

**Why Risk it, When You Can {rix} it: A Tutorial for Computational Reproducibility Focused
on Simulation Studies**

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Abstract

Reproducibility remains limited in psychology, in part because reproducibility exists on a spectrum – from sharing isolated code fragments to providing fully executable pipelines that ensure identical results. This article introduces Nix and the {rix} R package as a way to provide a comprehensive solution for achieving full computational reproducibility in simulation studies.

Building on this, we also demonstrate a tutorial on how to use {rix} to obtain a reproducible manuscript using the apaquarto extension.

Keywords: reproducibility, Nix, simulation studies, R, computational methods

Why Risk it, When You Can {rix} it: A Tutorial for Computational Reproducibility Focused on Simulation Studies

Psychological science is in the midst of a credibility revolution, which has prompted substantial progress in how research is conducted and evaluated (Vazire, 2018). Yet, despite notable progress, a key cornerstone of science, reproducibility (i.e., the ability to precisely reproduce the results of a study or studies based on provided data, code, materials, and software/hardware) remains limited (Hardwicke et al., 2020).

Open-science initiatives have encouraged more transparent research practices. Journal incentives such as open-science badges (Kidwell et al., 2016), together with platforms like GitHub and the Open Science Framework, have made data (Levenstein & Lyle, 2018) and code sharing increasingly routine. However, these efforts have largely focused on *what* is shared rather than *how* shared materials can be executed in practice. Data and code are never self-sufficient; they depend on a hierarchy of software components known collectively as dependencies, including the version of the programming language, the set of packages used by the analysis, and the system libraries that those packages require in order to function correctly. When these dependencies differ from those used in the original analysis, code may fail, behave differently across machines, or yield conflicting numerical results (Baker et al., 2024; Glatard et al., 2015; Hodges et al., 2023; Nosek et al., 2022).

A key challenge in addressing this gap is that reproducibility is not a binary feature but instead exists along a continuum (Peng, 2011). At the lower end of this continuum, researchers may share only their manuscript. Further along the spectrum, they might provide partial code, full analysis scripts, or publicly accessible datasets. At the highest level, researchers document a fully specified computational environment that allows others to recreate identical results—from raw data to final manuscript output—with minimal friction. These issues are particularly acute for simulation studies, which rely on complex codebases, versioned dependencies, and intricate software configurations (Luijken et al., 2024; Siepe et al., 2024).

A figure highlighting this might be good here (JG)

To be clarified: what “this” refers to? (FV)

In this article, we use *computational environment* to refer to the complete software context required for an analysis to run successfully. This includes the version of the programming language (e.g., R 4.3.3), the versions of all required packages, the system libraries that those packages rely on, and the operating system under which the analysis executes (Rodrigues, 2023). Crucially, these components interact: a package version may require a specific system library; a system library may behave differently across operating systems; and certain analyses rely on features available only in particular language versions. We therefore define *computational environment reproducibility* as the ability to reconstruct this entire software stack—language, packages, system libraries, and operating system—on any machine and at any future time, such that executing the same code yields the same numerical results. Environment reproducibility is foundational, because even perfectly documented code cannot be executed reliably if its surrounding software context is unspecified or cannot be recreated.

Consistent with this definition, prior work emphasizes that reproducible research requires more than the availability of code and data; it also requires controlling software dependencies, relying on open-source tools, literate programming, and ensuring access to the outputs that substantiate reported claims (Epskamp, 2019; Peikert & Brandmaier, 2021; Rodrigues, 2023; Siepe et al., 2024; Wiebels & Moreau, 2021; Ziemann et al., 2023). Yet empirical assessments show that current practice falls short of these ideals. For example, Siepe et al. (2024) report that nearly two-thirds of simulation studies in psychology provide no accompanying code, and among those that do, documentation of the computational environment is rarely included. This gap is consequential: simulation studies inform methodological recommendations, meaning that insufficient reproducibility undermines confidence in those recommendations (Luijken et al., 2024; White et al., 2024).

These challenges may persist not because relevant tools are unavailable, but because researchers must navigate a fragmented landscape of solutions, each addressing only part of the computational environment. Package-level managers such as {renv} (Ushey, 2024), {groundhog}

([Simonsohn, 2020](#)), and `{rang}` ([Chan & Schoch, 2023](#)) stabilize R package versions but do not manage the R interpreter itself or the system-level libraries those packages depend on.

Conversely, interpreter-level tools such as `{rig}` (?) focus on managing R versions but do not address package or system dependencies. Documentation tools such `assessionInfo()` record aspects of the environment but do not allow users to reconstruct it. Meanwhile, workflow orchestration tools, such as `{targets}` ([Landau, 2021](#)) and Make ([Feldman, 1979](#)), support reproducibility in a different sense: they specify the structure of an analysis by formalizing the order in which steps should run and by tracking dependencies among intermediate results. These tools clarify how an analysis proceeds, but they assume that the software stack required to run each step is already stable. Containerization tools such as Docker and the Rocker project ([Boettiger, 2015](#); [Boettiger & Eddelbuettel, 2017](#)) offer a more comprehensive approach by bundling the full environment—operating system, system libraries, interpreter versions, and packages—into a single executable image. Containers thus solve an important part of the environment reproducibility problem. Yet their use requires familiarity with Linux system administration, including writing Dockerfiles, managing external repositories, and understanding image layering which may be perceived as “daunting” for some researchers ([Wiebels & Moreau, 2021](#)). Moreover, even containerization has limitations: as [Malka et al. \(2024\)](#) show, Dockerfiles often rely on mutable upstream repositories, meaning that rebuilding the same Dockerfile at a later time may not yield an identical environment. Containerization therefore improves reproducibility across machines but does not always ensure reproducibility across time.

Moreover, these challenges are compounded by the increasing complexity of modern psychological research. Many analyses involve more than one programming language (e.g., R and Python) and often incorporate system-level tools such as Quarto for manuscript generation, which in turn rely on external components such as LaTeX distributions whose versions and installed packages can vary substantially across systems. Coordinating dependencies across these heterogeneous components stretches existing tools beyond their intended scope. Researchers thus face a difficult choice between solutions that are accessible but incomplete or approaches that are

powerful but demand substantial technical expertise, especially for the integration of those tools.

In this article, we focus specifically on computational environment reproducibility as the foundation upon which other reproducibility practices depend. For that, we introduce Nix ([Dolstra et al., 2004](#)), a functional package manager designed to make software installation deterministic, and `{rix}` ([Rodrigues & Baumann, 2025](#)), an R interface that allows researchers to use Nix without needing deep knowledge of its underlying language or infrastructure. Our objective is not to introduce a specific workflow orchestration system or to prescribe a particular analytic structure. Instead, we aim to show how Nix and `{rix}` can establish a stable, cross-platform environment within which any analysis—whether organized through simple, documented script sequences using `source()` or through more formal orchestration tools—can be executed reliably.

We illustrate these ideas through a reproducible simulation study conducted in R, culminating in an automated APA-formatted manuscript generated with `apaquarto` ([Schneider, 2024](#)). Although the example centers on R because of its prominence in psychological methodology, the principles underlying environment reproducibility apply equally to other languages, including Python and Julia, and to different development environments such as RStudio, VS Code, Emacs, or Positron. Later in the article, we briefly comment on `{rixpress}` ([Rodrigues, 2025](#)), which extends Nix-based reproducibility to workflows requiring more sophisticated coordination across languages. Unlike `{targets}`, which is limited to R-based workflows, `{rixpress}` is designed for polyglot pipelines. This distinction is conceptually relevant, but workflow orchestration is not the focus of the present tutorial, which assumes a basic, documented execution order for scripts. Throughout, our emphasis remains squarely on the reproducibility of computational environments as the essential basis for transparent, reliable, and durable scientific workflows.

A Practical Example: Setting up a Reproducible Simulation Study with `{rix}`

Before proceeding with the technical implementation and tutorial, we refer readers to the Appendix A, which presents a simulation study scenario designed to ground the subsequent

discussion in a concrete example¹. The scenario mimics a typical methods manuscript, describing both the statistical design and the computational details one might encounter in practice. While the example is illustrative rather than substantive—readers can follow the tutorial without engaging with its particulars—we include it to anchor the discussion in something more tangible.

Simulation studies typically structure code into multiple component files, each handling a distinct analytical phase. Our implementation follows this convention, organizing the workflow into five sequential files²: data generation function (`01_data_generation.R`), statistical model specification (`02_models.R`), simulation execution (`03_run_simulation.R`), performance metric calculation (`04_performance_metrics.R`), and results visualization (`05_plots.R`). The simulation script (`03_run_simulation.R`) sources the data generation and model functions, executes the Monte Carlo replications, and saves results. The subsequent scripts read these saved results to compute performance metrics and generate visualizations. For convenience, we provide a master script (`06_run_all.R`) that loads all required packages and executes the complete workflow sequentially. Note that such sequential structures could benefit from explicit workflow orchestration tools and a clear documentation³. Therefore, this workflow depends on several R packages and more. The data generation depends on the `{rvinecopulib}` package (Nagler & Vatter, 2025). The `{marginaleffects}` provides the function for computing average causal effects (Arel-Bundock et al., 2024). The `{dplyr}` package is used for data wrangling (Wickham et al., 2023) and `{simhelpers}` supplies the functions for calculating the simulation performance metrics (Joshi & Pustejovsky, 2025). Parallel processing is handled by `{doParallel}` (Corporation & Weston, 2022), with `{doRNG}` (Gaujoux, 2025) ensuring reproducible random number generation across parallel workers. Visualization relies on `{ggplot2}` (Wickham, 2016) and

¹ Note that the rationale, programming-related choices, and results should not be used for substantial interpretation. For instance, the usage of `{rvinecopulib}` and the parallel set-up may be considered an overhead.

² Readers can find the files for these simulations here: <https://github.com/felipelfv/Why-risk-it-when-you-can-rix-it>

³ For instance, in this context, we use parallel processing which requires specifying the amount of cores to be used. This type of information should be mentioned.

{cowplot} ([Wilke, 2025](#)).

Now, suppose a researcher would have access to the .R files and attempts to run the simulation. What might prevent them from obtaining identical results?. The most immediate concern may involve package versions. A researcher installing packages today may encounter errors if functions have been renamed or deprecated, or may obtain results that differ subtly due to changes in computational defaults. Beyond package versions, some R packages depend on system-level libraries that must be installed separately from R itself. Our simulation illustrates this directly: the {rvinecopulib} package provides an interface to a C++ library and links against Boost, Eigen, and RcppThread ([Nagler & Vatter, 2025](#)). Moreover, the R language itself introduces version dependencies. Code written with R 4.3 may use syntax or functions unavailable in R 4.0. More subtly, R’s random number generator has changed across major versions, meaning that identical code with identical seeds can produce different random sequences depending on the R version. For simulation studies where reproducibility of specific random draws matters, this version sensitivity is consequential. Moreover, if one also employs literate programming for the manuscript, additional dependencies arise: R Markdown or Quarto documents require pandoc, and PDF output requires a LaTeX distribution—each with its own versioning and platform-specific installation.

Nix and {rix}: A Comprehensive Solution

Nix is a package manager built around declarative, isolated environments rather than ad hoc system-level installations. Unlike familiar tools such as `install.packages()` in R or `apt-get` on Linux, Nix manages language versions, package versions, system dependencies, and cross-platform consistency through a single framework ([Rodrigues & Baumann, 2025](#)). Rather than modifying shared directories, Nix builds each environment as an explicit, self-contained specification. This addresses the fragmented landscape described before: where researchers currently must coordinate separate tools for package management, interpreter versions, and system dependencies, Nix handles all three within a unified declarative model.

Maybe compare Nix to renv and Docker to highlight what nix gives us (JG)

Core Principles

Rather than installing software into global directories (e.g., `/usr/lib`), Nix places every package in its own directory under `/nix/store`. Each package path contains a cryptographic hash representing its precise inputs—source code, dependencies, and build instructions. Because these paths are content-addressed, multiple versions of the same software can coexist without conflict. A researcher can, for example, maintain projects requiring R 4.1.0 and R 4.3.3 side by side, or use different package versions across analyses, switching between them seamlessly ([Rodrigues & Baumann, 2025](#)).

The Nix ecosystem is built around `nixpkgs`, a version-controlled repository comprising more than 120,000 packages, including nearly all of CRAN and Bioconductor. By pinning a specific commit or date, researchers freeze the entire software stack—R itself, R packages, and all system libraries—at that point in time. This eliminates the system-dependency problems that tools like `renv` cannot address ([Rodrigues & Baumann, 2025](#)).

This architecture also ensures stability over time. Large-scale empirical work rebuilding over 700,000 packages from historical `nixpkgs` snapshots shows rebuildability rates above 99% and bit-for-bit reproducibility between 69–91%, demonstrating strong protection against temporal drift. Combined with binary caches, which often allow environments to materialize in seconds, Nix becomes practical for interactive research workflows ([Rodrigues & Baumann, 2025](#)).

The `{rix}` Package: R Interface to Nix

Nix expressions are written in a dedicated functional language unfamiliar to most researchers. The `{rix}` package removes this barrier by providing an R-native interface. A single call to `rix()` generates complete Nix configurations from standard R syntax, specifying R versions, CRAN packages, system libraries, and even Python or Julia components when required. Users never need to read or write Nix code directly, as `{rix}` performs the translation automatically ([Rodrigues & Baumann, 2025](#)).

A key feature of `{rix}` is its integration with `rstats-on-nix`, a community-maintained fork offering daily CRAN snapshots and weekly tested environments on Linux and macOS.

Researchers can request, for example, `rix(date = "2024-12-14")` to obtain a validated and reproducible environment without manually assessing compatibility. After the configuration is generated, `nix_build()` instantiates the environment, and binary caches typically allow this to complete within seconds ([Rodrigues & Baumann, 2025](#)).

Although Nix is capable of replacing tools like Docker for isolation or `{renv}` for package management, it does not require an all-or-nothing transition. Researchers can adopt it gradually and use it alongside familiar tooling. For instance, by building Docker images with Nix, converting existing `{renv}` lockfiles, or running `{targets}` pipelines within a Nix-defined environment ([Rodrigues & Baumann, 2025](#)). This allows Nix to strengthen reproducibility while preserving established workflows. For projects requiring more sophisticated pipeline management, `{rixpress}` extends Nix's guarantees to workflow orchestration, enabling step-level isolation across languages, though such capabilities lie beyond the present focus on environment reproducibility. We will come back to this after the tutorial.

Step I: Installing Nix and `{rix}`⁴

Installing Nix

Installation procedures differ across systems, and we highly suggest readers to consult the `{rix}` documentation and links therein for more information⁵.

Windows (via WSL2). On Windows, Nix runs inside the Windows Subsystem for Linux 2 (WSL2). To enable WSL2, run the following in PowerShell as an administrator (Listing 1):

After installing a Linux distribution (e.g., Ubuntu), it is recommended to activate

⁴ It is possible to use `{rix}` to generate Nix expressions even without having Nix installed on your system. In practice, this means that you can write a configuration (e.g., a `default.nix` file) without using Nix directly, but you cannot build or enter the resulting environment unless Nix is installed ([Rodrigues & Baumann, 2025](#)). Think of it like writing a recipe without needing a kitchen—`{rix}` helps you document exactly what ingredients are needed (e.g., which R version, which packages, which system dependencies), but you need Nix (the kitchen) to actually cook the meal.

⁵ See: <https://docs.ropensci.org/rix/articles/b2-setting-up-and-using-rix-on-macos.html> and <https://docs.ropensci.org/rix/articles/b1-setting-up-and-using-rix-on-linux-and-windows.html>

Listing 1 Enabling WSL2 on Windows

```
wsl --install
```

systemd, which improves compatibility with Nix. In your WSL2 Ubuntu shell, edit /etc/wsl.conf (Listing 2):

Listing 2 Editing the WSL configuration file

```
sudo -i  
nano /etc/wsl.conf
```

Then, this will open the /etc/wsl.conf in a nano (a command line text editor). Add (Listing 3):

Listing 3 Enabling systemd in WSL2

```
[boot]  
systemd=true
```

Next, save the file, then shut down WSL from PowerShell (Listing 4):

Listing 4 Shutting down WSL2

```
wsl --shutdown
```

After shutting down WSL, launch your WSL2 Ubuntu environment again from the Start menu.

Installing on Linux and Windows. Once your Linux or WSL2 environment is ready⁶, install Nix using the Determinate Systems installer (Listing 5):

After installation, set up the rstats-on-nix binary cache, which provides pre-built R packages and speeds up environment builds (Listing 6):

⁶ Windows users who choose not to enable systemd may need to append `--init none`; see {rix} documentation highlighted above.

Listing 5 Installing Nix on Linux and Windows (WSL2)

```
curl --proto '=https' --tlsv1.2 -sSf \
-L https://install.determinate.systems/nix | \
sh -s -- install
```

Listing 6 Configuring the rstats-on-nix binary cache on Linux/Windows

```
nix-env -iA cachix -f https://cachix.org/api/v1/install
cachix use rstats-on-nix
```

Although `{rix}` includes a `setup_cachix()` helper, the `{rix}` documentation recommends configuring the cache with the `cachix` client, as this properly updates system-level files when needed.

Installing on macOS.. On macOS, install Nix using the same Determinate Systems installer (Listing 7):

Listing 7 Installing Nix on macOS

```
curl --proto '=https' --tlsv1.2 -sSf \
-L https://install.determinate.systems/nix | \
sh -s -- install
```

Then enable the `rstats-on-nix` binary cache (Listing 8):

Listing 8 Configuring the rstats-on-nix binary cache on macOS

```
nix-env -iA cachix -f https://cachix.org/api/v1/install
cachix use rstats-on-nix
```

Installing {rix}

The method for installing `{rix}` depends on whether you already have R installed on your system. If you have R installed, you can install `{rix}` as follows (Listing 9):

Listing 9 Installing the {rix} package

```
# CRAN version
install.packages("rix")

# Development version
install.packages("rix", repos = c("https://ropensci.r-universe.dev"))
```

Once {rix} is installed, you can use it to generate `default.nix` files for your projects, which you then build with Nix. This latter part is explained in the next subsection (i.e., Specifying the Computational Environment; in Listing 12).

However, note that if you have installed Nix but do not yet have R on your system, or if you prefer to work entirely within the Nix ecosystem from the start, you can obtain both R and {rix} directly through Nix without installing R through the “traditional” means. The simplest approach is to create a temporary Nix shell that includes both R and {rix} by running this command in your terminal (Listing 10):

Listing 10 Creating a temporary Nix shell with R and {rix} (development version)

```
nix-shell --expr "$(curl -sL
  https://raw.githubusercontent.com/ropensci/rix/main/inst/extdata/default.nix)"
```

After downloading the necessary packages, an R session will start inside your terminal. You can then use {rix} to generate your project’s `default.nix` file (again, see Listing 12 in the next subsection). Alternatively, if you prefer the stable CRAN version of {rix}, you can create a temporary shell with (Listing 11):

Listing 11 Creating a temporary Nix shell with R and {rix} (CRAN version)

```
nix-shell -p R rPackages.rix
```

Note that the {rix} documentation recommends managing R versions exclusively through Nix rather than mixing system-installed R with Nix-managed environments for optimal

reproducibility, though both approaches are supported (see the following {rix} documentation: <https://docs.ropensci.org/rix/articles/z-advanced-topic-walkthrough-project.html>).

Step II: Specifying the Computational Environment

The initial step in establishing a reproducible environment is to create a script that will generate the environment specification. We recommend creating a file named `generate_env.R` (or similar) in the project directory. This script will use the `rix()` function from the {rix} package to produce a `default.nix` file—a declarative specification that precisely defines all software dependencies required for the project.

For our simulation study, we implement the environment specification shown, which can be found on the GitHub repository as a file named `generate_env.R` (Listing 12):

Note that we have more than the packages specified for the simulation scripts. In Appendix B, we mention more specifically the reasons for adding each package in `r_pkgs()` and `tex_pkgs()`.

The Environment Generation Script

The `rix()` function⁷ constructs this specification through a series of parameters that collectively describe the computational environment. Each parameter serves a distinct purpose in defining the environment’s characteristics.

Specifying the R version (line 1). Researchers must first determine which version of R to use. This can be accomplished in two ways: The `r_ver` parameter accepts an exact version string (e.g., “4.3.3”) or special designations such as “latest-upstream” for the most recent stable release. Alternatively, the `date` parameter specifies a particular date (e.g., “2024-11-15”), which ensures that R and all packages correspond to the versions available on that date. The date-based approach is generally preferable for reproducibility, as it captures a complete snapshot of the R ecosystem at a single point in time. For this tutorial, we use the `date` parameter to ensure temporal consistency across all software components (Rodrigues & Baumann, 2025) (see {rix} documentation for

⁷ For an overarching information on the function `rix()`, we suggest the following {rix} documentation: <https://docs.ropensci.org/rix/articles/c-using-rix-to-build-project-specific-environments.html>

more: <https://docs.ropensci.org/rix/articles/d2-installing-system-tools-and-texlive-packages-in-a-nix-environment.html>.

Declaring R package dependencies (line 2). The `r_pkgs` parameter accepts a character vector listing all required R packages by their CRAN names. These packages will be installed from the version repository corresponding to the specified date or R version. It is important to list all packages that the analysis will load directly; dependencies of these packages are automatically resolved by Nix. For packages requiring specific versions not corresponding to the chosen date, researchers can specify exact versions using the syntax "`packagename@version`" (e.g., `"ggplot2@2.2.1"`). For packages available only on GitHub or other Git repositories, the `git_pkgs` parameter accepts a list structure containing repository URLs and specific commit hashes (Rodrigues & Baumann, 2025). This ensures that exact development versions are obtained. For our simulation study, all packages were used with their CRAN versions (see `{rix}` documentation for more: <https://docs.ropensci.org/rix/articles/d2-installing-system-tools-and-texlive-packages-in-a-nix-environment.html>).

Including system-level dependencies (line 3). Many R-based workflows require tools beyond R packages. The `system_pkgs` parameter specifies system-level software such as Quarto for document generation, Git for version control, or Pandoc for document conversion. Critically, we include Quarto as a system package because this tutorial demonstrates full computational reproducibility—not merely of the simulation code, but of the complete manuscript itself. Our manuscript uses the `apaquarto` extension for APA formatting, stored in the project's `_extensions/` directory (Rodrigues & Baumann, 2025) (see `{rix}` documentation for more: <https://docs.ropensci.org/rix/articles/d2-installing-system-tools-and-texlive-packages-in-a-nix-environment.html>).

Specifying LaTeX packages (line 4). The `tex_pkgs` parameter specifies LaTeX packages needed for PDF compilation. When any packages are listed, Nix automatically includes a minimal TexLive distribution (`scheme-small`) as a base, to which the specified packages are added. Determining the required LaTeX packages typically involves some trial and

error—Quarto’s error messages during PDF rendering indicate which packages are missing, and these can then be added to `tex_pkgs` (see `{rix}` documentation for more: <https://docs.ropensci.org/rix/articles/d2-installing-system-tools-and-texlive-packages-in-a-nix-environment.html>).

Multi-language environment support. While this tutorial focuses on R, researchers working across multiple programming languages can include Python or Julia in their environments. The `py_conf` parameter accepts a list specifying a Python version and required packages (e.g., `py_conf = list(py_version = "3.12", py_pkgs = c("polars", "pandas"))`). Similarly, `jl_conf` enables Julia package installation. This capability is particularly useful for projects requiring statistical computing in R alongside machine learning pipelines in Python or numerical optimization in Julia (Rodrigues & Baumann, 2025) (see `{rix}` documentation for more:

<https://docs.ropensci.org/rix/articles/d1-installing-r-packages-in-a-nix-environment.html>).

Configuring the development environment (line 5). The `ide` parameter determines whether an integrated development environment should be included. Setting `ide = "rstudio"` installs a project-specific version of RStudio within the Nix environment. Note that on macOS, RStudio is only available through Nix for R versions 4.4.3 or later (or dates after 2025-02-28); for earlier versions, alternative editors must be used. Other supported IDEs include Positron (`ide = "positron"`), Visual Studio Code (`ide = "code"`), and command-line tools such as Radian (`ide = "radian"`). Each IDE installed via Nix is project-specific and will not interfere with system-wide installations. Researchers preferring to use an already-installed editor can set `ide = "none"` and configure their editor to interact with Nix shells (Rodrigues & Baumann, 2025) (see `{rix}` documentation for more: <https://docs.ropensci.org/rix/articles/e-configuring-ide.html>).

Setting file output parameters (line 7). The `project_path` parameter indicates where the `default.nix` file should be written (“.” denotes the current directory), while `overwrite` controls whether an existing file should be replaced. Setting `print = TRUE` displays the generated specification in the console for immediate verification (Rodrigues & Baumann, 2025).

Generating the Environment Specification

Executing this script, either by running from the terminal `Rscript generate_env.R`, sourcing it from within R using `source("generate_env.R")`, or running the `rix::rix()` function above, generates the `default.nix` file in the project directory. This file serves as the formal, machine-readable specification of the computational environment. Importantly, `rix()` automatically invokes `rix_init()`, which creates a project-specific `.Rprofile` file that prevents package library conflicts and disables `install.packages()` to maintain environment integrity.

Step III: Building and Using the Reproducible Environment

Once the `default.nix` file has been generated, the next step is to build the environment and use it to reproduce either the simulation analyses or the complete manuscript. This section demonstrates both workflows.

Building the Environment

From the terminal, navigate to the study directory containing the `default.nix` file and execute (Listing 13):

This command builds the environment according to the specification. The first execution will download and install all required packages, which may take a few minutes depending on network speed and system resources. Subsequent builds use cached packages and complete in seconds. Upon successful completion, a symbolic link named `result` appears in the project directory, pointing to the constructed environment in the Nix store.

To activate the environment, run (Listing 14):

This command drops the user into a shell where all specified packages and tools are available. The shell prompt typically changes to indicate that a Nix environment is active (e.g., `[nix-shell:~/project]$`). If RStudio was specified via `ide = "rstudio"`, it can be launched from within this shell by typing `rstudio`, ensuring it uses the project-specific R installation and package library. However, this will only work for R version 4.4.3 at least, or for a date on or after the 2025-02-28 (see <https://docs.ropensci.org/rix/articles/e-configuring-ide.html>).

Reproducing the Simulation

As described before, our example contains multiple scripts. For streamlined execution, we provide a master script (`06_run_all.R`) that runs the simulation, calculates the performance criteria, and creates the plots. This `.R` file has the following content (Listing 15):

Thus, to reproduce the simulation from within the Nix shell, meaning after running `nix-build` and `nix-shell` (Listing 16):

This executes the complete simulation sequentially: first running the Monte Carlo replications which save results to `sim_results.rds`, then computing performance metrics and saving the calculated values to `performance_summary.rds`, and finally generating all figures. Alternatively, individual scripts can be executed separately. The key advantage of executing within `nix-shell` is that all dependencies—R version, packages, and system tools—match exactly those specified in `default.nix`.

Reproducing the Complete Manuscript⁸

Beyond reproducing computational results, the Nix environment enables full manuscript reproducibility. The manuscript source file (`article.qmd`) combines narrative text, executable code chunks, and references to simulation outputs. In our specific case, we do not integrate the simulation run itself in the manuscript (but you can). We just load the obtained performance measures and integrate the code chunks that produce the plots (see Figure 1). To render the manuscript (Listing 17):

You can if we use rixpress

This command executes all code chunks in the manuscript, incorporates results and figures, and generates a formatted PDF following APA style guidelines via the `apaquarto` extension (Schneider, 2024). This extension is saved in the project repo already.

To download this extension for your own work you can install the extension by using the terminal (Listing 18):

⁸ See the `{rix}` documentation for more:

<https://docs.ropensci.org/rix/articles/z-advanced-topic-building-an-environment-for-literate-programming.html>

or in the console (Listing 19):

The final document (.pdf) is saved directly in the project folder. Because Quarto is installed as a system-level package in our Nix specification, the rendering occurs entirely within a fully reproducible environment, ensuring consistent output across machines regardless of local software configurations. If desired, the manuscript can also be reproduced interactively by opening the project folder in the user’s preferred IDE and running the code chunks directly.

Additional Considerations for Advanced Workflows

Workflow Orchestration: {targets} and {rixpress}

Complex simulation studies often benefit from workflow management systems that track dependencies between computational steps, cache intermediate results, and enable selective re-execution when inputs change. Two complementary approaches exist within the Nix ecosystem: using {targets} inside a Nix environment, or using {rixpress} to leverage Nix itself as the build automation tool.

Using {targets} within Nix. As mentioned, the {targets} package (Landau, 2021) provides workflow orchestration for R-based projects. This combination ensures both computational reproducibility (via Nix controlling the environment) and computational efficiency (via targets’ intelligent caching). To integrate {targets} with Nix, simply include “targets” in the r_pkgs parameter of `rix()`, and execute the pipeline within `nix-shell` using `Rscript -e 'targets::tar_make()'`. The {targets} metadata directory (`_targets/`) should be excluded from version control while the `_targets.R` configuration file should be committed alongside `default.nix` (Rodrigues & Baumann, 2025). This approach is ideal for projects that remain within the R ecosystem and do not require different computational environments for different pipeline steps (see {rix} documentation: <https://docs.ropensci.org/rix/articles/z-advanced-topic-reproducible-analytical-pipelines-with-nix.html>).

Using {rixpress} for polyglot pipelines. The {rixpress} package (Rodrigues, 2025), a sister package to {rix}, uses Nix itself as the build automation tool rather than operating within a Nix environment. Each pipeline step becomes a Nix derivation, providing hermetic builds with

sandboxed execution and content-addressable caching. The key advantage of {rixpress} emerges in multi-language workflows: different steps can execute in different Nix-defined environments (e.g., one step using R 4.2.0 with specific packages, another using Python 3.12 with machine learning libraries, another using Julia for numerical optimization). The package interface, inspired by {targets}, uses functions like `r xp_r()`, `r xp_py()`, and `r xp_jl()` to define pipeline steps, with automatic serialization handling data transfer between languages. Objects are stored in the Nix store and can be inspected interactively using helper functions like `r xp_read()` and `r xp_load()` (see {rixpress} documentation: <https://docs.ropensci.org/rixpress/articles/intro-concepts.html>).

Converting Existing {renv} Projects

Many researchers have existing projects using {renv} for package management. The `renv2nix()` function facilitates migration by reading an `renv.lock` file and generating an equivalent Nix specification. This conversion is particularly valuable for projects where {renv} encountered system dependency issues or where stricter reproducibility guarantees are desired. However, researchers should note that while {renv} snapshots R package versions, Nix additionally pins system libraries and compilers, potentially exposing previously hidden dependencies on system configuration (Rodrigues & Baumann, 2025) (see {rix} documentation: <https://docs.ropensci.org/rix/articles/f-renv2nix.html>).

Containerization with Docker

Institutions with existing Docker-based infrastructure may wish to combine Nix with containers. While this might seem redundant—both technologies provide isolation—the combination offers complementary benefits: Nix ensures bit-reproducible builds across systems, while Docker provides a familiar deployment mechanism for non-Nix-aware computing environments. The approach is to use Nix as the base layer within a Docker container (Rodrigues & Baumann, 2025). This strategy is particularly relevant, for example, for projects requiring deployment to cloud computing platforms or high-performance computing clusters where Docker is the standard containerization technology (see {rix} documentation: <https://docs.ropensci.org/rix/articles/z-advanced-topic-using-nix-inside-docker.html>]).

Discussion

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Listing 12 Environment specification for the simulation study using rix()

```
library(rix)

rix(
  date = "2025-08-25", # line 1
  r_pkgs = c( # line 2
    "rix", "quarto", "knitr", "marginaleffects", "simhelpers",
    "ggplot2", "doParallel", "doRNG", "cowplot", "dplyr", "svglite",
    "rvinecopulib"
  ),
  system_pkgs = c("quarto"), # line 3
  tex_pkgs = c( # line 4
    "amsmath", "ninecolors", "apa7", "scalerel", "threeparttable",
    "threeparttablex", "endfloat", "environ", "multirow", "tcolorbox",
    "pdfcol", "tikzfill", "fontawesome5", "framed", "newtx",
    "fontaxes", "xstring", "wrapfig", "tabulararray", "siunitx",
    "fvextra", "geometry", "setspace", "fancyvrb", "anyfontsize"
  ),
  ide = "rstudio", # line 5
  project_path = ".", # line 6
  overwrite = TRUE # line 7
)
```

Listing 13 Building the Nix environment

```
nix-build
```

Listing 14 Activating the Nix environment

```
nix-shell
```

Listing 15 Master script for running the complete simulation workflow

```
# required packages

library(marginaleffects); library(simhelpers); library(rvinecopulib)

library(doParallel); library(doRNG); library(ggplot2); library(cowplot);

library(dplyr)

# step 1: run simulation

# this will source the 01_data_generation.R function and parameters for the
# data generation. It also sources 02_models.R, which contains the model
# estimation function and another function for calculate the true ACE based
# on a large sample size

source("03_run_simulation.R")

# step 2: calculate performance metrics

# this file calculates the performance criteria based on the saved results
# from the 03_run_simulation.R

source("04_performance_metrics.R")

# step 3: generate plots

# this file retrieves the performance metrics and generates separate plots
# see Figure 1

source("05_plots.R")
```

Listing 16 Running the complete simulation workflow

```
Rscript 06_run_all.R
```

Listing 17 Rendering the manuscript with Quarto

```
quarto render article.qmd
```

Listing 18 Installing the apaquarto extension

```
quarto use template wjschne/apaquarto
```

Listing 19 Installing the apaquarto extension from R

```
quarto::quarto_use_template("wjschne/apaquarto")
```

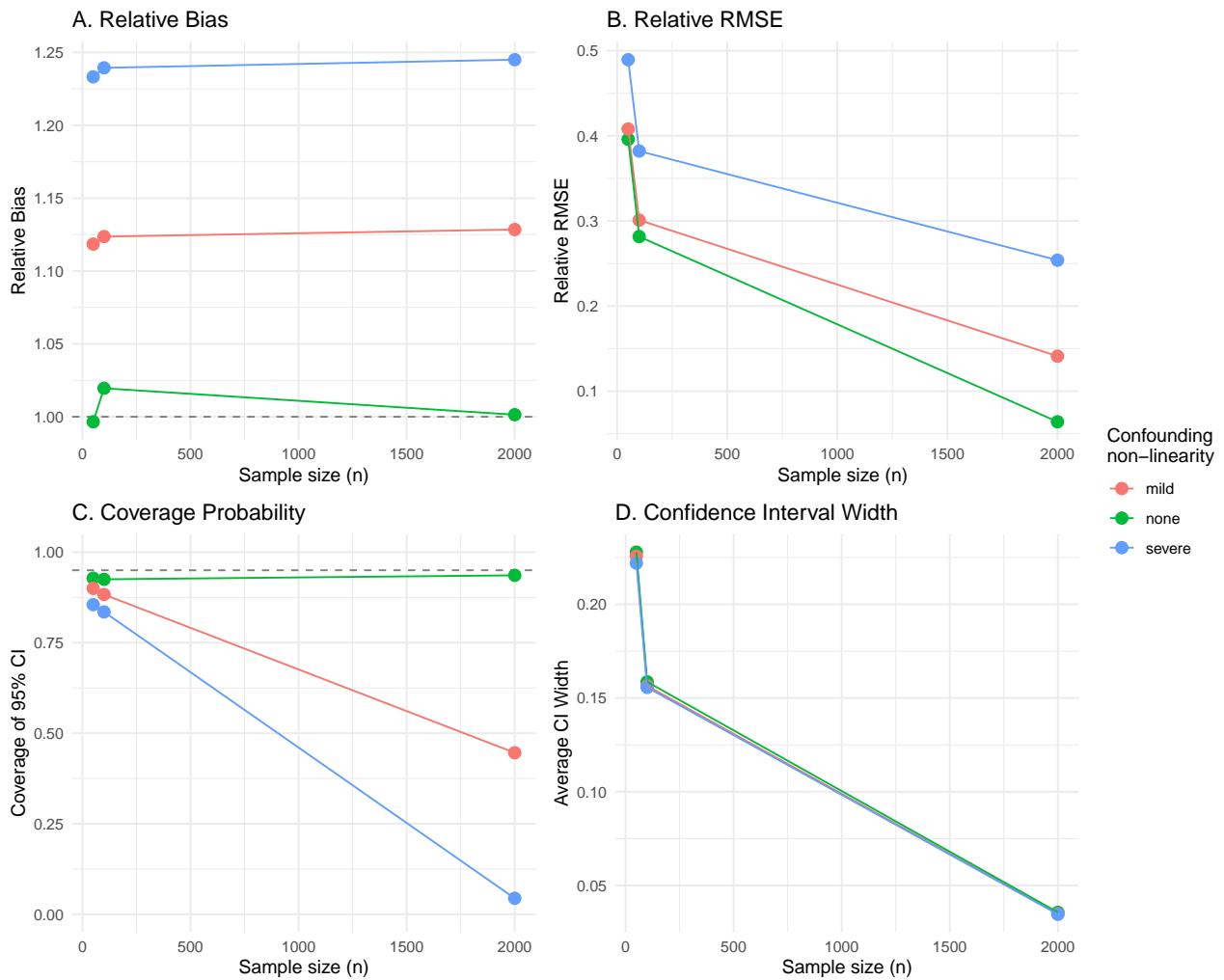
Table 1

Performance metrics for ACE estimator across simulation conditions

Sample Size	Confounding	Relative Bias	Relative RMSE	Coverage	CI Width
50	none	0.997	0.396	0.928	0.228
100	none	1.020	0.282	0.925	0.159
2000	none	1.001	0.064	0.936	0.036
50	mild	1.118	0.408	0.900	0.226
100	mild	1.124	0.301	0.883	0.157
2000	mild	1.128	0.141	0.446	0.035
50	severe	1.233	0.489	0.855	0.222
100	severe	1.239	0.382	0.835	0.156
2000	severe	1.245	0.254	0.044	0.035

Figure 1

Performance of ACE estimator across sample sizes and confounding severity. Panel A shows relative bias, Panel B shows relative RMSE, Panel C shows coverage probability of 95% confidence intervals (dashed line at nominal 0.95 level), and Panel D shows average confidence interval width. Results demonstrate that model misspecification induces systematic bias that persists across sample sizes, while increasing sample size improves precision but not accuracy under misspecification.



Appendix A

Simulation Study Design

Here we present a rather short description following recommendations from previous research, but ideally even more may be reported (Morris et al., 2019; Pawel et al., 2025; Siepe et al., 2024; White et al., 2024). This mimics a methods or similar section in articles.

Factorial Design. The simulation employs a full factorial design with two factors: sample size ($n \in \{50, 100, 2000\}$) and degree of confounding non-linearity ($\gamma_2 \in \{0, 0.3, 0.8\}$, labeled as none, mild, and severe). The parameter γ_2 controls the strength of the quadratic confounder effect on the outcome (see Data Generation). This yields nine conditions, each replicated $K = 1000$ times.

Data Generation. For each replication, data are generated following a causal structure where a confounder X_2 affects both treatment assignment and the outcome. The confounder and treatment error term are generated using the `{rvinecopulib}` package: pairs (U_1, U_2) are drawn from an independence copula via `rbi/cop()`, then transformed to standard normals via $X_2 = \Phi^{-1}(U_1)$ and $\epsilon = \Phi^{-1}(U_2)$. The independence copula is simply $C(u, v) = uv$, meaning the resulting uniforms are independent—mathematically equivalent to calling `rnorm()` directly. We use `{rvinecopulib}` intentionally because it depends on C++ libraries.

Treatment assignment follows $X_1 = \alpha_0 + \alpha_1 X_2 + \alpha_2 X_2^2 + \epsilon$ where $\alpha_0 = 0$, $\alpha_1 = 0.5$, and $\alpha_2 = 0.2$. This creates confounding because X_2 influences treatment assignment through both linear and quadratic terms. The binary outcome is generated from the true logistic regression model:

$$\text{logit}(P(Y = 1 | X_1, X_2)) = \beta_0 + \beta_1 X_1 + \gamma_1 X_2 + \gamma_2 X_2^2$$

with parameters $\beta_0 = -0.5$, $\beta_1 = 0.7$ (the causal effect of interest), $\gamma_1 = -0.4$, and γ_2 varying by condition. The analyst misspecifies the outcome model by omitting the quadratic confounder term, fitting instead:

$$\text{logit}(P(Y = 1 | X_1, X_2)) = \beta_0 + \beta_1 X_1 + \gamma_1 X_2$$

This misspecification creates residual confounding because the omitted term $\gamma_2 X_2^2$ is

correlated with X_1 (since X_1 depends on both X_2 and X_2^2), violating the conditional exchangeability assumption given linear adjustment alone.

Estimand. The target estimand is the average causal effect (ACE) of X_1 on Y , properly adjusted for confounding:

$$\text{ACE}(X_1) = \mathbb{E} \left[\frac{\partial P(Y = 1 | X_1, X_2)}{\partial X_1} \right] = \mathbb{E} \left[\beta_1 \cdot \frac{\exp(\eta)}{(1 + \exp(\eta))^2} \right]$$

where $\eta = \beta_0 + \beta_1 X_1 + \gamma_1 X_2 + \gamma_2 X_2^2$ is the correctly specified linear predictor, and the expectation is taken over the joint distribution of (X_1, X_2) . For each γ_2 condition, the “true” ACE (denoted θ) is approximated once using a very large sample ($N = 200,000$) with the correctly specified model including X_2^2 .

Estimator. The causal effect is estimated from the misspecified model (omitting X_2^2) as:

$$\widehat{\text{ACE}}(X_1) = \frac{1}{n} \sum_{i=1}^n \tilde{\beta}_1 \cdot \frac{\exp(\tilde{\eta}_i)}{(1 + \exp(\tilde{\eta}_i))^2}$$

where $\tilde{\eta}_i = \tilde{\beta}_0 + \tilde{\beta}_1 X_{i1} + \tilde{\gamma}_1 X_{i2}$ and $\tilde{\beta} = (\tilde{\beta}_0, \tilde{\beta}_1, \tilde{\gamma}_1)$ are maximum likelihood estimates from the misspecified logistic regression.

Performance Criteria. Table 1 presents the performance criteria used to evaluate the ACE estimator across simulation conditions.

Computational Details. The simulation was conducted on a MacBook Pro (...), running macOS Sequoia 15.6.1 All analyses were performed in R [@] (version X). Parallel processing was implemented through the {doParalell} package (version X) ([Corporation & Weston, 2022](#)), with {doRNG} (version X) ([Gaujoux, 2025](#)) to ensure independent and reproducible random number streams. For data generation we used the {rvinecopulib} package (version X) ([Nagler & Vatter, 2025](#)). The estimator was implemented using the {marginaleffects} package (version X) ([Arel-Bundock et al., 2024](#)). Data wrangling was performed with {dplyr} (version X) ([Wickham et al., 2023](#)). Method performance was assessed through multiple metrics following the formulas from the {simhelpers} package (version X) ([Joshi & Pustejovsky, 2025](#)). Figures were produced with {ggplot2} (version X) ([Wickham, 2016](#)) and {cowplot} (version X) ([Wilke, 2025](#)). Finally,

this paper was written with apaquarto [@] (see GitHub repository for more information on reproducing the manuscript and analyses).

Appendix B
Clarifying the packages used

Table B1

Performance criteria for evaluating the ACE estimator. $\hat{\theta}_k$ denotes the ACE estimate from replication k (for $k = 1, \dots, K$), where $K = 1000$ is the number of replications, and θ denotes the true ACE for a given condition. For coverage and width criteria, A_k and B_k denote the lower and upper endpoints of the 95% confidence interval from replication k , $W_k = B_k - A_k$ is the interval width, c_β is the estimated coverage probability, and $I(\cdot)$ is an indicator function equaling 1 if the condition is true and 0 otherwise. The Monte Carlo standard error (MCSE) quantifies the simulation uncertainty in each performance measure estimate

Criterion	Estimate	MCSE
Bias	$\frac{1}{K} \sum_{k=1}^K \hat{\theta}_k - \theta$	$\sqrt{\frac{1}{K(K-1)} \sum_{k=1}^K (\hat{\theta}_k - \bar{\hat{\theta}})^2}$
Variance	$\frac{1}{K-1} \sum_{k=1}^K (\hat{\theta}_k - \bar{\hat{\theta}})^2$	$\sqrt{\frac{K-1}{K} \cdot \frac{1}{K-1} \sum_{k=1}^K (\hat{\theta}_k - \bar{\hat{\theta}})^2}$
RMSE	$\sqrt{\frac{1}{K} \sum_{k=1}^K (\hat{\theta}_k - \theta)^2}$	$\sqrt{\frac{K-1}{K} \sum_{j=1}^K \left(\sqrt{(\hat{\theta}_j - \theta)^2} - \overline{RMSE} \right)^2}$
Relative Bias	$\frac{1}{\theta K} \sum_{k=1}^K \hat{\theta}_k$	$\frac{1}{\theta} \sqrt{\frac{1}{K(K-1)} \sum_{k=1}^K (\hat{\theta}_k - \bar{\hat{\theta}})^2}$
Relative RMSE	$\frac{1}{\theta} \sqrt{\frac{1}{K} \sum_{k=1}^K (\hat{\theta}_k - \theta)^2}$	$\frac{1}{\theta} \sqrt{\frac{K-1}{K} \sum_{j=1}^K \left(\sqrt{(\hat{\theta}_j - \theta)^2} - \overline{RMSE} \right)^2}$
Coverage	$\frac{1}{K} \sum_{k=1}^K I(A_k \leq \theta \leq B_k)$	$\sqrt{\frac{c_\beta(1-c_\beta)}{K}}$
Width	$\frac{1}{K} \sum_{k=1}^K (B_k - A_k)$	$\sqrt{\frac{1}{K(K-1)} \sum_{k=1}^K (W_k - \bar{W})^2}$