgs into two dark matter scalars, $H \rightarrow h_1 h_1$, which is kinematically open when $M_{h_1} < M_H/2$; and the contribution of the charged Higgs loops to the $H \rightarrow \gamma\gamma$ decay. In principle, we would need to do a two-parameter fit of the available Higgs data. None of the fits presented in [75] can therefore be directly applied in our case.

A simpler possibility is, instead, to consider the best possible bound from the available fits on the two parameters. We follow this simpler procedure, confident that it will lead to a somewhat more conservative estimation of the bounds. For the invisible Higgs branching ratio, we consider the bound coming from the dedicated ATLAS search [76]

$$\text{Br}(H \rightarrow \text{invisible}) < 28\% \quad (25)$$

at the 95% C.L., which is comparable with a 36% limit from the combined CMS analysis [77].²

For the second observable, the diphoton decay rate, we consider the result from the combined fit on the signal strength in the diphoton channel [75]:

$$\frac{\text{Br}^{\text{BSM}}(H \rightarrow \gamma\gamma)}{\text{Br}^{\text{SM}}(H \rightarrow \gamma\gamma)} = \mu^{\gamma\gamma} = 1.14^{+0.38}_{-0.36}, \quad (26)$$

where we doubled the 1σ errors given in [75] to obtain the $\mu^{\gamma\gamma}$ range at the 95% C.L. A sufficiently light charged

²One could also limit $\text{Br}(H \rightarrow \text{invisible})$ using $\text{Br}(H \rightarrow \text{BSM}) < 34\%$ at 95% C.L. exclusion from Run 1 ATLAS-CMS Higgs data analysis [75]. However, here we use the $\text{Br}(H \rightarrow \text{invisible}) < 28\%$ limit from a dedicated ATLAS search as it is less model dependent.

Higgs with sufficiently large λ_3 coupling to the SM Higgs boson, which would bring the $H \rightarrow \gamma\gamma$ decay beyond the quoted limit, is excluded.

It should be noted that we would expect a proper two-parameter fit to lead to stronger constraints than the ones we use; however, the qualitative impact of the constraints should be unchanged. For example, the partial decay width of the Higgs into DM which is defined by

$$\Gamma(H \rightarrow h_1 h_1) = \frac{1}{8\pi} \frac{\lambda_{345}^2 M_W^2}{g_W^2 M_H} \sqrt{1 - 4 \frac{M_{h_1}^2}{M_H^2}}, \quad (27)$$

where g_W is the weak coupling constant, provides the following bound on λ_{345} :

$$|\lambda_{345}| < \left(\frac{8\pi g_W^2 \Gamma_{\text{SM}} M_H}{M_W^2 \left(\frac{1}{\text{Br}_{\text{invis}}^{\text{max}}} - 1 \right) \sqrt{1 - 4 \frac{M_{h_1}^2}{M_H^2}}} \right)^{1/2}, \quad (28)$$

where $\text{Br}_{\text{invis}}^{\text{max}} = 0.28$ is the current bound on the maximal value of branching ratio of the Higgs boson decay into invisible mode. The above limit on λ_{345} is M_{h_1} dependent: for $M_{h_1}/M_H \ll 1$ it is about 0.019, while for M_{h_1} closer to the threshold, e.g. 60 GeV, the limit on λ_{345} increases almost by a factor of 2 and reaches a value of 0.036. In addition, we have included the limit from $H \rightarrow h_2 h_2$ when h_2 is close in mass to h_1 , which can be trivially done, taking into account that $H h_2 h_2$ coupling is equal to $\tilde{\lambda}_{345}$ in Eq. (8). We discuss these limits in more details below, together with the DM constraints.

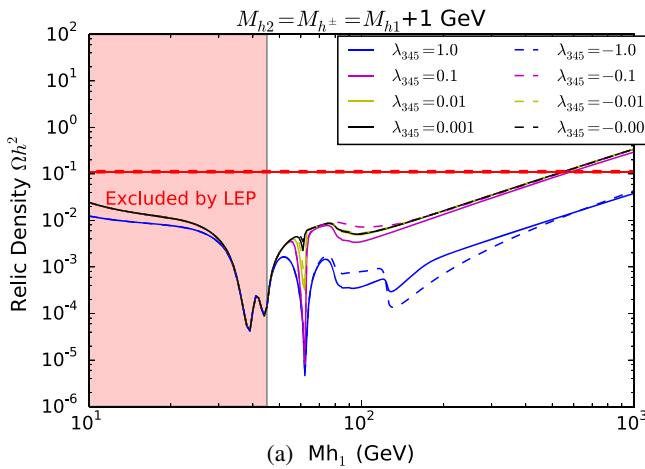
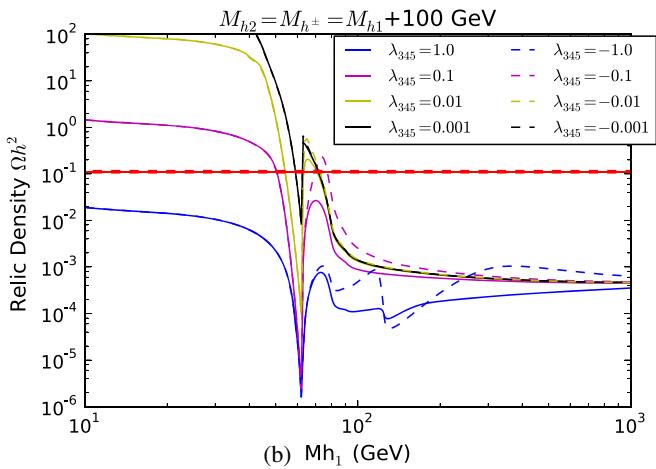
(a) M_{h_1} (GeV)(b) M_{h_1} (GeV)

FIG. 4. The relic density, $\Omega_{\text{DM}} h^2$, as a function of M_{h_1} for various λ_{345} parameters. The red-shaded region in the left frame is excluded by the LEP data, since in this region W and Z bosons would decay to the light inert scalars. The horizontal red line corresponds to the relic density upper limit given by Eq. (30).

F. Dark matter relic density and direct/indirect detection

The results from PLANCK [78,79] (see also WMAP [80]) have further decreased the error on the already quite precise measurement of the dark matter relic density, $\Omega_{\text{DM}} h^2$:

$$\Omega_{\text{DM}}^{\text{Planck}} h^2 = 0.1184 \pm 0.0012. \quad (29)$$

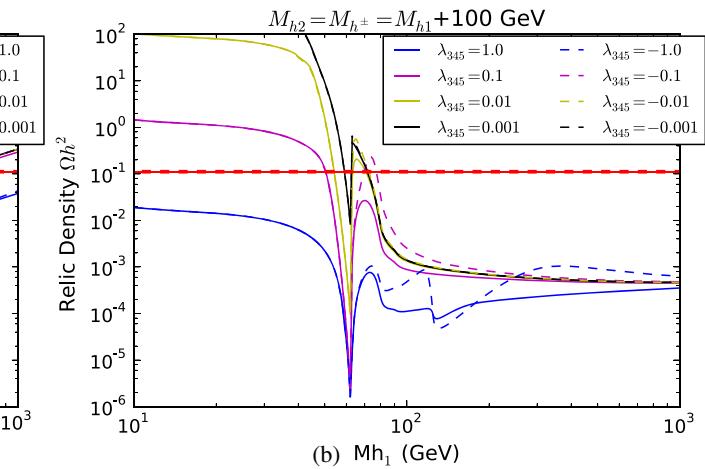
In the i2HDM model, the lightest inert scalar h_1 is stable and contributes to this relic density. In our study we take the upper limit on $\Omega_{\text{DM}} h^2$ as the hard one, excluding the parameter space points which lead to DM overabundance. However, we do not exclude the i2HDM parameter space regions where h_1 is underabundant, allowing for other sources of DM coming from an additional new physics sector.

We have evaluated $\Omega_{\text{DM}} h^2$ with the MICROMEGAS 2.4.1 package [81–83] since it directly reads the model files in CALCHEP format. In our analysis we have assumed 10% theoretical uncertainty on the DM relic density prediction since it is based on the tree-level calculation. This uncertainty is the dominant one in comparison to about 1% uncertainty on DM fit from the latest PLANCK results given above and relax the DM relic density limit to the following one at 95% C.L.:

$$\begin{aligned} \Omega_{\text{DM}}^{\text{limit}} h^2 &= 0.1184 \pm 2 \times 0.1184/10 \\ &\simeq 0.118 \pm 2 \times 0.012, \end{aligned} \quad (30)$$

which we will refer here still as “PLANCK limit.”

Figure 4(a) shows the relic density in the case of quasidegenerate h_1 , h_2 , and h^+ masses, $M_{h_2} = M_{h^+} = M_{h_1} + \Delta M = M_{h_1} + 1$ GeV. This case is qualitatively



different from the case with a non-negligible mass splitting as illustrated in Fig. 4(b), where we chose $M_{h_2} = M_{h^+} = M_{h_1} + \Delta M = M_{h_1} + 100$ GeV. One should also note that scenarios with positive or negative λ_{345} values of the same magnitude are qualitatively similar, except for the effect of interference (see dashed versus solid curves in Fig. 4). One can observe the following effects and features of the model in Fig. 4:

- (i) The red-shaded region in Fig. 4(a) is excluded by the LEP data, since in this region W and Z bosons would decay to the light inert scalars. Respectively, the effect of the resonant coannihilation, $h_1 h_2 \rightarrow Z$ and $h_1 h^+ \rightarrow W^+$, can be seen in this region in the first two dips for $M_{h_1} \sim 40$ and 45 GeV. These processes are governed by the gauge coupling constant and are independent of λ_{345} .
- (ii) In the case of larger $M_{h_2} - M_{h_1}$ mass split [Fig. 4(b)], this effect disappears since $M_{h_1} + M_{h_2} > M_Z$ and $M_{h_1} + M_{h^+} > M_W$.
- (iii) The sharpest dip in the $\Omega_{\text{DM}} h^2$ dependence of M_{h_1} is at 65 GeV and corresponds to the DM annihilation through the Higgs boson $h_1 h_1 \rightarrow H$. It is present in both cases.
- (iv) At higher masses, we observe a wider and more shallow dip at around 80–90 GeV from $h_1 h_1 \rightarrow W^+ W^-$ and $h_1 h_1 \rightarrow ZZ$ channels which are merged together.
- (v) Finally, the last dip around 125 GeV corresponds to the reduction of the DM relic density due to the opening of the $h_1 h_1 \rightarrow HH$ annihilation channel. This dip takes place only for large values of λ_{345} , which provide a high enough rate for the $h_1 h_1 \rightarrow HH$ process via the s -channel Higgs boson.
- (vi) The pattern of these last three dips is the same for the larger mass split scenario presented in Fig. 4(b). In both scenarios, the interference effect is sensitive to the sign of λ_{345} and appears in this region as a result of the positive or negative interference of the s -channel Higgs boson exchange diagram and the rest of annihilation diagrams.
- (vii) One can also observe qualitative differences in the asymptotic behavior of the DM relic density for small and large M_{h_1} values for different ΔM . In the $\Delta M = 1$ GeV case with $M_{h_1} < 65$ GeV, the effective coannihilation of the inert scalars keeps the DM density always below the PLANCK limit. For $\Delta M = 100$ GeV, DM coannihilation is suppressed and the relic density is equal or below the experimental limit only for large values of λ_{345} ($\lambda_{345} \gtrsim 0.3$) which are excluded by LHC limits on the invisible Higgs decay; see Eq. (28).
- (viii) For M_{h_1} well above 65 GeV, coannihilation effects become less important in comparison with $h_1 h_1$ annihilation into vector bosons, which opens in this region. For this annihilation process the quartic

couplings of DM with longitudinal vector bosons $h_1 h_1 V_L V_L$ play an important role. For $h_1 h_1 Z_L Z_L$, it is equal to $\tilde{\lambda}_{345}$ defined in (8), while for $h_1 h_1 W_L W_L$ it is given by $\lambda_3 = \lambda_{345} + 2(M_{h^+}^2 - M_{h_1}^2)/v^2$. For small mass splittings $\Delta M_c = M_{h^+} - M_{h_1}$ and $\Delta M_2 = M_{h_2} - M_{h_1}$, the correspondingly small values of the $h_1 h_1 V_L V_L$ quartic couplings generate a low $h_1 h_1$ annihilation cross section $\langle \sigma v \rangle$, which decreases with growing M_{h_1} . Eventually this leads to a comparatively high value of $\Omega_{\text{DM}} h^2$ (which increases with M_{h_1} both due to the decrease of $\langle \sigma v \rangle$ as well as the increase of the DM mass) which reaches the PLANCK limit for large enough M_{h_1} as one can see from Fig. 4(a). On the contrary, for large ΔM_c and/or ΔM_2 , the mass splittings generate a high rate for $h_1 h_1$ annihilation into vector bosons, which rises with growing M_{h_1} . This generates a DM density below the experimental limit even for large values of M_{h_1} . In this scenario the potential increase of $\Omega_{\text{DM}} h^2$ due the large DM mass is compensated by the respective increase of $\langle \sigma v \rangle$ and leads to an approximately flat $\Omega_{\text{DM}} h^2$ versus M_{h_1} in the 100–1000 GeV range. This makes the asymptotic behavior of the DM density versus M_{h_1} qualitatively different for $\Delta M = 100$ GeV as compared to $\Delta M = 1$ GeV; see Fig. 4(b). These two scenarios with the large and small ΔM_c , ΔM_2 mass splittings qualitatively cover the whole parameter space of the i2HDM.

We have also checked whether the i2HDM parameter space is consistent with the limits from DM DD experiments. We have evaluated the spin-independent cross section of DM scattering off the proton, σ_{SI} , also using the MICRONEGAs package. In Fig. 5 limits from LUX100 are shown by the shaded green area where the left and right frames illustrate the small and large ΔM scenarios as in Fig. 4. To present the results in Fig. 5, we use the rescaled DD cross section, $\hat{\sigma}_{\text{SI}} = R_\Omega \times \sigma_{\text{SI}}$, where the scaling factor $R_\Omega = \Omega_{\text{DM}}/\Omega_{\text{DM}}^{\text{Planck}}$ takes into account the case of h_1 representing only a part of the total DM budget, thus allowing for a convenient comparison of the model prediction with the limits from LUX [84].

The flat asymptotic of $\hat{\sigma}_{\text{SI}}$ in Fig. 5(a) for high M_{h_1} means that the decrease of the proton-DM scattering cross section σ_{SI} with increasing M_{h_1} is compensated by the growth of the relic density which one can observe in Fig. 4(a). In Fig. 5(b), on the other hand, $\hat{\sigma}_{\text{SI}}$ drops with large and increasing values of M_{h_1} . This can be understood by observing from Fig. 4(b) that in this region $R_\Omega = \Omega_{\text{DM}}/\Omega_{\text{DM}}^{\text{Planck}} \simeq \text{const}$, and therefore the asymptotic behavior of $\hat{\sigma}_{\text{SI}}$ is the same as for σ_{SI} ; that is, it goes down as M_{h_1} grows due to the reduced $\langle \sigma v \rangle$.

A related question is whether the model can be better probed by indirect detection (ID) experiments, i.e. the

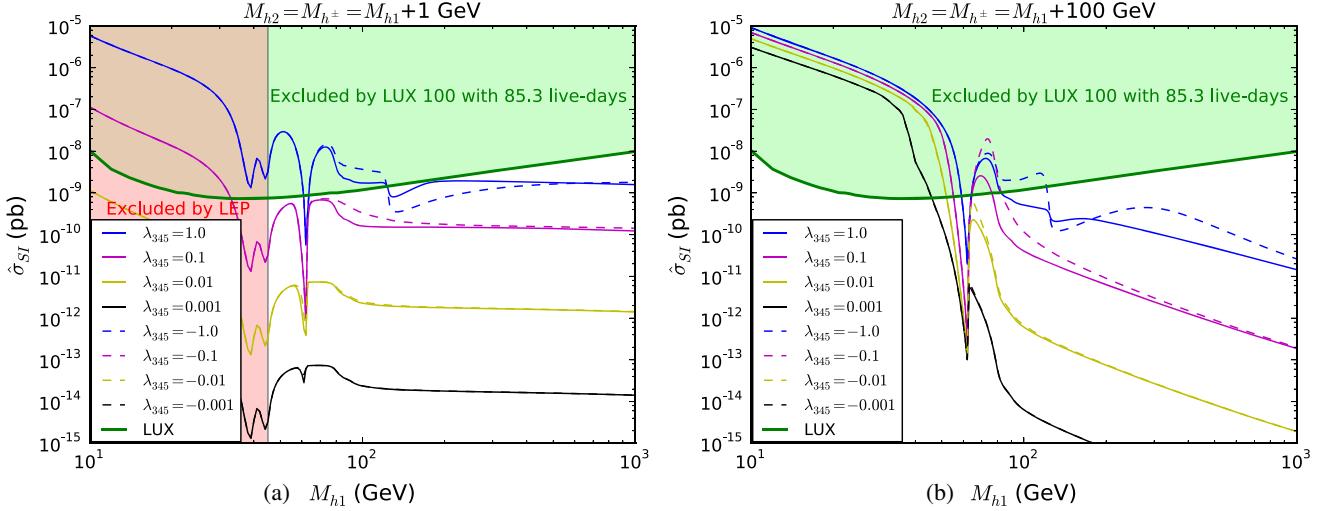


FIG. 5. Rescaled spin independent direct detection rates $\hat{\sigma}_{SI}$ versus M_{h_1} and the LUX100 constraint. The red-shaded region in the left frame is excluded by LEP data.

detection of energetic cosmic rays like e^+ , γ , p , or \bar{p} , which may be created by the annihilation of h_1 pairs. We have checked that the strongest bounds on the i2HDM parameter space coming from such experiments are set by gamma ray telescopes: both the Fermi-LAT gamma-ray space telescope [85] as well as ground based telescopes. Fermi-LAT is sensitive to gamma rays particularly in the low mass range up to $\mathcal{O}(100 \text{ GeV})$, but the bounds are not competitive with those coming from DD. This conclusion is also confirmed by studies in Ref. [60]. Another recent work, Ref. [86], indirectly confirms that the present Fermi-LAT data do not place additional strong constraints on the i2HDM parameter space. The authors of that work looked at the so-called gamma-ray Galactic center excess [87] and asked if it can be explained via the DM annihilation in i2HDM. They indeed found a few possible regions, and estimate that one would need 15 years of Fermi-LAT data to conclusively test it. In our work, we stay conservative and do not interpret such signals as the DM evidence. We can only state that the regions selected in Ref. [86] as promising are, at best, not excluded by Fermi-LAT data. Since the other regions were not favored by the Galactic center excess in the Fermi-LAT data, their expected contributions to the ID signals are weaker. Finally, we stress that incorporating ID limits into our picture would bring novel uncertainties of purely astrophysical origin such as the poorly known DM distribution profile. Thus, they cannot easily be translated into a new constraint on the i2HDM parameter space.

III. NUMERICAL SCAN OF THE PARAMETER SPACE

A. Results of the general scan

To have a complete picture of the properties of i2HDM in the whole parameter space, we have performed

a five-dimensional random scan of the model parameter space with about 10^8 points, evaluating all relevant observables and limits mentioned above. The range for the model parameters of the scan was chosen according to Eq. (18).

When performing the scan, we took into account the constraints mentioned above in the following succession. First, we applied only theoretical constraints from vacuum stability, perturbativity, and unitarity; second, we applied the collider constraints (LEP, EWPT, LHC Higgs data); last, we placed the upper bound on the DM relic density at $\Omega_{\text{DM}} h^2 \leq 0.1184 + 2 \times 0.0012$ given by the PLANCK result plus 2 standard deviations, and took into account the negative results of the DM DD searches at LUX.

The salient features of the results of this scan, with all three groups of constraints applied successively, are presented in Fig. 6 on the (M_{h_1}, λ_{345}) projection. The results are presented in the form of color maps, where the color encodes the value of the thermal relic density. The points with higher relic density are always on top of those with low density. To make the exposition as clear as possible, we decided to show here only this specific two-dimensional (2D) projection. The reader can find more information and insights in Appendix, which contains more projections and a more detailed description of the effects of each set of constraints. Our scan highlights the following features:

- (i) The lower bound of λ_{345} corresponds to the theoretical lower limit in Eq. (18). The upper bound on λ_{345} depends on M_{h_1} and comes from the vacuum stability condition given in Eq. (17). Taking into account the collider constraints, and in particular the invisible Higgs decay and the $H\gamma\gamma$ coupling strength, restricts λ_{345} to $|\lambda_{345}| \leq 0.02$ at $M_{h_1} < M_H/2$.
- (ii) The LEP and LHC data also place constraints on the other inert scalars. Charged scalars lighter than 70 GeV as well as $M_{h_2} < M_Z/2$ are generically

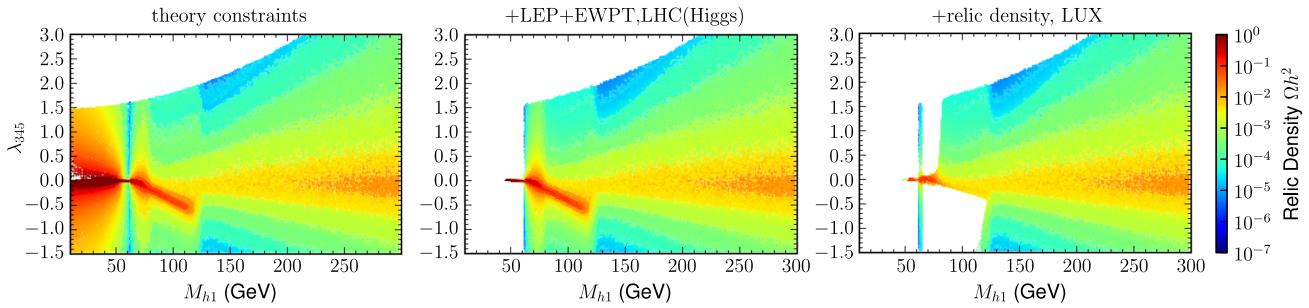


FIG. 6. Color maps of DM relic abundance projected on the plane (M_{h_1}, λ_{345}) . The three plots correspond to the surviving points after progressively imposing the three layers of constraints described in the text.

excluded. For M_{h_2} above this value and below approximately 100 GeV, the only surviving region is a narrow strip with $M_{h_2} - M_{h_1} < 8$ GeV. The effect from these constraints can be seen in Fig. 7 which shows the points surviving all constraints in a projection in the masses, and more details can be found in Appendix.

- (iii) The narrow strip at $M_{h_1} < M_H/2$ surviving after collider data, which is seen in Fig. 6(b), is further cut off once the relic density constraint, in addition, is taken into account. Indeed, for such a small M_{h_1} and λ_{345} (and not too small M_{h_2} to prevent $Z \rightarrow h_1 h_2$ decays), there remains no mechanism for sufficiently active removal of DM in the early universe. The resulting DM relic density turns out too high and is ruled out. We already saw this feature in Fig. 4(b). Values of $M_{h_1} > 45$ GeV are still allowed but they require a close M_{h_2} for an efficient coannihilation in the early universe. This region is well visible as a protrusion in the (M_{h_1}, M_{h_2}) in Fig. 7.
- (iv) The masses $M_{h_1} > M_H/2$ are not constrained by the relic density, but the DM DD results from LUX cut off a part of the parameter space. This is visible in the last plot in Fig. 6, for $M_{h_1} \lesssim M_H$ and with large and intermediate $|\lambda_{345}|$. In this region, the sizable $|\lambda_{345}|$ simultaneously keeps the relic density below the Planck upper bound and allows the scattering cross section to be enhanced due to the Higgs boson exchange. The interplay of *moderately low* relic

density and a sizable cross section leads to a DD signal which could have been seen by LUX. For larger DM masses, the direct annihilation into WW , ZZ , HH pairs opens up, and the relic density drops further, making LUX insensitive to this region.

- (v) Finally, we remark that above 200 GeV, EWPT forces M_{h_2} and M_{h^+} to stay rather close to each other, see again Appendix for more details.

In summary, after all constraints mentioned here and exposed in more detail in Appendix, we found that the parameter space with

$$M_{h_1}, M_{h_2} < 45 \text{ GeV} \quad \text{or} \quad M_{h^+} < 70 \text{ GeV} \quad (31)$$

is completely excluded. Our results agree with the conclusions of previous studies on the i2HDM (see, e.g., [29,60]). In particular, the authors of [29] have also stated the $M_{h_1}, M_{h_2} < 45$ GeV limit. However, we would like to stress that the general exclusion for M_{h_1}, M_{h_2} and for M_{h^+} given by Eq. (31) is established here for the first time, to the best of our knowledge. In [29], for example, the authors demonstrate [see Fig. 6 and Eq. (18) in [29]] that M_{h^+} above M_H is excluded from a specific scan. Here we find that M_{h^+} as light as 70 GeV is allowed by all present constraints, while M_{h_1} and M_{h_2} are generically allowed to be as light as 45 GeV. One should note that specific regions of the parameter space can be excluded using dilepton and missing transverse momentum signatures: for example, in a recent study [73] the authors showed that values of the

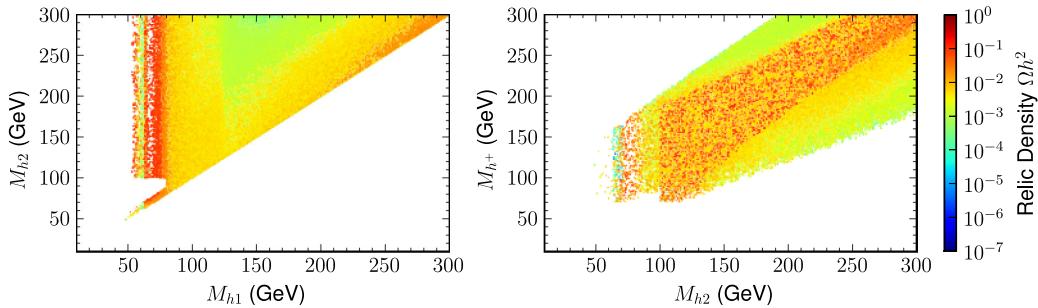


FIG. 7. Color maps of DM relic abundance projected on the planes (M_{h_1}, M_{h_2}) and (M_{h_2}, M_{h^+}) , with all the constraints imposed.

masses below $M_{h_1} \lesssim 50$ GeV and $M_{h_2} \lesssim 140$ GeV can be excluded using this signature, provided that the mass gap between M_{h_2} and M_{h_1} is large enough. However, we find that this parameter space region is already excluded by the upper cut on the relic density, as one can see from Fig. 7: for $M_{h_2} > 100$ GeV, the entire region $M_{h_1} \lesssim 50$ GeV is excluded by the relic density cut combined with previous constraints including LEP II limits.

B. Fitting the relic density

In our analysis, we generically allow the DM relic density to be equal or below the PLANCK constraints, Eq. (30). This is the concept of our approach: we assume that in the case of underabundance there should be either additional sources of DM or mechanisms other than thermal freeze-out that compensate for the DM deficit, such as DM freeze-in scenarios [88]. Keeping this in mind, we exclude in our analysis only those regions of the parameter space where the relic density exceeds the PLANCK constraint.

However, it is also instructive to explore the parameter space where both the upper and the lower PLANCK limits are satisfied. This parameter space region is presented in Fig. 8, for a wider scan $10 \text{ GeV} < M_{h_1}, M_{h_2}, M_{h^+} < 1000$ GeV and, separately, for the “zoomed” region $10 \text{ GeV} < M_{h_1}, M_{h_2}, M_{h^+} < 200$ GeV. Here, we show the two most revealing 2D projections: (M_{h_1}, λ_{345}) and (M_{h_1}, M_{h_2}) . Additional plots can be found in Appendix.

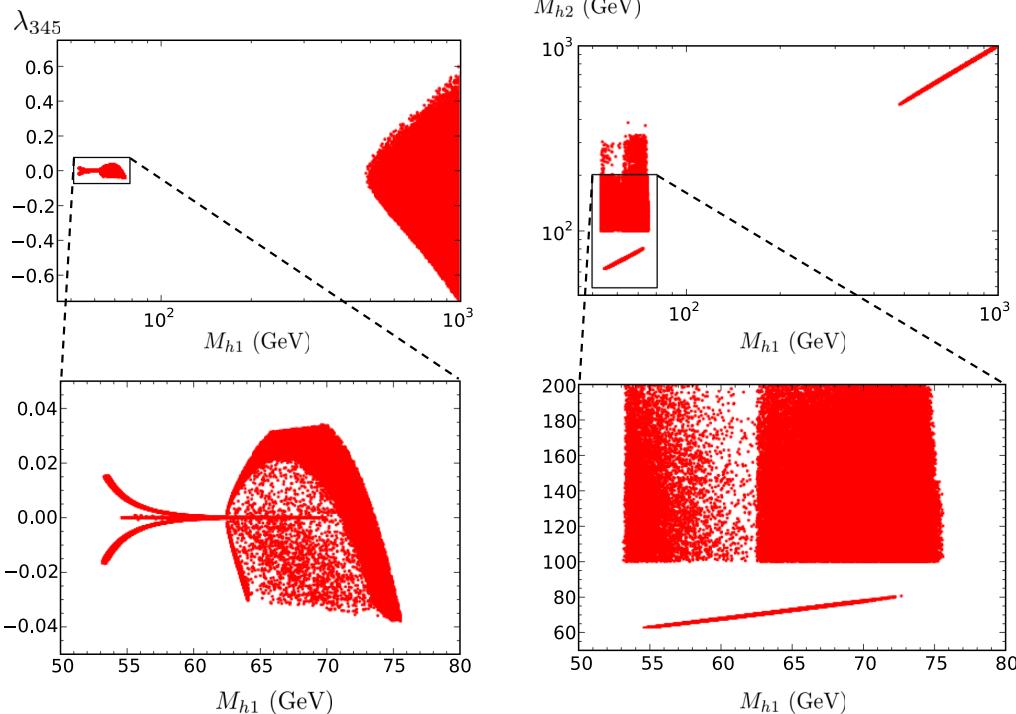


FIG. 8. Projection on two planes of the scan points passing all constraints, and fitting the PLANCK relic abundance within two sigmas. We show both a wide scan with masses between 10 and 1000 GeV, and a zoom on the low mass region.

Many interesting features of the i2HDM parameter space arise once the “correct” amount of DM relic density is required. One observes two very distinct M_{h_1} regions: a low mass region for $53 \text{ GeV} \lesssim M_{h_1} \lesssim 76 \text{ GeV}$, shown also in the zoomed panels, and a high mass region for $M_{h_1} \gtrsim 490 \text{ GeV}$. Below, we discuss them separately.

1. The low mass region

In the low mass region we clearly distinguish three regimes with specific physical properties:

- (a) A thin horizontal line with very small values of λ_{345} can be seen, corresponding to $h_1 h_2$ coannihilation: this region is novel, and it has been missed in previous studies. It can also be seen in the (M_{h_1}, M_{h_2}) plots as the thin diagonal strip at low M_{h_2} starting from 54 GeV and extending beyond $M_H/2$ up to about 73 GeV.

The width of this strip is defined by the maximum allowed value of $\Delta M = M_{h_2} - M_{h_1} = 8 \text{ GeV}$, above which the parameter space is excluded by LEP dilepton searches until $M_{h_2} > 100$ GeV [see Eq. (23)]. In this allowed region DM relic density is never above the PLANCK limit given by Eq. (30). The maximum value of Ωh_{DM}^2 reaches the value of about 0.11 for $M_{h_2} - M_{h_1} \simeq 8 \text{ GeV}$ and $\lambda_{345} \simeq 0$, when the only $h_1 - h_2$ coannihilation takes place. For $\Delta M < 8 \text{ GeV}$ and $M_{h_1} < 54 \text{ GeV}$, the Ωh^2 is

below the $0.118 - 2 \times 0.012$ limit which we use in our study because $h_1 - h_2$ coannihilation via Z -boson increases with the decrease of h_1, h_2 masses. On the other hand, the upper edge at 73 GeV is defined by the rapid increase of the $h_1 h_1 \rightarrow WW^*$ contribution, which does not require coannihilation above this mass. The typical $M_{h_2} - M_{h_1}$ mass split in the coannihilation region is 7–8 GeV, as required to make the relic density consistent with the PLANCK limit.

- (b) For $M_{h_1} < M_H/2$, two symmetric wings can also be seen, extending for positive and negative λ_{345} , clearly visible in the zoomed (M_{h_1}, λ_{345}) panel. They correspond to DM annihilation via the Higgs boson exchange.
- (c) In the region $M_H/2 < M_{h_1} \lesssim 76$ GeV, large absolute values of λ_{345} are allowed by the LHC Higgs data; however, LUX data require $|\lambda_{345}|$ to be below about 0.04. In this region, we remark on the asymmetric pattern in the (λ_{345}, M_{h_1}) plane for positive and negative values of λ_{345} , which is related, respectively, to the positive and negative interference of $h_1 h_1 \rightarrow VV$ ($V = Z, W$) annihilation diagrams via Higgs boson exchange and diagrams with quartic $h_1 h_1 VV$ interactions.

2. The high mass region and the LHC sensitivity

The relic density can also be “just right” at large masses $M_{h_1} \gtrsim 490$ GeV, as shown in Fig. 8. The most salient feature of this high-mass region is the high degree of degeneracy among the three inert Higgs boson masses. This is clearly seen in the upper right corner of the (M_{h_1}, M_{h_2}) plane, as well as in Fig. 28 in Appendix. Numerically we find that the maximal mass difference among h_1, h_2 , and h^+ , which we call ΔM^{\max} , does not exceed a few GeV.

Remarkably, the mass split is required to be *large enough*, so that the relic density can reach the *lower value* of the PLANCK limit: the increase of the mass split is, in fact, correlated with the increase of the quartic coupling $h_1 h_1 V_L V_L$ of the DM to longitudinal Z and W bosons, which enhances the $h_1 h_1$ annihilation cross section, thus bringing the DM relic density down to within the experimental limits. Because of the connection between the mass split and the $h_1 h_1 V_L V_L$ couplings [see Eq. (8)], this effect is actually stronger than the effect of the h_1, h_2 , and h^+ coannihilation, which becomes subdominant in this high-mass region. One should also mention that ΔM^{\max} of the order of a few GeV is *generically* not small enough to lead to long-lived h_2 or h^+ at detector level. However, in the small mass tip, in the interval $550 \text{ GeV} \gtrsim M_{h_1} \gtrsim 490 \text{ GeV}$, ΔM^{\max} can take values about 0.2 GeV. This specific range of the mass split simultaneously provides an $\Omega_{\text{DM}} h^2$ consistent with the PLANCK constraint and a lifetime for h^+ large enough to travel about 10 cm or more in the detector, thus providing disappearing charged track

signatures which have been recently explored by CMS [89] Collaboration.

This small ΔM region deserves a special discussion which we give below. For the mass splitting $\Delta M \simeq 0.2 \text{ GeV} = 200 \text{ MeV}$ the h^+ will dominantly decay into $\pi^+ h_1$ as soon as $\Delta M = M_{h^+} - M_{h_1} > m_{\pi^+} \simeq 140 \text{ MeV}$. This happens because when the ΔM is of the order of pion mass, the naive perturbative calculation of $h^+ \rightarrow h_1 W^{+*} \rightarrow h_1 u \bar{d}$ underestimates the width by about 1 order of the magnitude and therefore overestimates the lifetime of h^+ by the same amount. For proper evaluation of the lifetime which is crucial for the collider phenomenology we have used the nonperturbative $W - \pi$ mixing,

$$\mathcal{L}_{W\pi} = \frac{gf_\pi}{2\sqrt{2}} W_\mu^+ \partial^\mu \pi^- + \text{H.c.}, \quad (32)$$

leading to the effective Lagrangian for $h^+ \rightarrow h_1 \pi^+$ interactions, which in momentum space reads as

$$\mathcal{L}_{h^+ h_1 \pi^+} = \frac{ig^2 f_\pi}{4\sqrt{2} M_W^2} (p_{h^+} - p_{h_1}) \cdot p_\pi, \quad (33)$$

where $f_\pi = 130 \text{ MeV}$ is the pion decay constant. This effective Lagrangian is represented by the diagram shown in Fig. 9 with the virtual W boson line contracted to pointlike interaction.

From the Lagrangian above one can find the following formula for the $h^+ \rightarrow h_1 \pi^+$ width in the $\Delta M/M \ll 1$ limit:

$$\Gamma = \frac{g^4 f_\pi^2}{64\pi M_W^4} \Delta M^2 \sqrt{\Delta M^2 - m_{\pi^+}^2}, \quad (34)$$

where g is the weak coupling constant. In Fig. 10 we present the decay width of h^+ (left) as well as lifetime and decay length (right) which are functions of ΔM only. One can see that, for ΔM in the range 140–200 MeV, h^+ will provide a disappearing charged track signature with the length of 100–10 cm, respectively. For ΔM below the pion mass the width is defined by the $h^+ \rightarrow W^{+*} h_1 \rightarrow e^+ \nu_e h_1$ process and drops to the level of 10^{-18} GeV or below, meaning that h^+ becomes collider stable and goes through

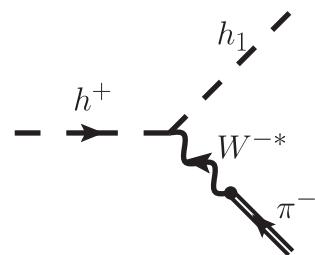
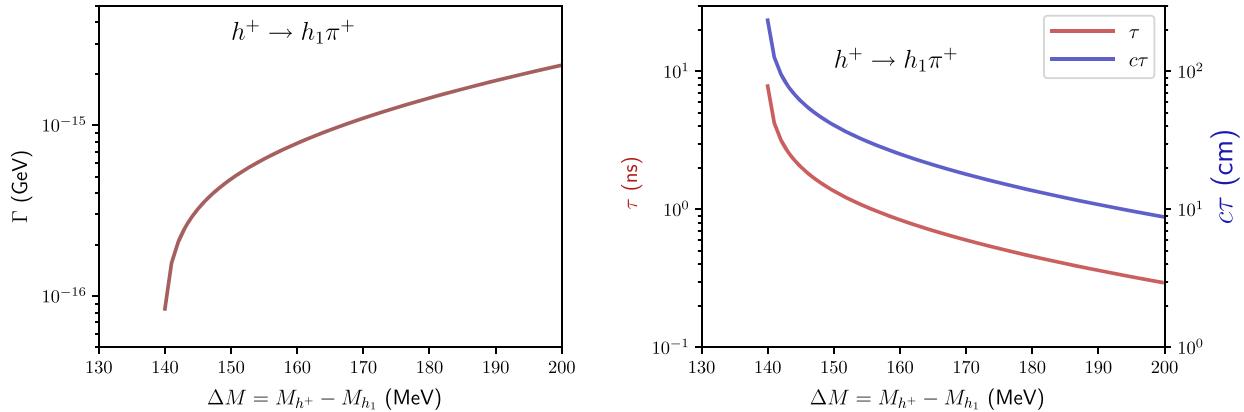


FIG. 9. Feynman diagram representing effective $h^+ \rightarrow h_1 \pi^+$ via $W - \pi$ mixing.

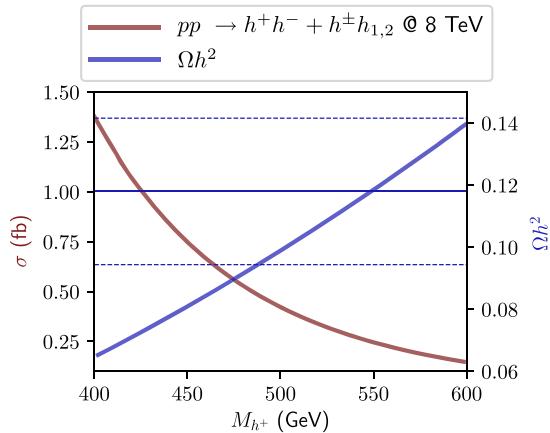
FIG. 10. The decay width of h^+ (left) as well as its lifetime together with the decay length (right).

the whole detector. For such a small mass split, the width of h^+ is proportional to $\Delta M^5/M_W^4$.

The next step is to check which M_{h^+} mass range in the $\Delta M/M \ll 1$ and λ_{345} parameter space is consistent with the relic density constraints given by Eq. (30). Let us stress that in the $\Delta M/M \ll 1$ and $\lambda_{345} \approx 0$ regime the relic density is maximized for $M_{h^+} \approx 500$ GeV or above (this happens because the boost of DM annihilation into the gauge bosons dominates the reduction of co-annihilation effects with $\Delta M/M$ increase). In Fig. 11 we present the Ωh^2 value for $\Delta M/M \ll 1$ and $\lambda_{345} \approx 0$ parameter space which grows with M_{h^+} and becomes consistent with upper and lower limits for relic density constraints in the range of $490 < M_{h^+} < 600$ GeV masses.

At the same time the figure presents the $pp \rightarrow h^+h^- + h^\pm h_{1,2}$ production rate which we have evaluated for the LHC@8 TeV with NNPDF23LO (as_0119_qed) parton density function (PDF) set [90] and QCD scale chosen to be equal to the averaged transverse mass of the final state particles.

After applying efficiency for the disappearing charged track signatures provided by CMS [89] as a function of

FIG. 11. The Ωh^2 value for $\Delta M/M \ll 1$ and λ_{345} parameter space and the $pp \rightarrow h^+h^- + h^\pm h_{1,2}$ production rate evaluated for the LHC@8 TeV.

charged track transverse momentum as well as efficiency for distance traveled by the charge particle, we have estimated that CMS@8 TeV with 19.5 fb^{-1} data excludes h^+ in the 490–550 GeV mass range for $\Delta M = 140$ –200 MeV. For example, for $M_{h^+} = 500$ GeV the sum of the cross section of $pp \rightarrow h^+h^-$ and $pp \rightarrow h^\pm h_{1,2}$ is about 0.4 fb, and the product of this cross section, the luminosity, and the above efficiencies gives about 2.5 events which are above the 2 event exclusion level.

One should also note that with increasing DM mass, the required split among h_1 , h_2 , and h^+ increases. At about 20 TeV for M_{h_1} , the DM relic density constraint together with the requirement of unitarity and perturbativity which are saturated by $\Delta M^{\max} \approx 10$ GeV close the i2HDM parameter space.

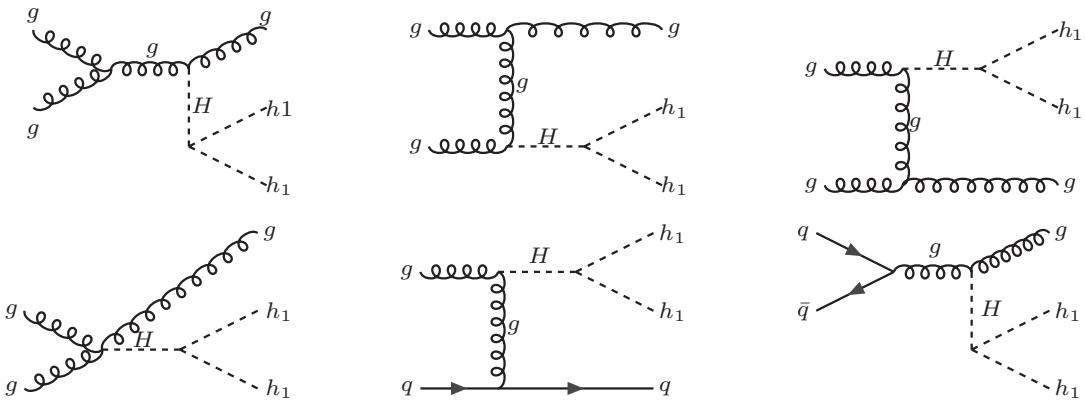
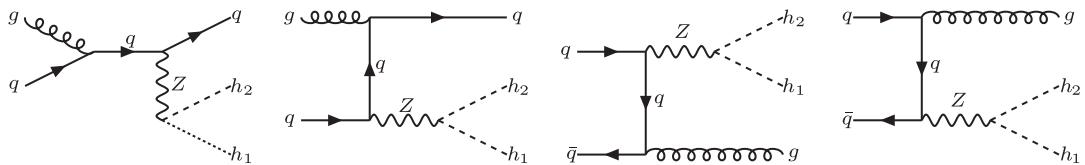
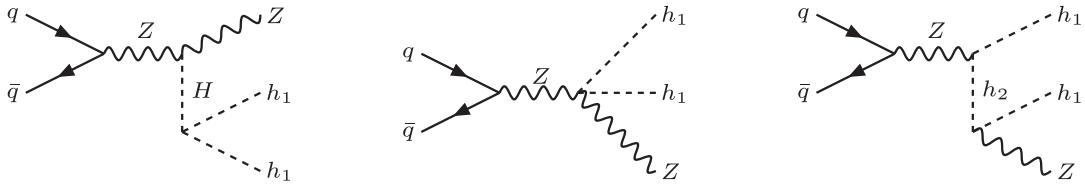
IV. PROBING DARK MATTER SIGNALS FROM I2HDM AT THE LHC

The i2HDM exhibits various signatures that are potentially accessible at the LHC. They can be generically described as “mono-object production,” that is, production of several final states in association with large missing transverse momentum. In this section, we undertake a detailed exploration of such processes which goes beyond the previously published state-of-the-art. We will first list the relevant processes, and then produce a cumulative plot which helps us compare their rates. With this knowledge, we will formulate convenient benchmark points which represent various qualitatively distinct regimes of i2HDM, and finally go into a more detailed calculation of monojet production.

A. Dark matter signatures: Diagrams and features

1. Monojet production

The monojet signature originates from the $pp \rightarrow h_1 h_j$ process, the Feynman diagrams for which are presented in Fig. 12. For this process, the relevant nontrivial parameter space is one dimensional: it is just the DM mass, M_{h_1} , since

FIG. 12. Feynman diagrams for the $pp \rightarrow h_1 h_1 j$ process contributing to a monojet signature.FIG. 13. Feynman diagrams for the $q\bar{q} \rightarrow h_1 h_2 g$ ($gq \rightarrow h_1 h_2 q$) process contributing to a monojet signature.FIG. 14. Feynman diagrams for the $q\bar{q} \rightarrow h_1 h_1 Z$ process contributing to a mono-Z signature.

the second parameter, λ_{345} , simply scales the production cross section which is proportional to $(\lambda_{345})^2$ for $M_{h_1} > M_H/2$. One should note that the mediator mass for this signature is the Higgs mass, $M_H = 125$ GeV, thus the EFT approach is not applicable for this process. Also, the recent limits by ATLAS [91] and CMS [92,93] Collaborations are not directly applicable for this process since they have been obtained for a different spin of the mediator and a different spin of DM.

There is one more process, namely $q\bar{q} \rightarrow h_1 h_2 g$ ($gq \rightarrow h_1 h_2 q$) (see diagrams in Fig. 13), that can contribute to a monojet signature in the special case of a small mass split between h_1 and h_2 . In this scenario h_2 decays to h_1 plus soft jets and/or leptons. The essential parameter space for this process is the two-dimensional (M_{h_1}, M_{h_2}) plane which fixes its cross section. This channel is particularly relevant in the $\Lambda_{345} \sim 0$ region at low mass that we discovered in this study.

2. Mono-Z production

Besides monojets, the i2HDM gives rise to a mono-Z signature, the diagrams for which are presented in Fig. 14.

The first diagram scales with λ_{345} while the other two are fixed by electroweak interactions.³ In general, nontrivial interference takes place between the three different topologies represented by each of three diagrams, so this process cannot be approximated by a simplified model. However, we found that when $|\lambda_{345}| \gtrsim 0.02$ with $M_{h_1} < M_H/2$ (below the Higgs boson threshold) or $|\lambda_{345}| \gtrsim 1$ with $M_{h_1} > M_H/2$ (above the Higgs boson threshold), the first diagram is dominant and defines the event kinematics. So for these values of λ_{345} and M_{h_1} , a simplified model with the Higgs boson as the mediator is sufficient to set the LHC limits.

One should also note that for values of $|\lambda_{345}|$ below 0.02 the contribution from diagrams scaling with $|\lambda_{345}|$ drops below 1%. In this case the Z boson will be the only mediator to probe the i2HDM model at the LHC, with the mono-Z process being the leading signature for this

³For the second diagram, the $ZZ h_1 h_1$ vertex for transverse Z bosons is fixed by the weak coupling, while for a longitudinal Z boson it scales with $\tilde{\lambda}_{345}$ in Eq. (8). When this coupling is small, the strength of the $ZZ h_1 h_1$ vertex therefore is fixed by the gauge interactions.

purpose (and not only as a probe complementary to the monojet signature). This signature will be especially pronounced if $M_{h_2} - M_{h_1} > M_Z$, so that the cross section of the mono- Z signature is essentially defined by the cross section of the $2 \rightarrow 2$ process, $pp \rightarrow h_1 h_2 \rightarrow h_1 h_1 Z$. For small mass split, as it happens in the $\lambda_{345} \sim 0$ region, the mono- Z will complement the signal in the monojet described above. The parameter space for this process is the two-dimensional (M_{h_1}, M_{h_2}) plane.

3. Mono-Higgs production

The i2HDM could also provide a mono-Higgs signature via $gg \rightarrow h_1 h_1 H$ and $q\bar{q} \rightarrow h_1 h_2 H$, whose diagrams are presented in Figs. 15 and 16, respectively. The only mediator for $gg \rightarrow h_1 h_1 H$ is the Higgs boson, and the respective cross section scales as $(\lambda_{345})^2$ for small values of

λ_{345} and $(\lambda_{345})^4$ for large values of λ_{345} because of the second diagram. On the other hand, the $q\bar{q} \rightarrow h_1 h_2 H$ process takes place via either a Z boson or an h_2 as a mediator: the first diagram does not scale with λ_{345} , while the last two do. Therefore for large λ_{345} , the $(\lambda_{345})^2$ scaling takes place for the $q\bar{q} \rightarrow h_1 h_2 H$ process. In fact, the contribution from the second and the third diagrams of $q\bar{q} \rightarrow h_1 h_2 H$ to the total cross section drops below 1% only for $\lambda_{345} < 0.002$, below which the process kinematics and the cross section are determined by the first diagram with two Z -boson propagators.

4. Vector boson fusion

Finally, one should mention the production of DM via vector boson fusion, $pp \rightarrow h_1 h_1 jj$, the diagrams for which are presented in Fig. 17. Similar to the mono- Z process, there

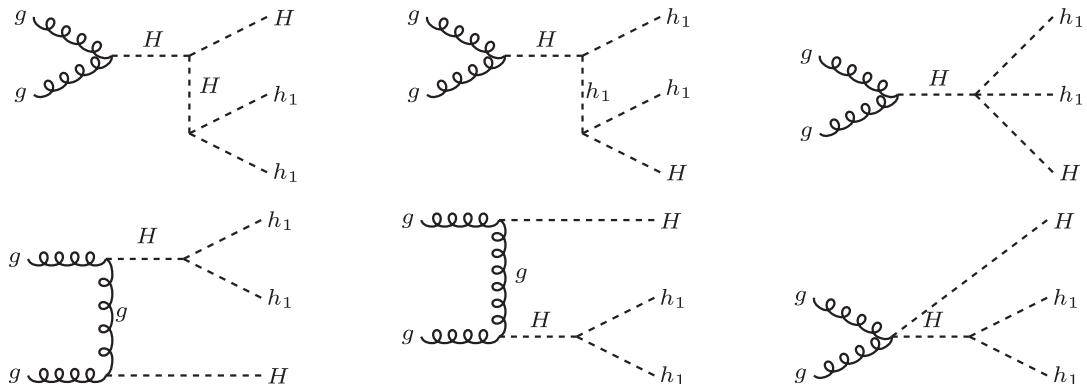


FIG. 15. Feynman diagrams for the $gg \rightarrow h_1 h_1 H$ process contributing to a mono-Higgs signature.

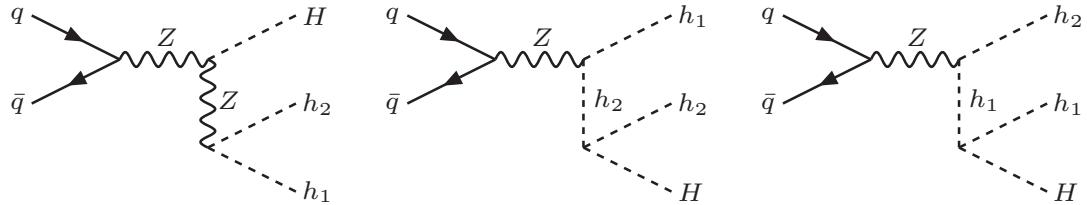


FIG. 16. Feynman diagrams for the $q\bar{q} \rightarrow h_1 h_2 H$ process contributing to a mono-Higgs signature.

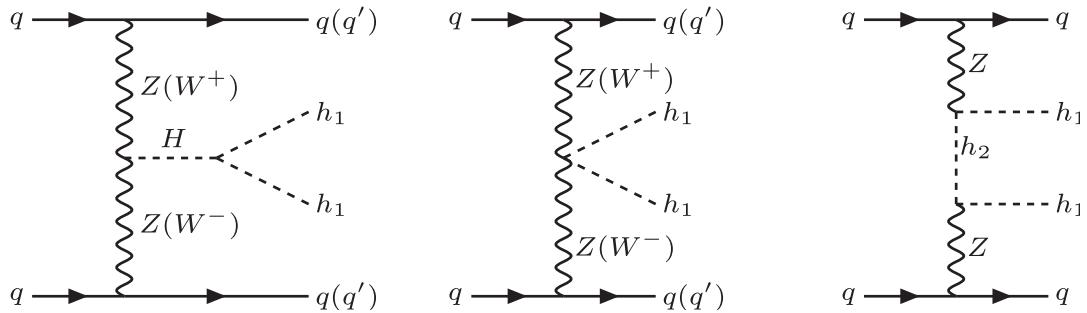


FIG. 17. Diagrams for $qq \rightarrow q^{(\prime)} q^{(\prime\prime)} h_1 h_1$ DM production in the vector boson fusion process.

are three diagrams with different topologies and mediators which contribute to this process; thus, it cannot be described by just one simplified model. The first two diagrams scale with λ_{345} . To be accurate, the $Z_L Z_L h_1 h_1$ coupling in the second diagram is proportional to $\tilde{\lambda}_{345}$ [see Eq. (8)], which is approximately equal to λ_{345} for small $M_{h_2} - M_{h_1}$. They give the dominant contribution to the $pp \rightarrow h_1 h_1 jj$ process for $\lambda_{345} \simeq 1$, but their contribution is negligible with very small λ_{345} . On the other hand, for large $h_1 - h_2$ and $h_1 - h^+$ splittings, they get stronger even with small λ_{345} and enhance the vector boson fusion (VBF) process. This opens a new perspective for the exploration of the i2HDM model which we plan to perform in the near future.

B. Mono-object production: Rates and comparison

1. Implementation and cuts

When calculating the cross sections of mono-object production at the LHC, we used the following setup for the process evaluation:

- (i) the QCD renormalization and factorization scales Q were chosen to be equal to the transverse momentum of the pair of DM particles, i.e. missing transverse momentum, E_T^{miss} for all processes;
- (ii) the PDF and the strong coupling constant are as provided by the NNPDF23LO (as_0119_qed) PDF set [90];
- (iii) for all processes a cut on the minimal value of missing transverse momentum of 100 GeV was applied;
- (iv) the VBF cross section has been evaluated with the following additional cuts:

$$P_T^j > 30 \text{ GeV}, \quad \Delta\eta_{jj} > 4, \quad E_j > 400 \text{ GeV}. \quad (35)$$

Below we present plots and numbers for cross sections (in the text and table) with three significant digits corresponding to the accuracy of the MC phase space integration. But we would like to note that when Q is varied in the range $E_T^{\text{miss}}/2$ to $2 \times E_T^{\text{miss}}$, the QCD scale uncertainty is around 20%–30% for the tree-level cross sections presented, dominating over PDF uncertainties which are below 10%. The presentation and detailed discussion of these uncertainties is out of the scope of this paper.

2. Production rates

In Fig. 18 we present a summary of the cross sections versus dark matter mass M_{h_1} for all the processes mentioned above, which contribute to the monojet, mono-Z, mono-Higgs, and VBF signatures for the LHC at 8 and 13 TeV. In the plot we chose some particular values of the mass split $M_{h_2} - M_{h_1}$ and of the coupling λ_{345} ; however, the cross sections in other cases can easily be inferred by referring to the scaling properties mentioned in Sec. IV A. It

is evident from the plot that the dominant cross sections always tend to be monojet processes (in grey), and the mono-Z signature coming from the on-shell decay of h_2 .

It is also worth focusing on the new $\lambda_{345} \sim 0$ region at small masses: the relevant cross sections are related to the mono-jet process $pp \rightarrow jh_1 h_2$ at a small mass split (dashed grey curves in Fig. 18) and mono-Higgs production (dotted red curves). In the low M_{h_1} region, below 75 GeV, the former channel provides cross sections of several tens of fb at 13 TeV, which may be probed in monojet searches. This is a very important point, as the $\lambda_{345} \sim 0$ region is very difficult to probe in DD experiments due to the suppressed coupling to the Higgs.

The plot also shows that the mono-Higgs channels does not yield detectable rates.

The process $pp \rightarrow jh_1 h_2$ is also relevant for larger mass splits: while the cross section drops, for splits of few tens of GeV, the h_2 decays can provide visible leptons and thus produce Supersymmetry-like signatures. Finally, when the mass split grows above the Z mass, on-shell decays of h_2 allow for mono-Z signatures, as shown by the blue-dashed line.

C. Benchmark points

The experience we have gained so far, in both relic density and mono-object cross section calculations, allows us to discern several qualitatively distinct regimes of i2HDM and find their representative benchmark points. In Table I we present six benchmarks (BM) from the i2HDM parameter space together with corresponding observables: DM relic density ($\Omega_{\text{DM}} h^2$), spin-independent DM scattering rate on the proton (σ_{SI}^p) accompanied with its ratio to the experimental limit from LUX following rescaling with the relic density: $R_{\text{SI}}^{\text{LUX}} = (\sigma_{\text{SI}}^p / \sigma_{\text{SI}}^{\text{LUX}}) \cdot (\Omega_{\text{DM}} / \Omega_{\text{DM}}^{\text{Planck}})$. We also present the LHC cross sections for the monojet, mono-Z, and mono-H signatures discussed above with a $E_T^{\text{miss}} > 100$ GeV cut applied. All of these benchmarks are allowed by the present experimental data. In Table I we do not give specific benchmarks for the long-lived h^+ scenario discussed above since in Fig. 11 we have effectively provided the whole parameter space for this scenario ($\Delta M = 140$ –200 MeV, $\lambda_{345} = 0$, $M_{h^+} = 490$ –600 GeV).

The first two benchmarks have small and medium values of λ_{345} and correspond to the scenario when M_{h_1} is below $M_H/2$, and the mass split $\Delta M = M_{h_2} - M_{h_1}$ is small. BM1 has a very small value of $\lambda_{345} = 10^{-4}$ and is therefore characterized by having a small $\text{Br}(H \rightarrow h_1 h_1)$ value and a very low DM direct detection rate, σ_{SI}^p , while the relic density is consistent with the Planck limit due to coannihilation. The $h_1 h_1 j$ monojet signature rate at the LHC scales with $(\lambda_{345})^2$ and is therefore very low, while the λ_{345} -independent $h_1 h_2 j$ signature cross section is about 36.7 fb (LHC@8 TeV) and 92.4 fb (LHC@13 TeV).

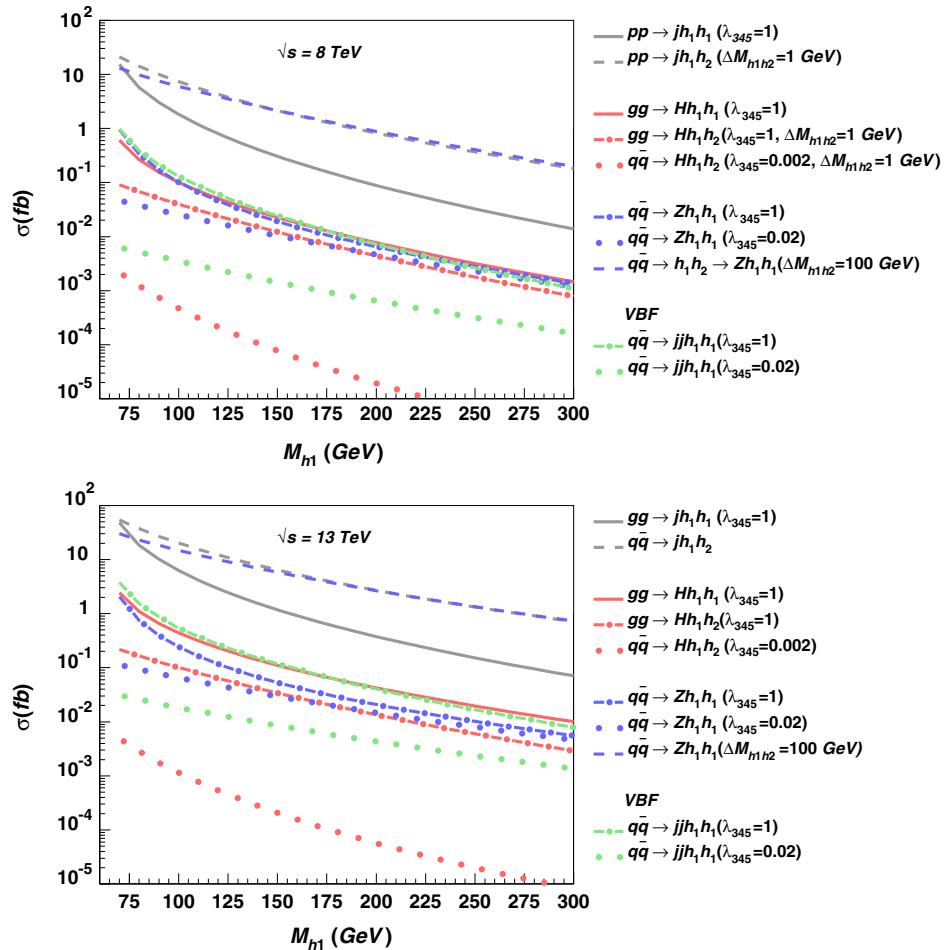


FIG. 18. Cross sections versus dark matter mass, M_{h_1} , for processes contributing to monojet, mono-Z, mono-Higgs, and VBF signatures for the LHC@8 TeV and LHC@13 TeV.

BM2 differs from BM1 only by the value of $\lambda_{345}=0.027$, which is chosen as the maximum value allowed by the Higgs invisible branching ratio. For this λ_{345} , the $h_1 h_1 j$ monojet production rates are 288 fb (LHC@8 TeV) and 878 fb (LHC@13 TeV).

BM3 and BM4 correspond to the scenarios where $\Delta M > M_Z$ with M_{h_1} below and above $M_H/2$, respectively, with the other parameters chosen such that the relic density is consistent with Planck data. In comparison to BM3, BM4 has a very low $h_1 h_1 j$ production cross section because the SM Higgs boson is produced off mass shell. At the same time the $h_1 h_1 Z$ cross section is of the same order for both benchmarks: 6.48 fb and 3.90 fb for LHC@8 TeV, and 17.8 fb and 11.1 fb for LHC@13 TeV, respectively.

Finally, BM5 and BM6 represent the cases with a small (5 GeV) mass split and $M_{h_1} = 100$ GeV. The only difference in the input parameters is the value of λ_{345} : large $\lambda_{345} = 1$ for BM5 and small $\lambda_{345} = 0.002$ for BM6. For both benchmarks, the DM relic density is well below the PLANCK limit, and therefore an additional source of dark matter is required. Even for BM6 which has a small value of λ_{345} , the DM relic density is of the order of 10^{-3} because

the DM effectively annihilate via $h_1 h_1 \rightarrow VV$ and $h_1 h_1 \rightarrow HH$ channels. They are open for this value of DM mass and are defined essentially by the weak coupling, the contribution from $h_1 h_1 \rightarrow V_L V_L$ being small because of the small $h_1 - h_2$ mass split and the contribution from coannihilation being subdominant for this value of mass split. For both of these benchmarks, the $h_1 h_2 j$ channel which has cross sections of 6.93 fb (LHC@8 TeV) and 19.1 fb (LHC@13 TeV) looks the most promising.

From Table I one can see that different mono-object signatures are very complementary for these suggested benchmarks, especially the $h_1 h_1 j$ and $h_1 h_2 j$ processes which are the main focus of the collider study presented below.

D. Limits from LHC@8 TeV and projections for LHC@13 TeV

In the previous subsections, we calculated the mono-object production cross sections at the LHC as a function of DM mass M_{h_1} for a selection of parameters. In this subsection, we invert the problem: we examine the limits on the parameter space which follow from the current

TABLE I. Benchmarks (BM) from the i2HDM parameter space together with corresponding observables: DM relic density ($\Omega_{\text{DM}} h^2$), spin-independent DM scattering rate on the proton (σ_{SI}^p) accompanied with its ratio to the experimental limit from LUX following rescaling with the relic density: $R_{\text{SI}}^{\text{LUX}} = (\sigma_{\text{SI}}^p / \sigma_{\text{SI}}^{\text{LUX}}) \cdot (\Omega_{\text{DM}} / \Omega_{\text{DM}}^{\text{Planck}})$, and the LHC cross sections for monojet, mono-Z, and mono- H signatures with a $E_T^{\text{miss}} > 100$ GeV cut applied.

BM	1	2	3	4	5	6
M_{h_1} [GeV]	55	55	50	70	100	100
M_{h_2} [GeV]	63	63	150	170	105	105
M_{h_+} [GeV]	150	150	200	200	200	200
λ_{345}	1.0×10^{-4}	0.027	0.015	0.02	1.0	0.002
λ_2	1.0	1.0	1.0	1.0	1.0	1.0
$\Omega_{\text{DM}} h^2$	9.2×10^{-2}	1.5×10^{-2}	9.9×10^{-2}	9.7×10^{-2}	1.3×10^{-4}	1.7×10^{-3}
σ_{SI}^p [pb]	1.7×10^{-14}	1.3×10^{-9}	4.8×10^{-10}	4.3×10^{-10}	5.3×10^{-7}	2.1×10^{-12}
$R_{\text{SI}}^{\text{LUX}}$	1.6×10^{-5}	0.19	0.51	0.37	0.48	2.5×10^{-5}
$\text{Br}(H \rightarrow h_1 h_1)$	5.2×10^{-6}	0.27	0.13	0.0	0.0	0.0
$\sigma_{\text{LHC}8}$ [fb]						
$h_1 h_1 j$	5.44×10^{-3}	288	134	6.05×10^{-3}	1.80	7.23×10^{-6}
$h_1 h_2 j$	36.7	36.7	6.48	3.90	6.93	6.93
$h_1 h_1 Z$	6.14×10^{-2}	21.4	30.7	12.2	0.101	2.52×10^{-2}
$h_1 h_1 H$	1.70×10^{-4}	8.98	4.21	2.19×10^{-4}	0.100	3.33×10^{-7}
$h_1 h_2 H$	5.35×10^{-3}	6.31×10^{-3}	9.80×10^{-3}	7.54×10^{-3}	3.86×10^{-2}	5.51×10^{-4}
$h_1 h_1 jj$	2.39×10^{-2}	17.2	8.11	4.44×10^{-2}	0.212	1.62×10^{-2}
$\sigma_{\text{LHC}13}$ [fb]						
$h_1 h_1 j$	1.67×10^{-2}	878	411	1.93×10^{-2}	6.25	2.50×10^{-5}
$h_1 h_2 j$	92.4	92.4	17.8	11.1	19.1	19.1
$h_1 h_1 Z$	0.153	46.2	66.9	28.3	0.241	6.47×10^{-2}
$h_1 h_1 H$	6.69×10^{-4}	35.3	16.5	9.08×10^{-4}	0.441	1.51×10^{-6}
$h_1 h_2 H$	1.18×10^{-2}	1.40×10^{-2}	2.47×10^{-2}	1.99×10^{-2}	9.82×10^{-2}	1.34×10^{-3}
$h_1 h_1 jj$	0.101	62.7	29.6	0.189	0.904	7.49×10^{-2}

8 TeV and projected 13 TeV LHC data. We concentrate on limits from monojet processes, as these are the mono-object signatures with the highest cross sections, as shown in Fig. 18. For monojet signals we consider two different processes: $pp \rightarrow h_1 h_1 j$ and $pp \rightarrow h_1 h_2 j$. The cross section of the former depends on the two parameters only, the dark matter mass M_{h_1} and λ_{345} . For the latter, all the vertices depend only on the gauge constants. The only two parameters that shape its cross section are the inert scalar masses M_{h_1} and M_{h_2} , or equivalently M_{h_1} and $\Delta M = M_{h_2} - M_{h_1}$.

1. Implementation and the LHC data used

In order to calculate the limits from the LHC at 8 TeV, we used the CHECKMATE [94–102] framework, which allows an easy application of the implemented search analyses. This tool takes a given sample of Monte Carlo events in the HEP or HepMC format after parton showering and hadronization, for which we used PYTHIA-6 [103], and performs a detector simulation on these events using DELPHES-3 [95]. Subsequently CHECKMATE can apply any of its preprogrammed and validated analyses to the generated signal events and uses the resulting efficiencies along with published information, such as the 95% confidence level

limit on signal count, to produce results from which we can find the cross section limit placed on our model by each analysis.

The signature of both processes that we consider, $pp \rightarrow h_1 h_1 j$ and $pp \rightarrow h_1 h_2 j$, is a high- p_T jet and a large missing transverse momentum, E_T^{miss} . In the case of $pp \rightarrow h_1 h_2 j$, the h_2 will decay via a h_1 and a $Z^{(*)}$ boson. When ΔM is very small, the decay products of the Z will generally be too soft to be reconstructed in the detector. Therefore in this case $pp \rightarrow h_1 h_2 j$ will give a monojet + E_T^{miss} signature. Using CHECKMATE and HepMC files created with the i2HDM model implemented in CALCHEP, we calculated the limits given by all of the monojet + E_T^{miss} analyses currently implemented in CHECKMATE [93,104–106] (3 ATLAS and 1 CMS analyses).

For both processes considered, we found that the lowest cross section limits for each benchmark point considered were provided by one of the ATLAS monojet + E_T^{miss} analyses [106]. These are the limits presented in this section. This analysis requires a leading jet with a $p_T > 120$ GeV and $|\eta| < 2.0$, and the leading jet $p_T/E_T^{\text{miss}} > 0.5$. Furthermore, to reduce the multijet background where the large E_T^{miss} originates mainly from the jet energy mismeasurement, we place a requirement

on the azimuthal separation $\Delta\phi(\text{jet}, p_T^{\text{miss}}) > 1.0$ between the direction of the missing transverse momentum and that of each jet. A number of different signal regions are considered with increasing E_T^{miss} thresholds from 150 to 700 GeV. Full details are available in the ATLAS paper [106].

In order to project these limits for increased luminosity and to 13 TeV, we use Monte Carlo events to estimate the efficiencies for the signal and background at 13 TeV, which is a function of M_{h_1} and depends on the best analysis signal region for each mass. We make the assumption that the analysis cuts for 13 TeV data will be the same as for 8 TeV data, which does not take into account improvements in the signal to background ratio which would likely occur with new analysis cuts at 13 TeV. Therefore our projected limits will be slightly conservative.

2. Limits from $pp \rightarrow h_1 h_1 j$

The results for the process $pp \rightarrow h_1 h_1 j$ are shown for 8 TeV in Fig. 19(a) with projections to 13 TeV and higher luminosities in Fig. 19(b). The limits are denoted by the solid lines, while the cross sections for the i2HDM for different values of λ_{345} are shown by the dashed lines. For $M_{h_1} < M_H/2$, the maximum allowed value of λ_{345} is given by the bound on the invisible Higgs branching ratio in Eq. (25) (this constraint has not been applied on the dashed blue $\lambda_{345} = 0.1$ curve), while when $M_{h_1} > M_H/2$ the maximum allowed value is calculated using the constraints of Eq. (17). The cross section with this maximum value of λ_{345} is denoted by the dashed green line. We see in Fig. 19(a), that the 8 TeV LHC monojet + E_T^{miss} searches do not constrain the i2HDM via the $pp \rightarrow h_1 h_1 j$ process. However, at 13 TeV, shown in Fig. 19(b), with around

100 fb^{-1} of data (purple solid curve), we would be able to set limits on λ_{345} for M_{h_1} up to 66 GeV, and for 3000 fb^{-1} (black solid curve) LHC data would set limits on λ_{345} for M_{h_1} up to 83 GeV. It should be remarked that the spike in cross section on the green dashed line at $M_{h_1} \sim M_H/2$ is due to the release of the ($H \rightarrow \text{invisible}$) bound on λ_{345} once the decay of the Higgs into DM is kinematically closed.

We should note that a similar projection of CMS monojet limits [93] at 14 TeV has been studied previously [60], where the projected limits were slightly stronger than in Fig. 19(b). Their projection was able to limit M_{h_1} for values of λ_{345} as small as $\lambda_{345} = 0.01$, while we require slightly larger values of λ_{345} in order to limit M_{h_1} . We would like to note that in our paper the limits are based on the fast detector simulations rather than parton level ones used in [60] done for 14 TeV. Taking this into account we consider our results as a more realistic projection of the future LHC data potential.

In Fig. 20 we provide the limit on λ_{345} versus M_{h_1} for different projected luminosities at the LHC@13 TeV. This limit is derived from the analysis presented in Fig. 19 and could be more practical for comparison with limits on λ_{345} from different experiments.

3. Limits from $pp \rightarrow h_1 h_2 j$

For $pp \rightarrow h_1 h_2 j$, the results are shown in Fig. 21(a) for 8 TeV and in Fig. 21(b) for 13 TeV. We consider two scenarios with a small ($\Delta M = 1$ GeV in blue curves) and large ($\Delta M = 100$ GeV in yellow curves) mass split. The projected cross section limits are again denoted by the solid lines. When $\Delta M = 1$ GeV, the current LHC Run I results are able to rule out $M_{h_1} < 35$ GeV. In this case, it should be

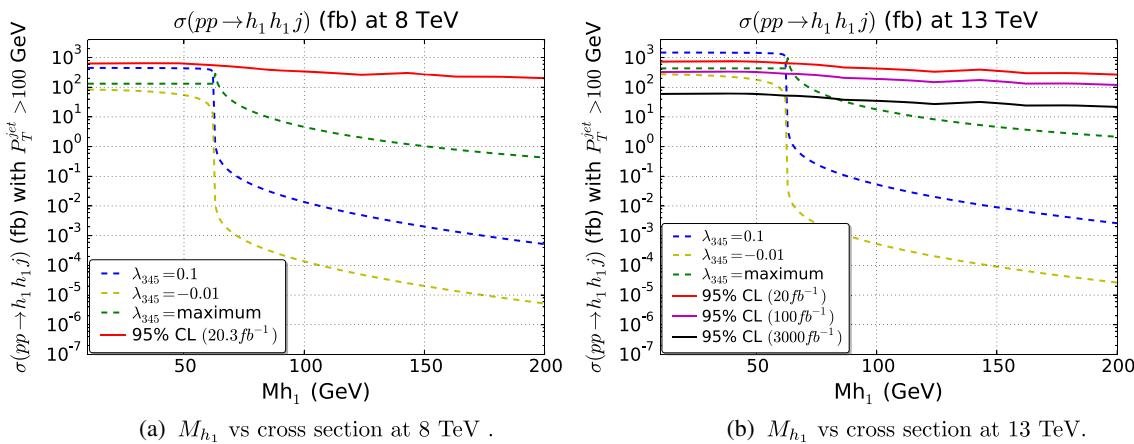


FIG. 19. Cross sections and 95% C.L.s for $pp \rightarrow h_1 h_1 j$ versus M_{h_1} at 8 and 13 TeV. In both cases, the cross sections are shown for three different values of λ_{345} : (i) $\lambda_{345} = 0.1$ (blue dashed curve), (ii) $\lambda_{345} = -0.01$ (yellow dashed curve), and (iii) the maximum λ_{345} value (green dashed curve) allowed by constraints (described in text). (a) Results for 8 TeV, with limits (solid red curve) calculated using the ATLAS analysis [106]. (b) Results for 13 TeV, with projected limits for the ATLAS analysis [106] with luminosities of 20 fb^{-1} , 100 fb^{-1} , and 3000 fb^{-1} (red, magenta, and black solid lines) at 13 TeV.

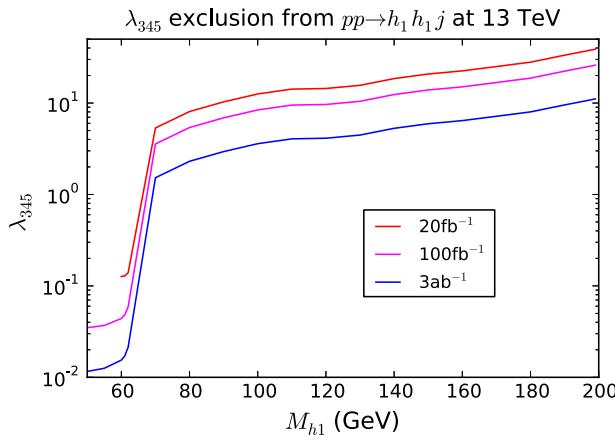


FIG. 20. Projected limit on λ_{345} from $pp \rightarrow h_1 h_1 j$ at 13 TeV derived from the analysis presented in Fig. 19.

emphasized that as the couplings of the relevant diagrams (see Fig. 13) are fixed by the gauge couplings, this limit on M_{h_1} is independent of all parameters other than ΔM . At 13 TeV, and at higher luminosities, this lower limit on M_{h_1} in this degenerate mass scenario is improved slightly to 41 GeV, 43 GeV, and 55 GeV for 20 fb^{-1} (solid red curve), 100 fb^{-1} (solid magenta curve), and 3000 fb^{-1} (solid black curve) of integrated luminosity, respectively, as is shown in Fig. 21(b). For $\Delta M = 100 \text{ GeV}$, the production cross section is much smaller and the model is not constrained via monojet and E_T^{miss} signatures from the $pp \rightarrow h_1 h_2 j$ process. However, in this region other collider signatures such as dilepton + E_T^{miss} from the decay $h_2 \rightarrow h_1 Z$ are available and will provide stronger limits as studied for example in [73].

V. CONSTRAINING i2HDM: FUTURE PROJECTIONS

Taking into consideration these collider limits and also adding the projections of the direct detection XENON1T experiment, we are able to impose the complete set of constraints on the i2HDM parameter space. It is worth stressing that, as before, we present the limits using the rescaled DD cross section $\hat{\sigma}_{\text{SI}} = R_\Omega \times \sigma_{\text{SI}}$, where $R_\Omega = \Omega_{\text{DM}}/\Omega_{\text{DM}}^{\text{Planck}}$, which allows us to take into account additional sources that could contribute to the DM relic density.

A. Highlighting the “always allowed” regions

The results of the constraints are presented in Fig. 22 as the color map of DM relic density in the (M_{h_1}, λ_{345}) plane together with the projected sensitivity of the LHC@13 TeV with 3 ab^{-1} of integrated luminosity using $h_1 h_2 j$ and $h_1 h_1 j$ channels, as well as a projection for the XENON1T experiment 95% C.L. exclusion regions. These constraints are indicated by black, dark grey, and light grey colors, respectively. In this figure we plot *excluded points on the top of the allowed points* demonstrating the colored region of the parameter space which will always be allowed (AA). Figures 22(a) and 22(b) present AA parameter space for the combined constraints (black on the top of dark grey and dark grey on the top of light grey) for large and zoomed (M_{h_1}, λ_{345}) regions, respectively, while Figs. 22(c) and 22(d) present AA regions for separate XENON1T and $h_1 h_1 + \text{jet}$ LHC13 constraints, respectively. From Fig. 22(a)–22(c) one can see how constraints from the LHC and XENON1T are complementary to each other. One can see that XENON1T will exclude large M_{h_1} masses for

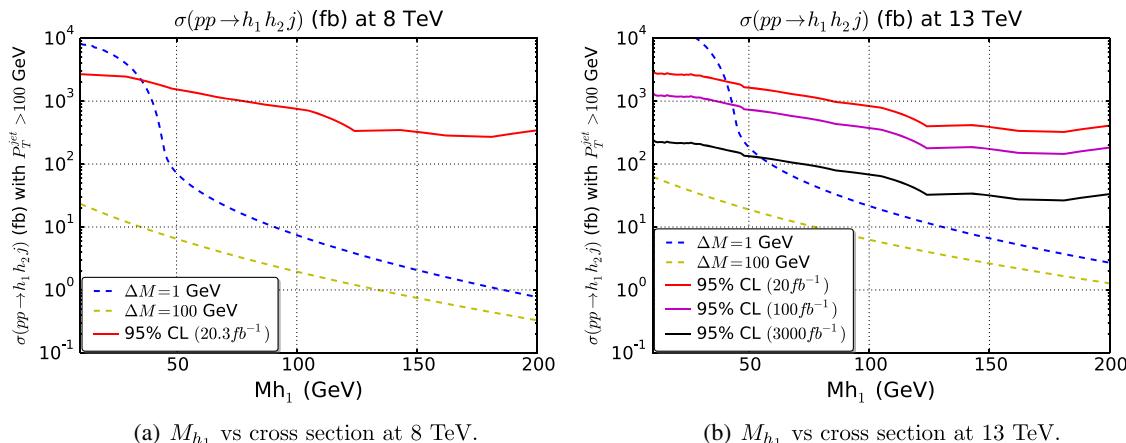


FIG. 21. Cross sections and 95% C.L.s for $pp \rightarrow h_1 h_2 j$ versus M_{h_1} at 8 and 13 TeV. In both cases, the cross sections are shown for two different values of $\Delta M = M_{h_2} - M_{h_1}$: (i) $\Delta M = 1 \text{ GeV}$ (blue dashed curve), and (ii) $\Delta M = 100 \text{ GeV}$ (yellow dashed curve). (a) Results for 8 TeV, with limits (solid red curve) calculated using the ATLAS analysis [106]. (b) Results for 13 TeV, with projected limits for the ATLAS analysis [106] with luminosities of 20 fb^{-1} , 100 fb^{-1} , and 3000 fb^{-1} (red, magenta, and black solid lines) at 13 TeV.

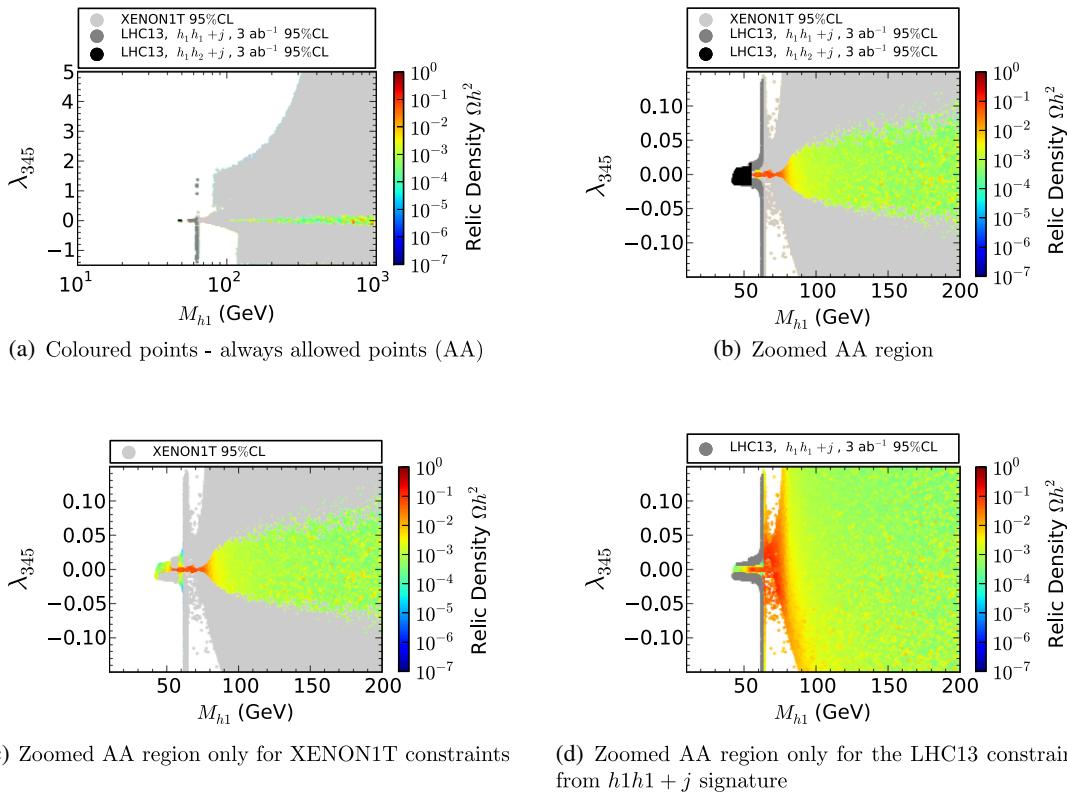


FIG. 22. Projection of the 5D random scan of the i2HDM into the (M_{h_1}, λ_{345}) plane and the expected reach of the LHC@13 TeV with 3 ab^{-1} of integrated luminosity using $h_1 h_2 j$ and $h_1 h_1 j$ channels as well as for XENON1T experiment indicated by black, dark grey, and light grey colors, respectively. Excluded points are plotted on the top of the allowed points demonstrating the colored region of the parameter space which will always be allowed (AA): (a) and (b) present AA parameter space for the combined constraints for large and zoomed (M_{h_1}, λ_{345}) regions, respectively; (c) and (d) present AA regions for separate XENON1T and $h_1 h_1 + j$ jet LHC13 constraints, respectively.

large enough values of λ_{345} while the LHC will probe the region of smaller values of λ_{345} for M_{h_1} below the $M_H/2$ threshold using the $h_1 h_1 j$ channel, and will cover all values of λ_{345} using the $h_1 h_2 j$ channel for M_{h_1} below 55 GeV.

B. Highlighting the “always excluded” regions

Besides the AA region it is informative to find and analyze the region with *allowed points on the top of excluded points*; therefore the black and grey colors present the region which always will be probed—and in the case of negative results, always excluded (AE)—by the above experiments. Such a region is presented in Figs. 23(a) and 23(b) in exact analogy to Figs. 22(a) and 22(b).

When comparing Figs. 22(a) and 22(b) and Figs. 23(a) and 23(b)—i.e. the plots with AA versus AE points—one observes a big difference between the order of the overlay of the excluded and allowed points. This is related to the fact that the $\Omega_{\text{DM}} h^2$ can substantially vary: even for fixed M_{h_1} and λ_{345} values, a large $M_{h_1^+}$ or $M_{h_2^-}$ can provide, respectively, large quartic couplings $h_1 h_1 W_L W_L$ and $h_1 h_1 Z_L Z_L$ [see Eq. (8)], which lead in their turn to an effective $h_1 h_1 \rightarrow VV$ annihilation. This brings the relic

density down and avoids the XENON1T constraints (once we use DD rates rescaled to relic density). In the (λ_{345}, M_{h_1}) plane, for example, these points overlap with the points where the quartic couplings mentioned above are small and the $\Omega_{\text{DM}} h^2$ (and, respectively, exclusion) is driven only by λ_{345} . So the most complete picture comes from the combination of AA and AE plots: the most conservative allowed region comes from AA plots of Fig. 22, while the most conservative exclusion region is presented by AE plots of Fig. 23.

From Figs. 22 and 23 one can see that imposition of the XENON1T constraint reduces substantially the parameter space, greatly expanding the previous limits imposed by LUX. This effect is not so evident in the other planes, presented in Fig. 24 in analogy to Fig. 23, because the spin-independent cross section $\hat{\sigma}_{\text{SI}}$ for DD is driven by the t -channel Higgs boson exchange and therefore is proportional to λ_{345}^2 .

One should stress again the importance of the $pp \rightarrow h_1 h_2 + j$ process, using which one can exclude $M_{h_1} < 55 \text{ GeV}$ when $M_{h_2} - M_{h_1}$ is small for all values of λ_{345} . This is shown clearly with the black dots in Figs. 24(b) and 24(d) where the (co)annihilation and respective mass

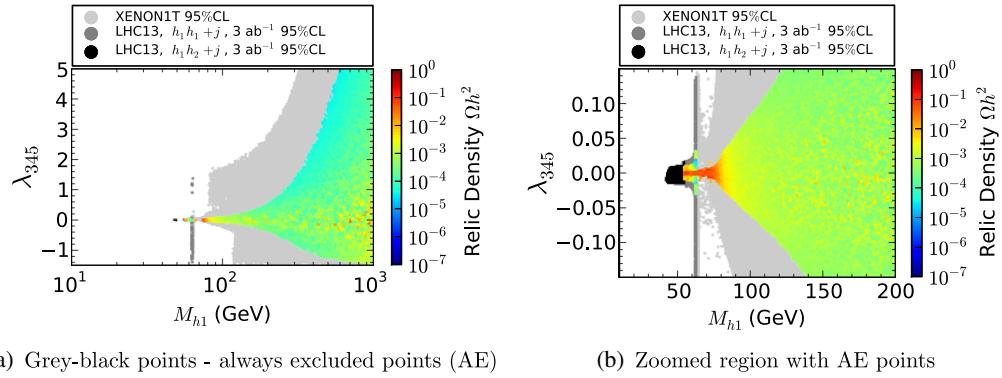


FIG. 23. Projection of the 5D random scan of the i2HDM into the (M_{h_1}, λ_{345}) plane and the expected reach of the LHC@13 TeV with 3 ab^{-1} of integrated luminosity using h_1h_2j and h_1h_1j channels as well as for the XENON1T experiment. Allowed points are on the top of the excluded ones; therefore the black and grey colors present the region which will always be excluded (AE) or probed by the above experiments.

degeneracy between M_{h_1} and M_{h_2} take place. Finally the $pp \rightarrow h_1h_1 + j$ process imposes an extra constraint for the zone with low relic density corresponding to the $h_1h_1 \rightarrow H$ resonant annihilation just above $M_{h_1} = M_H/2$. In this case the invisible Higgs decay $H \rightarrow h_1h_1$ is closed and there is no restriction on $|\lambda_{345}|$, as we can see in Figs. 24(b) and 24(d) represented by the dark grey points.

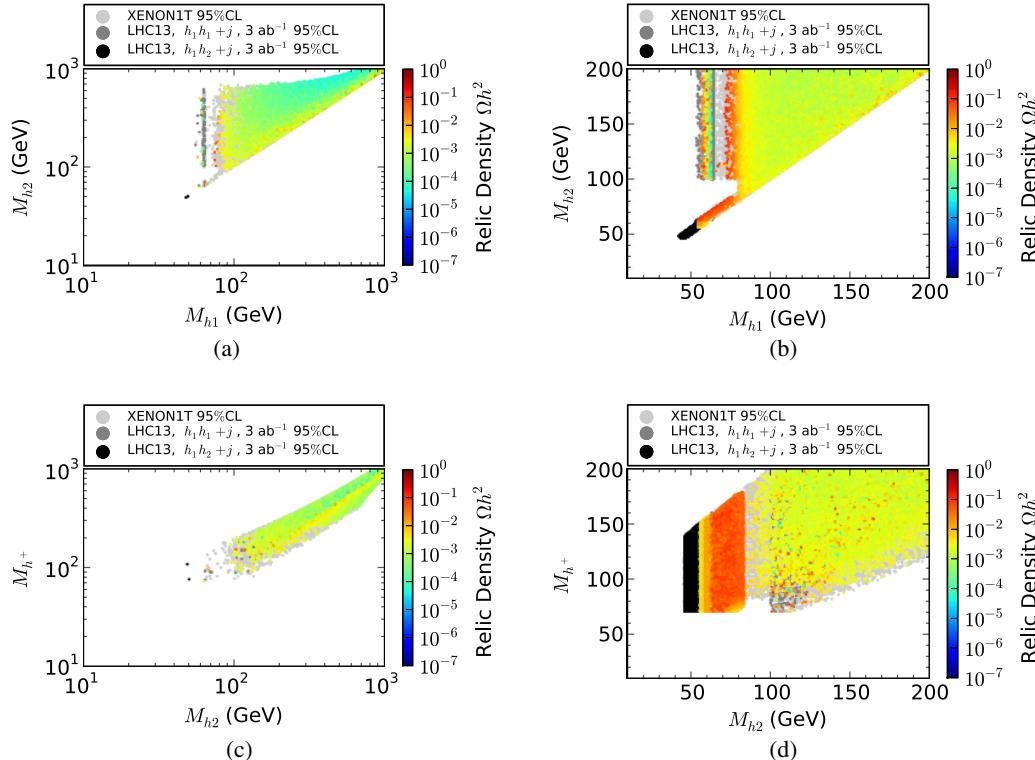
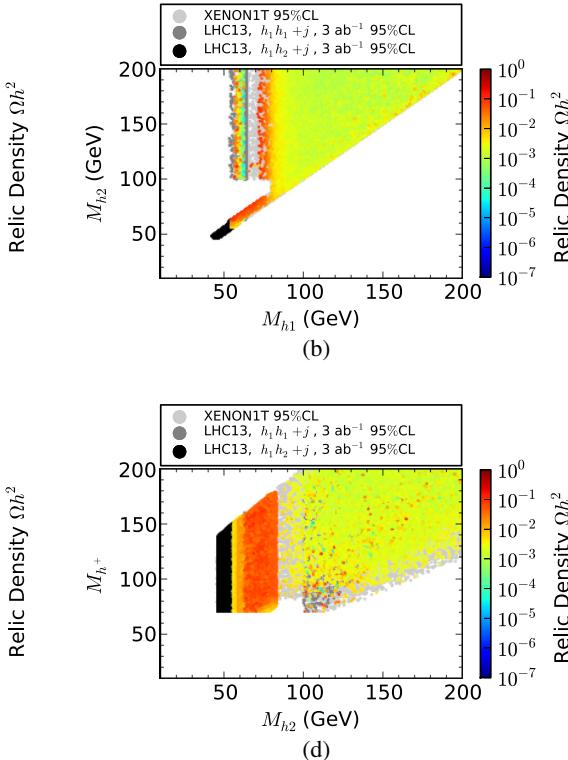


FIG. 24. Projection of the 5D random scan of the i2HDM into (a),(b) (M_{h_1}, M_{h_2}) and (c),(d) (M_{h_2}, M_{h^+}) planes and the expected reach of the LHC@13 TeV with 3 ab^{-1} of integrated luminosity using h_1h_2j and h_1h_1j channels as well as for the XENON1T experiment. Allowed points are on the top of the excluded ones, presenting AE points. The left panels (a),(c) present a bigger region of the parameter space, while the right ones (b),(d) present a zoomed region with AE points.

C. Fitting the PLANCK data: Future projections

We have also found the projected limits from colliders of monojet signatures and the XENON1T DD experiment for the i2HDM points which satisfy both the upper and the lower PLANCK limits, Eq. (30). In this case, the scattering cross section σ_{SI} is not rescaled, because we are in the zone with the right amount of DM relic density. The results of



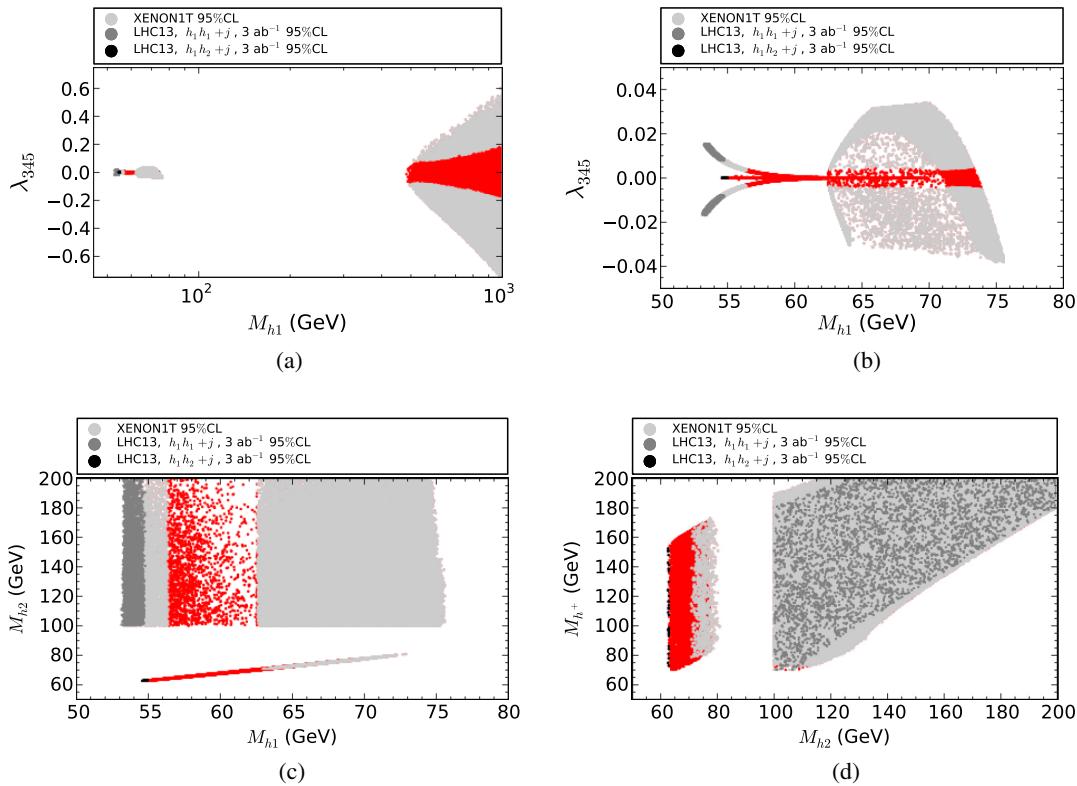


FIG. 25. The 2D projections of the 5D random scan of the i2HDM satisfying all constraints (Cut-1 to Cut-4) considered above for Figs. 26 and 27 plus the lower limit on the constraint on relic density given by Eq. (30), taking into consideration the collider limits of monojet signatures at 13 TeV with 3 ab^{-1} of integrated luminosity and the projections of the DD XENON1T experiment. In the first row we present the parameter space of the plane (M_{h_1}, λ_{345}) in the range $\subset [10 \text{ GeV} - 1000 \text{ GeV}]$. In the second row we present the planes (M_{h_1}, λ_{345}) and (M_{h_1}, M_{h_2}) in the range $\subset [50 \text{ GeV} - 80 \text{ GeV}]$.

these constraints are presented in Fig. 25 as a scatter plot where the red zones represent the right amount of DM relic density. In the first row we show the parameter space of the plane (M_{h_1}, λ_{345}) in the full mass range from 10 to 1000 GeV. In the second row we present the planes (M_{h_1}, λ_{345}) and (M_{h_1}, M_{h_2}) but in a narrow mass range between 50 and 80 GeV.

As we can see, the incorporation of the DD constraint sets important restrictions on the parameter space. Still, in Fig. 25(a) there is a zone in the upper mass range that is not ruled out. Also in the low mass range there is a region between $55 \text{ GeV} < M_{h_1} < 74 \text{ GeV}$ which survives the restrictive constraint for small values of λ_{345} . We zoom into the surviving low mass region in Figs. 25(b) and 25(c). Because of the improved limits of the DD experiment, the parameter λ_{345} is very sensitive to the scattering cross section, which sets a limit of $|\lambda_{345}| < 0.01$ for this mass range.

The $p p \rightarrow h_1 h_2 + j$ process sets the exclusion limit for $M_{h_1} < 55 \text{ GeV}$ (black dots) at the beginning of the $h_1 h_2$ coannihilation region represented by the thin horizontal strip for very small values of λ_{345} in Fig. 25(b), which is also seen in the lower part of Fig. 25(c). The $p p \rightarrow h_1 h_1 + j$ process imposes an extra constraint on the lower mass zone

where the DM annihilates through the Higgs boson exchange and is visible in Fig. 25(b) in the shape of two symmetric wings for negative and positive values of λ_{345} . This excludes the $M_{h_1} < 55 \text{ GeV}$ region. XENON1T will improve this constraint and exclude the $M_{h_1} < 56.5 \text{ GeV}$ region.

VI. CONCLUDING REMARKS

The i2HDM is a clear example of a minimal consistent DM model which is very well motivated by theoretical considerations. At the same time this model could provide monojet, mono-Z, mono-Higgs, and VBF + E_T^{miss} signatures at the LHC complemented by signals in direct and indirect DM search experiments.

The model is implemented into the CALCHEP and MICROMEGAs packages and is publicly available at the HEPMDB database together with the LanHEP model source. It is ready for further exploration in the context of the LHC, relic density, and DM direct detection.

In this paper we have performed detailed analysis of the constraints in the full 5D parameter space of the i2HDM from perturbativity, unitarity, electroweak precision data, Higgs data from the LHC, DM relic density, direct/indirect

DM detection, and the LHC monojet analysis as well as implications of experimental LHC studies on disappearing charged tracks relevant to the high DM mass region. The LHC monojet analysis for the i2HDM model has been performed at the fast detector simulation level and provides new results together with limits from disappearing charged tracks at the LHC. Our results on non-LHC constraints are summarized in Figs. 6–8 in Sec. III as well as in more detailed Figs. 26–28 in Appendix which show the effect of consequent application of constraints from the following: (a) vacuum stability, perturbativity, and unitarity; (b) electroweak precision data, LEP constraints, and the LHC Higgs data; and (c) relic density constraints as well as constraints from LUX on DM from direct detection. In this paper we have explored for the first time the parameter space where DM from the i2HDM is underabundant implying an additional source of DM, using the above constraints complemented by the collider searches. We have also explored the parameter space in which the DM candidate of i2HDM represents 100% of the total DM budget of the Universe. We found that the parameter space with $M_{h_1}, M_{h_2} < 45$ GeV or $M_{h^+} < 70$ GeV is completely excluded, confirming the first limit found previously complemented the second one found in this study.

Though in general the parameter space of the i2HDM is five-dimensional, the parameter space relevant to the LHC monojet signature is only one or two dimensional, so the model can be easily explored at the LHC. There are two qualitatively different and complementary channels in monojet searches: $pp \rightarrow h_1 h_1 j$ and $pp \rightarrow h_1 h_2 j$, with the second one being relevant to the monojet signature when the mass gap between h_2 and h_1 is of the order of a few GeV. In the case of $h_1 h_2$ degeneracy, the rate for $pp \rightarrow h_1 h_1 j$ will be effectively doubled since $g_{Hh_2h_2} = g_{Hh_1h_1}$ [see Eq. (8)], and this easily can be taken into account for the estimation of constraints in the respective region of the parameter space. For a fixed M_{h_1} , the strength of the first process depends only on λ_{345} because the Higgs boson is the only mediator, while the strength of the second process is fixed by the weak coupling since the Z boson is the only mediator for this process. The last process is important to cover the $h_1 h_2$ coannihilation region available for $54 \text{ GeV} < M_{h_1} < 73 \text{ GeV}$, where the relic density agrees with the PLANCK data. The results on this process and on this region are new to our best knowledge. Therefore these two processes complement each other in covering the parameter space: for large values of λ_{345} , $pp \rightarrow h_1 h_1 j$ would be the dominant LHC signature, while for small or vanishing values of λ_{345} , the $pp \rightarrow h_1 h_2 j$ process will cover additional parameter space as demonstrated in Figs. 22–25.

Talking about quantitative results, the LHC has rather limited potential to probe M_{h_1} with the monojet signature. Even for the projected luminosity of 3 ab^{-1} , we have found that the LHC could set a limit on M_{h_1} up to 83 GeV from

the $pp \rightarrow h_1 h_1 j$ process with the maximal value allowed for λ_{345} and only up to 55 GeV from $pp \rightarrow h_1 h_2 j$ for any value of λ_{345} , covering just the tip of the $h_1 h_2$ coannihilation region. Such a weak sensitivity of the LHC is related to the similarity between the shapes of the E_T^{miss} distribution of the dominant $Zj \rightarrow \nu\nu j$ background and that of the signal which has the same Z-boson mediator, while the DM mass is not very different from $M_Z/2$, which as shown in [15] is the reason for such a similarity in E_T^{miss} shape. At the same time, the potential of the LHC using a search for disappearing charged tracks is quite impressive in probing M_{h_1} masses up to about 500 GeV already at 8 TeV with 19.5 fb^{-1} luminosity as we have found in our study.

We have also explored the projected potential of XENON1T to probe the i2HDM parameter space and have found that it is quite impressive, confirming results of previous studies. In our study we have presented “absolutely allowed” and “absolutely excluded” points in different projections of the i2HDM 5D space demonstrating different features of the models and the potential of current and future experiments. In general, DM DD experiments and collider searches complement each other: the $pp \rightarrow h_1 h_1 j$ process covers in the region with large λ_{345} coupling where DM DD rates are low because of the low relic density rescaling, while the $pp \rightarrow h_1 h_2 j$ process is sensitive to the parameter space with low λ_{345} where DM DD rates are low because of the low rate of DM scattering off the nuclei.

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APPENDIX: NUMERICAL SCAN: DETAILED DISCUSSION

To have a complete picture of the properties of i2HDM in the whole parameter space, we have performed

a five-dimensional random scan of the model parameter space with about 10^8 points, evaluating all relevant observables and limits mentioned above. The range for the model parameters of the scan was chosen according to Eq. (18).

To better delineate the impact of each constraint, we have imposed different cuts on the parameter space sequentially, following the classification below:

Cut-1: theoretical constraints on the potential from vacuum stability [Eqs. (11), (12), and (17)], perturbativity and unitarity [Eqs. (13)–(16)];

Cut-2: constraints from LEP [Eqs. (19) and (23)], EWPT [Eq. (22)], and the LHC Higgs data [Eqs. (25) and (26)];

Cut-3: constraint on the relic density [$\Omega_{\text{DM}} h^2 \leq 0.1184 + 2 \times 0.012$], where we consider only the upper bound within 2 standard deviations;

Cut-4: constraints from DM DD searches from LUX.

The results of the scan are presented in Fig. 26 in the form of a color map of DM relic density, projected on two-dimensional planes: (M_{h_1}, λ_{345}) in the first, (M_{h_1}, M_{h_2}) in the second, and (M_{h_2}, M_{h^+}) in the third column, respectively. The four rows reproduce the effect of the progressive application of the four cuts defined above. In Fig. 27 we also present, in the same format, the results of a finer scan, zoomed to the region of low masses, where the range has been restricted to 10–200 GeV for the three masses M_{h_1} , M_{h_2} , and M_{h^+} . The latter is the most relevant corner of parameter space for the LHC phenomenology that we will discuss in the next section. Note that the lower bound of λ_{345} presented in these plots corresponds to the lowest limits allowed by unitarity, perturbativity, and scalar potential constraints (see Fig. 2).

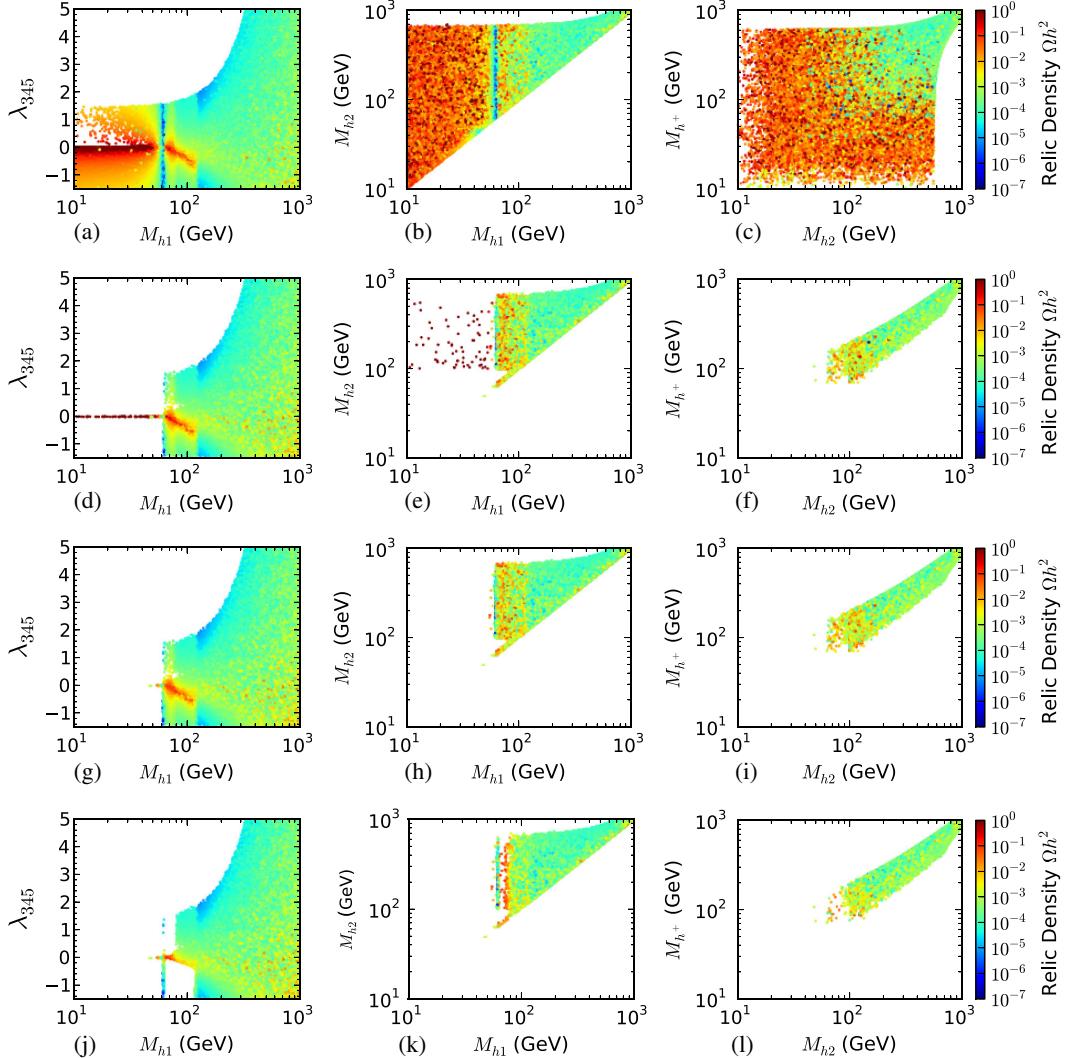


FIG. 26. Color maps of DM relic density for 2D projections of the 5D random scan of the i2HDM: each row demonstrates the effect of consequent application of the experimental and theoretical constraints in the (M_{h_1}, λ_{345}) , (M_{h_1}, M_{h_2}) , and (M_{h_2}, M_{h^+}) planes. Each row corresponds to Cut-1–Cut-4, described in the text: Cut-1 for (a)–(c) [Eqs. (11)–(15)]; Cut-2 for (d)–(f) [Eqs. (19), (23), (22), (25), (26)]; Cut-3 for (g)–(i) [$\Omega_{\text{DM}}^{\text{Planck}} h^2 \leq 0.1184 + 2 \times 0.012$]; Cut-4 for (j)–(l) [LUX].

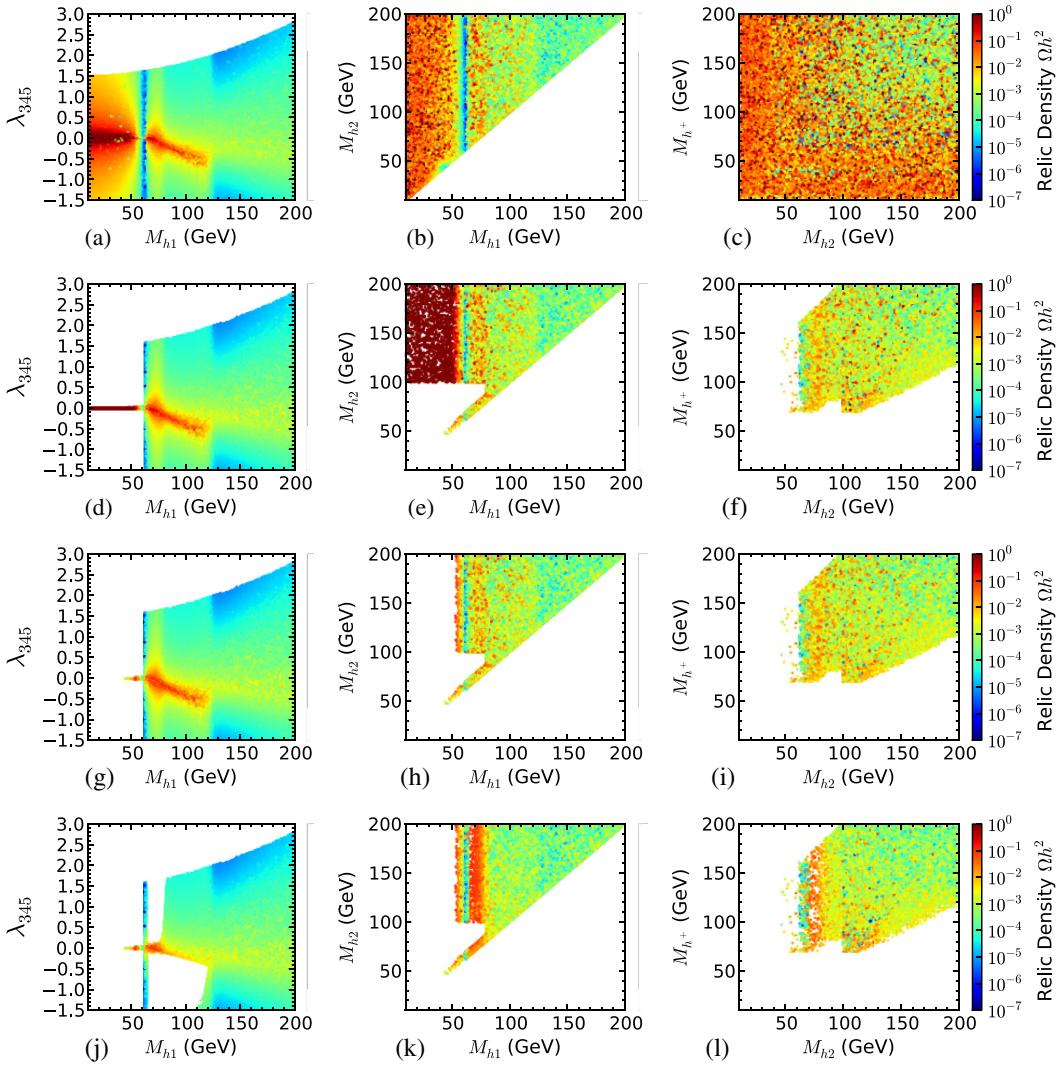


FIG. 27. Color maps of DM relic density for 2D projections of the 5D random scan of the i2HDM for the parameter space restricted to (10 GeV–200 GeV) for M_{h_1} , M_{h_2} , and M_{h^+} . As for Fig. 26 each row corresponds to Cut-1–Cut-4, described in the text: Cut-1 for (a)–(c) [Eqs. (11)–(15)]; Cut-2 for (d)–(f) [Eqs. (19), (23), (22), (25), (26)]; Cut-3 for (g)–(i) [$\Omega_{\text{DM}}^{\text{Planck}} h^2 \leq 0.1184 + 2 \times 0.012$]; Cut-4 for (j)–(l) [LUX].

One can see from Figs. 26 and 27(a) that λ_{345} is limited from above, and the dependence which defines the shape of this limit as a function of M_{h_1} comes from the vacuum stability condition given by Eq. (16). One can also see from Figs. 26, 27(a), 27(b), and analogous figures in the rows below, that the relic density is too high for small M_{h_1} values and small λ_{345} . Therefore, the relic density constraint combined with the LHC Higgs data constraints (limiting the invisible decays of the Higgs) restricts M_{h_1} to be above 45 GeV, as it can clearly be seen from Figs. 26, 27(g), and 27(h). For example, the range $45 \text{ GeV} < M_{h_1} < 50 \text{ GeV}$ is allowed but it requires $h_1 h_2$ coannihilation and respective mass degeneracy, as one can see from Figs. 26, 27(h), and 27(k). From Figs. 26, 27(a), 27(b), and analogous ones in the rows below, one can see a clear vertical blue pattern of

low relic density corresponding to the $h_1 h_1 \rightarrow H$ resonant annihilation. For $M_{h_1} > M_H/2$ the pattern of DM relic density follows the pattern of WW , ZZ , and HH thresholds presented earlier in Fig. 4.

One can also observe that the effect of Cut-1 plus Cut-2 is quite dramatic: (a) $\text{Br}(H \rightarrow h_1 h_1) < 0.28$ and $\mu^{\gamma\gamma} = 1.14^{+0.38}_{-0.36}$ constraints require $\lambda_{345} \leq 0.02$ for $M_{h_1} < M_H/2$ [Figs. 26–27(d)]; (b) LEP constraints require $M_{h_2} \gtrsim 100 \text{ GeV}$ if $M_{h_2} - M_{h_1} > 8 \text{ GeV}$ [Figs. 26–27(e)]; and (c) LEP and LHC Higgs data constraints require $M_{h^+} > 70 \text{ GeV}$, while M_{h_2} is generically excluded below $M_Z/2$ [Figs. 26–27(f)]. The effect from adding the (upper) cut from relic density (Cut-3) is shown in Figs. 26–27(g)–27(i): one can see that this cut (combined with the previous ones) excludes $M_{h_1} < M_Z/2$ for the whole i2HDM

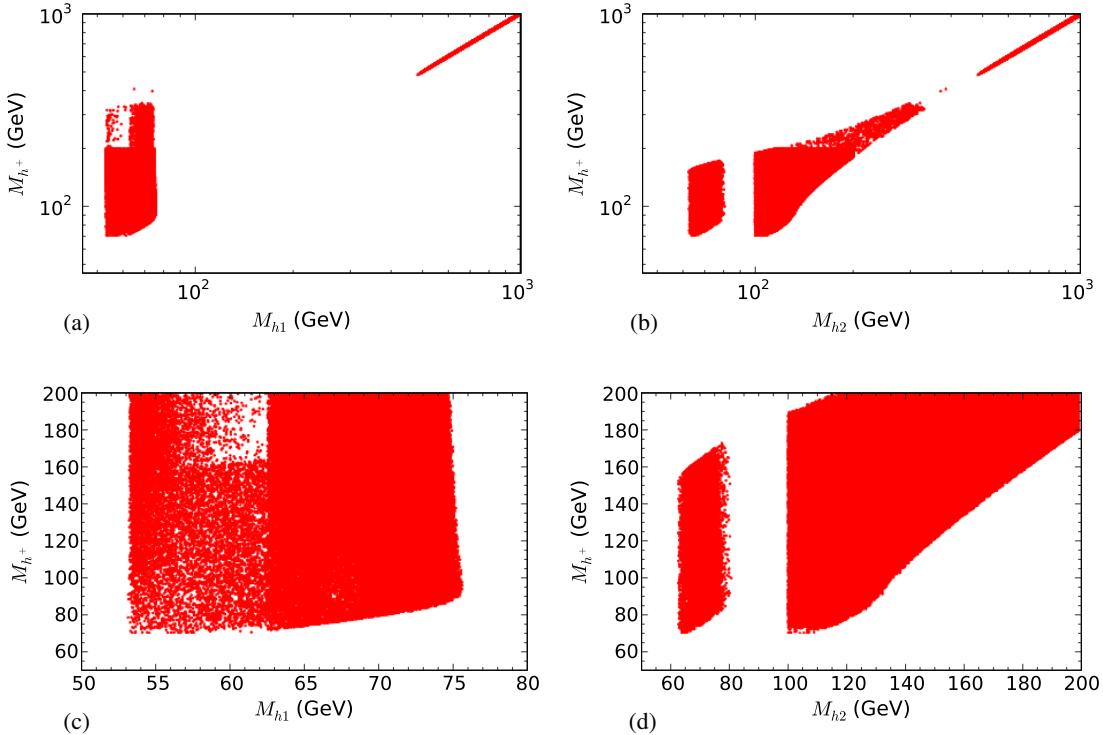


FIG. 28. The 2D projections of the random scan of the i2HDM for points satisfying all constraints and providing the correct relic abundance within two sigmas of the PLANCK result. The top row corresponds to the “full” parameter space $10 \text{ GeV} < M_{h_1}, M_{h_2}, M_{h^+} < 1000 \text{ GeV}$, while the lower row refers to the “zoomed” parameter space $10 \text{ GeV} < M_{h_1}, M_{h_2}, M_{h^+} < 200 \text{ GeV}$.

parameter space [Figs. 26–27(g) and 27(h)], but does not have a visible effect in the (M_{h_2}, M_{h^+}) plane [Figs. 26–27(i)]. Actually the region with $M_{h_1} < M_Z/2$ is excluded due to the interplay of several constraints. In the $M_{h_1} < M_H/2$ region with $|\lambda_{345}| \lesssim 0.02$ as required by LHC Higgs data, the only possibility for relic density of h_1 to be sufficiently low to satisfy the PLANCK constraints is the $h_1 h_2$ coannihilation channel: potentially this coannihilation could provide low enough relic density for M_{h_1} down to about 20 GeV. However, for $M_{h_1} + M_{h_2} < M_Z$ the $Z \rightarrow h_1 h_2$ decay is open and contributes significantly to the invisible Z-boson decay that is strongly limited by LEP. As the Z-boson partial width for this decay channel is defined just by M_{h_1} and M_{h_2} , since $Z h_1 h_2$ coupling is fixed by the gauge invariance, the $M_{h_1} + M_{h_2} < M_Z$ parameter space is completely excluded. For the $h_1 h_2$ coannihilation region, this exclusion is equivalent to $M_{h_1}, M_{h_2} \gtrsim M_Z/2$. The $h_1 h_2$ coannihilation corridor which provides relic density below or equal to the PLANCK limit is clearly visible in Figs. 26–27(e), 27(h), 27(k).

The additional constraint from DM DD from LUX (Cut-4) removes a substantial portion of the parameter space for large and intermediate $|\lambda_{345}|$ values for $M_{h_1} \lesssim M_H$ [Figs. 26–27(j)]. In this excluded parameter space the scattering cross section of h_1 on the proton is quite large due to the Higgs boson exchange enhanced by $|\lambda_{345}|$, while the relic density is respectively low, again due to the large

value $|\lambda_{345}|$, but it is not low enough to suppress the DM detection rate below the experimental exclusion. So, the LUX cut removes the low relic density region, and one can see this clearly in Figs. 26–27(k), 27(l) by the enhanced yellow-red color in the $M_{h_1} \lesssim M_H$ region in comparison to the respective Figs. 26–27(h), 27(i) where the DM DD cut was not applied. For $\lambda_{345} \gtrsim 0.2$ the parameter space is excluded for $M_H/2 < M_{h_1} < M_W$ while for $\lambda_{345} \lesssim -0.2$ it is excluded for $M_H/2 < M_{h_1} < M_H$ as illustrated in Figs. 26–27(j). Once the $h_1 h_1 \rightarrow W^+ W^-$ channel is open for positive λ_{345} , or the $h_1 h_1 \rightarrow HH$ channel is open for negative λ_{345} , the relic density drops substantially below the PLANCK limit, which makes the rescaling factor low enough to avoid limits from LUX searches. The difference between the positive and negative λ_{345} cases is related to the respective positive and negative interference of the $h_1 h_1 \rightarrow H \rightarrow XX$ channel with non-Higgs-exchange diagrams. This asymmetry between positive and negative λ_{345} cases was seen initially in Fig. 4, where the h_1 relic density was presented as a function of M_{h_1} for different λ_{345} values.

We would also like to point to some features of the scan for the region of M_{h_1}, M_{h_2} , and M_{h^+} above 200 GeV, presented in Fig. 26. From Figs. 26(f), 26(i), 26(l), one can see that EWPT constraints require a very modest mass split between M_{h_2} and M_{h^+} since this mass split is directly related to values of the M_{h_2} and M_{h^+} couplings to the SM Higgs as well as to the couplings to longitudinal

components of the W and Z bosons. Therefore constraints from S and T parameters leave only a rather narrow corridor in the (M_{h^+}, M_{h_2}) plane.

Finally, for the case when the relic density is required to fit the PLANCK result within two sigmas, 2D projections on the (M_{h_1}, M_{h^+}) and (M_{h_2}, M_{h^+}) are shown in Fig. 28.

The plots in the top row show results for the “full” scan $10 \text{ GeV} < M_{h_1}, M_{h_2}, M_{h^+} < 1000 \text{ GeV}$, while in the lower row we present the “zoomed” scan $10 \text{ GeV} < M_{h_1}, M_{h_2}, M_{h^+} < 200 \text{ GeV}$. These plots complement the information on the surviving regions given by Fig. 8 in the main text.

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