

UNIVERSIDADE FEDERAL DE RORAIMA
DISCIPLINA DE ÁLGEBRA LINEAR
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LISTA 19

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① a) $T: \mathbb{R}^3 \rightarrow \mathbb{R}^3$ $T(x, y, z) = (2x, 2y, x+y+3z)$

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 1 & 3 \end{bmatrix}$$

$$P(\lambda) = (A - \lambda I)$$

$$\det(A - \lambda I) = \begin{vmatrix} 1-\lambda & 0 & 0 & 1-\lambda & 0 \\ 0 & 1-\lambda & 0 & 0 & 1-\lambda \\ 1 & 1 & 3-\lambda & 1 & 1 \end{vmatrix}$$

$$A - \lambda I = \begin{bmatrix} 1-\lambda & 0 & 0 & 0 \\ 0 & 1-\lambda & 0 \\ 1 & 1 & 3-\lambda \end{bmatrix}$$

$$\det(A - \lambda I) \Rightarrow (1-\lambda) \cdot (1-\lambda) \cdot (3-\lambda) = 0$$

$$\begin{array}{l} 1-\lambda=0 \quad 3-\lambda=0 \\ \boxed{\lambda_1=1} \quad \boxed{\lambda_2=3} \end{array}$$

Para $\lambda_1=1$:

$$\begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 1 & 1 & 3 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \end{bmatrix} = 1 \cdot \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{array}{l} 2x = x \quad \therefore x = y = 0 \\ 2y = y \quad \therefore x + y + 3z = 0 \\ x + y + 3z = 0 \end{array}$$

$$\vec{v}_1 = (0, 0, 0)$$

Para $\lambda_2=3$:

$$\begin{array}{l} 2x = 3x \\ 2y = 3y \\ x + y + 3z = 3z \end{array}$$

$$x=0$$

$$y=0$$

$$z=0$$

$$\vec{v}_2 = (0, 0, 0)$$

1/b) $S: \mathbb{R}^3 \rightarrow \mathbb{R}^3$ definido por $S(x, y, z) = (x, x+y, x-2z)$

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 0 & -2 \end{bmatrix}$$

$$\det(A - \lambda I) = \begin{vmatrix} 1-\lambda & 0 & 0 \\ 1 & 1-\lambda & 0 \\ 1 & 0 & -2-\lambda \end{vmatrix}$$

$$\det(A - \lambda I) = (1-\lambda) \cdot (1-\lambda) \cdot (-2-\lambda) = 0$$

$$1-\lambda=0 \quad -2-\lambda=0$$

$$\boxed{\lambda_1 = 1} \quad \boxed{\lambda_2 = -2}$$

Para $\lambda_2 = -2$:

$$\begin{bmatrix} 3 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 0 & -2 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \end{bmatrix} = -2 \cdot \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{cases} x = -2x \\ x+y = -2y \\ x-2z = -2z \end{cases}$$

$$\boxed{x=0}$$

$$x-2z = -2z \quad \boxed{x=0}$$

$$x = -2y - y$$

$$\boxed{x = -3y}$$

$$\vec{v}_1 = (0, -3, 0)$$

Para $\lambda_1 = 1$:

$$\begin{cases} x = x \Rightarrow 0 \\ x+y = y \Rightarrow 0 \\ x-2z = z \end{cases}$$

$$x-2z-z=0$$

$$x-3z=0$$

$$\boxed{x=3z}$$

$$\vec{v}_2 = (0, 0, 3)$$

Selma

L19 - AL

(12) b) A é diagonalizável pois os autovalores encontrados usando o polinômio característico formam uma base e A é diagonal.